ON THE USE OF THE MOLLWO-IVEY RELATIONSHIP

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Departures from the Mollwo-Ivey relationship are expected to be pronounced in crystals containing large cations.

The F and M centre transition energies in alkali halides are given to a first approximation by

$$E = \alpha a^{-n} \tag{1}$$

where a is the lattice spacing and α and n are constants which depend on the type of colour centre. This (Mollwo-Ivey) relationship [1] is an empirical rule which is often useful for interpolation. It is not a general rule and does not describe, for example, F centre emission in alkali halides [2]. It is not a reliable substitute for experimental and theoretical investigation and recently it has been used in a way which is not valid [3]. We wish to stress the limits within which (1) may be used and to show that its misuse led to an incorrect assignment of the F band in BaF $\frac{3}{2}$.

The F band peak in BaF_2 has recently been experimentally located at 611 nm [4]. The sequence of investigations which led to this identification was as follows:

1) The 2 S ground state of the F centre in additively coloured CaF₂, SrF₂ and BaF₂ was thoroughly explored by e.p.r. and ENDOR methods [5].

2) The ENDOR parameters were calculated [5] using point ion wavefunctions [6] and compared with experiment [5].

3) The F band peaks were identified and the spin-orbit coupling constant in the ${}^{2}P$ state of the F centre was measured in additively coloured CaF₂, SrF₂ and BaF⁴₂ using the large temperature dependent magneto-optical effect characteristic of F centres. The crystals were first

checked for F centre content by e.p.r. methods.

4) The spin-orbit coupling constant in the excited ^{2}P state of the F centres was calculated [4] using point ion wave functions [6] and compared with experiment [4].

Using (1) and the F band peak positions in CaF2 and SrF2 it was estimated [4] that the F band peak would occur at 513 nm in BaF2; this value may be compared with the calculated point ion value of 475 nm [6]. However, careful investigation showed that no absorption band peak occurs in the region of 500 nm in additively coloured BaF2 crystals known from e.p.r. measurements to contain ~ 10^{18} F centres/cm³ and it was pointed out [4] that, on the basis of experiment, the Mollwo-Ivey relation does not apply to BaF2.

Theoretically, the transition energy will depend on the lattice parameter alone only if the potential in which the colour centre electrons move scales with the lattice parameter, i.e. V =V(r/a). The only simple potential of this sort is the point ion potential [7]. If, in addition, the electronic wave-function scales with the lattice parameter, $\psi = \psi (r/a)$, it may then be readily shown [8] that the coefficient in (1) lies in the range $1 \le n \le 2$. The applicability of (1) is in doubt when n is much greater than 2.

Detailed quantitative estimates of corrections to the point ion model have been made recently for F centres in alkali halides and alkaline earth fluorides [9]. This work showed that deviations from (1) occurred because the detailed electronic structure of the ions cannot be ignored. These "ion-size" effects are particularly striking when the nearest neighbour cations are large, as in

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CsF and BaF₂. In such cases the potential is not a function just of lattice parameter and the Mollwo-Ivey rule does not apply [9]. The importance of ion size effects should show up in deviations from predictions of the point ion model, increasing along the sequence CaF₂, SrF₂, BaF₂. Precisely this trend is shown by the transition energy [4], the h.f.s. constants in the ²S ground state [5] and the spin-orbit coupling constant in the ²P excited state of the F centre [4].

The F band peak in BaO has been found experimentally [10] to be at 620 nm. This assignment has also been questioned [3] on the basis of (1). However, the objections that apply to the use of (1) in BaF₂ are expected to apply also in BaO.

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DEUTERON SPIN-LATTICE RELAXATION AND PHASE TRANSITIONS IN GeD4

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Deuteron spin-lattice relaxation time (T_1) measurements in polycrystalline GeD4 show discontinuities at the first-order phase transition points at 75.5 and 77.8°K, and a change in the temperature dependence of T_1 at the λ -point at 67.7°K. A deuteron quadrupole coupling constant of 82 kHz was obtained.

The spin-lattice relaxation time T_1 of deuterons in solid GeD₄ was measured in the temperature range 40 to 110^oK at 6 MHz, using NMR pulse methods [1]. The results are shown in fig. 1. The sample was prepared by reduction of GeCl₄ by LiAlD₄ in ethereal solution [2], and it was purified of oxygen impurities by the mischmetal getter technique [3].

The principal relaxing mechanism for deuteron is the electric quadrupole interaction with the molecular field gradient. The temperature dependence of T_1 suggests that this relaxation takes place through the reorientational motion of the molecules. Thus the conventional formula [4]

$$\frac{1}{T_1} = C \left[\frac{\tau_c}{1 + (\omega_0 \tau_c)^2} + \frac{4\tau_c}{1 + (2\omega_0 \tau_c)^2} \right]$$

was used to interpret the results. Here $C = \frac{3}{10} \pi^2 (1 + \frac{1}{3} \eta^2) (e^2 q Q/h)^2$, and τ_c is the correlation time for the reorientation of the field gra-

dient. Assuming that C does not change appreciably in the temperature range of interest, and assuming a thermally activated Arrhenius process for the random molecular reorientations, $\tau_{\rm C} = \tau_0 \exp(E_{\rm a}/kT)$, where $E_{\rm a}$ is the apparent activation energy for the molecular motion, the temperature dependence of $\tau_{\rm C}$ was deduced from the experimental data, and is shown in fig. 1.

Calorimetric investigations indicate that GeH₄ has four solid state phases in the temperature range from about 12°K to the melting point [5]. The heat capacity curve is discontinuous at 73.2 and 76.6°K, indicating first-order phase transitions. The low temperature transition at 62.9°K occurs over a range of a few degrees and shows a λ -anomaly suggesting a higher-order transition. No structural investigation has been found for either GeH₄ or GeD₄ in the available literature.

In the present data, discontinuities in T_1 versus T occur at temperatures 77.8 and 75.5°K, and a pronounced change in the temperature de-