

Supplementary Material

Optimisation Approaches for the Synthesis of Water Treatment Plants

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MILFP data discretisation

Table ?? and Table ?? present the discretisation points of pressures and operating conditions for the seawater desalination case study. Points that resulted in separation efficiencies approaching or below zero were disregarded.

Table S1: Pressure points in MILFP model, seawater desalination example

Discrete level j	Pressure p_{ij}							
	CF	DAF	MMF	MF	UF	NF	RO1	RO2
$j1$	0.10	0.40	0.10	0.10	0.10	0.5	5.0	5.0
$j2$	0.15	0.70	0.12	0.12	0.12	0.8	5.3	5.2
$j3$	0.20	0.40	0.15	0.15	0.14	1.0	5.5	5.5
$j4$	0.10	0.70	0.18	0.18	0.18	1.3	5.8	5.8
$j5$	0.15	0.40	0.20	0.20	0.20	1.6	6.0	6.0
$j6$	0.20	0.70	0.10	0.10	0.22	0.5		5.0
$j7$	0.10	0.40	0.12	0.12	0.24	0.8		5.2
$j8$	0.15	0.70	0.15	0.15	0.26	1.0		5.5
$j9$	0.20	0.40	0.18	0.18	0.28	1.3		5.8
$j10$	0.10	0.70	0.20	0.20	0.30	1.6		6.0
$j11$	0.15	0.40	0.10	0.10		0.5		
$j12$	0.20	0.70	0.12	0.12		0.8		
$j13$	0.10	0.40	0.15	0.15		1.0		
$j14$	0.15	0.70	0.18	0.18		1.3		
$j15$	0.20	0.40	0.20	0.20		1.6		
$j16$	0.10	0.70	0.10					
$j17$	0.15	0.40	0.12					
$j18$	0.20	0.70	0.15					
$j19$			0.18					
$j20$			0.20					
$j21$			0.10					
$j22$			0.12					
$j23$			0.15					
$j24$			0.18					
$j25$			0.20					
$j26$			0.10					
$j27$			0.12					

Table S2: Operating conditions points in MILFP model, seawater desalination example

Discrete level j	Coagulant dose		Energy input	Residence time	Length	Load	Media dia	Temp	Hydrophobicity	MWCO	pH
	cd_{1j}	cd_{2j}	gf_{ij}	tf_{ij}	l_{ij}	ld_{ij}	d_{ij}^{MED}	tem_{ij}	h_{ij}	$mwco_{ij}$	ph_{ij}
	CF SED	CF DAF	CF	CF	MMF	MMF	MMF	MF	NF	NF	RO2
j_1	1	1	10	5	0.5	0.5	2	20	0.002	300	8.0
j_2	3	1	10	5	1.5	0.5	2	25	0.05	800	8.0
j_3	4	1	10	20	2.5	0.5	2	30	0.3	1,200	8.0
j_4	7	1	10	20	0.5	1.0	2	20	0.8	300	8.0
j_5	10	1	10	35	1.5	1.0	2	25	1.0	800	8.0
j_6	12	1	10	35	2.5	1.0	2	30	0.002	1,200	9.5
j_7	13	1	120	5	0.5	1.5	2	20	0.05	300	9.5
j_8	16	1	120	5	1.5	1.5	2	25	0.3	800	9.5
j_9	18	1	120	20	2.5	1.5	2	30	0.8	1,200	9.5
j_{10}	20	1	120	20	0.5	0.5	5	20	1.0	300	9.5
j_{11}		1	120	35	1.5	0.5	5	25	0.002	800	
j_{12}		1	120	35	2.5	0.5	5	30	0.05	1,200	
j_{13}		20	10	5	0.5	1.0	5	20	0.3	300	
j_{14}		20	10	5	1.5	1.0	5	25	0.8	800	
j_{15}		20	10	20	2.5	1.0	5	30	1.0	1,200	
j_{16}		20	10	20	0.5	1.5	5				
j_{17}		20	10	35	1.5	1.5	5				
j_{18}		20	10	35	2.5	1.5	5				
j_{19}					0.5	0.5	8				
j_{20}					1.5	0.5	8				
j_{21}					2.5	0.5	8				
j_{22}					0.5	1.0	8				
j_{23}					1.5	1.0	8				
j_{24}					2.5	1.0	8				
j_{25}					0.5	1.5	8				
j_{26}					1.5	1.5	8				
j_{27}					2.5	1.5	8				

Table ?? and Table ?? present the discretisation points of pressures and operating conditions for the surface water treatment case study. Points that resulted in separation efficiencies approaching or below zero were disregarded.

Table S3: Pressure points in MILFP model, surface water treatment example

Discrete level j	Pressure $p_{i,j}$						
	CF	DAF	MMF	MF	UF	NF	RO1
j_1	0.10	0.40	0.10	0.10	0.10	0.5	3.0
j_2	0.15	0.70	0.12	0.12	0.12	0.8	3.5
j_3	0.20	0.40	0.15	0.15	0.14	1.0	4.0
j_4	0.10	0.70	0.18	0.18	0.18	1.3	4.5
j_5	0.15	0.40	0.20	0.20	0.20	1.6	5.0
j_6	0.20	0.70	0.10	0.10	0.22	0.5	
j_7	0.10	0.40	0.12	0.12	0.24	0.8	
j_8	0.15	0.70	0.15	0.15	0.26	1.0	
j_9	0.20	0.40	0.18	0.18	0.28	1.3	
j_{10}	0.10	0.70	0.20	0.20	0.30	1.6	
j_{11}	0.15	0.40	0.10	0.10		0.5	
j_{12}	0.20	0.70	0.12	0.12		0.8	
j_{13}	0.10	0.40	0.15	0.15		1.0	
j_{14}	0.15	0.70	0.18	0.18		1.3	
j_{15}	0.20	0.40	0.20	0.20		1.6	
j_{16}		0.70	0.10				
j_{17}		0.40	0.12				
j_{18}		0.70	0.15				
j_{19}			0.18				
j_{20}			0.20				
j_{21}			0.10				
j_{22}			0.12				
j_{23}			0.15				
j_{24}			0.18				
j_{25}			0.20				
j_{26}			0.10				
j_{27}			0.12				

Table S4: Operating conditions points in MILFP model, surface water treatment example

Discrete level j	Coagulant dose cd_{tj}	Energy input gf_{tj}	Residence time tf_{tj}	Length l_j	Load ld_{tj}	Media diameter d_{tj}^{MED}	Temperature tem_{tj}	Hydrophobicity h_{tj}	MWCO $mwco_{tj}$	pH ph_{tj}
	CF	CF	CF	MMF	MMF	MMF	MF	NF	NF	CF
$j1$	10	10	5	0.5	0.5	2	20	0.002	300	3.0
$j2$	30	10	5	1.5	0.5	2	25	0.05	800	4.0
$j3$	50	10	20	2.5	0.5	2	30	0.3	1,000	5.0
$j4$	10	10	20	0.5	1.0	2	20	0.8	300	6.0
$j5$	30	10	35	1.5	1.0	2	25	1.0	800	7.0
$j6$	50	10	35	2.5	1.0	2	30	0.002	1,000	8.0
$j7$	10	120	5	0.5	1.5	2	20	0.05	300	3.0
$j8$	30	120	5	1.5	1.5	2	25	0.3	800	4.0
$j9$	50	120	20	2.5	1.5	2	30	0.8	1,000	5.0
$j10$	10	120	20	0.5	0.5	5	20	1.0	300	6.0
$j11$	30	120	35	1.5	0.5	5	25	0.002	800	7.0
$j12$	50	120	35	2.5	0.5	5	30	0.05	1,000	8.0
$j13$	10	10	5	0.5	1.0	5	20	0.3	300	3.0
$j14$	30	10	5	1.5	1.0	5	25	0.8	800	4.0
$j15$	50	10	20	2.5	1.0	5	30	1.0	1,000	5.0
$j16$	10	10	20	0.5	1.5	5			6.0	
$j17$	30	10	35	1.5	1.5	5			7.0	
$j18$	50	10	35	2.5	1.5	5			8.0	
$j19$				0.5	0.5	8				
$j20$				1.5	0.5	8				
$j21$				2.5	0.5	8				
$j22$				0.5	1.0	8				
$j23$				1.5	1.0	8				
$j24$				2.5	1.0	8				
$j25$				0.5	1.5	8				
$j26$				1.5	1.5	8				
$j27$				2.5	1.5	8				