

35 **INTRODUCTION AND BACKGROUND**

36 Brittle fractures observed during the M6.7 1994 Northridge earthquake instigated extensive
37 examination (e.g., the SAC Joint Venture (1996, 1995)) of welded beam-column connections in
38 Steel Moment Resisting Frames (SMRFs). These studies determined that pre-existing flaws, in
39 conjunction with low toughness materials and poor connection design were responsible for these
40 fractures. Ultimately, these studies led to stringent material toughness and detailing requirements
41 as well as guidelines for upgrading vulnerable connections in SMRFs and other structural systems
42 (AISC, 2010). Although beam-column connections were the primary focus of post-Northridge
43 investigations and subsequent retrofit, other connections, such as welded column splices (WCSs)
44 with Partial Joint Penetration (PJP) welds were identified to be vulnerable as well (CUREe, 1995).
45 Figure 1 schematically illustrates a pre-Northridge welded column splice detail. Referring to the
46 Figure, these connections featured low flange weld penetrations, i.e., weld throat between 40%-
47 60% of the thinner flange thickness (Nudel et al., 2015). Moreover, the Charpy V Notch (CVN)
48 energy of weld filler materials in these connections was in the range of 5-10 ft-lbs (Chi et al.,
49 2000); this is significantly lower than the post-Northridge requirements (AISC, 2010) that mandate

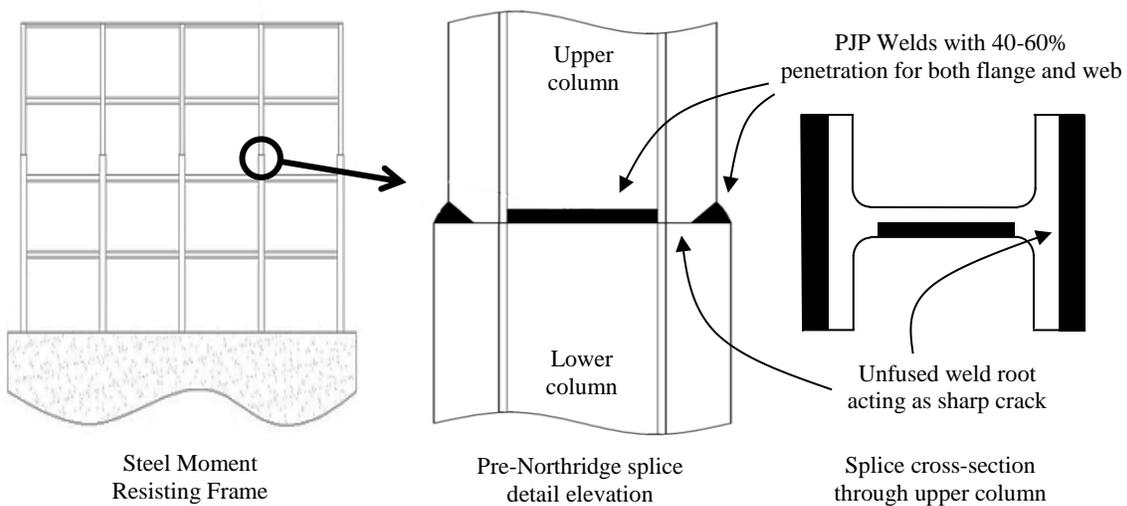


Figure 1: Partial Joint Penetration (PJP) welds in pre-Northridge Steel Moment Resisting Frame

50 weld filler metal CVN toughness greater than 20 ft-lb at 0⁰F. The lack of full penetration in these
51 splices produces a crack-like flaw (a stress raiser) that renders them susceptible to fracture, and
52 significantly lowers their strength. To address this, the post-Northridge design provisions (AISC,
53 2010) also mandate the use of Complete Joint Penetration (CJP) welds in welded column splice
54 connections, eliminating the crack-like flaw. The fracture vulnerability of pre-Northridge PJP
55 splices (implied by the new design provisions) is confirmed by experiments (Bruneau and Mahin,
56 1991), and finite element simulations by Nuttayasakul (2000), and more recently by Stillmaker et
57 al. (2016). These studies indicate that pre-Northridge splices have flange fracture strengths in the
58 range of 15-25ksi (in contrast to the expectation of flange yielding, i.e., ~55 ksi, as implied by the
59 current provisions – AISC, 2010).

60 The design provisions (both pre- and post-Northridge) require welded splice connections to be
61 located near mid story height, where moment demands are anticipated to be low under first-mode
62 building response. However, nonlinear time history simulations (Shaw et al., 2015; Shen et al.,
63 2010) indicate that moment and axial force demands at these locations (especially in high-rise
64 frames) are significant, such that the peak tensile stresses at the splices approach the yield strength
65 of the column flanges. This is due to higher mode response (which causes single curvature bending
66 of the columns) and column tension from overturning effects that are dominant in high-rise frames.
67 Galasso et al., (2015) conducted probabilistic risk analysis of splice fracture within a Performance
68 Based Earthquake Engineering (PBEE) based framework. This analysis indicates that high tensile
69 stress demands and low strengths of pre-Northridge WCSs result in a high risk of fracture. More
70 specifically, for the 20-story building considered by Galasso et al., (2015), the return period for
71 splice fracture was determined to be as low as 87 years. This may be considered unacceptably
72 high. These observations (and the observation that many existing buildings on the West Coast of

73 the United States still have unrepaired pre-Northridge details with PJP welds) have resulted in
74 increased initiative to retrofit these splices in existing buildings (Nudel et al., 2015) to achieve
75 conformance with current design and safety standards (AISC, 2010). Retrofit of these splices
76 (which typically involves replacing the PJP welds with CJP welds) is costly, since the columns are
77 in the gravity load path and often cannot be conveniently accessed in operational buildings. The
78 high likelihood of fracture (as suggested by these studies) implies that a large majority of splices
79 in mid- to high-rise pre-Northridge SMRFs may require retrofit for compliance with current
80 performance standards. Although such a retrofit strategy is well-intentioned, it assumes that
81 fracture in any splice is unacceptable and that splice fracture will inevitably lead to loss of safety
82 or collapse. While this may be the case for some configurations and ground motions, none of the
83 aforementioned studies have examined the effect of splice fracture on frame response; specifically,
84 whether the loss of one splice triggers a cascading effect leading to loss of strength capacity and
85 collapse, or alternatively, whether fracturing splices alter the dynamic response of the system (e.g.,
86 through period elongation or frame rocking) such that post-fracture response is less adverse.
87 Qualitative, physics-based arguments may be made in support of either response mode (or an
88 interaction of the two). However, a rigorous characterization of building response that quantifies
89 the risk of structural (rather than connection) limit states in a probabilistic manner is necessary to
90 fully elucidate the tradeoffs between the cost and benefits of retrofit.

91 It is interesting to note here that a key shortcoming of first-generation PBEE documents (Applied
92 Technology Council, 1997; ASCE, 2006) is cited as their reliance on component limit states as
93 indicators of system response (Applied Technology Council, 2006). The notion of assuming splice
94 failure as an indicator of structural failure and mitigation strategies that consider connection failure

95 in isolation may be criticized similarly. With this background, the specific objectives of this study
96 are:

- 97 1. To examine the effect of splice fractures on the seismic response (including story deformations
98 and collapse) of generic SMRF buildings representative of pre-Northridge construction, in a
99 probabilistic, performance-based engineering framework consistent with modern
100 interpretations of PBEE (Applied Technology Council, 2012; LATBC, 2014) that emphasize
101 global structural response, in addition to local failure modes.
- 102 2. To generate fundamental insights into physical modes of structural response that follow splice
103 fracture to inform engineering intuition and retrofit strategies.
- 104 3. Based on the above, to provide general commentary regarding the retrofit of pre-Northridge
105 SMRF buildings that are subject to welded column splice fracture.

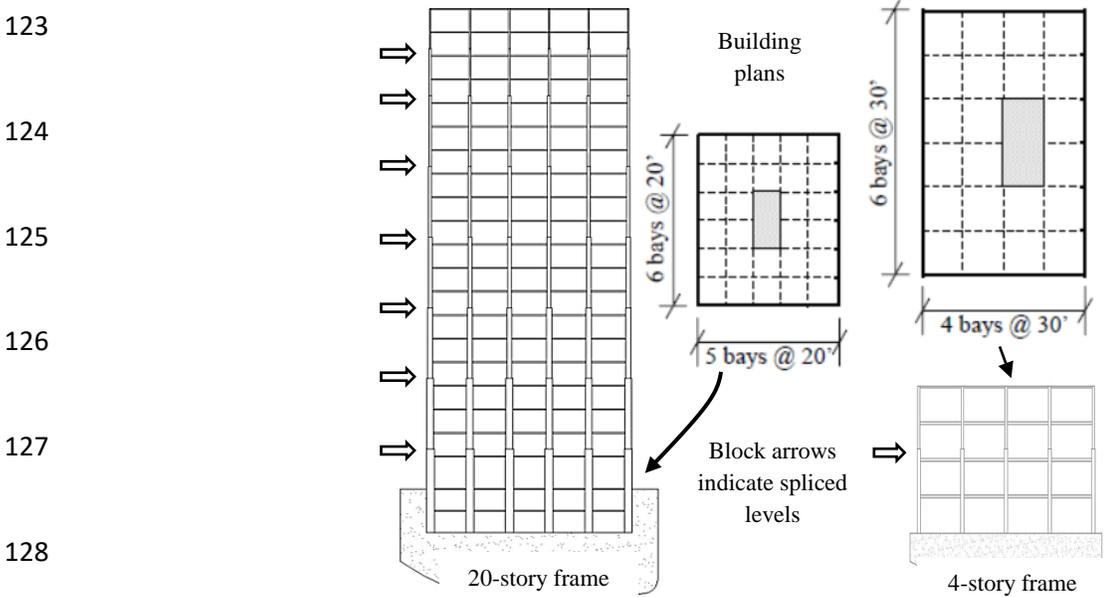
106 The primary scientific basis for the paper is a series of Non-Linear Response History Analyses
107 (NLRHA) of two generic (4- and 20- story) SMRFs subjected to a suite of ground motions. The
108 simulations include: (1) frames with non-fracturing splices (representative of a retrofitted frame)
109 and (2) frames with simulated splice fracture. A distinguishing feature of the NLRHA is the high-
110 fidelity simulation of splice fracture; this has two aspects: (1) it is based on previous experimental
111 and fracture mechanics studies by the authors (Shaw et al., 2015; Stillmaker et al., 2016), such that
112 the fracture stress is simulated with accuracy, and (2) post-fracture phenomena including loss of
113 tensile capacity and subsequent gapping and closure are simulated in a rigorous manner.

114 The next section summarizes pertinent aspects of the archetype frames and the NLRHA models,
115 including the methodology used to simulate fracture. This is followed by a discussion of the
116 probabilistic framework for performance assessment (within which the NLRHA models are used)

117 and the simulation strategy to interrogate various scenarios in support of the objectives above.
118 Results of the simulations are then discussed, along with implications for design and retrofit, and
119 limitations of the study.

120 **ARCHETYPE FRAMES AND SIMULATION MODEL**

121 As discussed in the introduction, two generic frames (4- and 20- story) were examined in this
122 study. These frames are schematically illustrated in Figure 2.



129 **Figure 2:** Moment frames considered in this study – overall geometry, elevation, and building plans

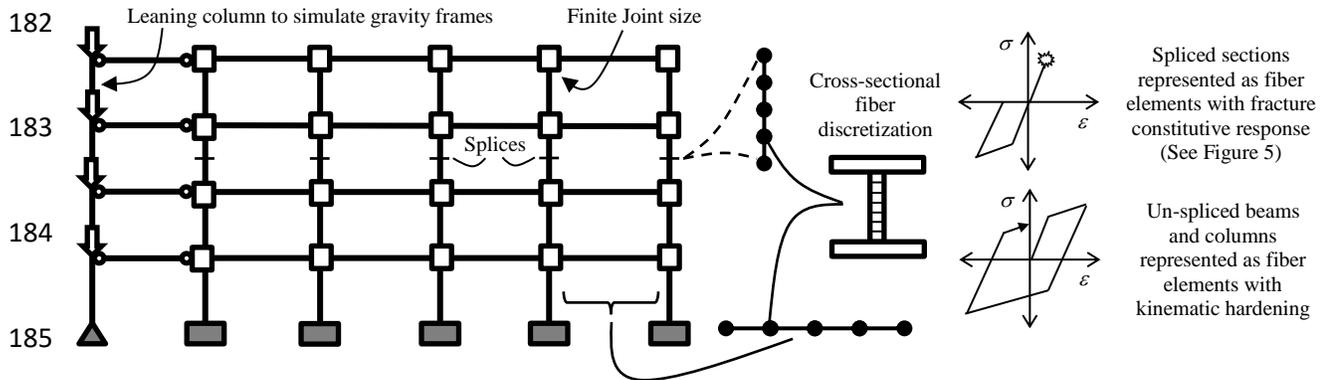
130 These structures are identical to those used by Shen et al. (2010), Shaw et al.(2015), and
131 subsequently Galasso et al. (2015) for demand assessment in WCSs. The frames are geometrically
132 similar to those in model buildings studied in the SAC Steel Project (Gupta and Krawinkler, 1999),
133 with some modifications. The extensive prior study on these buildings provides an opportunity to
134 evaluate the effects of splice fracture against benchmark response data that does not simulate splice
135 fracture. The frames conform to the loadings of ASCE 7-05 (ASCE, 2005) and the design
136 provisions of the AISC Seismic Provisions, i.e., AISC 341-10, implying that they may be

137 considered “post-Northridge” in terms of their structural design. However, as noted by Gupta and
138 Krawinkler (1999), pre- and post- Northridge frames are similar in terms of global response and
139 member force demands, assuming that: (1) these frames have been constructed in the 1973-1994
140 era, and benefit from Strong-Column-Weak-Beam (SCWB) considerations that were introduced
141 during the 1970s following soft-story collapses observed during the 1971 San Fernando
142 earthquake, and (2) beam-column connections do not fracture due to retrofit. While these
143 assumptions represent response of a large portion of the building stock, their limitations are
144 discussed during interpretation of the results. The frames were designed for seismicity consistent
145 with the Los Angeles, California region, and typical gravity loading of an office building. Firm
146 soil conditions (NEHRP – National Earthquake Hazards Reduction Program – Site Class D) were
147 assumed in design. Shaw (2013) outlines design assumptions, loadings, and other aspects of the
148 frames including specific member sizes in greater detail.

149 The splices were located 4 feet from the lower story beam in each spliced story. This is the
150 minimum distance required as per AISC 341-10 with the presumption that first mode response
151 results in maximum moments at the ends of the column (with a point of inflection at mid-story
152 height). Providing column splices at the minimum required distance represents the least
153 conservative scenario within current design standards. Elastic modal analysis indicated that the
154 fundamental periods for the 4- and 20- story frames were 0.94 and 2.37 seconds, respectively. For
155 both frames, simulation models were developed in OpenSEES (Mazzoni et al., 2009), which
156 allows for the simulation of highly nonlinear structural response. For illustration, Figure 3
157 schematically shows the OpenSEES model for the 4-story frame; the model for the 20-story frame
158 employs similar modeling assumptions. Referring to Figure 3, the main modeling assumptions and
159 features are now summarized:

- 160 1. All beams and columns were simulated as force-based fiber elements (Spacone et al., 1996),
161 with the objective of simulating axial force and moment interaction as well as spread of
162 plasticity through the member length. To appropriately represent curvature gradients,
163 approximately 5 elements were used per column, and approximately 1 element were used per
164 beam. Additional elements were inserted to represent the RBS details in the beams. Each
165 element had 5 Gauss integration points along its length. Figure 3 also shows typical
166 discretization of a cross-section with fibers; between 64 and 192 fibers were used for various
167 cross sections to capture gradients across the cross-section.
- 168 2. Figure 3 also schematically illustrates the uniaxial material properties used to represent beam
169 and column sections. Referring to the figure, a kinematic hardening model was used to
170 represent cyclic response of the steel material, with elastic modulus $E = 29,000 \text{ ksi}$, a hardening
171 slope 5% of the elastic modulus, and yield stress $\sigma_y = 55 \text{ ksi}$. These values are consistent with
172 previous simulations by the authors (Galasso et al., 2015), as well as experimental data
173 (Kanvinde and Deierlein, 2004; Ricles et al., 2004).
- 174 3. Finite joint size was simulated using rigid offsets, although panel zone flexibility (or yielding)
175 was not explicitly simulated.
- 176 4. Both member ($P - \delta$) and story ($P - \Delta$) effects were explicitly simulated through the use of
177 geometric transformations. A leaning column (also shown in Figure 3) was used to simulate
178 the destabilizing effect of the vertical loads on the gravity frames. The lateral resistance of the
179 gravity frames themselves was discounted – a conservative assumption from the standpoint of
180 structural performance.

181



186 **Figure 3:** Schematic illustration frame simulation model used in NLRHA, shown for the 4-story frame

187 In view of the major objectives of this study, splice fracture was simulated rigorously within the

188 constraints of frame-based analysis. A review of prior experimental (Bruneau and Mahin, 1991;

189 Shaw et al., 2015) and computational fracture mechanics (Stillmaker et al., 2016) studies on PJP

190 WCSs informs this approach. Specifically, the following observations from these prior studies are

191 relevant:

- 192 1. Fracture originates at the root of the weld, i.e., at the tip of the crack like flaw created by the
- 193 unfused region within the flange and instantaneously severs the flange (see Figure 4 below –

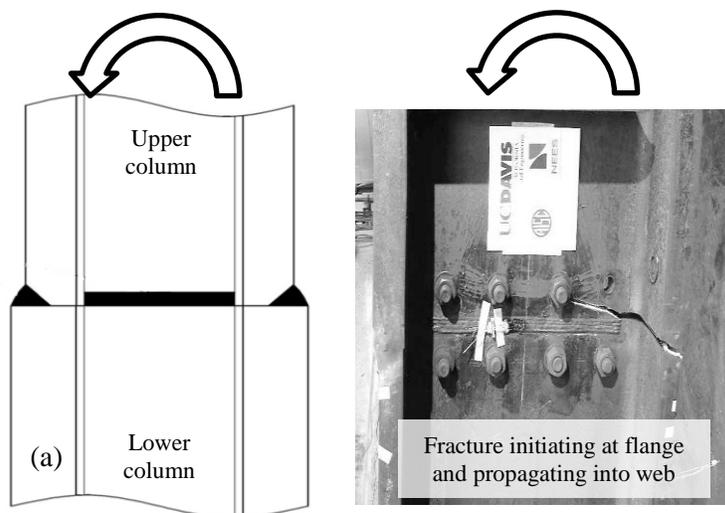


Figure 4: Fracture propagation in welded column splice (from Shaw et al., 2015)

194 from the tests of Shaw et al., 2015). The fracture usually propagates through a significant
195 portion of the web before being arrested. Although varying degrees of localized yielding are
196 observed in the splice details (depending on the degree of weld penetration and flange sizes),
197 fracture may be considered stress controlled, such that a flange stress may be uniquely assigned
198 to the occurrence of fracture. Moreover, the fracture may also be considered independent of
199 stress history, occurring when the stress exceeds a predetermined critical value for the first
200 time.

201 2. Further to the point above, this critical stress may be determined through classical fracture
202 mechanics theory (Anderson, 1995), applied through finite element simulations to the splice
203 connection of interest and the attendant configurational parameters such as weld penetration,
204 flange thickness, and material toughness. A comprehensive overview of such simulations, as
205 well as simplified analytical equations to predict initiation of fracture based on splice
206 configuration, may be found in Stillmaker et al., (2016).

207 3. All the experiments in the studies cited were terminated upon splice fracture, and further
208 reversed cycles were not applied. Consequently, the effects of column re-seating (and closure
209 of fractured crack faces) on a subsequent load reversal during seismic loading have not been
210 observed experimentally. In this study, it is assumed that the column re-seats in compression;
211 implications of this assumptions are discussed during the interpretation of results.

212 Based on the above observations, each spliced section is simulated as a beam-column element of
213 a small length, i.e., 2 inches. The length of this element is not germane to the simulation, except
214 for representing a segment of the member over which moment gradient is low, such that a stress-
215 based fracture criterion may be applied to this element. Within this cross-section, all fibers are

216 assigned a constitutive model that is able to replicate the response associated with fracture. The
217 primary characteristics of this model are as follows:

218 1. Elastic response in tension until a fracture stress, $\sigma_{fracture}$, is reached. The fracture stress is
219 determined for each fiber within the spliced cross-section depending on the degree of weld
220 penetration and the thicknesses of the flanges or webs being connected. Specifically, $\sigma_{fracture}$
221 was determined following the work of Stillmaker et al., (2016), either from results of finite
222 element based fracture simulations (as in the case of the 4-story frame) or per Equation 1
223 below:

$$224 \quad \sigma_{fracture} = \frac{K_{IC}}{\sqrt{\pi \times (\eta / 2\xi) \times t_u}} \times \frac{1}{f(\eta, \xi)} \quad (1)$$

225 In the above equation, K_{IC} is the critical stress intensity factor of the weld material at the root
226 of the flaw, taken as 38.1 ksi \sqrt{in} to reflect in-situ material toughness of pre-Northridge
227 connections (Chi et al., 2000) converted to a stress intensity factor conservatively using the
228 relation proposed by Barsom (1975). The variable $\eta = a / t_l$ represents the percentage of crack
229 penetration, while $\xi = t_u / t_l$ indicates the ratio of the flange (or web) thicknesses. The term
230 $f(\eta, \xi)$ represents a polynomial function with coefficients regressed to optimize agreement
231 with experimental results (Shaw et al., 2015) and finite element based fracture mechanics
232 simulations (Stillmaker et al., 2016). Equation (1) is specifically customized to the geometry
233 of the PJP splice details, and is able to characterize the effect of crack tip yielding. For the
234 various splices in the frames considered in this study, $\sigma_{fracture}$ is in the range of 8.6 -25.7 ksi.

235 2. After $\sigma_{fracture}$ is reached, the material loses all stress capacity in tension. Note that this is
236 different from simulating fracture through a negative slope in the constitutive response of the
237 fiber construct, which would produce mesh dependency of the solution (e.g., see Wu and
238 Wang(2010)), and also result in energy dissipation, which is spurious and physically
239 inconsistent with brittle fracture.

240 3. In compression, the model is elastic up to the expected yield strength, and then hardens
241 indefinitely with a slope 5% of the elastic modulus, assuming that the column effectively re-
242 seats, and compressive behavior is unaffected by tension fracture.

243 A constitutive model to reflect the above response is not available in OpenSEES. Consequently,
244 the response was constructed by arranging pre-implemented material models in “series” or
245 “parallel” fashion, as indicated schematically in Figure 5a. The resulting cyclic response is
246 illustrated in Figure 5b. The points marked numerically (i.e., 1,2,3,...) in Figure 5b show the
247 sequential evolution of the stress-strain history, showing initial elastic loading 0-1, unloading and
248 compressive loading and yielding 2-3-4, and fracture upon reloading in the tensile direction at 5.
249 Referring to the figure, this manner of simulating fracture is able to (1) simulate “snap-back,”
250 wherein the strain returns elastically to zero after fracture, and then increases back up to the applied
251 strain 5-6-7, eliminating spurious dissipation, and (2) eliminate mesh sensitivity, both of which are
252 problematic if fracture is simulated through a steep negative slope, i.e. following the path indicated
253 by 5-6'-7, as is often done. Subsequent to fracture, the material has no strength in tension, although
254 it maintains strength in compression, see points 7-8-9-10.

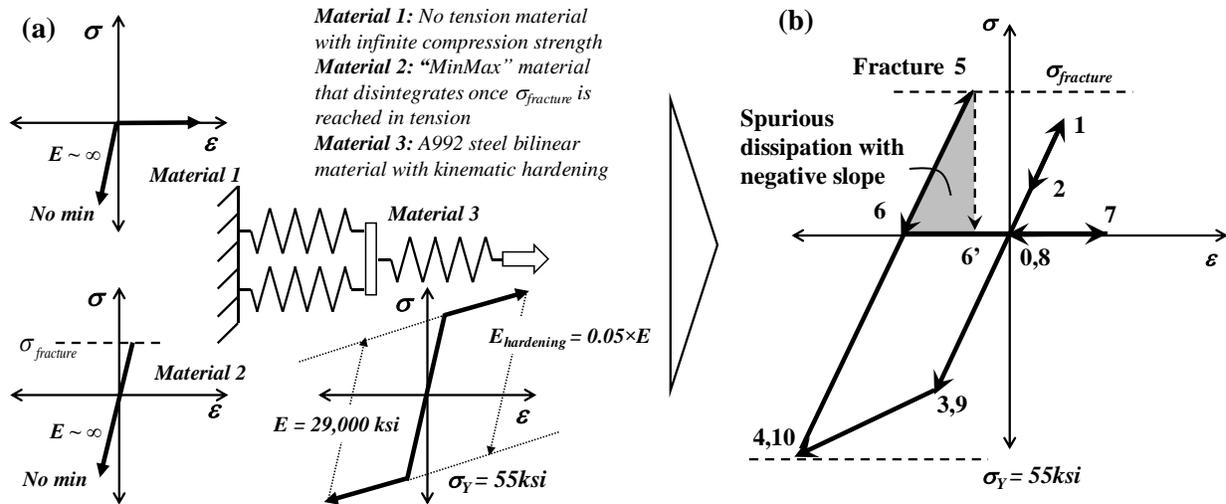


Figure 5: Constitutive material model for simulating fracture and post-fracture response: (a) Construction of model using series and parallel springs in OpenSEES, (b) Resultant response

255 Referring to Figure 3, each flange was represented as one fiber to reflect its instantaneous fracture
 256 consistent with experimental observations. The web was discretized into approximately 64 fibers,
 257 such that the model could simulate partial fracture of the splice (such as shown in Figure 4
 258 previously). Several Engineering Demand Parameters (EDPs), and other phenomena were
 259 monitored during the simulations. Of these, three are most relevant to the objectives of this paper:
 260 (1) the interstory drift, as well as lateral displacement histories at every level, which are used as a
 261 general indicator of system response, as well as to infer collapse, (2) the vertical displacement
 262 history at the top of the frame, to record rocking after splice fracture, and (3) the stress and strain
 263 histories in all fibers at the splice locations, which are used to track the precise instant of fracture.
 264 The next section discusses the framework within which the frame models were applied.

265 **FRAMEWORK FOR PERFORMANCE ASSESSMENT AND SIMULATION STRATEGY**

266 Following the methodology discussed in the previous section, frame models were constructed in
 267 OpenSEES for both the 4- and the 20- story archetype frames. Two sets of analyses were
 268 conducted for each of the frames: (1) Analyses that do not simulate fracture of the splices – in

269 effect setting the quantity $\sigma_{fracture} = \infty$ for all splices; these are denoted N and (2) Analyses that
270 reflect splice fracture as per the constitutive model discussed in the previous section, which are
271 denoted F.

272 Each of these analysis sets includes a suite of NLTHA simulations conducted using “Cloud
273 Analysis” (Jalayer, 2003), which is based on simple regression in the logarithmic space of
274 structural response (from NLTHA) versus seismic intensity for a set of recorded ground motions.
275 Hence, to determine the statistical properties of the *cloud* response (Jalayer and Cornell, 2009), the
276 linear least squares is applied on EDPs versus Intensity Measures (IMs) for a suite of ground
277 motion (unscaled) in order to estimate the conditional mean and standard deviation of EDP
278 given IM. The simple power-law model is used here:

$$279 \quad \quad \quad EDP = aIM^b \quad \quad \quad (2)$$

280 where a and b are the parameters of the regression. The standard deviation (s) of the regression is
281 assumed to be constant with respect to IM over the range of IMs in the cloud. The power-law
282 model illustrated in Equation (2) can be simply re-written as shown below in Equation (3) as a
283 linear expression of the natural logarithm of the EDP and the natural logarithm of the IM:

$$284 \quad \quad \quad \ln(EDP) = \ln(a) + b \ln(IM) \quad \quad \quad (3)$$

285 The use of logarithmic transformation indicates that the EDPs are assumed to be conditionally
286 lognormally distributed (conditional upon the values of the IMs); this is a common assumption
287 that has been confirmed as reasonable in many past studies.

288 Unscaled ground motion records from the SIMBAD (Selected Input Motions for displacement-
289 Based Assessment and Design) database (Smerzini et al., 2014), were used as input for the cloud

290 analysis. SIMBAD includes 467 tri-axial accelerograms, consisting of two horizontal (X-Y) and
291 one vertical (Z) components, generated by 130 worldwide seismic events (including main shocks
292 and aftershocks). These accelerograms were assembled from various ground motion databases
293 derived for different regions of the world. In particular, the database includes shallow crustal
294 earthquakes with moment magnitudes (M) ranging from 5 to 7.3 and epicentral distances $R \leq$
295 35 km. This provides strong ground motion records of engineering relevance for most of the design
296 conditions of interest without introducing large scaling factors. From this suite, a subset of 100
297 ground motion records was considered to provide a statistically significant number of strong-
298 motion records of engineering relevance for the applications of this study. These records were
299 selected for each building characterized by its T_1 , by first ranking the 467 records in terms of their
300 $S_a(T_1)$ values (by using the geometric mean of the two horizontal components) and then keeping
301 the component with the largest $S_a(T_1)$ value (for the 100 stations with highest mean $S_a(T_1)$).
302 Spectral acceleration at the structure's fundamental period, $S_a(T_1)$, was selected as the IM for this
303 study. Results of the cloud analysis for the N and F analysis sets are now discussed.

304 **Results of cloud simulations for Non-Fracture (N) runs**

305 Referring to prior discussion, one set of cloud simulations was conducted for both the 4- and 20-
306 story frames, albeit without simulation of splice fracture. These provide an assessment of the
307 "ideal" response, assuming all splices are strong enough to resist fracture. This may be considered
308 indicative of a building that has been fully retrofitted (e.g., with CJP welds) to mitigate splice
309 fracture. These simulations represent building performance perfectly prior to fracture of the first
310 splice. As a result, they may be conservatively interpreted for assessing loss of building
311 performance, assuming that fracture of the first splice will trigger system instability; the
312 conservatism inherent in this type of assessment is a major motivator for this study. Figures 6a and

313 b below show scatter plots (triangular markers) of maximum interstory drift ratio (MIDR) versus
 314 the selected IM, i.e., $S_a(T_1)$ for the 4- and 20- story frames respectively, as generated from the
 315 cloud simulations (conducted as per the methodology discussed previously). Also indicated on the
 316 plot are corresponding scatter points from the cloud analyses (F) that simulate splice fracture; these
 317 are discussed later. Each of the scatter plots identifies important levels of IM; these are: (1) The
 318 design level (10% probability of exceedance in 50 years) $S_a(T_1)^{10/50}$ corresponding to the building
 319 design parameters discussed earlier (Los Angeles, on stiff soil), (2) $S_a(T_1)^{2/50}$ corresponding to the
 320 Maximum Considered Event (2% probability of exceedance in 50 years), and (2) the lowest
 321 $S_a(T_1)^{\text{First-fracture}}$ at which the stress demand in any splice flange exceeds its capacity, as determined
 322 by Equation (1). This $S_a(T_1)$ corresponds to the lowest intensity at which fracture was observed
 323 during the (F) simulations. The hollow triangles represent runs during which the capacity of at
 324 least one splice was exceeded, implying that the (N) simulations are unsatisfactory for these runs,
 325 since they cannot simulate post-fracture response of the frames. Referring to Figures 6a and b, the
 326 following observations may be made:

- 327 1. As expected, for both buildings, response is identical from the N and F runs when no fracture
 328 is observed (i.e., below $S_a(T_1)^{\text{First-fracture}}$).

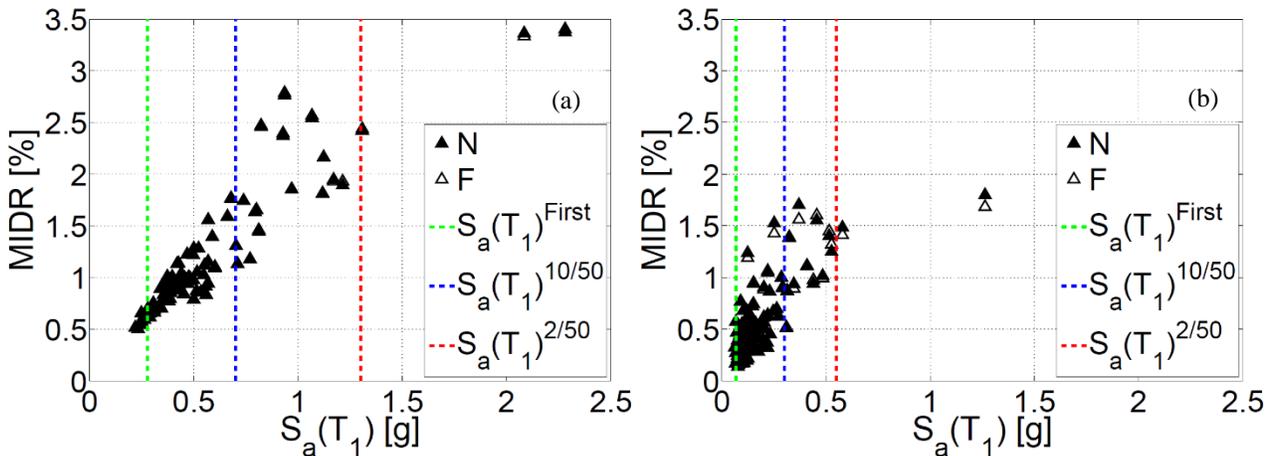


Figure 6: Maximum interstory drift ratio versus ground motion intensity (spectral acceleration) for (a) 4-story frame, and (b) 20-story frame

- 329 2. Collapse is not observed in any of the cases (for either of the buildings). Referring to the figure,
330 it is noted that most of the ground motions used have $S_a(T_1)$ values less than the 2/50 IM level.
331 For a well-designed building, absence of collapse at this level is not surprising. In fact, this is
332 in agreement with Incremental Dynamic Analysis (IDA; –Vamvatsikos and Cornell, 2002))
333 previously conducted for the same buildings by the authors (Galasso et al., 2015), as well with
334 results of NLRHA simulations on the same buildings by others (Shen et al., 2010).
- 335 3. The IM level $S_a(T_1)^{\text{First-fracture}}$ corresponds to about a 45/50 probability of exceedance for the
336 20-story building (i.e., about 87 year return period). For the 4-story building, $S_a(T_1)^{\text{First-fracture}}$
337 corresponds to about a 75/50 probability of exceedance for the 20-story building (i.e., about
338 35 year return period). These values are relatively similar to those determined previously by
339 Galasso et al., (2015) through IDA and suggest that the first splice fracture occurs with an
340 unacceptably high likelihood.

341 Point 3 above, when considered together with Figure 6a and b indicates that: (1) for a large range
342 of IM (hazard) levels, analysis that do not simulate splice fracture are invalid, unless it is assumed
343 that splice fracture in itself is an indicator of loss of building performance/collapse, and (2) if this
344 assumption is made, then the resultant probabilities (or return periods) are unacceptably high,
345 essentially requiring complete retrofit of all splices. This motivates the next set of cloud analyses.

346 **Results of cloud simulations for runs simulating splice fracture (F)**

347 Referring to the discussion above, if loss of building safety is assessed solely based on the first
348 splice fracture, the implications are unacceptable. Consequently, the Cloud Analysis was repeated
349 for both frames, including the simulation of splice fracture as per the process summarized earlier,
350 to examine building response after splices begin to fracture. For this set of simulations, each fiber
351 within the spliced section was assigned the constitutive model schematically illustrated in Figure

352 5. Figure 6a and b (which plot the $S_a(T_1)$ against peak interstory drift) also show scatter points
353 from the (F) simulations – these are the hollow triangles. Comparing the point clouds from the (N)
354 and the (F) simulations, the following points may be made:

355 1. As previously observed, until the first splice fractures (indicated by the vertical line
356 corresponding to $S_a(T_1)^{\text{First-fracture}}$), the response from both simulations are coincident as
357 expected.

358 2. For stronger motions (i.e., those with a higher $S_a(T_1)$), the response of the (F) simulations
359 deviates from the (N) simulations, such that on average, the interstory drift is less than 1% for
360 the 4-story and about 2% for the 20-story lower as compared to the interstory drift for the same
361 $S_a(T_1)$ as obtained from the (N) simulations. Similar percentages are observed at design level
362 and MCE $S_a(T_1)$ values. Given this, collapse is not observed for any of the ground motions.

363 3. The above observation is counterintuitive, suggesting that in terms of interstory drift, the splice
364 fractures improve structural performance, rather than exacerbate it. To explain this response, a
365 closer investigation of the underlying physics is warranted. Figures 7a-b, and Figures 8a-b
366 provide such an examination. For illustrative purposes, Figures 7a and b illustrate the time
367 history of the vertical displacement of a roof node at an exterior column for the 4- and 20- story
368 frames respectively, for both the (N) and (F) analyses. The time history corresponds to one
369 representative ground motion for each of the frames (i.e., corresponding to an IM level
370 consistent with MCE for the 4-story frame and to the maximum IM level in the database for
371 the 20-story frame); responses for all other ground motions in which splices fracture are
372 qualitatively similar. Figures 7a and b indicate response for both the (F) and (N) analyses
373 corresponding to this ground motion. Referring to the figure, it is observed that immediately
374 after the first splice fractures (which is also indicated in the time histories), the vertical

375 displacements of the (F) simulations immediately deviate from the (N) simulations, indicating
376 the onset of rocking deformations in the portion of the frame above the splice fracture. As more
377 splices fracture, the rocking deformations increase. It is well known (Housner, 1963; Makris,
378 2014) that building rocking may be extremely beneficial to structural response, by mobilizing
379 the rotational inertia of the rocking body. In fact, various researchers have recommended
380 allowing such rocking to enhance structural performance – these solutions include systems
381 with uplifting bases (Eatherton et al., 2014; Huckelbridge and Clough, 1978), as well as those
382 that feature columns with no tension capacity (Wada et al., 2001), resulting in behaviour very
383 similar to that observed after splice fracture in this study. In each case, experiments as well as
384 simulations have indicated an improvement in response. When considered cumulatively, this
385 research suggests that the observed reduction in frame drifts due to splice fracture is less
386 surprising.

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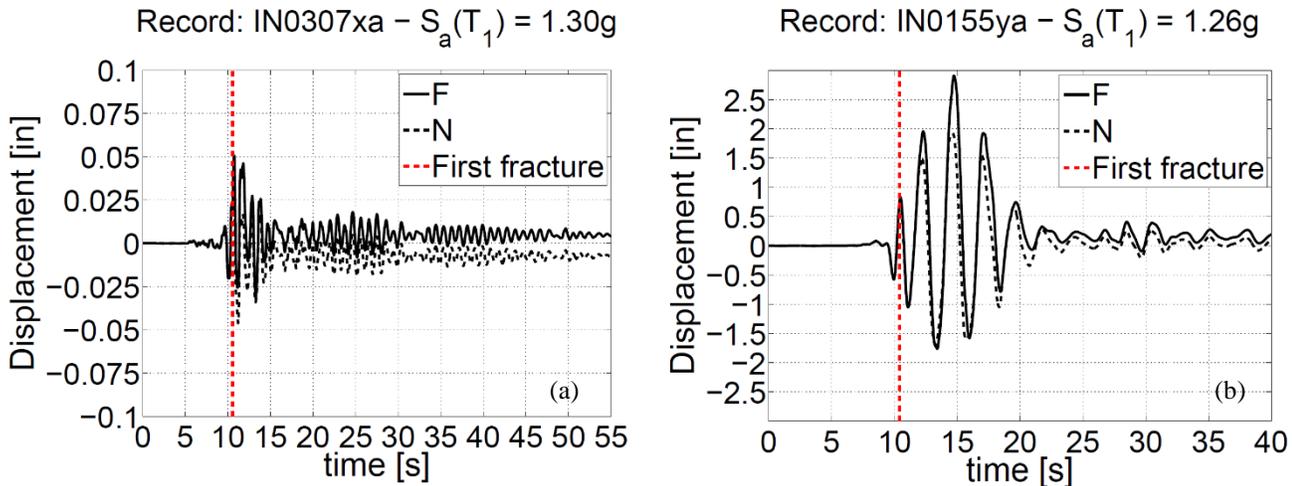


Figure 7: Representative time histories of vertical displacement at top story of exterior column for (a) 4-story frame, and (b) 20-story frame

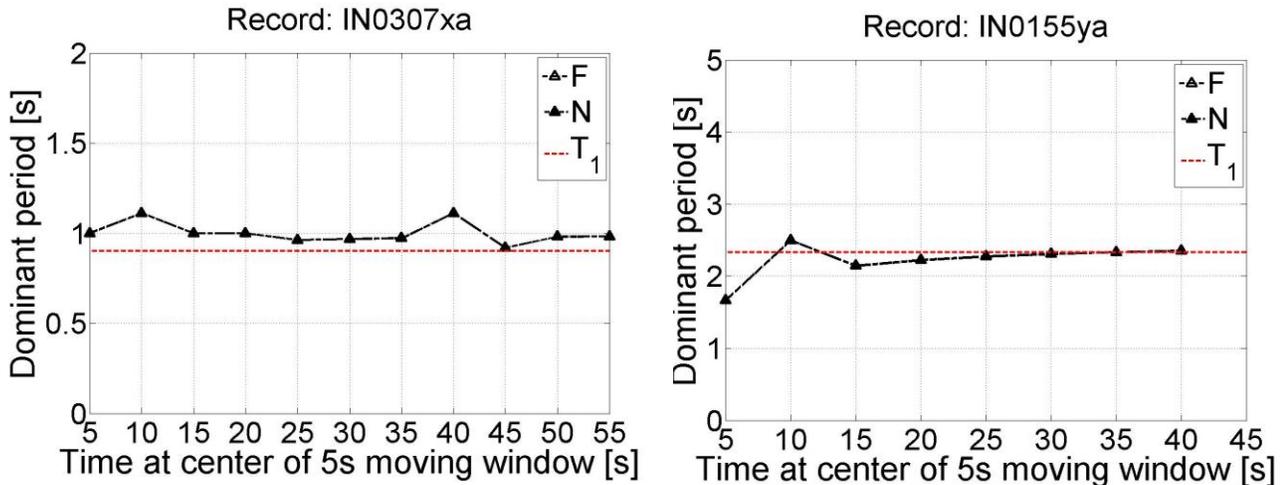


Figure 8: Representative evolution of dominant structural period for (a) 4-story frame, and (b) 20-story frame

391 Using the ground motions selected for Figures 7a and b, above, Figures 8a and b plot the evolution
 392 in frame dynamic characteristics (specifically, the dominant period) over the duration of the
 393 ground motion. This is accomplished by generating a moving window Fourier transform of the
 394 lateral roof displacement history for each of the ground motions, and recovering the peak or
 395 dominant period. Figures 8a and b show this evolution for both the (N) and (F) simulations, for
 396 both the 4- and 20 story buildings. Referring to the figure, the dominant dynamic frequency of
 397 either frame does not change appreciably (less than 10%) over the duration of the motion. It is

398 worth noting that over this duration, 2 splices fractured for the ground motion shown for the 4-
399 story building, whereas 13 splices fractured for the 20-story building. The relatively modest
400 increase in building period after splice fracture may be attributed to the following factors: (1) the
401 building resists force primarily through a shear mode, such that the loss of splices and associated
402 overturning response does not affect dynamic characteristics, and (2) the splices are dominated
403 (for most of the time history) by compressive forces, due to the presence of gravity loads. Under
404 these conditions, the splices are fully functional and able to carry load. When considered along
405 with Figures 7a and b, this suggests that the improved performance may be attributed to rocking
406 (and associated mobilization of rotational inertia), rather than any isolation effect due to period
407 elongation.

408 In summary, the (F) simulations suggest that due to the transition of structural response to a rocking
409 dominated mode, the fracture of splices has a positive effect on structural performance, if interstory
410 drift is considered as its primary indicator. While the above discussion summarizes the net effect
411 of splice fracture on key aspects of structural response, the phenomenology of splice fracture is
412 interesting in itself, and may be used for more refined insights into post-fracture response, with
413 possible implications for generalization of findings. To develop this understanding, the instants of
414 individual splice flange fractures were monitored during each of the time histories in the (F) cloud
415 analyses. More specifically, the initiation of fracture (i.e., triggering the critical stress as shown in
416 Figure 5b earlier) was monitored at each flange within each splice, during all ground motions in
417 the cloud analysis. In some splices, both flanges fractured instantaneously, whereas in others one
418 flange and part of the web (i.e., fibers corresponding to this portion of the cross-section) fractured.
419 Both cases are considered in the fracture pattern analysis presented in Figure 9a-e. Once

420 aggregated, information regarding the instants of splice fracture may be synthesized to develop
421 several observations regarding the phenomenology of splice fracture:

- 422 1. In the 4-story frame, there is only one spliced level (see Figure 2). During all ground motions
423 in which fracture was observed, only the splices in the exterior columns fractured, with the
424 interior columns splices remaining intact. Thus, no more than two splices fractured in any
425 ground motion.
- 426 2. Figures 9a-e depict the phenomenology of splice fracture in the 20-story building, which is not
427 quite as straightforward. In Figure 9a, the number indicated adjacent to each splice location
428 indicates the fraction of ground motions (out of all ground motions that caused any splice
429 fracture) during which that particular splice fractured. This indicates the vulnerability of
430 fracture for any given splice, in a general manner. The fracture percentages shown on Figure9a
431 are mirrored to reflect building symmetry, and the notion that ground motion polarity in the
432 horizontal direction is arbitrary.
- 433 3. Referring to Figure 9a, it is immediately apparent that splices 7 and 12 (exterior columns on
434 the 5th story are most likely to fracture), such that they fracture in ~84% of ground motions that
435 cause fracture. This is closely followed by splices 13 and 18 (also in the exterior columns) in
436 the 8th story. Fracture at these locations is evidently controlled by overturning actions, which
437 are most pronounced (due to higher mode effects) in the lower third of the building. The second
438 story splices (1 and 6) have a somewhat lower incidence of fracture, presumably due to a
439 combination of lower overturning moments (due to mode shape effects), higher compressive
440 gravity loads, and larger column sections.
- 441 4. In terms of fracture probability, the next group of splices is in the higher stories of the frame
442 (i.e., splices 25-30 in the 14th story). Interestingly, for the higher stories, the interior columns

443 are about as likely to fracture as the exterior ones, indicating the fracture is controlled by axial
 444 tension in the columns due to overturning, as well as flexure.

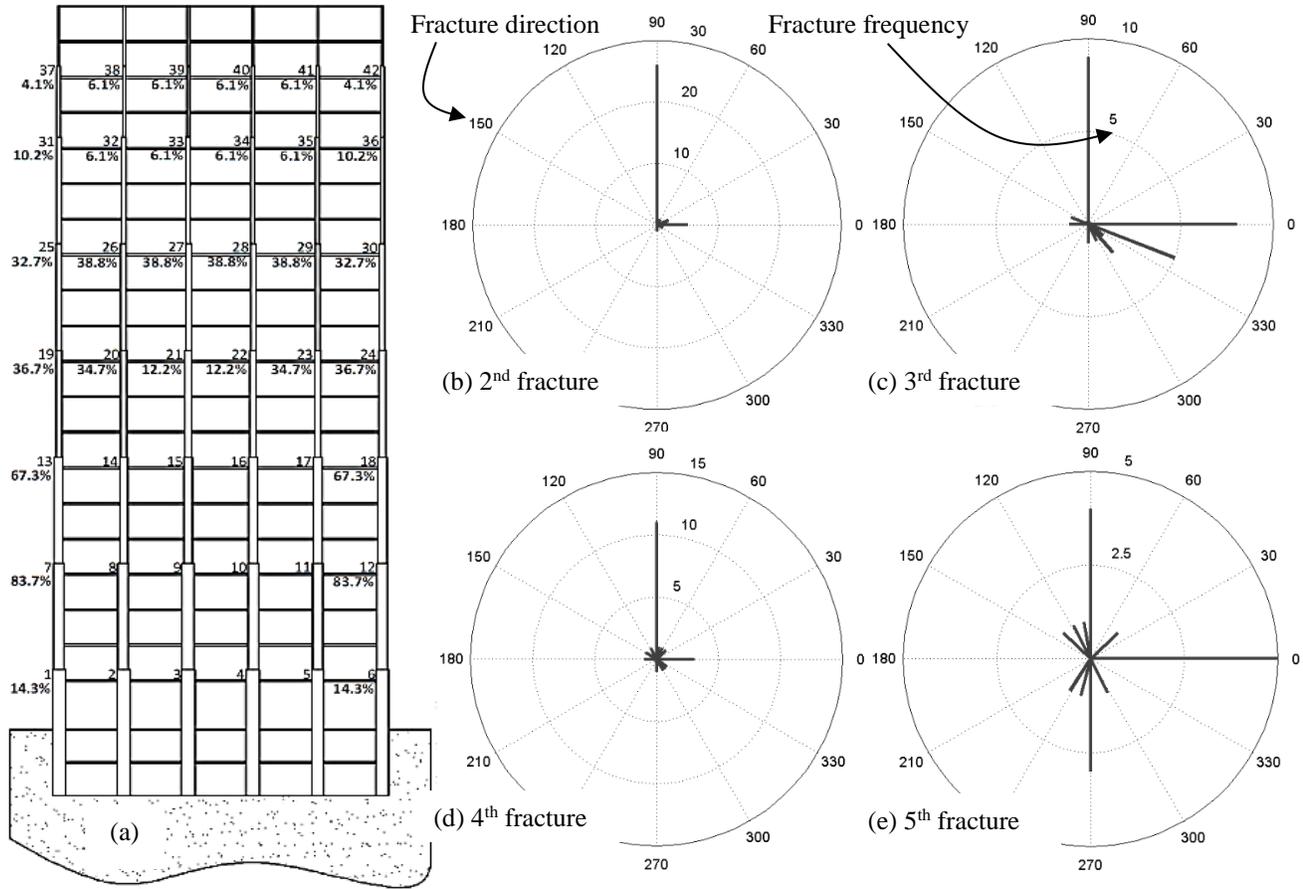


Figure 9: Fracture patterns in 20-story frame (a) Fracture likelihood at each splice, and (b)-(e) Polar histograms indicating directions of fracture propagation from splice to splice

445 The above observations provide a general sense of splices that are most vulnerable, suggesting that
 446 fractures begin in the exterior splices of lower stories, and propagate upwards and inwards.
 447 However, this observation about the temporal propagation is conjecture, since only aggregate
 448 probabilities are shown in Figure 9a, without information about the propagation of fracture from
 449 one splice to the next. To this end, Figures 9b-e illustrate polar histograms of fracture, which
 450 represent the “propagation directions” of splice fractures for each ground motion, and represent
 451 the vector direction from the i^{th} to the $i+1^{th}$ splice fracture. For example, positive 90 degrees on

452 the polar histogram indicates that the $i+1^{th}$ splice fracture was directly above the i^{th} fracture,
453 whereas 0 degrees indicates that it was directly to the right. Figures 9b-e show this information for
454 the 2nd, 3rd, 4th, and 5th splice fractures respectively. A corresponding figure is not shown for the
455 4-story frame, since only two splices fracture. With this background, an examination of Figures
456 9b-e reveals the following:

- 457 1. Referring to Figure 9b, a large majority of the 2nd fractures show an angle of 90 degrees, i.e.,
458 upwards. This is interesting, in that it represents that rather than propagating across a story, the
459 fractures propagate upwards through a column. Recall that the first fractures are predominantly
460 in the exterior columns in the lower stories. Interior columns in these stories have significantly
461 lower axial tension, as well as greater compression due to gravity; this may explain the
462 tendency of fracture to initially propagate upwards. From a behavioral standpoint, this type of
463 fracture propagation (as opposed to one that would sever a story) possibly results in a greater
464 retention of base shear capacity, such that structural performance is not severely compromised,
465 as shown previously in Figures 6a and b.
- 466 2. As shown in Figures 9c-e, subsequent fractures are less consistent in their direction of
467 propagation, possibly because as the fractures move to higher stories, interior column splices
468 become more prone to fracture as well, as discussed earlier.

469 In summary, Figures 9a-e (i.e., the fracture percentages and the polar histograms) suggest a general
470 pattern of splice fracture. In broad terms, fractures begin in the lower exterior columns then move
471 upwards, and inwards in the higher stories. There is no observed tendency for fractures to
472 propagate horizontally severing a story. When considered along with the previous observations
473 regarding the beneficial effects of frame rocking, and the ability of splices to carry compression

474 even after fracture, this may well explain the satisfactory performance of the building even with
475 splice fracture.

476 It is important to recall here that the (F) simulations only examine the response of *intact* or
477 undamaged buildings with respect to splice fractures. However, referring to Figures 5a and b and
478 associated discussion, it is highly likely that frames undergo fracture at hazard levels significantly
479 below design level, with the implication that several splice fractures may already be present in
480 existing buildings. The effect of these pre-existing fractures merits future examination.

481 **SUMMARY AND CONCLUSIONS**

482 This study examines the effect of Welded Column Splice fracture on the seismic response of Steel
483 Moment Resisting Frames (SMRFs). The primary motivation for this paper is pre-Northridge
484 welded column splice details with large crack like flaws that arise at the root of Partial Joint
485 Penetration (PJP) welds. Previous research has shown these details to be highly susceptible to
486 fracture. When analyzed within a Performance Based Earthquake Engineering (PBEE) framework,
487 this susceptibility results in unacceptably high probabilities of splice fracture over the life of the
488 building. Further, splices in many buildings from the pre-Northridge era have not been retrofitted;
489 the post-Northridge retrofits have focused mainly on welded beam to column connections. The
490 implication is that WCSs may well be a weak link in building safety and performance. Retrofitting
491 splices in operational buildings is costly and challenging, and typically involves replacing the
492 entire PJP weld with a Complete Joint Penetration (CJP) weld. However, such a strategy is
493 predicated on the assumption that splice fracture will necessarily trigger building failure. In
494 addition to being possibly conservative, this assumption is simplistic and consistent with building
495 performance assessment based on component response (the state of the art in the 1990s) in contrast
496 to comprehensive system-based performance assessment, which is currently prevalent. Against

497 this backdrop, this study examines the seismic response of two SMRFs (4- and 20- story) including
498 the effects of splice fracture within a modern PBEE framework.

499 The response is examined through a series of “cloud” analyses of the frames, where each cloud
500 analysis includes Nonlinear Response History Analysis of the frame models subjected to 100
501 ground motions. This procedure allows for an examination of frame response across a range of
502 ground motions as well as seismic intensities. When combined with local hazards, these analyses
503 may be used for risk assessment of various aspects of structural response such as peak
504 deformations, splice fracture, and collapse. The frame models simulate key aspects of structural
505 response such as geometric and material nonlinearity, and finite joint size. Most importantly from
506 the perspective of this study, the models are able to simulate tension fracture of the splice. The
507 modeling methodology relies on previous experimental, computational, and analytical research on
508 splices such that both the stress that triggers splice fracture, as well as subsequent cyclic response
509 are suitably simulated.

510 Two sets of cloud analyses are conducted. The first set examines frames with splices that do not
511 fracture, representing the performance of fully retrofitted splices. The second set examines initially
512 intact frames with simulated fracture; these represent unretrofitted frames that have not
513 experienced a damaging earthquake.

514 The primary finding of the cloud simulations is that splice fracture may not exacerbate structural
515 response or trigger collapse. In fact, splice fracture mobilizes rocking motions in the frame,
516 engaging the rotational inertia of the building above the fractured splice. This rocking reduces
517 structural deformations, possibly increasing the margin of safety against collapse. This type of
518 rocking-induced performance enhancement is well studied in literature, to the point that research

519 has specifically examined tension-gapping columns as response mitigation mechanism (Wada et
520 al., 2001). A closer examination of the fracture patterns indicates that the fractures usually
521 originate in the exterior columns of the lower stories. For the 20 story frame, the primary tendency
522 is for the fractures to propagate upwards through a column, rather than sideways across a story.
523 The absence of story-severing fractures may additionally explain the satisfactory performance
524 observed despite the splice fractures. Subsequent (less frequent fractures) in higher stories tend to
525 be distributed more uniformly through the story, rather than just in the exterior columns.

526 Although the general finding is that for the considered frames, splice fracture is not significantly
527 detrimental to performance, this must be interpreted very cautiously against the limitations of the
528 study, which are numerous. From a methodological perspective, the main issue is that only two
529 buildings are studied. Although these are fairly generic in their floorplan and frame configuration,
530 deviations from these structural forms will result in behavior dissimilar to that reported in this
531 study. Also from a methodological perspective, the limitations of cloud analysis (e.g. assuming
532 the dispersion in response to be a constant at all IM levels) may be questioned. However, the
533 general trends in response are strong (and similar to those researched previously through
534 Incremental Dynamic Analysis of the same frames –(Galasso et al., 2015)), suggesting that this
535 limitation is not serious. Other methodological assumptions including simulating the building
536 response, including splice fracture as deterministic, such that the only variability is in the ground
537 motions. However, in the context of establishing baseline behavioral trends, this assumption is
538 reasonable.

539 From a modeling perspective, some issues must be noted as well. Chiefly, the splices simulate
540 tension fracture of the flange and web material. As a result, the post fracture response can simulate
541 axial gapping (separation) of the column, as well as flexural loss of strength. However, it cannot

542 directly simulate the loss of shear strength at the splice, although it does reduce the lateral stiffness
543 of the columns due to introduction of the hinge within the column. The influence of this limitation
544 on simulated response may be interpreted as follows: (1) when the splice does not fracture
545 completely (as is the case in several splices), the modeling assumptions are valid, (2) in cases
546 where the splice is completely severed, then the simulations in this study may yield unconservative
547 insights (simulated performance better than true performance) especially if the remainder of the
548 structure is not sufficiently redundant; even in this case it is worth noting that the splices carry
549 shear in compression, and (3) if relative shear deformations are restricted at splices (through details
550 as such as full depth web plates welded to one of the connected columns) then response similar to
551 that observed in this study is possible. Modeling the loss of shear capacity due to tension fracture
552 is challenging within the constraints of frame-element based simulation. Recognizing this,
553 upcoming modeling guidelines for performance assessment of existing buildings (ATC 114 – n.d.)
554 propose a modeling approach similar in intent to the one used here. Other modeling limitations
555 include the use of 2-dimensional frame simulation, versus 3-dimensional building simulation, and
556 the use of only unidirectional (horizontal) ground motions, rather than 3-dimensional motions
557 including vertical accelerations. In summary, while the study reveals beneficial response modes
558 and behavioral trends, the results must be cautiously interpreted against all these limitations.

559 Finally, from a practical standpoint, this study suggests that full retrofit of the splices (i.e.
560 replacement of PJP with CJP welds) may not always be necessary, as a rule, and the NLRHA
561 conducted within a rigorous, probabilistic framework may respond beneficial response modes that
562 mitigate risk. In fact, such analyses may reveal contrary results; for the frames studied herein, the
563 simulations representing the retrofitted frames showed higher deformations. The analyses also
564 suggest considering other retrofit strategies that may be more economical than complete weld

565 replacement. These may include details that restrain unseating or loss of shear capacity of the
566 column e.g., through guiding plates on the flanges or a bolted web plate. From a scientific
567 standpoint, the approach for modeling post-fracture response of fibers (through the constructed
568 constitutive model – Figure 5) may be considered a contribution. In closing, it is emphasized that
569 the main value of the study is not in the actual results of the NLRHA, which are somewhat specific
570 to the considered buildings, and limited by modeling assumptions. Rather, the study indicates that
571 NLRHA (if conducted within a sophisticated modeling framework), may suggest counterintuitive
572 response, and strategies for risk mitigation, which may or may not include retrofit, based on a
573 refined consideration of tradeoffs.

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