

# Is Positive Sentiment missing in Corporate Reputation?

Peter Mitic<sup>1</sup> <sup>a</sup>

<sup>1</sup>Department of Computer Science, UCL, London, England  
p.mitic@ucl.ac.uk

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**Abstract:** The value of a perceived negative bias is quantified in the context of corporate reputation time series, derived by exhaustive data mining and automated natural language processing. Two methods of analysis are proposed: State-Space using a Kalman filter time series with a Normal distribution profile, and Forward Filtering Backward Sampling for those without. Normality tests indicate that approximately 92% of corporate reputation time series do fit the Normal profile. The results indicate that observed positive reputation profiles should be boosted by approximately 4% to account for negative bias. Examination of the observed balance between negative and positive sentiment in reputation time series indicates dependence on the sentiment calculation method, and region. Positive sentiment predominates in the US, Japan and parts of Western Europe, but not in the UK or in Hong Kong/China.

## 1 INTRODUCTION

Measuring sentiment and opinion using *Natural Language Processing (NLP)* has been an established procedure since work on *Phase-Structure Grammar* in the 1950s (Chomsky, 1957). Translation of natural language sentences into a format that can be used by computers remains the basis of *NLP* today, including the recent *Large Language Models* (OpenAI, 2019). This paper concerns a particular aspect of the accuracy of sentiment measures, embedded in a much wider framework: *reputation*. That aspect is "missing positive sentiment", which is closely related to the idea of *negative bias*. Our proposition is that *negative bias* exists in the context of reports on corporate affairs, and is due to unexpressed positive content.

Written statements about particular organisations can be positive (as exemplified by words such as "good" or "improved"), or they can be negative (using words such as "poor" or "bad"). The underlying idea of this paper is the possibility that there is a proportion of positive statement that is not expressed, possibly because of a lack of emotion associated with positivity. The analysis presented aims to detect and quantify the extent of unexpressed content. In doing so, the overall balance between positive and negative sentiment is noted.


### 1.1 Structure of this paper

The paper is divided into the following sections.

1. This introduction, including a statement of the problem to be solved (Section 1).
2. An example of reputation, expressed as a time series (Section 1.2.1)
3. Related literature (Section 2)
4. Methods used (Section 3)
5. Results (Section 4)
6. Discussion and issues arising (Section 5)

The core of the *Methods* section is to first assess the positive/negative balance for reputation time series using observed reputation time series. Then, assuming that some positive sentiment is "missing", we attempt to measure its extent by using *State-Space* analyses. The purpose is to reveal an underlying relatively noise-free 'hidden' reputation time series, from which it is possible to estimate the missing positive component of that reputation. An alternative procedure which is more widely-applicable but is slower to calculate is proposed for validation of the result.

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<sup>a</sup>  <https://orcid.org/0000-0002-9845-4435>

## 1.2 Reputation and Sentiment: a brief overview

The analysis in this paper is heavily dependent on time series and statistical concepts, so it is important to formulate the term "reputation" in terms that fit the necessary paradigms. To do that, we separate the terms "reputation" and "sentiment". The latter is well-defined in the context of *NLP* (for example by (Liu, 2015)), but the former is a relatively new concept. Consequently, both are defined in a formal way in Section 3.1. Additionally, the term "opinion" is also defined.

Details of the reputation measurement process used to derive the data used in this study can be found in (Mitic, 2017). Compiling a daily reputation time series comprises the following stages, targeted upon a particular organisation,  $T$ .

1. Exhaustive data mining of textual records. Text is derived by setting up dedicated data feeds to both social and 'traditional' media sources. Examples of 'traditional' media include radio and TV news channels (e.g. BBC, Sky TV, Fox Media), newspapers (e.g. the Financial Times, Wall Street Journal), financial organisations (e.g. Bloomberg, Reuters), and consumer reviews (e.g. from Google, Amazon). Social media sources include  $X$  ("Twitter"), Facebook and WhatsApp.
2. *NLP* to derive sentiment per record.
3. Averaging sentiments received on each day, weighted by importance/significance. This is the 'observed' sentiment for day  $t$ , denoted by  $y_t$  in this paper).
4. Conditioning  $y_t$  to remove 'noise'.
5. Forming a time series  $\{y_t\}, t = 1, 2, \dots$ , which is the 'reputation' of  $T$

### 1.2.1 Reputation Examples

To crystallise the ideas of casting reputation as a time series, and to illustrate the essential characteristics of those time series, Figures 1, 2 and 3 show recent views of typical reputation profiles: *Lego*, *NASA* and *Singapore Airlines*. Each plot shows the sentiment score  $y_t$  on the vertical axis on a scale of -100 to +100, for each of 730 days on the horizontal axis. The horizontal line at  $y_t = 0$  sentiment indicates entirely neutral sentiment. The portions of the plot above that line indicate positivity (for example, for increased profits recorded on financial statements), whereas the portions of the plot below indicate negativity (for example, for negative customer experience). The plots in-

clude *Loess*-generated smoothed profiles, and *Loess*-generated trend curves.

Many reputation plots express mostly positive sentiment (illustrated by *Lego*) or mostly negative sentiment (illustrated by *NASA*). Plots that straddle the positive/negative border with a high frequency oscillation, similar to that of *Singapore Airlines*, are less common. Together, the three plots illustrate features typical of all reputation time series, listed below.

- A macro-structure of peaks and troughs, with little discernable periodic effect or length (in time) between successive peaks and troughs.
- Large upward or downward moves over short time periods. The *NASA* plot has several.
- Small day-to-day variation, representing 'noise'.
- Isolated 'shocks': extreme (usually negative) sentiment lasting one or two days, often due to multiple reports of the same adverse event. Several are shown on the *Lego* plot. Negative 'shocks' are more common than positive 'shocks'.
- Sentiment concentration principally within a broad range (-50,50). Very few instances of sentiment outside this range are encountered. This concentration is most likely due to averaging processes in *NLP* calculations.

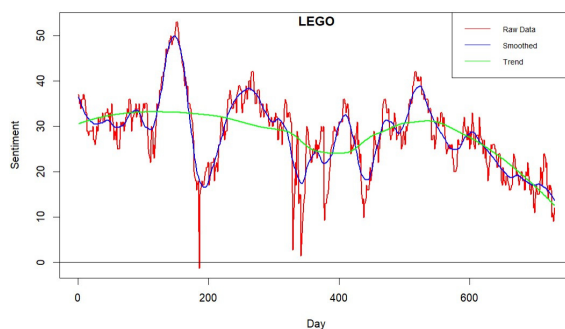


Figure 1: Lego (daily) reputation (in red) July 2021-June 2023. Blue line: smoothed sentiments; green line: trend. Data source: *Penta Group*.

## 2 RELATED WORK

In this review, we concentrate specifically on one particular aspect which is of relevance to our study. That is the excess of negative sentiment compared to positive sentiment in instances of daily accumulation and analysis of sentiment. Most research has concentrated on the detection and analysis of sentiment bias which we regard as a precursor for the existence of excess negative sentiment. For example, (Rozin and

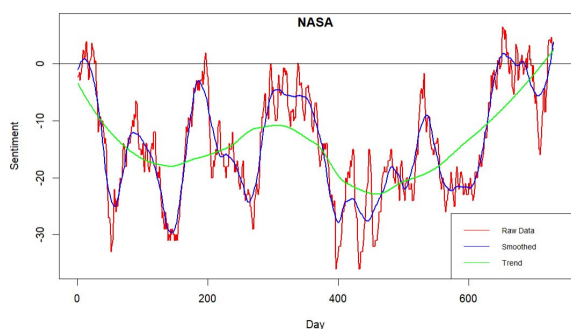


Figure 2: NASA (daily) reputation (in red) July 2021-June 2023. Blue line: smoothed sentiments; green line: trend. Data source: *Penta Group*.

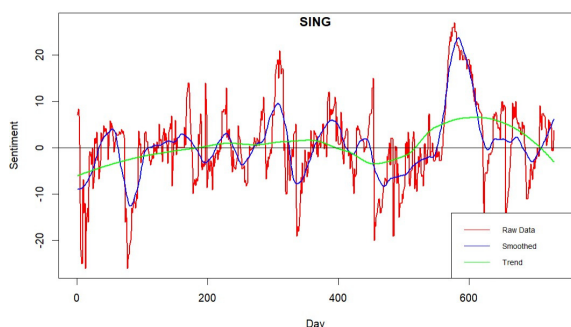


Figure 3: Singapore Airlines (daily) reputation (in red) July 2021-June 2023. Blue line: smoothed sentiments; green line: trend. Data source: *Penta Group*.

Royzman, 2001) offer a full discussion of sentiment bias, and initiated the term 'negative bias'. Here we consider research on the *value* of excess negative sentiment.

Direct evidence comes from (Zendesk, 2013) in a study of responses to customer service. They found that people are more likely to express negative experiences rather than positive. Consequently, there is an excess volume of negative sentiment. Specifically they report that 95% of users were likely to share a negative experience, as opposed to 87% percent for a positive experience. Some reasons for these findings are suggested. First, negative comments are driven by emotional responses, which last longer in the mind and appear more urgent than positive comments. Second, for the same reason, negative comments are given unprompted, whereas positive comments often have to be solicited. It is tentatively suggested that customers take more note of negative comments, and are more likely to post negatives in order to warn other customers.

(Finkelstein and Fishbach, 2012) suggest that a potential reason for an excess of negative feedback is that there is a difference in responses from novices

and experts. Novices seek and provide positive feedback in order to make decisions, whereas experts are more likely to provide negative feedback because positive sentiment is what they already know. Since there are fewer novices, negative feedback prevails.

The study by (Moe and Schweidel, 2012) (and summarised in (Moe and Schweidel, 2013)) indicates an excess of negative comments due to different behaviour modes for less active and more active people who posted online comments. They consider that online opinions are dominated by 'activists' who offer negative opinions, and skew sentiment negatively.

(Tsugawa and Ohsaki, 2017) investigated the relationship between message sentiment on social media and the volume and speed of message diffusion. They analysed 4.1 million tweets and their retweets, and found that the reposting volume of negative messages was 20–60% higher than that of positive and neutral messages. The result is reinforced by (Ferrara and Yang, 2015), who found that negative messages spread faster on social media than positive ones. However, positive messages reached larger audiences. Their dataset, which was not a random selection, comprised approximately 36% of positive tweets, 22% of negative tweets, with 42% neutral. The opposite effect is reported by (Stieglitz and Dang-Xuan, 2013), who found, in the context of tweets, no evidence of sentiment bias.

Two later studies investigated the incidence of positive and negative sentiment on social media. (Bellovary and Goldenberg, 2021) investigated the spread speed of online sentiment. Overall, negativity was about 15% more prevalent than positivity, and more users responded to negative tweets than did to positive tweets. This result is particularly insightful in the context of reputational analysis. A major (data-mined) source of reputational data is news reports, for which, the authors found, negativity is more frequent and more impactful than positivity. (Antypas and Camacho-Collados, 2023) reached a similar conclusion.

An example of intrinsic negative bias is (arguably) the *Net Promoter Score - NPS*<sup>1</sup> (Reichheld, 2003), which is a very simple scoring system based on subjective answers to a single question: *On a scale of 0-10, how likely are you to recommend this company to a friend or colleague?*. The NPS is then the difference between the percentage of 9-10 (promoter)

<sup>1</sup>Published by Bain and Co., <https://www.bain.com/>

scores and the percentage of 0-6 scores (detractors). Scores 7 and 8 are regarded as "passive". The numerical imbalance induces negative bias.

Overall, previous research indicates evidence of an excess of negative sentiment, particularly on social media. This result prompts us to consider whether or not some positive sentiment is "missing" from reputation time series. The main reason is the emotional response triggered preferentially by negative feelings, as surmised in (Zendesk, 2013). We present our own findings on this topic in section 4.1.

## 2.1 Positive Bias

Few indications of positive bias are available in the context of products or organisations. (Park and Rhim, 2018) studied online chat satisfaction surveys, and concluded that a majority of non-respondents were likely to be dissatisfied with the chat service. However, a majority of respondents had positive opinions. That result agrees with earlier work on Amazon Online product reviews by (Hu and Zhang, 2007). Reviews, expressed as "star ratings" were significantly more positive (4\* and 5\*) than negative (1\* and 2\*) for books, DVDs and videos.

Closely related to positive bias is the concept of *Confirmation bias*. (Powell and Holyoak, 2017) provide confirmation bias examples in which people preferred a product with more reviews to one with fewer reviews, even though their statistical model indicated that the latter was likely to be of higher quality than the former.

## 3 METHODS

A brief investigation of negative/positive sentiment balance is outlined. All of the following sub-sections deal with finding how "missing positive sentiment" might be quantified, assuming that it is present.

### 3.1 Definitions

In this section we give a brief definition of *Opinion*, *Sentiment* and *Reputation*. There are indications of the necessary definitions in, for example, (Loke and Vergeer, 2022) in phrases such as "collective view" and "built over time". The general idea of the scope of reputation is summarised in (Loke and Kisoen, 2022): "a summary of internal and external perceptions of an organisation". We argue that reputation should extend much further. Specifically, it should include broad-

casting, news reports, company statements and social media.

(Liu, 2015) defines *Opinion* as a function or algorithm  $\mathcal{F}$  of a comment  $X$  in text form, provided by a *Holder*  $H$ , aimed at a target organisation  $T$  with influence  $U \in (0, 1)$ , and given at a time  $t$  (nominally one day).  $\mathcal{F}$  maps  $X$  to a subset of the real numbers  $[-r, r]; r \in \mathbb{R}^+$ . This defines a numeric "score" for textual content. *Sentiment*,  $S$ , is a set of opinions expressed by  $n_h$  holders, in  $n_x$  texts, on the same target  $T$ , all at the same time, using a function  $\Psi$  which forms a weighted average of the opinion holders using their influences. The idea that *Sentiment* should refer to a set of *Opinions* is unusual, and differs from the view expressed in (Liu, 2015), where in the context of *NLP*, the distinction is not needed. *Reputation*,  $y_t(T)$ , is a time series of *Sentiments* over an extended time period of length  $\tau$ . For convenience, we omit the target  $T$  in the equations in Section 3.

#### Definition: *Opinion*

$$O_t(X, H, T, U) = \mathcal{F}(X | H, T, U) \in [-r, r] \quad (1)$$

#### Definition: *Sentiment*

$$S_t(T) = \Psi(\{O_t(X_i, H_j, T, U_j)\}); \\ i = 1..n_x; j = 1..n_h \quad (2)$$

#### Definition: *Reputation*

$$y_t(T) = \{S_t(T)\}; \quad t = 1..\tau \quad (3)$$

### 3.2 Negative/Positive sentiment analysis

We first undertake a simple analysis of the balance between positive and negative sentiment in reputation time series. Evidence from section 2 indicates that excess negative sentiment is prevalent in many contexts, predominantly in social media. For each reputation time series, the number of days on which positive, neutral and negative sentiment was recorded, were noted. In this context, three sentiment categories were designated as in equation 4. In practice, the results were insensitive to the 'neutral' limit 2. There was little variation in the results by extending the 'neutral' limit to 5.

$$\begin{cases} \text{Positive:} & y_t > 2; & t = 1..\tau \\ \text{Neutral:} & -2 \leq y_t \leq 2 & t = 1..\tau \\ \text{Negative:} & y_t < -2 & t = 1..\tau \end{cases} \quad (4)$$

The results are shown in section 4.1.

### 3.3 Negative bias analysis

We now surmise that excess negative sentiment does exist in reputational signals. To quantify it, for any given corporate organisation, we use *State-Space* analysis and the *Kalman filter* (Harvey, 1990) to extract the *state* ('hidden') signal. The *state* signal preserves the profile of the observed signal, but removes some of the noise. That extraction also defines a variance component. Together, the estimate of the *state* signal and its variance enable a high quantile of the estimated state to be calculated, and the difference between the high quantile and the observed signal is taken as the 'missing' signal. So if  $y_t$  represents the observed sentiment on day  $t$ ,  $x_t$  and  $P_t$  are the *state* sentiment mean and variance respectively, then the 'missing' sentiment on day  $t$ ,  $m_t$ , is given by the first part of equation 5. The value of  $z$  represents either 95% or 99% (2-tailed) confidence. A single figure measure of the 'missing positive sentiment',  $M_z$ , for the organisation is the mean of all values of  $m_t$  over a day range  $1 \dots \tau$ .

$$\begin{aligned} m_t &= x_t + z\sqrt{P_t} \\ M_z &= \overline{m_t} \quad 1 \leq t \leq \tau \end{aligned} \quad (5)$$

### 3.4 Data

Reputation data is sourced from *Penta Group* (<https://pentagroup.co>). Two data sets were extracted. The first was used for the "missing positive sentiment" analysis. We selected 261 corporate organisations representing the principal world industrial and service sectors: energy, manufacturing, travel, education, financial, media, food production, and retail. The data range was two years: from Q3 2021 to Q3 2023, a total of 730 days. The observed data is presented on a continuous scale from -100 (worst possible sentiment) to +100 (best possible sentiment). Zero (or very near to zero) represents neutral sentiment.

The second data set was used for the positive/negative sentiment balance analysis. Reputational time series for constituents of a range of major stock indices were sourced, together with 40 reputational time series for organisation that are non stock-exchange listed. The second selection is nearer to a random sample than is the first.

Full details of both data sets are given in Sections 4.1 and 4.2.

### 3.5 Assumptions

- Measurements of the observed data must be independent in order to estimate the values of  $x_t$  and  $P_t$

in the *Kalman filter* calculation (section 3.7). The method of data collection ensures independence, because components of the sentiment measure for day  $t$  originates on day  $t$  only. The reputation value therefore starts from zero on each day.

- The set of sentiments must be Normally distributed. This point is discussed in section 3.6. The non-normal case is discussed in section 3.8.

### 3.6 Gaussian data requirement

The histograms of the two-year reputation data for many organisations show that, informally, Normal distributions might apply. All reputation data series were tested for normality using the *TNA* test (Mitic, 2015), which is a generalisation of a  $Q-Q^2$  plot, and is insensitive to outliers, and to data set size. Applying the *TNA* test, the normality null hypothesis was rejected in only 19 cases. The remaining 19 could be 'normalised' by at least one of the following transformations.

- A log transformation, applied separately to positive and negative sentiment:  $y_t[y_t > 0] \rightarrow \log(y_t)$ ;  $y_t[y_t \leq 0] \rightarrow -\log(-y_t)$
- A square root transformation, applied separately to positive and negative sentiment:  $y_t[y_t > 0] \rightarrow \sqrt{y_t}$ ;  $y_t[y_t \leq 0] \rightarrow -\sqrt{-y_t}$
- A Box-Cox transformation, using the modification by (Yeo and Johnson, 2000), which can accommodate negative arguments. For positive  $\alpha$ ,  $\lambda$  is selected to 'normalise' by transforming  $y_t \rightarrow \frac{(y_t + \alpha)^{\lambda} - 1}{\lambda}$ ;  $\lambda \neq 0$  and  $y_t \rightarrow \log(y_t + \alpha)$ ;  $\lambda = 0$ .
- Removal of extreme outliers.

We use the *State-Space* method applied to unmodified reputation data as the primary means of estimating whether or not negative bias exists in the data. Data transformations, as described, can be used to generate normally distributed data, but may have contingent effects that are undesirable. In particular, proving that *State-Space* analysis applied to transformed data has precisely the same effect as for untransformed data needs much more analysis. In Section 3.8 a *Markov Chain Monte Carlo (MCMC)* method, applicable for non-normal data, is discussed. The *MCMC* and *State-Space* results are similar (Tables 4 and 5), but *State-Space* analysis is much faster. We are therefore content to apply a *State-Space* analysis to unmodified reputational data, and to use *MCMC* as a comparison.

<sup>2</sup>*Quantile-Quantile*: a plot of empirical quantiles against quantiles calculated using a theoretical distribution

### 3.7 State-space estimation: outline

The sequence of equations in this sub-section follows the exposition by (Shumway and Stoffer, 2016), as does the *R*-code to implement it. We start with a reputation time series  $\{y_t : 1 \leq t \leq \tau\}$  measured in days from 1 to  $\tau$ . These are 'noisy' observations of a 'hidden' signal, which is less noisy. We aim to determine a parallel series  $\{x_t\}$  which represents the *state* of the system: quantities that are not observed directly, but can only be inferred via the actual observation. The aim is to estimate an upper limit for the state vector  $x_t$  given the observations  $y_t$ , and to attribute the difference between that upper state limit and the corresponding observations as unobserved (or 'missing') positive sentiment.

We assume that  $x_t$  and  $y_t$  are related, in a general case, as in equation 6. In those equations,  $w_t$  and  $v_t$  are stochastic errors, and are functions of matrices  $Q$  and  $R$ , which describe the correlation structures of the stochastic error associated with  $x_t$  and  $y_t$  respectively.  $\Phi$  is the correlation matrix for vector  $x_t$ , and has to be estimated from observations. The matrix  $A_t$  is the *observation matrix* and represents a measurement scaling. The time dependency of  $A_t$  distinguishes a *State-Space* process from a conventional linear model. The vector  $u(t)$  is an exogenous vector, scaled by matrices  $\gamma$  and  $\Gamma$  in the two cases.

$$\begin{aligned} x_t &= \Phi x_{t-1} + \gamma u_t + w_t; & w_t &\sim N(0, Q); 1 \leq t \leq \tau \\ y_t &= A_t x_t + \Gamma u_t + v_t; & v_t &\sim N(0, R); 1 \leq t \leq \tau \end{aligned} \quad (6)$$

The *State-Space* exposition in (Shumway and Stoffer, 2016) describes the development of estimators  $\hat{x}_t$  of the  $x_t$ , with corresponding variance estimators  $\hat{P}_t$  via the *Kalman filter*. The variance estimators are used to calculate upper confidence limits that represent the "missing positive sentiment". The estimators are, in general:

$$\begin{aligned} \hat{x}_t &= \mathbb{E}(x_t | y_t) & 1 \leq t \leq \tau \\ \hat{P}_t &= \mathbb{E}((x_t - \hat{x}_t)(x_t - \hat{x}_t)') & 1 \leq t \leq \tau \end{aligned} \quad (7)$$

The *Kalman filter* provides a way to update the state vector  $x_t$  from the previous state vector  $x_{t-1}$  plus a new observation  $y_t$  without having to reprocess all previous observations. The update equations take the form in equation 8, in which  $K_t$  is the *Kalman gain*.

$$\begin{cases} K_t = P_{t-1} A_t' (A_t P_{t-1} A_t' + R)^{-1} \\ x_t = x_{t-1} + K_t (y_t - A_t x_{t-1} - \Gamma u_t) \\ P_t = (I - K_t A_t) P_{t-1} \end{cases} \quad (8)$$

The corresponding predictors are shown in equation array 9, in which  $\mu_0$  and  $\sigma_0^2$  are initial mean and variance values.

$$\begin{cases} \hat{x}_t = \Phi \hat{x}_{t-1} + \gamma u_t & 1 \leq t \leq \tau \\ \hat{P}_t = \Phi \hat{P}_{t-1} \Phi' + Q & 1 \leq t \leq \tau \\ \hat{x}_0 = \mu_0 \\ \hat{P}_0 = \sigma_0^2 \end{cases} \quad (9)$$

The sequences in equations 8 and 9 assume the Normal-Normal conjugacy property: if  $y_t | x_t$  is normally distributed and  $x_t | y_{t-1}$  is normally distributed, then the conjugate posterior distribution  $x_t | y_t$  is also normally distributed. The entire sequence then comprises normally distributed variates, provided that the initial observation (i.e. the raw data),  $y_0$ , is normally distributed.

The "missing positive sentiment" is then calculated in the following way. The term  $\hat{x}_t$  in equation 9 defines an estimate of the system state (i.e. the unobserved, or "missing") sentiment. The deviation of an upper confidence limit of that estimate from the observed sentiment, denoted here by  $m_t$ , represents the 'missing positive sentiment' for each value of  $t$  in the range  $1 \dots \tau$ . The mean of all of those differences,  $M_z$ , where  $z$  defines a confidence level, is then an overall measure of the 'missing positive sentiment' (equation 10). For 2-tailed confidence,  $z = 1.975$  for 95% confidence and 2.576 for 99% confidence, assuming a normal distribution of residuals.

$$\begin{aligned} m_t &= \hat{x}_t + z \sqrt{\hat{P}_t} - y_t & 1 \leq t \leq \tau \\ M_z &= \overline{m_t} & 1 \leq t \leq \tau \end{aligned} \quad (10)$$

In section 4 we give estimates of the "missing positive sentiment" at both confidence levels.

### 3.8 State-space estimation: extension to non-Normal data

Non-Normal data can be accommodated using a *MCMC* analysis. The general technique is to generate a posterior distribution from data and a prior distribution, and then to sample from the posterior distribution. We have used the implementation due to (Fruehwirth-Schnatter, 1994), and (Carter and Kohn, 1994). Inverse Gamma (*IG*) priors are used for  $Q$  and  $R$  in equation 6, since *IG* prior-posterior pairs are conjugate for a likelihood with unknown variance. They are:  $Q \sim IG(a_0/2, b_0/2)$  and  $R \sim IG(c_0/2, d_0/2)$ , where the hyper-parameters  $a_0, b_0, c_0, d_0$  are set to give approximately the same "missing positive sentiment" value as for the *State-Space* analysis. The

initial state is  $u_t = 0$ . There is sufficient data in the reputation time series used to be confident that data will predominate over the priors in the *MCMC* step.

Then, with these inverse gamma likelihoods, if the prior on  $\Phi$  is Normal, the distribution  $\Phi|Q, x_t, y_t$  is also Normal. The update equations for the variances take the form

$$Q|\Phi, x_t, y_t \sim IG\left(\frac{1}{2}(a_0 + t), \frac{1}{2}(b_0 + \sum_{i=1}^t (x_i - \Phi x_{i-1})^2)\right)$$

$$R|x_t, y_t \sim IG\left(\frac{1}{2}(c_0 + t), \frac{1}{2}(d_0 + \sum_{i=1}^t (y_i - x_i)^2)\right) \quad (11)$$

With these updates, we sample the state vectors from the posterior density  $p(x|\Theta, y)$ , where  $\Theta$  is the set of hyper-parameters  $a_0, b_0, c_0, d_0$ . The *MCMC* stage uses a *Forward Filtering Backward Sampling (FFBS)* algorithm, summarised by the following equations.

$$p_{\Theta}(x_0, y_1) = p_{\Theta}(x_t|y_t) \times p_{\Theta}(x_{t-1}|x_t, y_{t-1})$$

$$\times \dots \times p_{\Theta}(x_0, x_1)$$

$$\implies p_{\Theta}(x_t|x_{t+1}, y_t) \propto p_{\Theta}(x_t|y_t) \times p_{\Theta}(x_{t+1}|x_t) \quad (12)$$

Therefore, using  $x_t|y_t \sim N(\hat{x}_t, \hat{P}_t, \Theta)$  and  $x_{t+1}|x_t \sim N(\Phi x_t, Q, \Theta)$ , we calculate the conditional means and variances  $\mathbb{E}_{\Theta}(x_{t+1}|y_t)$  and  $\mathbb{V}_{\Theta}(x_t|y_t, x_{t+1})$ . That is done by running the algorithm update step  $N$  times, and accumulated the results of each run in a matrix  $D$ . Each row in  $D$  is a draw of the entire time series (i.e. times  $1 \dots \tau$ ) from the posterior distribution, so that  $D$  has  $N$  rows and  $\tau$  columns.

To get the measure of "missing positive sentiment", we extract the upper  $z$ -quantile at each column of  $D$ . So if  $Q_z$  is a function that extracts a  $z$ -quantile, the required 'missing positive sentiment' is (the equivalent of equation 10):

$$m_t = Q_z(D_{it}) - y_t; \quad i = 1..N, z = 0.975 \text{ or } 0.995$$

$$M_z = \overline{m_t} \quad 1 \leq t \leq \tau \quad (13)$$

## 4 RESULTS

We first show results for the negative/positive sentiment balance, and then present example results to illustrate the 'shape' of a reputation profile, with a selection of "missing positive sentiment" values.

### 4.1 Negative/Positive sentiment results

To gain some idea of the positive/negative sentiment balance (as distinct from the sentiment *bias*), we have examined the proportion of days on which positive and negative sentiment was registered for organisations that are the constituents of a range of major world stock exchanges, plus 40 that are non-listed. The stock exchange-listed organisations form groups that give some indication of a geographical effect. The regions represented are North America (Dow Jones Industrial Average - DJIA and S&P500), Germany (DAX40), France (CAC40), UK (FTSE100), Japan (Nikkei225) and Hong Kong/China (Hang Seng). Some stocks were omitted if sufficient reputation data was not available, and only the top 100 stocks by market capitalisation in the S&P500 were used. The "Unlisted" category includes some well-known organisations, such as *Lego*, *LIDL*, *IKEA*, *NASA*, *Bosch* and *SpaceX*. The results in Table 1 indicate that positive sentiment predominates, in contrast to many of the results noted in Section 2.

Table 1: Positive/Negative Sentiment balance

Index	Sample size	Proportion	
		+	-
Section 3.4 '261'	261	0.60	0.40
FTSE100	94	0.46	0.54
DJIA	30	0.67	0.33
Hang Seng	57	0.21	0.79
DAX	38	0.79	0.21
NIKKEI225	85	0.61	0.39
S&P500	100	0.75	0.25
CAC40	40	0.83	0.17
Unlisted	40	0.53	0.47

Notably, the FTSE and Hang Seng results indicate negative sentiment bias, in contrast to all of the others. Overall, Table 1 shows that whether or not negative sentiment predominates over positive depends on what is being measured, and on location. This point will be taken up in Section 5. Notably, the "Section 3.4 '261'" sample, which was specifically selected to cover industry sectors, had an overall positive sentiment balance.

### 4.2 Missing Positive Sentiment

In order to gain some idea of the results of applying the State-Space process, Table 2 shows a random selection of organisations, with estimates of their

”missing positive sentiments”, obtained using upper 95% and 99% confidence bounds for the state-space reputation signals (Equation 10). Results for both methods are shown: *State-Space* (Section 3.7) and *MCMC* (Section 3.8.) The interpretation of these figures is that they should represent, for each organisation, an amount that should be added to the entire reputation profile. The 95% and 99% are intended to provide a range, from which the precise amount to be added should be taken. We suggest that it should be nearer to the higher figure, to be more consistent with the high positive/negative sentiment discrepancies uncovered in Section 2.

Table 2: Examples of ”Missing positive sentiment” values. *State-Space* evaluation, based on a 200-point scale [-100, 100]

Organisation	<i>State-Space</i>	
	95%	99%
Qantas	8.73	11.49
Mercedes-Benz	5.65	7.40
ExxonMobil	6.06	7.89
Walt Disney Corp.	7.43	9.70
HSBC	5.96	7.75
Astra Zeneca	7.89	10.50
Spotify	6.60	8.74
Kellogg	7.59	10.13
Samsung	4.27	5.71
Fedex	7.65	10.00
Thyssen Krupp	4.83	6.44
Antofagasta	7.22	9.51

Table 3: Examples of ”Missing positive sentiment” values. *MCMC* evaluation, based on a 200-point scale [-100, 100]

Organisation	<i>MCMC</i>	
	95%	99%
Qantas	6.37	8.36
Mercedes-Benz	6.23	8.15
ExxonMobil	6.30	8.27
Walt Disney Corp.	6.21	8.14
HSBC	6.26	8.18
Astra Zeneca	6.39	8.38
Spotify	6.19	8.13
Kellogg	6.37	8.36
Samsung	6.17	8.07
Fedex	6.38	8.38
Thyssen Krupp	6.37	8.34
Antofagasta	6.48	8.51

The entries in Table 3 show a clear difference be-

tween the two groups, even though the values shown for the two groups correspond reasonably well. The *MCMC* group are more tightly clustered. This observation is very clear when one views descriptive statistics for *all* organisations in this study. Tables 4 and 5 show the results for the 261 organisations in the first data set described in Section 3.4. In particular, it is notable that the standard deviation for the *MCMC* calculation method is much smaller than the standard deviation for the *State-Space* method. The small standard deviations also indicate consistency across all organisations, and independence from industry sector. The mean values for the two methods are approximately the same.

Table 4: Distributional Statistics for ’missing positive sentiment’,  $\hat{x}_M$ , in equations 10 and 13. *State-Space* evaluation, based on a 200-point scale [-100, 100]

Organisation	<i>State-Space</i>	
	95%	99%
Maximum	11.5	14.49
Minimum	3.48	4.59
Mean	6.36	8.4
SD	1.29	1.68

Table 5: Distributional Statistics for ’missing positive sentiment’,  $\hat{x}_M$ , in equations 10 and 13. *MCMC* evaluation, based on a 200-point scale [-100, 100]

Organisation	<i>MCMC</i>	
	95%	99%
Maximum	8.97	11.77
Minimum	6.16	8.07
Mean	6.42	8.41
SD	0.32	0.42

Figure 4 shows a view of the ”missing positive sentiment” that encompasses all organisations analysed. There is a small difference between the evaluations at 95% and 99% confidence, and in this case it would be acceptable to value ’missing positive sentiment’ at ”between 6.5 and 8.5, based on the overall sentiment range of [-100, 100].

Using the *MCMC* method (3.8, under the assumption that reputation data is not necessarily Normally distributed) provides a different view. It is very apparent from Table 5 that there is a difference between the 95% and 99% estimations. That difference is very marked in Figure 5, since there is minimal intersection between the two histograms. *MCMC* evaluation has also produced a distinct tail at both 95% and 99%



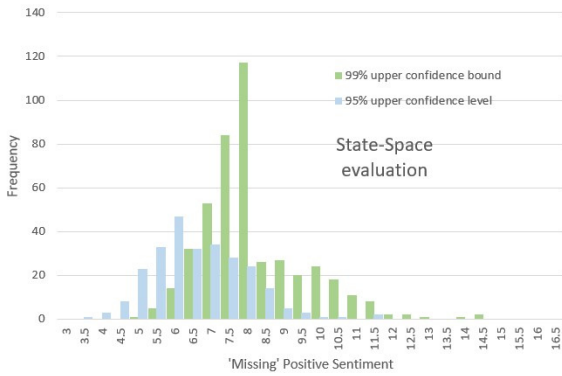


Figure 4: "Missing positive sentiment" distributions, all organisations, using the *State-Space* evaluation (3.7).

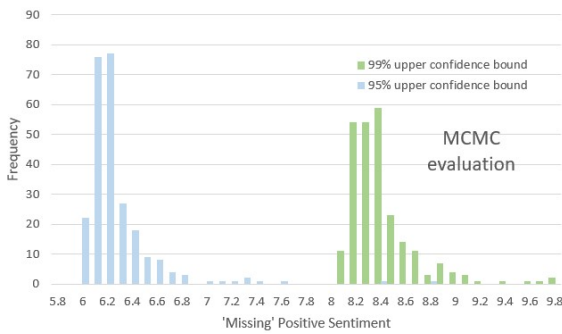


Figure 5: "Missing positive sentiment" distributions, all organisations, using the *MCMC* evaluation (3.8).

confidence, although the mean values are consistent with the *State-Space* evaluation.

We now consider a particular organisation to illustrate (Figure 6) the extended reputation profile, its *State-Space* representation, and the confidence bound used to calculate the "missing positive sentiment". *American Express* is a typical profile, with frequent peaks and troughs, a few downward plunges (representing limited bad publicity) and high inter-peak volatility. The state-space representation is close to the observed values, although in some cases it falls slightly below the observations. *American Express* is unusual compared to other financial organisations, which show largely negative sentiment.

## 5 DISCUSSION

The statistical analysis in this paper is based on the presumption that negative sentiment predominates over positive sentiment. The indications from the literature review are that excess negative sentiment does exist in many contexts. Its origin lies in an innate psychological negative bias. An examination of reputa-

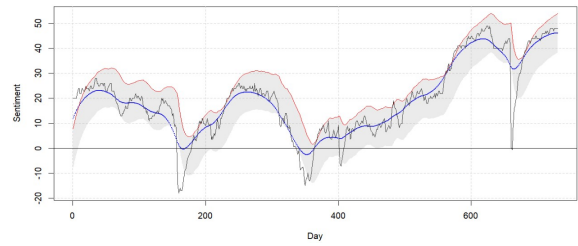


Figure 6: Amex reputation profile. Black trace: observed sentiment. Blue trace: smoothed observed. Red dotted trace: upper 95% confidence bound for the *State-Space* representation. Day range: October 2021 to September 2023 (730 days). The grey region marks the 95% error margin. The lower confidence bound is not shown but is at the lower boundary of the grey region.

tion time series reveals a very mixed picture. It appears that factors such as the method of sampling, the mode of analysis of the samples, and sample location are all significant factors. Consider, first, the way in which data are procured and processed. Data feeds are set up to source texts targeted on particular keywords. *NLP* is used to extract sentiment from each, and an averaging process then determines daily sentiment from the texts received during the day. The entire process is automatic and objective, and is geared to corporate organisations by up-weighting sources from 'traditional' media (the press and broadcasting). Social media, in many cases, is a minor component of sentiment, except in contentious cases. This method of data sourcing and analysis differs from the the studies in the literature review in the following ways.

- The type of sentiment sourced: corporate affairs, product review, or social comment.
- The calculation method for opinion and sentiment.
- The sentiment source.
- The measurement period: one-off or extended.

The second significant determinant of "missing positive sentiment" is sampling. The original sample for this analysis (Section 3.4) was selected on the basis of industry coverage, which was not a random sample. The stock index results are derived from predefined groups, which makes them representative of a particular class of corporates. It was not possible to draw a truly random sample from all data available, since a necessary part of downloading the data is to target specific organisation names rather than unique identifiers. Therefore, stock index constituents are as near as we can get to a random sample.

A third factor is also apparent. There appears to be a regional difference in measuring missing

positive sentiment in the context of reputation. The analysis of the FTSE and Hang Seng data show precisely the reverse 'missing' sentiment compared to data from other locations. This may indicate a more negative economic outlook in the UK and Hong Kong/China. The consequence of these differences is that we might not expect consistency with previous analyses of negative bias.

The "missing positive sentiment" figures in Tables 2 and 3 (Section 4.2) show that at the 95% significance level, acceptable consistency is returned by the *State-Space* and *MCMC* methods. Focussing on those figures, the measured "missing positive sentiment" is approximately 6.5 (95% confidence), and 8.4 (99% confidence), measured on a scale [-100,100]. In percentage terms, that scales to 3.25% with respect to the measured sentiment, independent of scale. Using the 99% confidence figures, the equivalent figure is 4.2% of the measured sentiment, independent of scale. We therefore propose a figure for "missing positive sentiment" between 3.25% and 4.2%, and suggest a 'round' 4% to account for some long tails with the *MCMC* assessment. A simple practical way in which to apply the 4% figure for "missing positive sentiment" is to inflate all positive sentiment figures by 4%, leaving negative sentiment figures unchanged.

The results of this study are significant for two reasons. First, quantification of negative bias using automated methods coupled with exhaustive data mining is a much more reliable than one-off survey methods. Therefore, we can place considerable reliance on the final proposed figure of 4%. Second, the discrepancy between the positive/negative sentiment balance shows that the context in which measurement takes place (sources and media), and geographical region are both important. Generalisation to other contexts and regions is unsafe.

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