

# The impact of spectral line wing cut-off: recommended standard method with application to MAESTRO opacity data base

Ehsan (Sam) Gharib-Nezhad,<sup>1,2\*</sup>† Natasha E. Batalha,<sup>1</sup> Katy Chubb<sup>3</sup>,<sup>3</sup> Richard Freedman<sup>4,1,4</sup>,  
 Iouli E. Gordon<sup>5</sup>,<sup>5</sup> Robert R. Gamache,<sup>6</sup> Robert J. Hargreaves,<sup>5</sup> Nikole K. Lewis,<sup>7</sup>  
 Jonathan Tennyson<sup>8</sup> and Sergei N. Yurchenko<sup>8</sup>

<sup>1</sup>Space Science and Astrobiology Division, NASA Ames Research Center, Moffett Field, CA, 94035, USA

<sup>2</sup>Bay Area Environmental Research Institute, CA, 94035, USA

<sup>3</sup>School of Physics and Astronomy, University of St Andrews, St Andrews, KY169SS, UK

<sup>4</sup>Carl Sagan Center, SETI Institute, 515 North Whisman Road, Mountain View, CA 94043, USA

<sup>5</sup>Atomic and Molecular Physics, Harvard-Smithsonian Center for Astrophysics, Cambridge, MA, 02138, USA

<sup>6</sup>Department of Environmental, Earth, and Atmospheric Sciences, University of Massachusetts, Lowell, MA, 01854, USA

<sup>7</sup>Department of Astronomy, Cornell University, Ithaca, NY, 14850, USA

<sup>8</sup>Department of Physics and Astronomy, University College London, London, WC1E 6BT, UK

Accepted 2023 November 30. Received 2023 November 10; in original form 2023 June 16

## ABSTRACT

When computing cross-sections from a line list, the result depends not only on the line strength, but also the line shape, pressure-broadening parameters, and line wing cut-off (i.e. the maximum distance calculated from each line centre). Pressure-broadening can be described using the Lorentz line shape, but it is known to not represent the true absorption in the far wings. Both theory and experiment have shown that far from the line centre, non-Lorentzian behaviour controls the shape of the wings and the Lorentz line shape fails to accurately characterize the absorption, leading to an underestimation or overestimation of the opacity continuum depending on the molecular species involved. The line wing cut-off is an often overlooked parameter when calculating absorption cross-sections, but can have a significant effect on the appearance of the spectrum since it dictates the extent of the line wing that contributes to the calculation either side of every line centre. Therefore, when used to analyse exoplanet and brown dwarf spectra, an inaccurate choice for the line wing cut-off can result in errors in the opacity continuum, which propagate into the modelled transit spectra, and ultimately impact/bias the interpretation of observational spectra, and the derived composition and thermal structure. Here, we examine the different methods commonly utilized to calculate the wing cut-off and propose a standard practice procedure (i.e. absolute value of  $25 \text{ cm}^{-1}$  for  $P \leq 200 \text{ bar}$  and  $100 \text{ cm}^{-1}$  for  $P > 200 \text{ bar}$ ) to generate molecular opacities which will be used by the open-access MAESTRO (Molecules and Atoms in Exoplanet Science: Tools and Resources for Opacities) data base. The pressing need for new measurements and theoretical studies of the far-wings is highlighted.

**Key words:** wing cut-off – Data Methods – line profile – Voigt profile – Lorentz profile – absorption cross section.

## 1 INTRODUCTION

Observations of a diverse set of atmospheres, from brown dwarfs and hot gas giants, to small rocky worlds, will be a legacy of *JWST* and the future next-generation ground based telescopes. In order to robustly compare observations to models, the community needs access to validated and up-to-date opacities. In many cases, computing opacities for a single molecule, under a specified pressure–temperature–gas mixture combination, is not trivial. For exoplanet conditions specifically (i.e. high temperature and exotic, non-air gas mixtures), data are often incomplete (as outlined in Fortney et al. 2019) and could lead to noticeable errors in modelling transit spectra of exoplanets (e.g. Gharib-Nezhad & Line 2019; Niraula et al. 2022)

and brown dwarf atmospheres (e.g. Iyer et al. 2023). Beyond line list data use, other modelling choices in opacity calculations affect the resultant calculation, including line profile, intensity cutoffs, and wing cut-offs. This was the motivation for the MAESTRO<sup>1</sup> (Molecules and Atoms in Exoplanet Science: Tools and Resources for Opacities) data base: an open NASA-supported opacity service that can be accessed by the community via a web interface. Of priority for the MAESTRO project is to develop community standards in computing and publishing molecular and atomic opacity data. The main principles of the MAESTRO interface are to highlight: (1) known updates from line lists communities that need to be incorporated into the community data base, (2) opacity calculation cautions that specify when approximations or estimations have been made, (3) limits of use for comparing models to observations (e.g.

\* E-mail: [e.gharibnezhad@asu.edu](mailto:e.gharibnezhad@asu.edu)

† All authors have contributed equally to this study.

<sup>1</sup>[science.data.nasa.gov/opacities/](https://science.data.nasa.gov/opacities/)

completeness and line position accuracy), and (4) the full breadth of data (including relevant citations) that are used for a single opacity calculation. Currently, the focus of this work is on molecular, not atomic opacities. Atomic opacities will be the focus of future work. For the molecular opacity calculation cautions listed, we currently employ a set of standard warnings. We have six standard warnings that pertain to the broadening choices (e.g. ‘Laboratory or theoretical broadener information not available at all’ or ‘Broadener data for an air mixture was used in place of this broadener gas’), and two standard warnings that pertain to the line list choices [‘Line list used is not suitable for this temperature regime’ and ‘The line position accuracy is suitable for *JWST*-quality spectra only ( $R = 100\text{--}3000$ )’].

We aim to accept community contributions to the MAESTRO opacity data base, which will undergo an open peer review through our contributor portal on Github.<sup>2</sup> In order to facilitate community contributions we must first agree on a standard method for wing cut-offs such that we can effectively execute community model comparisons. Therefore, here, we document our standard methods that we will adopt in the MAESTRO data base. This paper specifically focuses on the impact of different line wing cut-off methods and the ‘best’ method implemented to generate opacity data sets using Voigt profile. In a future MAESTRO update, we aim to expand our calculation cautions to include those that pertain specifically to wing-cut-offs choices such that users can assess how choices in wing-cut-off might affect their opacity data.

The Voigt profile, which is a convolution of Lorentz and Doppler (Gaussian) profiles, is a common profile when generating model spectra from molecular/atomic line lists. While this profile is extensively utilized for generating absorption cross-sections (ACS), spectroscopic measurements have shown that non-Lorentzian behaviour plays a key role in both the line centre and the wings [for example, for the distortion from the line centre see Ngo et al. (2013, 2017); Wcislo et al. (2016); Burch, France & Williams (1963); Burch & Gryvnak (1971); Burch, Gryvnak & Patty (1967, 1968); Burch, Howard & Williams (1956); Burch & Williams (1962), and for the wings see (Hartmann, Boulet & Brodbeck 2002)]. Establishing a consistent policy for determining the limit of the extent of the line profile is a difficult and complex problem. The far wing is usually defined as the region beyond a certain multiple of the line widths from the line centre. For most species, knowledge of the far wing may not be well established either by theory, experiment, or a combination of the two. This deviation from the perfect Lorentzian behaviour begins at  $\sim 5\text{--}30\text{ cm}^{-1}$  from the line centre, and depends on the absorber, broadening agent, pressure, and temperature.

The inclusion of the non-Lorentz behaviour in the ACS data is challenging due to the lack of complete spectroscopic parameters. The main technique used in astrophysics to minimize the issue is to introduce a wing cut-off,  $R_{\text{cut}}$ , parameter.  $R_{\text{cut}}$  can be a fixed spectral distance (e.g.  $25\text{ cm}^{-1}$  is typically used for calculations of terrestrial radiative transfer; Mlawer et al. 2012) applied to all lines in the ACS calculation equally, or it can be dependent on a property of each line. For example, some studies have used  $R_{\text{cut}} = 200\gamma_v$  to  $500\gamma_v$  (Freedman et al. 2014; Grimm & Heng 2015; Hedges & Madhusudhan 2016; Chubb et al. 2021; Grimm et al. 2021), where  $\gamma_v$  is the Voigt half-width-at-half-maximum (HWHM). In addition, a maximum cutoff can be used to prevent the line wings from becoming too large at higher pressures (Chubb et al. 2021). Some studies have employed a fixed value for all or different pressure ranges (MacDonald 2019; Zhang et al. 2020; Gharib-Nezhad et al.

2021a, b), or even use a pressure-dependent cutoff, such as  $\min(25P, 100)\text{ cm}^{-1}$ ,<sup>3</sup> where  $P$  is the total gas pressure in atmospheres, and also apply normalization correction factors to ensure that the total strength of the profile is conserved (Sharp & Burrows 2007). In another study, Letchworth & Benner (2007) have proposed different equations to control the truncation of the line wing in under different P–T conditions including the elimination of the weak lines and evaluating the resultant errors.

A few studies, however, calculated semi-empirical parameters or ‘correction factors’ to improve the Voigt result. Examples are limited to few spectroscopic measurements and for room temperature including  $\text{CH}_4$ -in- $\text{H}_2$  for  $P_{\text{H}_2} = 10\text{--}200\text{ atm}$  (Hartmann et al. 2002), and  $\text{CH}_4$ -in- $\text{CO}_2$  for  $P_{\text{H}_2} = 3\text{--}25\text{ bar}$  (Tran et al. 2022). Correction factors are often different for different bands of a molecule; for instance, the spectral mapping atmospheric radiative transfer model (Meadows & Crisp 1996) derives correction factors and their functional implementations for different bands of  $\text{CO}_2$  based on existing experimental studies and spectra of Venus. The spectral wings generated from all these different methods are not necessarily consistent, and hence different ACS spectra are generated and used for atmospheric modelling. This hinders cross comparisons between studies, even when the source line lists used are identical. As a result of different choices in the wing cut-off, this imposes difficulties when comparing the resultant physical inferences from substellar spectra.

In addition to the inconsistency problem, inaccurate choice of  $R_{\text{cut}}$  results in many types of errors. First, a small value of  $R_{\text{cut}}$  results in an underestimation of the opacity continuum, particularly at high pressures ( $\gtrsim 200\text{ bar}$ ) where the Voigt (or Lorentzian) HWHM can be a few tens of wavenumbers. This means that the wing region should be extended. Secondly, having a large value for  $R_{\text{cut}}$  leads to an overestimation of the opacity continuum at low pressures ( $\lesssim 10^{-2}\text{ bar}$ ) where the Voigt HWHM is  $\lesssim 0.01\text{ cm}^{-1}$ . Thirdly, far wing effects are often included in continuum models (Mlawer et al. 2012; Shine et al. 2016) to correct the overall opacity continuum (see Section 3 below) and it is important to match  $R_{\text{cut}}$  with the definition of these functions to avoid over/under counting. Another related problem specific to low pressure calculations is that the line profile is sometimes narrower than the size of the wavelength grid intervals. This can lead to undersampling, or no sampling at all, and impact the accuracy of the ACS.<sup>4</sup> Among the solutions are moving the line centres to the nearest grid point (Sharp & Burrows 2007) or using the line profile binning over the grid point instead of sampling (Hill, Yurchenko & Tennyson 2013). These inaccuracies become crucial in spectral regions with a large number of spectral lines because they add up and make the overall opacity continuum stronger or weaker.

Our main objective in this study is to propose a ‘standard practice’ method to control inaccuracies resulted by calculations of the non-

<sup>3</sup>To prevent the absorption from becoming unrealistically large, a pressure-dependent cutoff with maximum value of  $100\text{ cm}^{-1}$  is proposed.

<sup>4</sup>To generate absorption cross-sections, a line-by-line code typically iterates over all transitions in the line list. A wavelength grid vector is created before the loop to accumulate the opacity values from the Voigt profile for each generated line profile within the loop. Subsequently, these values are added to the wavelength grid vector. At very low pressures and very low frequencies, the line widths become extremely narrow, potentially some of these lines will not be added accurately to the grid if they are very narrower than the chosen grid spacing. Therefore, the key point here is that the wavelength grid spacing should be sufficiently smaller than the spectral line widths to include the opacity contributions from all the lines and minimize the loss of intensity in such cases.

<sup>2</sup>[github.com/maestro-opacities/submit-data](https://github.com/maestro-opacities/submit-data)

Voigt behaviour for the MAESTRO opacity data base. MAESTRO spans a wide range of pressures and temperatures (i.e.  $10^{-6}$ –3000 bar and 75–4000 K). The justification for such a wide range of pressures and temperatures in the context of atmospheric radiative transfer modelling is provided by Section 2. Spectroscopic drawbacks in calculating the non-Voigt profile and its impacts on far wings are discussed in Section 3. Section 4 deals with other challenges: the challenges with the theoretical calculation of the thermochemical phase of the materials/gases in a very high-pressure regime are discussed in Section 4.1, and the impact of the window regions in Section 4.2. Two popular methods for choosing the  $R_{\text{cut}}$  to mitigate the effect of non-Voigt behaviour of the spectral lines are quantitatively analysed and discussed for CH<sub>4</sub>-in-air system in Section 5.1. These two scenarios are then tested using the experimental spectrum of CO<sub>2</sub>-in-N<sub>2</sub> system in Section 5.2. The accuracy of the superlines technique and its impact on the opacity continuum for the SO<sub>2</sub>-in-H<sub>2</sub> system is assessed in Section 5.3. Our recommendations for a current default line wing cut-off are presented in Section 6, followed by instructions on how to control the line wing cut-off parameter in some example well-used codes in Section 7. We finish with our conclusions in Section 8.

## 2 ASTROPHYSICAL CONTEXT FOR THE TEMPERATURE AND PRESSURE RANGES

Missions to the gas giant planets in our own solar system (e.g. *Cassini*, *Galileo*, *Juno*) have long sought to probe their deep atmospheres, which critically shape the chemistry and circulation patterns in the visible portion of their atmospheres. Since we cannot yet send spacecraft to visit planets orbiting other stars, we must rely on a combination of remote observations and atmospheric modelling to tie together the processes in their deep atmospheres/interiors and observable upper atmospheres. Theoretical models of giant exoplanet atmospheres critically depend on assumptions about atmospheric opacity sources which control the radiative balance between external and internal heating sources. Internal heat in giant exoplanets arising from both their formation and external forcing critically shapes the deep adiabatic region of their atmospheres (pressures greater than 10s to 100s of bars) which feeds into the radiative processes in the upper atmosphere (e.g. Thorngren, Gao & Fortney 2019). Fig. 1 illustrates the thermal structure in an atmosphere of a generic hot Jupiter across the pressure–temperature space (left), and associated contribution functions over the relevant *JWST* wavelengths for thermal emission (middle) (Lothringer, Barman & Koskinen 2018) and transmission (Mollière et al. 2019) observations.

Additionally, giant planets orbiting close to their host stars are expected to have deep atmospheric radiative zones extending to pressures of 1000 bar or more (e.g. Showman & Guillot 2002; Fortney et al. 2005). In order to attempt to capture the radiative, advective, and chemical processes that occur throughout giant exoplanet atmospheres, we must make assumptions about the atmospheric opacity at pressures well beyond the 1–10 bars typically considered. Hence, our opacity data for the MAESTRO data base are calculated for a wide range of pressures,  $10^{-6}$ –3000 bar, to be applicable to modelling all cases. Table 1 lists the temperature and pressure grid points in detail.

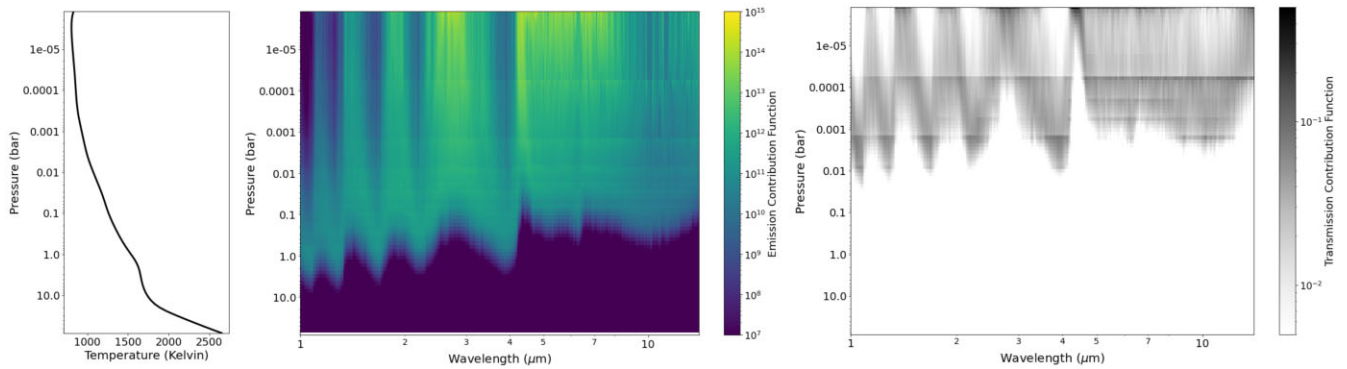
## 3 A BRIEF COMMENT ON THE LINE SHAPE THEORY AND THE CHALLENGES WITH CALCULATING THE SPECTRAL FAR WING

The dipole moment of an atom or molecule describes the separation of charge within it. The line shape can be formally defined as the

Laplace transform<sup>5</sup> of the thermally averaged dipole autocorrelation function, which is a measure of the loss of coherence of the radiation due to the environment (perturbing electrons, ions, molecules, ...). The relationship between frequency in the line shape and time in the autocorrelation function shows that the time dependence of certain phenomena will impact different parts of the line shape. Processes that happen within a certain time  $\Delta t$  will appear in the spectrum within a frequency range of  $\Delta f = 1/\Delta t$ . Because small  $\Delta f$  samples large  $\Delta t$ , the cores of lines are in the dynamic limit because the perturbing particles move appreciably within a large  $\Delta t$ . In the wings of the lines, large  $\Delta f$  corresponds to short  $\Delta t$ . At short  $\Delta t$  the perturbing particles do not move appreciably and appear ‘static’. Thus, the line wings can be determined by ‘quasi-static’ methods. For example, Ma & Tipping (1990b) developed a theory for the calculation of the continuous absorption due to the far wing contributions of allowed lines of H<sub>2</sub>O–H<sub>2</sub>O absorption based on a generalization of Fano’s theory and later extended it using the quasi-static approximation for the far wing limit and the binary collision approximation (Ma & Tipping 1991). Their development was limited to binary collisions (first-order in density). Hussey, Dufty & Hooper (1975) developed expressions containing a generalized Fano operator that has terms containing the effects of three- or four-body collisions for spectral line broadening in plasmas. These terms would be necessary for high-pressure applications. The wings of spectral lines can be either sub-Lorentzian or super-Lorentzian. It is the interaction between the radiating and perturbing molecules in the quasi-static limit that determines the sub- or super-Lorentzian behaviour.

The simulation of molecular spectra has become routine and automated since the development of the spectroscopic data bases in the early 1970s (McClatchey et al. 1973): HITRAN (Gordon et al. 2022), GEISA (Delahaye et al. 2021), ATMOS (Gunson et al. 1996), etc. Here we will use HITRAN as the standard. However, many problems remain, and therefore these data bases and their functionality are periodically updated and extended. First, there is always the question of the quality of the molecular parameters in these data bases. Positions and lower state energies (term values as the units are  $\text{cm}^{-1}$ ) are well-known for many molecules, but the line intensities are relatively known for a number of molecules in mostly low temperature ranges. The line shape parameters,  $\gamma$ , and  $\delta$  (i.e. the Lorentzian pressure-broadening and pressure-shift parameters, respectively) are the least well-known. For limited number of the molecules in HITRAN, there are measured half-widths and a small number of shifts. However, for many cases, these pressure-broadening coefficients are limited to few transitions, and hence they are estimated for all other lines. The uncertainty in the estimated half-width ranges from  $\sim 1$ –100 per cent, and in some cases, where the experimental or theoretical data is lacking, the values in HITRAN (Gordon et al. 2022) are estimated using different methods. For instance, they can be estimated by scaling data from other collision systems (Gamache & Laraia 2009), using the mass dependence of half-widths (Lamouroux et al. 2010), or using the ratios based on the few available empirical values available in the literature (Tan et al. 2022), or by averaging the values as a function of quantum numbers (for instance, for unmeasured transitions of water vapour in HITEMP2010 (Rothman et al. 2010), or simply a constant

<sup>5</sup>The Laplace transform is a mathematical technique used to convert a function from the time domain to the frequency domain. By taking the Laplace transform of the dipole autocorrelation function, the line shape can be characterized as a function of frequency



**Figure 1.** Typical hot Jupiter pressure–temperature profile (left) and associated contribution functions over relevant *JWST* wavelengths. Contribution functions dictate the pressure regions that the observable spectrum is sensitive to. The emission contribution function (middle) is defined in Lothringer et al. (2018). The transmission contribution (right) is defined in Mollière et al. (2019).

**Table 1.** Opacity computational details for MAESTRO data base.

<b>T(K) grid: (73 points)</b>							
75	100	110	120	130	140	150	160
170	180	190	200	210	220	230	240
250	260	270	275	280	290	300	310
320	330	340	350	375	400	425	450
475	500	525	550	575	600	650	700
750	800	850	900	950	1000	1100	1200
1300	1400	1500	1600	1700	1800	1900	2000
2100	2200	2300	2400	2500	2600	2700	2800
2900	3000	3100	3200	3300	3400	3500	3750
4000							
<b>P(bar) grid: (20 points)</b>							
$10^{-6}$	$3 \times 10^{-6}$	$10^{-5}$	$3 \times 10^{-5}$	$10^{-4}$	$3 \times 10^{-4}$	–	–
$10^{-3}$	$3 \times 10^{-3}$	$10^{-1}$	$3 \times 10^{-1}$	$10^{-2}$	$3 \times 10^{-2}$	–	–
1	3	10	30	100	300	–	–
1000	3000	–	–	–	–	–	–

value for all transitions. The line shifts are even less certain as they exhibit much stronger vibrational dependence.

One of the main problems associated with using the Voigt or Lorentz profiles is that the model does not give the correct profile over the whole extent of a spectral line. Burch *et al.* (Burch & Williams 1962; Burch *et al.* 1956, 1963, 1967, 1968; Burch & Gryvnak 1971) made several studies in the sixties and seventies showing that the Lorentzian line shape does not match measured spectra. They note for CO<sub>2</sub> ‘Beyond a few cm<sup>-1</sup> from line centre all lines absorb less than Lorentz-shaped lines with the same  $\gamma$ .’ For water vapour, the opposite is true, the absorption is greater than that modelled by Lorentzian as one moves away from the line centre. At around the same time, the radiative transfer model FASCODE (Smith *et al.* 1978; Clough *et al.* 1981) was being developed [now it is the LBLRTM (Clough *et al.* 2005) code]. To deal with this problem and to reduce the computation time, line wings were cut off at  $\pm 25$  cm<sup>-1</sup> from the line centre. For broad (low *J*) lines, of H<sub>2</sub>O and CO<sub>2</sub> at room temperature and 1 atmosphere, this amounts to going out to  $\sim 333$  half-widths, but note as Burch *et al.* have suggested there are noticeable differences in the absorption at  $\sim 25$  half-widths from the line centre. Note also that for narrow lines (generally high *J*), going out  $\pm 25$  cm<sup>-1</sup> corresponds to many more half-widths. To correct for this cut-off additional absorption is accounted for by what has been called the continuum, designated as the correction factor or  $\chi$  factor. Such a correction factor was used for simulating CO<sub>2</sub> emission to compare

to observations of the night side of Venus (Pollack *et al.* 1993). The continuum is different for each absorbing molecule. For water vapour, it was based on the work of Clough *et al.* and was called CKD (Clough, Kneizys & Davies 1989; Ma & Tipping 1992). This model has been updated many times based on new measurements and simulations. The current version is called MT-CKD (Mlawer *et al.* 2012). The use of the continuum recognizes that the absorption arises from several mechanisms and that corrections need to be made by cutting off the lines at 25 cm<sup>-1</sup>. First, there is the far-wing collision-induced absorption (CIA) as modelled by Ma and Tipping (Ma & Tipping 1990a, b, 1991, 1992, 1994; Ma *et al.* 1999), and there is also absorption by metastable species (Simonova *et al.* 2022) (dimers, trimers, etc. although most of this can be attributed to the dimers). For example, the H<sub>2</sub>O absorption can be broken into CIA, dimer spectrum, and a correction for the line cut-off. It will be similar to other molecules.

## 4 CHALLENGES

### 4.1 Computing opacities for high pressures: line mixing

Spectroscopic studies of exoplanets largely probe regions whose pressure are less than a few bars and, in many cases, a lot lower than this. For these regions, the Voigt profile is known to give a reasonable approximation to the pressure and temperature-dependent line shape in the region of the line centre although subtle collision effects are known to lead to minor distortions of this (Tennyson *et al.* 2014). At high pressures, there are a number of complications in simulating the spectrum. Table 1 lists the T and P grid points for the MAESTRO data base. The line shape parameters are determined based on the number density of the perturbing molecules with the pressure of 1 atm. At high pressures, non-ideal behaviour of the gases occurs and the line shape parameters should be taken at the corrected pressure corresponding to the number density of the real gas. The correction can be found in the appendix of Sung *et al.* (2019) who discuss O<sub>2</sub>; information on compressibility for key molecules can be found in the on-line NIST Chemistry Webbook.<sup>6</sup> However, the largest distortion away from a Voigt profile is caused by line mixing. Physically line mixing occurs due to collisions that connect the two transitions (Lévy, Lacombe & Chackerian 1992; Pieroni *et al.* 2001; Hartmann, Boulet & Robert 2008). To see this, consider two

<sup>6</sup><https://webbook.nist.gov/chemistry/>

transitions that mix,  $f \leftarrow i$  and  $f' \leftarrow i'$ . Line mixing provides an alternative path to go from  $i$  to  $f$ . A molecule in state  $i$  undergoes a collisional transition to  $i'$ , which then absorbs a photon and goes to  $f'$ ;  $f'$  then undergoes a collisional transition to  $f$ , thus completing the path from  $i$  to  $f$ . This path amounts to a redistribution of population, which does not affect the line position, but the line intensity and line shape parameters can be greatly affected. To be efficient, the frequencies of the two transitions should be very close to each other and the probability of the collisional connections, which are given by reduced matrix elements (Lamouroux, Gamache & Schwenke 2014; Gamache et al. 2019), should be large. As pressure increases CIA, which depends on the square of the pressure, becomes increasingly dominant.

First, Sung et al. (2019) discussed it only for one single molecule, O<sub>2</sub>. One good source of compressibility would be the NIST Chembook on-line. Secondly, what is underlined is not quite true. CIA is density-square dependent while line mixing effect is proportional to density. Therefore, toward high pressures, the CIA effect is expected to be significant (10 bars), substantial (100 bars), and eventually dominant (1000 bars) over the ACS based on the Voigt profile. The effect of line mixing with increasing pressure is gradually blending discrete lines into a single, strongly broadened absorption feature [see fig. IV.2 of Hartmann et al. (2008) for a nice illustration of this process]. At terrestrial temperatures and pressures, line mixing is only significant in a few special cases where lines lie particularly close together such as  $Q$ -branch transitions of CO<sub>2</sub>. Thus, for example, the current HITRAN2020 release (Gordon et al. 2022) implements full and first-order line-mixing for air- and self-broadened CO<sub>2</sub> lines (Hashemi et al. 2020) and first-order line mixing of N<sub>2</sub>O and CO lines (Hashemi et al. 2021); see also a recent experimental analysis of line mixing models for CO<sub>2</sub> at high temperature and pressure (Cole et al. 2023).

However, models of gas giant exoplanets need to consider radiative transport effects in regions where the pressure is much higher than 1 bar; the MAESTRO data base provides cross-sections extending up to 3000 bar. In this high-pressure regime, the ideal gas law is not longer obeyed and line mixing not only becomes important but increasingly becomes the dominant pressure-broadening mechanism. The standard procedure for modelling line mixing is via the use of a frequency-dependent relaxation matrix (Lévy et al. 1992; Hartmann et al. 2008). Empirical tests of the methodology using the spectrum of NO molecule at pressures of 30–100 bar and temperatures over 500 K (Fu, Borysow & Moraldi 1996; Almodovar et al. 2021) suggest that this methodology is reasonably successful at modelling the effects of line mixing. We note that in this pressure–temperature regime, the individual transitions merge into single quasi-continuous features more characteristic of a condensed phase than the usually heavily structured line spectra which characterize gas phase spectra. In this context, we note that in the high-pressure regime of interest for the interior of gas giant (exo)-planets the species generally exist in an environment well above their triple point meaning that there is no longer a distinction between gas and liquid phases. It is therefore not altogether surprising that the resulting spectra take on some of the characteristics of a condensed phase spectrum.

Very recently, Ren et al. (2023) performed an experimental study of high-pressure absorption coefficients for CO<sub>2</sub>, CO, and H<sub>2</sub>O for pressures up to 80 bar. They found that an empirical pseudo-Lorentz line shape model, which considers line-mixing effects is easy to implement and relatively accurate at modelling high-pressure gas spectra for the conditions they tested. This suggestion certainly merits further investigation.

We are not aware of any exoplanetary models which allow for the effects of line mixing. This is not surprising as the explicit coupling of the very many transitions that occur in a hot spectrum via a relaxation matrix which links these transitions together represents a significant extra complication in the radiative transport problem. It is likely that this problem is best addressed by generating effective temperature- and pressure-dependent cross-section sets which include line-mixing effects which can simply be used in the appropriate models. This idea is left to future work. The onset of high-precision *JWST* spectra as well as high-precision medium-resolution ground-based spectra of Brown Dwarfs and giant planets will enable constraints on pressure–temperature profiles to pressures of  $\sim 1$ –10 bar (e.g. Hood et al. 2023, and as seen in Fig. 1). Therefore, we will soon be able to shed light on whether line mixing seems to be driving temperature structure by comparing radiative–convective-derived models to retrieved temperature profiles.

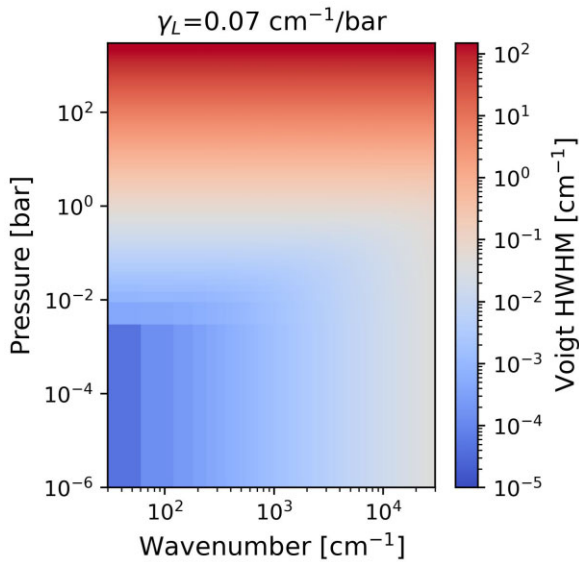
## 4.2 Spectral windows regions

The question of how to limit the extent of the line wings as a function of pressure and temperature is complex. At higher pressures, in order to capture the majority of the opacity in any given line transition it may be necessary to extend the line wings far beyond the line core and thus far beyond the validity of the Lorentzian profile. The lack of an extension will result in underestimating the total opacity, which will predominantly effect regions of low opacity – so-called ‘spectral windows’. Because these regions of low opacity contribute significantly to the character of the emerging radiation, they have to be modelled correctly. The areas of the spectrum that are already optically thick will not be affected to any great degree by decisions to modify the line wing extent. However because the far wings in many cases are known to be very sub-Lorentzian, the correct approach to the modelling of the spectra is complicated. One approach is to establish a cutoff (in  $\text{cm}^{-1}$ ) from the line centre for the profile and then attempt to compensate for the missing line wings by a pseudo-continuum contribution that would have to be computed separately. Although this approach is already used in many applications related to the Earth’s atmosphere for water opacity (as discussed in Section 3), how this would be handled in the astronomical case is less clear. A recent study by Anisman et al. (2022) found that transmission spectra of exoplanet atmospheres which are close to Earth’s atmospheric temperature can be significantly impacted if data for the water continuum is not included in models. The significance of the continuum is less clear at higher temperatures, but is generally assumed to follow a negative temperature dependence (Shine et al. 2016). Exoplanetary and brown dwarf atmospheric radiative-transfer models cover a wide range of temperatures and pressures that are never encountered on the Earth and include many species whose spectra may not be fully documented.

## 5 CASE STUDIES

### 5.1 Benchmark the effect of different wing cut-off methods on CH<sub>4</sub>-in-air system

Given the challenges on the theory side as well as the lack of sufficient experimental spectroscopic parameters, our goal is to propose the standard practice for calculating the wing cut-off for the astronomy community. But first, we need a quantitative overview of the range of Voigt HWHM (i.e.  $\Gamma_V$ ) values. Fig. 2 provides this information across a wide range of pressures and wavenumbers



**Figure 2.** Estimated Voigt HWHM across a wide range of spectral range and pressure for  $\text{CH}_4$  broadened by air with a constant Lorentz coefficient of  $0.07 \text{ cm}^{-1} \text{ bar}^{-1}$  and for room temperature. The calculated Voigt HWHM varies smoothly with pressure and position, the apparent steps are an artefact of the number of points calculated.

for room temperature.<sup>7</sup> For the sake of simplicity in comparison, a constant Lorentz coefficient of  $\gamma_L = 0.07 \text{ cm}^{-1} \text{ bar}^{-1}$  is used here but in reality,  $\gamma_L$  is dependent on the molecular symmetry and quantum numbers of the transition. In this figure shows that  $\Gamma_V$  HWHM has a wide range of  $10^{-1}$ – $150 \text{ cm}^{-1}$  across the pressure-wavenumber space. Cases with very low pressures ( $\lesssim 10^{-2} \text{ bar}$ ) and low wavenumbers  $\lesssim 10^3 \text{ cm}^{-1}$  (or  $\gtrsim 10 \mu\text{m}$ ), have  $\Gamma_V$  lower than  $10^{-2} \text{ cm}^{-1}$ . On the other hand, very high pressures ( $\gtrsim 10^1 \text{ bar}$ ) lead to a large  $\Gamma_V$  HWHM, i.e.  $> 20 \text{ cm}^{-1}$ , and up to  $\sim 150 \text{ cm}^{-1}$ .

Fig. 3 represents the generated ACS data sets for the  $\text{CH}_4$ -in-air system for a wide range of pressures and temperatures,  $10^{-6}$ – $10^3 \text{ bar}$  and  $75$ – $4000 \text{ K}$ , and for four wavenumber (WN) regions:  $90$ – $110$ ,  $900$ – $1100$ ,  $4900$ – $5100$ , and  $9900$ – $10100 \text{ cm}^{-1}$  (or  $100$ ,  $10$ , and  $2$ ,  $1 \mu\text{m}$ , respectively) with  $R_{\text{cut}}$  calculated using equations (1) and (2). To quantify the impact of the wing cut-off, Fig. 4 represents the differences in MAPE (the mean absolute percentage error) metric between the ACS data sets for hundreds of spectra.

$$R_{\text{cut,Abs}} = \begin{cases} 30 \text{ cm}^{-1} & \text{for } P \leq 200 \text{ bar} \\ 150 \text{ cm}^{-1} & \text{for } P > 200 \text{ bar} \end{cases} \quad (1)$$

$$R_{\text{cut,HWHM}} = 500 \times \gamma_{\text{Voigt}} \quad (2)$$

If we take the  $R_{\text{cut,Abs}}$  as the actual value, then MAPE formula is expressed as follows:

$$\text{MAPE} = \left( \frac{100}{n_{\text{gp}}} \right) \sum_{i=1}^{v_{\text{gp}}} \left| \frac{\sigma_{R_{\text{cut,Abs}}(v,T,P)} - \sigma_{R_{\text{cut,HWHM}}(v,T,P)}}{\sigma_{R_{\text{cut,Abs}}(v,T,P)}} \right|, \quad (3)$$

where  $n_{\text{gp}}$  is the number of grid points in the pressure-temperature space and  $v_{\text{gp}}$  is the wavelength of the transition. Few examples of the generated ACS spectra from the two scenarios of the wing cut-off are represented in Fig. 3 for  $T = 300 \text{ K}$  and pressures  $10^{-3}$ ,

$10^{-1}$ ,  $10 \text{ bar}$  and wavelength  $90$ – $110$ ,  $490$ – $510$ ,  $990$ – $1010$ , and  $9990$ – $10010 \text{ cm}^{-1}$ . We see the largest discrepancies in the generated ACS are from cases with low pressures,  $P < 0.1$ , and low wavenumbers.

Following that, Fig. 4 illustrates the differences between these two scenarios in the pressure–temperature space and across a wide spectral range. The balance between the Doppler widths and Lorentz widths plays a key role in the MAPE amount between these two  $R_{\text{cut}}$  scenarios. This difference is  $> 50$  per cent for very low wavenumbers (i.e.  $WN \leq 1000 \text{ cm}^{-1}$  or at far-infrared  $\lambda > 10 \mu\text{m}$ ). MAPE error becomes less than 10 per cent for high wavenumbers. The lesson learned from this figure is that the generated opacities at low wavenumbers, low pressures, and low temperatures are highly sensitive to the spectral wings and wing cut-off approaches. This is in agreement with the findings of Niraula et al. (2023) where the effect (or lack of effect) of pressure broadening and far-wing on the retrievals from the WASP 39b spectra (which probed the low-pressure/high-temperature layer of the atmosphere) was investigated. Please note that this figure serves as an illustration of the magnitude of the MAPE error for this specific absorber. For absorbers with different molecular masses (and consequently different Doppler widths), the errors would differ accordingly.

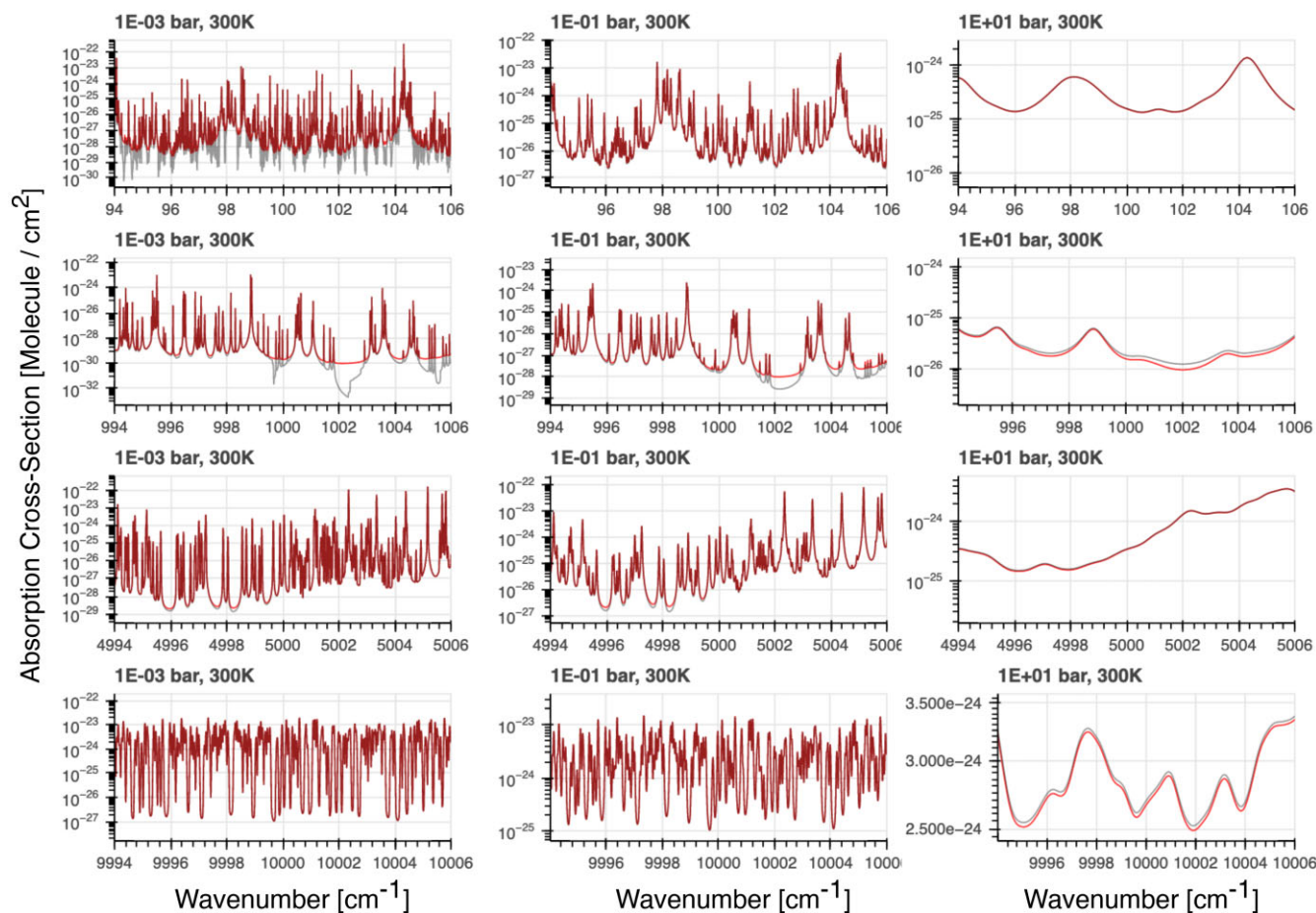
The current focus of exoplanet and brown dwarf atmospheric spectroscopy with *JWST* is on the spectral range at wavenumbers  $> 500 \text{ cm}^{-1}$ . For example, the very first *JWST* early release science observations focused on exoplanets and brown dwarfs featured a  $1$ – $20 \mu\text{m}$   $R \sim 1000$ – $3700$  spectrum of VHS 1256–1257 b (Miles et al. 2023), and a  $1$ – $5 \mu\text{m}$   $R < 300$  spectrum of WASP-39b (*JWST* Transiting Exoplanet Community Early Release Science Team 2023). Additionally, radiative-convective climate modelling demands accurate opacities throughout the expected spectral energy distribution of the planet’s emitted flux. Fig. 3 in Mukherjee et al. (2023) shows typical wavelength bins used for radiative-convective models of planets with  $T_{\text{eff}} = 300$ – $1000 \text{ K}$ . These wavelength bins extend to  $30 \text{ cm}^{-1}$  ( $333 \mu\text{m}$ ). Therefore, from an observational and heat transport perspective, it is essential to establish uniform methods of computing wing cut-offs.

## 5.2 Benchmark the effect of different wing cut-off methods on $\text{CO}_2$ -in- $\text{N}_2$ system

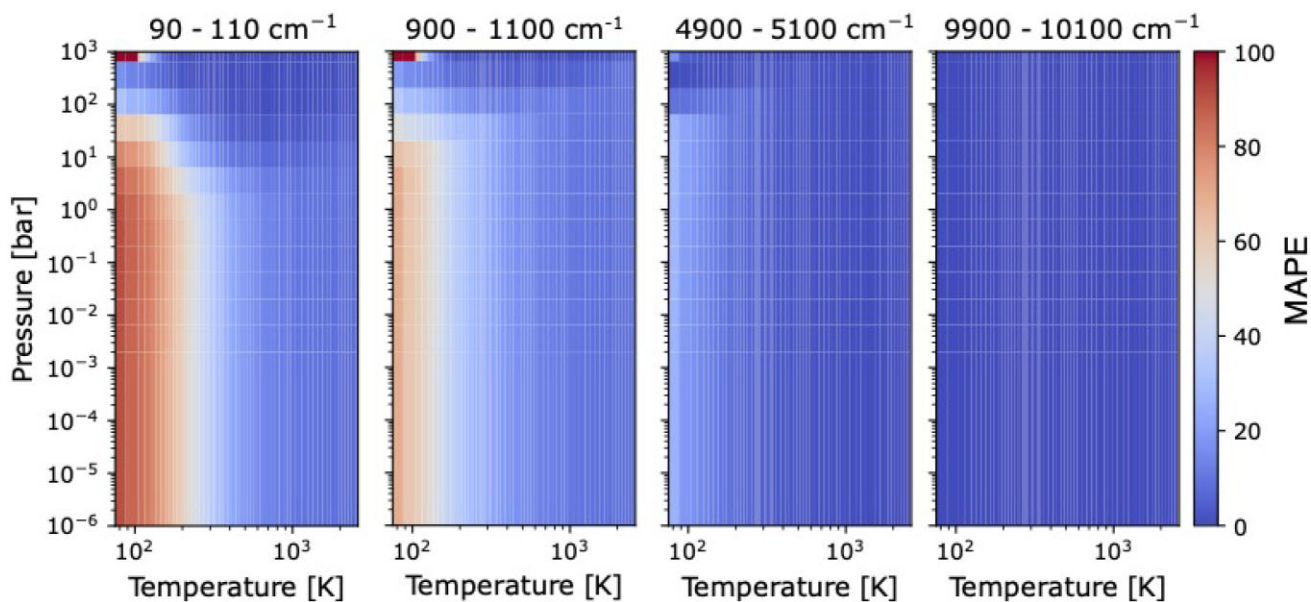
The strong  $\nu_3$  vibrational mode of  $\text{CO}_2$  near  $2350 \text{ cm}^{-1}$  ( $4.25 \mu\text{m}$ ) provides an opportunity to test the impact of the line wing cut-off over a complete absorption band. This band is readily observed in terrestrial atmospheres and has recently been detected in *JWST* observations of WASP-39b (*JWST* Transiting Exoplanet Community Early Release Science Team 2023).

Fig. 5 compares the effect of the line wing cut-off for the  $\nu_3$  region of  $\text{CO}_2$ . The left panel displays an experimental ACS of  $\text{CO}_2$  at  $25^\circ \text{C}$  broadened by  $1.0 \text{ atm}$  of  $\text{N}_2$  recorded by the Pacific Northwest National Laboratory, PNNL (Sharpe et al. 2004). The experimental measurement (black line) is shown in the region of the strong  $\nu_3$  vibrational mode near  $2350 \text{ cm}^{-1}$  on a logarithmic scale. The approximate sensitivity of the experimental measurement is  $\sim 10^{-23} \text{ cm}^2$  per molecule. Overplotted are four spectra calculated with Voigt line shapes using HAPI (Kochanov et al. 2016) and the  $\text{CO}_2$  line list from HITRAN2020 (Gordon et al. 2022). The only difference between the four calculated spectra is the treatment of the line wing cut-offs. These include line wings calculated from each line centre in multiples of the Voigt HWHM ( $250\times$  and  $500\times$ ) as well as fixed widths ( $25$  or  $100 \text{ cm}^{-1}$ ). The effect of the different line wing treatments is clearly seen in the region  $> 2380 \text{ cm}^{-1}$ .

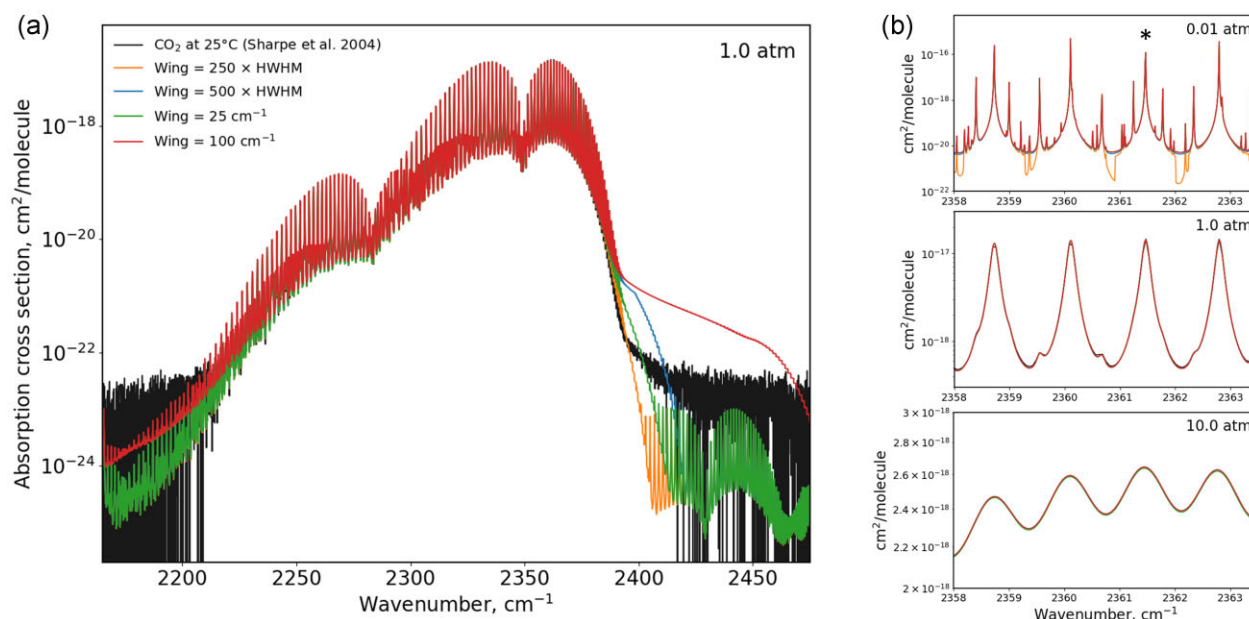
<sup>7</sup>Note that the Voigt HWHM ( $\Gamma_V$ ) in Fig. 2 is calculated with the following equation:  $\Gamma_V = 0.5346 \Gamma_L + \sqrt{0.2166 \Gamma_L^2 + \Gamma_G^2}$ , where  $\Gamma_G$  is the Doppler HWHM in  $\text{cm}^{-1}$  (Olivero & Longbothum 1977).



**Figure 3.** Calculated cross-sections of  $\text{CH}_4$  at 300 K broadened by air at three sample pressures (0.001, 0.1, 10.0 bar) in four spectral regions, using fixed line wings ( $R_{\text{cut, Abs}}$ , red spectra) and line wings dependent on the pressure-broadening ( $R_{\text{cut, HWHM}}$ , grey spectra) represented in equations (1)–(2).



**Figure 4.** Mean absolute percentage error (MAPE) from the two wing cut-off approaches for different spectral ranges: From left to right:  $\sim 100$ ,  $\sim 10$ ,  $\sim 2$ , and  $\sim 1 \mu\text{m}$  for  $\text{CH}_4$  in air. This figure shows that the generated opacities at low wavenumbers, low pressures, and low temperatures are highly sensitive to the spectral wings and wing cut-off approaches. The lack of broadening coefficients and appropriate line profile for very high pressures is another issue. See Section 5.1 for further details.



**Figure 5.** A demonstration of the effect of the line wing cut-off for the  $\nu_3$  region of  $\text{CO}_2$ . (a) An experimental absorption cross-section of  $\text{CO}_2$  at  $25^\circ\text{C}$  broadened by  $1.0\text{ atm}$  of  $\text{N}_2$  recorded by the Pacific Northwest National Laboratory, PNNL (Sharpe et al. 2004), compared to four calculated spectra with different line wing cut-off limits. (b) A zoomed in comparison at  $25^\circ\text{C}$  for three pressures. Note, only the plots at  $1.0\text{ atm}$  include the PNNL spectrum. See Section 5.2 for further details.

The right panel of Fig. 5 shows a zoomed-in region near the centre of the band for three different pressures (the example at  $1.0\text{ atm}$  is the same as the left panel). At lower pressures, the limitation of calculating a line wing that is dependent on the line broadening is shown to produce unexpected steps in the ACS between the strongest lines. In this example, these steps are a consequence of calculating the line wings up to  $250 \times \text{HWHM}$ . This can be seen for the line indicated by an asterisk, where at  $0.01\text{ atm}$  the broadening is  $0.002\text{ cm}^{-1}$ , which results in line wings of approximately  $\sim 0.5\text{ cm}^{-1}$  either side of the line centre.

It should be noted that the comparisons in Fig. 5 use the air-broadening half-widths from HITRAN. For a more accurate comparison to the PNNL spectra, it would be necessary to use  $\text{N}_2$ -broadening parameters along with line-mixing. However, the effects observed by the different choices in line wing cut-off would still be observed.

### 5.3 Assess the impact of the super-lines method on wing cut-off: $\text{SO}_2$ -in- $\text{H}_2/\text{He}$ system

Here we assess the effect of using the super-lines method to compute absorption cross-sections as a comparison to the effect of line-wing cut-off. Some line lists are very large and can contain billions of transitions between many millions of energy states. When computing cross-sections from such large line lists, studies such as Rey et al. (2016) and Yurchenko et al. (2017) have employed the so-called super-lines. The general principle is to first compute line intensities  $I_{ij}$  at a given temperature (i.e. stick spectra) and then to sum together the intensities of all lines within a specified spectral bin to create a so-called super-line. Thus super-lines are effectively temperature-dependent spectral histograms computed on a spectral grid. In order to ensure error transmission is kept to a minimum, a non-uniform grid of  $R = 1000000$  is typically used for the first step of the super-lines computations with a typical size of a few million grid points (super-lines) for each of the 20–30 temperatures used. A Voigt broadening profile is then applied to each of these super-lines. Since

the computation of the Voigt profile is the most expensive part of a simulation, this two-step procedure provides a huge reduction in the computation time.

The main source of error of the super-line procedure is that any dependence of the pressure broadening line profiles on the quantum numbers and molecular symmetry is ignored. This is because each super-line is a combination of multiple transitions connecting different states falling into the given spectroscopic bin.

Here we consider the high-resolution cross-sections computed for ExoMolOP (Chubb et al. 2021), prior to sampling down to sampled cross-sections or k-tables.<sup>8</sup> We compare the cross-sections of  $\text{SO}_2$ , using the ExoCross (Yurchenko, Al-Refaeie & Tennyson 2018) code with the ExoMol ExoAmes line list of Underwood et al. (2016), as an illustrative example, with and without using the super-lines method. The super-lines methods necessitate that average- $J$  rather than  $J$ -dependent broadening parameters are used.

The  $\text{SO}_2$  line list of Underwood et al. (2016) contains 1.4 billion transitions between 3.3 million ro-vibrational energy levels and covers up to  $8000\text{ cm}^{-1}$  (down to  $1.25\text{ }\mu\text{m}$ ).

We use average broadening parameters (i.e. not  $J$ -dependent) for the super-lines method, compared to  $J$ -dependent broadening parameters extracted from the HITRAN data base (Gordon et al. 2022) for the broadening of  $\text{SO}_2$  by  $\text{H}_2$  and  $\text{He}$ . A fixed line wing cut-off of  $25\text{ cm}^{-1}$  was used for both the super-lines and the standard non-super-lines methods. A variable grid spacing is used to try and ensure at least four sampling points for each line, with a maximum separation of  $0.01\text{ cm}^{-1}$ .

<sup>8</sup>The general principle of k-tables is to order spectral lines within a given spectral bin, producing a smooth cumulative distribution function to represent opacity. This smooth distribution can be more efficiently sampled, allowing k-tables to reach comparable accuracy as sampled cross-sections for a much smaller  $R = \frac{\lambda}{\delta\lambda}$ .



**Table 2.** Mean absolute percentage error (MAPE) of the super-lines versus non-super-lines method for computing cross-sections of SO<sub>2</sub> for a selection of pressures and temperatures.

Temperature (K)	Pressure (bar)	MAPE (per cent)
1500	1	$7.8 \times 10^{-4}$
1500	$1 \times 10^{-2}$	0.09
1500	$1 \times 10^{-5}$	0.18
1000	1	$5.90 \times 10^{-3}$
1000	$1 \times 10^{-2}$	0.21
1000	$1 \times 10^{-5}$	0.83
500	1	0.03
500	$1 \times 10^{-2}$	0.03
500	$1 \times 10^{-5}$	6.34

To compute the mean absolute percentage error (MAPE), we use the metric of equation (3). Here we take the non-super-lines approach as the actual value, where we also use a fixed line wing cut-off of  $25 \text{ cm}^{-1}$ . We focus on the region  $1300\text{--}1400 \text{ cm}^{-1}$  ( $7.1\text{--}7.7 \mu\text{m}$ ). The MAPE value between the non-super-lines and the super-lines method for a selection of pressures and temperatures using SO<sub>2</sub> as an example is summarized in Table 2.

It can be seen that the error increases with lower pressures and temperatures, where the lines are narrower than at higher pressures and temperatures. An example of cross-sections of SO<sub>2</sub> computed using the two methods at 500 K and  $1 \times 10^{-5}$  bar can be seen in Fig. 6.

The cross-sections computed using the super-lines technique (which necessitates the use of average- $J$  broadening parameters) have negligible differences when compared to those computed without, while they have a huge saving in efficiency. This is particularly true for large line lists with many millions of levels and billions of transitions. The differences appear to be much smaller than the typical differences found between using different wing cut-off methods. The latter is illustrated by Fig. 4.

We assess that cross-sections computed with the use of super-lines are appropriate for low- to mid-resolution applications, such as modelling *JWST* observations. As long as each of the super-lines is adequately sampled then the overall opacity will largely be conserved.

## 6 OUR RECOMMENDATION FOR CHOOSING THE WING CUT-OFF

The scope of our paper does not encompass resolving current challenges such as line mixing, non-Lorentzian behaviour, or inaccuracies in various Voigt algorithms. Our primary objective is to establish a standardized approach for opacity calculations within the exoplanetary and astrophysical communities, specifically focusing on wing cutoffs. For the systems where the empirical parametrizations of far-wing exist, they should be used, although one has to be aware that there is still room for improvement. Further theoretical studies and spectroscopic measurements are still required to create comprehensive insights into the physics of the far wings across the pressure regime and within the different mixtures of atmospheric gases that have not been studied yet. However, given the different scenarios, we examined in Figs 3–5, we propose the following method, assuming a Voigt profile, to calculate the wing cut-off for these pressure ranges:

$$R_{\text{cut,Abs}} = \begin{cases} 25 \text{ cm}^{-1} & \text{for } P \leq 200 \text{ bar} \\ 100 \text{ cm}^{-1} & \text{for } P > 200 \text{ bar} \end{cases} \quad (4)$$

This method is chosen for the following reasons :

(i) For intermediate pressures and high wavenumber ( $>5000 \text{ cm}^{-1}$ ), the two common methods in equations (1) and (2) are in a very good agreement. However, for very low pressures ( $<10^{-1}$ ) and for some spectral ranges, they result in some disagreement as shown in Figs 3–5. At low pressures, the Voigt HWHM is  $<0.01 \text{ cm}^{-1}$  (see Fig. 2) and the values calculated using 2 are physically small, therefore using fixed values is beneficial.

(ii) For very high pressure i.e.  $>200$  bars, the Voigt HWHM is more than  $20 \text{ cm}^{-1}$  and so to model the core of the line profile and a part of the wing, an absolute value of  $100 \text{ cm}^{-1}$  is proposed. It is worthwhile to note that this value might seem very small for  $P > 1000$  bar, but the lack of sufficient thermodynamics and spectroscopic studies in this high-pressure regime forced us to conservatively choose this number of  $100 \text{ cm}^{-1}$  (see Section 4.1).

(iii) A line wing of  $25 \text{ cm}^{-1}$  is typically used for calculations of terrestrial radiative transfer (Mlawer et al. 2012). Hence, our proposed method is very well aligned with the planetary community and could be utilized for their modelling studies as well.

## 7 INSTRUCTION ON HOW TO CONTROL $R_{\text{CUT}}$

The pre-generated ACS data in the current version of MAESTRO were computed using HAPI and ExoCross codes. Hence, you can see a short description on how to control the  $R_{\text{cut}}$  in these tools.

### 7.1 HAPI

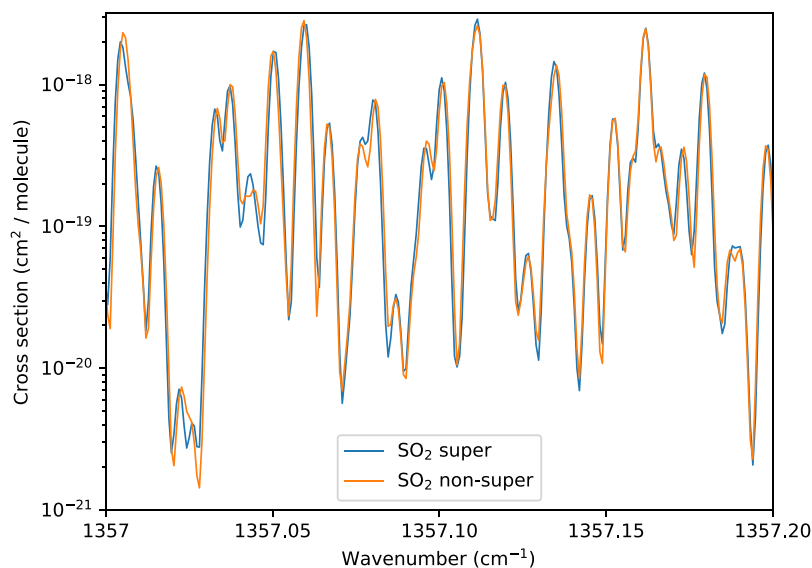
The HITRAN Application Programming Interface (HAPI) (Kochanov et al. 2016) is a set of Python libraries that allow users to download the HITRAN data and carry out different calculations, including absorption cross-sections, emission, transmission, etc. HAPI has a number of line shape functions, and complex probability functions implemented. The users can select among these functions or provide their own. One can also specify the wing cut-off. Although the default value is  $50 \text{ HWHM}$ , for the applications to planetary atmospheres under pressures encountered in the terrestrial atmosphere, it is recommended to use  $25 \text{ cm}^{-1}$ . Going outside of the terrestrial conditions, one can implement user-defined functions on a case-by-case basis. We will implement recommendations from this paper in future HAPI distributions. In any case, the flexibility of the open-source code gives all power to the user to implement different line shape functions.

### 7.2 ExoCross

ExoCross (Yurchenko et al. 2018) is a Fortran 2003 open-source program to compute spectra of molecules developed and maintained by the ExoMol project (Tennyson et al. 2020). ExoCross provides several line profiles as well as algorithms to compute them. Apart from the main-stream algorithm by Humlíček (1979), two fast Voigt methods are also provided in ExoCross: an approximated vectorized Voigt and a binned Voigt profile with analytical integrals. Different line profiles can be easily implemented in ExoCross.

The default wing cut-off value is  $25 \text{ cm}^{-1}$  which however can be changed by the user. A python version of ExoCross, PyExoCross<sup>9</sup> has also recently been developed (Zhang, Tennyson & Yurchenko, in preparation) and treats the wing cut-offs similarly.

<sup>9</sup><https://pyexocross.readthedocs.io/en/latest/index.html>



**Figure 6.** An example of cross-sections of  $\text{SO}_2$  computed using ExoCross (Yurchenko et al. 2018), with the super-lines method compared to without, at 500 K and  $1 \times 10^{-5}$  bar. See Section 5.3 for further details.

## 8 CONCLUSIONS

The main goal of this study is to provide a standard method for controlling the spectral line wing cut-off. Inconsistencies, potential inaccuracies/biases, and the lack of necessary theoretical studies or laboratory measurements are reviewed in this work to highlight the difficulties involved in implementing line shapes and wing cut-off relevant to modelling extrasolar atmospheres.

The generated absorption cross-sections can be very sensitive to the choice of wing cut-off, particularly in certain pressure and temperature ranges across the wavelength space. With the incredible advancements in space exploration over the last decade and a large number of detected exoplanets and brown dwarfs, it is crucial to utilize accurate and standardized cross-sections across different research groups. Our main objective in this study is to promote consistency in atmospheric modelling results by recommending a ‘standard’ and ‘default’ method for the wing cut-off. The recommendations and discussions provided here aim to provide insights into the applications of the MAESTRO data base, but they are also valid and applicable across the fields of astronomy and spectroscopy.

Given the spectral parameters, the simulation of a spectrum has a number of other complications, most are associated with the line shape. Some molecules exhibit line-coupling effects (or line-mixing effects), which can greatly change the simulated spectra. There are theoretical models for each mechanism. However, the main challenge to simulate a spectrum is the choice of a line-shape model. Most of the line-shape data on HITRAN is for the Lorentz profile; in applications, this is coupled with Doppler broadening to create the Voigt profile. The suggested model is the Hartmann–Tran Profile (Tran, Ngo & Hartmann 2013, 2014; Tennyson et al. 2014), but little data are available, especially for large-scale simulations. There are parameters available for a small number of transitions for other more sophisticated line-shape models.

The lack of pressure broadening data for pressure and temperature ranges relevant to exo-atmospheres is another issue. Most laboratory spectroscopic measurements are limited to Terrestrial and Jovian atmospheric temperature ranges ( $\leq 350$  K) and up to a few tens of bars. At high pressures, the assumption of the Voigt profile (binary

collisions between absorbers and broadeners) is not valid, and more sophisticated line shapes are required to account for non-binary collisions and the intensive interactions that exist between these species.

Therefore, for now, we recommend the default or standard practice, in particular with regards to the MAESTRO (Molecules and Atoms in Exoplanet Science: Tools and Resources for Opacities) data base, to be the use of a Voigt profile with a line-wing cut-off of  $25 \text{ cm}^{-1}$  for pressures of 200 bar or less, and  $100 \text{ cm}^{-1}$  for pressures above 200 bar. Our main reasons for this choice are outlined in Section 6. We hope future theoretical and laboratory work will facilitate more precise line profiles for a wide range of species, which can, in turn, be easily implemented in codes to compute cross-sections and thus included in future releases of MAESTRO. Having a current ‘standard’ or ‘default’ recommendation will at least allow for a consistency and thus fair comparison between different studies. Such a comparison is particularly important for the open-access MAESTRO data base, as it will allow for an easier peer review process<sup>10</sup> for allowing community contributions of opacity data.

## ACKNOWLEDGEMENTS

*Author contributions:* All authors have contributed equally to this study.

NB and EGN both acknowledge support from the NASA Astrophysics Division. EGN, NB, and BG acknowledge support from the NASA XRP funding NNH21ZDA001N-XRP. NEB, NKL, IEG, RJH et al. MAESTRO Grant (NASA Grant Number 80NSSC19K1036). KLC acknowledges funding from STFC under project number ST/V000861/1. SNY and JT acknowledge supported by the European Research Council (ERC) under the European Union’s Horizon 2020 research and innovation programme through Advance Grant number 883830 (ExoMolHD). We also would like to thank the anonymous reviewers for their insightful comments.

<sup>10</sup>[github.com/maestro-opacities/submit-data](https://github.com/maestro-opacities/submit-data)

**Software:** HAPI (Kochanov et al. 2016); ExoCross (Yurchenko et al. 2018) which is available from <https://github.com/ExoMol/ExoCross>.

## DATA AVAILABILITY

The data underlying this article will be shared on reasonable request to the corresponding author.

## REFERENCES

- Almodovar C. A., Su W.-W., Choudhary R., Shao J., Strand C. L., Hanson R. K., 2021, *J. Quant. Spectrosc. Radiat. Transfer*, 276, 107935
- Anisman L. O., Chubb K. L., Elsey J., Al-Refai A., Changeat Q., Yurchenko S. N., Tennyson J., Tinetti G., 2022, *J. Quant. Spectrosc. Radiat. Transfer*, 278, 108013
- Burch D. E., Gryvnak D. A., 1971, *J. Opt. Soc. Am.*, 61, 499
- Burch D. E., Williams D., 1962, *Appl. Opt.*, 1, 587
- Burch D. E., Howard J. N., Williams D., 1956, *J. Opt. Soc. Am.*, 46, 452
- Burch D. E., France W. L., Williams D., 1963, *Appl. Opt.*, 2, 585
- Burch D. E., Gryvnak D. A., Patty R. R., 1967, *J. Opt. Soc. Am.*, 57, 885
- Burch D. E., Gryvnak D. A., Patty R. R., 1968, *J. Opt. Soc. Am.*, 58, 335
- Chubb K. L. et al., 2021, *A&A*, 646, A21
- Clough S. A., Kneizys F. X., Rothman L. S., Gallery W. O., 1981, in Tescher A. G., Ebrahimi T., eds, Proc. SPIE Conf. Ser. Vol. 0277, Atmospheric Transmission. SPIE, Bellingham, p. 152
- Clough S. A., Kneizys F. X., Davies R. W., 1989, *Atmos. Res.*, 23, 229
- Clough S. A., Shephard M. W., Mlawer E. J., Delamere J. S., Iacono M. J., Cady-Pereira K., Boukabara S., Brown P. D., 2005, *J. Quant. Spectrosc. Radiat. Transfer*, 91, 233
- Cole R. K., Tran H., Hoghooghi N., Rieker G. B., 2023, *J. Quant. Spectrosc. Radiat. Transfer*, 297, 108488
- Delahaye T. et al., 2021, *J. Mol. Spectrosc.*, 380, 111510
- Fortney J. J., Marley M. S., Lodders K., Saumon D., Freedman R., 2005, *ApJ*, 627, L69
- Fortney J. J. et al., 2019, Astro2020: Decadal Survey on Astronomy and Astrophysics, 200, 146
- Freedman R. S., Lustig-Yaeger J., Fortney J. J., Lupu R. E., Marley M. S., Lodders K., 2014, *ApJS*, 214, 25
- Fu Y., Borysow A., Moraldi M., 1996, *Phys. Rev. A*, 53, 201
- Gamache R. R., Laraia A. L., 2009, *J. Mol. Spectrosc.*, 257, 116
- Gamache R. R., Rey M., Vispoel B., Tyuterev V. G., 2019, *J. Quant. Spectrosc. Radiat. Transfer*, 235, 31
- Gharib-Nezhad E., Line M. R., 2019, *ApJ*, 872, 27
- Gharib-Nezhad E., Iyer A. R., Line M. R., Freedman R. S., Marley M. S., Batalha N. E., 2021a, *ApJS*, 254, 34
- Gharib-Nezhad E., Marley M. S., Batalha N. E., Visscher C., Freedman R. S., Lupu R. E., 2021b, *ApJ*, 919, 21
- Gordon I. et al., 2022, *J. Quant. Spectrosc. Radiat. Transfer*, 277, 107949
- Grimm S. L., Heng K., 2015, *ApJ*, 808, 182
- Grimm S. L. et al., 2021, *ApJS*, 253, 30
- Gunson M. R. et al., 1996, *Geophys. Res. Lett.*, 23, 2333
- Hartmann J.-M., Boulet C., Brodbeck C., 2002, *J. Quant. Spectrosc. Radiat. Transfer*, 72, 117
- Hartmann J.-M., Boulet C., Robert D., 2008, Collisional Effects on Molecular Spectra: Laboratory Experiments and Models, Consequences for Applications. Elsevier Science, Amsterdam
- Hashemi R. et al., 2020, *J. Quant. Spectrosc. Radiat. Transfer*, 256, 107283
- Hashemi R. et al., 2021, *J. Quant. Spectrosc. Radiat. Transfer*, 271, 107735
- Hedges C., Madhusudhan N., 2016, *MNRAS*, 458, 1427
- Hill C., Yurchenko S. N., Tennyson J., 2013, *Icarus*, 226, 1673
- Hood C. E., Fortney J. J., Line M. R., Faherty J. K., 2023, *ApJ*, 953, 170
- Humlíček J., 1979, *J. Quant. Spectrosc. Radiat. Transfer*, 21, 309
- Hussey T., Dufty J. W., Hooper C. F., 1975, *Phys. Rev. A*, 12, 1084
- Iyer A. R., Line M. R., Muirhead P. S., Fortney J. J., Gharib-Nezhad E., 2023, *ApJ*, 944, 41
- JWST Transiting Exoplanet Community Early Release Science Team 2023, *Nature*, 614, 649
- Kochanov R. V., Gordon I. E., Rothman L. S., Wcislo P., Hill C., Wilzewski J. S., 2016, *J. Quant. Spectrosc. Radiat. Transfer*, 177, 15
- Lamouroux J., Tran H., Laraia A. L., Gamache R. R., Rothman L. S., Gordon I. E., Hartmann J.-M., 2010, *J. Quant. Spectrosc. Radiat. Transfer*, 111, 2321
- Lamouroux J., Gamache R., Schwenke D., 2014, *J. Quant. Spectrosc. Radiat. Transfer*, 148, 49
- Letchworth K. L., Benner D. C., 2007, *J. Quant. Spectrosc. Radiat. Transfer*, 107, 173
- Lévy A., Lacombe N., Chackerian C., 1992, in Rao K. N., Weber A., eds, Spectroscopy of the Earth's Atmosphere and Interstellar Medium. Academic Press, Cambridge, MA, p. 261
- Lothringer J. D., Barman T., Koskinen T., 2018, *ApJ*, 866, 27
- Ma Q., Tipping R. H., 1990a, *J. Chem. Phys.*, 93, 7066
- Ma Q., Tipping R. H., 1990b, *J. Chem. Phys.*, 93, 6127
- Ma Q., Tipping R. H., 1991, *J. Chem. Phys.*, 95, 6290
- Ma Q., Tipping R. H., 1992, *J. Chem. Phys.*, 96, 8655
- Ma Q., Tipping R. H., 1994, *J. Quant. Spectrosc. Radiat. Transfer*, 51, 751
- Ma Q., Tipping R. H., Boulet C., Bouanich J.-P., 1999, *Appl. Opt.*, 38, 599
- MacDonald R. J., 2019, PhD thesis, University of Cambridge, UK
- McClatchey R., Benedict W., Clough S., Burch D., Calfee R., Fox K., Rothman L., Garing J., 1973, *Environ. Res. Papers*, 434, 1
- Meadows V. S., Crisp D., 1996, *J. Geophys. Res.*, 101, 4595
- Miles B. E. et al., 2023, *ApJ*, 946, 6
- Mlawer E. J., Payne V. H., Moncet J.-L., Delamere J. S., Alvarado M. J., Tobin D. C., 2012, *Phil. Trans. R. Soc. A: Math. Phys. Eng. Sci.*, 370, 2520
- Mollière P., Wardenier J. P., van Boekel R., Henning T., Molaverdikhani K., Snellen I. A. G., 2019, *A&A*, 627, A67
- Mukherjee S., Batalha N. E., Fortney J. J., Marley M. S., 2023, *ApJ*, 942, 71
- Ngo N., Lisak D., Tran H., Hartmann J.-M., 2013, *J. Quant. Spectrosc. Radiat. Transfer*, 129, 89
- Ngo N., Lin H., Hodges J., Tran H., 2017, *J. Quant. Spectrosc. Radiat. Transfer*, 203, 325
- Niraula P., de Wit J., Gordon I. E., Hargreaves R. J., Sousa-Silva C., Kochanov R. V., 2022, *Nat. Astron.*, 6, 1287
- Niraula P., de Wit J., Gordon I. E., Hargreaves R. J., Sousa-Silva C., 2023, *ApJ*, 950, L17
- Olivero J., Longbothum R., 1977, *J. Quant. Spectrosc. Radiat. Transfer*, 17, 233
- Pieroni D., Hartmann J.-M., Camy-Peyret C., Jeseck P., Payan S., 2001, *J. Quant. Spectrosc. Radiat. Transfer*, 68, 117
- Pollack J. B. et al., 1993, *Icarus*, 103, 1
- Ren T., Han Y., Modest M. F., Fateev A., Clausen S., 2023, *J. Quant. Spectrosc. Radiat. Transfer*, 302, 108555
- Rey M., Nikitin A. V., Babikov Y. L., Tyuterev V. G., 2016, *J. Mol. Spectrosc.*, 327, 138
- Rothman L. et al., 2010, *J. Quant. Spectrosc. Radiat. Transfer*, 111, 2139
- Sharp C. M., Burrows A., 2007, *ApJS*, 168, 140
- Sharpe S. W., Johnson T. J., Sams R. L., Chu P. M., Rhoderick G. C., Johnson P. A., 2004, *Appl. Spectrosc.*, 58, 1452
- Shine K. P., Campargue A., Mondelain D., McPheat R. A., Ptashnik I. V., Weidmann D., 2016, *J. Mol. Spectrosc.*, 327, 193
- Showman A. P., Guillot T., 2002, *A&A*, 385, 166
- Simonova A. A., I. V. Ptashnik, Elsey J., McPheat R. A., Shine K. P., Smith K. M., 2022, *J. Quant. Spectrosc. Radiat. Transfer*, 277, 107957
- Smith H., Dube D., Gardner M., Clough S., Kneizys F., 1978, Tech. rep. Fascade-Fast Atmospheric Signature Code (Spectral Transmittance and Radiance). Visidyne Inc, Burlington, MA
- Sung K. et al., 2019, *J. Quant. Spectrosc. Radiat. Transfer*, 235, 232
- Tan Y., Skinner F. M., Samuels S., Hargreaves R. J., Hashemi R., Gordon I. E., 2022, *ApJS*, 262, 40
- Tennyson J. et al., 2014, *Pure Appl. Chem.*, 86, 1931

- Tennyson J. et al., 2020, *J. Quant. Spectrosc. Radiat. Transfer*, 255, 107228
- Thorngren D., Gao P., Fortney J. J., 2019, *ApJ*, 884, L6
- Tran H., Ngo N. H., Hartmann J.-M., 2013, *J. Quant. Spectrosc. Radiat. Transfer*, 129, 199
- Tran H., Ngo N. H., Hartmann J.-M., 2014, *J. Quant. Spectrosc. Radiat. Transfer*, 134, 104
- Tran H., Vander Auwera J., Bertin T., Fakhardji W., Pirali O., Hartmann J.-M., 2022, *Icarus*, 384, 115093
- Underwood D. S., Tennyson J., Yurchenko S. N., Huang X., Schwenke D. W., Lee T. J., Clausen S., Fateev A., 2016, *MNRAS*, 459, 3890
- Wcislo P. et al., 2016, XVIIIth Symposium on High Resolution Molecular Spectroscopy (HighRus-2015), Vol. 177. Tomsk, Russia, p. 75
- Yurchenko S. N., Amundsen D. S., Tennyson J., Waldmann I. P., 2017, *A&A*, 605, A95

- Yurchenko S. N., Al-Refai A. F., Tennyson J., 2018, *A&A*, 614, A131
- Zhang M. et al., 2020, *ApJ*, 899, 27

## SUPPORTING INFORMATION

Supplementary data are available at *RASTAI* online.

### suppl\_data

Please note: Oxford University Press is not responsible for the content or functionality of any supporting materials supplied by the authors. Any queries (other than missing material) should be directed to the corresponding author for the article.

This paper has been typeset from a  $\text{\TeX/L\AA\TeX}$  file prepared by the author.