

1 **Size effect on the compressive strength of laminated bamboo lumber**
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19 **ABSTRACT:** The size effect on the axial compressive performance of laminated bamboo lumber is studied
20 through compression tests on three groups of short columns with different heights and section sizes. The
21 failure modes, bearing capacity, strain distribution, and deformation capacity were analyzed. Based on the
22 test results, three groups of Ramberg-Osgood models of laminated bamboo lumber with different sizes are
23 presented. The simulated results were in good agreement with the test results. The slope method and the
24 parameter method were used to calculate the size effect coefficient and the results showed that the linear
25 regression parameter analysis method is more efficient for analyzing the size effect. It is concluded that the
26 size effect coefficients of compressive strength, ultimate load, elastic modulus, ductility, and
27 compressibility are 0.043(1/23.26), 0.6676(1/1.52), 0.064(1/15.63), 0.0529(1/18.90), and 0.133(1/7.52)
28 respectively.

29 **Keywords:** A. Laminated bamboo lumber; B: Compressive strength; C: Size effect; D: Stress-strain model

30 **1 Introduction**

31 Nowadays, because of the increasing carbon emissions in the construction industry, it is necessary to
32 mobilise and develop new sustainable materials for construction use (Chen et al. 2020a, 2020b; Lv and
33 Liu 2019; Sun et al. 2020; Yang et al. 2020). Bamboo, as a widely distributed natural resource especially
34 in Asia and South America (Li et al. 2014) has the potential to fulfil this role (Sulaiman et al. 2006;
35 Krzesinska et al. 2008; Chen et al. 2020; Wang et al. 2020). A relatively new engineered material —
36 laminated bamboo lumber (LBL) (Li et al. 2016; Xu et al. 2019; Wu. 2014; Porras and Maranon 2012; Brito
37 et al. 2018) has attracted increasing attention from researchers (Sharma et al. 2015; Mahdavi et al.
38 2011,2012). The mechanical properties of laminated bamboo lumber could be compared with that of wood,
39 indicating this material has the potential to be an alternative and highly renewable building material (Verma
40 and Chariar 2012, 2013; Lopez and Correal 2009; Flander and Rovers 2008; Nugroho and Ando 2001;
41 Amada et al. 1997; Sharma 2017; Sinha et al. 2014; Correal et al. 2010,2014). As a new type of construction
42 material, laminated bamboo lumber not only maintains the advantage of high strength, good stiffness, and
43 low shrinkage, but can also be designed and manufactured into units of different shapes and sizes which
44 are easy to standardize and modularize (Li et al. 2015).

45 A specific code is essential for the application of laminated bamboo, and the size effect is an important
46 factor to determine design values. There has been multiple related researche studies on the compressive
47 properties of laminated bamboo lumber (Li et al. 2013, 2015), however, theoretical research on the size
48 effect on the compressive strength of laminated bamboo lumber is still lacking (Sharma 2017; Sinha et al.
49 2014; Correal et al. 2010, 2014; Verma 2013; Hong et al. 2019; Verma and Chariar 2012,2013). Therefore,
50 it is necessary to find out the size effect on structural laminated bamboo lumber for the further development
51 and promotion of standards based on exsiting studies.

52 The effect of size on the strength of brittle materials, such as wood, is based mostly on the Weibull
53 brittle-fracture theory. (Weibull 1939). Madsen and Buchanan (1986) studied the relationship between
54 flexural strength and the size of wood beams. Based on Weibull brittle-fracture theory, Zhou et al. (2010,
55 2011) calculated the parameters of size effect by both the slope method and parameter method. Barrett and
56 Griffin (1989) conducted tests on the flexural properties of Canadian SPF lumber from and concluded that
57 the size effect coefficient of bending strength is 0.22. Also, research showss that this theory is feasible in
58 analyzing the size effect of some bamboo-based composites. Madsen (1992, 2011) used the Weibull brittle-

59 fracture theory to explain the size effect of bamboo lumber and calculated the size effect coefficient. Wang
60 and Shao (2014) analyzed the fracture strength distribution of bamboo fibers and determined the influence
61 of size variations on their length and diameter according to Weibull brittle-fracture theory. Monteiro et al.
62 (2017) used the Weibull method to analyze the relationship between tensile strength and the diameter of
63 fibers extracted from a giant bamboo stem. Zhang et al. (2002) selected four groups of specimens with
64 different sizes to study the effect of size on the elastic modulus and tensile strength of KENAF fiber. Zhao
65 and Zhang (2019) designed specimens with five cross-section types to verify the feasibility of using the
66 Weibull brittle-fracture theory to explain the size effect of structural bamboo scrimber. The studies above
67 showed the feasibility of applying Weibull brittle-fracture theory on the analysis of size effect of wood and
68 bamboo composites. However, it is still not clear whether Weibull theory is efficient to study the size effect
69 on laminated bamboo lumber.

70 In this paper, specimens with three different cross-section sizes were designed and conducted axial
71 compression test to verify the feasibility of Weibull theory. The brittle-fracture theory of material strength
72 obeying Weibull distribution was established to study the size effect on the compressive strength of
73 laminated bamboo lumber. On this basis, the analysis model of size effect and the size effect coefficient
74 s_r of laminated bamboo lumber were determined.

75 **2 Test methods**

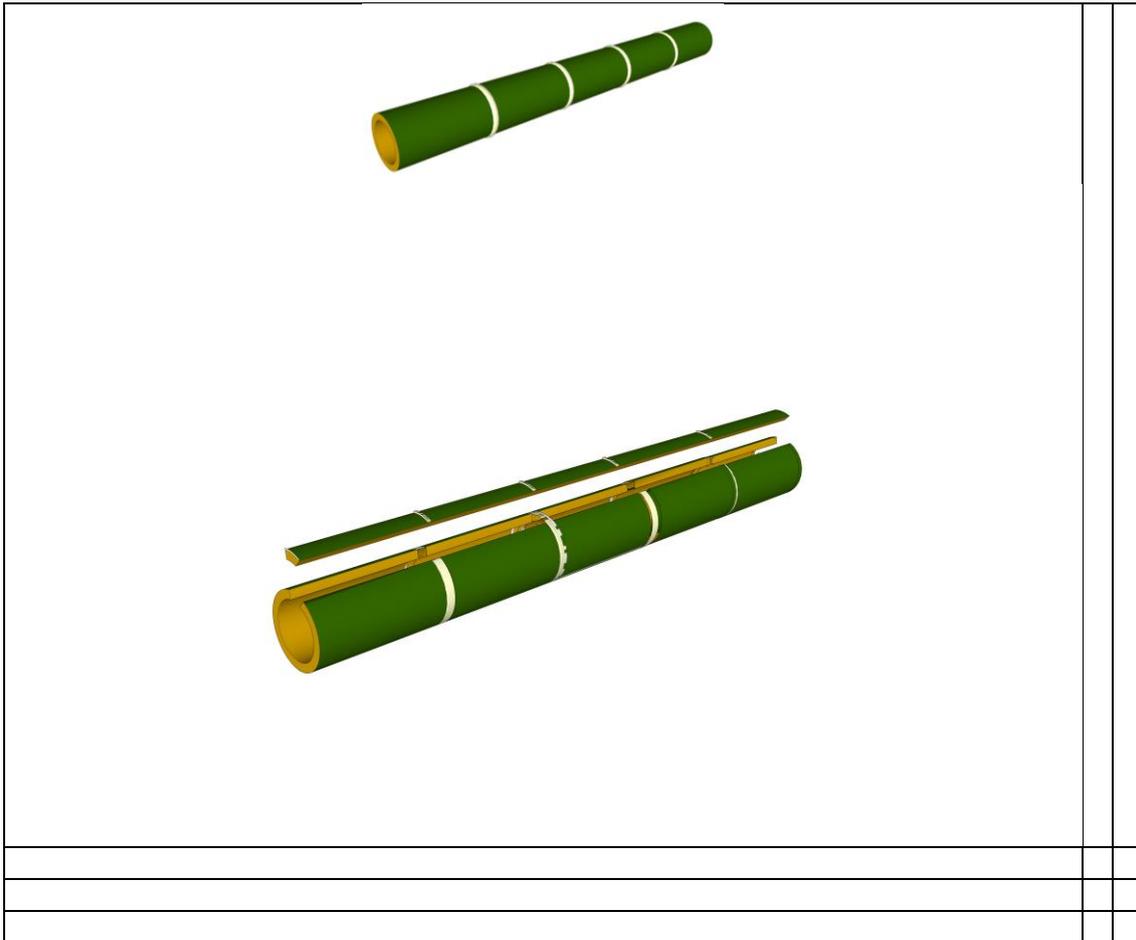
76 2.1 Design and fabrication of specimens

77 The source Moso bamboo (*Phyllostachys pubescens*, from Feng-xin, Jiang-xi province, China) was
78 harvested at the age of 3-4 years and manufactured into bamboo strips with the size of 2005mm×21 mm
79 ×7 mm. Then the specimens were made by hot pressing for 15 minutes under the conditions of main
80 pressure of 9 MPa, side pressure of 6.5 MPa, and temperature of 157 °C with resorcin as adhesive. The
81 production process is shown in Fig. 1.

82

83 **Fig. 1** Schematic diagram of the side-pressing laminated bamboo lumber production process

84 In this experiment, three groups of compression sp



85 specimens of different sizes were used based on ASTM D143. The ratio of height to thickness of all
 86 specimens was 2. The design sizes were 25mm×25mm×50mm, 50mm×50mm×100mm, and 100mm
 87 ×100mm×200mm, respectively. ASTM D143 specifies the use of specimens with an aspect ratio of 1:1:4
 88 however, Li et al. (2019) investigated the influence of length upon the behavior of parallel bamboo strand
 89 lumber (PBSL) specimensconcluding that the size of the specimen with instability failure was 50mm×50
 90 mm×200mm (slenderness ratio is 1:1:4). Therefore, 50mm×50 mm×200mm is not a good specimen size to
 91 include in a standard for measuring compression strength. This study also found that a 100 mm-long
 92 specimen with the same section size (50 mm×50 mm×100 mm) was subjected to a state of stress close to
 93 ideal axial compression. Therefore, 50 mm×50 mm×100 mm (slenderness ratio 1:1:2) would be the
 94 preferred size to include in a code of standard to measure compression strength. According to the above
 95 analysis, LBL and PBSL both belong to engineered bamboo, thus, specimens with an aspect ratio of 1:1:2
 96 were designed. The dimensions (b , h , l), moisture content (w), and density (ρ) of each set of specimens
 97 are listed in Table 1. As an example, 36 specimens in group C25 were numbered C25-1 to C25-36, with the

98 remaining specimens following the same nomenclature.

99 2.2 Test method

100 The test was carried out in the civil engineering and structural laboratory of Nanjing Forestry
101 University. Three different tonnage microcomputer-controlled electro-hydraulic servo universal testing
102 machines were used due to the differences in the maximum bearing capacity of the specimens with different
103 sizes, the broad side of the bamboo is marked as 'A' side, and then the clockwise direction is marked as A,
104 B, C, and D side in turn. The strain gauges are arranged in a 'T' shape and are attached to the four surfaces
105 of A, B, C, and D respectively.

106 The data were collected by a TDS-530 data acquisition instrument, and the axial displacement is
107 measured by a displacement meter. Load control was applied first with the speed of 700N/s until 150kN
108 was reached, then the displacement control was adopted by 5mm/min. The test duration of all specimens was
109 controlled in about 8 minutes, and the test was stopped when the load dropped to 70% of the ultimate load.
110 The diagram of the test set up is shown in Fig. 2.

111 **Fig. 2** Experimental setup for determining the compressive strength

112 3 Analysis of failure modes

113 The typical failure modes of each group of laminated bamboo lumber are divided into three types,
114 namely, end compression and buckling failure (mode 1), middle compression and buckling failure (mode
115 2), adhesive layer failure (mode 3), the number of failure in each mode for each group of specimens is
116 shown in Table 1.

117 **Table 1** Number of failure modes for each group of specimens

118 3.1 Failure mode 1

119 Fig. 3 shows the failure mode of six faces of the specimen C25-12 under failure mode 1. It can be seen
120 that the failure mode 1 is an end-buckling failure. The crack appeared at the end of the specimen where this
121 failure occurred, and the crack extended from the end to the middle and upper part of the specimen. As
122 shown in Table 1, 25 specimens were damaged in this way, accounting for 32.05% of the 78 specimens.

123 **Fig. 3** Mode 1 failure state (C25-12)

124 3.2 Failure mode 2

125 Fig. 4 shows the failure mode of the six surfaces of the specimen C50-14. It can be seen cracks
126 occurred first at the middle part of the specimens and extended to both ends of the specimens. Obvious
127 cracks can be seen at the lower part of the A and D faces, and the cracks at the middle part of the B and D
128 sides extended toward the end, accompanied by parallel cracks, which were not obvious around the bottom.
129 With the appearance of the joint, specimens were divided into two or more units, the whole rigidity of the
130 specimens were reduced and the bearing capacity were decreased. With the increase of deformation, the
131 bamboo strips broke and the specimens were destroyed.

132 **Fig. 4 Mode 2 failure state (C50-14)**

133 There were 36 middle compression-buckling failure specimens, accounting for 46.15% of the 78
134 specimens. Combined with the first failure mode, 61 specimens were damaged by ultimate buckling,
135 accounting for 78.21% of the total specimens. It can be seen that the compression specimens along the grain
136 were destroyed mainly because of buckling.

137 3.3 Failure mode 3

138 The failure mode of the C50-23 specimen is presented in Fig. 5. It can be seen that the failure mode 3
139 was caused by a crack in the glue line. At first, many parallel cracks occurred in the top part of the B face.
140 With the increase of load, the cracks extended downward and penetrated to the bottom of the specimen, the
141 laminated bamboo lumber was damaged by the bending of bamboo strips due to the cracking of the glue
142 joint between the laminates.

143 **Fig. 5 Mode 3 failure state (C50-23)**

144 It can be seen that when a certain load was reached, tiny cracks occurred first at the weak part of the
145 glue joint. With the continuous increase of the load, the crack began to spread to the whole glue joint surface,
146 and the weak side (the side close to the glue joint partition) began to bend. The number of such failure was
147 17, accounting for 21.79% of the total number of specimens. The main cause of the damage was the
148 adhesive failure, leading to the rapid decline of the load-carrying capacity.

149 3.4 Displacement-load analysis

150 The load-displacement curves are shown in Fig. 6, from group C25 to group C100.

151 **Fig. 6 Displacement-load diagrams**

152 As can be seen from Fig.6, specimens with compression load along to grain of LBL showed obvious
153 elastic-plastic behavior. Taking the specimen C50-5 as an example, the deformation stages of compression
154 along to grain were analyzed briefly. The failure process of specimen C50-5 can be divided into three stages:
155 elastic stage, yield stage, and failure stage.

156 Elastic stage: At this stage, the specimen was completely in the linear elastic state, the load and
157 displacement show a positive linear correlation, and there were no cracks.

158 Yield stage: The specimen showed an obvious plastic deformation after the elastic stage. In the second
159 half of this stage, bamboo strips showed an obvious increase in bending deformation while the load increase
160 was very small with accompanying micro-cracks which occurred locally and gradually extended to the
161 whole bonding surface.

162 Failure stage: With the appearance and extension of the crack, the specimen was divided into two or
163 more units with the whole rigidity of the specimen reduced and its bearing capacity decreased leading to
164 an uneven bearing force due to the inclination of the spherical seating of the loading platen. Due to the
165 friction between the two ends and the support surface, the transverse deformation was restrained leading to
166 the bulging of the bamboo specimen.

167 4 Results and discussion

168 4.1 Ramberg-Osgood model

169 In this paper, the Ramberg-Osgood model (Ramberg and Osgood 1943) was used for fitting the stress-
170 strain curve. The Ramberg-Osgood model (ROR) is suitable for stress-strain curves without an obvious
171 yield point. As shown in Eq. 1, the original formula for the Ramberg-Osgood model (Ramberg and Osgood
172 1943) is:

$$173 \quad \varepsilon = \frac{\sigma}{E} + k \left(\frac{\sigma}{E} \right)^n \quad (1)$$

174 Where ε is the strain; n is the strain index; k and n are set according to the properties of the material.
175 σ/E and $k(\sigma/E)^n$ are the elastic and plastic strains respectively. A parameter α , which is related to k ,
176 is defined by introducing σ_e as the reference strength in any state of the material at the elastic stage:

$$177 \quad \alpha = k \left(\frac{\sigma_e}{E} \right)^{n-1} = k \varepsilon_e^{n-1} \quad (2)$$

178 The improved equation of the Ramberg-Osgood model is obtained by substituting Eq. 2 into Eq. 3:

$$179 \quad \varepsilon = \frac{\sigma_e}{E} + \alpha \left(\frac{\sigma_e}{E} \right)^n \quad (3)$$

180 Substituting ε and ε_e in Eq. 8, and introducing the corresponding ratios to eliminate the elastic
181 modulus E, the stress-strain equation of Ramberg-Osgood model is obtained as follows:

$$182 \quad \frac{\varepsilon}{\varepsilon_e} = \frac{\sigma}{\sigma_e} + \alpha \left(\frac{\sigma}{\sigma_e} \right)^n \quad (4)$$

183 As long as the coefficients α and n are confirmed, a Ramberg-Osgood stress-strain constitutive model
184 can be determined as shown for specimens C25 to C100 in Fig. 7 below.

185 Fig. 7 Ramberg-Osgood model

186 As shown in the diagram above, the Ramberg-Osgood stress-strain models of different sizes of
187 laminated bamboo lumber are fitted according to the group type. The Ramberg-Osgood equation for each
188 group is shown below:

$$189 \quad \text{Group C25:} \quad \begin{cases} \frac{\varepsilon}{0.003} = \frac{\sigma}{38} + 0.133 \left(\frac{\sigma}{38} \right)^{4.85} & (0 \leq \varepsilon < 0.019) \\ \frac{\sigma}{65.90} = 1 & (0.019 \leq \varepsilon < 0.064) \end{cases} \quad (5)$$

$$190 \quad \text{Group C50:} \quad \begin{cases} \frac{\varepsilon}{0.003} = \frac{\sigma}{28} + 0.112 \left(\frac{\sigma}{28} \right)^{4.48} & (0 \leq \varepsilon < 0.016) \\ \frac{\sigma}{62.32} = 1 & (0.016 \leq \varepsilon < 0.088) \end{cases} \quad (6)$$

$$191 \quad \text{Group C100:} \quad \begin{cases} \frac{\varepsilon}{0.004} = \frac{\sigma}{30} + 0.133 \left(\frac{\sigma}{30} \right)^{5.49} & (0 \leq \varepsilon < 0.023) \\ \frac{\sigma}{57.03} = 1 & (0.023 \leq \varepsilon < 0.054) \end{cases} \quad (7)$$

192 4.2 Theory

193 Weibull brittle-fracture theory (Weibull 1939) lays the foundation for the study of the failure of brittle
194 materials such as wood or fiber-reinforced composites. The theory assumes that the material is composed
195 of many randomly selected units, and that failure of any unit leads to the failure of the specimen with the
196 strength of the unit following a Weibull distribution. According to Weibull theory, for the same loading
197 mode, the relation of average strength f to f_0 of specimens with volumes of V and V_0 can be given
198 by the following equation:

199
$$\frac{f_0}{f} = \left(\frac{V}{V_0}\right)^s = \left(\frac{V_0}{V}\right)^{-s} = \left(\frac{b}{b_0}\right)^{s_b} \left(\frac{h}{h_0}\right)^{s_h} \left(\frac{l}{l_0}\right)^{s_l} \quad (8)$$

200
$$\frac{f_0}{f} = \left(\frac{V_0}{V}\right)^{-s} = \left(\frac{b_0}{b} \times \frac{h_0}{h} \times \frac{l_0}{l}\right)^{-s} = \left(\frac{b_0}{b} \times \frac{h_0}{h} \times \frac{\tau b_0}{\tau b}\right)^{-s} = \left(\frac{h_0}{h} \times \frac{b_0^2}{b^2}\right)^{-s} \quad (9)$$

201 Where f and f_0 are the specimen strength; V and V_0 are specimen volumes; s is the size effect
 202 coefficient; s_t is the cross-section effect parameter; h and h_0 are specimen width; b and b_0 are the
 203 thickness of the specimen; l and l_0 are specimen length; τ is the height-thickness ratio of the
 204 specimen; s_b , s_h and s_l are size effect coefficients of specimen width, thickness and length respectively.
 205 In this test, the value of τ is 2.

206 The coefficient s_t can be evaluated by Weibull's brittle fracture theory. The slope method was used
 207 in this paper. For two specimens with the same section width to thickness ratio and different widths, Eq. 8
 208 can be simplified to Eq. 9 when the section ($b \times h$) and the strength f of the basic unit have been
 209 determined, the compressive strength f_0 of any specimen with the section ($b_0 \times h_0$) can be obtained.

210 Assuming that the laminated bamboo lumber specimen consists of an infinite number of randomly
 211 selected brittle units, the total specimen strength distribution function for all brittle units can be expressed
 212 by a three-parameter Weibull distribution function:

213
$$F(f) = 1 - \exp\left[-\left(\frac{f - \kappa_0}{m}\right)^z\right] \quad (10)$$

214 In Eq. 10, z, m, κ_0 are the shape, scale, and position parameters of the Weibull's brittle fracture theory,
 215 respectively. If the position parameter κ_0 is assumed to be 0. Then the Eq. 10 becomes a two-parameter
 216 Weibull distribution function, as shown in Eq. 11.

217
$$F(f) = 1 - \exp\left[-(f/m)^z\right] \quad (11)$$

218 If a specimen contains n units, the cumulative distribution function of the specimen should be derived
 219 from a unit function. When a unit function is a two-parameter Weibull distribution function, then n unit
 220 functions are:

221
$$1 - F_n(f) = [1 - F_1(f)]^n = \exp\left[-n(f/m)^z\right] \quad (12)$$

222 As shown in Eq. 12, $F_n(x), F_1(x)$ are two-parameter Weibull's brittle fracture theory functions of n

223 units and one unit, respectively. Eq. 12 can be transformed to give the compressive strength under different
 224 fractile of probabilistic distribution:

$$225 \quad f_q = m \cdot n^{-1/z} [-\ln(1-q)]^{1/z} \quad (13)$$

226 For two specimens of different sizes containing n_1 and n_2 units, the compressive strength ratio at any
 227 fractile is:

$$228 \quad \frac{f_q(n_1)}{f_q(n_2)} = \frac{mn_1^{-1/z} [-\ln(1-q)]^{1/z}}{mn_2^{-1/z} [-\ln(1-q)]^{1/z}} = \left(\frac{n_1}{n_2}\right)^{-1/z} \quad (14)$$

229 The parameter method is used to estimate the size effect coefficient based on the Weibull's brittle
 230 fracture function. When the distribution of the compressive strength follows a two-parameter Weibull's
 231 brittle fracture theory function, the distribution of the compressive strength under any fractiles $s_r = 1/z$.
 232 Therefore, for specimens with the same height to thickness ratio and different section widths, the s_r is
 233 equal to the reciprocal of the shape parameter z in the Weibull's brittle fracture. Currently, there are three
 234 distribution function fitting methods: probability weighted moments, maximum likelihood, and linear
 235 regression. In this paper, the linear regression method and maximum likelihood were used.

236 The linear regression method for calculating the size effect coefficient is as follows: firstly, the
 237 compressive strength is arranged in ascending order x_1, x_2, \dots, x_n : each value is assigned a position
 238 $p_i = i/(n+1)$; by calculating $t_i = \ln[-\ln(1-p_i)]$ and $y_i = \ln x_i$, then the coordinate point (t_i, y_i) is
 239 determined. All coordinate points are linearly regressed according to $y = bt + c$. The shape parameter, the
 240 scale parameter, and the fitting line slope b of the two-parameter Weibull's brittle fracture theory function
 241 are obtained, and the relation of intercept c is $z = 1/b, m = \exp(c)$.

242 For maximum likelihood, the likelihood function of the two parameter Weibull's brittle fracture theory
 243 function can be written as Eq. 15:

$$244 \quad \ln L = \sum_{i=1}^n \ln f(x_i) = n \ln z - nz \ln m + (z-1) \sum_{i=1}^n \ln x_i - \sum_{i=1}^n \left(\frac{x_i}{m}\right)^z \quad (15)$$

245 The partial derivatives of Eq. 15 are solved by an asymptotic method and iterative method.

246 4.3 Size effect of compressive strength

247 Table 2 presents the statistics of the ultimate load P_0 , the ultimate displacement u_0 , the compressive
248 strength σ_0 , the average longitudinal strain of the four faces ε_{y0} , the average transverse strain of the four
249 faces under ultimate load ε_{x0} . In addition, $\nu_{A,C}$ is the average Poisson's ratio of face A to face C, $\nu_{B,D}$
250 is the average Poisson's ratio of face B to face D, μ is ductility factor, a is compression coefficient, ρ
251 is the density of each group, and the mean value, standard deviation, coefficient of variation, and 95%
252 confidence value of the elastic modulus E . In this table, COV is the coefficient of variation; SDV the
253 standard deviation and CHV the characteristic value, calculated on the basis that 95% of specimens
254 exceeding the characteristic value (mean value-1.645×SDV).

255 Table 2 Statistics of test results

256 As can be seen from Table 2, the compressive strength of C25, C50, and C100 specimens decreases
257 with the increase of the cross-sectional area, which shows that there is an obvious size effect. The density
258 of the C25 group with a 95% confidence was 0.755g/mm³ (COV=2.31%), the C50 group was 0.667g/mm³
259 (COV=5.85%) and the C100 group was 0.720 g/mm³ (COV=0.935%). It can be seen that the density of
260 group C50 is lower than that of group C100, but its strength is higher than group C100, which shows that
261 the effect of density on the strength of bamboo laminated lumber is uncertain. Besides, the difference of
262 density with a 95% confidence between C50 and C100 groups is large, but the difference of MOE is small,
263 which shows that the effect of density on elastic modulus is uncertain.

264

265 The results show that when the ratio of height to thickness is constant, the compressive strength
266 decreases with the increase of the cross-sectional dimension, which indicates that the compressive strength
267 is obviously affected by the size values of laminated bamboo.

268 4.3.1 Determination of size effect coefficient by slope method

269 According to Weibull brittle-fracture theory (Weibull 1939) and ASTM D2915-1047 (2010), the
270 compressive strength along the grain direction of laminated bamboo lumber was determined knowing that

271 the length and thickness of the specimen have no size effect on the compressive strength along the grain
272 (ASTM D1990-2007). The application of the "Weibull brittle-fracture theory" to analyze the mechanical
273 properties of bamboo materials has been studied and the results showed that it is feasible to use the Weibull
274 brittle-fracture theory to study the size effect of laminated bamboo lumber.

275 In this paper, by applying the slope method and parametric method, specimens of group C25 were
276 taken as standard specimens. The fitted curve of the ultimate load of all groups is shown in Fig. 8(a). The
277 ultimate load size effect coefficient is 0.6254. The fitted curve of the compressive strength is shown in Fig.
278 8(b). The size effect coefficient of the compressive strength is 0.035(1/28.57).

279 In addition, the fitted curves of the mean Poisson's ratios of face A to face C and face B to face D are
280 given in Fig. 8(c) and Fig. 8(d) respectively. The size effect coefficients of the average Poisson's ratio of
281 face A and C, face B and D were 0.035 (1/28.57) and 0.027 (1/37.04), respectively. Fig. 8(e) shows the
282 fitted curves of the elastic moduli of all the test groups. In Fig. 8(g), it can be seen that the size effect
283 coefficient of the compression modulus of the laminated bamboo lumber is 0.09(1/11.11).

284 **Fig. 8** Scatter plot of material parameters

285 P_0 is the ultimate load, V is the volume, σ_0 is the compressive strength, $\nu_{A,C}$ is the average
286 poisson's ratio of face A and face C, $\nu_{B,D}$ is the average poisson's ratio of face D and face E, μ is the
287 ductility coefficient of each specimen; a is the compression coefficient, E is the elastic modulus of each
288 specimen.

289 In this paper, the size effect coefficient was calculated based on the test group C25. Fig. 9 shows the
290 fitted curves of different mechanical properties with a 95% guarantee rate for each group of specimens and
291 gives the fitted equations. As shown in Fig. 9(a), the fitted curve of the ultimate load with a 95% confidence
292 for each group of specimens varies with the volume of the specimens. The size effect coefficient for the
293 ultimate load is 0.668(1/1.50).

294 The compressive strength values of the three groups of specimens with a 95% confidence are
295 respectively marked in Fig. 9(b). The size effect coefficient of the average compressive strength of
296 laminated bamboo lumber specimens with a 95% confidence is 0.034(1/29.41).

297 The ductility coefficient of three groups of specimens with a 95% confidence is shown in Fig. 9(c).
298 From the fitted curve it can be seen that the size effect coefficient of the laminated bamboo lumber

299 compression specimen is 0.0529(1/18.90).

300 The compression coefficient of three groups of specimens with a 95% confidence is shown in Fig.
301 9(d). It can be seen that the size effect coefficient of the compression coefficient is 0.135(1/7.41). As shown
302 in Fig. 9(e), the size effect coefficient of the elastic modulus is 0.064(1/15.63) at the test with a 95%
303 confidence.

304 **Fig. 9** Fitted curves of mechanical properties with 95% guarantee rate

305 In the figures, $P_{0,95\%}$ is the values of the ultimate load, $\sigma_{0,95\%}$ the compressive strength, $\mu_{0,95\%}$ the
306 ductility coefficient value of the sample group and $a_{0,95\%}$ the compression coefficient of each test group
307 all with a 95% confidence level.

308 With the increase volume of specimens, the average compressive strength alongzxx grain decreased.
309 It can be concluded that the size effect coefficient is 0.034(1/29.41), which indicates that there is an obvious
310 size effect on the compressive strength of laminated bamboo lumber.

311 4.3.2 Determination of size effect coefficient by the parametric method

312 The size parameters of Weibull distribution estimated by the parametric method are almost consistent
313 with the results of non-parametric calculation when the two-parameter Weibull distribution functions are
314 fitted to the strength data (Zhou et al. 2011). This section uses the two-parameter method to calculate the
315 size effect coefficient. Currently, there are three commonly used methods, including the probability-
316 weighted moment method, maximum likelihood method, linear regression method. The linear regression
317 method and maximum likelihood calculation were used in this paper. As shown in Fig. 10, for the linear
318 regression fitted curves of three groups of specimens, the shape parameters λ and the size parameters m
319 of each group can be obtained, as well as the values of λ are averaged and compared with the reciprocal
320 of the size effect coefficient s_r obtained by the slope method. The results are shown in Table 3.

321 **Fig. 10** Two parameter Weibull distribution linear regression curves

322

323 **Table3** Estimated parameters of 2P-Weibull

324 As can be seen from Table 3, when the compressive strength follows a two-parameter Weibull
325 distribution function, the mean value of the shape parameter λ obtained by both linear regression and

326 maximum likelihood estimation is lower than the reciprocal of the shape parameter s_r obtained by the
327 slope method and so the slope method underestimates the effect of specimen size on compressive strength.
328 The size effect coefficient z is obtained by the slope method, and the size effect coefficient s_r is
329 obtained by the linear regression method and the maximum likelihood method. The final size effect
330 coefficients are 0.043(1/23.08) and 0.036(1/27.16) respectively, that is to say, when the ratio of height to
331 thickness is the same, the compressive strength decreases to 0.971 and 0.975 times when the width is
332 doubled.

333 Therefore, the Weibull brittle-fracture theory can be used to analyze the compressive strength of the
334 laminated bamboo lumber and other engineered bamboo.

335 The size effect of the 5%-fractile of the laminated bamboo lumber compressive strength is 0.034, that
336 is to say, the compressive strength of bamboo laminated lumber decreases to 0.977 when the width of the
337 laminated bamboo lumber is doubled under a certain ratio of height to thickness. The size effect coefficient
338 obtained by the slope method is smaller than that obtained by the parameter method, so it is suggested to
339 use the shape parameter method to obtain the size effect coefficient s_r .

340 The results of Zhou et al. (2010) show that the size effect coefficient of the compressive strength of
341 Chinese fir for wood structures is 0.11, with the linear regression method adopted to determine the final
342 value, the size effect coefficient of compressive strength along laminated bamboo lumber was
343 0.043(1/23.26). The results showed that the effect of dimension on wood compressive strength was more
344 obvious than that of laminated bamboo lumber. Zhao et al. (2019) studied the effect of the size of the
345 bamboo reconstituted material on the compressive strength. The results showed that the size effect
346 coefficient of the parallel bamboo strand lumber was 0.053, that is, the compressive strength of the parallel
347 bamboo strand lumber decreased by a factor of 0.964 for every doubling of the sample volume. It can be
348 seen that the compressive strength of engineered bamboo such as laminated bamboo lumber and parallel
349 bamboo strand lumber is lower than engineered timber, and the reason for this result is that there are more

350 internal defects (such as nodes and knots and other local wood characteristics) in wood than laminated
 351 bamboo lumber, and engineered bamboo timber is made by hot pressing and has a higher density and fewer
 352 pores than wood, so the size effect of laminated bamboo lumber is smaller than wood. Besides, the results
 353 of this study apply to axially compressed laminated bamboo lumber columns with strength failure, but not
 354 to those with unstable failure.

355 Through the above analysis, it can be seen that the compression test for laminated bamboo lumber
 356 conforms to the general rule of size effect, and the size effect formula of compressive strength of bamboo
 357 aggregate can be obtained as Eq. 16:

$$358 \quad \frac{f_0}{f} = \left(\frac{V}{V_0}\right)^{0.043} \quad (16)$$

359 f_0 and V_0 are the control specimens with known volume and axial compressive strength. If the
 360 volume V of laminated bamboo lumber aggregate is known, the compressive strength f can be
 361 obtained. The units of f and f_0 are megapascal (MPa), and the units of V and V_0 are cubic meters
 362 (m^3). In this paper, the C25 specimens are used as A reference, and its average resistance to pressure f_0
 363 degree is 69.4 MPa and its volume V_0 is $3.125 \times 10^{-5} \text{m}^3$. Therefore, this formula can be further simplified
 364 into Eq. 17. In this test, the compressive strength of three groups of specimens can be expressed in Eq. 18:

$$365 \quad \frac{69.4}{f} = \left(\frac{V}{3.125 \times 10^{-5}}\right)^{0.043} \quad (17)$$

$$366 \quad f_{25} = 1.030f_{50} = 1.061f_{100} \quad (18)$$

367 In the formula, f_{25} is the average compressive strength of the group C25, f_{50} is the average
 368 compressive strength of the C50 group, f_{100} is the average compressive strength of the C100 group.

369

370 **5 Conclusions**

371 In this paper, the effects of different sizes on the compressive strength of laminated bamboo lumber
 372 were studied, and the failure mechanism and size effects of different sizes were analyzed. An increase in

373 the specimens volume led to a decrease in the compressive strength along the grain. Based on the Ramberg-
374 Osgood model, a new stress-strain curve model was proposed.

375 The slope method and the parameter method were used to calculate the size effect coefficient. The
376 results showed that the linear regression parameter analysis method is more suitable to analyze the size
377 effect. It is concluded that the size effect coefficients are: 0.043(1/23.26) for compressive strength,
378 0.064(1/15.63) for elastic modulus, 0.0529(1/18.90) for ductility coefficient, and 0.133(1/7.52) for
379 compression coefficient. Compared with wood, the size effect has less effect on the compressive strength
380 of laminated bamboo lumber.

381

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393

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493

494 Figure Caption List

495 Fig. 1 Schematic diagram of the side-pressing laminated bamboo lumber production process:

496 (a) Original bamboo (b) Splitting (c) Original bamboo strip (d) Peeling (e) Bamboo strip (f) Laminated
497 bamboo lumber

498 Fig. 2 Experimental setup for determining the compressive strength

499 Fig. 3 Mode 1 failure state (C25-12):

500 (a) A side (b) B side (c) C side (d) D side (e) Top side (f) Bottom side

501 Fig. 4 Mode 2 failure state (C50-14):

502 (a) A side (b) B side (c) C side (d) D side (e) Top side (f) Bottom side

503 Fig. 5 Mode 3 failure state (C50-23):

504 (a) A side (b) B side (c) C side (d) D side (e) Top side (f) Bottom side

505 Fig. 6 Displacement-load diagrams:

506 (a) Displacement-load diagram of group C25 specimens (b) Displacement-load diagram of group C50
507 specimens (c) Displacement-load diagram of group C100 specimens

508 Fig. 7 Ramberg-Osgood model:

509 (a) Ramberg-Osgood model of a C25 group specimen (b) Ramberg-Osgood model of a C50 group
510 specimen (c) Ramberg-Osgood model of a C100 group specimen

511 Fig. 8 Scatter plot of material parameters:

512 (a) Relationship between ultimate load and volume (b) Relationship between compressive strength and
513 volume (c) Mean Poisson's of A and C surfaces (d) Mean Poisson's of B and D surfaces (e) Elastic
514 modulus (f) Ductility coefficient.tif (g) Coefficient of compressibility

515 Fig.9 Fitted curves of mechanical properties with 95% guarantee rate:

516 (a) 95% guaranteed ultimate load (b) 95% guaranteed compressive strength (c) 95% guaranteed
517 ductility coefficient (d) 95% guaranteed compression coefficient (e) 95% guaranteed elastic modulus

518 Fig10 Two parameter Weibull distribution linear regression curves

519

520

Table 1 Number of failure modes in compression test for each group of Specimens

Specimen set	Mode 1	Mode 2	Mode 3	Total
C25	9	16	10	35
C50	13	16	6	35
C100	3	4	1	8
Total	25	36	17	78

521

522

Table 2 Statistics of test results

Group	P_{\max} (kN)	u_0 (mm)	σ_0 (MPa)	ε_{y0}	ε_{x0}	$\nu_{A,C}$	$\nu_{B,D}$	E (MPa)	μ	a	ρ (g/cm ³)	
C25	AVG	44.47	8.3	69.4	55267	30814	0.38	0.311	10619	2.07	0.172	0.787
	SDV (%)	2.468	2.2	3.76	22824	17974	0.119	0.073	1419	0.442	0.032	0.018
	COV	5.55	26	5.41	41.3	58.33	31.43	23.54	13.37	21.31	18.88	2.31
	CHV	40.41	4.8	63.2	17722	1247	0.183	0.191	8284	1.35	0.119	0.787
C50	AVG	170.2	13	66.8	39271	20606	0.361	0.296	8355	1.80	0.130	0.738
	SDV (%)	11.4	2	4.38	12971	10950	0.091	0.063	1235	0.426	0.019	0.043
	COV	6.70	15	6.55	33.03	53.14	25.19	21.23	14.78	0.236	0.147	5.85
	CHV	151.5	9.9	59.6	17933	2593	0.211	0.192	6323	1.10	0.099	0.667
C100	AVG	571	20	57.8	36390	10751	0.355	0.273	7781	2.20	0.098	0.731
	SDV (%)	16.27	3.71	1.82	10243	4781	0.035	0.039	877	0.319	0.019	0.007
	COV	2.85	19	3.14	28.15	44.47	9.76	14.18	11.28	0.145	0.190	0.935
	CHV	544.2	14	54.8	19541	2887	0.298	0.209	6338	1.68	0.068	0.720

523

524

Table3 Estimated parameters of 2P-Weibull

Specimen	Regression		Likelihood		Slope method
	z	m	z	m	z
C25	21.10	71.10	21.52	71.15	
C50	17.57	68.77	17.56	68.95	—
C100	30.58	58.69	42.40	58.58	
Mean value	23.08	66.19	27.16	66.23	29.41

525