Planet gap-opening feedback on disc thermal structure and composition

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ABSTRACT
(Exo-)planets inherit their budget of chemical elements from a protoplanetary disc. The disc temperature determines the phase of each chemical species, which sets the composition of solids and gas available for planet formation. We investigate how gap structures, which are widely seen by recent disc observations, alter the thermal and chemical structure of a disc. Planet–disc interaction is a leading hypothesis of gap formation and so such changes could present a feedback that planets have on planet-forming material. Both the planet gap-opening process and the disc thermal structure are well studied individually, but how the gap-opening process affects disc thermal structure evolution remains an open question. We develop a new modelling method by iterating hydrodynamical and radiative transfer simulations to explore the gap-opening feedback on disc thermal structure. We carry out parameter studies by considering different planet locations $r_p$ and planet masses $M_p$. We find that for the same $r_p$ and $M_p$, our iteration method predicts a wider and deeper gap than the non-iteration method. We also find that the inner disc and gap temperature from the iteration method can vary strongly from the non-iteration or disc without planets, which can further influence dust-trap conditions, iceline locations, and distribution of various ices, such as H$_2$O, CO$_2$, and CO on large dust grains (‘pebbles’). Through that, a gap-opening planet can complicate the canonical picture of the non-planet disc C/O ratio and influence the composition of the next generation of planetesimals and planets.

Key words: hydrodynamics – radiative transfer – planets and satellites: composition – planet–disc interactions – protoplanetary discs.

1 INTRODUCTION
Chemical element abundance ratios in planets, and in comets or asteroids, are determined by the chemical composition and physical–chemical evolution of the protoplanetary disc they form in. The study of chemical element abundance ratios such as C/O (Oberg, Murray-Clay & Bergin 2011; Madhusudhan, Amin & Kennedy 2014) or N/S (Turrini et al. 2021) may allow to connect planetary bodies to their formation history, which is important for understanding how the chemical diversity of planetary systems arises. The distribution of volatile chemical elements in the solid (dust, ice) and gas phases is set by the location of their icelines, which depend on the disc temperature structure. In this work, we employ hydrodynamical (HD) and radiative transfer (RT) models to study the feedback of planet-induced gaps on the temperature structure and hence the location of icelines.

ALMA observations have revealed that rings and gaps in the dust and gas components are common in protoplanetary discs (e.g. Andrews et al. 2018; Oberg et al. 2021). One possible and intriguing explanation for the formation of such substructures is embedded young planets in discs. Despite great efforts, very few protoplanets have been detected in discs by direct imaging (Kepler et al. 2018, 2019; Haffert et al. 2019; Benisty et al. 2021; Currie et al. 2022; Hammond et al. 2023). Direct imaging is, however, biased towards super-Jupiter mass protoplanets, whereas most gaps may be due to lower mass giant planets. Their masses can be inferred from the gap structure or gas kinematics (e.g. Teague et al. 2018; Zhang et al. 2018). Alternative scenarios to explain gaps and rings without planets have also been proposed, such as secular gravitational instabilities (Takahashi & Inutsuka 2014), dust evolution (Birnstiel et al. 2015), zonal flows (Flock et al. 2015), and icelines (Zhang, Blake & Bergin 2015).

A gap in the disc implies a reduced optical depth in a radially confined region. This allows shorter wavelength photons to penetrate deeper and heat the disc mid-plane, as well as the edges of the gap, so gaps potentially affect the disc temperature structure. An opposite, cooling effect may result from fewer photons being scattered by dust towards the mid-plane. The balance of these effects around a given dust gap can be studied with Monte Carlo radiative transfer (MCRT) models (Broome et al. 2023). Previous studies of temperature changes around gaps used analytically prescribed surface density profiles: Cleeves, Bergin & Harries (2015) explored the spatial distribution of molecular abundances resulting from increased heating due to an accreting protoplanet in a gap, while Broome et al. (2023) used MCRT to investigate the dust temperature structure around analytical gap profiles in a hydrostatic 1 + 1D disc model.

The temperature change caused by a gap can also affect the structure of the gap itself. HD simulations of planet–disc interactions

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and gap-opening processes assuming a locally isothermal equation of state (EoS) provide empirical formulas of gap depth and width (Fung, Shi & Chiang 2014; Kanagawa et al. 2015, 2016; Zhang et al. 2018; Duffell 2020). Recently, Miranda & Rafikov (2019, 2020) suggest that the assumptions of the EoS, locally isothermal or adiabatic assumptions, can affect the gap properties by altering the propagation of density waves. Additionally, Zhang & Zhu (2020) used simulations to show that the cooling time-scale can influence the gap profile.

Disc thermodynamics plays an important role in setting the location of different icelines in discs. An iceline of a specific location is where the temperature is low enough so that such molecules freeze out from the gas phase on to dust grains. Though direct measurements of the location of molecular icelines are rare in observations (e.g. water iceline, van ‘t Hoff et al. (2018); CO iceline, van ‘t Hoff et al. (2017); Zhang et al. (2017)), icelines can play an important role in planet formation. Across icelines, the gas composition and ice reservoirs for the planet and planetesimal formation are changed (e.g. Oberg, Murray-Clay & Bergin 2011), and the efficiency of planetesimal formation can increase at the water iceline (e.g. Stevenson & Lunine 1988; Schoonenberg & Ormel 2017). In addition, dust trapping is closely related to the planet gap-opening process, which in combination with the location of icelines determine the location of planetesimal formation and their composition. Dust trapping in local pressure maxima is proposed to overcome rapid dust loss due to radial drift by the drag between the gas and the dust in discs Whipple (1972). For example, Pinilla, Benisty & Birnstiel (2012b) demonstrated that the pressure bump outside the gaps opened by planets can trap dust and produced ring-like structures as observed.

Conventionally, previous studies on gap modelling or thermal structures in discs only conduct HD or RT simulations, or combine the final results from HD to RT simulations to compare with observations. However, as planets open gaps in discs, the temperature around gaps could deviate significantly from the temperature adopted for discs without planets. In the meantime, the temperature changes affect the disc gas scale height $H$ and volume density $\rho$ distribution.

In this paper, we build a new model to investigate the planet gap-opening process and the gap-opening feedback on disc thermal structure. Because the temperature controls which species can exist as solid ices, our model allows us to investigate the question: what is the feedback effect of giant planets on the composition of material subsequently accreted by the planets themselves, or by a new generation of forming planetesimals? In order to improve previous models, we first feed HD simulations with a more physical energy field from RT models. During the planet gap-opening process, we combine the HD and RT simulations together and iterate them. We implement the new temperature calculated by RT to correct the energy field of HD simulations.

This paper is organized as follows. In Section 2, we describe our modelling method of how we iterate the HD and RT simulations to study the gap-opening process. In Section 3, we present and quantify our modelling results of gap properties, disc temperature structure, and ice distributions. Section 4 discusses the impact of our results on disc composition, disc substructure observation, and the limits of our models. Section 5 summarizes the main conclusions of this paper.

## 2 Methods

In this section, we describe the codes and setup of our HD and RT simulations, as well as the workflow of how we iterate these two simulations to study the temperature structure of a disc with a gap-opening planet.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>$M_p$</td>
<td>$3M_J$, $1M_J$, $100M_\oplus$, $10M_\oplus$</td>
</tr>
<tr>
<td>$\alpha$</td>
<td>0.001</td>
</tr>
<tr>
<td>$r_i = r_p$ (au)</td>
<td>4, 10, 30</td>
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<tr>
<td>$r_{\mathrm{min}}$ (r$_p$)</td>
<td>0.25, 0.1, 0.033</td>
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<tr>
<td>$r_{\mathrm{max}}$ (r$_p$)</td>
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</tr>
<tr>
<td>Aspect ratio</td>
<td>0.04, 0.05, 0.066</td>
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<tr>
<td>$\Sigma_1$ (r$_p^2$)</td>
<td>1.8$^{-4}$, 4.5$^{-4}$, 1.34$^{-3}$</td>
</tr>
<tr>
<td>$N_\text{HD}$</td>
<td>580, 460, 350</td>
</tr>
<tr>
<td>$N_{\phi, \text{HD}}$</td>
<td>790, 630, 480</td>
</tr>
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### 2.1 Hydrodynamical Simulations

We conduct 2D HD simulations in polar coordinate ($r$, $\phi$) to study surface density evolution with FARGO3D (Benitez-Llambay & Masset 2016). The main parameters of FARGO3D simulations are shown in Table 1.

For grid setup, we conduct global disc simulations of a transition disc which extend from $r_{\mathrm{min}} = 1$ au to $r_{\mathrm{max}} = 100$ au. The global disc simulations for FARGO3D avoid the radial extrapolation of the sound speed $c_s$ setups for global disc RADMC-3D simulations. Such consideration is necessary, as the extrapolation could be impractical for a radially non-smooth $c_s$ field. We set up mesh grids linearly distributed in $\phi$ direction, and logarithmically distributed in $r$ direction. The grid numbers ($N_{\text{HD}, \phi}$, $N_{\text{phi, HD}}$) resolve the gas scale height at the location of the planet with at least 5 grid cells and make the grid cells square shape at the planet location. We also do convergence tests by doubling the resolution, finding that the gap depth variations are less than 20 per cent. So we keep on using the resolution in Table 1 to minimize simulation time during each iteration step.

Regarding the physical model setup, we only include gas in our simulations without dust and the radial initial gas density profile is $\Sigma_r = \Sigma_0(r/r_0)^{-1}$. We assume the whole disc mass is 0.028 $M_\odot$, which is a normal choice for solar-mass star (e.g. see review in Manara et al. 2022). The EoS is assumed locally isothermal and the flared disc is built with aspect ratio $H/r_\phi \propto r^{1/4}$. However, since we update $c_s$ for each iteration step as described in Section 2.3, we only use aspect ratios and flaring index as the initial conditions but do not need to use them at any later step of evolution. We adopt a Shakura & Sunyaev (1973) viscosity parameter $\alpha = 10^{-3}$. We use the scale-free parameter setup in FARGO3D which means $G, M_\ast, r_0 = 1$. Here, we set $r_0 = r_p$ and fix planets at circular orbits. The indirect term of potential is included in the simulations. The planets are introduced into discs from the beginning of the simulations without including any accretion on to the planets. We also examine introducing planets into a disc with a mass-taper function but find no significant difference in the results.

At the radial boundaries, we adopt power-law extrapolation densities and Keplerian extrapolation azimuthal velocities at both $r_{\mathrm{min}}$ and $r_{\mathrm{max}}$. In terms of radial velocities, we adopt an outflow inner boundary and a symmetric outer boundary. Periodic boundaries are imposed in the azimuthal direction.

### 2.2 Radiative transfer simulations

After obtaining the 2D $\Sigma_1$ and $c_s$ fields from FARGO3D simulations, we perform 3D MCRT with RADMC-3D (Dullemond et al. 2012) to obtain the temperature structure. The output gas temperature $T_{\text{gas}}$...
is used to update the corresponding $c_e$ field for FARGO3D (see Section 2.3). Within RADMC-3D simulations, all parameters are in units of cgs and the main parameters are shown in Table 2.

For grid cell setup, RADMC-3D keeps the same global transition disc simulation domain in $(r, \phi)$ direction as FARGO3D. The vertical domain is $\theta = [\pi/2 - 0.5, \pi/2]$ with mirror symmetry along the mid-plane. The azimuthal and vertical directions are sampled in linear space, while the radial direction is sampled in logarithmic space. We test different combinations of grid resolutions and decide $(N_r, N_\phi, N_z) = (256, 30, 53)$ in radial, vertical, and azimuthal directions is a proper resolution for using $N_{\text{photon}} = 10^8$ photon packages. For small $N_r$, $N_\phi$, the asymmetry temperature feature in discs due to eccentric gaps is not recovered properly. For larger $N_r$, $N_\phi$, the $T_{\text{mid}}$ map gets bad photon statistics and it is noisy unless we adopt a larger number of photons $N_{\text{photon}} > 10^9$, which takes more than 10 h with parallelising 40 threads for just one iteration step. Also, $N_{\text{photon}} = 10^8$ gets similar smooth temperature results as $N_{\text{photon}} > 10^9$ with more grid cells. Hence, we keep $N_{\text{photon}} = 10^9$ for all the simulations presented in this paper. After RADMC-3D, we interpolate the values in RADMC-3D grid cells to match the $(r, \phi)$ grid cells in FARGO3D.

For the stellar parameters, we adopt typical values for a T Tauri star, $M_* = 1 M_\odot$, $R_* = 1.7 R_\odot$, and $T_* = 4730$ K. We only consider stellar radiation as the heating source and ignore viscous heating. We assume silicate dust particles with isotropic scattering and the intrinsic density is 3.710 g cm$^{-3}$. We also assume dust-to-gas mass ratio $\epsilon = 0.01$ and dust grain size of 0.1 $\mu$m. As the small dust grains couple well to the gas, we do not assume any dust settling. Also, we do not consider any dust evolution process, such as dynamics, growth, or fragmentation of particles (Birnstiel, Dullemond & Brauer 2010). The disc density distribution in three dimensions is assumed to be

$$\rho_d(r, z, \phi) = \frac{\Sigma_d(r, \phi)}{\sqrt{2\pi} H(r)} \exp\left(-\frac{z^2}{2H(r)^2}\right)$$  \hspace{1cm} (1)$$

where $\Sigma_d(r, \phi)$ is the dust surface density and $\Sigma_d(r, \phi) = \epsilon \Sigma_g(r, \phi)$. $H(r)$ is the gas pressure scale height and $z = r \tan \theta$.

### 2.3 Workflow

Our iterative approach makes use of FARGO3D and RADMC-3D codes. The workflow of our iteration method is illustrated in Fig. 1. The green, blue, and yellow boxes represent the steps of FARGO3D, RADMC-3D, and post-processing from RADMC-3D to FARGO3D, respectively. Our methodology consists of the following steps:

**Step 1:** We set up our initial physical disc models without planets by assuming azimuthal symmetric 1D gas surface density $\Sigma_g(r)$ and aspect ratio $H/r$ of the discs (shown in Box(1)). Then, we output FARGO3D results of 0 orbit to obtain initial 2D $\Sigma_g(r, \phi)$ and sound speed $c_s(r, \phi)$ map. Note that the energy field outputs in FARGO3D simulations in this paper are actually the isothermal $c_e$.

**Step 2:** 2D surface density field from FARGO3D are read by RADMC-3D and extend to 3D volume density by following equation (1), where the scale height $H$ is calculated from FARGO3D $c_e$ field. Then the dust RT simulations are conducted (Box (2)),

![Diagram](https://example.com/diagram.png)

**Figure 1.** The workflow of the iteration method. The green, blue, and yellow boxes represent the steps of FARGO3D, RADMC-3D, and post-processing between RADMC-3D and FARGO3D, respectively. The iteration step is 100 planet orbits.
the output of the dust temperature $T_{\text{dust}}(r, \theta, \phi)$ is obtained. As RADMC-3D does not include any photochemistry simulations, we assume $T_{\text{gas}}(r, \theta, \phi) = T_{\text{dust}}(r, \theta, \phi)$. From $T_{\text{dust}}(r, \theta, \phi)$, the mid-plane temperature $T_{\text{mid}}(r, \phi)$ can be obtained (Box (3)). Using this RADMC-3D temperature as the non-planet disc temperature can help us to get rid of the initial temperature profile assumption in FARGO3D. In fact, such a step is also done in fig. 6(a) in Bae et al. (2019) to get the first MCRT temperature, which aims to get rid of the assumed stellar irradiation-dominated temperature $T_{ir}$. We also test the iteration process (assuming vertical hydrostatic equilibrium) described in appendix A in Bae et al. (2019) to get the multiple iteration MCRT temperature but the differences between the first MCRT temperature and multi-time MCRT temperature in our disc model are negligible. This MCRT iteration process makes no difference in our case but at least doubles our MCRT workload and costs much more computation time. So we directly use our RADMC-3D temperature for later steps.

**Step 3:** By using the $T_{\text{mid}}(r, \phi)$ from the last step, we could infer a new $c_s$ field by assuming a vertical isothermal approximation. Even though we still use the isothermal assumption here, because of the non-smooth $T_{\text{mid}}(r, \phi)$ reflecting the gap-opening process, such new $c_s$ does not equal the initial isothermal $c_{s0}$ anymore. The new $c_s$ is treated as the new gasenergy.dat file for the next FARGO3D run (Box 4). This is the important step that moves beyond the isothermal assumption in the conventional non-iteration method and shows the feedback effect of the gap-opening process. In Appendix B, we have a test to compare a vertical density weighted temperature with $T_{\text{mid}}$. We find that they are similar, especially in gap regions. For simplicity, we use $T_{\text{mid}}$ in this paper. Next, we restart the FARGO3D simulation and evolve it over 100 orbital times (we assume the iteration step is 100 orbit here) (Box (5)) and as a result, we get the output as Box(6).

Again, during the FARGO3D step, the EoS is assumed isothermal. Malygin et al. (2017) and Pfeil & Klahr (2019) demonstrate that the thermal relaxation time varies across the disc, and in some regions, there is large cooling time ($>100$ local orbits), where our iteration time is a good approximation. However, in some outer disc regions, like a few tens of au, (the specific regions depend on the model conditions) have short cooling time, where our choice of 100 orbits can be too long. As a test, we performed simulations with iteration steps of 50 orbits in Appendix A, and found no difference with the 100 orbits case. We also test iteration step of 100 orbits against 500 orbits in Appendix A, which do not converge very well in gap regions. It means the iteration step of 500 orbits could not replace 100 orbits. For these reasons, we keep 100 orbits for all the main simulations of this work.

**Step 4:** The result of 100 orbit FARGO3D is used as the input for RADMC-3D (Box(7)). During the RADMC-3D setup, the gas pressure scale height $H$ is given by the FARGO3D $c_s$, $H = c_s/\Omega$. Therefore, the extension of 2D $\Sigma_{\text{gas}}$ to 3D volume density $\rho$ [shown as equation (1)] can be also modified by the gap-opening feedback.

**Step 5:** Repeat Step 2 to Step 4 and iterate until reaching a quasi-steady state, which also means the iteration process is from Box(2) to Box(7). We iterate all the simulations over 2000 planet orbital time which corresponds to $1.6 \times 10^7$ yr for $r_p = 4$ au, $6.4 \times 10^8$ yr for $r_p = 10$ au, $3.3 \times 10^9$ yr for $r_p = 30$ au, respectively.

In summary, there is density and velocity evolution but no energy/$c_s$ evolution over time in HD simulations, while the energy/$c_s$ field is evolved by executing RT simulations. Meanwhile, the evolving $c_s$ field contains the information from the gap-opening feedback. As a comparison, in this paper, the conventional non-iteration method is running FARGO3D then RADMC-3D simulation once. To be more specific, non-iteration uses FARGO3D with the physical assumptions (initial isothermal $c_s$) in Box(1) to obtain $\Sigma_{\text{g}}$. Then input this $\Sigma_{\text{g}}$ into RADMC-3D to get the temperature $T_{\text{mid}}$. The whole process is finished after doing this once.

### 3 Results

In this section, we describe the results of our simulations, and compare the results between the iteration and non-iteration methods.

#### 3.1 Gas Surface Density

Based on Step 3 in the iteration workflow described in Section 2.3, we can obtain the surface density in discs. From left to right columns, Fig. 2 shows the 2D gas surface density maps of gaps opened by planets at 2000 orbits in masses of $3M_J$, $1M_J$, $100M_\oplus$, and $10M_\oplus$ at orbital radii of 4 au. The iteration and non-iteration results are presented in upper and lower panels, respectively. The gaps from the iteration method are generally deeper and wider than their counterparts simulated by the non-iteration method.

As gap structures are shown in most simulations, we quantify the gap width and depth from the data of surface density and compare iteration with the non-iteration models. In this work, we define the gap width $\Delta_{\text{gap}}$ with the method in Kanagawa et al. (2016) which is the radial region where $\Sigma_{\text{gap}}/\Sigma_0 \leq 0.5$. Meanwhile, we define the gap depth $\Sigma_{\text{gap}}/\Sigma_0$ as that in Fung, Shi & Chiang (2014) which is the radial averaging value within $2 \times \max(R_H, H)$ of the planet, where $R_H$ and $H$ are hill radius and scale height at $r_p$. Both the gap width and gap depth are obtained by azimuthal averaging and the last 500-orbit averaging.

Fig. 3 displays the comparison of the normalized gap width $\Delta_{\text{gap}}/r_p$ (green) and gap depth $\Sigma_{\text{gap}}/\Sigma_0$ (blue) as a function of $M_p$ of iteration (dashed lines) and non-iteration (solid lines) methods. From top to bottom panels, $r_p = 4, 10, 30$ au, respectively. Uncertainty of gap depths and widths are also shown, which come from time averaging of the last 500 orbits. The choice of final 500 orbits is because our simulations appear to reach quasi-steady states at around 1500 orbits though gap depth and gap eccentricity are still slightly fluctuating. Under the definition of gap width and gap depth here, $M_p = 10 M_\oplus$ cannot open gaps except for $r_p = 4$ au of iteration. With regard to the $\Sigma_{\text{gap}}/\Sigma_0$ of non-iteration method, we find them consistent with the empirical formulas in Fung, Shi & Chiang (2014) except the eccentric case caused by $M_p = 3M_J$. In general, the iteration method infers a slightly wider gap width $\Delta_{\text{gap}}$ than the non-iteration method, whereas iteration predicts an order of magnitude deeper gap depth $\Sigma_{\text{gap}}/\Sigma_0$ than non-iteration. The reason for the deeper gap in iteration is the aspect ratio $H/r$ at the gap region is smaller than the non-iteration. Based on equation (3) in Fung, Shi & Chiang (2014), a lower $H/r$ lead to a smaller $\Sigma_{\text{gap}}$. As the iteration method predicts a deeper gap than the non-iteration method, which means a lower mass planet can possibly open a deep gap. For instance, in Fig. 3(a), when $r_p = 4$ au, the iteration predicts that a Saturn mass planet can open a gap as deep as a Jupiter-mass planet in the non-iteration method. This can help to explain why massive planets predicted by usual non-iteration simulations are supposed to be observable but have not actually been widely detected in real observations.

Among the gap depth of the iteration method, as $M_p$ increases, $\Sigma_{\text{gap}}/\Sigma_0$ decreases, though this trend is invalidated to $M_p = 3M_J$ at $r_p = 4$ or 10 au. In these two cases, planets open appreciable eccentric gaps and streamer structures appear, which increases gas density in gaps. Similar situations also happen in the non-iteration cases, though the streamers are less strong and the measured $\Sigma_{\text{gap}}/\Sigma_0$ are close for $M_p = 1M_J$ and $3M_J$. In terms of gap width $\Delta_{\text{gap}}$, as $M_p$
increases, $\Delta_{\text{gap}}$ increases. For $M_p = 3M_J$, it can open a gap roughly as wide as the planet orbit $r_p$ in our disc models. For a fixed $M_p$, if $r_p$ increases, the normalized gap width $\Delta_{\text{gap}}/r_p$ is smaller and the gap depth $\Sigma_{\text{gap}}/\Sigma_0$ is shallower. This is because the higher disc scale height $H/r$ in the outer disc makes pressure torque stronger to prevent the gap-opening process. Besides the disc density profiles of planets at 4 au, Fig. C1 and C2 in Appendix show the 2D gas surface density map of planets at 10 and 30 au. As planets move further away from the central stars, they open shallower gaps than their counterparts at 4 au.

### 3.2 Mid-plane temperature

After implementing dust RT (described in Step 2 in Section 2.3) and assuming $T_{\text{gas}} = T_{\text{dust}}$, we get the 3D $T_{\text{gas}}$ structure of discs. As we are concerned about icy-pebbles or planetesimals which mainly concentrate at the disc mid-plane, we focus on the mid-plane temperature $T_{\text{mid}}$ derived from both iteration and non-iteration methods.

Fig. 4 shows the comparisons between azimuthal averaged $T_{\text{mid}}$ (cyan lines) of planets at 4 au over 2000 orbits calculated by iteration method (upper panels) and non-iteration method (lower panels). The grey shading regions represent the $T_{\text{mid}}$ in different azimuthal angles. Three molecules and their pressure-dependent sublimation temperatures $T_{\text{sub,H}_2O}$, $T_{\text{sub,CO}_2}$, and $T_{\text{sub,CO}}$ [calculations follow the recipe in Hollenbach et al. (2009)] are marked as blue, green, and red dashed–dotted lines, respectively. We use binding energy provided on KIDA1 data base. The uncertainty of $T_{\text{sub,CO}}$ due to different binding energy choices is shown as a light red shading area. As for comparison, the constant sublimation temperatures $T_{\text{sub,H}_2O} = 125 \, \text{K}$, $T_{\text{sub,CO}_2} = 47 \, \text{K}$, $T_{\text{sub,CO}} = 25 \, \text{K}$ in Oberg, Murray-Clay & Bergin (2011) are marked as short horizontal arrows in corresponding colors.

Overall, the iteration method predicts distinct $T_{\text{mid}}$ when compared with the non-iteration method at two regions. In particular, in the inner disc regions ($r < 10$ au) and the gap regions. At the inner disc, iterated $T_{\text{mid}}$ drops more rapidly than non-iterated $T_{\text{mid}}$. For example, we can clearly see the differences between panels (d) and (h) in these three figures. As $M_p = 10M_\odot$, such low planet has negligible effects on disc temperature as they are difficult to open gaps to influence $T_{\text{mid}}$. Therefore, the difference between panels (d) and (h) does not come from the planet opening gaps, instead, the difference comes from the methods we adopt, iteration or non-iteration. The underlying physical explanation will be discussed in more detail in Section 4.3. In short, the puff-up of the scale height at the inner dust rim cause a strong shadowing effect and lower the temperature in these regions.

At the gap regions, iteration predicts more significant $T_{\text{mid}}$ contrasts between inside gap regions and outside gap edges than the non-iteration. The highest contrast of $T_{\text{mid}}$ can be up to 40 K (increase from 30 to 70 K) when $3M_J$ or $1M_J$ at 4 au of iteration method (see panels a and b). The underlying explanation is the iteration tends to open deeper gaps than the non-iteration and allows more stellar photons to penetrate into the mid-plane and increase $T_{\text{mid}}$. However, the peak values of $T_{\text{mid}}$ from both methods are similar in the same $M_p$ and $r_p$ conditions.

Regarding the iteration results, as $M_p$ increases, the $T_{\text{mid}}$ at gaps increases more significantly. It is because more massive planets are able to open deeper and wider gaps and more stellar photons can penetrate deeper at the gap region and heat up mid-plane dust and gas. Such a trend is also seen in the non-iteration method. Furthermore, the mid-plane temperature of $r_p = 10$, 30 au are shown in Fig. D1 and D2, respectively.

By combing the sublimation temperature and the disc mid-plane temperature, we can measure where the mid-plane icelines of different molecules are in Section 3.5. The numbers of icelines primarily rely on the values of $T_{\text{sub}}$ and the disc $T_{\text{mid}}$. If we use the values of binding energy suggested in Oberg, Murray-Clay & Bergin

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1https://kida.astrochem-tools.org
When comparing the density results within either iteration or non-iteration method, if the planet masses $M_p < 1M_J$, they open quite circular gaps and more massive planets open deeper and wider gaps. In terms of the most massive cases of $3M_J$ in our modelling, the planets open eccentric gaps. Our results agree with the results from Kley & Dirksen (2006) who found that planets with mass $M_p > 3M_J$ open eccentric gaps in discs with a viscosity of $\nu = 10^{-5}$ or $\approx 0.004$. In this section, we quantify the eccentricity $e$ of the gaps opened by $M_p = 3M_J$ or $1M_J$ with two kinds of methods. Because the inner and outer edge of a gap has different eccentricities, we measure them separately.

The first method is obtaining $e$ by fitting ellipses to the shape of the inner/outer edges of gaps. The second method is using equation 28 in Ju, Stone & Zhu (2016)

$$e(r) = \frac{\int d\phi \Sigma(r, \phi) v_\phi \exp(i\phi)}{\int d\phi \Sigma(r, \phi) v_\phi}$$

(2)

to calculate $e$ at the location of the inner/outer edges of gaps. Fig. 6 displays an example of using the equation (2) to calculate the $e$ as a function of radius of the simulation of $3M_J$ at 4 au over 2000 orbit by using iteration method. At this case, $e \approx 0.06$ at the gap outer edge, which is not very different from the value in Kley & Dirksen (2006) though the disc parameters (e.g. viscosity $\alpha$, aspect ratio $H/r$) are not exactly the same.

Table 3 summarizes gap eccentricities $e$ from different simulations measured by different methods, fitting ellipse in ‘graph’ or calculating with ‘formula’. Names of different cases are written in abbreviations. For example, $3mj4au_{it}$ graph means the case of $3M_J$ at 4 au of iteration measured by graph method, and so on. In both methods, we average the values of the last 500 orbits (shown as ‘mean’ in Table 3) and calculate their standard deviations (shown as ‘std’ in Table 3). In general, both iteration and non-iteration methods get similar $e$. Also, the values of $e$ are closed from the graph and formula measuring method. $M_p = 3M_J$ induces relatively high $e \approx 0.07$ when $r_p = 4$ or 10 au, which could also be seen from the eccentric gaps in Figs 2 and C1. $M_p = 1M_J$ only open gaps in almost circular shapes.

The high eccentricity of a gap can have a non-neglectable effect on the temperature. For the most eccentric case, for example, $e = 0.08$ measured by graph fitting of $3mj4au$ of the iteration method, we can obtain $r_{\min} = 6$ au and $r_{\max} = 7.6$ au from fitting the ellipse of the outer gap edge. By plugging them into the corresponding temperature profile, we can find $T_{\text{mid}}$ varies from about 40 to 27 K. In other words, CO ice might exist at the semimajor axis side but sublimate at the semiminor axis side of the outer edge of gaps.

### 3.4 Dust trap

Dust grains in a disc experience radial drift unless they get trapped in gas pressure bumps (e.g. Pinilla et al. 2012a; Pinilla, Benisty & Birnstiel 2012b; Dullemond et al. 2018). We can investigate pressure gradient profiles around the gaps to see how our model affects dust-trapping conditions. Pressure is given by $P(r) = \Sigma(r)c_i^2(r)$. Here, both the gas surface density and sound speed $c_i$ are azimuthally averaged after 2000 orbits. Different pressure gradients from iteration and non-iteration can lead to different efficiency of dust trapping. Thus, dust of different sizes could be distributed differently.

The location of the pressure maximum, also named dust-trapping location $r_{\text{th}}$ here, is when the pressure gradient is zero (dlog $P$/dlog $r = 0$). We obtain the $r_{\text{th}}$ of different cases of $M_p$ and $r_p$ of the iteration and non-iteration methods. We find that there are no dust traps in the cases of $M_p = 10M_J$ when planets are at $r_p = 10$ au of the non-iteration method, and $r_p = 30$ au of both methods. Fig. 7 shows the normalized dust trapping location $(r_{\text{th}} - r_p)/R_H$ as a function of planet mass $M_p$. If for a specific case, there is no dlog $P$/dlog $r = 0$, we put $(r_{\text{th}} - r_p)/R_H = 0$. In general, if a planet can form a pressure maximum to trap dust around the outer gap edge, $r_{\text{th}} = r_p = 7 \sim 10R_H$ regardless of different $M_p$ and $r_p$. The dust-trapping locations $r_{\text{th}}$ from both methods do not show a big difference, especially for...
Figure 4. Mid-plane temperature $T_{\text{mid}}$ as a function of disc radius from RADMC-3D simulations of planets at 4 au over 2000 orbits of iteration method (upper panels) and non-iteration method (lower panels). The cyan solid lines represent the azimuthal averaged $T_{\text{mid}}$, while the shading areas represent the deviation of the profiles along different azimuthal angles. From left to right, there are results of 3MJ, 1MJ, 100MJ, and 10MJ, respectively. The blue, green, and red dashed–dotted lines near the horizontal direction represent the pressure-dependent sublimation temperature $T_{\text{sub, H}_2}$, $T_{\text{sub, CO}_2}$, and $T_{\text{sub, CO}}$, respectively. $T_{\text{sub, CO}}$ is shading with a light red region to highlight the wide range of possible values calculated from different binding energies given by KIDA. As a comparison, constant $T_{\text{sub}}$ in Oberg, Murray-Clay & Bergin (2011) are marked with short arrows in these three colours on the right edge of each panel. The vertical cyan dashed lines and grey dotted lines mark the location of the planets and pressure maximum/dust trapping.

Figure 5. Similar to Fig. 4 (a) but $T_{\text{sub}}$ is calculated by using molecule binding energy in Oberg, Murray-Clay & Bergin (2011).

Figure 6. Disk eccentricity calculated from equation (2) for an example of 3MJ at 4 au of iteration method. Planet location is marked with a vertical blue dashed line. The gap inner and outer edges are marked by red dashed lines.

$r_p = 30$ au cases. In smaller $r_p$ cases, iteration tends to trap grains in slightly outer locations than non-iteration for a given $M_\ast$ and $r_f$. Furthermore, $r_{gc} - r_p$ is roughly equal to the gap widths in each case. In other words, the outer gap edges are approximately the middle points between planets and dust-trapping locations.

Table 3. Comparison of inner and outer gap edge eccentricity $e$ of massive planets at different $r_p$ from iteration or non-iteration method. $e$ is measured by either 'graph' or 'formula' method and the averaged values of the last 500 orbits are marked as ‘mean’ and the uncertainty are marked as ‘std’. Values of $e > 0.05$ are highlighted with purple background.

<table>
<thead>
<tr>
<th>$r_p$</th>
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\[e = \frac{a - a_{\text{in}}}{a_{\text{out}} - a_{\text{in}}},\]

where $a_{\text{in}}$ and $a_{\text{out}}$ are the inner and outer gap edges, respectively.
As small dust particles can couple well with gas and may flow through the dust trap, there should be a minimum grain size so that grains larger than this threshold can be trapped by the pressure bump. Thus, we can further infer what ratio of dust is trapped by a pressure bump. The minimum particle size that can be trapped is described by:

\[ d_{\text{critical}} = \frac{6\pi a_{\text{critical}}}{\rho \pi (d \log P / d \log r)} \left( \frac{3}{2} + \frac{d \log \Sigma}{d \log r} \right) \]

(3)

In our modelling, \( \alpha = 10^{-3} \), \( \rho_s = 3.710 \text{ g cm}^{-3} \). We find that the iteration has similar \( a_{\text{critical}} \) of about 0.3 cm as the non-iteration results at the location of pressure maximum \( r_p \). Furthermore, we assume grain size distribution follows Mathis, Rumpl & Nordsieck (1977), \( n(a) \propto a^{-p} \), where \( p = 3.5 \). The range of dust sizes is from 0.1 \( \mu \text{m} \) to \( a_{\text{lag}} \), where \( a_{\text{lag}} \) is the maximum particle size before they fragment due to turbulent relative velocities \( v_f \) (Birnstiel, Klahr & Ercolano 2012):

\[ a_{\text{lag}} = \left( \frac{2}{3\pi \rho \alpha c_s^2} \right)^{1/3} \]

(4)

Follow Pinilla, Benisty & Birnstiel (2012b), we set \( v_f = 10 \text{ m s}^{-1} \). We find that the iteration, \( a_{\text{lag}} \) could be a few times higher than non-iteration. By using the number of particles at a size beam \( n \) in a mass of a particle (assume spherical particle) and integrating from \( a_{\text{critical}} \) to \( a_{\text{lag}} \), we can obtain the fraction of dust mass that gets trapped in the dust trapping regions discussed. The dust-trap fraction is:

\[ f_{\text{trap}} = \frac{a_{\text{lag}}^2 - a_{\text{critical}}^2}{(a_{\text{lag}}^2 - a_{\text{min}}^2)} \]

where \( f_{\text{trap}} \) represents the fraction of the dust mass that could be trapped in the pressure bump region compared to the total dust mass of the pressure bump region.

If we take the 3M_\odot at 4r_p as an example, at the region of the pressure bump (assume from outer gap edge \( r_{\text{gap, out}} \) to \( 2r_p - r_{\text{gap, out}} \)), both iteration and non-iteration have similar averaged \( a_{\text{critical}} = 2 \times 10^{-2} \) cm. If we assume \( a_{\text{min}} = 10^{-5} \) cm, and plug in averaged \( a_{\text{lag}} = 10 \text{ cm} \) for iteration or averaged \( a_{\text{lag}} = 3 \text{ cm} \) for non-iteration. Therefore, we have \( f_{\text{trap}} = 0.96 \) for iteration and \( f_{\text{trap}} = 0.92 \) non-iteration, which means a slightly higher fraction of dust mass could be trapped in the pressure bump predicted by the iteration. Proper inclusion of dust evolution is needed to test this hypothesis in the future.

3.5 Distribution of ice species

Figs 4, D1, and D2 show \( T_{\text{gas}} \) from the iteration method and how it deviates from the non-iteration approach. For this reason, the ices of H_{2}O, CO_{2}, and CO are distributed in different locations when comparing the two methods. More ice means more solid masses could contribute to the pebble or planetesimal formation, while the available species of ice can affect the final planetesimal composition. Therefore, in this section, we use temperature and pressure information to show where different icelines are, where ice distributes throughout the whole disc, and what kinds of ice species form at dust trapping locations.

For each specific molecular iceline, the number of radial icelines depends on the number of intersections between the disc mid-plane temperature \( T_{\text{mid}} \) and the radial pressure-dependent sublimation temperature \( T_{\text{sub}} \). We notice the bonding energy of CO has a wide range of values in KIDA and we show the uncertainty of the \( T_{\text{sub}} \). CO with light red shading regions in Figs 4, D1, and D2. Therefore, we need to keep in mind that the numbers and locations of CO iceline could vary due to adopting different bonding energy of CO.

Fig. 8 summarizes the ice distribution of H_{2}O, CO_{2}, and CO throughout the whole disc. The left and right columns show iteration and non-iteration results. In each column, from top to bottom panels, \( M_p = 3M_\odot, 1M_\odot, 100M_\oplus, \) and \( 10M_\oplus \) are shown. In each panel, from bottom to top, cases of \( r_p = 4, 10, \) and 30 au are shown. The icelines of H_{2}O, CO_{2}, and CO are displayed as horizontal blue, green, and red bars, respectively. Planet and dust trap locations are marked as cyan and grey-dashed lines. To simplify, here we only consider the azimuthal averaged \( T_{\text{mid}} \) to obtain the radial mid-plane iceline locations for different volatiles. However, for some high eccentric cases caused by massive planets, the iceline locations can vary at different azimuthal angles. In addition, we define an iceline as the boundary where volatile freeze out and condense into solid, but do not count it when volatile sublimes.

Without considering the time evolution and dust drift, our static ice distribution model gives the following results for the main species:

H_{2}O ice: all modelling results from the iteration or non-iteration methods for different \( M_p \) and \( r_p \) yield only one water iceline in the disc, and similar iceline locations at around 1.2 au in our disc model. Therefore, planetesimals formed outside 1.2 au can have H_{2}O ice.

CO_{2} ice: both iteration and non-iteration methods in the massive planet cases can have two obvious CO_{2} icelines shown in panels a, b, c, and f (except \( r_p = 30 \text{ au} \) in panels b and f) in Fig. 8. Because the presence of a massive planet (\( M_p \geq 1M_\odot \)) opens deep enough gaps that increase the \( T_{\text{mid}} \), which causes CO_{2} ice to sublimate at the gap regions and freeze out again in the outer discs. Locations of outer CO_{2} icelines are close to gap outer edges. In the inner disc, locations of CO_{2} icelines are predicted to be around 1.5 au in iteration whereas about 3 au in non-iteration.

CO ice: One of the most distinct features between the two kinds of models is that the iteration predicts more complicated CO icelines features than non-iteration. Because of the \( T_{\text{mid}} \) increase at the gap regions, all models of iteration suggest the CO ice would sublimate except 10M_\oplus cases. For \( r_p = 4 \text{ au} \), despite neglecting the short discontinuations in red bars (due to noise in RT temperature) in those iteration panels, we find three icelines of CO in iteration while only one iceline in non-iteration. In this case, the CO ice can exist in three discrete radial regions in iteration results. The first region, from 1 au to somewhere close to the inner edges of gaps, where the inner disc \( T_{\text{mid}} \) drops. The second region, from somewhere near the outer edges of the gap to around 10 au, is ascribed to gap heating with the shadowing effect in the inner disc causing \( T_{\text{mid}} \) to drop. The third region starting from about 25 au is due to the outer disc temperature decrease, which is broadly similar to the non-iteration CO ice distribution region outside 20 au.
4 DISCUSSION

Our coupled treatment of hydrodynamics and RT allows us to shed new light on the feedback of gap-opening planets on the temperature and pressure structure of the protoplanetary disc, which in turn may influence the composition of planetesimals and planets. We discuss this below, followed by a discussion of iceline and disc substructure, as well as caveats of this work and potential improvements for future models.

4.1 The C/O ratio as a planet formation tracer

The carbon-to-oxygen ratio is a potential signature of the history of planet formation (Oberg, Murray-Clay & Bergin 2011). Physical and chemical models of protoplanetary discs, with varying degrees of complexity, have been developed to understand the radial behaviour of the C/O ratio (e.g. Cleeves et al. 2018; Miotello et al. 2019; Zhang et al. 2019; Bosman et al. 2021). Recently, an azimuthal C/O ratio variation in protoplanetary disc has also been reported and modelled (Keyte et al. 2023). As we have shown, planet-induced gaps introduce significant new complexity to this picture by creating feedback and altering the thermal structure. This in turn modifies various ice lines and thus the C/O-ratio imprinted on subsequently forming planetesimals and planets.

To investigate how radial variations in the C/O ratio are affected by feedback from gap-opening planets, and the presence of a puffed-up inner rim, we follow the prescription from Oberg, Murray-Clay & Bergin (2011). We assume the only C and O carriers are H$_2$O, CO, CO$_2$, refractory carbon, and silicate minerals, using the same abundances as that study. The total abundance of each species summed over the gas and solid phase does not vary with radius.

Fig. 9 shows how the gas- and solid-phase C/O ratio varies as a function of location in a disc, and for different $M_p$ at $r_p = 4$ au, for models using our iteration method. For comparison, the baseline model without a planet is also shown, analogous to the standard ‘Oberg model’ for the C/O profile. We note that analogous changes can be observed for planets at larger orbits, but due to the relevance to most known planetary systems which are close-in, as well as the analogy with the Solar system, we focus here on the 4au case.

Based on our iterative models, the introduction of a gap-opening planet significantly alters the radial profile of the C/O ratio in the gas and solid phase, compared to the baseline (no-planet) case.
Finally, the presence of a gap makes the disc temperature (and pressure) profile strongly non-monotonic, which can create multiple iceline locations for a single chemical species. A monotonous, smoothly decreasing temperature profile underlies the widely studied picture of well-defined, unique icelines. In that case, the more refractory species (silicates, organic carbon, water ice) each have their iceline closer to the star than the more volatile species (e.g. CO).

Secondly, by comparing the results from discs hosting different mass planets, we can see the planet gap-opening effect on C/O is stronger as planet mass increases. The reduced optical depth within the gap leads to increased heating which causes $T_{\text{mid}}$ to rise above the CO$_2$ sublimation temperature. This returns proportionally more oxygen than carbon back to the gas phase, thereby decreasing the gas-phase C/O ratio locally.

Our results show that the feedback from gap-opening planets can significantly affect the gas- and solid-phase C/O ratio at small spatial scales within a protoplanetary disc. Such variations have important implications for the composition of icy planetesimals, and the gas from which giant planets accrete their envelopes. Additionally, our findings demonstrate that radially distinct regions of the disc can be characterized by the same C/O ratio, which complicates the usage of C/O as a formation tracer. To construct more accurate models, it is essential that future observations focus in measuring the C/O ratio at planet-forming scales. We note, however, that some of the variations seen in the radial location of molecular icelines in our models are as little as $\sim$1 au, which can be difficult to resolve even with ALMA, though the larger shifts ($\sim$ 10 au or more) can be more easily measured. The largest-scale variations are evident for high-mass planets at large separations ($M_p = 3M_J$ at 30 au in our model, Fig. 8a).

The degree to which the gap-modified gas and solid composition will be reflected in the atmospheric composition of a forming planet will further depend on the degree of mixing between the core and atmosphere, and the amount of sublimation that takes place during accretion. The scenario is further complicated by considering the vertical layer in which planets accrete their envelopes. Meridional flows from the disc surface may favour the accretion of gas and small grains from the disc surface layers, for example (e.g. Teague, Bae & Bergin 2019).

4.2 Ice lines and dust rings

The altered thermal and ice line structure of a disc with a gap-opening planet has implications for the observational study of disc substructure, both spectroscopy of the gas and also the dust rings which are widely observed in discs with ALMA.

We illustrate this for the case outlined in Fig. 4(a), a 3$M_J$ planet at 4 au. Heating due to gap-opening increases the local mid-plane temperature above the CO sublimation temperature, introducing a new CO condensation front at the outer edge of the gap in a region of the disc where CO would otherwise be entirely frozen out.

As also highlighted in Fig. 4, a dust trap is located in the pressure maximum just outside a gap. Furthermore, results in the literature suggest regions near ice lines may be favourable for the pile-up of icy pebbles (e.g. Hyodo, Ida & Charnoz 2019). As pebbles cross the ice line and sublimate, outward diffusion followed by recondensation may locally enhance the surface density outside of the iceline, triggering instabilities which can lead to rapid pebble and planetesimal growth (Drążkowska & Alibert 2017). High dust-to-gas ratios and viscosity gradients produced by the density enhancement could further amplify the effect (e.g. Brauer, Henning & Dullemond 2008; Ros & Johansen 2013; Bitsch et al. 2014; Drążkowska & Dullemond 2014; Flock et al. 2015).

This rapid growth of pebbles around condensation fronts is tentatively supported by observations of discs such HL Tau, where the location of millimeter dust rings has been linked to the icelines of water and other key volatiles (Zhang, Blake & Bergin 2015).
Similarly, grain size distributions inferred from ALMA observations of HD 163296 are consistent with the enhanced production of large grains at the CO iceline (Guidi et al. 2016). However, no unambiguous correlation between dust rings and ice lines on a standard monotonously radially decreasing temperature profile has been found. Results using empirical temperature estimates seem to disfavor such correlation (Long et al. 2018).

Although icelines have been invoked to explain the rings and gaps observed in a handful of discs, such as HL Tau (Zhang, Blake & Bergin 2015), icelines are not a preferred explanation when looking at large surveys of protoplanetary discs (Huang et al. 2018; Long et al. 2018; Van Der Marel et al. 2019). This is because most of the locations of substructures do not coincide with the sublimation temperature of the main disc volatiles, when assuming that the disc temperature is set by stellar irradiation. Under this hypothesis, a correlation between the location of substructures and the stellar luminosity is expected.

However, as we show in this work, this potential correlation may get much more complicated when a planet is embedded in the disc. The planet alters the temperature–pressure profile of the disc, moving the ice lines to different radii and even creating multiple, radially widely separated ice lines for a single species. Therefore, our current results suggest that it is not necessarily a correlation with the stellar luminosity as it is usually assumed, but that embedded gap-opening planets need to be accounted for to fully assess the locations of ice lines and their correlation with the locations of dust (pebble) rings.

In addition, Pinilla et al. (2017) demonstrated that due to the variations of dust sticking properties, ice-covered dust particles can create ‘traffic jams’, which result in rings and gaps when observed at different wavelengths. The inclusion of dust evolution models in the framework of our models is needed to test if multiple substructures are expected in the discs as a result of a single-planet embedded and multiple icelines locations of different volatiles.

### 4.3 Inner rim mid-plane temperature drops

In this section, we discuss the temperature decrease in the inner few au in discs in Section 3.2. As Figs 4, D1, and D2 show, even the lowest $M_p = 10 M_\oplus$ case which represents minor or no planet effect on the disc, the iteration method predicts strong $T_{\text{mid}}$ drops in this inner disc region. On the contrary, such an effect is not shown in the non-iteration method. The physical explanation is that the puff-up of the scale height can cause a strong shadowing effect to decrease the temperature within 10 au in the RADMC-3D simulation. The reason why there is a puff-up scale height at the inner rim at 1 au in our transition disc models is that stellar photons hit a dust wall, increasing the dust temperature.

As we assume the dust and gas temperatures are well coupled, the gas temperature is also high and causing the gas scale height to have a strong puff-up. This phenomenon is also suggested in fig. 3 in Dulmond, Dominik & Natta (2001), as well as Jiang-Condell & Turner (2012, 2013), Siebenmorgen & Heymann (2012), and Zhang et al. (2021). In our RADMC-3D setups, we input time evolving scale height for the surface density to volume density extension process. As the scale height indicated by the $T_{\text{mid}}$ from last RADMC-3D has puff-up in the inner rim, our iteration models can naturally capture such effects. However, in the non-iteration method, the input scale height for RADMC-3D is just the smooth flaring scale height as that in the FARGO3D setup. Therefore, the iteration can have an advantage in making use of the physical temperature obtained by RT for a specific disc model rather than using the initially assumed temperature as non-iteration. In addition, we measure the aspect ratio $H/r$ of the puff-up inner rim at 1 au is about 0.035 and then it decreases to the lowest value of about 0.015 at about 1.5 au. For the region further away from 1.5 au, $H/r$ increases as a power law with a flaring index of 0.25 which is similar to the power law profile of non-iteration $H/r$.

The change in inner disc temperature structure between the commonly used isothermal (non-iteration) method and our iteration method also impacts the behaviour of elemental ratios like C/O. In our models using the iteration method, shadowing by the puffed-up inner rim causes $T_{\text{mid}}$ dropping off more quickly within the inner disc, moving the H$_2$O and CO$_2$ icelines inwards. This translates to a steep rise in the gas-phase C/O ratio, as a large proportion of the total atomic oxygen is frozen-out into solids. In this scenario, C/O reaches unity within $\sim$1.5 au, compared to $\sim$3 au in the non-iteration and classical models.

### 4.4 Assumptions and limitations

There are a number of simplifications in our HD and RT simulations that can be improved in future work. First, we only consider 2D HD simulations in radial and azimuthal directions instead of full 3D HD simulations, which benefited us for speeding up the whole iteration process. However, 3D HD simulations can allow one to get rid of the vertical isothermal assumption which will be useful for addressing vertical stratified problems (e.g. ice-surface distribution, gas molecule emission layers). In this paper, we only focus our discussion on the mid-plane temperature and its effect on mid-plane ice distribution.

Second, we have some simplifications about dust in our modeling. In HD simulations, we do not include dust species in order to speed up the simulation process. In addition, only one small grain size, 0.1 µm, is included in the radiativetransfer simulations. If we consider grain size distribution or dust evolution process, like grain growth or fragmentation, it is still unclear how can these factors change the dust distribution and hence disc temperature. Because we do not have a dust density distribution in our models, we also neglect dust settling in our models. As a consequence, it is possible that when dust settling is included, less dust remains on the disc surface, allowing stellar radiation to penetrate deeper into the disc and increase $T_{\text{mid}}$. Our models also neglect to account for dynamical effects such as radial drift and mass accretion, which add considerable complexity. For example, studies have shown that radial drift can produce multiple icelines Cleeves (2016) or make icelines thermally unstable under typical disc conditions (Owen 2020). Icy volatiles drift faster that those in the gas-phase, which results in the iceline progressively moving inwards, condensing more volatiles. The iceline then recedes as volatiles sublimate, on timescales much shorter that the disc lifetime (1000-10,000 years). Similarly, the mass accretion rate plays an important role in iceline evolution, with iceline moving inwards when accretion rates are high, and migrating back out in the later stage of disc evolution when the accretion rate decreases (Oka, Nakamoto & Ida 2011). The combined effects of radial drift and mass accretion can cause molecular icelines to moves inwards by as much as 60 per cent (Piso et al. 2015).

Third, we do not consider viscous heating which can be dominant in the mid-plane of the inner disc (e.g. Broome et al. 2023). Thus, the viscous heating may have sufficient effects on increasing the very inner disc $T_{\text{mid}}$. This may have a strong effect on our 4 au cases. Also, our models do not capture shock heating from the planet which can be significant for massive planet cases.

Finally, we choose 100 orbits as our iteration step to implement the feedback from RADMC-3D to FARGO3D. However, we notice that the thermal relaxation time can vary from about 100 to 0.1 dynamic
time-scale from 1 to a few tens au (Malygin et al. 2017; Pcieł & Klahr 2019) and our model can not capture this. The number of the iteration step we decide is a balance between the total simulation time and reflecting the gap-opening thermal feedback properly. One possible way to improve the approach is if we are only concerned about the radial temperature structure but ignore the azimuthal variations, we can use fewer photon package numbers for fewer azimuthal grid cell RADMC-3D simulations to speed up each iteration step and do more iterations.

In future work, we will focus on the improvement of some of these limitations, in particular the effect of including dust in the models.

5 CONCLUSIONS

In this paper, we present a new method to study the gap-opening effect on protoplanetary disc temperature structure by iterating HD and RT simulations. We quantify the planet-opening gap profiles including gap width, depth, and eccentricity, and explore the dust-trapping condition in outer gap edges. By obtaining the temperature profiles in discs, we study the volatile iceline locations and ultimately provide new C/O ratio for discs with embedded planets. During the modeling, we compare our iteration models with the conventional non-iteration models and conduct parameter studies of different planet masses \( M_p \) and planet locations \( r_p \). Our main conclusions are as follows:

(i) Gap profiles: the iteration method predicts deeper and more eccentric gaps than the non-iteration. The most significant difference in gap depth comparison between these two methods is seen at \( 1M_J \) at 4 or 10 au, where the iteration gap depth is about an order of magnitude deeper than the non-iteration.

(ii) Dust trap: both iteration and non-iteration indicate similar locations of pressure maximum for dust trapping \( r_d \), which is about 7–10 \( R_J \) further away from \( r_p \). However, the iteration predicts a larger fragmentation grain size across the pressure bump, and as a consequence, a slightly higher fraction of dust could be trapped in the pressure bump.

(iii) Mid-plane temperature: our iteration models can capture the gap-opening process by a planet and its effect on the time evolution of the disc temperature structure, whereas the conventional non-iteration models do not capture. By implementing the iteration method, we show that the strong mid-plane temperature drops in the inner few au of discs because of the shadowing effect caused by the puff-up disc inner rim. Meanwhile, the mid-plane temperature \( T_{\text{mid}} \) increases significantly in the gap regions due to more photons can penetrate into the mid-plane. The maximum \( T_{\text{mid}} \) contrast between gap edges and gap center is about 40 K when \( 3M_J \) or \( 1M_J \) presents at 4 au.

(iv) Icelines: because of \( T_{\text{mid}} \) drops, CO and CO ice may exist in the inner disc region (at a few au) in the iteration model. At gap regions, both iteration and non-iteration predict that CO2 or CO ice may sublimate. As a result, the non-iteration suggests that more than one CO2 or CO iceline can appear in a disc, whereas the iteration models propose that even more CO icelines might exist in giant planet-forming discs. This result suggests that the combination of an embedded planet and different locations of the iceline of the same volatile can still explain the observed substructures in protoplanetary discs.

(v) C/O ratio (Fig. 9): the radial C/O ratio profile across the disc is significantly more complex due to the presence of gaps opened by giant planets in comparison to disc models without embedded planets. As a consequence, the feedback of the planet-opening gap on the disc thermal structure can significantly influence the composition of material available for the giant planet’s atmosphere or for the next generation of planet formation.

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DATA AVAILABILITY

Data from our numerical models are available on reasonable request to the corresponding author. The FARGO3D code is publicly available from https://fargo3d.bitbucket.io/download.html. The RADMC-3D code is available from https://www.ita.uni-heidelberg.de/~dullemond/software/radmc-3d/

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APPENDIX A: TESTS OF ITERATION STEPS

We compare the mid-plane temperature after 2000 planetary orbits by implementing iteration steps of 50 orbits, 100 orbits, or 500 orbits in Fig. A1. We show two case of $3M_j$ at 4 au (left) and $3M_j$ at 30 au (right). The differences between the iteration step of 100 orbits and 500 orbits displayed by blue lines are small, especially at the gap regions, the normalized temperature difference $\Delta T/T_{i_{100}} \sim 0$ and the maximum is $<0.1$. On the other hand, the differences between the iteration step of 100 orbits and 500 orbits show relatively larger fluctuations around 0. Therefore, the iteration step of 100 orbits basically is able to reproduce the iteration step of 50 orbits, whereas the iteration step of 500 orbits could not reproduce the iteration step of 100 orbits very well. Meanwhile, we acknowledge that the thermal relaxation time can vary more than several magnitudes in different disc radii (Malygin et al. 2017; Pfeil & Klahr 2019) but our model cannot capture this. Nevertheless, due to the limit of computing capability, we think adopting 100 orbit as the iteration step is suitable for our studies.

![Comparison of mid-plane temperature over 2000 orbits by using different iteration steps.](https://academic.oup.com/mnras/article/527/2/2049/7330168)

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**Figure A1.** Comparison of mid-plane temperature over 2000 orbits by using different iteration steps. The y-axes $\Delta T/T_{i_{100}}$ show the normalized temperature difference between two iteration steps. $T_{i_{100}}$, $T_{i_{100}}$, or $T_{i_{500}}$ is the temperature by adopting iteration steps of 50, 100, or 500 orbits, respectively.
APPENDIX B: COMPARISONS BETWEEN MIDPLANE TEMPERATURE AND DENSITY-WEIGHTED VERTICAL AVERAGED TEMPERATURE

We compare the mid-plane temperature and the density-weighted vertical averaged temperature from RADMC-3D simulations of $3M_J$ at 4 au over 100 orbits.

\[
T(r) = \frac{\int \rho(r,z)T(r,z)dz}{\int \rho(r,z)dz},
\]

\hspace{1cm} (B1)

where $T(r,z)$ is the azimuthal average temperature.

Overall, the density-weighted temperature is not significantly different from the mid-plane temperature as the volume density is much higher in the mid-plane than on the surface. Especially the gap region temperature is very similar. The strongest difference is in the shadowing region where the mid-plane temperature is lower than the weighted temperature for up to 10 K. This is because the shadowing effect is strongest for the mid-plane. As the weighted temperature has a contribution from the surface temperature, which is not heavily affected by the shadowing effect, it makes the weighted temperature higher.

APPENDIX C: GAS DENSITY OF PLANETS AT 10 AND 30 AU

Figs. C1 and C2 show the 2D gas density map of gaps opened by $3M_J$, $1M_J$, $100M_\oplus$, and $10M_\oplus$ planets at 10 and 30 au, respectively. The results of iteration and non-iteration are displayed in the upper and lower panels, respectively.

Figure C1. Similar to Fig. 2 but for planets at 10 au.
APPENDIX D: TEMPERATURE OF PLANETS AT 10 AND 30 AU

Fig. D1 and D2 show the mid-plane temperature as a function of disc radius when planet location is $r_p = 10$ and 30 au, respectively.
Figure D2. Similar to Fig. 4 but for planets at 30 au.

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