# X-ray polarimetry and spectroscopy of the neutron star low-mass X-ray binary GX 9+9: An in-depth study with IXPE and NuSTAR 

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#### Abstract

We report on a comprehensive analysis of simultaneous X-ray polarimetric and spectral data of the bright atoll source GX $9+9$ with the Imaging X-ray Polarimetry Explorer (IXPE) and NuSTAR. The source is significantly polarized in the $4-8 \mathrm{keV}$ band, with a degree of $2.2 \% \pm 0.5 \%$ (uncertainty at the $68 \%$ confidence level). The $N u S T A R$ broad-band spectrum clearly shows an iron line, and is well described by a model including thermal disc emission, a Comptonized component, and reflection. From a spectro-polarimetric fit, we obtain an upper limit to the polarization degree of the disc of $4 \%$ (at the $99 \%$ confidence level), while the contribution of Comptonized and reflected radiation cannot be conclusively separated. However, the polarization is consistent with resulting from a combination of Comptonization in a boundary or spreading layer, plus reflection off the disc, which significantly contributes in any realistic scenario.


Key words. accretion, accretion disks - stars: neutron - polarization - X-rays: general - X-rays: binaries - X-rays: individuals: GX 9+9

## 1. Introduction

Weakly magnetized neutron star low-mass X-ray binaries (NS-LMXBs) accrete mass via Roche lobe overflow from a lowmass stellar companion. They are historically divided into two classes, Z and atoll, according to their tracks on the colour-colour-diagram (Hasinger \& van der Klis 1989). The differences between the two classes are probably driven by the mass accretion rate, which is close to the Eddington limit in Z sources, and relatively low in atoll sources (e.g. van der Klis 1994; Muñoz-Darias et al. 2014). However, the distinction between Z and atoll is not clear-cut, because atoll sources also exhibit Z-shape tracks when observed on a long enough timescale (Gierliński \& Done 2002; Muno et al. 2002). Furthermore, a single source may also oscillate between having a Z and atoll behaviour, as observed in XTEJ1701-462 (Lin et al. 2009; Homan et al. 2010).

The X-ray spectra of NS-LMXBs in the soft state are generally well described by two main components, a thermal one

[^0]dominating in the soft band below $\sim 1 \mathrm{keV}$, and a hard one possibly due to Comptonization of soft photons in a plasma with a temperature of $\sim 3 \mathrm{keV}$ (e.g. Barret 2001; Paizis et al. 2006; Farinelli et al. 2008). In the so-called eastern model, the soft component is a multi-temperature black body produced by the accretion disc, while the hard component arises from Comptonization of NS seed photons (Mitsuda et al. 1984, 1989). Physically, this scenario could correspond to Comptonization occurring in a boundary layer (BL) between the disc and the NS (Pringle 1977; Shakura \& Sunyaev 1988; Popham \& Sunyaev 2001) or a more vertically extended spreading layer (SL) around the NS (Inogamov \& Sunyaev 1999; Suleimanov \& Poutanen 2006). Alternatively, the so-called western model assumes that the soft component is a single-temperature black body due to the NS, while the hard component originates from Comptonization of disc photons (White et al. 1988). However, more complex scenarios have been proposed. For example, Lin et al. (2007) discussed a three-component model including both NS and disc thermal emission plus Comptonization, while Cocchi et al. (2011) proposed a model in which both NS and disc seed
photons are Comptonized in an extended corona. Furthermore, in addition to the primary continuum, reflection of X-ray photons off the accretion disc is detected in a number of sources (e.g. Di Salvo et al. 2009; Miller et al. 2013; Mondal et al. 2017, 2018; Ludlam et al. 2017, 2019, 2022), albeit not ubiquitously (Homan et al. 2018; Ludlam et al. 2019).

The exact nature of the X-ray emitting regions in NS-LMXBs thus remains elusive, because the models outlined above are spectroscopically degenerate. X-ray polarimetry, on the other hand, can significantly constrain the geometry of the system, and thus its physical properties. X-ray polarimetric studies are now possible thanks to the Imaging X-ray Polarimetry Explorer (IXPE; Soffitta et al. 2021; Weisskopf et al. 2022), which launched in December 2021. The first two nonpulsating NS-LMXBs observed by IXPE are GS 1826-238 (Capitanio et al. 2023) and Cyg X-2 (Farinelli et al. 2023), with both being observed in a high soft state. For GS 1826-238, Capitanio et al. (2023) find an upper limit to the polarization of $1.3 \%$ (at the $99.73 \%$ confidence level) over the IXPE $2-8 \mathrm{keV}$ energy range. This result is consistent with a quasi-spherical geometry of the X-ray source, such as an extended SL, or with a non-spherical source seen at a small viewing angle $\left(\$ 40^{\circ}\right)$. In the case of Cyg X-2, Farinelli et al. (2023) find a polarization degree of $1.8 \% \pm 0.3 \%$, with a polarization angle consistent with the direction of the radio jet, and thus it is most likely parallel to the rotation axis. This rules out the accretion disc itself as the main source of polarized X-rays, as well as a geometry in which the boundary layer is coplanar with the disc (Farinelli et al. 2023), because in the optically thick case polarization is parallel to the disc (Chandrasekhar 1960). Interestingly, Long et al. (2022) find a similar result for Sco X-1, based on PolarLight data in the $3-8 \mathrm{keV}$ band.

GX $9+9$ is a bright atoll source (Hasinger \& van der Klis 1989), whose light curve shows a 4.2 h modulation in both the optical and X-ray bands (Hertz \& Wood 1988; Schaefer 1990). Its distance is not well known; however, the estimates range between 5 kpc (Christian \& Swank 1997) and 10 kpc (Savolainen et al. 2009). This source has been consistently observed in a bright soft state (Gladstone et al. 2007; Savolainen et al. 2009; Iaria et al. 2020). The average X-ray flux in the $2-20 \mathrm{keV}$ band is $\sim 200 \mathrm{mCrab}$ (Iaria et al. 2020), and the X-ray spectrum is well represented by a two-component emission model plus reflection (Kong et al. 2006; Savolainen et al. 2009; Iaria et al. 2020). In fact, Iaria et al. (2020), studying the broad-band X-ray spectrum with XMM-Newton and BeppoSAX, report the presence of a significant relativistic reflection component and estimate an inclination of $40^{\circ}-50^{\circ}$, consistent with the upper limit of $70^{\circ}$ indicated by the lack of X-ray eclipses (Schaefer 1990; Savolainen et al. 2009). In this paper, we report on the spectral and polarimetric analysis of GX 9+9 with simultaneous NuSTAR and IXPE observations. We also discuss numerical simulations specifically developed for the source. The IXPE polarimetric data have been recently presented by Chatterjee et al. (2023), together with AstroSat non-simultaneous spectral data taken in 2020. However, the NuSTAR capability to detect the reflection component and the simultaneity with IXPE give us the possibility to relate the polarization properties to specific spectral components with good confidence.

The paper is structured as follows. In Sect. 2, we describe the observation and the IXPE and NuSTAR data reduction. In Sect. 3, we report on the analysis of the spectral and polarimetric data. Section 4 is devoted to the discussion of the results and the summary.

Table 1. Logs of the IXPE and NuSTAR observations.

| Satellite | Obs. Id. | Start time <br> (UTC) | Net exp. <br> (ks) |
| :--- | :---: | :---: | :---: |
| IXPE | 01002401 | $2022-10-09 T 12: 09: 58$ | 92.5 |
| NuSTAR | 30801021002 | $2022-10-09 \mathrm{~T} 10: 21: 09$ | 38.5 |

## 2. Observation and data reduction

### 2.1. IXPE

IXPE observed the source on 2022 October 9 with its three detector units (DUs)/mirror module assemblies (MMAs), for a net exposure time of 92.5 ks (Table 1). We produced cleanedlevel two event files using standard filtering criteria with the dedicated FTOOLS (v6.31) tasks ${ }^{1}$ and the latest calibration files (CALDB 20221021) and response matrices (v12). The $Q$ and $U$ Stokes spectra produced by the instrument pipeline are in the FITS format, and associated with an ancillary response matrix and a modulation response function (namely the product of the effective area and the modulation factor). The joint spectropolarimetric analysis of the Stokes parameters can thus be carried out with standard techniques and software tools. We extracted the Stokes $I, Q$, and $U$ spectra from circular regions with a radius of $120^{\prime \prime}$. We did not subtract the background, following the prescription by Di Marco et al. (2023) for bright sources. However, we verified that background subtraction does not significantly alter the results, especially the polarimetric measurements. Given the source brightness, each energy bin of the flux (I) spectra contains more than 40 counts, ensuring the applicability of the $\chi^{2}$ statistics. Thus, we did not rebin the $I$ spectra, while we applied a constant energy binning of 0.2 keV for $Q$ and $U$ Stokes spectra. We fitted the $I, Q$, and $U$ Stokes spectra from the three DU/MMAs independently.

### 2.2. NuSTAR

NuSTAR (Harrison et al. 2013) observed the source with its X-ray telescopes on Focal Plane Module A (FPMA) and B (FPMB), with a net exposure of 38.5 ks simultaneously with the first half of the IXPE exposure. We produced cleaned event files with the dedicated nupipeline task and the latest calibration files (CALDB 20230208). In the case of NuSTAR, the background is not negligible at all energies, and therefore we performed background subtraction as follows. For both detectors, we extracted the background from a circular region with a standard radius of 1.22 , while we set the source radius at $2^{\prime}$ following a procedure that maximizes the signal-to-noise ratio (Piconcelli et al. 2004). We rebinned the spectra with the standard task ftgrouppha, implementing the optimal scheme by Kaastra \& Bleeker (2016) with the additional requirement of a minimum signal to noise of 3 in each bin. The FPMA and FPMB spectra were fitted independently. We used the data in the $3-30 \mathrm{keV}$ range, since the background starts dominating above 30 keV .

## 3. Data analysis

GX 9+9 is known to exhibit complex long-term X-ray variability (Kotze \& Charles 2010); however, as of 2009, the light curve

[^1]

Fig. 1. MAXI daily light curve of GX $9+9$ (photon $\mathrm{cm}^{-2} \mathrm{~s}^{-1}$ ). Top panel: $2-20 \mathrm{keV}$ photon flux. Bottom panel: hardness ratio between the $10-$ 20 keV and $4-10 \mathrm{keV}$ photon fluxes. The vertical dashed line marks the date of the IXPE and NuSTAR observation.
of the Monitor of All-sky X-ray Image (MAXI; Matsuoka et al. 2009) has shown a rather constant baseline and small amplitude variations (Asai et al. 2022). The MAXI light curve spanning one year between 2022 January 26 and 2023 January 26 is shown in Fig. 1. The X-ray flux is quite stable, while the hardness ratio (HR) shows variations by a factor of 2 on timescales of roughly 1-2 months. In Fig. 2 we show the NuSTAR light curve of the source, together with the HR. The NuSTAR hardnessintensity diagram and the colour-colour diagram are shown in Figs. 3 and 4, respectively. Some spectral variability is apparent for a short interval at the beginning of the NuSTAR exposure. However, the variation in HR is not dramatic, and no flaring is detected. Therefore, in the following analysis, we consider the spectrum averaged over the whole observation.

In Table 2, we report the polarization degree (PD) and polarization angle (PA), as measured from IXPE spectra using XSPEC 12.13.0 (Arnaud 1996), with the $68 \%$ confidence level uncertainty for one parameter of interest. These values are well consistent within the errors with those found from the polarization cubes extracted with IXPEOBSSIM (Baldini et al. 2022). The twodimensional contour plots of PD and PA are shown in Fig. 5. The results are consistent within the errors with those reported by Chatterjee et al. (2023).

### 3.1. The NuSTAR spectrum

As a first step, we assessed the spectral properties of the source by fitting the NuSTAR data in the $3-30 \mathrm{keV}$ band. In all of our models, we have included interstellar absorption (tbabs model in XSPEC; Wilms et al. 2000), with a column density fixed at $3 \times 10^{21} \mathrm{~cm}^{-2}$ (Iaria et al. 2020) because the energy band does not extend to low energies where absorption is strong, and thus the fit is not very sensitive to this parameter. We started by fitting the $N u S T A R$ spectrum with a standard two-component model composed by a disc multi-colour black body (diskbb in XSPEC; Mitsuda et al. 1984) and a Comptonized spectrum (comptt in XSPEC; Titarchuk 1994), including a cross-calibration constant between FPMA and FPMB which is found to be $1.006 \pm 0.001$. However, we find a discrepancy between the FPMA and FPMB spectra at low energies ( $3-4 \mathrm{keV}$ ), with the FPMA flux being significantly larger. This could be an effect of a known rip in

IXPE and NuSTAR light curves


Fig. 2. IXPE and $N u S T A R$ light curves of GX $9+9$ (count s ${ }^{-1}$ ). The lower panel shows the $N u S T A R$ hardness ratio $(10-30 \mathrm{keV}) /(3-10 \mathrm{keV})$. Time bins of 200 s are used.

NuSTAR Hardness-Intensity


Fig. 3. NuSTAR count rate hardness ratio $(10-30 \mathrm{keV} / 3-10 \mathrm{keV})$ vs. total count rate $(3-30 \mathrm{keV})$. Time bins of 200 s are used.
the multi-layer insulation that encloses the optics (Madsen et al. 2020), which is not fully accounted for by the current calibration. Following Madsen et al. (2020), we included in our model the multiplicative table numliv1 specifically designed to correct this issue ${ }^{2}$.

The simple model diskbb+comptt does not provide a good fit to the NuSTAR data, because it leaves clear residuals especially in the $6-7 \mathrm{keV}$ range, giving a total $\chi^{2} /$ d.o.f. $=319 / 228$ (see Fig. 6). We note that in comptt the seed photons are distributed according to Wien's law, so that the model low-energy tail goes as $E^{3}$. To check if the observed residuals may be due to the interplay with the softer disc emission, we replaced comptt

[^2]

Fig. 4. NuSTAR hard colour ( $6-30 \mathrm{keV} / 4.5-6 \mathrm{keV}$ ) vs. soft colour (4.5$6 \mathrm{keV} / 3-4.5 \mathrm{keV}$ ). Time bins of 200 s are used.

Table 2. PD and PA measured with xSPEC.

| Energy range (keV) | PD (\%) | PA (deg) |
| :--- | :---: | :---: |
| $2-8$ | $1.4 \pm 0.3$ | $68 \pm 6$ |
| $2-4$ | $<1.8$ | - |
| $4-8$ | $2.2 \pm 0.5$ | $61 \pm 7$ |

Notes. The uncertainties are given at the $68 \%(1 \sigma)$ confidence level for one parameter of interest. The upper limit is quoted at the $99 \%$ confidence level.
with comptb (Farinelli et al. 2008), in which the seed photon spectrum is a black body. However, the behaviour of the residuals did not change substantially. It is also worth noting that Iaria et al. (2020) find that a relativistic smeared reflection component is needed to fit the broadband spectrum, but they do not find clear evidence of a Fe K emission line, while this is apparent in the NuSTAR spectrum. Including a narrow Gaussian line at 6.4 keV improves the fit which, however, does not remain very $\operatorname{good}\left(\chi^{2} /\right.$ d.o.f. $\left.=282 / 226\right)$.

A further improvement was found replacing the narrow Gaussian with a relativistically broadened emission line (relline; Dauser et al. 2013). In relline we fixed the emissivity index at three and the dimensionless spin at 0.2 , because the fit is not very sensitive to these parameters. We noticed that the line energy and the disc inclination are degenerate in the spectral fit, and thus we initially fixed the inclination at $40^{\circ}$. We find a fit with $\chi^{2} /$ d.o.f. $=261 / 225$; the inner disc radius of relline is $6 \pm 3$ in units of the innermost stable circular orbit (ISCO), the line energy is $6.51_{-0.10}^{+0.09} \mathrm{keV}$, and its equivalent width is $16 \pm 3 \mathrm{eV}$. The line energy might be consistent with an origin from ionized material. Indeed, if we assume an inclination of $30^{\circ}$, we obtain a statistically equivalent fit with a line energy of $6.70_{-0.06}^{+0.05} \mathrm{keV}$, that is to say consistent with the Fe XXV $\mathrm{K} \alpha$ line. However, if we assume an inclination greater than $50^{\circ}$, the line is consistent with being neutral. These results motivated us to test a more self-consistent reflection model to try to break the degeneracy. We also checked whether the emission line could actually be an artefact of absorption, but replacing the emission line with an absorption edge at $\sim 7 \mathrm{keV}$ results in a worse fit $\left(\chi^{2} /\right.$ d.o.f. $\left.=274 / 226\right)$ with significant residuals in the $6-7 \mathrm{keV}$ band.


Fig. 5. Contour plots of the PD and PA at the 68, 90, and $99 \%$ confidence levels in the $2-4 \mathrm{keV}$ (orange dotted), $4-8 \mathrm{keV}$ (blue dashed), and $2-8 \mathrm{keV}$ (black solid) energy bands, respectively.


Fig. 6. Fit of the $N u S T A R$ spectrum. Top panel: deconvolved NuSTAR spectrum fitted with a model composed of diskbb (dash-dotted line) and comptt (dashed line). Bottom panel: residuals in units of $\sigma$. The data from the two detectors FPMA and FPMB were combined (with setplot group in XSPEC) for plotting purposes only.

Finally, we replaced the line with a complete reflection model. The residuals observed in Fig. 6 do not show the presence of an obvious Compton hump, indicating that reflection is produced by a softer illuminating spectrum than the typical non-thermal (power-law) continuum assumed in standard reflection models. We thus employed relxillns (García et al. 2022), a flavour of relxill (García et al. 2014; Dauser et al. 2014) in which the primary continuum illuminating the disc is a single temperature black-body spectrum (physically corresponding to the NS surface or a SL). The code assumes an illuminating spectrum incident at $45^{\circ}$ on the surface of the disc (García et al. 2022). In relxillns we fixed some parameters that the fit does not constrain at reasonable values. We set the emissivity index $q_{\mathrm{em}}=3$ (see, e.g. Wilkins 2018), the dimensionless spin $a=0.2$, the iron abundance $A_{\mathrm{Fe}}=1$, and the number density $\log n_{\mathrm{e}}=18$ (e.g. Ludlam et al. 2022) ${ }^{3}$. We also tied the black-body temperature to that of the seed photon spectrum

[^3]Table 3. Best-fitting model parameters of the fits to the NuSTAR and NuSTAR+IXPE data.

| Parameter | NuSTAR | NuSTAR+IXPE |
| :---: | :---: | :---: |
| diskbb |  |  |
| $k T_{\text {in }}(\mathrm{keV})$ | $1.00 \pm 0.04$ | $1.020 \pm 0.005$ |
| $N_{\text {d }}$ | $190 \pm 25$ | $168 \pm 5$ |
| comptb |  |  |
| $k T_{\text {S }}(\mathrm{keV})$ | $1.59 \pm 0.07$ | $1.575 \pm 0.005$ |
| $\alpha$ | $2.5 \pm 0.3$ | [2.5] |
| $k T_{\text {e }}(\mathrm{keV})$ | $3.4 \pm 0.3$ | [3.4] |
| $N_{\text {c }}\left(10^{-2}\right)$ | $3.7 \pm 0.1$ | $3.77 \pm 0.03$ |
| relxillns |  |  |
| $q_{\text {em }}$ | [3] | [3] |
| $a$ | [0.2] | [0.2] |
| incl (deg) | $28 \pm 8$ | [28] |
| $R_{\text {in }}$ (units of $R_{\text {ISCO }}$ ) | $5 \pm 3$ | [5] |
| $k T_{\text {bb }}(\mathrm{keV})$ | $=1.59$ | $=1.575$ |
| $\log \left(\xi / \mathrm{erg} \mathrm{cm} \mathrm{s}^{-1}\right)$ | $3.3 \pm 0.3$ | [3.3] |
| $A_{\mathrm{Fe}}$ | [1] | [1] |
| $\log n_{\text {e }}$ | [18] | [18] |
| $N_{\mathrm{r}}\left(10^{-4}\right)$ | $4 \pm 1$ | $3.3 \pm 0.3$ |
| Cross-calibration |  |  |
| numliv1 | $0.94 \pm 0.01$ | [0.94] |
| $C_{\text {FPMB-FPMA }}$ | $1.006 \pm 0.001$ | [1.006] |
| $C_{\text {DU1-FPMA }}$ |  | $0.907 \pm 0.005$ |
| $C_{\text {DU2-FPMA }}$ |  | $0.877 \pm 0.005$ |
| $C_{\text {DU3-FPMA }}$ |  | $0.827 \pm 0.004$ |
| ( Gain shift |  |  |
| $\alpha_{\text {DU1 }}$ |  | $0.989_{-0.002}^{+0.001}$ |
| $\beta_{\text {DU1 }}(\mathrm{eV})$ |  | $-24_{-8}^{+7}$ |
| $\alpha_{\text {DU2 }}$ |  | $0.987 \pm 0.002$ |
| $\beta_{\text {DU2 }}(\mathrm{eV})$ |  | $-16 \pm 8$ |
| $\alpha_{\text {DU1 }}$ |  | $0.990_{-0.001}^{+0.002}$ |
| $\beta_{\text {DU1 }}(\mathrm{eV})$ |  | $-15_{-6}^{+8}$ |
| $\chi^{2} /$ d.o.f. | 229/224 | 865/841 |
| Photon flux ratios ${ }^{(a)}$ |  |  |
| $2-8 \mathrm{keV}$ |  |  |
| $F_{\text {diskbb }} / F_{\text {tot }}$ | 0.51 |  |
| $F_{\text {comptb }} / F_{\text {tot }}$ | 0.43 |  |
| $F_{\text {relxillns }} / F_{\text {tot }}$ | 0.06 |  |
| 2-4 keV |  |  |
| $F_{\text {diskbb }} / F_{\text {tot }}$ | 0.66 |  |
| $F_{\text {comptb }} / F_{\text {tot }}$ | 0.30 |  |
| $F_{\text {relxillns }} / F_{\text {tot }}$ | 0.04 |  |
|  | $4-8 \mathrm{keV}$ |  |
| $F_{\text {diskbb }} / F_{\text {tot }}$ | 0.26 |  |
| $F_{\text {comptb }} / F_{\text {tot }}$ | 0.66 |  |
| $F_{\text {relxillns }} / F_{\text {tot }}$ | 0.08 |  |
| Energy flux ( $2-8 \mathrm{keV}$ ) |  |  |
| $F_{\text {tot }}\left(\mathrm{erg} \mathrm{cm}^{-2} \mathrm{~s}^{-1}\right)$ | $4.1 \times 10^{-9}$ |  |

Notes. Uncertainties are given at the $68 \%$ confidence level for one parameter of interest. Parameters in square bracket were kept frozen during the fit. ${ }^{(a)}$ The photon fluxes are in units of photon $\mathrm{cm}^{-2} \mathrm{~s}^{-1}$.
of comptb. We left the inclination, the inner disc radius (in units of the ISCO), and the ionization parameter free to vary. The inclusion of the relxillns component provides an excellent fit, with $\chi^{2} /$ d.o.f. $=229 / 224$. We report the best-fitting parameters in Table 3. From the spectral index $\alpha$ and electron temperature of comptb, using equations (17) and (22) of

Titarchuk \& Lyubarskij (1995), we obtain an optical depth $\tau$ equal to $2.1 \pm 0.3$ and $5.1 \pm 0.4$ for slab and spherical geometry, respectively.

The best-fitting parameters are quite typical for a NS-LMXB in the soft state. Assuming a distance to the source of 7.5 kpc , the normalization of diskbb corresponds to an inner disc radius of $\sim 10 \sqrt{\cos i} \mathrm{~km}$ (where $i$ is the inclination). As for the Comptonization component, we can estimate the size of the seed photon-emitting region from the best-fit parameters of comptb. Assuming that all seed photons are Comptonized, we computed the flux of the seed black-body spectrum, and hence the luminosity and the emission area as well (see also in 't Zand et al. 1999). We estimate that the seed photon-emitting region has an equivalent spherical radius of 5 km . This is consistent with the seed photons originating in a region smaller than the entire NS, such as the boundary layer.

The parameters that we derived with NuSTAR are not the same as those found by Chatterjee et al. (2023), who fitted AstroSAT data with a two-component model consisting of diskbb plus the Comptonization model nthcomp. For example, we find an inner disc temperature of $1.00 \pm 0.04 \mathrm{keV}$, while Chatterjee et al. (2023) report $0.65 \pm 0.04 \mathrm{keV}$. Concerning the Comptonization component, we find a seed photon temperature $k T_{\mathrm{s}}=1.59 \pm 0.07 \mathrm{keV}$, an electron temperature $k T_{\mathrm{e}}=3.4 \pm 0.3 \mathrm{keV}$, and an optical depth $\tau=5.1 \pm 0.4$ (assuming spherical geometry); Chatterjee et al. (2023) find $k T_{\mathrm{s}}=1.05 \pm 0.03 \mathrm{keV}, k T_{\mathrm{e}}=5.58 \pm 0.82 \mathrm{keV}$, and $\tau=3.72 \pm 0.69$ (also in spherical geometry). We note, however, that the AstroSAT data used by Chatterjee et al. (2023) were taken in July 2020, namely more than two years before the IXPE and NuSTAR observations. Chatterjee et al. (2023) performed a spectro-polarimetric fit using the time-average spectrum; however, they also report a time-resolved analysis of the AstroSAT spectrum split into four time intervals. From their Table 1, the spectral parameters during the fourth interval (i.e. the hardest spectral state) are most similar to the parameters we derived with NuSTAR. It is thus likely that the differences between our results and those of Chatterjee et al. (2023) are due to the spectral variability of the source.

### 3.2. Spectropolarimetric analysis

Once we obtained a satisfactory baseline model (diskbb+comptb+relxillns) for the source spectrum with $N u S T A R$ data, we used it to jointly fit the NuSTAR and IXPE spectropolarimetric data. As any of the three emission components can be polarized, we first employed the following XSPEC model:
c_cal $\times$ tbabs $\times\left(\right.$ polconst ${ }^{(d)} \times$ diskbb

+ polconst $^{(c)} \times$ comptb + polconst $^{(r)} \times$ relxillns $)$,
where c_cal denotes the cross-calibration constants. We note that relxillns includes the fluorescent iron line, which should be unpolarized; however, the line contribution to the photon flux of relxillns is only $\sim 10 \%$ in the $6-7 \mathrm{keV}$ band.

We find significant residuals at low and high energies in the IXPE/I spectra, which very likely are an artefact of calibration issues already observed in other sources (Taverna et al. 2022; Krawczynski et al. 2022; Marinucci et al. 2022). To correct them, we applied a gain shift to the response files of IXPE/I spectra with the gain fit command in XSPEC, and linked the gain parameters of $Q$ and $U$ spectra to those of the $I$ spectra. The energy shift was calculated using the relation $E^{\prime}=E / \alpha-\beta$,


Fig. 7. Best fit of the IXPE and NuSTAR spectra. Left panel: IXPE and NuSTAR deconvolved spectra with best-fitting model (see Table 3) and residuals. The model includes diskbb (dashed dotted line), comptb (dashed line), and relxillns (dotted line). Right panel: IXPE $Q$ and $U$ Stokes spectra with the best-fitting model, assuming either comptb (solid lines) or diskbb (dashed lines) as the only polarized component, and the corresponding residuals. Data from different detectors were combined (with setplot group) for plotting purposes.


Fig. 8. Left panel: contour plots of the PD and PA at 68,90 , and $99 \%$ confidence levels for the Comptonization component, assuming that it is the only polarized one. Right panel: similar contour plots for the reflection component. It is important to note the very different scale in the two plots.
where in our case $\alpha$ is not far from one and $\beta$ has an absolute value of $15-20 \mathrm{eV}$ (see Table 3 ).

In the model above, polconst assumes that the PD and PA of each component are energy-independent. To reduce degeneracy effects in the narrower IXPE band, we kept some parameters of relxillns and comptb fixed at their best value obtained with NuSTAR (see Table 3). The overlap in the $3-8 \mathrm{keV}$ range between IXPE and NuSTAR spectra, as well as $50 \%$ of their exposures (see Fig. 2) is expected to minimize the systematics in the derived polarimetric XSPEC parameters. However, the IXPE bandpass did not allow us to obtain tight constraints on the PD and PA of each component, so a series of assumptions based on theoretical and observational expectations was needed.

As a first test, we assumed that only one of the three spectral components is polarized, with the other two having a null PD. In first assuming a polarized disc only, the fit provides $\chi^{2} /$ d.o.f. $=879 / 841$ (151/96 for the subset of Stokes $Q$ and $U$
spectra). The fit is acceptable, but the assumption is not consistent with the observed PD increasing with energy (see Fig. 5); in fact, the opposite is expected from the disc contribution to the total photon flux (see Table 3). Considering, on the other hand, the case where either comptb or relxillns is the only polarized component, we obtain a better fit with $\chi^{2} /$ d.o.f. $=865 / 841$ (137/96 for the Stokes $Q$ and $U$ spectra) in both cases. We show in Fig. 7 the best fit assuming comptb as the only polarized component, noting that the residuals are essentially the same as the case where relxillns is the only polarized component. The model provides a good fit of both the flux spectra (left panel of Fig. 7) and the Stokes $Q$ and $U$ spectra (right panel of Fig. 7). In particular, we do not find strong residuals for the $Q$ and $U$ spectra (right, centre panel). For comparison, in Fig. 7 we also show the residuals for the $Q$ and $U$ spectra assuming that diskbb is the only polarized component (right, bottom panel). In Fig. 8, we show the contour plots of the PD and PA in the

Table 4. Polarization degree and angle of each spectral component for different scenarios described in Sect. 3.2.

| Component | PD (\%) | PA (deg) |
| :--- | :--- | :--- |
| diskbb | $[1]$ | $-41 \pm 25$ |
| comptb | $[1]$ | $63 \pm 7$ |
| relxillns | $30 \pm 8$ | $=\mathrm{PA}_{\text {comptb }}$ |
| diskbb | $<3.6$ | $=\mathrm{PA}_{\text {comptb }}-90$ |
| comptb | $[1]$ | $67 \pm 6$ |
| relxillns | $33 \pm 12$ | $=\mathrm{PA}_{\text {comptb }}$ |
| diskbb | $<3.7$ | $=\mathrm{PA}_{\text {relxillns }}-90$ |
| comptb | $[0]$ | - |
| relxillns | $44 \pm 12$ | $67 \pm 6$ |
| diskbb | $<2.9$ | $=\mathrm{PA}_{\text {comptb }}-90$ |
| comptb | $3 \pm 1$ | $67_{-6}^{+5}$ |
| relxillns | $[10]$ | $=\mathrm{PA}_{\text {comptb }}$ |

Notes. Parameters in square bracket are frozen.
two cases of Comptonization-only and reflection-only polarization. The reflection-dominated scenario requires a very large PD, because the reflection component is significant but subdominant, contributing to roughly $10 \%$ of the $4-8 \mathrm{keV}$ flux.

Besides the extreme cases tested above, there are many possible combinations that could explain the observed polarization. If we remove all assumptions and we leave all the polconst components free to vary, the PD of the Comptonized and reflected radiation are not well constrained, because these two components are quite degenerate: they peak at the same energy and have a similar spectral shape. Their total flux is clearly different, but their relative contribution to the polarized flux is uncertain.

Then, because of the similarity in spectral shape of GX 9+9 to Cyg X-2 (and in general to bright LMXBs in a soft state), following Farinelli et al. (2023), and the fact that the reflection component has a PA perpendicular to the disc surface (Matt 1993; Poutanen et al. 1996; Schnittman \& Krolik 2009), we assume that the PA of the reflected and Comptonized radiation are the same. We note that this configuration is consistent with a geometry in which the BL-SL has a vertical height significantly greater than its radial extension, with $H \gg \Delta R$. We started by fixing the PD of the Comptonized component at $1 \%$, assuming for the disc PD a conservative value of $1 \%$ at the inferred source inclination. We obtain a PD of the reflection component of $30 \% \pm 8 \%$, while the PA is $63^{\circ} \pm 7^{\circ}$ for the BL+reflection and $-41^{\circ} \pm 25^{\circ}$ for the disc ( $68 \%$ confidence). The disc PA is not tightly constrained; however, it is consistent with being perpendicular to the observed PA. We then assumed that the PA of the disc and BL+reflection components are perpendicular to each other. We subsequently left the PD of the disc free to vary, finding an upper limit of $3.6 \%$ ( $99 \%$ confidence on a single parameter) and a PD of the reflection component of $33 \% \pm 12 \% ~(68 \%$ confidence). Then, we fixed the PD of the Comptonized component at zero, obtaining an upper limit to the disc PD of $3.7 \%$ and a PD of the reflection component of $44 \% \pm 12 \%$. Finally, we left the PD of both the disc and Comptonized components free to vary, and we assumed that the reflected radiation has a PD of $10 \%$ (see, e.g. Fig. 7 in Matt 1993). In this case, we obtain an upper limit to the disc PD of $2.9 \%$ ( $99 \%$ confidence) and a PD of the Comptonized component of $3 \% \pm 1 \%$ ( $68 \%$ confidence). In Table 4 we summarize the different tests discussed above.

## 4. Discussion and conclusions

We investigated the X-ray spectro-polarimetric properties of the bright atoll NS-LMXB GX $9+9$ using IXPE and NuSTAR data. The polarimetric measurements are in agreement with those reported by Chatterjee et al. (2023); however, those authors fitted non-simultaneous AstroSat data with a two-component model that does not include reflection. The NuSTAR spectrum shows the presence of a $\mathrm{Fe} \mathrm{K} \alpha$ emission line, and a reflection component is needed to properly fit the data (see also Iaria et al. 2020). To the best of our knowledge, this is the first detection of a relativistically broadened iron line in this source. The reflection component is likely to play a significant role, as we argue in the following.

Similar to the case of Cyg X-2 (Farinelli et al. 2023), we only find an upper limit of $3-4 \%$ to the disc PD, which, because of the source inclination, did not allow us to ultimately derive tight constraints about the properties of a scattering atmosphere above the surface where the quasi-thermal spectrum is emitted (Shakura \& Sunyaev 1973; Page \& Thorne 1974). The marginal hint of a disc PA at a right angle with respect to the reflection component could be indicative of the presence of a scattering medium with $\tau \gtrsim 2$ anyways (Sunyaev \& Titarchuk 1985).

On the other hand, the data are consistent with the Comptonized component being significantly polarized, up to 3$4 \%$ depending on the assumptions. Gnarini et al. (2022) and Capitanio et al. (2023) discuss detailed numerical simulations of the X-ray polarization due to the Comptonizing region in NS-LMXB, assuming different geometrical configurations. In our case, the PA does not carry information because the orientation of the source is unknown; however, the measured PD constrains the possible geometries. The PD depends on both the shape of the Comptonizing region and on the inclination of the source to the line of sight. For the latter parameter, the fit with the relxillns model provides values in the range $i \approx 20^{\circ}-40^{\circ}$, namely an upper bound consistent with the value $i=40^{\circ}$ reported by Iaria et al. (2020). In any case, the inclination is known to be less than $70^{\circ}$ in this source (Schaefer 1990; Savolainen et al. 2009).

We show in Fig. 9 simulations of PD and PA of the Comptonized component, performed with the relativistic ray-tracing code MONK (Zhang et al. 2019) applied to the case of neutron stars (for details, see Gnarini et al. 2022). We assume three different geometries: an ellipsoidal shell around the NS equator, a torus covering the disc, and a wedge. The wedge and elliptical shell were chosen in order to reproduce the SL-BL geometries. The wedge is a spherical shell without polar caps that radially extends from the NS surface up to the inner edge of the accretion disc, and it covers the NS up to a latitude of $30^{\circ}$. The elliptical shell is characterized by a semi-major axis coinciding with the inner disc radius, and a maximum latitude of $30^{\circ}$. The torus has a minor diameter of 10 gravitational radii and covers part of the disc starting from its inner edge; it thus physically represents a puffed-up inner region of the disc. For the SL-BL geometries, the optical depth was measured in the radial direction from the NS surface (Popham \& Sunyaev 2001), while for the torus it is proportional to the minor radius. In all cases, we set an electron temperature of 3.4 keV , a seed photon temperature of 1.575 keV , and an optical depth of 5.1, corresponding to the best-fit values reported above (see Table 3).

We obtain a PD in the $2-8 \mathrm{keV}$ band of roughly $1-2 \%$ for the SL-BL and around $3-4 \%$ for the torus. The PA is approximately $180^{\circ}$ for all the three geometries, which in MONK corresponds to the polarization being parallel to the rotation axis. The torus


Fig. 9. MONK simulations of the PD and PA of the Comptonized component, as a function of the energy in the $2-8 \mathrm{keV}$ band, for three geometries: the elliptical shell, torus, and wedge. The assumed inclination is $40^{\circ}$ in all cases. The PA in MONK was measured from the projection of the rotation axis onto the sky plane.
geometry seems to produce a polarization signal consistent with our results. However, the BL or SL geometry is more realistic if we assume that the accretion flow extends down to the NS surface - as is expected for a source in the soft state.

All in all, it is likely that the observed polarization comes from a combination of different components. For example, a BL or SL with an ellipsoidal or wedge-like geometry could be consistent with the observed polarization if we include the contribution from polarized radiation reflected off the disc. On the other hand, a small or null PD of the Comptonized component, which would be expected for a shell-like geometry (Gnarini et al. 2022), seems to require a highly polarized reflection component. However, we cannot rule out the presence of a further, highly ionized reflection component, whose spectral shape would be almost indistinguishable from the primary continuum. For example, a highly ionized disc with $\log \left(\xi / \mathrm{erg} \mathrm{cm} \mathrm{s}^{-1}\right)=4$ would produce an essentially featureless reflection component (García et al. 2022). According to our results, the observed reflection component is not so highly ionized, but the reflecting medium also does not extend down to the ISCO. This leaves open the possibility that part of the reflection is due to a highly ionized innermost region of the disc, extended down to the ISCO. Unfortunately, the present data do not allow us to place strong constraints on this putative component because it is highly degenerate with the primary continuum and with the lower-ionization reflection component, which is - in any case needed to produce the iron line. If in our fits we include a further relxillns component with $\log \left(\xi / \mathrm{erg} \mathrm{cm} \mathrm{s}^{-1}\right)=4$ and an inner radius equal to the ISCO, its contribution to the $2-8 \mathrm{keV}$ photon flux is between zero and $30 \%$. Therefore, we cannot exclude that ionized reflection from the innermost region of the disc could significantly contribute to the observed PD.

As already discussed by Farinelli et al. (2023) in the case of Cyg X-2, reflection is likely to have a significant impact on the polarization signal. On the other hand, if the reflection component was the only one to be polarized, it would require a very large PD. The PD of the reflected radiation is not obvious to predict because it depends on the assumed geometry; however, it is not likely to exceed $\sim 20 \%$ (Matt 1993; Poutanen et al. 1996; Schnittman \& Krolik 2009). It is worth mentioning the results of

Lapidus \& Sunyaev (1985) who considered the case of radiation scattered off the accretion disc illuminated by the SL or the full NS surface corresponding to the emission during type I X-ray bursts. For an inclination angle $i \approx 40^{\circ}$, the PD reaches $\approx 5 \%$ for the SL over the NS radius-to-height ratio $H / R_{\mathrm{NS}}=0.1-0.2$ (see Fig. 7 in their paper). As the authors did not consider the direct disc emission, it can be instructive to include it and perform a simple Stokes vectorial analysis. We define the two polarization pseudo-vectors (here in the form of normalized Stokes parameters) for the BL+reflection and direct disc components:
$q_{i}=P_{i} f_{i} \cos 2 \Psi_{i}$,
$u_{i}=P_{i} f_{i} \sin 2 \Psi_{i}$,
where $P_{i}$ and $\Psi_{i}$ are the PD and PA of the two components ( $i=1,2$ ), respectively, while $f_{i}$ is their relative contribution to the total photon flux in the $2-8 \mathrm{keV}$ energy band. Using the values for $f_{i}$ reported in Table 3 and assuming $P_{1}=5 \%, \Psi_{1}=0^{\circ}$ for BL plus reflection and $P_{2}=1 \%, \Psi_{2}=90^{\circ}$ for the disc (i.e. parallel to the disc plane; see Farinelli et al. 2023), the total PD and PA are $\mathrm{PD}_{\mathrm{tot}}=\left(q_{\mathrm{tot}}^{2}+u_{\mathrm{tot}}^{2}\right)^{1 / 2}=1.94 \%$ and $\mathrm{PA}_{\mathrm{tot}}=0^{\circ}$, with the value of $\mathrm{PD}_{\text {tot }}$ being not far from the observed one. The same calculation in the $2-4 \mathrm{keV}$ and $4-8 \mathrm{keV}$ bands yields $\mathrm{PD}_{\text {tot }}=1.8 \%$ and $\mathrm{PD}_{\text {tot }}=3.7 \%$, respectively. To produce the net total PD, the disc PD can be quite low, which is well consistent with the observed upper limit of $3 \%-4 \%$. The energy-dependent PD value can be naturally explained by considering that the disc photon flux in the $2-4 \mathrm{keV}$ energy range is about five times higher than that in the $4-8 \mathrm{keV}$ interval, and thus the effect of polarization cancellation by two components polarized at about right angles is less at higher energies. This analysis shows that the accretion geometry of GX $9+9$, a bright atoll in the soft state whose spectrum resembles that of Z sources, is consistent with a BL-SL illuminating the ionized surface of the disc, producing polarized reflection as well as the (unpolarized) fluorescent iron line.

If the high-energy components do indeed dominate the X-ray polarization, a harder spectrum should be associated with larger polarization. Further observations of both atoll and Z sources in different spectral states will improve our understanding of the X-ray polarization of NS-LMXB, and thus of their accretion geometry.

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[^0]:    $\dagger$ Deceased.

[^1]:    https://heasarc.gsfc.nasa.gov/docs/ixpe/analysis/ IXPE-SOC-DOC-009-UserGuide-Software.pdf

[^2]:    ${ }^{2}$ https://nustarsoc.caltech.edu/NuSTAR_Public/
    NuSTAROperationSite/mli.php

[^3]:    3 The adopted number density is consistent with the inner region of a standard disc (see García et al. 2016, and references therein). Our fit is not sensitive to this parameter, because its effects on the X-ray reflection spectrum are only significant at lower energies (Ballantyne 2004; García et al. 2016).

