

# The temporal characteristics of the early and late stages of L- and M-cone pathways that signal brightness

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## ABSTRACT

Flickering 560-nm light appears brighter and less saturated than steady light of the same average intensity. The changes in appearance are consistent with the visual signal's being distorted at some nonlinear site (or sites) within the visual pathway at which new temporal components, not part of the original waveform, are produced. By varying the input stimulus to manipulate these new temporal components—called “distortion products”—and measuring observers' sensitivity in detecting them, we derived the temporal attenuation characteristics of the early (pre-nonlinearity) and late (post-nonlinearity) stages of the L- and M-cone pathway that signals brightness.

We found that the early stage acts like a band-pass filter peaking at 10-15 Hz with sensitivity losses at both lower and higher frequencies, whereas the late stage acts like a two-stage low-pass filter with a corner frequency near 3 Hz. Although brightness is often associated with the fast achromatic or luminance pathway, these filter characteristics, and particularly those of the late filter, are consistent with comparable features of the L-M chromatic pathway that produce mainly chromatic distortion products (Petrova, Henning, and Stockman, 2013). A plausible site for the nonlinearity is after surround antagonism from horizontal cells. Modelling suggested the form of the nonlinearity to be initially expansive, but possibly with a hard limit at the highest input levels.

**Keywords:** Brightness, saturation, luminance, colour vision, flicker sensitivity, nonlinearity, temporal processing.

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## INTRODUCTION

Flickering a light of constant time-averaged intensity may enhance its brightness (e.g., Bartley, 1938, 1939, 1951a, 1951b; Brewster, 1838; Brücke, 1848) or change its hue (e.g., Ball, 1964; Ball & Bartley, 1966, 1971; Bartley & Nelson, 1960; Bleck & Craig, 1965; Petrova, Henning, & Stockman, 2013; Stewart, 1887; van der Horst & Muis, 1969). Such effects seem to arise from nonlinearities that distort the representation of the visual input within the visual pathway.

Flicker-induced changes in brightness differ from flicker-induced changes in hue in several ways: First, though the two effects can occur together, they can also occur separately. For instance, a deep-red flickering target looks yellower and less saturated than a steady field of the same time-averaged intensity but with little apparent change in brightness, whereas a flickering light near 560 nm looks brighter than a steady field with little or no change in hue (e.g., Ball, 1964; van der Horst & Muis, 1969). Second, the two effects have very different spectral sensitivities. For luminance-equated lights, the hue change is strongly dependent on wavelength, whereas the brightness enhancement is not (van der Horst & Muis, 1969; Walters & Harwerth, 1978). For instance, the threshold spectral sensitivity for brightness enhancement approximately follows the  $V(\lambda)$  photopic spectral sensitivity (Walters & Harwerth, 1978). Third, the brightness enhancement is consistent with an expansive nonlinearity (e.g., Wu, Burns, Reeves, & Elsner, 1996), whereas the hue change in the red-green range is consistent with a compressive nonlinearity (Petrova et al., 2013; van der Horst & Muis, 1969) thus the two effects are probably generated by different nonlinearities. These distinctions raise the intriguing possibility that the two nonlinearities lie in different postreceptoral pathways, one, perhaps, in a chromatic pathway and the other, perhaps, in an achromatic or luminance pathway. In our previous paper, we investigated the hue change induced by 650-nm flicker (Petrova et al., 2013). In this paper, we focus on brightness enhancement, which is sometimes referred to as the “Brücke-Bartley” effect.

The principal stimulus used in these experiments was a contrast-modulated, sinusoidally-flickering 560-nm light that, when the flicker contrast is high, appears brighter than steady light of the same radiance and wavelength. A wavelength of 560 nm was chosen because, as our own observations confirm, flicker near that wavelength induces little change in hue (Ball, 1964; van der Horst & Muis). The contrast-modulated 560-nm stimulus consists of a sinusoidal carrier (of frequency  $f_c$  Hz) the contrast of which is sinusoidally modulated at a much lower modulation frequency ( $f_m$  Hz). This stimulus has no component at  $f_m$  Hz, but produces brightness changes at that frequency. We assume that the enhancement in brightness is caused by the distortion of the visual signal at some internal nonlinear site (or sites) at which new components, called distortion products,

are generated. In the contrast-modulated stimulus, components at the frequencies of the distortion products do not exist until after the nonlinearity. Consequently, distortion products can be used to distinguish characteristics of the “early” visual processes that precede the nonlinearity from “late” processes that follow it.

In this context, the visual system is treated as a linear-nonlinear-linear “sandwich” of stages (e.g., Burns, Elsner, & Kreitz, 1992; Burton, 1973; Chen & Makous, 1990; Chen, Makous, & Williams, 1993; MacLeod, Williams, & Makous, 1992; Marmarelis & Marmarelis, 1978; Petrova et al., 2013; Spekreijse & Reits, 1982; Stockman & MacLeod, 1986; Stockman, MacLeod, & Lebrun, 1993; Stockman & Plummer, 1998; Trimble & Phillips, 1978; Victor & Shapley, 1980; Victor, Shapley, & Knight, 1977; Wu et al., 1996). Several aspects of our work are directly comparable with the previous work of Wu *et al.* (1996), as noted below.

[Insert Figure 1 about here]

Figure 1 illustrates the application of the sandwich model to the case of brightness enhancement. The left-hand column of Figure 1 illustrates one cycle of the temporal waveform of the visual input (panel S1) and the presumed representation of the waveform after it has been modified by successive stages of the linear-nonlinear-linear sandwich (subsequent panels). The right-hand column (panels C1 to C4) shows the amplitude spectra corresponding to the temporal waveforms shown in the left-hand column (i.e., the amplitudes of their constituent sinusoidal components). The waveforms and their spectra are intended merely to indicate the information present at each stage and should not be taken as the form in which the information is transmitted.

Panel S1 shows one modulation cycle of the contrast-modulated stimulus, which is produced by sinusoidally flickering a light at  $f_c$  Hz and sinusoidally modulating its contrast at a lower frequency of  $f_m$  Hz. Panel C1 at the top right illustrates the amplitude spectrum of the stimulus, which comprises three high-frequency sinusoidal components: the “carrier” frequency at  $f_c$  Hz, and two “side-bands” at  $f_c - f_m$  and  $f_c + f_m$  Hz. The component at 0 Hz corresponds to the mean (“DC”) level around which the light is modulated. At this stage there is no sinusoidal component at  $f_m$  Hz. Consequently, all an observer should perceive is flicker at  $f_c$  varying in strength at  $f_m$ .

The temporal characteristics of the “early” linear stages before the visual nonlinearity are exemplified in Figure 1 by a low-pass filter (panel F1). The filter attenuates the components of the visual stimulus (Panel C1) to produce the intermediate spectrum (Panel C2). The intermediate stimulus, when  $f_m \ll f_c$ , is approximately an attenuated version of the input stimulus (Panel S2). In the continued absence of a component at  $f_m$ , no perceptible change in brightness at  $f_m$  should be expected (as illustrated by the unchanging icons above Panel S2).

The linear early stage is followed in the sandwich model by a nonlinearity (N). The example in Figure 1 shows an expansive nonlinearity that selectively expands high signal intensities relative to low ones, thus selectively enhancing the peaks of the waveform (Panel S3). The contrast-modulated flicker signal passing through the nonlinearity has its frequency spectrum altered by the nonlinearity (Bedrosian & Rice, 1971). Components at higher harmonics of the carrier and side-bands are produced as well as components, called inter-modulation distortion products. Among the latter, there is one at  $f_m$  and one at  $2 f_m$  Hz (Panel C3). It is the component at  $f_m$  Hz that we wish to consider as the distortion product that produces the brightness changes illustrated by the icons above Panel S3. For simplicity, we assume that the nonlinearity is static, in that its input-output relation depends on the instantaneous value of the input, not on previous inputs, and that the form of the nonlinearity is independent of temporal frequency. We further assume that it is the distortion product at the frequency of  $f_m$  Hz that produces the brightness change that the observers see at that frequency.

The collective temporal characteristics of the linear processes after the nonlinearity are represented in Figure 1 by a second low-pass filter (Panel F2). This late filter, like the early one, selectively attenuates frequencies near  $f_c$ , but not enough for them to fall below the flicker threshold (Panel C4). Thus, brightness enhancement at  $f_m$  is accompanied by flicker near  $f_c$ , as we find (see Figure 2, below). The goal of this work is to determine the forms of both the early and the late filters. We emphasize that these filters are hypothetical and depend on the applicability of the sandwich model to the phenomenon of flicker-induced brightness enhancement.

Versions of the sandwich model have been explored in analysing the nonlinear interactions that produce hue changes (Petrova et al., 2013) and our techniques have been described there in full. The work by Wu, Burns, Reeves, and Elsner (1996) is also directly relevant. They estimated the magnitude of brightness enhancement at a series of carrier frequencies and stimulus modulations by matching one cycle of the amplitude-modulated flicker against one cycle of a sinusoidally-varying matching light, from which they inferred that the early part of the visual pathway signalling brightness is consistent with an accelerating nonlinearity preceded by a broadly tuned bandpass filter peaking at about 16 Hz. Their technique, however, did not yield direct estimates of the characteristics of a late filter.

Given that we see mainly an increase in brightness, it seems reasonable to suppose that we are dissecting a brightness pathway. Whether brightness is mediated by the so-called achromatic or luminance pathway or by some other pathway, however, is a question to which we will return in the General Discussion.

## GENERAL METHODS

This research adhered to the tenets of the Declaration of Helsinki. Many of the experimental details can be found in our companion paper (Petrova et al., 2013). We describe here the essential characteristics of the methods.

### ***Apparatus***

A Maxwellian-view optical system with a 2.5-mm entrance pupil illuminated by a 900-W Xe arc lamp was used to produce the stimuli. Wavelengths were selected by interference filters with full-width at half-maximum bandwidths of between 7 and 11 nm (Ealing or Oriel). The radiance of each channel was controlled by the insertion of fixed neutral density filters (Ealing or Oriel or Melles Griot) and by the rotation of circular, variable  $3\text{-log}_{10}$  unit neutral density filters (Rolyn Optics). The flickering waveforms were generated by pulse-width modulation of fast, liquid-crystal, light shutters running at 400 Hz with rise and fall times faster than  $50\ \mu\text{s}$  (Displaytech) thus effectively producing variable width rectangular pulses at a fixed rate of 400 Hz. The pulse-width was varied under computer control using programmable timers (Data Translation, DT2819) to produce sinusoidal components at the desired frequencies and at signal modulations up to 92%.

### ***Observers***

The same observers participated as in the experiments of Petrova *et al.* (2013). Both were authors, one male (GBH) and one female (DP), and both were experienced psychophysical observers with normal colour vision and normal (DP) or corrected to normal (GBH) spatial acuity.

### ***Stimuli***

Visual stimuli were centrally-fixated target discs of  $4^\circ$  diameter. The flickering target was a 560-nm light that was set, in the main experiments, to one of four time-averaged radiance levels (8.26, 8.86, 9.51, or  $10.11\ \text{log}_{10}\ \text{quanta}\ \text{s}^{-1}\ \text{deg}^{-2}$ , corresponding to 2.16, 2.76, 3.41, and  $4.01\ \text{log}_{10}$  trolands). The background was dark. The target was sinusoidally flickered at  $f_c$  Hz and its contrast was sinusoidally-modulated at  $f_m$  Hz to produce “contrast-modulated sinusoidal flicker” (Panel S1, Figure 1). [Occasionally unmodulated sinusoidal flicker ( $f_m = 0$  Hz) was used.] Flicker in both cases was around a given time-averaged radiance.

Since the waveforms we used are somewhat atypical, we again describe them and the naming conventions we adopted: we refer to the amplitude of the flicker waveform relative to the mean radiance as the “overall modulation”,  $m$ , which is defined as the conventional Michelson contrast:

$$m = \frac{I_{max} - I_{min}}{I_{max} + I_{min}}, \quad [1]$$

where  $I_{max}$  and  $I_{min}$  are the maximum and minimum radiances of the stimulus, respectively. Thus, for simple sinusoidal flicker the waveform,  $A(t)$ , is given by:

$$A(t) = \bar{R}\{1 + m \sin(2\pi f_c t)\}, \quad [2]$$

where  $\bar{R}$  is the mean radiance and  $f_c$  is the rate of flicker (Hz).

In experiments in which contrast-modulated flicker was used, the temporal waveform,  $A_m(t)$ , is:

$$A_m(t) = \bar{R}\{1 + m [0.5 + 0.5 \cos(2\pi f_m t)] \sin(2\pi f_c t)\}, \quad [3]$$

where  $f_c$  is the carrier frequency,  $f_m$  is the modulation frequency (both in Hz), and  $m$  is the overall modulation. We call this stimulus “contrast-modulated flicker”. The factor in square brackets is sometimes called the “amplitude modulation” and the amplitude-modulation in our experiments always varied sinusoidally between 1 and zero at  $f_m$  Hz; i.e., it was 100% amplitude modulation.

The flickering component of Equation [3] can be expanded to show that it comprises three sinusoidally-flickering terms:

$$A_m(t) = \bar{R}\{1 + m [0.5 \sin(2\pi f_c t) + 0.25 \sin(2\pi(f_c - f_m)t) + 0.25 \sin(2\pi(f_c + f_m)t)]\}, \quad [4]$$

where the components, at  $f_c$  Hz, with amplitude  $\bar{R}m/2$  and two sidebands at  $f_c - f_m$  and  $f_c + f_m$  Hz with half the amplitude of the carrier, are made explicit. (Note that in our experiments the amplitude modulation was always 100% and the overall modulation of the entire waveform,  $m$ , was varied with the result that the sidebands always had half the contrast of the carrier.) For further details, see Petrova et al. (2013).

### **Calibration**

The radiant fluxes of test and background fields were measured daily in the plane of pupil using a calibrated UDT S370 optometer (UDT Instruments, San Diego). The means by which we checked for system linearity is described in our earlier paper (Petrova et al., 2013).

### **Procedures**

The visual stimulus, focused in the plane of the pupil, was the only visible light source for the observers in an otherwise darkened room. They used their right eye for observation; their left eye was covered. The image of the source in the plane of the observer’s pupil was 2.5 mm diameter—

always less than the diameter of the natural pupil. The method of adjustment was used to measure visual responses in the experiments.

In experiments using contrast-modulated stimuli, the observers were asked to find: (i) the modulation depth at which all flicker disappeared, and (ii) the modulation depth at which brightness changes at the modulation frequency,  $f_m$ , disappeared. The results for three runs of each sort were averaged and the mean and standard error for each condition determined. The procedures were similar to those described in Petrova (2013).

## **PRELIMINARY EXPERIMENT: Fusion frequencies for detecting flicker or brightness enhancement**

### ***Introduction***

In a preliminary experiment, we determined the highest carrier frequency ( $f_c$ ) at which either flicker at  $f_c$  or brightness change at  $f_m$  can be detected as a function of target radiance. These are known as critical fusion frequencies. Our goal was to determine the separation between the two fusion frequencies, in part to see if the Talbot-Plateau Law failed at any target radiances. A failure of the Talbot-Plateau law (Plateau, 1835; Talbot, 1834), which holds that a light flickering above the fusion frequency should appear identical to a steady light of the same time-averaged intensity, would be found if the fusion frequency for detecting flicker near  $f_c$  was lower than that for detecting the brightness change at  $f_m$ .

### ***Methods***

We used a contrast-modulated stimulus and fixed the modulation frequency,  $f_m$ , at 0.5 Hz. In separate blocks of trials, the time-averaged radiance of the contrast-modulated, 560-nm target was varied in steps of approximately 0.45  $\log_{10}$  unit from 5.81 to 10.11  $\log_{10}$  quanta  $s^{-1} \text{ deg}^{-2}$ . At each radiance, observers varied  $f_c$  in 0.5 Hz steps to find the highest frequency at which either flicker or brightness change was just perceptible. Three flicker settings were made first followed by three brightness settings.

### ***Results***

Figure 2 shows the threshold frequencies (linear scale) for flicker (white dotted circles) and brightness-change (green dotted diamonds) as a function of  $\log_{10}$  radiance. Data for each observer are shown separately and the error bars indicate  $\pm$  one standard error.

[Insert Figure 2 about here]

Curves for both observers increase steadily with increasing radiance from about  $6.0$  to  $9.0 \log_{10}$  quanta  $s^{-1} \text{ deg}^{-2}$ . The curves for detecting a brightness change begin to flatten with further increases in radiance at a slightly lower radiance than those for detecting flicker, but both appear to decrease slightly at the very highest radiance used.

### **Discussion**

One reason for this experiment was to discover whether the Talbot-Plateau fails at any target radiance as it does with S-cone isolating stimuli (Stockman & Plummer, 1998). Although the separation between the brightness and the flicker fusion frequencies is smaller for GBH than for DP, the fusion frequencies for seeing a brightness change are always below those for seeing flicker. Consequently, the results are consistent with the Talbot-Plateau law. The gap in frequency between reporting flicker and reporting brightness change suggests that near-threshold *flicker* is relatively unaffected by the nonlinearity. This result indicates that at any frequency, there will be a range of near-threshold modulations within which flicker will be visible but the distortion product that produces brightness change will be undetectable and that we may safely assume small-signal linearity near the threshold for flicker.

It may be helpful to outline what observers typically see in these experiments as the carrier frequency at  $f_c$  is increased. Below the fusion frequency for detecting both flicker near  $f_c$  and the brightness change at  $f_m$ , observers see mainly a brightness change at  $f_m$  Hz (as illustrated by the icons above Panel S4 in Figure 1) superimposed on a slow waxing and waning of the strength of the flicker at the same low frequency, with the increased brightness coinciding with the increased amplitude of flicker. Below the fusion frequency for flicker detection but above that for detecting the brightness change, observers see only the waxing and waning of the flicker strength at  $f_m$  Hz with no brightness variation. Lastly, above the fusion frequency for detecting both the flicker and the brightness change, the observer sees only a steady, non-flickering target. Experienced observers can dissociate the brightness change from flicker under most conditions, except when  $f_c$  and  $f_m$  are both low in frequency where they become difficult to distinguish (see below).

## **EXPERIMENT I: TCSFs for brightness change, flicker and chromatic flicker as a function of $f_c$**

### **Introduction**

In Experiment I, we measured temporal contrast-sensitivity functions (TCSFs) using contrast-modulated stimuli with  $f_m$  fixed at 0.5 Hz and variable  $f_c$  Hz. Observers varied the overall modulation to find thresholds for detecting the 0.5-Hz brightness change at each  $f_c$ .



Given that the 0.5-Hz brightness component is present in the system only after the nonlinearity and that observers vary the modulation to produce the *same* threshold 0.5-Hz brightness signal at the input to the late filter for all  $f_c$  Hz, the effect of the late filter on the brightness-change thresholds will be a constant factor, possibly different for different radiances, but independent of  $f_c$ . The TCSF, therefore, provides a direct measure of the attenuation characteristics of the early filter (F1 in Figure 1). For further details see our earlier paper (Petrova et al., 2013).

In this experiment, we also compare the brightness-change thresholds with conventional TCSFs measured with sinusoidal monochromatic (560-nm) and chromatic flicker. The conventional TCSFs are also used later in the General Discussion to estimate missing parts of the early and late filter characteristics (see below).

### **Methods**

The three experiments were carried out at mean radiances of 8.26, 8.86, 9.51, and 10.11  $\log_{10}$  quanta  $s^{-1} \text{ deg}^{-2}$  indicated by the coloured triangles just above the abscissae of Figure 2.

#### *(i) Brightness-enhancement temporal sensitivity measurements*

The primary target was the 4° diameter, contrast-modulated 560-nm light of Equation [3] with the carrier at  $f_c$  and contrast-modulation,  $f_m$ , fixed at 0.5 Hz. Observers varied the overall modulation ( $m$  in Equation [3] or [4]) in either 0.02 or 0.10  $\log_{10}$  unit steps to find the threshold for just detecting a brightness change at  $f_m$ . The carrier frequency,  $f_c$ , was varied from 5 to 60 Hz. Below an  $f_c$  of 5 Hz, flicker at  $f_c$ , like the brightness change at  $f_m$ , appeared as changing brightness, so that it was difficult to separate the two.

#### *(ii) Conventional temporal sensitivity (flicker) measurements*

We measured conventional TCSFs with simple sinusoidally flickering stimuli (Equation [2]) with the same 4°, 560-nm target and the same observers. At each  $f_c$ , observers varied the overall modulation ( $m$  in Equation 2) in either 0.02 or 0.10  $\log_{10}$  unit steps to set the modulation of the target at which they could just detect its flicker. Contrast-modulation was not used for these measurements, because when  $f_c$  was low, the frequency components near  $f_c$  Hz and the distortion products near  $f_m$  were similar in frequency and appearance, and threshold settings consequently difficult. At higher  $f_c$ , the fusion thresholds for contrast-modulated flicker with  $f_m$  fixed at 0.5 Hz (not shown) were very similar to the thresholds with  $f_m$  fixed at 0 Hz shown as open symbols in Figure 3.

#### *(iii) Temporal contrast sensitivity for detecting equiluminant chromatic flicker.*

In these experiments, we first determined a series of equiluminant or “chromatic” stimuli with which to measure the chromatic TCSFs by superimposing a 4°, 650-nm target on the 4°, 560-nm

target, both flickering sinusoidally but 180° out-of-phase. The 560-nm and 650-nm components were luminance-equated individually for each observer by asking the observers to cancel the flicker of the superimposed targets. To do this, two 30-Hz targets were superimposed in opposite phase. Both were set to the maximum 92% modulation and the radiance of the 560-nm light was fixed. The observers then varied the radiance of the 650-nm light to null the perception of flicker. [Observers were also able to make small phase adjustments (in steps of 2 or 10°) to perfect the null, but the optimum phase for the null was always near 180°.] At the highest 560-nm radiance of 10.11 log<sub>10</sub> quanta s<sup>-1</sup> deg<sup>-2</sup> we had to use a 630-nm target to cancel 560-nm flicker because our most intense 650-nm target was insufficient. The mean time-averaged luminances of the combined, luminance-equated, 560-nm and 650-nm (or 630-nm) stimuli were then set to four different time-averaged luminances of the 560-nm target alone using the Sharpe *et al.* luminous efficiency estimates (2005, 2011) now adopted as a standard by the CIE (2006). Note that the addition of the 650-nm component changed the appearance of the steady target from yellow-green to an orange-yellow. As for the monochromatic measurements, the target for chromatic flicker was sinusoidally-flickered at  $f_c$  Hz (i.e.,  $f_m = 0$  Hz). The assumption behind this type of measurement is that flicker photometric cancellation silences the luminance pathway, so that flicker detection with the luminance-equated stimuli must be by some “chromatic” pathway (for review, see Stockman & Brainard, 2009). Hence, we term them chromatic TCSF measurements.

The chromatic TCSFs were then measured by jointly adjusting the modulation (Equation [2]) of the out-of-phase, luminance-equated 560- and 650-nm stimuli while maintaining the appropriate equiluminant ratio. Adjustments were made in steps of 0.02 or 0.10 log<sub>10</sub> unit to find the modulation at which the observers could just detect flicker

## Results

Figure 3 shows the log modulation thresholds for detecting the brightness change at  $f_m$  (filled coloured symbols), for detecting monochromatic (equichromatic) flicker at  $f_c$  (open symbols), and for detecting chromatic (equiluminant) flicker at  $f_c$  (grey symbols)—all plotted as a function of  $f_c$  (Hz, logarithmic axis). Results for DP are shown in the left-hand column, those for GBH, in the right-hand column. The time-averaged radiance (log<sub>10</sub> quanta s<sup>-1</sup> deg<sup>-2</sup>) for each row (indicated at the top right of each panel in the right-hand column) increases from 8.26 at the top to 10.11 at the bottom.

[Insert Figure 3 about here]

The results in Figure 3 show that the brightness-change TCSFs (filled coloured symbols) particularly for DP fall-off slightly less steeply with increasing frequency than the monochromatic 560-nm flicker TCSFs (open symbols). (The differences are plotted as open symbols in Figure 10,

below.) The chromatic TCSFs (grey symbols) have a limited range at high-frequencies, but where they overlap with the brightness change TCSFs, the chromatic TCSFs fall -off much more steeply with increasing frequency. (The differences are plotted as grey symbols in Figure 7, below.)

### **Discussion**

We expected the brightness-change TCSFs to be shallower than the chromatic flicker TCSFs, because the brightness-change TCSFs depend on a fixed-frequency distortion product and thus are not affected by attenuation by the late filter. The relatively smaller differences in high-frequency slope found between the brightness-change TCSFs and the monochromatic TCSFs may suggest that the brightness change and monochromatic flicker are detected by different pathways (see Discussion). The monochromatic TCSFs (open symbols in Figure 3) are band-pass in form. They peak between about 5 and 10 Hz and fall-off at low frequencies with slopes of about  $0.8 \log_{10}$  unit per decade, and at high frequencies with slopes of more than  $4 \log_{10}$  units per decade. The low- and high-frequency losses are consistent with other achromatic and monochromatic flicker TCSFs (e.g., De Lange, 1958; Green, 1969; Kelly, 1961, 1973; Petrova et al., 2013; Varner, Jameson, & Hurvich, 1984). By contrast, the chromatic TCSFs (grey symbols) are low-pass in form and fall-off in sensitivity above 5 to 10 Hz more steeply than the monochromatic TCSFs. These data are similar in shape to other TCSFs measured with equiluminant chromatic flicker (e.g., Kelly, 1975; Kelly & van Norren, 1977; Varner et al., 1984). Given the difficulty of perfectly equating the luminances of counter-phase flickering lights across the entire stimulus area, the chromatic TCSFs may contain some luminance-flicker artefacts at the highest temporal frequencies where the chromatic signal is so much smaller than the luminance signal (e.g., Kelly & van Norren, 1977; Varner et al., 1984).

As in our companion paper, the TCSFs will be used to estimate the characteristics of the early and late filter at frequencies at which they could not be determined from the brightness-change measurements (see General Discussion).

## **EXPERIMENT II: TCSFs for brightness change as a function of $f_m$**

### **Introduction**

The contrast-sensitivity for detecting the brightness change at  $f_m$  as a function of  $f_m$  for a fixed  $f_c$  allows us to extract an estimate of temporal characteristics of the filter after the nonlinearity--- the late filter. The contrast-modulated stimuli generate a distortion product at  $f_m$  Hz *after* the nonlinearity, which is seen as a brightness change. The observers' task, as before, was to detect the

slow brightness change at  $f_m$  Hz. Since the stimuli have the same  $f_c$  and  $f_m \ll f_c$ , they are similarly affected by the linear (early) filter that precedes the nonlinearity. Consequently, the changes in sensitivity with  $f_m$  are determined by the nonlinearity and the late filter. (A supplementary experiment described in the next section is required to estimate the temporal characteristics of the late filter independent of the effects of the nonlinearity.)

## **Results**

Figure 4 shows the TCSFs for detecting brightness change as a function of  $f_m$  (logarithmic axes). Data for DP are shown in the upper panel and those for GBH in the lower panel. Functions for four radiance levels ( $\log_{10}$  quanta  $s^{-1} \text{ deg}^{-2}$ ) are shown: 8.26 (dark triangles), 8.86 (dark green circles), 9.51 (light green diamonds), and 10.11 (light green squares). For these measurements, the 560-nm target was contrast-modulated at various  $f_m$  (Hz) with a fixed carrier frequency,  $f_c$ , of 30 Hz.

[Insert Figure 4 about here]

The results extend only up to 5 Hz because at higher modulation frequencies observers could not detect a brightness change varying at  $f_m$ . The TCSFs are mainly low-pass in form falling at about  $0.5 \log_{10}$  units per decade. Sensitivity increases between the two lowest radiances, but then decreases with further increases in radiance.

## **Discussion**

As noted in our companion paper, the shapes of these functions reflect the characteristics of both the non-linearity and the post non-linearity (late) filter. Because  $f_m \ll f_c$ , and  $f_c$  is fixed, the vertical positions of the functions, but not their shapes, are affected by the early filter. Sensitivity at each radiance is thus represented on logarithmic co-ordinates up to an unknown constant vertical displacement in terms of the overall modulation of the stimulus at the input to the nonlinearity. In the next section, we estimate the relation between the contrast of the distortion product at the output of the nonlinearity and the overall modulation,  $m$ , of the contrast-modulated stimulus at the input to the nonlinearity, so that the late filter (F2 in Figure 1) can be characterized.

To estimate the characteristics of the hypothesized late filter, we need to know how the amplitude of the distortion product at  $f_m$  Hz created by the nonlinearity is related to the overall modulation at the input to the nonlinearity, because it is the overall modulation at the input that we manipulate. In other words, we need to know, at each of the mean radiances we used, how changing the overall modulation at the input to the non-linearity affects the contrast of the distortion product at  $f_m$  at its output. A technique for determining this is described in the following supplementary experiment.

## **SUPPLEMENTARY EXPERIMENT: dependence of brightness change on modulation**

### ***Introduction***

In this supplementary experiment, we determine how the contrast of the  $f_m$ -distortion product at the output of the nonlinearity depends on the overall modulation,  $m$ , of the contrast-modulated stimulus at the input to the nonlinearity. Knowledge of this relation allows us to extract the late filter characteristics (F2 in Figure 1) from the brightness-change TCSF measurements made as a function of  $f_m$  and shown in Figure 4. To measure the size of the brightness enhancement, we use a matching procedure.

[Insert Figure 5 about here]

### ***Methods***

In a series of preliminary studies, we evaluated various methods of nulling or matching the brightness enhancement. We eventually adopted a side-by-side matching technique in which the 4° target was split into left and right hemi-fields. The stimulus arrangement is illustrated in Figure 5. In the left hemi-field, the observer was presented with the contrast-modulated, 560-nm target (with  $f_c = 30$  Hz and  $f_m = 0.5$  Hz). In the right hemi-field, the observer was presented with a brightness matching stimulus. The matching stimulus comprised two superimposed components: (i) a steady 560-nm “pedestal” that had the same time-averaged radiance and appearance as a non-flickering, 560-nm light in the left hemi-field; and (ii) a 560-nm light that was sinusoidally flickered at 0.5 Hz and set to the maximum 92% modulation with the same phase as the 0.5-Hz contrast-modulation ( $f_m$ ) of the left hemi-field. The combined stimulus in the right half-field produced brightness changes that were comparable to those produced by the contrast modulation in the left hemi-field. The observers adjusted the time-average radiance of the matching light (keeping the 92% modulation constant) to match the brightness of the left hemi-field at the peak of its contrast modulation. This was done under computer control using response buttons. Subjects could vary the radiance of the matching light in steps of either  $0.01 \log_{10}$  or  $0.08 \log_{10}$  to complete the match (see Figure 5). (The observers were also able to vary the phase between the contrast-modulation flicker and the sinusoidal flicker of the two hemi-fields in 2° or 10° steps until the maximum change in appearance of the two fields coincided. Even though the phase adjustments away from in-phase were relatively small, we retained them as part of the procedure because they helped the observers to make matches.) We tried various other techniques, such as varying the modulation of the 560-nm matching light, but they produced much poorer matches due to differences in the perceived brightness between the target and matching stimulus that could not be eliminated.

Wu et al. (1996) used a comparable method for matching flicker-induced brightness changes, but their stimuli were separated in time rather than space.

## **Results**

Figure 6 shows the L- or M-cone contrasts (which are the same for a monochromatic light) of the 0.5-Hz sinusoidal stimulus that matched the brightness of the contrast-modulated test stimulus at the peak of its 0.5-Hz contrast modulation plotted as a function of the overall modulation,  $m$ , of the contrast-modulated test hemi-field—both with linear scales. Data for DP are shown in the left-hand panel and those for GBH in the right-hand panel (note the change in scale on the ordinates for the two observers). The error bars indicate  $\pm$  one standard error. Extensive functions for three radiance levels, all in  $\log_{10}$  quanta  $s^{-1}deg^{-2}$ , are shown: 8.86 (dark green circles), 9.51 (light green diamonds), and 10.11 (yellow squares), but only two points could be measured at the lowest level of 8.26 (dark triangles).

[Insert Figure 6 about here]

With increasing modulation the brightness-matching data for DP become steeper at low modulations up to a modulation of about 0.3 but thereafter are roughly linear with modulation (except for the highest modulation at the 8.86 level), whereas those for GBH are roughly linear with modulation at low modulations but flatten slightly at modulations above about 0.7. Thus, there are qualitative differences between the functions for the two observers at low and high contrast modulations. Between 0.3 and 0.7 the shapes of the functions for the two observers are similar.

One notable feature of the functions for DP is that the brightness matches first increase as radiance increases from 8.26 to 9.51  $\log_{10}$  quanta  $s^{-1}deg^{-2}$  but then decrease; whereas for GBH they increase monotonically with radiance. Assuming small-signal linearity, the matching contrasts at a given radiance are effectively determined by the slope of the linear approximation to the nonlinearity at that radiance. Thus the increase in matching contrast from 8.26 to 9.51  $\log_{10}$  quanta  $s^{-1}deg^{-2}$  suggests an increasingly steep (accelerating) nonlinearity while the decrease for DP at 10.11  $\log_{10}$  quanta  $s^{-1}deg^{-2}$  suggests a flattening (“hardening”) of the nonlinearity at high radiances as in the case with S-cone isolating stimuli (Stockman & Plummer, 1998). No such flattening is indicated in the data of GBH. Another important feature of the functions for both subjects is that all the effects of mean target radiance can be approximately accounted for by a scaling factor. We will return to the potential significance of this scaling property in the next paper in this series (Stockman, Petrova, & Henning, submitted).

## Discussion

The contrasts of the matching stimuli are always less than about 43% for DP and less than 75% for GBH. The large contrasts, particularly for GBH, raise the concern that the 0.5-Hz sinusoidal matching stimulus may itself be distorted by the nonlinearity. However, the 0.5 Hz matching stimulus is substantially attenuated by the early filter, roughly indicated at the low-frequency end by the model fits in Figure 8. Thus, for the worst case ( $10.11 \log_{10}$  quanta  $s^{-1}deg^{-2}$  for GBH;  $9.51 \log_{10}$  quanta  $s^{-1}deg^{-2}$  for DP) the 0.5-Hz sinusoid at the input to the nonlinearity will be smaller by a factor of more than  $1.4 \log_{10}$  unit. Consequently the highest matching contrast at the input to the nonlinearity for GBH is about 3.0% and for DP, about 1.7% and most matching contrasts will be lower. These small contrasts at the input to the nonlinearity, together with the gap between flicker and brightness-change thresholds in Figure 2, suggest that, in the matching experiment, a linear approximation to the nonlinearity at each mean radiance is not unreasonable. Thus, there will be only an unknown scaling factor at each radiance that converts the input modulation,  $m$ , of the contrast-modulated waveform to the contrast of the distortion product at the output of the nonlinearity; i.e., at the input to the late filter. We therefore replaced the overall contrast of the contrast-modulated waveform (abscissae of the panels in Figure 4) by scaled values of the corresponding ordinates of the panels of Figure 6. The rescaled TCSFs for detecting the brightness change at  $f_m$  are plotted as the filled coloured symbols for the two observers in Figure 7. The shapes of the functions are correct, but they have been vertically shifted to align with the predictions from the model described below. These rescaled data constitute our estimates for the low-frequency end ( $f \leq 5$  Hz) of the post-nonlinearity (late) filter. The qualitative differences seen in between DP and GBH at low- and high-input modulations Figure 6 seem to have relatively little effect on the shapes of rescaled functions, except perhaps at the highest modulations where the rescaled functions for GBH are shallower at the two highest mean radiances.

[Insert Figure 7 about here]

The assumption of small-signal linearity is an approximation. If the matching stimuli are significantly distorted by an expansive nonlinearity—the form of the nonlinearity at low signal levels suggested by our analysis below—then we would be underestimating the size of the distortion product after the nonlinearity.

## GENERAL DISCUSSION

### *Combining the results at low and high frequencies*

From the brightness-change thresholds at  $f_m$  Hz, we were able to characterize the attenuation characteristics of the early filter above 5 Hz, and those of the late filter below 5 Hz. Given that both estimates depend upon a single type of threshold judgement, they can be reasonably assumed to depend on a single process. These estimates, therefore, represent our strong conclusions. They are highlighted by the coloured symbols in Figures 7 and 8.

To estimate the characteristics of the early filter below 5 Hz and the late filter above 5 Hz, where directly measured data could not be obtained, we assume that the shapes of the conventional TCSFs of Figure 3 reflect the multiplicative combination of the early and the late filters. Thus, the logarithmic differences between them and our early or late filter measurements should yield estimates of the shapes of the missing parts of each filter. Such estimates, however, depend on different types of threshold judgements, so that the assumption that they depend on a single process is less secure. Consequently, these estimates represent our weaker conclusions. They are indicated by the achromatic symbols in Figures 7 and 8.

A remaining question, then, is which of the monochromatic and chromatic TCSF estimates should be used to estimate the missing parts of the early and late filters? On the grounds that the contrast-modulated flicker used to generate the distortion product is monochromatic, and therefore subject to the same low-frequency attenuation, we assumed that the inferred shapes of the early filters below 5 Hz should be the logarithmic differences between the *monochromatic* TCSFs (open symbols, Figure 3) and the late filter estimates (coloured symbols, Figure 7). These estimates are shown as the open symbols in Figure 8, where they have been aligned with the direct estimates of the early filters (coloured symbols).

The choice of TCSFs for the derivation of the late filter above 5 Hz proved to be less straightforward. We initially supposed that the brightness variation is signalled by a luminance channel, which would be insensitive to chromatic flicker. Thus, the inferred shapes of the missing parts of the late filter should also be the logarithmic differences between the *monochromatic* TCSFs (open symbols, Figure 3) and the early filter estimates (coloured symbols, Figure 8). However, these differences, which are shown below in Figure 10, are complex and do not lend themselves to simple modelling or interpretation. In contrast, the logarithmic differences between the *chromatic* TCSFs (grey symbols, Figure 3) and the early filter estimates (coloured symbols, Figure 8) are consistent with a simple 2-stage lowpass filter. These differences are shown as the grey symbols in Figure 7,



where they have been aligned with the coloured symbols in each panel, to form the estimates of the late filters for each observer. As we discuss below, this simplicity lends weight to the hypothesis that brightness changes in these experiments are mediated by a pathway with temporal characteristics similar to chromatic pathways.

In simply differencing the conventional TCSFs, we ignore the effects of the nonlinearity intervening between the early and late filters. This seems a reasonable simplification near flicker threshold where small-signal linearity and the separation between the flicker and brightness-change fusion frequencies (see Figure 2) suggest that the nonlinearity plays little role.

[Insert Figure 8 about here]

In each panel of Figures 7 and 8, the filter estimates are plotted separately for DP (left-hand panels) and GBH (right-hand panels) for the four radiance levels ( $\log_{10}$  quanta  $s^{-1} \text{ deg}^{-2}$ ): 8.26 (triangles), 8.86 (circles), 9.51 (diamonds), and 10.11 (squares). The alignments of the measured and estimated filter characteristics below and above 5 Hz are not fixed by our data. To fix the alignments shown in Figures 7 and 8, we developed simple models of the early and late filters. These models not only help to align the data, but also yield insights into the underlying physiological mechanisms.

### **Modelling the early and late filters**

This models were developed in Petrova, Henning & Stockman (2013), where further details can be found. Briefly, we take the classic approach using filters composed of cascading leaky integrating stages (or buffered RC circuits) (see, Watson, 1986). The amplitude response,  $A(f)$ , of  $n$  cascaded, identical, leaky integrators is:

$$A(f) = (1/2\pi f_0)^n [(f/f_0)^2 + 1]^{-\frac{n}{2}}, \quad [4]$$

where  $f_0$  (Hz) is the “cut-off” or “corner frequency”. For more details, see Petrova et al. (2013), for which this model was first developed.

The early filter estimates (Figure 8) are clearly bandpass in shape. In this they are similar to the early filter of Wu *et al.* (1996). To account for the low-frequency attenuation, we divide a “centre” temporal response of a cascade of filters by a “surround” temporal response of another cascade of filters, thus:

$$A(f) = \tau_c^{n_c} [(f/f_{0c})^2 + 1]^{-\frac{n_c}{2}} / \tau_s^{n_s} [(f/f_{0s})^2 + 1]^{-\frac{n_s}{2}}, \quad [5]$$

where the subscript “*c*” refers to the parameters of the central cascade of filters, and the subscript “*s*” refers to the parameters of the surround cascade (e.g., Foley, 1994).

Fits were made using the logarithm of Equation [5] and the data. A scaling constant, *k*, that could vary with target radiance level was allowed. In terms of the model, *k* represents a frequency-independent sensitivity loss that is in addition to any losses resulting from the changing corner frequencies of the filters. In addition, an extra arbitrary constant, *v*, was added to the low-frequency data for each level, the value of which was individually optimized for each set of data to determine the best-fitting vertical alignment of the low- and high-frequency data, thus:

$$\log[A(f)] = \begin{cases} \log[A(f_{\text{low}})] + k + v, & \text{low frequency estimates} \\ \log[A(f_{\text{high}})] + k, & \text{high frequency estimates.} \end{cases} \quad [6]$$

Best-fitting versions of the model were obtained using a standard non-linear, least-squares curve-fitting algorithm (implemented in SigmaPlot, SPSS) to account for the data obtained for each observer at each of the four time-averaged radiances. Equations [5] and [6] were fitted simultaneously to the estimates of the functions for both DP and GBH. The model was simplified by fixing those parameters that did not vary systematically with target radiances or across observers. Our aim was to derive a plausible, descriptive model with as few parameters as could reasonably account for the totality of the data.

Implicit in the use of Equation [5] is the simplification that at any target radiance the cut-off frequencies of all centre stages ( $f_{oc}$ ) and all surround stages ( $f_{os}$ ) are the same. The number of stages in both centre and surround ( $n_c$  and  $n_s$ ) were allowed to take on non-integer values in preliminary fits, but in the final fits we fixed them at the nearest integer values ( $n_c = 8$  and  $n_s = 2$ .) A further simplification that could be made was that the surround corner frequency,  $f_{os}$ , was fixed across levels. Both scaling (the vertical logarithmic shift, *k*) and the centre cut-off frequencies were allowed to vary between observers and between levels.

[Insert Figure 9 about here]

The results of the final fit of the model for the early filters are shown in Figure 8 as the continuous dark lines. The parameters from the fit are tabulated in Table 1, and plotted in the left-hand panels of Figure 9. The values of *v*, which are not experimentally constrained, are not given. These values are largely arbitrary because they depend on the relative sensitivities of the low- and high- frequency filter estimates, one of which was measured directly (and in the case of the late filter rescaled) and the other of which was obtained indirectly by logarithmically differencing other sensitivities measured in different units (achromatic versus chromatic modulation). The upper left-hand panel of Figure 9 shows the corner frequencies (linear) for the “centre” cascade for DP (yellow

squares) and GBH (filled squares) plotted as a function of target radiance (logarithmic) The grey symbols show the common corner frequency for the “surround” cascade that does not depend on radiance. The lower panel shows the scaling (or log sensitivity) losses for DP (yellow circles) and GBH (filled circles) that were required in addition to the losses caused by changes to the corner frequency. Overall, the model accounts for the data well with an  $R^2$  value of 0.986. The corner frequencies and sensitivity losses are slightly larger for DP than for GBH.

**Table 1**

Parameter	DP	GBH
$n_c$ (fixed)	8	
$n_s$ (fixed)	2	
$f_{0s}$ (fixed)	1.31±0.08	
$f_{0c}$ 8.26	19.80±0.70	15.52±0.56
$f_{0c}$ 8.86	22.81±0.77	18.12±0.55
$f_{0c}$ 9.51	25.95±0.95	20.98±0.62
$f_{0c}$ 10.11	23.25±0.80	22.01±0.66
$k$ 8.26	0.00±0.09	0.00±0.09
$k$ 8.86	0.25±0.09	0.07±0.07
$k$ 9.51	0.60±0.10	0.30±0.07
$k$ 10.11	1.53±0.09	0.71±0.07
$R^2$	0.986	

The late filter for both observers (solid red lines, Figure 7) is broadly consistent with the simple low-pass filter of Equation [4]. We fitted this equation simultaneously to the estimates of the functions for both DP and GBH. Again, the model was simplified by fixing parameters that did not systematically vary across either target radiances or observers. In preliminary estimates, we found that we could fix the cut-off frequencies across radiance levels. We also allowed the number of

stages to take on non-integer values, but in the final fit constrained them to the nearest integer values of  $n = 2$ . Again, an additional alignment constant,  $v$ , was added to the low-frequency data of each set and individually optimized to determine the best-fitting vertical alignment of the low- and high-frequency (see Equation [6]).

The parameters from the final fit are tabulated in Table 2, and plotted in the right-hand panels of Figure 9. The upper panel shows the fixed corner frequencies (linear ordinate) for DP (yellow squares) and GBH (filled squares) plotted as a function of target radiance (logarithmic), the lower panel shows the scaling or sensitivity losses for DP (yellow circles) and GBH (filled circles). As indicated by the red line with a slope of 1, the increases in the sensitivity losses with target radiance are consistent with Weber's Law.

Overall, the model accounts for the data well with an  $R^2$  value of 0.988.

**Table 2**

Parameter	DP	GBH
$n$ (fixed)	2	
$f_0$ (fixed)	3.19±0.33	3.39±0.34
$s_{8.26}$	0.00±0.07	0.00±0.07
$s_{8.86}$	0.52±0.07	0.62±0.07
$s_{9.51}$	1.17±0.07	1.23±0.07
$s_{10.11}$	1.95±0.07	1.83±0.07
$R^2$	0.988	

### ***Related psychophysical measurements***

Our estimates of the form of the early filter can be usefully compared with the previous estimate of Wu *et al.* (1996). Both estimates depend on the nonlinear distortion that produces brightness enhancement, but there are some differences in methodology. First, Wu *et al.* measured the magnitude of brightness enhancement by supra-threshold matching, whereas we measured its threshold. Second, they used flicker of 594 nm, which would have generated a small hue change as

well as a change in brightness (see above), whereas we used flicker of 560 nm. Third, their mean luminance of  $4.25 \log_{10}$  photopic td was higher than our highest mean luminance of  $4.01 \log_{10}$  photopic td ( $10.11 \log_{10}$  quanta  $s^{-1} \text{deg}^{-2}$ ). They obtained data from three observers. Their mean data, like ours, are bandpass in form, but their estimate has a broader peak. The differences may be due to the differences in method.

### ***Site of the nonlinearity***

Previous work on the distortion of high-spatial frequency gratings and of types of flicker has suggested that the relevant nonlinearities are at an early level of the visual system, perhaps close to the photoreceptors (MacLeod et al., 1992; Stockman & Plummer, 1998; Wu et al., 1996). Yet, even for unresolvable gratings produced by laser interference, the nonlinearity seems to follow an earlier stage of surround antagonism (Chen et al., 1993), which places the nonlinearity at least after, or coincident with, horizontal cell feedback. Our estimates of the early filter shape from the brightness enhancement of 560-nm flicker (Figure 8) show a substantial loss of low-frequency sensitivity, which suggests that this nonlinearity also follows a stage of surround antagonism. Comparable results obtained with 650-nm flicker, the distortion of which is seen as a hue change, show similar effects (Petrova et al., 2013). We conclude that the expansive nonlinearity that enhances brightness is acting on L- and M-cone signals that have been shaped in some way by opponency.

But in which postreceptoral pathway is the brightness enhancement most likely to occur? Is the nonlinearity within the achromatic or luminance *flicker* pathway sensitive to higher temporal frequencies that is often linked to the magnocellular stream of retinal processing? Or is it within the achromatic or luminance pathway sensitive to higher spatial frequencies and linked to the parvocellular stream of processing, which also encodes chromatic information. The dual nature of the luminance pathway has been discussed in several papers by Ingling & his co-workers (Ingling & Drum, 1973; Ingling & Martinez-Uriegas, 1983, 1985; Ingling & Martinez, 1983; Ingling & Tsou, 1988), and has also been covered in several reviews (e.g., Lennie, Pokorny, & Smith, 1993; Stockman & Brainard, 2009).

We initially supposed that brightness enhancement occurs within the luminance *flicker* pathway. Consequently, the TCSFs shown in Figure 3 for brightness enhancement and those for detecting monochromatic flicker [which at threshold should be mediated mainly by the luminance pathway (see Lennie et al., 1993)] should be measures of the temporal properties of stages within a common pathway. On the assumption that the brightness-enhancement TCSFs correspond to the shapes of the early filter, while the monochromatic TCSFs correspond to the shapes of the combined early and

late filters (see above), the logarithmic differences between them should produce a plausible estimate of the shape of late filter. Those differences are shown as open symbols in Figure 10 for DP (left-hand panel) and GBH (right-hand panel) where they have been vertically aligned with the other data near 2.5 Hz. Rather than being simple, the differences are complex: the estimates for DP, in particular, show clear evidence for a secondary peak near 15 Hz. If the inferred late filter is consistent with a cascade of low-pass filters, then its high-frequency logarithmic slope should decline with an integer logarithmic slope. Yet, the estimates for DP have a best-fitting linear slope across all four levels of -0.68 (black lines), and those for GBH have a slope of -0.50 (black lines).

[Insert Figure 10 about here]

In contrast to the estimates based on the monochromatic TCSFs, those based on the *chromatic* TCSFs (which at threshold should be mediated mainly by the chromatic pathway, see above) fall off with a logarithmic slope of -2 (red lines, Figure 10), and are thus consistent with the simple interpretation that the late stage is a 2-stage low-pass filter. This simplicity, and the finding that a nearly identical 2-stage filter can also account for the late filter estimated using *chromatic* distortion (Petrova et al., 2013), suggests that the brightness signal after the nonlinearity is transmitted principally through a pathway that combines brightness and chromatic information.

We conclude that the brightness enhancement of flicker is produced by distortion in pathways that can also carry chromatic signals. This is consistent with the double-duty of the parvocellular pathway, which is both chromatically-opponent and spatially-opponent. Thus, it can encode chromatic information, which is dependent upon the difference between the spectral sensitivities of the centre and surround, and it can also encode “achromatic” information, which is dependent on the sum of the centre and surround spectral sensitivities. For colour, the centre and surround behave synergistically to produce a low-pass response to spatial variations in chromaticity, but for luminance they behave antagonistically to produce a more band-pass response to spatial variations in luminance (Ingling & Martinez-Uriegas, 1983, 1985; Ingling & Martinez, 1983). Thus, it is reasonable to assume that the parvocellular stream carries luminance and/or brightness information as well as colour information (e.g., Ingling & Drum, 1973; Ingling & Martinez-Uriegas, 1985; Ingling & Martinez, 1983; Ingling & Tsou, 1988; Kelly, 1983; Lennie & D’Zmura, 1988; Merigan & Eskin, 1986; Schiller, Logothetis, & Charles, 1990). Simple mechanisms for decoding the luminance and chromatic signals from multiplexed signals have been proposed that difference or sum centre-surround chromatically-opponent neurons (e.g., Billock, 1991; Kingdom & Mullen, 1995; Lennie, 1984; Lennie & D’Zmura, 1988; Martinez-Uriegas, 1985). See Stockman & Brainard (2009) for a recent discussion. Note that our results are consistent with the behaviour of a single process with a characteristic early

and a late filter. We do not need to invoke multiple brightness components to explain the data (e.g., Drum, 1984).

It is possible that at carrier frequencies low enough for individual flicker cycles to be resolved, subjects base their responses partly on the appearance of the peaks of the flicker rather than on the distortion signal varying at  $f_m$  Hz. Although still an inherently nonlinear process, the effective nonlinearity is likely to be at a very different stage of the processing stream than the one that produces brightness enhancement at  $f_m$ . This complication may be one of the reasons why reliable brightness threshold settings cannot be made at  $f_c < 5$  Hz.

The idea that brightness and chromatic signals are perceptually related is central to the substantial literature developed from Hering's (1878, 1920) opponent-color theory in which perceptions of red and green, blue and yellow, and black and white are opposed (e.g., De Valois & De Valois, 1993; Guth, 1991; Guth & Lodge, 1973; Guth, Massof, & Benzscharwel, 1980; Hurvich & Jameson, 1955, 1956; Ingling & Tsou, 1977; Jameson & Hurvich, 1955, 1956; Krantz, 1975; Schrödinger, 1925).

### ***Characteristics of the nonlinearity***

We cannot determine the shape of the underlying nonlinearity precisely from our observations and data, but we can infer its general characteristics. From the subjective observations that contrast-modulated, sinusoidally-flickering 560-nm light appears brighter when the contrast modulation is high, we can infer that the primary nonlinearity is likely to be expansive. We can also use the data relating the output contrast after the nonlinearity to the input contrast before it (see Figure 6) to test the feasibility of different nonlinear forms. We generated a range of nonlinear forms and then used each one to generate predictions for the data of Figure 6 using MatLab and Simulink (MathSoft) for all calculations and to generate the Fourier transform of the input and output signals before and after the nonlinearity.

To generate the predictions, we started with a particular nonlinear input-output function, such as the example shown in the upper panel of Figure 11. This particular example has the form:

$$y = \begin{cases} 0.2x + 0.2x^2, & x < 4 \\ 4, & x \geq 4, \end{cases} \quad [7]$$

where  $x$  is the input to the nonlinearity and  $y$  is the output. The units are arbitrary. We assumed that as the time-averaged 560-nm target radiance increases, the DC (mean) input level (which we call the "offset") also rises, thus moving up the nonlinear input-output function. In the simulation, we varied the DC offset from 0.0 to 2.5, and at each level varied the modulation of the contrast-modulated input from 0 to 100%, where 100% was the maximum modulation possible at that DC level (for

example, at a DC level of 1, the minimum and maximum of the contrast-modulated input signal are 0 and 2, respectively). At each combination of DC level and modulation, we calculated the contrast of the distortion product at  $f_m$ ; that is, the ratio of the amplitude of the distortion product at  $f_m$  to the total DC *after* the nonlinearity. The simulated contrast of the signal at  $f_m$  is plotted as a function of the DC offset and input modulation in the lower panel of Figure 11.

[Insert Figure 11 about here]

It is important to recognize that the nonlinearity in these simulations affects the contrast-modulated flicker by introducing the  $f_m$ -intermodulation distortion product in which we are interested, and, in addition, a steady-state (DC) term that changes the mean radiance around which the stimulus flickers. The *contrast* of the  $f_m$  distortion product, which we can reasonably assume determines its detectability, and is plotted in Figure 11, depends on both of these products. If the nonlinearity is expansive, the amplitude of the  $f_m$  term has a positive coefficient and the mean (DC) level is increased. The contrast and therefore the relative *detectability* of the  $f_m$ -component depend on the interplay between these components.

Any candidate nonlinearity must account for the features of Figure 6. The contrast of the distortion product must grow with input modulation and the functions must increase as the mean radiance increases from 8.26 to 9.51 log quanta  $s^{-1} \text{ deg}^{-2}$ . However, at the highest level, between 9.51 and 10.11 log quanta  $s^{-1} \text{ deg}^{-2}$ , the function describing the nonlinearity, certainly for DP, must get shallower again. We found that most of the tested nonlinear forms could account for some but not all features of the input contrast to output contrast functions. The simplest nonlinearity that could easily account for the functions (including the fall-off for DP) was one that was expansive at low input levels but that reached a ceiling at high levels (like the example shown in the upper panel of Figure 11.) The changes in the simulated modulation versus  $f_m$  contrast functions with DC offset in the lower panel of Figure 11 mirror the changes in the output contrast with input modulation in Figure 6. These similarities suggest that the nonlinearity of Figure 11 is a reasonable model of the underlying nonlinearity.

These simulations and modelling are largely descriptive, but they allow us to draw some general conclusions about the nonlinearity. In order to simulate the decrease in the input versus output contrast functions between the two highest levels for DP, we suggest that the nonlinearity must have an abrupt ceiling. We note that the inferred nonlinearity of Figure 11 relates only to the four 560-nm mean radiance levels from 8.26 to 10.11 log quanta  $s^{-1} \text{ deg}^{-2}$  used in the experiments. At lower levels, the nonlinearity may have a different form or may be missing. However, the critical-



fusion- frequency data of Figure 2 indicate that distortion can still be detected at 560-nm down to radiances as low as  $5.81 \log \text{ quanta s}^{-1} \text{ deg}^{-2}$ .

### **Conclusions**

A nonlinearity in the L-M chromatic pathway that causes a 560-nm light to look brighter when flickered has been used as an internal landmark at which to dissect the pathway into early (pre-nonlinearity) and late (post-nonlinearity) stages. The early temporal stage acts like a band-pass filter with sensitivity losses at higher temporal frequencies that are consistent with the nonlinearity occurring relatively early in the visual pathway. The losses at lower frequencies, however, suggest that the nonlinearity must be after the action of substantial surround antagonism.

Modelling suggests that the form of the nonlinearity is smoothly expansive perhaps with a hard saturating limit at high input levels. But what advantage is there in having such a prominent expansive nonlinearity in this pathway? One obvious advantage is that the nonlinearity will enhance time-varying signals at middle to high temporal frequencies after reciprocal von Kries adaptation (1905) at low temporal frequencies—probably at the photoreceptor level—has removed the mean (DC) signal (see for review and model Stockman, Langendörfer, Smithson, & Sharpe, 2006). Thus, the early gain control at the photoreceptor helps to keep the mean output within the dynamic range of the later neural circuits, while the expansive nonlinearity enhances the remaining signals. Note that we minimize the effect of photoreceptor adaptation in our experiments by maintaining a constant time-averaged level about which stimuli are modulated.

The late stage acts like a simple two-stage low-pass filter with cut-off frequencies around 3 Hz. The purpose of this filter may be to extract a slowly changing, mean brightness signal from the input signal.

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### **REFERENCES**

Ball, R.J. (1964). An investigation of chromatic brightness enhancement tendencies. *American Journal of Optometry and Physiological Optics*, 41, 333-361.

- Ball, R.J., & Bartley, S.H. (1966). Changes in brightness index, saturation and hue produced by luminance-wavelength-temporal interactions. *Journal of the Optical Society of America*, 66, 695-699.
- Ball, R.J., & Bartley, S.H. (1971). Several aspects of visual perception. *Journal of the American Optometric Association*, 42, 649-652.
- Bartley, S.H. (1938). A central mechanism in brightness enhancement. *Proceedings of the Society for Experimental Biology and Medicine*, 38, 535-536.
- Bartley, S.H. (1939). Some effects of intermittent photic stimulation. *Journal of Experimental Psychology*, 25, 462-480.
- Bartley, S.H. (1951a). Brightness comparisons when one eye is stimulated intermittently and the other steadily. *Journal of Psychology*, 34, 165-167.
- Bartley, S.H. (1951b). Brightness enhancement in relation to target intensity. *Journal of Psychology*, 32, 57-62.
- Bartley, S.H., & Nelson, T.M. (1960). Certain chromatic and brightness changes associated with rate of intermittency of photic stimulation. *Journal of Psychology*, 50, 323-332.
- Bedrosian, E., & Rice, S. O. (1971). The output properties of Volterra systems (nonlinear systems with memory) driven by harmonic and Gaussian inputs. *Proceedings of the IEEE*, 59, 1688-1707.
- Billock, V.A. (1991). The relationship between simple and double opponent cells *Vision Research*, 31, 33-42.
- Bleck, F. C., & Craig, E. A. (1965). Brightness enhancement and hue II. Hue shift as a function of steady and intermittent photic stimulation. *Journal of Psychology*, 59, 251-258.
- Brewster, D. (1838). On the influence of succession of light upon the retina. *Philosophical Magazine*, 4, 241.
- Brücke, E. (1848). Über die Nutzeffect intermitterender Netzhautreizungen. *Sitzungsberichte der Mathematisch-Naturwissenschaftlichen Classe der Kaiserlichen Akademie der Wissenschaften*, 49, 128-153.
- Burns, S.A., Elsner, A.E., & Kreitz, M.R. (1992). Analysis of nonlinearities in the flicker ERG. *Optometry and Vision Science*, 69, 95-105.
- Burton, G.J. (1973). Evidence for non-linear response processes in the human visual system from measurements on the thresholds of spatial beat frequencies. *Vision Research*, 13, 1211-1225.
- Chen, B., & Makous, W. (1990). Temporal modulation at high spatial frequencies. *Investigative Ophthalmology and Visual Science (supplement)*, 31, 428.

- Chen, B., Makous, W., & Williams, D.R. (1993). Serial spatial filters in vision. *Vision Research*, 33, 413-427.
- CIE. (2006). *Fundamental chromaticity diagram with physiological axes – Part 1. Technical Report 170-1*. Vienna: Central Bureau of the Commission Internationale de l'Éclairage.
- De Lange, H. (1958). Research into the dynamic nature of the human fovea-cortex systems with intermittent and modulated light. I. Attenuation characteristics with white and colored light. *Journal of the Optical Society of America*, 48, 777-784.
- De Valois, R.L., & De Valois, K.K. (1993). A multi-stage color model. *Vision Research*, 33, 1053-1065.
- Drum, B. (1984). Flicker and suprathreshold spatial summation: Evidence for a two-channel model of achromatic brightness. *Perception & Psychophysics*, 36, 245-250.
- Foley, J.M. (1994). Human luminance pattern-vision mechanisms: masking experiments require a new model. *Journal of the Optical Society of America A*, 11, 1710–1719.
- Green, D.G. (1969). Sinusoidal flicker characteristics of the colour-sensitive mechanisms of the eye. *Vision Research*, 9, 591-601.
- Guth, S.L. (1991). A model for color and light adaptation. *Journal of the Optical Society of America A*, 8, 976-993.
- Guth, S.L., & Lodge, H.R. (1973). Heterochromatic additivity, foveal spectral sensitivity, and a new color model. *Journal of the Optical Society of America*, 63, 450-462.
- Guth, S.L., Massof, R.W., & Benzschawel, T. (1980). Vector model for normal and dichromatic color vision. *Journal of the Optical Society of America*, 70, 197-212.
- Hering, E. (1878). *Zur Lehre vom Lichtsinne. Sechs Mittheilungen an die Kaiserliche Akademie der Wissenschaften in Wien*. Wien: Carl Gerold's Sohn.
- Hering, E. (1920). *Grundzüge der Lehre vom Lichtsinn*. Springer: Berlin.
- Hurvich, L.M., & Jameson, D. (1955). Some quantitative aspects of an opponent-colors theory. II. Brightness, saturation, and hue in normal and dichromatic vision. *Journal of the Optical Society of America*, 45, 602-616.
- Hurvich, L.M., & Jameson, D. (1956). Some quantitative aspects of an opponent-colors theory. IV. A psychological color specification system. *Journal of the Optical Society of America*, 46, 1075-1089.
- Ingling, C.R., Jr., & Drum, B.A. (1973). Retinal receptive fields: correlations between psychophysics and electrophysiology. *Vision Research*, 13, 1151-1163.
- Ingling, C.R., Jr., & Martinez-Uriegas, E. (1983). The relationship between spectral sensitivity and spatial sensitivity for the primate r-g X-channel. *Vision Research*, 23, 1495-1500.

- Ingling, C.R., Jr., & Martinez-Uriegas, E. (1985). The spatiotemporal properties of the r-g X-cell channel. *Vision Research*, 25, 33-38.
- Ingling, C.R., Jr., & Martinez, E. (1983). The spatio-chromatic signal of the r-g channels. In J. D. Mollon & L. T. Sharpe (Eds.), *Colour Vision: Physiology and Psychophysics* (pp. 433-444). London: Academic Press.
- Ingling, C.R., Jr., & Tsou, H.B.-P. (1977). Orthogonal combination of the three visual visual channels. *Vision Research*, 17, 1075-1082.
- Ingling, C.R., Jr., & Tsou, H.B.-P. (1988). Spectral sensitivity for flicker and acuity criteria. *Journal of the Optical Society of America A*, 5, 1374-1378.
- Jameson, D., & Hurvich, L.M. (1955). Some quantitative aspects of an opponent-colors theory. I. Chromatic responses and spectral saturation. *Journal of the Optical Society of America*, 45, 546-552.
- Jameson, D., & Hurvich, L.M. (1956). Some quantitative aspects of an opponent-colors theory. III. Changes in brightness, saturation, and hue with chromatic adaptation. *Journal of the Optical Society of America*, 46, 405-415.
- Kelly, D.H. (1961). Visual responses to time-dependent stimuli I. Amplitude sensitivity measurements. *Journal of the Optical Society of America*, 51, 422-429.
- Kelly, D.H. (1973). Lateral inhibition in human colour mechanisms. *Journal of Physiology*, 228, 55-72.
- Kelly, D.H. (1975). Luminous and chromatic flickering patterns have opposite effects. *Science*, 371-372.
- Kelly, D.H. (1983). Spatiotemporal variation of chromatic and achromatic contrast thresholds. *Journal of the Optical Society of America*, 73, 742-750.
- Kelly, D.H., & van Norren, D. (1977). Two-band model of heterochromatic flicker. *Journal of the Optical Society of America*, 67, 1081-1091.
- Kingdom, F.A.A., & Mullen, K.T. (1995). Separating colour and luminance information in the visual system. *Spatial Vision*, 9, 191-219.
- Krantz, D.H. (1975). Color measurement and color theory: II Opponent-colors theory. *Journal of Mathematical Psychology*, 12, 304-327.
- Lennie, P. (1984). Recent developments in the physiology of color vision. *Trends in Neurosciences*, 7, 243-248.
- Lennie, P., & D'Zmura, M. (1988). Mechanisms of color vision. *CRC Critical Reviews in Neurobiology*, 3, 333-400.
- Lennie, P., Pokorny, J., & Smith, V.C. (1993). Luminance. *Journal of the Optical Society of America A*, 10, 1283-1293.

- MacLeod, D.I.A., Williams, D.R., & Makous, W. (1992). A visual nonlinearity fed by single cones. *Vision Research*, 32, 347-363.
- Marmarelis, P.Z., & Marmarelis, V.Z. (1978). *Analysis of Physiological Systems: the white-noise approach*. New York: Plenum Press.
- Martinez-Uriegas, E. (1985). A solution to the color-luminance ambiguity in the spatiotemporal signal of primate X cells. *Investigative Ophthalmology and Visual Science (supplement)*, 26, 183.
- Merigan, W.H., & Eskin, T.A. (1986). Spatio-temporal vision of macaques with severe loss of Pb retinal ganglion cells. *Vision Research*, 26, 1751-1761.
- Petrova, D., Henning, G. B., & Stockman, A. (2013). The temporal characteristics of the early and late stages of the visual pathways that signal colour. *Journal of Vision*, in press.
- Plateau, J. (1835). Sur un principe de photométrie. *Bulletins de l'Académie royale des sciences et belles-lettres de Bruxelles*, 2, 52-59.
- Schiller, P., Logothetis, N. K., & Charles, E. R. (1990). Functions of the colour-opponent and broad-band channels of the visual system. *Nature*, 343, 68-70.
- Schrödinger, E. (1925). Über das Verhältnis der Vierfarben zur Dreifarben-theorie. *Sitzungsberichte. Abt. 2a, Mathematik, Astronomie, Physik, Meteorologie und Mechanik. Akademie der Wissenschaften in Wien, Mathematisch-Naturwissenschaftliche Klasse*, 134, 471.
- Sharpe, L.T., Stockman, A., Jagla, W., & Jägle, H. (2005). A luminous efficiency function,  $V^*(\lambda)$ , for daylight adaptation. *Journal of Vision*, 5, 948-968.
- Sharpe, L.T., Stockman, A., Jagla, W., & Jägle, H. (2011). A luminous efficiency function,  $V^*(\lambda)$ , for daylight adaptation: a correction. *Color Research & Application*, 36, 42-46.
- Spekreijse, H., & Reits, D. (1982). Sequential analysis of the visual evoked potential system in man; nonlinear analysis of a sandwich system. *Annals New York Academy of Sciences*, 388, 72-97.
- Stewart, G.N. (1887). Is the law of Talbot true for very rapidly intermittent light? *Proceedings of the Royal Society of Edinburgh*, 15, 441-464.
- Stockman, A., & Brainard, D. H. (2009). Color vision mechanisms. In M. Bass, C. DeCusatis, J. Enoch, V. Lakshminarayanan, G. Li, C. Macdonald, V. Mahajan & E. van Stryland (Eds.), *The Optical Society of America Handbook of Optics, 3rd edition, Volume III: Vision and Vision Optics* (pp. 11.11-11.104). New York: McGraw Hill.
- Stockman, A., Langendörfer, M., Smithson, H.E., & Sharpe, L.T. (2006). Human cone light adaptation: from behavioral measurements to molecular mechanisms. *Journal of Vision*, 6, 1194-1213.
- Stockman, A., & MacLeod, D.I.A. (1986). Visible beats from invisible flickering lights: Evidence that blue-sensitive cones respond to rapid flicker. *Investigative Ophthalmology and Visual Science (supplement)*, 27, 71.

- Stockman, A., MacLeod, D.I.A., & Lebrun, S. (1993). Faster than the eye can see: blue cones respond to rapid flicker. *Journal of the Optical Society of America A*, *10*, 1396-1402.
- Stockman, A., Petrova, D., & Henning, G. B. (submitted). The L- and M-cone pathways signal colour and brightness in a common pathway? *submitted*.
- Stockman, A., & Plummer, D.J. (1998). Color from invisible flicker: a failure of the Talbot-Plateau law caused by an early "hard" saturating nonlinearity used to partition the human short-wave cone pathway. *Vision Research*, *38*, 3703-3728.
- Talbot, H.F. (1834). Experiments on light. *Philosophical Magazine Series 3*, *5*, 321-334.
- Trimble, J., & Phillips, G. (1978). Nonlinear analysis of the human visual evoked response. *Biological Cybernetics*, *30*, 55-61.
- van der Horst, G.J.C., & Muis, W. (1969). Hue shift and brightness enhancement of flickering light. *Vision Research*, *9*, 953-963.
- Varner, D., Jameson, D., & Hurvich, L.M. . ( 1984). Temporal sensitivities related to colour theory. *Journal of the Optical Society of America A*, *1*, 474-481.
- Victor, J.D., & Shapley, R. (1980). A method of nonlinear analysis in the frequency domain. *Biophysical Journal*, *29*, 458-483.
- Victor, J.D., Shapley, R.M., & Knight, B.W. (1977). Nonlinear analysis of retinal ganglion cells in the frequency domain. *Proceedings of the National Academy of Sciences of the United States of America*, *74*, 3068-3072.
- von Kries, J. (1905). Influence of adaptation on the effects produced by luminous stimuli. In D. L. MacAdam (Ed.), *Sources of Color Science (1970)* (pp. 120-1126). Cambridge, MA: MIT Press.
- Walters, J.W., & Harwerth, R.S. (1978). The mechanism of brightness enhancement. *18*, 777-779.
- Watson, A.B. (1986). Temporal sensitivity. In K. Boff, L. Kaufman & J. Thomas (Eds.), *Handbook of Perception and Human Performance* (Vol. 1, pp. 6-1-6-43). New York: Wiley.
- Wu, S., Burns, S.A., Reeves, A., & Elsner, A.E. (1996). Flicker brightness enhancements and nonlinearity. *Vision Research*, *36*, 1573-1583.

## FIGURE LEGENDS

### **Figure 1.**

The figure illustrates an example of an expansive nonlinearity (N) separating early (F1) and a late (F2) linear filters operating on a contrast-modulated sinusoidally flickering stimulus. (One modulation cycle of the stimulus is shown in panel S1.) The amplitude spectrum of the stimulus is

shown in panel C1. Amplitude spectra at successive stages are shown in panels C2-C4 and as corresponding time “waveforms” in panels S2-S4. The nonlinearity (N) introduces new components at harmonics and at sum and difference frequencies of the Fourier components of the stimulus. The colours of the icons above S1-S4 represent the approximate brightness and saturation changes that might be expected at the peaks and troughs of the contrast-modulated flicker. (The Fourier components are illustrative; they are not drawn to scale.) This figure can be compared with Figure 1 of Petrova, Henning & Stockman (2013), which illustrated the compressive case.

**Figure 2.** Critical fusion frequencies,  $f_c$ , for the carrier of a contrast-modulated flicker as a function of the time-averaged radiance ( $\log_{10}$  quanta  $s^{-1} \text{ deg}^{-2}$ ) of a 560-nm target. The sinusoidal flicker at  $f_c$  was 100% contrast-modulated at  $f_m = 0.5$  Hz and with the overall modulation fixed at 92%. The frequencies for detecting flicker at  $f_c$  are shown as white dotted circles and for detecting brightness change at  $f_m$  as green dotted diamonds. The frequency scale is linear. The error bars indicate  $\pm 1$  standard error of the mean (s.e.m.). The four downward pointing coloured triangles just above the abscissae indicate the four radiance levels used in Experiments I and II.

**Figure 3.** The  $\log_{10}$  modulation sensitivities for DP (left-hand column) and GBH (right-hand column) for detecting either monochromatic (equichromatic) (open symbols) or chromatic (equiluminant) (grey symbols) flicker at  $f_c$ , or for detecting the brightness enhancement at  $f_m$  (dark coloured symbols) all plotted as a function of  $f_c$  (logarithmic axis). Each row shows results for the different time-averaged radiances shown in the top corner of the panels in the right-hand column: 8.26- (inverted dark brown triangles), 8.86- (dark green circles), 9.51- (green diamonds) and 10.11- (light green squares)  $\log_{10}$  quanta  $s^{-1} \text{ deg}^{-2}$ . Unmodulated sinusoidal flicker at  $f_c$  was used for the monochromatic and chromatic flicker measurements. For the brightness-change measurements, the sinusoidal flicker at  $f_c$  was contrast-modulated at  $f_m = 0.5$  Hz Error bars indicate  $\pm 1$  s.e.m. The chromatic flicker was made up of luminance-equated 560-nm and 650-nm targets flickering in opposite phase. At each level, the overall time-averaged luminance of the combined 560- and 650-nm lights was set to be the same as the time-averaged luminance of the 560-nm targets used in the monochromatic measurements using the Sharpe *et al.* luminous efficiency estimates (Sharpe *et al.*, 2005, 2011). (At the 10.11  $\log_{10}$  quanta  $s^{-1} \text{ deg}^{-2}$  level we had to use a 630-nm target to cancel 560-nm flicker because the brightest 650-nm target was too dim.) In increasing order of the radiance of the 560-nm target for the three lowest radiances, the 650-nm equiluminant quantal radiances were 1.16, 1.22, and 1.37 more than the 560-nm radiances for DP and 0.98, 0.98, and 1.08 more for GBH.

At the highest radiance of the 560-nm target, the 630-nm equiluminant quantal radiances were 0.74 more than the 560-nm radiance for DP and 0.65 more for GBH. The modulations for the chromatic flicker are those of 560-nm component (or 650-nm component) alone.

**Figure 4.** The  $\log_{10}$  modulation sensitivities for DP (upper panel) and GBH (lower panel) for detecting brightness change at  $f_m$  as a function of the contrast modulation frequency,  $f_m$  (logarithmic axis) at four time-averaged target radiances: 8.26- (inverted dark triangles), 8.86- (dark green circles), 9.51- (green diamonds) and 10.11- (light green squares)  $\log_{10}$  quanta  $s^{-1} \text{ deg}^{-2}$ . The sinusoidal flicker at  $f_c = 30$  Hz was contrast-modulated at  $f_m$  Hz. Error bars indicate  $\pm 1$  s.e.m.

**Figure 5.** The arrangement used to match the brightness change and desaturation of a 560-nm contrast-modulated flicker (left hemi-field and left stimulus) by varying the time-averaged radiance and amplitude of 92% modulated 560-nm sinusoidal stimuli superimposed on a 560-nm pedestal of the same time-averaged radiance as the contrast-modulated target (right hemi-field and right stimuli). The small discs at the bottom of the figure indicate the approximate appearances of the hemi-fields when the matching contrast-modulation (left) and sinusoidal flicker amplitude (right) are at their minima and maxima.

**Figure 6.** Both panels show L or M-cone contrasts of the 0.5-Hz sinusoidally flickering hemi-field that matches the appearance of 0.5-Hz contrast-modulated 30-Hz flicker in an adjacent hemi-field as a function of the overall modulation ( $m$ ) of the contrast-modulated stimuli (both axes linear). The left-hand panel shows matches for DP and the right-hand panel, for GBH. The time-averaged radiances were: 8.26- (inverted dark triangles), 8.86- (dark green circles), 9.51- (light green diamonds) and 10.11- (yellow squares)  $\log_{10}$  quanta  $s^{-1} \text{ deg}^{-2}$ . Error bars indicate  $\pm 1$  s.e.m. (Only two points could be measured at the 8.26 radiance level.)

**Figure 7.** Estimates of the logarithmic sensitivities corresponding to the attenuation characteristics of the late filter for DP (left-hand panel) and GBH (right-hand panel) at each of the four time-averaged radiance levels of 8.26- (inverted triangles), 8.86- (circles), 9.51- (diamonds) and 10.11- (squares)  $\log_{10}$  quanta  $s^{-1} \text{ deg}^{-2}$ . The frequency axis is logarithmic. Error bars indicate  $\pm 1$  s.e.m. The coloured symbols show the logarithmic sensitivities for detecting the brightness change at  $f_m$  as a function of  $f_m$  (from Figure 5 rescaled according to the input versus output contrast functions shown



in Figure 6). Each set of data has been vertically aligned so that it has the same maximum amplitude sensitivity in  $\log_{10}$  quanta  $s^{-1} \text{ deg}^{-2}$  before and after rescaling. The grey symbols are the sensitivity differences between the early filter estimates (coloured symbols, Figure 4) and the chromatic TCSF measurements (grey symbols, Figure 4). The alignment of the grey symbols with the coloured ones was determined by the fit of a 2-stage low-pass filter model (red lines), the details of which are described in the text. Error bars indicate  $\pm 1$  s.e.m.

**Figure 8.** Estimates of the logarithmic sensitivities corresponding to the attenuation characteristics of the early filter for DP (left-hand panel) and GBH (right-hand panel) at each of the four time-averaged radiance levels of 8.26- (inverted triangles), 8.86- (circles), 9.51- (diamonds) and 10.11- (squares)  $\log_{10}$  quanta  $s^{-1} \text{ deg}^{-2}$ . The frequency axis is logarithmic. Error bars indicate  $\pm 1$  s.e.m. The coloured symbols are the logarithmic sensitivities for detecting the brightness change at 0.5 Hz as a function of  $f_c$  from Figure 4 (also shown there as coloured symbols). The sensitivities are the logarithmic amplitude sensitivities in  $\log_{10}$  quanta  $s^{-1} \text{ deg}^{-2}$ . The open symbols are the sensitivity differences between the late filter estimates (coloured symbols, Figure 7) and the monochromatic TCSF measurements (open symbols, Figure 4). The alignment of the open symbols with the coloured ones was determined by the fit of a model (black lines), the details of which are described in the text. Error bars indicate  $\pm 1$  s.e.m.

**Figure 9.** Fitting parameters of the models describing filter characteristics: early filter (left panels) and late filter (right panels). The upper left-hand panel shows the corner frequencies of the “center” cascade for DP (yellow squares) and GBH (black squares) and the lower panel the Log scaling or sensitivity losses for DP (yellow circles) and GBH (black circles) that were required in addition to the effects of changes in corner frequency all as a function of  $\log_{10}$  radiance. The grey diamonds in the upper panel show the common corner frequency for the “surround” cascade for both observers; it does not depend on radiance. The upper right-hand panel shows the corner frequencies for the 2-stage late filter; the lower panel the log scaling parameters: yellow squares (DP), dark green squares (GBH) both as a function of radiance. The red line in the bottom panel indicates the prediction of Weber’s Law. Overall, for both observers, the model accounts for the data well with an  $R^2$  value of 0.989.

**Figure 10.** Estimates of the late filter (coloured symbols) and the model fits (red lines) for DP (left-hand panel) and GBH (right-hand panel) replotted from Figure 7. The open symbols in each panel

show the differences between the early filter estimates at higher frequencies (coloured symbols, Figure 8) and the monochromatic TCSFs (open symbols, Figure 3). The open symbols have been fitted by a line with a best-fitting slope across all four levels of  $-0.68$  for DP and  $-0.50$  for GBH (black lines), and the lines and data have been vertically shifted together so that the lines align with the chromatic curves at  $2.5$  Hz. Error bars indicate  $\pm 1$  s.e.m. The vertical positions of the top set of data in each panel are the same as in Figure 8, but for clarity the second, third and fourth sets have been shifted downwards by an extra 1, 2 and 3  $\log_{10}$  units, respectively.

**Figure 11.** Effect of the clipped expansive nonlinearity illustrated in the upper panel on the contrast of the distortion product at  $f_m$ . The upper panel shows the input/output function of Equation [7] and the lower panel the contrast of the distortion product at  $f_m$  resulting from a contrast-modulated input with the input modulations and DC offsets shown. For details, see text.

## TABLE LEGENDS

**Table 1.** Best-fitting parameters for the model of the early filter. See text for details.

**Table 2.** Best-fitting parameters for the model of the late filter. See text for details.