1 Title:

Modeling Fuzzy Fidelity: Using Microsimulation to Explore Age, Period, and Cohort Effects in
 Secularization

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21 Abstract

- 22 This article presents a microsimulation that explores age, period, and cohort effects in the decline
- 23 of religiosity in contemporary societies. The model implements a well-known and previously
- 24 empirically validated theory of secularization that highlights the role of "fuzzy fidelity," i.e., the
- 25 percentage of a population whose religiosity is moderate (Voas 2009). Validation of the model
- 26 involved comparing its simulation results to shifts in religiosity over 9 waves of the European
- 27 Social Survey. Simulation experiments suggest that a cohort effect, based on weakened
- transmission of religiosity as a function of the social environment, appears to be the best
- 29 explanation for secularization in the societies studied, both for the population as a whole and for
- 30 the proportions of religious, fuzzy, and secular people.

31 Keywords

32 demographic projection, religiosity, secularization, microsimulation, cohort effects

33 Introduction

- 34 What are the mechanisms that drive secularization in contemporary societies? Under what
- 35 conditions are populations most likely to experience a decline in religiosity? What role do age,
- 36 period, and cohort effects play in these processes? These are among the most contested

- 37 questions discussed by researchers interested in religion and demography. In this article we
- 38 attempt to contribute to these debates by describing the construction (and reporting on the
- 39 simulation experiment results) of a microsimulation model designed to simulate processes of
- 40 secularization hypothesized in a prominent theory of secularization (Voas 2009).

41 Secularization and Fuzzy Fidelity

The term secularization commonly refers both to the waning power of religious institutions and 42 to the waning of religiosity at the individual level, i.e.: "a decline in the extent to which people 43 44 engage in religious practices, display beliefs of a religious kind, and conduct other aspects of their lives in a manner informed by such beliefs" (Bruce 2002, p. 3). We focus in this article on 45 secularization at individual level, which involves a drifting away from identifying with a religion, 46 holding supernatural beliefs, attending worship services, praying, and regarding religion as 47 personally important. Here we will use the term "secular" as opposite to "religious" and the term 48 49 "secularity" to refer to the state of being secular.

50 Voas (2008) argues that the process of secularization (i.e., the long-term religious decline and 51 the complex of causal connections that promote it) is analogous to the demographic transition (i.e., the shift to longer life expectancy and then low birth rates in the presence of economic 52 53 development) in a number of respects, not least in that the trends are clear but the mechanisms 54 are not. The "secular transition" comes late in the course of modernization, and it is difficult to 55 slow, stop, or reverse once it begins. Voas subsequently offers a model to illustrate how the 56 seemingly disparate and complex patterns of religious change observed across Europe could all emerge from a common process of secularization. This article aims to replicate two key elements 57 in this theoretical and empirical treatment of "The rise and fall of fuzzy fidelity in Europe" (Voas 58 59 2009). The first is a quasi-linear downward trend in average religiosity. Although the levels of 60 religious involvement are very different across Europe (being high in Poland and low in the Czech Republic, for example), decline seems to be proceeding at about the same pace across the 61 continent. The second is the way that the share of the population that is neither fully religious 62 nor wholly secular - a group Voas labels the "fuzzy faithful" - rises and then falls over a period 63 64 of two centuries or more.

In keeping with the literature on the diffusion of innovations (Kucharavy and De Guio 2011; 65 Rogers 2003), the model assumes that the rise of secularity follows a logistic (S-shaped) 66 67 trajectory. People do not convert from active religiosity to complete secularity in a single step. The rise in the secular share of the population lags behind the decline in the religious share, 68 69 which makes it possible for the fuzzy faithful to become a majority. Ultimately, however, the proportion in the fuzzy middle falls as the secular transition continues. Explaining these 70 71 processes of secularization requires attending to three effects: age, period, and cohort. Age 72 effects change religiosity in individuals at particular points in the life course (as a result, for 73 example, of having children or losing parents). Period effects have an impact on everyone alive at 74 a given time and might be associated with crises such as war, recession, or pandemics. Cohort 75 effects are generation-specific changes that are typically linked to the environment of upbringing 76 and peer interactions in teenage years.

77 The APC Identification Problem

Because any two of age, current year, and year of birth determine the third, there is no unique way (at least on the surface) to determine which of the three processes explain religious decline in secularizing contexts. This is the so-called APC identification problem, which was first analyzed in terms of the APC accounting model (Mason et al. 1973). For example, cohort effects could be equivalently explained by combining period and age effects. The difficulty in identifying these processes is exacerbated in part because data is available only for a couple of decades. Fortunately, in the specific case of the secularization process, we are not helpless in the face of

85 the APC identification problem. There is now aggregate data spanning over four decades and 86 analyses of this data have led researchers to strongly favor a cohort-replacement explanation of 87 the secularization process; even though it is still logically possible that alternative explanations may have produced the observed patterns (Voas 2009; Voas and Chaves 2016). It is then 88 89 possible to make a plausibility argument: when cohort effects explain religious decline with 90 decent fit, it is mathematically possible but sociologically implausible that apparently independent 91 age and period effects could be so perfectly synced that they produce the same result (e.g., Voas 92 & Chaves 2016).

93 But we can rarely be confident that only one or two of these effects are in play with any 94 particular demographic phenomenon, so something else needs to be done to escape the APC identification problem. One approach is to use so-called 'side information' to guide our choice in 95 96 the set of feasible solutions. However, this approach relies on theoretical assumptions that are 97 rarely justified or verifiable (Reeves 2016). Another is to use non-linear models of these effects as 98 a way around their linear dependence. Assuming that all three are indeed in play, however, one 99 might wonder whether age, period, and cohort effects interact such that hidden constraints might permit optimal explanations. This has led to innovations such as the APC-interaction 100 model (APC-I). Luo & Hodges (Luo and Hodges 2020) use the APC-I to handle a classic 101 instance of interaction effects with the possibility of distinctive interactions between age and 102 103 period. The APC-I enhancement and correction to the classical APC accounting model is an example of a cautious embrace within sociology and demography of methods capable of 104 105 handling formally complex systems, which are characterized by non-linear interaction effects,

amplifying loops, and dampening processes.

107 *Rationale for Using Microsimulation*

108 The most powerful method for understanding and explaining complex social systems is computational simulation, which can be thought of as an intensification of the move Luo and 109 Hodges made in introducing the APC-I. Computational simulations can give expression to every 110 kind of interaction effect, not just the one type that appears in the APC-I. Moreover, they need 111 not be limited to linear models, unlike the APC-I. They can handle forbidding complexity in 112 terms of time periods, non-linearity of interacting variables, and underlying causal processes. 113 This latter point seems promising to social psychologists, for whom the sociologist's traditional 114 framing of the APC identification problem is an odd abstraction from the concreteness of 115 human minds in which age, period, and cohort effects are merely facets of a complex process of 116 self-evaluation and self-transformation in rich social settings. Methods suited to handling 117 complexity, and computational simulation above all, have enormous potential to tackle seemingly 118 119 intractable problems, such as the APC identification problem that arises whenever sociologists 120 try to explain population change in secularizing contexts.

121 The model presented in this paper does not go so far as to articulate a causal architecture of religious change within individual human minds. That is a possibility for computational 122 123 simulations and one that our research group hopes to realize in due course. The current model 124 has a more modest aim: to implement the potential APC processes as described in the literature and demonstrate the possibility and usefulness of a model that (1) is not based on linear 125 126 assumptions, as APC models have tended to be; (2) includes all three processes of change operative within the same artificial society; (3) promotes evaluation of the relative importance of 127 128 those types of change; and (4) simulates up to two and half centuries, from early modernity all 129 the way through the last several decades and onwards into the future yielding population 130 projections for religiosity. Thus, this is a proof-of-concept model, establishing that the vehicle 131 functions well even if its full power remains to be exploited. The conclusion of the analysis is 132 secondary. In fact, assuming the kind of S-curve process of decay in religiosity documented in 133 Voas 2009, the model shows that cohort effects supply the best explanation, which is a

134 conclusion broadly favored within the literature (Idler 2021; McAndrew and Richards 2020; 135 Molteni and Biolcati 2018; Stolz, Biolcati, and Molteni 2021; Voas and Chaves 2016; Brauer 136 2018). But that result should be understood not as an argument for the greater importance of 137 cohort changes so much as validation of a proof-of-concept model with almost unlimited potential for deeper exploration. 138

139 Using agent-based models in this context combines the benefits of top-down (driven by macro-level forces) and bottom-up (driven by individual-level behaviors) analysis. On the one 140 141 hand, complicated theories about the origins and operation of age, period, and cohort effects can 142 be represented straightforwardly. The influences can wax and wane in non-linear ways, and likewise they can interact with each other. It would be extremely difficult to infer details of such 143 complexity from a statistical model. The simulation can thus be theory-driven and deductive 144 145 rather than wholly data-driven and inductive. Data have an important role in validating and calibrating a computational simulation, but theoretical considerations are the starting point. On 146 the other hand, the outcome of the simulation ultimately depends on individual-level actions and 147 148 decisions. The environment can matter a great deal, but the unit of analysis is the agent rather 149 than some impersonal force. Explanation may start and end at the macro level, but it must also operate via the micro level (Coleman 1994). If we want to understand the social or psychological 150 151 mechanisms at work, we need to track what individual agents do. This focus on agency makes 152 simulation more humanistic than might be immediately apparent (Diallo et al. 2019).

There is significant empirical evidence related to the age, period, and cohort effects that are 153 154 at work in religious change. For example, panel data from countries where there has not been much aggregate movement away from religion (including highly developed countries such as 155 Israel) can help us to see whether and how religious involvement changes with age or life stage in 156 the absence of secularization (Eisenstein, Clark, and Jelen 2017). No simple story applies 157 universally: we can see clear signs of period effects (with many people drifting away from religion 158 159 during adulthood) in some countries and not in others, for example. And even where generational replacement appears to have far greater impact than age or time, the size of the 160 161 generation gaps (i.e., cohort effects) will also rise and fall (Voas 2009; Molteni and Biolcati 2018; McAndrew and Richards 2020; Stolz 2020; Idler 2021; Brauer 2018). 162

163 We aim, then, to implement our best conjectures about the proximate mechanisms of 164 religious change in a model to see what trajectories they produce, from the outset of the 165 secularization process to a point centuries later. Models generating outcomes that are at odds with our real-world observations can be rejected. The objective is to identify a small number of 166 models that are consistent with 1) theories about how religiosity is or is not acquired, maintained, 167 and transmitted; and 2) data from societies at different stages in the secular transition. Ideally, we 168 will be able to identify patterns of religious change that apply to many countries, as past work 169 170 suggests may be possible. We also hope to find models that accommodate exceptions or 171 variations.

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Below we provide a description of the APC processes implemented in the simulation.

173 *Period effect processes*

We conceive two different period-effect processes, one static and one dynamic. In the static 174 175 process, agents' religiosity decreases every year at a constant rate throughout their life, regardless of starting religiosity, inherited parental religiosity, or age of agent. This static process is 176 177 capturing latent societal-level factors (e.g. improving education, existential security) that are 178 theorized to encourage decline in religiosity over time (Bruce 2011; Norris and Inglehart 2011; 179 Wildman et al. 2020) and these impact everyone living in the society. In the dynamic process, 180agents' religiosity decreases throughout the life of the individual, regardless of starting religiosity, 181 inherited parental religiosity, or age of agent, but the degree of change is a function of religiosity. 182 Thus, the absolute decline in an agent's religiosity varies across time, where change is smallest

among the most religious and secular individuals, and there is a larger decline for those in the
middle of the religiosity spectrum. This dynamic process therefore accounts for highly religious
traditions that preserve their religiosity better than others, as well as a reluctance among the
nominally religious to reject all religion and become wholly secular (Day 2011; Smith and Denton
2009).

188 *Cohort effect processes*

189 Parents transmit their religiosity to their offspring with a bias towards lower religiosity values. We call this a cohort effect, since after the inheritance event, when the individual reaches age 12, 190 their religiosity remains constant. This cohort process is supported by evidence that a 191 consistently large predictor of one's own religiosity is the religiosity of one's parents and there is 192 a net decline in religiosity from parents to children in secularizing societies (Cragun et al. 2018; 193 194 Min, Silverstein, and Lendon 2012; Storm and Voas 2012; Brauer 2018). We also consider an alternative in which the size of the cohort effect depends on how religious the society is. In this 195 196 case, agents inherit the religiosity of their parents minus a value that reflects the current secularity 197 of the environment (i.e., the share of individuals classified as seculars). We test which of five different measures provides the best fit, based on the relative frequency in the population of the 198 199 religious, fuzzy, secular, or non-religious (i.e., secular plus fuzzy), or on the product of the religious and secular shares. The rationale behind this assumptions is that just as in the real 200 201 world, the social environment in the model changes over time, and the aggregate level of 202 religiosity has an impact on religious transmission and socialization of individuals in adolescence, when their religious identities, beliefs and practices are being formed (Min, Silverstein, and 203 204 Lendon 2012; Strhan and Shillitoe 2019; Voas and Storm 2021).

205 Age effect processes

It is easily argued that age effects on their own cannot produce religious decline. Although 206 people may become more or less religious as they age, that fact would not alter the average 207 208 religiosity of a stationary population (Voas 2009). To explain secularization, we require period or cohort effects, or some combination of the two, with age effects having at most a moderating 209 influence. Those might still be significant (if some people return to church while raising a family, 210 for example), but the central question is whether individual-level religious change occurs mostly 211 212 early in life (especially adolescence and young adulthood) or is spread over much of the life 213 course.

214 Based on findings from the literature, we devised three different processes by which age 215 affects agents' religiosity, independently of inheritance at age 12. In the first process, agents decrease their religiosity as they become older (Lechler and Sunde 2020). In the second one, the 216 effect is reversed, i.e., the religiosity of agents increases as they become older (Argue, Johnson, 217 218 and White 1999; Azzi and Ehrenberg 1975; Bengtson et al. 2015; Iannaccone 1998). In the third one, agents decrease their religiosity up to an age at which their religiosity starts to increase again, 219 220 a U-shape effect (Hayward and Krause 2013). These age effects always occur in combination 221 with period or cohort processes because (as mentioned above) age effects alone can never explain secularization processes. 222

223 The Fuzzy Fidelity Microsimulation

224 *Microsimulation overview*

225 The microsimulation explores the way that different APC processes lead to a decrease in 226 religiosity over time in a stationary population. (For specificity, we adapted the initial age 227 structure and vital rates from those for Norway, as described below.) The microsimulation was 228 implemented in AnyLogic 8 University version 8.5.2. We designed this microsimulation mindful 229 of the concerns of social and cognitive scientists of religion, particularly those interested in 230 religious decline. The entities represented in the simulation are human agents characterized by 231 age, generation, and religiosity. The religiosity of agents ranges between 0 and 1. We subdivide 232 this range into three equal intervals, classifying agents as religious (R) if their religiosity (a variable 233 ranging between 0 and 1) is \geq 0.66, seculars (S) if it is \leq 0.33, and fuzzies (F) otherwise. During the simulation, the religiosity value of each agent changes according to specific APC processes. 234 These processes are based on theory and evidence about the age, period, and cohort effects that 235 236 we find in studies of religious change. The overall decrease of agents' religiosity in each of these 237 APC processes is an umbrella estimate representing several factors hypothesized and shown to 238 decrease religiosity in human societies, e.g., religious socialization, existential security, pluralism, 239 education, freedom of expression, etc. (Stolz 2020; Wildman et al. 2020; Gervais, Najle, and 240 Caluori 2021).

241 Voas (2009) starts from a population that is 95% religious, with only 4% in the fuzzy 242 category. In our view that distribution exaggerates the level of religious commitment in even the most traditional societies; it is more realistic to assume that an appreciable proportion of the 243 population is slightly detached from belief and practice. We therefore assume that, although only 244 245 1% of the population qualifies as secular at the beginning of the process (agreeing with Voas), 246 15% can be regarded as fuzzy. A Weibull distribution with appropriate parameters is well suited 247 to defining our starting point. The overall mean religiosity at the outset is 0.81; within the three categories of religious, fuzzy, and secular, the group means are 0.86, 0.56, and 0.22, respectively. 248 249 The shares of these groups gradually change from one year to the next, and at the same time the 250 average distribution of religiosity changes in a secular direction.

251 The initial population is fixed at 1000 agents. The values for age, mortality, and fertility are 252 based on statistics obtained from Statistics Norway (Statistisk Sentralbyrå; 253 https://www.ssb.no/en/befolkning). The starting age distribution follows that of the Norwegian 254 population in 1900. For simplicity, we assume no gender and, to keep the population relatively 255 constant, the total fertility rate is fixed at 1.005 per agent throughout the simulation. Thus, every 256 agent produces an average of 1.005 new agents during the reproductive ages of 15-49, equivalent 257 to fertility of 2.01 children per woman. When turning 12 years old, agents born in the simulation 258 inherit a religiosity value similar to that of their parents (see APC processes). If the parent dies 259 before the agent turns 12, the value inherited is similar to that when the parent was last alive. Further, also for simplicity, we use a constant mortality schedule throughout, with life 260 261 expectancy of approximately 80 years. In each annual time step, agents experience the following: 262 they age by one year, die or give birth with a probability according to their age, and change their religiosity according to the APC process being applied. In all cases, the change in the agents' 263 264 religiosity is deterministic and governed by the equations given in each of the following 265 processes.

266 *Cohort effects: simple and social influence*

Cohort processes are supported by evidence showing that a consistently large predictor of one's
own religiosity is the religiosity of one's parents and that there is a net decline in religiosity from
parents to children in secularizing societies (Cragun et al. 2018; Min, Silverstein, and Lendon
2012; Storm and Voas 2012; Brauer 2018). Following this, in the model, at 12 years old agents
inherit the religiosity value of their parents with a bias (eq. 1).

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 $REL_{offspring} = REL_{parent} * Bias$ eq. (1)

where *REL* is the religiosity value of the offspring and parent, respectively, and *Bias* is a value drawn from the Weibull distribution function of AnyLogic. This function takes two different values: alpha, the shape parameter, and beta, the scale parameter. Its formula is given by equation2782:

 $f(x) = e^{\frac{x^{\alpha}}{\beta}}$ eq. (2)

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the values of alpha and beta are constrained within specific ranges so the distribution will be skewed and thus the religiosity values of offspring will be on average lower than those of their parents.

We implemented an alternative cohort effect that explicitly incorporates social influence rather than simply a general downward bias. In this case, 12-year-old agents inherit the religiosity of their parents minus a constant (*C*) multiplied by the proportion in the population of one of the following: a) non-religious, b) religious, c) fuzzies, d) seculars, or e) religious multiplied by seculars. The whole term is then multiplied by *Noise*, a value from a normal distribution with $\mu=1$ and $\sigma=sd$ (eq. 3). Where *sd* is a parameter determined during the optimization experiments (see below).

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$$REL_{offspring} = (REL_{parent} - (C * Prop. agent. category)) * Noise$$
 eq. (3)

Recall that agents are categorized as religious, fuzzy, or secular depending on whether they are in the upper, middle, or lower third of the religiosity range. The environment changes over time as the population becomes more secular, and transmission of religiosity from parents to children tends to be increasingly affected as aggregate religiosity falls.

299 *Period effects: static and dynamic*

We model period effects as the loss of individual religiosity over time. At age 12, agents inherit the religiosity of their parents times some noise (value from a normal distribution with μ =1, σ =0.05). Thereafter, their religiosity declines year by year according to equation 4. This static process captures latent societal-level factors (e.g. improving education, existential security) that are theorized to encourage decline in religiosity over time (Bruce 2011; Norris and Inglehart 2011; Wildman et al. 2020) and impact everyone living in the society.

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$$REL_{t+1} = REL_t - Inhibitor$$
 eq. (4)

The value of the inhibitor may be a constant or a dynamic value. When dynamic, the inhibitor is a function of the agent's current religiosity, as shown equation 5. This dynamic process accounts for highly religious traditions that preserve their religiosity better than others, as well as a reluctance among the nominally religious to reject all religion and become wholly secular (Day 2011; Smith and Denton 2009).

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Inhibitor =
$$A * (REL_t - 0.5)^2 + C$$
 eq. (5)

318 where REL is the religiosity value of the agent at time *t*, *C* is the vertex of the quadratic function 319 (i.e., the maximum value that the inhibitor can take), and *A* is a constant (-4**C*) that keeps the 320 boundaries of the quadratic function at 0 (Figure 1). Note that the decrease in religiosity occurs 321 fastest when current religiosity is close to 0.5 and more slowly when the value is near the 322 extremes of 0 or 1. This reflects that the most strongly religious families resist secularizing 323 processes within their children most effectively, and less religious families aren't as successful in religious transmission (cf. Smith 2005). Further, note that in both cases (static and dynamic), when the value of the inhibitor is greater than $Rel_{(t)}$, then $Rel_{(t+1)}$ is set to 0.

326 327

Fig 1 here

328 *Age effects: religiosity decreasing and increasing with age*

We devised three different processes: (1) agents decrease their religiosity as they become older, (2) agents increase their religiosity as they become older increase, and (3) agents decrease their religiosity up to an age at which their religiosity starts to increase again (U-shape effect). Note that these three effects have an empirical basis (see age processes section). Hence, in the model, when an agent becomes 12 years old and the decrease process is active, the age of the agent modulates the value of the religiosity inhibitor; see equation 6.

$$REL_{t+1} = REL_t - (Inhibitor * Age Effect)$$
 eq. (6)

where the inhibitor is a constant value or dynamic value (defined the same way as in eq. 4 and eq.5, above), and age effect is given by equation 7:

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354 355 356 Age effect = $(1 - Age_{standardized})^{\gamma}$ eq. (7)

The age of agents is standardized between 1 and 0: 1 when an agent's age is 12 years old and 0 when an agent's age is \geq 100 years old. Thus, when an agent is 12 years old the age effect is maximum and so is the value of the religiosity inhibitor (Fig 2). Thereafter the age effect decreases as an agent gets older; this decrease is linear or non-linear depending on the value of gamma (γ) (Fig. 2).

Under the influence of the second age effect process, the religiosity of agents increases as
they become older. Religiosity starts increasing when an agent reaches a minimum age, the age of
the agent then modulates the value of the religiosity enhancer; see equation 8.

$$REL_{t+1} = REL_t + (Enhancer * Age Effect)$$
 eq. (8)

Fig 2 here

357 where the enhancer is a constant value, and the age effect is given by equation 9:

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Age effect = $(Age_{standardized})^{\gamma}$ eq. (9)

Fig 3 here

In this case, age is standardized between 0 and 1: with 0 being the minimum age at which religiosity starts to increase and 1 being when agents are 100 years old or older. Thus, when an agent reaches the minimum age, the effect of age is minimum and so is the value of the enhancer (Fig 3). Thereafter the age effect increases with age reaching its maximum value at 100 years old. Depending on the value of gamma, the age effect may increase linearly or non-linearly (Fig. 3).

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369 Finally, when the third age effect process is active, religiosity starts decreasing at age 12,

according to equation 6 and 7; then, when reaching a minimum age, religiosity starts increasingaccording to equation 8 and 9.

372 *Microsimulation and APC processes combinations*

373 Table 1 summarizes the combinations of processes that were implemented in the microsimulation. We defined two types of cohort effects (simple and social-influence, in five 374 375 variations depending on the nature of the social influence), two types of period effects (static and 376 dynamic), and three types of age effects (decreasing, increasing, and decreasing/increasing with 377 age). From the numerous combinations possible, we selected those that express fundamental 378 options for interpreting demographic process of religious change. Note that the final option in 379 Table 1 includes all five variations of social influence expressing cohort change in religiosity (H, 380 I, J, K, L).

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Table 1 here

383 Analysis of empirical data

384 We needed to evaluate variants of the microsimulation model against data, and we did so using 385 three different approaches. The first and second approach assume that the religiosity decay is 386 logistic and calculate this decay at the cohort and population level respectively. For these calculations, we used the data generated in the model of Voas (see Voas 2009 for details of the 387 data analysis), which assumes logistic decay; this model passed tests against available data so 388 389 there is a sturdy empirical basis for using it. The third approach assumes that the religiosity decay 390 is linear, we used data from the European Social Survey, extrapolating outwards to cover 200 391 years. These comparator models are described below.

For the case that religiosity decay is logistic, the projected dynamics of the rise and fall of R-F-S shares over 200 years are shown in Figure 4. The basic concept is that the secular transition starts when the religious share of the population begins to decline, slowly at first, then more rapidly, and slowly again as it approaches a floor. The change in religious share (RS) is given by equation 10:

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$$RS = \frac{0.88}{1 + e^{-3.15} * e^{0.03 * Year}}$$
 eq. (10)

The wholly secular share (SS) rises from an initial level of just 1%, following the logistic
 trajectory given by equation 11:

$$SS = \frac{1}{1 + e^{4.6} * e^{-0.025 * Year}}$$
 eq. (11)

Fig 4 here

The slight lag between these two trends generates the rise of the fuzzy share (FS = 1 - [RS + SS]), which ultimately declines as more complete secularity takes hold (Figure 4). The R-F-S curves relate to birth cohorts, following Voas (2009), and hence we take these graphs as representing 40 5-year cohorts.

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412 The shares of the religious, fuzzy, and secular can be used in conjunction with the average 413 religiosity within each group to calculate the mean religiosity of the whole population. We assume that when the process begins, average religiosity within each category is higher than the 414 415 midpoint, at 0.86, 0.56 and 0.22 for the religious, fuzzy, and secular groups respectively. During the following two centuries, the shift towards lower religiosity means that these values gradually 416 417 decline. The largest drop is in the fuzzy group, where average religiosity falls from 0.56 to about 0.46. Multiplying the share of each group by the average religiosity within it gives us the overall 418 mean religiosity by birth cohort (Figure 5). 419

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Fig 5 here

Fig 6 here

Additionally, we also calculated the decay of religiosity at the population level. This calculation was done in two different ways. First, using the shares and mean religiosity values of R-F-S agents, we calculated the mean religiosity of each cohort as described above. We then calculated moving averages, where each average covers ten 5-year cohorts or 50 years of age (to include adults from age 25 to 74). Note that the initial pace of decline is lower because of the inertia from older generations (Figure 6).

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For the case that religiosity decay is linear, we used data from the 15 countries that 432 participated in all 9 waves of the European Social Survey (ESS 2018). Detail information on the 433 434 ESS can be found at https://www.europeansocialsurvey.org/). First, we calculated a continuous 435 variable called religiosity index using three questions from the ESS. These three questions were also used in the study by Voas 2009: (1) self-declared religiosity (SDR), "Regardless of whether 436 you belong to a particular religion, how religious would you say you are?"; (2) Attendance, 437 438 "Apart from special occasions such as weddings and funerals, about how often do you attend religious services nowadays?"; and (3) Pray, "Apart from when you are at religious services, how 439 often, if at all, do you pray?". The questions had a 11-, 7- and 7-point scale, respectively; thus, we 440 transformed SDR to a 7-point scale (SDR_7 = $0.6 \times SDR_{11} + 1$). The sum of these answers 441 constituted the religiosity index, ranging from 3 (non-religious) to 21 (very religious). Next, using 442 443 this religiosity index, we calculated the average religiosity of the population per country and 444 wave, and the average religiosity of the fifteen countries per wave (Table S1 in supplementary 445 information). These calculations show that the average religiosity of the population is decreasing 446 in all countries (Fig 7a). Then, using this data, we performed a linear regression, and found that 447 among these European countries the average religiosity of the population decreases linearly by 0.103 every two years (ESSs were done every two years). Finally, we transformed the religiosity 448 449 index [3,21] to the religiosity scale used in the model [0,1], and using the initial average religiosity 450 of the population in the model (0.81) as the intercept and the slope from the linear regression, 451 adjusted to the [0,1] scale, we extrapolated the religiosity decay for a period of 250 years. The resulting religiosity decay is shown in Figure 7b. Note that the period covered by the nine ESS 452 453 waves is only a small portion of the whole range, so the ESS data are consistent with both the logistic-decay and linear-decay hypotheses. Our purpose here is not to evaluate the ESS data but 454 455 to employ it to generate a credible version of the linear-decay hypothesis that we can use to evaluate the microsimulation alternatives. 456

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Fig 7 here

459 **Optimization of microsimulation parameters**

460 The main goal of the microsimulation is to find, for each combination of APC processes in Table 1, the right parameter values (listed in Table 1) leading to output that mimics the religious 461 decline observed across cohorts or at the population level (Figures 5-7). To do so, we used the 462 optimization engine of AnyLogic v 8.5.2. The optimization engine allows the user to explore 463 many combinations of parameter values with the goal of identifying values that produce the best 464 465 result, as defined by a particular function. In our case, we try to minimize the residual sum of 466 squares (RSS) between the values obtained from the model and the target religiosity decay curve 467 at: (a) the cohort level, logistic decay with S-shaped curve (Figure 5); (b) the population level,

logistic decay with S-shaped curve (Figure 6); and (c) the population level, linear decay (Figure 469 7b).

To calculate the RSS, we collected the average religiosity (at the cohort or population level as
appropriate) from each optimization experiment and compared these values to the
corresponding target. For each APC process (Table 1) and target curve, we ran five optimization
experiments. We then took the combination of parameter values that produced the lowest RSS

474 and reran the model 100 times, overlaying the target curve with the output of these 100 runs. We

- 475 thereby established the degree of success with which each APC process could reproduce the
- 476 target curves for the decline in average religiosity. Similarly, we compared the output of each
 477 APC process with the expected changes in R-F-S proportions (Figure 4). Note that the
- 478 parameters were optimized to produce the best fit with average aggregate religiosity, so the
- 479 degree to which each proposed solution reproduced the changing breakdown of religious, fuzzy,
- 480 and secular serves as a form of validation.

481 Results

482 *Targeting logistic decay of religiosity at the cohort level*

483 The best fit was produced by the cohort effect taking account of social environment (H-L in Table 2). These processes generated RSS values below 0.052, except when the social 484 environment was represented by the proportion of religious population (I in Table 2). Among 485 486 the different social environments, the best fits were produced when the social environment was represented by the proportion of non-religious (i.e., secular plus fuzzy) or fuzzy agents (H and J 487 488 in Table 2). Of the other APC processes, the best fits were produced by a static period with U-489 shaped age effect and a cohort with age effect (C and G respectively in Table 2), but they were 490 not as good as the cohort and social environment effects. All other APC processes produced a 491 much worse fit.

- 492
- 493 494

Table 2 here

Figure 8 shows the overlay between the cohort target curve and the trajectories of 100 model runs using the combination of parameter values producing the best fit for each of the APC processes. The trajectories in Figure 8 corroborate the results in Table 2: the best fits are produced by the cohort (social environment) effects, particularly when the social environment is represented by the proportion of non-religious or fuzzy agents.

500 Figure 9 compares the output of these 100 models runs with the dynamics of the R-F-S shares derived from Voas (2009). Here as well, the best fit is produced by the cohort effect when 501 the social environment is represented either by the proportion of fuzzies or non-religious agents. 502 The overlap is not perfect; when using the non-religious proportion as social environment, the 503 504 fit for the religious category is very good, but less so for fuzzies and seculars. There is a slightly higher proportion of fuzzies around 150 years and a slightly lower proportion of seculars during 505 506 the first 100 years of the run. In the case of the cohort effect with the fuzzy proportion defining the social environment, the proportion of religious individuals appears lower and that of fuzzies 507 508 higher during the first 100 years of the run. Overall, however, both processes reproduce the R-F-509 S dynamics well, especially considering that the parameter values of these processes were not 510 optimized to fit these dynamics. Regarding all other APC processes, none of them performs as 511 well as the two just described.

- 512
- 513Fig 8 here514Fig 9 here

- 515 The values of the parameters producing the best fit for each of the APC processes are shown in
- Table S2 (Supplementary Information). The *C* and *SD* values for the cohort process with social
- 517 environment represented by the proportion of non-religious agents are 0.172 and 0.058. Hence,
- 518 when this process is activated, the maximum decrease in religiosity from parent to offspring is a
- 519 bit higher than 0.172 (depending on the value of *noise*, eq. 3), but only when all agents are
- 520 categorized as secular or fuzzy. In other words, such a decrease will only happen when nearly the
- 521 whole population has become non-religious, which takes 200 years. On the other hand, in the 522 cohort process with the social environment represented by the proportion of fuzzies, the values
- 523 of *C* and *SD* are 0.187 and 0.115 respectively. In contrast to the previous case, the value of *C* and
- thus the maximum decrease in religiosity from parent to offspring (eq. 3) will never be reached
- 525 because the proportion of fuzzies is always well short of 1. Here the maximum decay in
- religiosity is reached after around 150 years, when the proportion of fuzzies is at its peak (Figure
- 527 9). Thereafter, the decrease in religiosity from parent to offspring lessens with time.

528 *Targeting logistic decay of religiosity at the population level*

When targeting the S-shaped decay in religiosity at the population (rather than cohort) level, the best fit was again produced by the cohort and social environment effect (H-L in table 3), particularly when using the proportion of fuzzies or non-religious individuals to characterize the social environments (H and J in Table 3). These processes generated RSS values below 0.052 and as low as 0.012. None of the other APC processes generated a good fit, and in fact all the RSS values were above 0.131 (Table 3). Comparing the 100 model runs with the target curve confirmed the results (Figure S2 in Supplemental Information).

536 Figure S3 (Supplemental Information) shows the overlap between the trajectories of 100 537 model runs for the R-F-S shares and the projections from Voas (2009). In contrast to the 538 previous results, none of the APC processes produces a good fit (though the same cohort with 539 environment effect solutions are the least unsatisfactory).

540 *Targeting linear decay of religiosity at the population level*

541 When targeting linear decay in religiosity at the population level, the best fit was produced by a 542 static period effect (*a* in Table 3). This process generated RSS values as low as 0.005. All other 543 processes performed much worse (Table 3). The results are best illustrated in the overlap 544 between the 100 model trajectories and the linear decay curve (Figure S4 in Supplemental 545 Information). Turning to the dynamics of the R-F-S shares, however, none of the APC processes 546 generated a good fit. All show a large disparity between the model results and the projections by 547 Voas (2009) (Figure S5 in SI).

- 548
- 549

Table 3 here

550 Discussion

551 This paper presents a computational model as a proof of concept that microsimulations can be

552 used effectively to investigate complex demographic processes such as secularization.

- 553 Microsimulations can easily express alternative theories of demographic change and enable
- scholars to evaluate those alternatives against data when available. Microsimulations even offer
- by permitting non-linear interactions among age,
- 556 period, and cohort effects, after which procedures of the kind demonstrated here allow us to
- 557 identify the best explanations for a demographic process.

558 It is important to note that the decline of religiosity in the microsimulation is generated by a

- simple rule: children receive their religiosity from parents and the transmission of parents'
- religiosity is moderated by the social environment. This reflects a macro-micro feedback loop, micro in the sense that religiosity is transmitted at the individual level from parents to children

561 micro in the sense that religiosity is transmitted at the individual level from parents to childre 562 and macro because the social environment influences the way both parents and children

563 maintain and pass on their religiosity. Under these conditions, the environment appears to have a

564 homogenous effect in the whole population, i.e., the effect of the environment is the same for all

565 individuals. Interestingly, this process would produce differences between societies if they

experience different environmental effects, but would not produce differences within the society,
i.e., at the individual level. This is what it is usually found in studies supporting existential
security theory, where differences in religiosity are apparent across societies with different GDP,
but much less so across individuals of the same society with different socio-economic status
(Norris and Inglehart 2011; Stolz 2020).

571 It is also important to note that the microsimulation is not capable of identifying the triggers 572 of secularization, nor can secularization be stopped in these models. Hence, something else may 573 be needed if we want to explore what may hinder societies from secularizing. However, this issue 574 is out of the scope of our current study; but see (Wildman et al. 2020), where it is considered in a 575 simulation).

576 Though framed primarily as a proof-of-concept exercise to demonstrate the value of microsimulations in demography of religion and non-religion, the model we have presented is 577 578 robust enough to make a substantive contribution to the understanding of secularization. When we entertained the hypothesis of linear decay in religiosity, the microsimulation identified a static 579 period effect as the best explanation of the data model, which makes good sense and helps to 580 validate the microsimulation. But a static period effect – and indeed, any of the putative 581 582 candidates for explaining linear decay of religiosity – could not produce anything close to the 583 correct proportions of religious, fuzzy, and secular people over time observed in the data. This 584 suggests that linear decay is a poor hypothesis and that we are better off with the logistic-decay 585 hypothesis. In light of this, our findings show substantively that Voas' interpretation of cohort replacement, based on weakened transmission of religiosity as a function of the social 586 587 environment, appears to be an excellent explanation, both for the population as a whole and for 588 the proportions of religious, fuzzy, and secular people.

At the very least, our findings are persuasive support for the claim that secularization is primarily a cohort process. Further exploration of the rich space of model variants possible within this microsimulation could no doubt fine-tune the fit even further and demonstrate how period and age effects play supplementary roles to the dominant cohort effect. That task is for future work.

594 Acknowledgments

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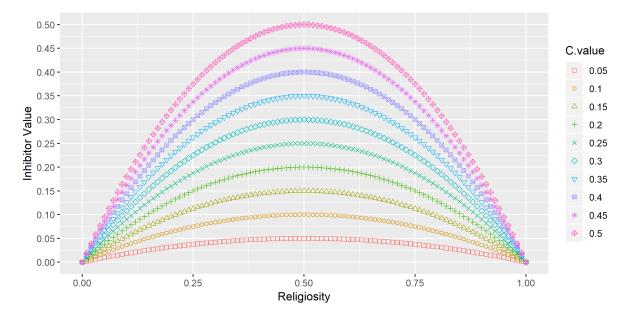
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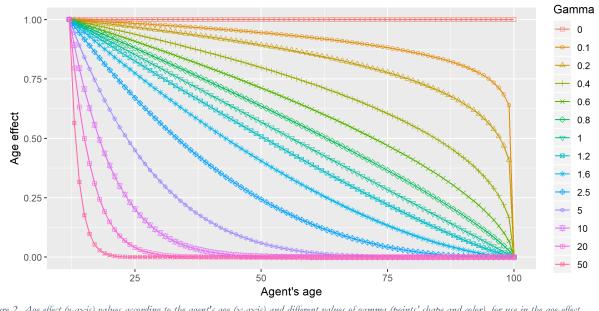
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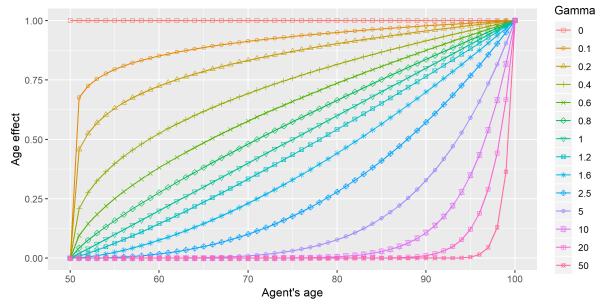
688 Tables and Figures



690 Figure 1. Values taken by the inhibitor (y-axis) according to the agent's religiosity value (x-axis) and different values of C (points' color and shape).



Agent's age693694695Figure 2. Age effect (y-axis) values according to the agent's age (x-axis) and different values of gamma (points' shape and color), for use in the age-effect
process where religiosity decreases with age.



697
698
699Age effect (y-axis) values according to the agent's age (x-axis) and different values of gamma (points' shape and color), for use in the age-effect
process where religiosity increases with age. In this example fifty years old is the minimum age at which religiosity starts to increase.

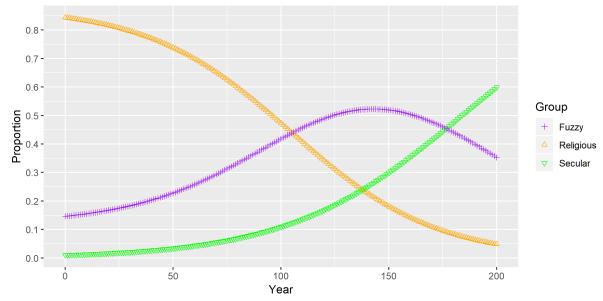
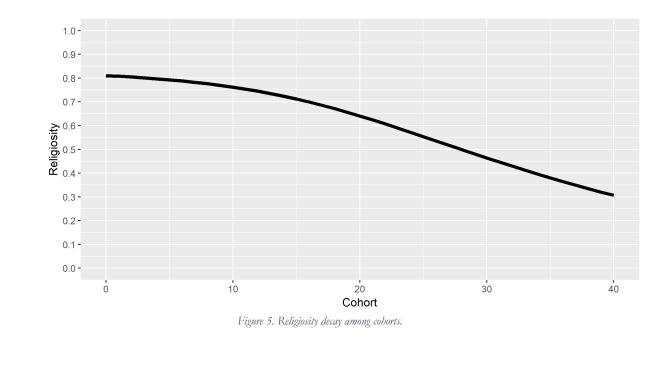
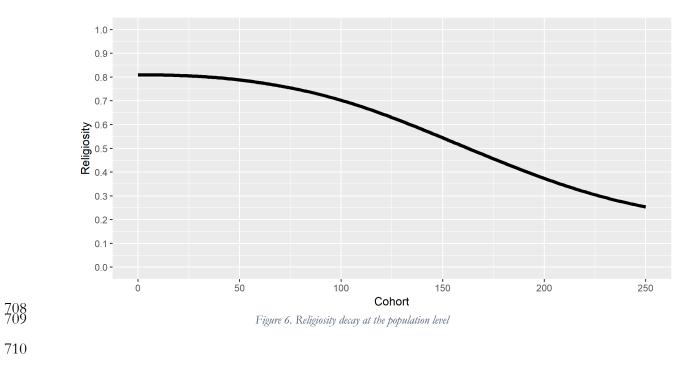
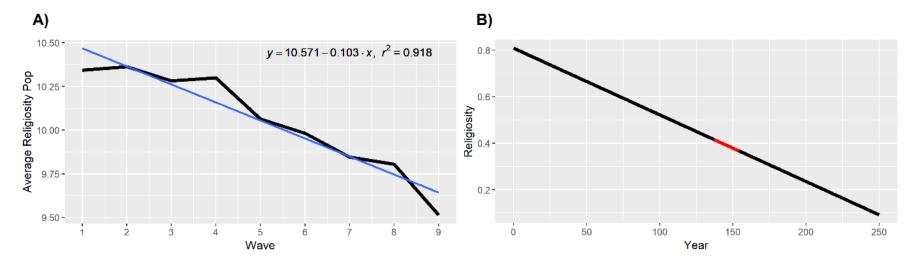


Figure 4. Dynamics of the proportions of religious, secular, and fuzzy people at the cohort level. Y-axis represents proportions and x-axis represents time in years.







712 Figure 7 A) Religiosity decay at the population level from the 15 countries in the 9 waves of the ESS; B) Religiosity decay at the population level extrapolated from the linear regression in (A) for a period of 250 years; in red, the stretch of religiosity decay calculated from the ESS data in (A).

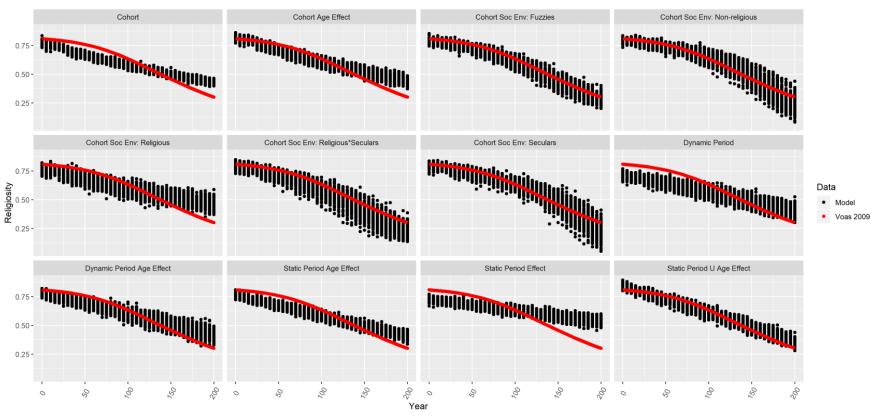


Figure 8. Trajectories of 100 model runs for each APC process (black) and the religiosity decay at the cohort level as target curve (red). See text for details

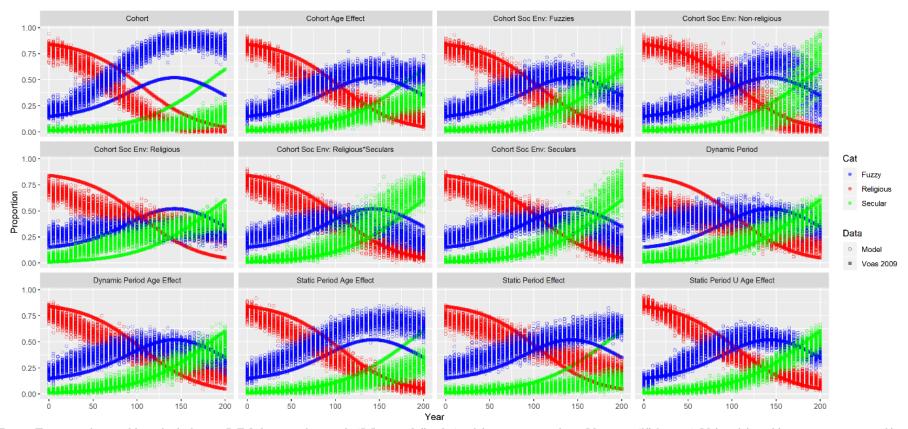


Figure 9 Trajectories of 100 model runs for the dynamics R-F-S shares according to each APC process (hollow dots) and the projections according to Voas 2009 (filled squares). Values of the model parameters were optimized by targeting the religious decay at the cohort level. Cat = category.

721		
	Code	A

Code	APC process	Equation type and figures	Parameters optimized
А	Static period effect: religiosity decay is constant every year	Equation 4: inhibitor is a constant	1. Inhibitor value
В	Static period effect with age effect (decreasing): Religiosity decay depends on inhibitor and decreases with age	Equation 4, 6 and 7; fig 2: Inhibitor is a constant modulated by agent's age	 Inhibitor value Gamma value (age effect)
С	Static period effect with U-shape age effect (decreasing): Religiosity decreases up to a certain age and then increases – U age effect	Equation 4, 6 and 7; fig 2: Inhibitor is a constant modulated by agent's age. Equation 8 and 9; fig 3: Enhancer is a constant modulated by agent's age.	 Inhibitor value Gamma value (first age effect) Inflection age, religiosity stops decreasing and starts increasing Enhancer value Gamma value (second age effect)
D	Dynamic period effect : decay value is a quadratic function of the agents' religiosity	Equation 4 and 5: Inhibitor is dynamic	1. C value (max inhibitor value)
Е	Dynamic period effect with age effect (decreasing): decay value is a quadratic function of agents' religiosity and decreases with age	Equations 4, 5, 6 and 7; fig 2: Inhibitor is dynamic and modulated by agent's age.	 C value (max inhibitor value) Gama value (age effect)
F	Cohort effect (simple) : inheritance is biased towards lower than parental religiosity.	Equation 1: Inheritance with bias.	1. alpha (shape) and beta (scale) values of the Weibull distribution
G	Cohort effect (simple) with age effect (increasing): inheritance is biased towards lower than parents' religious values and at a certain age religiosity starts to increase	Equation 1, 2, , 8, 9; fig 3: Inheritance with bias. Enhancer is a constant modulated by agent's age.	 alpha (shape) and beta (scale) values of the Weibull distribution Age at which religiosity starts increasing Enhancer value Gamma value (age effect)
H I J K L	Cohort effect (social environment) : Religiosity inherited from parents, minus an inhibitor reflecting the religiosity of the population.	Equation 3: Inheritance with noise. Inhibitor is dynamic.	 C value (max inhibitor value whe all the agents are religious) SD, standard deviation of the normal distribution

APC processes	RSS values range
A) Static period effect	[0.280-0.298]
B) Static period effect with age effect (decreasing)	[0.133-0.158]
C) Static period effect with U-shape age effect (decreasing)	[0.040-0.133]
D) Dynamic period effect	[0.219-0.241]
E) Dynamic period effect with age effect (decreasing)	[0.082-0.131]
F) Cohort effect (simple)	[0.145-0.156]
G) Cohort effect (simple) with age effect (increasing)	[0.052-0.068]
H) Cohort effect (social environment using proportion of non-religious)	[0.021-0.031]
I) Cohort effect (social environment using proportion of religious)	[0.171-0.206]
J) Cohort effect (social environment using proportion of fuzzies)	[0.022-0.044]
K) Cohort effect (social environment using proportion of seculars)	[0.038-0.052]
L) Cohort effect (social environment using proportion of religious*seculars)	[0.033-0.037]

Table 2. Results of five optimization experiments per APC process targeting the religiosity decay curve at the cohort level.

	RSS values range	
APC processes	S-shape decay	Linear decay
A) Static period effect	[0.674-2.232]	[0.005-0.058]
B) Static period effect with age effect (decreasing)	[0.317-0.365]	[0.122-0.348]
C) Static period effect with U-shape age effect (decreasing)	[0.332-0.370]	[0.130-0.145]
D) Dynamic period effect	[0.414-0.592]	[0.071-0.090]
E) Dynamic period effect with age effect (decreasing)	[0.131-0.184]	[0.195-0.225]
F) Cohort effect (simple)	[0.419-0.505]	[0.329-0.383]
G) Cohort effect (simple) with age effect (increasing)	[0.353-0.422]	[0.345-0.361]
H) Cohort effect (social environment using proportion of non-religious)	[0.029-0.052]	[0.459-0.555]
I) Cohort effect (social environment using proportion of religious)	[0.387-0.716]	[0.530-0.668]
J) Cohort effect (social environment using proportion of fuzzies)	[0.013-0.031]	[0.458-0.552]
K) Cohort effect (social environment using proportion of seculars)	[0.053-0.090]	[0.490-0.613]
L) Cohort effect (social environment using proportion of religious*seculars)	[0.026-0.059]	[0.495-0.583]
	1 1 1 1	1 1 11

726 Table 3. Results of five optimization experiments per APC process targeting the two religiosity decays at the population level: s-shape and linear decay.