New tools to generate realistic ice floe fields for computational models

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Global warming has extensively transformed Arctic sea ice from continuous level ice coverage to unconsolidated ice floe fields. Whilst the ice floes have a mixture of different sizes and their locations are randomly distributed, contemporary computational models lack effective methods to generate floe fields with such a natural pattern. This work introduces two original tools that can generate realistic ice floe fields for computational models. They are a sequential generator that sequentially handles ice floes one by one, and a genetic generator based upon a genetic algorithm. Demonstration of the tools is given, presenting samples of generating various shapes of floes and arbitrary mixtures of different shapes. Furthermore, an example is provided that combines the generated floe field with computational work modelling a ship transiting in ice floes. In addition, the source code of the tools is sharable with the public.

1 INTRODUCTION

Since the late 1970s when satellite observations began, the Arctic ice extent has decreased rapidly due to the effect of global warming [1]. The melting process has caused a widespread transformation of ice conditions in the Arctic, in particular, extensive unconsolidated ice floe fields have been replacing level-ice coverages, as shown in Fig. 1. With the transformation being ongoing, the ice floe environment has been reported to be a principal feature of the Arctic [2]. Also, the ice floe condition is dominant in the Antarctic [3, 4, 5].

The increasing ice floe fields play a significant role in both environmental and engineering areas. For example, it allows ocean surface waves to propagate through [6], which in turn dictates the ice extent, size and distribution. Contemporary climate models still cannot provide fully accurate prediction for Arctic ice evolution and global temperature change [7]. To improve this, a research gap is to appropriately integrate small-scale wave-ice interactions and floe-size distributions within large-scale climate models [8].

On the other hand, the ice floe environment is navigable for commercial ships without icebreaking capabilities, which led to the opening of numerous new shipping routes via the Arctic [9]. The new Arctic sea routes offer shorter voyage distances compared to their traditional counterparts and provide access to rich reserves of oil, gas, mines and fishing grounds. Yet, the ice floes that appear in the Arctic sea routes bring uncertainties to shipping operators, designers and builders, as there is the need to ascertain the additional resistance and structural loads from the floes on ships.

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Fig. 1: Ice floe fields emerging with climate change [4]

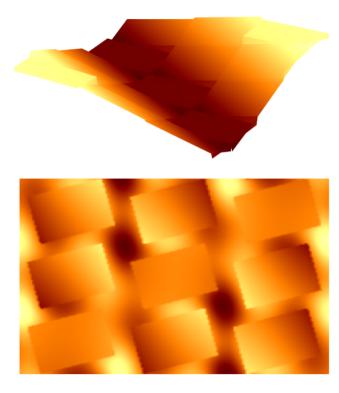


Fig. 2: The model of Porter [10] for simulating ocean waves propagating through an ice floe field, with regular floe size and distribution

2 PROBLEM DEFINITION

With the ongoing climate change, it is essential to build computational models for the environmental and engineering problems associated with the ice floe fields. However, there remain challenges to model ice-floe problems with high fidelity. For example, in computational models containing ice floe fields, the initial size and location of each floe need to be given, which is defined by the user based on assumptions. As a consequence, the modelled ice floe fields are usually imposed with subjective regularities. This may be seen in the model of Porter [10] studying the propagation of ocean waves through separated ice floes, the floes were set to be of uniform size and the distance between all the floes is initialised to be the same. It may be observed in Fig. 2 that the wave crests/troughs amongst the floes occur in regular locations, which is undesired due to its considerable affection on the propagation of wave energy. Thus, the model's prediction is dictated by the initial array that is subjectively defined.

The same issue can be seen in the model of Huang et al. [11] simulating a ship operating in ice floes, presented in Fig. 3. The ice loads on the ship are also dictated by the initial floe distribution, as the ship-ice contact points and angles are prescribed and a small change in the array can alter the ice impact. This kind of regular layout might provide acceptable accuracy for predicting average ice loads on structures, but would fail in predicting extreme loads or the distribution of loads on a hull.

This deficiency also appears in various existing models [12, 13, 14, 15, 16]. Moreover, multiple scholars have compared wave-ice and structure-ice interactions using different prescribed arrays of ice floes; they changed the row alignment and spacing, and proved that the influence of these subjectively-defined parameters on the prediction is essential [17, 18, 19, 20, 21]. These pieces of evidence indicate the need for methods that can replace the hypothetic regular floe fields with more natural floe fields, thus achieving high-fidelity reproduction of the reality.

Previous work on generating realistic ice floe fields for computational models have been given by [6, 22, 23, 24, 25, 26]. The work of Hopkins et al. [22] applied the approach of Voronoi tessellation and Delaunay triangulation, which was a theoretical approximation that did not match actual field measurements. The simulations of van den Berg et al. [23] and Yang et al. [24] used field and experimental images to reproduce the ice floes, but the image approach limits the size of the computational domain as well as the extension of the simulation for more scenarios. The methods of Montiel et al. [6], Metrikin [25] and Yulmetov et al. [26] have used field-measurement data of ice distribution law as input, while the floe shapes were limited to circular in [6] or random polygonal shapes in [25, 26].

To provide a more comprehensive approach for modelling ice floes, the present work introduces two different algorithms that can generate floe fields of any measured ice distribution law, and provide options to choose spe-

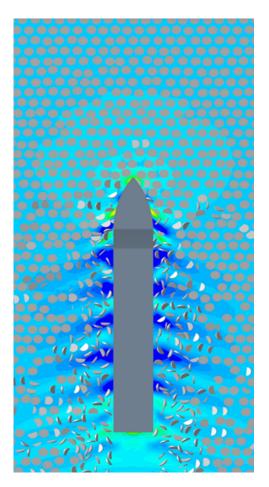


Fig. 3: The model of Huang et al. [11] for simulating a ship advancing in an ice floe field, with regular floe size and distribution

cific floe shapes (e.g. circular, triangular, square, rectangular and pentagonal) as well as arbitrary mixtures of different shapes in one domain.

Generating ice floe fields of arbitrary user-defined shapes can be beneficial for studying the underlying mechanism in different ice conditions, and for investigating the floe shape effect by comparing simulations of different shapes, as suggested by van den Berg et al. [23]. Also, the generated computational floe fields can match experiments that manufacture ice floes of designated shapes (usually use synthetic materials) [24]. In this way, the present work is expected to facilitate the development and validation of computational approaches for icefloe problems. More importantly, the developed source code is intended to be shared with other researchers, which is the first open-source work providing such tools.

3 SOLUTION

In a natural ice floe field, the floes are of different sizes and their locations are randomly distributed. There are many types of sea ice floe varying in shapes and sizes, two primary types are pancake ice and pack ice. In a sufficiently large region, the floe sizes of pancake and pack ice have been observed to distribute following a log-normal function [3, 27]; as shown in Fig. 4a, the majority of floes tend to have a size close to a medium value; the proportion for larger floes decreases with increased size, and the proportion for smaller floes decreases with decreased size. Such a curve is referred to as the curve of Floe-Size-Distribution (FSD). The FSD curve can have regional and seasonal variations, which can be obtained from field and aerial measurements [3, 28].

For both the generators in this work, an FSD curve is required as the governing input. Based on the FSD curve the total ice floes are divided into a certain number of groups, by different floe sizes; for each group, the floe size and the corresponding probability are extracted from the FSD curve, as shown in Fig. 4b. Fewer groups can be applied as long as the influence is negligible. For the size of a domain used to study an environmental or engineering problem in ice floe fields, the ice thickness of all floes usually do not have a notable variation [29], so the thickness of all floes in one computational domain is assumed to be constant; even so, the ice thickness can also be set to be varying if required. Other inputs include domain length and width of the specific computational model, the shape of the floes, and ice concentration (C, defined as the ice-covered area divided by the total sea-surface area, i.e. area of the domain). The complete condition of generating an ice floe field is that no overlapping occurs between any floes. Upon completion, the output is a matrix listing the x - y coordinates of every ice floe and the corresponding floe size, while z coordinates are aligned to the buoyancy-gravity equilibration of each floe.

The first generator is a heuristic named Sequential Generator (SG), because it handles the floes one by one until all floes fulfil the complete condition. Based on the inputs, it first calculates the total number of ice floes (n_p) , after which all floes are sorted by their decreasing sizes. Then, SG randomly positions ice floes into the computational domain, one by one, starting from the largest floe i = 1 to the smallest floe i = n_p . If overlapping occurs when SG is trying to position a floe, that floe will be randomly repositioned until it does not overlap with any previous floes; SG runs until all floes are successfully settled. During the process, SG changes only the position of the current ice floe while leaving all previously settled ice floes fixed. This can lead to a dead end, i.e. the fixed arrangement of previous ice floes may hinder subse-

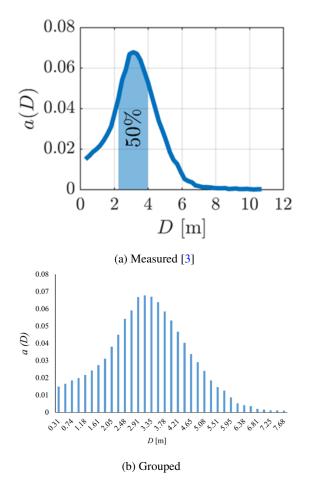


Fig. 4: An example of floe-size-distribution for pancake ice: the probability of occurrence (a) as a function of the floe diameter (D)

quent ice floes from being successfully settled. Therefore, a time-limit parameter is introduced to avoid this issue: if a solution has not been found within the time limit, the algorithm automatically restarts from the beginning. The time limit is suggested to be set at one minute for circular shape with any target C, while it may be increased for polygonal shapes with a high target C. Fig. 5 provides the flowchart of SG.

The second generator is named Genetic Generator (GG), because it is derived from the genetic algorithm based upon Darwin's principle: the survival of the fittest individuals [30]. GG defines a penalty factor to indicate the overlapping between ice floes; a higher penalty value corresponds to a higher overlapping area, i.e. an objective penalty factor of zero means no overlapping at all. GG starts by randomly producing a certain number (M_0) of initial solutions, corresponding to M_0 penalty values.

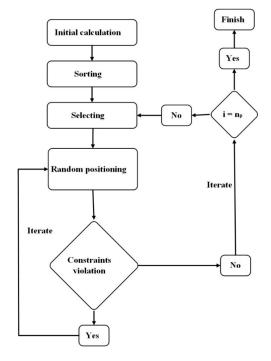


Fig. 5: Flowchart of SG

Subsequently, the algorithm selects a lower number of solutions (M_1) with averagely lower penalty values to be parents. By mixing parts of the parent solutions, M_0 child solutions are created, making up a total number of $M_0 + M_1$ solutions. Then M_0 solutions with the highest penalty values are discarded, and the total number of solutions goes back to M_0 , but a better average penalty factor has been achieved. Additionally, M_2 solutions with best penalty factors are denoted as elite individuals, and in order to diversify non-elite solutions, random changes are applied to M_3 randomly chosen individuals from the group of non-elite solutions ($M_0 - M_2$). The above process is iterated from generation to generation until a solution is found that satisfies the objective penalty factor. Fig. 6 provides the flowchart of GG.

4 DEMONSTRATION

As reported by Toyota et al. [31], the shape of ice floes can vary with the common types including circular, triangular, rectangular, pentagonal, hexagonal (and arbitrary polygonal). There can also be multiple shapes of floes co-existing in a certain region. This work provides the capability to generate floes of a user-defined shape and as a mixture of multiple shapes. Meanwhile, aspect ratio is an important parameter for ice floes. For example, pancake ice floes are closer to ellipses than circles [3],

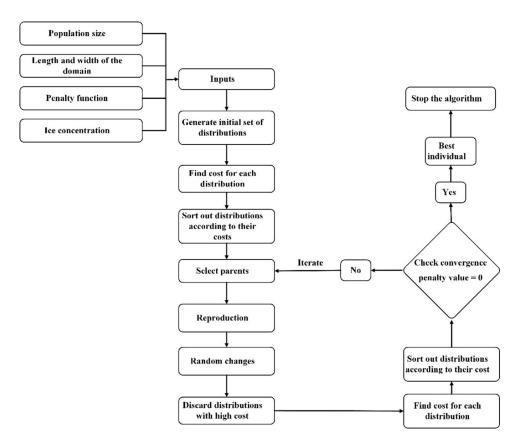


Fig. 6: Flowchart of GG

and ellipses are good approximations for wave-broken ice [32]. Hence, this work also offers the capability to define aspect ratio for floes. Examples of generated floe fields with different shapes and aspect ratios are given in Fig. 8.

Tests were run for both SG and GG for different ice concentration targets. It is seen that SG is a fast and oriented algorithm that the targeted FSD and C can be exactly achieved. The algorithm can generate an ice floe field within seconds, up to C = 70%, noting that the runtime scales with the total required computational domain (approximately linear with total floe number). However, SG gets slower for achieving C > 70%; this is because a relatively high C means there is a limited open-water area in the domain, and thus it is hard for SG to settle all floes into desirable space. Therefore, SG is not recommended to be used for generating a solution of C > 70%.

Unlike SG that considers only one solution at a time, GG handles a number of solutions simultaneously and requires multiple iterations. Thus the computational demand of GG is considerably higher than SG, where the runtime increases to an order of minutes. The intent for designing such an algorithm was to tackle very high ice concentrations for which SG would be unable to yield any solution in a reasonable time. Objective C = 75% and 80% have been attempted to be achieved using GG, as shown in Fig. 8, but a residual of 0.05-0.1% overlapping area could not be eliminated. The residual is not completely eliminable even after hours of iterating, which is reasonable as GG's algorithm is to select the optimal solutions while does not contain a step to enhance an optimal solution into a perfect solution. To further eliminate the residual, GG and partial SG may be coupled: GG could be performed to yield a solution with a minimal residual, followed by the "reposition" step of SG to find space to move the overlapping floes. This step may not be necessary in most cases, as the residual magnitude is very small. C = 80% is the highest concentration tested using GG, which is approximately the highest possible concentration of such floe fields without overlapping, e.g. Hopkins and Tuhkuri's experiments [37] show that C = 79%is the highest possible concentration, so C > 80% is out of the test scope here.

To further verify the algorithms and demonstrate the applicability, the tools have been used to generate pancake ice floe fields to replace the unrealistic floe fields shown in Fig. 3. The tools are easily compatible with the

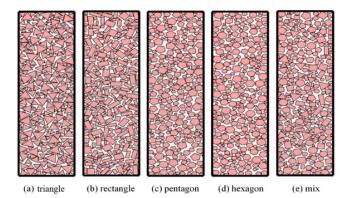


Fig. 7: Examples of generated ice floe fields with different shapes (C = 60%), in which, the rectangles' aspect ratio ranging from 1 to 3, and the mix contains six representative shapes (triangular, square, rectangular, pentagonal, hexagonal and circular)

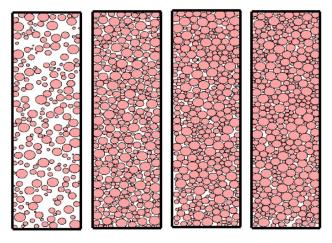
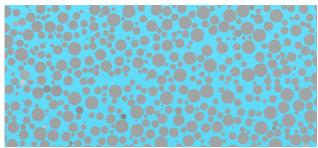


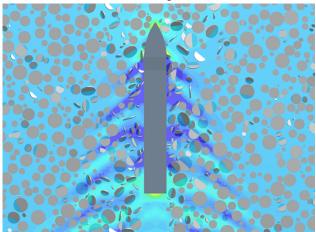
Fig. 8: Ice floe fields generated by SG, C = 40% and C = 70% (the left two); and by GG, C = 75% and C = 80% (the right two)

computational model, as the output is a list of floe dimension and location that can be directly used in the initial setups of a simulation. The updated ice floe fields are shown in Fig. 9. The updated was used to investigate the resistance of ships advancing in emerging Arctic shipping routes infested by floating ice floes. Compared with using regular floe fields, the model's accuracy of predicting ice resistance has been evidently improved by the more realistic floe fields, with deviation level against experiments reduced from < 30% to < 10% [11, 33]. The work was further validated by full-scale measurements, which proved the floe fields generated using the present tools can be used to accurately predict ship fuel consumption and

to optimise ship voyages in the Arctic [34, 35, 36].



(a) Generated floe field floating on sea surface, C = 60%.



(b) A ship advancing in the generated floe field

Fig. 9: Demonstration of a computational model combined with a floe field generated by the code developed in this work

5 CONCLUSIONS

This work has provided and demonstrated two complementary algorithms that can effectively generate realistic ice floe fields for computational models. With climate change, the code facilitates the contemporary models with fidelity to represent increasing ice-floe conditions in polar regions, which is essential for investigating relevant environmental and engineering problems. An example of application has been presented with a computational model simulating the operation of a ship in floeinfested waterways. Other applications of this work could be studying structure-ice interactions [37], the propagation of ocean waves in ice floe fields [38, 39], the collision and drift of floes [40, 41], as well as the associated thermodynamic and oceanographic modelling [7].

SOURCE CODE

The tools are written in MATLAB and instructions are given in the form of comments throughout the code. The authors intend to keep maintaining and developing the code. For requesting the latest version of the code or discussing additional functions, please email the corresponding author. The users are allowed to use/modify/develop the code for their own purposes, but the present paper should be cited where applicable.

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