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Decentralised output tracking of interconnected systems with unknown interconnections using sliding mode control*

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ABSTRACT

In this paper, a class of nonlinear interconnected systems with matched and unmatched uncertainties is considered. The isolated subsystem dynamics are described by linear systems with nonlinear components. The matched uncertainties and unmatched unknown interconnection terms are assumed to be bounded by known nonlinear functions. Based on sliding mode techniques, a state feedback decentralised control scheme is proposed such that the outputs of the controlled interconnected system track given desired signals uniformly ultimately. The desired reference signals are allowed to be time-varying. Using appropriate transformations, the considered system is transformed into a new interconnected system with an appropriate structure to facilitate the sliding surface design and the decentralised control design. A set of conditions is proposed to guarantee that the designed controller drives the tracking errors onto the sliding surface. The sliding motion exhibited by the error dynamics is uniformly ultimately bounded. The developed results are applied to a river quality control problem. Simulation results show that the proposed decentralised control strategy is effective and feasible.

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Decentralised control; large-scale system; sliding mode control; tracking control

1. Introduction

With the development of modern society, the need to control complicated systems is greatly increasing. This has motivated more researchers to focus on advanced control technology in order to deal with complex systems. Large-scale interconnected systems with non-linearities and uncertainties are typically complex systems. Such a class of systems widely exists in our real life, for example, a coupled inverted pendulum, river quality control, high-speed transportation and flight control (see, e.g. Lunze, 2020; Wu et al., 1998; Yan et al., 2017). Thus, these systems have received great attention and many results have been obtained (see, e.g. Onyeka et al., 2020; Su et al., 2018).

Large-scale systems are often mathematically modelled by interconnections of a set of lower-dimensional subsystems. One of the characteristics of such systems is that the dynamic of each subsystem is usually affected by the others due to the presence of the interconnections (Yan et al., 2017). It should be

noted that large-scale systems are usually distributed in space widely. Thus the designed systems should have a high tolerance of data loss during data transfer due to possible broken/unknown interconnections as well as poor communications to guarantee that the controlled large-scale systems exhibit the required degree of robustness. The control problem for large-scale interconnected systems is challenging. Compared with the centralised control and distributed control, decentralised control needs local information only, and thus information or data transfer between subsystems is not required. Specifically, when the network linking different subsystems is broken, or the data transfer between subsystems is poor or unstable, a centralised control or distributed control scheme cannot be implemented because both centralised control and distributed control need the other subsystems' information. In such cases, decentralised control provides advantages over centralised control and is a popular choice in the control of large-scale interconnected systems (Yan et al., 2017).

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Recently, the study of large-scale systems with interconnected terms has made great progress, and many interesting results have been obtained. In Kim et al. (2017), a large-scale fuzzy system with unknown interconnections is considered where matched uncertainties or disturbances are not included. There are also some results for interconnected systems (see, e.g. Huerta et al., 2019; Liu et al., 2019; Rinaldi et al., 2019; Song et al., 2020; Zhao et al., 2017), which require that interconnections are matched while unmatched interconnections and/or uncertainties are not involved. Moreover, some large-scale systems are considered to a simple or ideal dynamic model (see e.g. Han & Yan, 2020; Tan, 2020; Wan & Yin, 2020; Wu et al., 2018). These works just focus on a kind of special system structure that lacks generality. Decentralised sliding mode control has been developed in Yan et al. (2004) where the considered system is fully nonlinear with a more general structure, but only a stabilisation problem is considered where tracking control is not addressed.

Trajectory tracking and output tracking are important topics in both control theory and control engineering. Some tracking control results have been obtained by Cai and Hu (2017), Liu et al. (2019), and Zhao et al. (2017). However, most considered systems have special structures (see Han & Yan, 2020; Li & Liu, 2018; Tan, 2020; Wu et al., 2018). Decentralised tracking control for large-scale systems is considered in Pagilla et al. (2007), where model reference control is investigated. Tracking control for interconnected systems is considered based on adaptive fuzzy techniques in Ren et al. (2020). It should be noted that in both (Pagilla et al., 2007; Ren et al., 2020), it is required that the isolated subsystems are linear.

Sliding mode control is very popular in dealing with complex systems with uncertainties due to its unique characteristics (Song et al., 2022; Yan et al., 2014, 2020; Yao et al., 2020). On the one hand, the sliding mode dynamics are often composed of a reduced-order system when compared with the original system (Edwards & Spurgeon, 1998; Yan et al., 2017), which may simplify the corresponding system analysis and design. On the other hand, sliding mode control is totally robust to matched uncertainty and disturbances. This has resulted in the sliding mode control method being widely applied to deal with tracking problems, and many results have been achieved.

Trajectory tracking control schemes based on sliding mode techniques are proposed for specific vehicles in Wei et al. (2020) and Zhao et al. (2021). An output tracking sliding mode control is designed in Ruiz-Duarte and Loukianov (2020), where the considered system is linear. Although tracking control for nonlinear systems with uncertainties is considered in Farzad and Mohammad Hossein (2018), where event-triggered tracking is considered, only matched disturbances are considered. In Zhu et al. (2020), a tracking problem for a class of large-scale systems with interconnections is considered using sliding mode control. However, it is required that the reference signals are constant. It should be emphasised that the results concerning output tracking for large-scale nonlinear interconnected systems with unknown interconnections are very few, specifically when the ideal reference signals are time-varying.

In this paper, a class of nonlinear interconnected systems is considered where both unknown matched uncertainty and unmatched nonlinear interconnections are considered. Suitable coordinate transformations are introduced to transform the nominal subsystems of the interconnected system to systems with special structure. This separates each subsystem of the transformed system into two parts to facilitate the system analysis and control design for output tracking. Then the tracking error dynamic systems are developed, and the sliding surface based on the tracking error system is designed. A set of conditions is proposed to guarantee the uniform ultimate boundedness of the corresponding sliding motion. A decentralised sliding mode control scheme is proposed to drive the nonlinear interconnected systems to the designed sliding surface. The main contributions of this paper can be summarised as follows

- The proposed control scheme is decentralised.
- The nominal subsystem of the interconnected systems is nonlinear, and the interconnections are unknown and unmatched.
- The developed results can guarantee that the system states are uniformly ultimately bounded while all the uncertainties and interconnections are bounded.
- The developed results have high robustness against uncertainties and unknown interconnections. Both the bounds on uncertainties and the unknown

interconnections have more general nonlinear forms.

Finally, the obtained results are applied to a river quality control problem to show the practicability and feasibility of the proposed approach.

2. Preliminaries

In this paper, for a square matrix A , $\lambda_{\min}(A)$ denotes the minimum eigenvalue of matrix A . The expression $A > 0$ means that A is symmetric positive definite, and I_n denotes the unit matrix with dimension of n . The set of $n \times m$ matrices with elements defined in R will be denoted by $R^{n \times m}$ and $\text{diag}\{A_1, A_2, \dots, A_N\}$ represents a block-diagonal matrix with diagonal elements A_1, A_2, \dots, A_N . $\text{col}(\cdot)$ is a column matrix. Finally, $\|\cdot\|$ denotes the Euclidean norm or its induced norm.

Consider initially a linear system

$$\begin{aligned} \dot{x} &= Ax + Bu \\ y &= Cx \end{aligned} \quad (1)$$

where $x \in R^n$, $u \in R^m$ and $y \in R^p$ are the states, inputs and outputs, respectively. The triple (A, B, C) are constant matrices of appropriate dimensions with B being of full column rank and C being of full row rank.

Consider system (1) in the case of $m = p$, which means the system (1) is a square system. Since B has full column rank, there exists a coordinate transformation $\bar{x} = \bar{T}x$ such that in the new coordinate \bar{x} , the triple (A, B, C) can be described by

$$\bar{A} = \begin{bmatrix} A_{11} & A_{12} \\ A_{21} & A_{22} \end{bmatrix}, \quad \bar{B} = \begin{bmatrix} 0 \\ B_2 \end{bmatrix}, \quad \bar{C} = [C_1 \quad C_2] \quad (2)$$

where $A_{11} \in R^{(n-m) \times (n-m)}$, $B_2 \in R^{m \times m}$ is nonsingular. $C_1 \in R^{m \times (n-m)}$.

Assume that $\text{rank}(CB) = m$ and the invariant zeros of (A, B, C) lie in the left half plane. From Section 5.3 in Edwards and Spurgeon (1998), it follows that the matrix $C_2 \in R^{m \times m}$ in (2) is nonsingular because $m = \text{rank}(CB) = \text{rank}(\bar{C}\bar{B}) = \text{rank}(C_2B_2)$ and B_2 is nonsingular. Then, a coordinate transformation $\hat{x} = \hat{T}\bar{x}$ with \hat{T} defined by

$$\hat{T} = \begin{bmatrix} I & 0 \\ C_1 & C_2 \end{bmatrix} \quad (3)$$

is further introduced. Again from section 5.3 in Edwards and Spurgeon (1998), the triple $(\bar{A}, \bar{B}, \bar{C})$ in

the new coordinates \hat{x} has the following structure

$$\hat{A} = \begin{bmatrix} \hat{A}_{11} & \hat{A}_{12} \\ \hat{A}_{21} & \hat{A}_{22} \end{bmatrix}, \quad \hat{B} = \begin{bmatrix} 0 \\ \hat{B}_2 \end{bmatrix}, \quad \hat{C} = [0 \quad I] \quad (4)$$

where $\hat{A}_{11} \in R^{(n-m) \times (n-m)}$ is Hurwitz stable, $\hat{B}_2 = C_2B_2$ is nonsingular.

Remark 2.1: It should be pointed out that the first transformation matrix \bar{T} is used to change the original system (A, B, C) into the regular form as in (2), and the second transformation matrix \hat{T} is to make that the sub-matrix \hat{A}_{11} of the triple in (4) is Hurwitz stable and the matrix \hat{C} in (4) has the form of $[0 \quad I]$.

3. System description and basic assumptions

Consider a nonlinear large-scale system formed by N interconnected subsystems as follows

$$\begin{aligned} \dot{x}_i &= A_i x_i + f_i(x_i) + B_i(u_i + \Delta g_i(x_i)) + h_i(x) \\ y_i &= C_i x_i \quad i = 1, 2, \dots, N \end{aligned} \quad (5)$$

where $x = \text{col}(x_1, x_2, \dots, x_N)$, $x_i \in R^{n_i}$, $u_i \in R^{m_i}$ and $y_i \in R^{m_i}$ represent the states, inputs and outputs of the i th subsystem respectively and $m_i < n_i$. The triple (A_i, B_i, C_i) represents constant matrices of appropriate dimensions where B_i is full column rank and C_i is full row rank. The function $f_i(x_i)$ represents a known nonlinear term in the i th subsystem which is used to model the nonlinear part of the i th isolated subsystem, and the matched uncertainty of the i th isolated subsystem is denoted by $\Delta g_i(x_i)$ which is acting in the input channel. The term $h_i(x)$ represents the system interconnection, including all unmatched uncertainties. All the nonlinear functions in (5) are assumed to be continuous in their arguments to guarantee the existence of solutions of the controlled system (5).

The objective of this paper is, for a given desired signal $y_{id}(t)$, to design a decentralised sliding mode control such that the system output $y_i(t)$ of the controlled system (5) can track the desired signal $y_{id}(t)$, i.e. the tracking errors $y_i(t) - y_{id}(t)$ are uniformly ultimately bounded for $i = 1, 2, \dots, N$ while all the state variables of system (5) are bounded.

Remark 3.1: It should be noted that in this paper, it is required that system (5) is square for simplification of statement, that is, the dimension of each subsystem output is equal to the dimension of the corresponding

subsystem input. However, the developed results can be easily extended to the case when the dimension of subsystem output is greater than the dimension of the subsystem input by slight modification.

In order to deal with the tracking problem stated above, some assumptions are imposed on the considered interconnected system (5).

Assumption 3.1: All the invariant zeros of the triple (A_i, B_i, C_i) lie in the left half plane, and $\text{rank}(C_i B_i) = m_i$ for $i = 1, 2, \dots, N$.

It follows from the preliminaries in Section 2. Under Assumption 3.1, there exists a nonsingular coordinate transformation $z_i = T_i x_i$ such that the triple $(\hat{A}_i, \hat{B}_i, \hat{C}_i)$ with respect to the new coordinates z_i has the following structure

$$\begin{bmatrix} \hat{A}_{i11} & \hat{A}_{i12} \\ \hat{A}_{i21} & \hat{A}_{i22} \end{bmatrix}, \quad \begin{bmatrix} 0 \\ \hat{B}_{i2} \end{bmatrix}, \quad \begin{bmatrix} 0 & I_{i2} \end{bmatrix} \quad (6)$$

where $\hat{A}_{i11} \in R^{(n_i-m_i) \times (n_i-m_i)}$ is Hurwitz stable, the square matrices $\hat{B}_{i2} \in R^{m_i \times m_i}$ and $I_{i2} \in R^{m_i \times m_i}$ are nonsingular for $i = 1, 2, \dots, N$.

Assumption 3.2: Suppose that $f_i(x_i)$ has the decomposition $f_i(x_i) = \Gamma_i(x_i)x_i$, where $\Gamma_i \in R^{n_i \times n_i}$ is a continuous function matrix for $i = 1, 2, \dots, N$.

Remark 3.2: If $f_i(0) = 0$ and f_i is sufficiently smooth, then the decomposition $f_i(x_i) = \Gamma_i(x_i)x_i$ is guaranteed. Therefore, the limitation to $f_i(x_i)$ in Assumption 3.2 is not strict.

Assumption 3.3: There exist known continuous functions $\rho_i(x_i)$ and $\eta_i(x)$ with $\eta_i(0) = 0$, and $\eta_i(\cdot)$ is differentiable at the origin, such that $\|\Delta g_i(x_i)\| \leq \rho_i(x_i)$ and $\|h_i(x)\| \leq \eta_i(\|x\|)$ for $i = 1, 2, \dots, N$.

Remark 3.3: If the interconnection $h_i(x)$ in (5) satisfies the condition in Assumption 3.3, then from Yan et al. (1999) and Yan et al. (1998), it follows that there exist a continuous function $\gamma_i(\cdot)$ such that

$$\eta_i(\|x\|) = \gamma_i(\|x\|)\|x\|. \quad (7)$$

Remark 3.4: Assumption 3.3 requires that the bounds on all uncertainties in system (5) are known but they are allowed to be nonlinear. Moreover, the unknown

interconnections are allowed to have a more general nonlinear form.

Assumption 3.4: The desired output signal $y_{id}(t)$ is differentiable and satisfies

- (i) $\|y_{id}(t)\| \leq L_{i1}$;
- (ii) $\|\dot{y}_{id}(t)\| \leq L_{i2}$

for $t \in [0, \infty)$, where L_{i1} and L_{i2} are known constants for $i = 1, 2, \dots, N$.

Remark 3.5: Assumption 3.4 is a limitation on the desired output signals $y_{id}(t)$. It is required that the desired output signal $y_{id}(t)$ and its derivative $\dot{y}_{id}(t)$ are bounded. This assumption is quite standard and can be satisfied in most practical cases.

4. System structure analysis

Consider the nonlinear interconnected system in (5). Under Assumption 3.1 and from (6), there exists a nonsingular coordinate transformation $z_i = T_i x_i$ such that in the new coordinate $z = \text{col}(z_1, z_2, \dots, z_N)$, system (5) has the following form

$$\begin{aligned} \dot{z}_i &= \begin{bmatrix} \hat{A}_{i11} & \hat{A}_{i12} \\ \hat{A}_{i21} & \hat{A}_{i22} \end{bmatrix} z_i + \begin{bmatrix} F_{i1}(z_i) \\ F_{i2}(z_i) \end{bmatrix} \\ &\quad + \begin{bmatrix} 0 \\ \hat{B}_{i2} \end{bmatrix} (u_i + \Delta g_i(T_i^{-1} z_i)) + \begin{bmatrix} H_{i1}(z) \\ H_{i2}(z) \end{bmatrix} \\ y_i &= [0 \quad I_{i2}] z_i, \quad i = 1, 2, \dots, N \end{aligned} \quad (8)$$

where \hat{A}_{i11} is stable, the square sub-matrices $\hat{B}_{i2} \in R^{m_i \times m_i}$ are nonsingular. $I_{i2} \in R^{m_i \times m_i}$ is an identity matrix, $\text{col}(F_{i1}, F_{i2}) = T_i f_i(x_i)|_{x_i=T_i^{-1} z_i}$ and $F_{i1}(z_i) \in R^{n_i-m_i}$, $F_{i2}(z_i) \in R^{m_i}$. $\text{col}(H_{i1}(z), H_{i2}(z)) = T_i h_i(x)|_{x=T_i^{-1} z}$ and $H_{i1}(z) \in R^{n_i-m_i}$, $H_{i2}(z) \in R^{m_i}$. The coordinate transformation $T := \text{col}(T_1, T_2, \dots, T_N)$.

Since \hat{A}_{i11} is stable for $i = 1, 2, \dots, N$, for any $Q_i > 0$, the following Lyapunov equation has a unique solution $P_i > 0$

$$\hat{A}_{i11}^T P_i + P_i \hat{A}_{i11} = -Q_i, \quad i = 1, 2, \dots, N. \quad (9)$$

Now, in order to fully exploit the structural characteristics, partition $z_i = \text{col}(z_{i1}, z_{i2})$ with $z_{i1} \in R^{n_i-m_i}$ and $z_{i2} \in R^{m_i}$. It follows that (8) can be described by

$$\dot{z}_{i1} = \hat{A}_{i11} z_{i1} + \hat{A}_{i12} y_i + F_{i1}(z_{i1}, y_i)$$

$$\begin{aligned}
& + H_{i1}(z_{11}, y_1, \dots, z_{N1}, y_N) \quad (10) \\
\dot{y}_i = & \hat{A}_{i21}z_{i1} + \hat{A}_{i22}y_i + F_{i2}(z_{i1}, y_i) \\
& + \hat{B}_{i2}(u_i + \Delta g_i(T_i^{-1}z_i)) \\
& + H_{i2}(z_{11}, y_1, \dots, z_{N1}, y_N). \quad (11)
\end{aligned}$$

From system (8) and Assumption 3.2,

$$\text{col}(F_{i1}, F_{i2}) = T_i \Gamma_i(x_i)|_{x_i=T_i^{-1}z_i} T_i^{-1} \text{col}(z_{i1}, y_i). \quad (12)$$

In order to reduce conservatism in the later analysis, the functions $F_{i1}(z_{i1}, y_i)$ in system (10) are described by

$$F_{i1}(z_{i1}, y_i) = \Gamma_{i11}(z_{i1}, y_i)z_{i1} + \Gamma_{i12}(z_{i1}, y_i)y_i \quad (13)$$

where $\Gamma_{i11}(\cdot)$ and $\Gamma_{i12}(\cdot)$ are defined by

$$\begin{bmatrix} \Gamma_{i11}(\cdot) & \Gamma_{i12}(\cdot) \\ \star & \star \end{bmatrix} = T_i \Gamma_i(x_i)|_{x_i=T_i^{-1}z_i} T_i^{-1}$$

and the \star s are function matrices that are not necessary to specify. Therefore, (10) can be described by

$$\begin{aligned}
\dot{z}_{i1} = & \hat{A}_{i11}z_{i1} + \hat{A}_{i12}y_i + \Gamma_{i11}(z_{i1}, y_i)z_{i1} \\
& + \Gamma_{i12}(z_{i1}, y_i)y_i + H_{i1}(z_{11}, y_1, \dots, z_{N1}, y_N) \quad (14)
\end{aligned}$$

where $\Gamma_{i11}(\cdot)$ and $\Gamma_{i12}(\cdot)$ satisfy (13).

5. Sliding mode tracking control design

The main results are to be presented in this section. Firstly, a sliding surface in terms of output tracking errors will be designed based on the system structure analysis in the previous section. Then sliding mode controllers will be designed to implement the output tracking.

5.1. Sliding mode dynamics analysis

Consider the situation when the desired output signal $y_{id}(t)$ satisfies Assumption 3.4. For system (5), the output tracking errors e_i are defined by

$$e_i(t) = y_i(t) - y_{id}(t), \quad i = 1, 2, \dots, N. \quad (15)$$

Then, it follows that

$$\dot{e}_i(t) = \dot{y}_i(t) - \dot{y}_{id}(t), \quad i = 1, 2, \dots, N. \quad (16)$$

Combining with (11), (14), and (16), a new system comprising z_{i1} and e_i can be developed by

$$\dot{z}_{i1} = \hat{A}_{i11}z_{i1} + \hat{A}_{i12}y_i + \Gamma_{i11}(z_{i1}, y_i)z_{i1}$$

$$+ \Gamma_{i12}(z_{i1}, y_i)y_i + H_{i1}(z_{11}, y_1, \dots, z_{N1}, y_N) \quad (17)$$

$$\begin{aligned}
\dot{e}_i = & \hat{A}_{i21}z_{i1} + \hat{A}_{i22}(e_i + y_{id}) + F_{i2}(z_{i1}, y_i) \\
& + \hat{B}_{i2}(u_i + \Delta g_i(T_i^{-1} \text{col}(z_{i1}, y_i))) \\
& + H_{i2}(z_{11}, y_1, \dots, z_{N1}, y_N) - \dot{y}_{id}(t) \quad (18)
\end{aligned}$$

for $i = 1, 2, \dots, N$.

From Assumption 3.3 and (7), it is easy to find functions $\gamma_{i1}(\cdot)$ and $\gamma_{i2}(\cdot)$ depending on $\eta_i(\cdot)$ and T such that the following inequalities

$$\begin{aligned}
& \| H_{i1}(z_{11}, y_1, \dots, z_{N1}, y_N) \| \\
& \leq \gamma_{i1}(\|T^{-1} \text{col}(z_{11}, y_1, \dots, z_{N1}, y_N)\|) \\
& \times \left(\sum_{j=1}^N \|z_{j1}\| + \sum_{j=1}^N \|y_j\| \right) \quad (19)
\end{aligned}$$

$$\begin{aligned}
& \| H_{i2}(z_{11}, y_1, \dots, z_{N1}, y_N) \| \\
& \leq \gamma_{i2}(\|T^{-1} \text{col}(z_{11}, y_1, \dots, z_{N1}, y_N)\|) \\
& \times \left(\sum_{j=1}^N \|z_{j1}\| + \sum_{j=1}^N \|y_j\| \right) \quad (20)
\end{aligned}$$

hold for $i = 1, 2, \dots, N$. For the system (17)–(18), the following sliding surface can be defined as

$$\begin{bmatrix} e_1 \\ e_2 \\ \vdots \\ e_N \end{bmatrix} = 0. \quad (21)$$

Then, the sliding mode dynamics have the following form according to the structure of (17)–(18)

$$\begin{aligned}
\dot{z}_{i1} = & \hat{A}_{i11}z_{i1} + \hat{A}_{i12}y_{id} + \Gamma_{i11}(z_{i1}, y_{id})z_{i1} \\
& + \Gamma_{i12}(z_{i1}, y_{id})y_{id} + H_{i1}(z_{11}, y_{1d}, \dots, z_{N1}, y_{Nd}) \quad (22)
\end{aligned}$$

for $i = 1, 2, \dots, N$.

Remark 5.1: When the sliding motion occurs, the Equation (21) holds. From (15) and (19), it follows that on the sliding surface (21),

$$\begin{aligned}
& \| H_{i1}(z_{11}, y_{1d}, \dots, z_{N1}, y_{Nd}) \| \\
& \leq \gamma_{i1}(\|T^{-1} \text{col}(z_{11}, y_{1d}, \dots, z_{N1}, y_{Nd})\|)
\end{aligned}$$

$$\times \left(\sum_{j=1}^N \|z_{j1}\| + \sum_{j=1}^N \|y_{jd}\| \right) \quad (23)$$

hold for $i = 1, 2, \dots, N$.

Obviously, the sliding mode dynamic (22) is a reduced-order interconnected system composed of N subsystems whose dimension is $n_i - m_i$.

Next, a stability result will be presented for the interconnected system (22).

Theorem 5.1: Consider the sliding mode dynamic given in (22) and under Assumptions 3.1–3.4, the sliding mode is uniformly ultimately bounded if there exists a domain Ω of the origin such that $M^T + M > 0$ in $\Omega \setminus \{0\}$ where $M := (m_{ij})_{N \times N}$ and for $i, j = 1, 2, \dots, N$.

$$m_{ij} = \begin{cases} \lambda_{\min}(Q_i) - \|R_i(\cdot)\| - 2\|P_i\|\gamma_{i1}(\cdot), & i = j \\ -2\|P_i\|\gamma_{i1}(\cdot), & i \neq j \end{cases} \quad (24)$$

with P_i and Q_i satisfying (9), and

$$R_i(\cdot) := \Gamma_{i11}(z_{i1}, y_{id})^T P_i + P_i \Gamma_{i11}(z_{i1}, y_{id})$$

where $\Gamma_{i11}(z_{i1}, y_{id})$ is given by (8) and $\gamma_{i1}(\cdot)$ is determined by (23).

Proof: From the analysis above, it only needs to prove that system (22) is uniformly ultimately bounded. For system (22), consider the following *Lyapunov* function candidate

$$V(z_{11}, z_{21}, \dots, z_{N1}) = \sum_{i=1}^N (z_{i1})^T P_i z_{i1} \quad (25)$$

where P_i satisfies (9).

Then, the time derivative of $V(z_{11}, z_{21}, \dots, z_{N1})$ along the trajectories of system (22) is given by

$$\begin{aligned} \dot{V}(z_{11}, z_{21}, \dots, z_{N1}) &= \sum_{i=1}^N [(\dot{z}_{i1})^T P_i z_{i1} + z_{i1}^T P_i \dot{z}_{i1}] \\ &= \sum_{i=1}^N [(\hat{A}_{i11} z_{i1} + \hat{A}_{i12} y_{id} \\ &\quad + \Gamma_{i11}(z_{i1}, y_{id}) z_{i1} + \Gamma_{i12}(z_{i1}, y_{id}) y_{id} \\ &\quad + H_{i1}(z_{11}, y_{1d}, \dots, z_{N1}, y_{Nd})]^T P_i z_{i1} \end{aligned}$$

$$\begin{aligned} &+ z_{i1}^T P_i (\hat{A}_{i11} z_{i1} + \hat{A}_{i12} y_{id} + \Gamma_{i11}(z_{i1}, y_{id}) z_{i1} \\ &\quad + \Gamma_{i12}(z_{i1}, y_{id}) y_{id} + H_{i1}(z_{11}, y_{1d}, \dots, z_{N1}, y_{Nd})) \\ &= \sum_{i=1}^N [z_{i1}^T \hat{A}_{i11}^T P_i z_{i1} + y_{id}^T \hat{A}_{i12}^T P_i z_{i1} \\ &\quad + z_{i1}^T \Gamma_{i11}^T(z_{i1}, y_{id}) P_i z_{i1} + y_{id}^T \Gamma_{i12}^T(z_{i1}, y_{id}) P_i z_{i1} \\ &\quad + H_{i1}^T(z_{11}, y_{1d}, \dots, z_{N1}, y_{Nd}) P_i z_{i1} \\ &\quad + z_{i1}^T P_i \hat{A}_{i11} z_{i1} + z_{i1}^T P_i \hat{A}_{i12} y_{id} \\ &\quad + z_{i1}^T P_i \Gamma_{i11}(z_{i1}, y_{id}) z_{i1} + z_{i1}^T P_i \Gamma_{i12}(z_{i1}, y_{id}) y_{id} \\ &\quad + z_{i1}^T P_i H_{i1}(z_{11}, y_{1d}, \dots, z_{N1}, y_{Nd})] \\ &= \sum_{i=1}^N \{-z_{i1}^T Q_i z_{i1} + z_{i1}^T [\Gamma_{i11}(z_{i1}, y_{id})^T P_i \\ &\quad + P_i \Gamma_{i11}(z_{i1}, y_{id})] z_{i1} + 2z_{i1}^T P_i \hat{A}_{i12} y_{id} \\ &\quad + 2z_{i1}^T P_i \Gamma_{i12}(z_{i1}, y_{id}) y_{id} \\ &\quad + 2z_{i1}^T P_i H_{i1}(z_{11}, y_{1d}, \dots, z_{N1}, y_{Nd})\} \quad (26) \end{aligned}$$

where (9) is used to establish the above. By (23) and (i) in Assumption 3.4, it follows that

$$\begin{aligned} \dot{V}(z_{11}, z_{21}, \dots, z_{N1}) &\leq \sum_{i=1}^N \{-\lambda_{\min}(Q_i) \|z_{i1}\|^2 + \|\Gamma_{i11}(z_{i1}, y_{id})^T P_i \\ &\quad + P_i \Gamma_{i11}(z_{i1}, y_{id})\| \|z_{i1}\|^2 \\ &\quad + 2\|z_{i1}\| \|P_i\| \|\hat{A}_{i12} y_{id}\| \\ &\quad + 2\|z_{i1}\| \|P_i\| \|\Gamma_{i12}(z_{i1}, y_{id}) y_{id}\| \\ &\quad + 2\|z_{i1}\| \|P_i\| \|H_{i1}(z_{11}, y_{1d}, \dots, z_{N1}, y_{Nd})\| \} \\ &= -\sum_{i=1}^N \{\lambda_{\min}(Q_i) - \|R_i(\cdot)\| \\ &\quad - 2\|P_i\|\gamma_{i1}(\cdot)\} \|z_{i1}\|^2 \\ &\quad + 2 \sum_{i=1}^N \sum_{\substack{j=1 \\ j \neq i}}^N \|P_i\| \|z_{i1}\| \gamma_{i1}(\cdot) (\|z_{j1}\| + L_{i1}) \\ &\quad + 2 \sum_{i=1}^N (\|\hat{A}_{i12} y_{id}\| + \|\Gamma_{i12}(z_{i1}, y_{id}) y_{id}\|) \\ &\quad \cdot \|P_i\| \|z_{i1}\| \\ &\leq -\frac{1}{2} \lambda_{\min}(M^T + M) \sum_{i=1}^N \|z_{i1}\|^2 \end{aligned}$$

$$\begin{aligned}
& + 2 \sum_{i=1}^N (\| \hat{A}_{i12} y_{id} \| + \| \Gamma_{i12}(z_{i1}, y_{id}) y_{id} \| \\
& + \gamma_{i1}(\cdot) L_{i1}) \cdot \| P_i \| \| z_{i1} \| \\
= & -\frac{1}{2} \sum_{i=1}^N \{ \lambda_{\min}(M^T + M) \| z_{i1} \| \\
& - 4(\| \hat{A}_{i12} y_{id} \| + \| \Gamma_{i12}(z_{i1}, y_{id}) y_{id} \| \\
& + \gamma_{i1}(\cdot) L_{i1}) \| P_i \| \} \| z_{i1} \| \quad (27)
\end{aligned}$$

where the matrix M is defined in (24). Under Assumption 3.4, $\| y_{id}(t) \| \leq L_{i1}$. It is clear to check $\dot{V} \leq 0$, if

$$\| z_{i1} \| \geq \frac{4(\| \hat{A}_{i12} L_{i1} \| + \| \Gamma_{i12}(z_{i1}, y_{id}) L_{i1} \| + \gamma_{i1}(\cdot) L_{i1}) \| P_i \|}{\lambda_{\min}(M^T + M)} \quad (28)$$

for $i = 1, 2, \dots, N$. Hence, the conclusion follows. ■

Remark 5.2: From (28), it is clear to see that the final bound of the sliding mode dynamics is affected by the upper bound of the desired output signal $y_{id}(t)$, the system sub-matrix \hat{A}_{i12} , the nonlinearity of the system Γ_{i12} and the bound of the interconnections γ_{i1} .

5.2. Decentralised sliding mode control design

The objective is now to design a feedback sliding mode control such that the system state is driven to the sliding surface.

For the interconnected system (17)–(18), the reachability condition (Yan et al., 2004, 2017) is described by

$$\sum_{i=1}^N \frac{e_i^T \dot{e}_i(t)}{\| e_i(t) \|} < 0. \quad (29)$$

Then, the following control law is proposed

$$\begin{aligned}
u_i = & -B_{i2}^{-1} \text{sgn}(e_i) \{ \| \hat{A}_{i21} z_{i1} \| + \| \hat{A}_{i22} y_i \| \\
& + \| F_{i2}(z_{i1}, y_i) \| \\
& + \| \hat{B}_{i2} \| \rho_i(z_{i1}, y_i) + k_i(z_{i1}, y_i) + L_{i2} \} \quad (30)
\end{aligned}$$

for $i = 1, 2, \dots, N$, where e_i and L_{i2} are defined by (15) and Assumption 3.4, respectively. $k_i(z_{i1}, y_i)$ is the control gain to be designed later.

Theorem 5.2: Consider the nonlinear interconnected system (17)–(18) and Assumptions 3.2–3.4, the controller (30) drives the system (17)–(18) to the composite

sliding surface (21) and maintains a sliding motion on it if the controller gains $k_i(z_{i1}, y_i)$ satisfy

$$\sum_{i=1}^N k_i(z_{i1}, y_i) > \sum_{i=1}^N \gamma_{i2}(\cdot) \sum_{j=1}^N (\| z_{j1} \| + \| y_j \|) \quad (31)$$

where γ_{i2} are defined in (20).

Proof: It is necessary to prove that the reachability condition (29) is satisfied. From (18) and Assumption 3.2,

$$\begin{aligned}
\dot{e}_i = & \hat{A}_{i21} z_{i1} + \hat{A}_{i22} y_i + F_{i2}(z_{i1}, y_i) \\
& + \hat{B}_{i2}(u_i + \Delta g_i(T_i^{-1} \text{col}(z_{i1}, y_i))) \\
& + H_{i2}(z_{11}, y_1, \dots, z_{N1}, y_N) - \dot{y}_{id} \quad (32)
\end{aligned}$$

for $i = 1, 2, \dots, N$. Substituting (30) into (32), it follows

$$\begin{aligned}
\frac{e_i^T \dot{e}_i}{\| e_i \|} = & \frac{e_i^T}{\| e_i \|} [\hat{A}_{i21} z_{i1} + \hat{A}_{i22} y_i + F_{i2}(z_{i1}, y_i) \\
& + \hat{B}_{i2} \Delta g_i(T_i^{-1} \text{col}(z_{i1}, y_i)) + H_{i2}(\cdot) \\
& - \dot{y}_{id}] - \| \hat{A}_{i21} z_{i1} \| - \| \hat{A}_{i22} y_i \| \\
& - \| F_{i2}(z_{i1}, y_i) \| - \| \hat{B}_{i2} \| \rho_i(z_{i1}, y_i) \\
& - k_i(z_{i1}, y_i) - L_{i2}. \quad (33)
\end{aligned}$$

It is clear to see

$$\begin{aligned}
& \| \hat{A}_{i21} z_{i1} + \hat{A}_{i22} y_i + F_{i2}(z_{i1}, y_i) \| \\
& \leq \| \hat{A}_{i21} z_{i1} \| + \| \hat{A}_{i22} y_i \| + \| F_{i2}(z_{i1}, y_i) \| . \quad (34)
\end{aligned}$$

From Assumptions 3.3 to 3.4,

$$\| \hat{B}_{i2} \Delta g_i(T_i^{-1} \text{col}(z_{i1}, y_i)) \| \leq \| \hat{B}_{i2} \| \rho_i(z_{i1}, y_i) \quad (35)$$

$$\begin{aligned}
& \| H_{i2}(z_{11}, y_1, \dots, z_{N1}, y_N) \| \\
& \leq \gamma_{i2}(\cdot) \sum_{j=1}^N (\| z_{j1} \| + \| y_j \|) \quad (36)
\end{aligned}$$

$$\| \dot{y}_{id} \| \leq L_{i2}. \quad (37)$$

Substituting the above four inequalities (34)–(37) into (33), it follows

$$\sum_{i=1}^N \frac{e_i^T \dot{e}_i(t)}{\| e_i(t) \|} < - \sum_{i=1}^N k_i(z_{i1}, y_i) + \sum_{i=1}^N \gamma_{i2}(\cdot)$$

$$\times \sum_{j=1}^N (\|z_{j1}\| + \|y_j\|).$$

If $k_i(z_{i1}, y_i)$ is chosen to satisfy (31), the reachability condition (29) will be satisfied.

Hence, the result follows. \blacksquare

Remark 5.3: Theorem 5.1 shows that the sliding mode dynamic (22), which is an interconnected system, is uniformly ultimately bounded. Theorem 5.2 shows that the reachability condition is satisfied. According to the sliding mode theory, Theorems 5.1 and 5.2 show that the closed-loop system is uniformly ultimately bounded.

Remark 5.3 shows that the closed-loop systems formed by applying the control (30) to the systems (17)–(18) are uniformly ultimately bounded, which implies that the variables $\|z_{i1}(t)\|$ and $\|e_i(t)\|$ are bounded for $i = 1, 2, \dots, N$. Further, from $e_i(t) = y_i(t) - y_{id}(t)$ and Assumption 3.4, which guarantees that $y_{id}(t)$ is bounded, it is straightforward to see that $y_i(t)$ are bounded due to

$$y_i(t) = e_i(t) + y_{id}(t)$$

for $i = 1, 2, \dots, N$. Therefore, all the state variables of the system (10)–(11) are bounded. Further, from $x_i = T_i^{-1}z_i$, the state variables x_i of system (5) are bounded. This shows that the designed decentralised control (30) can not only makes the system outputs to track the desired reference signals but also keep all the system state variables bounded.

6. Application to river quality control

In this section, the decentralised control scheme developed in this paper will be applied to a river pollution problem (Lunze, 2020) as shown in Figure 1. The water quality of a river is mainly dependent upon the concentrations of oxygen and pollutants. In a simplified manner, this problem can be stated as the task of controlling the pollutants discharged at different places along the river in such a way that the river pollution remains within a given tolerance.

Assume that the river has two regions and each region has a sewage station. Then, the river pollution system can be described by a nonlinear interconnected systems as follows (see Yan et al., 2017 for no delay

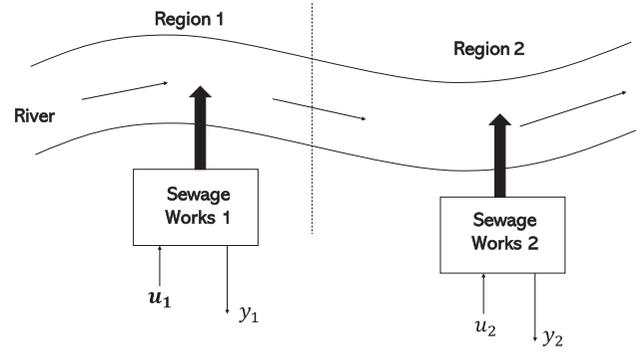


Figure 1. River with sewage.

case)

$$\dot{x}_1 = \underbrace{\begin{bmatrix} -1.32 & 0 \\ -0.32 & -1.2 \end{bmatrix}}_{A_1} x_1 + \underbrace{\begin{bmatrix} 1 \\ 0 \end{bmatrix}}_{B_1} (u_1 + \Delta g_1(\cdot)) + h_1(x) \quad (38)$$

$$y_1 = \underbrace{\begin{bmatrix} 1 & 0 \end{bmatrix}}_{C_1} x_1 \quad (39)$$

$$\dot{x}_2 = \underbrace{\begin{bmatrix} -1.32 & 0 \\ -0.32 & -1.2 \end{bmatrix}}_{A_2} x_2 + \underbrace{\begin{bmatrix} 1 \\ 0 \end{bmatrix}}_{B_2} (u_2 + \Delta g_2(\cdot)) + h_2(x) \quad (40)$$

$$y_2 = \underbrace{\begin{bmatrix} 1 & 0 \end{bmatrix}}_{C_2} x_2 \quad (41)$$

where $x_1 = \text{col}(x_{11}, x_{12})$, $x_2 = \text{col}(x_{21}, x_{22})$ and $x = \text{col}(x_1, x_2)$. The variables x_{i1} and x_{i2} for $i = 1, 2$ represent the concentration of biochemical oxygen demand (BOD) and the concentration of dissolved oxygen, respectively, the controllers u_i are the BOD of the effluent discharge into the river, Δg_i represent any matched uncertainties and h_i represent interconnections respectively for $i = 1, 2$. It is assumed that the concentrations of BOD for the two regions are measurable.

In this example, according to (5), the nonlinear term $f_i(x_1) = 0$, so Assumption 3.2 is not required. Moreover, it can be verified that $\text{rank}(C_i B_i) = 1 = m_i$ for $i = 1, 2$. So the Assumption 1 is satisfied. Some suitable coordinate transformation matrices T_i are introduced

as below ($z_i = T_i x_i$)

$$T_1 = T_2 = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}.$$

Then, the system (38)–(41) in z coordinates can be given by

$$\dot{z}_1 = \underbrace{\begin{bmatrix} -1.2 & -0.32 \\ 0 & -1.32 \end{bmatrix}}_{\hat{A}_1} z_1 + \underbrace{\begin{bmatrix} 0 \\ 1 \end{bmatrix}}_{\hat{B}_1} (u_1 + \Delta G_1(z_1)) + H_1(z) \quad (42)$$

$$y_1 = \underbrace{\begin{bmatrix} 0 & 1 \end{bmatrix}}_{\hat{C}_1} z_1 \quad (43)$$

$$\dot{z}_2 = \underbrace{\begin{bmatrix} -1.2 & -0.32 \\ 0 & -1.32 \end{bmatrix}}_{\hat{A}_2} z_2 + \underbrace{\begin{bmatrix} 0 \\ 1 \end{bmatrix}}_{\hat{B}_2} (u_2 + \Delta G_2(z_2)) + H_2(z) \quad (44)$$

$$y_2 = \underbrace{\begin{bmatrix} 0 & 1 \end{bmatrix}}_{\hat{C}_2} z_2 \quad (45)$$

For simulation purpose, the matched uncertainties $\Delta G_1(\cdot)$ and $\Delta G_2(\cdot)$ are chosen to satisfy

$$|\Delta G_1(\cdot)| \leq |-13.2z_{12}|, \quad |\Delta G_2(\cdot)| \leq |\cos^2(z_{22})| \quad (46)$$

and the interconnected terms are set as

$$\|H_1\| \leq |z_{22}|, \quad \|H_2\| \leq |0.9z_{12}|. \quad (47)$$

Combining (46)–(47), it is clear that Assumption 3.3 is satisfied. And the sliding surfaces S_i are

$$\dot{z}_{i1} = -1.2z_{i1} - 0.32z_{i2}, \quad i = 1, 2$$

The initial states are chosen as $z_1(0) = \text{col}(0, 1)$ and $z_2(0) = \text{col}(0, 0)$, and the desired output signals y_{id} are set as

$$y_{1d} = 2e^{-t}, \quad y_{2d} = \sin(0.5t) + 1.$$

It is clear that Assumption 3.4 is satisfied. Let

$$L_{12} = 2, \quad L_{22} = 0.5.$$

From (30), the proposed sliding mode controllers are as follows

$$u_1 = -\text{sgn}(y_1 - y_{1d})(|1.32z_{12}| + |13.2z_{12}| + 3) \quad (48)$$

$$u_2 = -\text{sgn}(y_2 - y_{2d})(|1.32z_{22}| + |\cos^2(z_{22})| + 2.3). \quad (49)$$

According to (9), choose $Q_1 = Q_2 = 1$. Combining (38)–(40), $A_{i11} = -1.2$ for $i = 1, 2$. Then

$$P_1 = P_2 = 0.416.$$

By direct calculation, it follows from (24) that

$$\begin{aligned} M^T + M &= \begin{bmatrix} -1.664\gamma_{11} + 2 & -0.832(\gamma_{11} + \gamma_{21}) \\ -0.832(\gamma_{11} + \gamma_{21}) & -1.664\gamma_{21} + 2 \end{bmatrix}. \end{aligned}$$

According to (23), (42) and (44),

$$\gamma_{11} = 6 \cdot \sin^2(z_{11}), \quad \gamma_{21} = 2 \cdot \cos(z_{21}) + 3.$$

By direct verification, it is straightforward to check that $M^T + M > 0$ in the domain Ω of the origin satisfying $\Omega = \{(z_{11}, z_{21}, \dots, z_{N1}) \mid |z_{11}| \leq 5.2 \ \& \ |z_{21}| \leq 3.9\}$.

According to (27) for this example

$$\dot{V}(z_{11}, z_{21}) \leq 0 \quad (50)$$

if $|z_{11}| \geq 0.3$ and $|z_{21}| \geq 0.25$. Therefore, system (38)–(41) is uniformly ultimately bounded.

The tracking results are shown in Figure 2, which offers a high tracking performance. The concentration of biochemical oxygen demand (BOD) of each

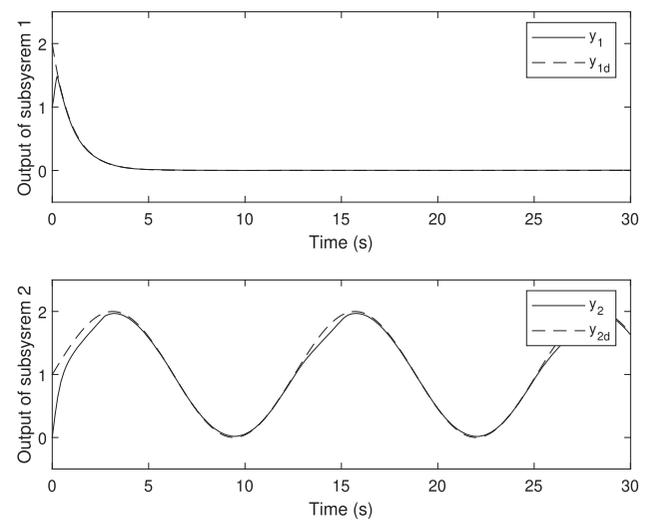


Figure 2. Time responses of system outputs and desired outputs.

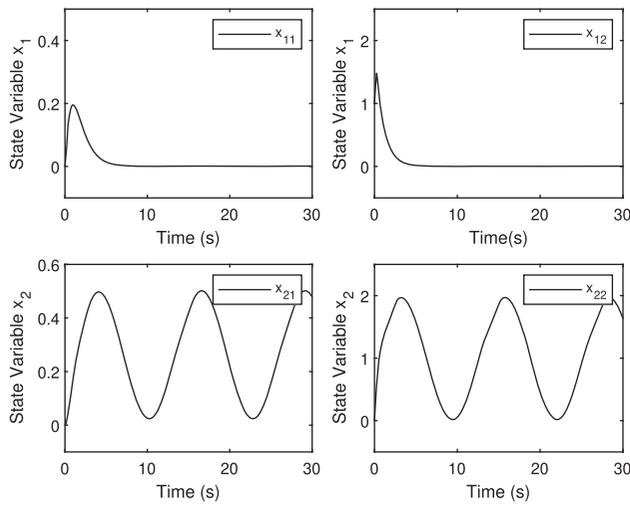


Figure 3. Time responses of system state variables.

subsystem y_i can track the ideal reference y_{id} using the controller from (48)–(49), even in the presence of uncertainties. The time responses of the states of the system (38)–(41) are shown in Figure 3, which indicates that the system states are bounded. Simulation results demonstrate that the method developed in this paper is effective.

7. Conclusions

This paper has presented a sliding mode control strategy to deal with the output tracking problem of a class of large-scale systems with unmatched unknown nonlinear interconnections. The desired reference signals are allowed to be time-varying. A decentralised sliding mode control scheme has been proposed to satisfy the reachability condition. This drives the interconnected system onto the pre-designed sliding surface. A set of conditions is developed to guarantee that the output tracking errors are uniformly ultimately bounded while all the state variables of the interconnected system are bounded. The application of the developed results to a river pollution control system has demonstrated that the proposed approach is effective and practicable.

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Data availability statement

The authors confirm that the data supporting the findings of this study are available within the article.

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