

Predicting lithium iron oxysulphides for battery cathodes

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Abstract

Cathode materials that have high specific energies and low manufacturing costs are vital for the scaling up of lithium-ion batteries (LIBs) as energy storage solutions. Fe-based intercalation cathodes are highly attractive because of the low cost and the abundance of raw materials. However, existing Fe-based materials, such as LiFePO_4 , suffer from low capacity due to the large size of the polyanions. Turning to mixed anion systems can be a promising strategy to achieve higher specific capacity. Recently, anti-perovskite structured oxysulphide Li_2FeSO has been synthesised and reported to be electrochemically active. In this work, we perform an extensive computational search for iron-based oxysulphides using *ab initio* random structure searching (AIRSS). By

performing an unbiased sampling of the Li-Fe-S-O chemical space, several oxysulphide phases have been discovered which are predicted to be less than 50 meV/atom from the convex hull and potentially accessible for synthesis. Among the predicted phases, two anti-Ruddlesden-Popper structured materials $\text{Li}_2\text{Fe}_2\text{S}_2\text{O}$ and $\text{Li}_4\text{Fe}_3\text{S}_3\text{O}_2$ have been found to be attractive as they have high theoretical capacities with calculated average voltages 2.9 V and 2.5 V respectively, and their distances to hull are less than 5 meV/atom. By performing nudged-elastic band calculations, we show that the Li-ion transport in these materials takes place by hopping between the nearest neighbouring sites with low activation barriers between 0.3 eV and 0.5 eV. The richness of materials yet to be synthesised in the Li-Fe-S-O phase field illustrates the great opportunity in these mixed anion systems for energy storage applications and beyond.

Keywords

American Chemical Society, L^AT_EX

1 Introduction

The cathode is a critical component for lithium-ion batteries (LIBs) to achieve high energy density, safe operation, and economical viability. Despite many technological advances in LIBs, the cathode materials have barely evolved in the last 15 years. Those found in commercialised LIBs are still based on one of the three systems: layered LiCoO_2 ,¹ spinel LiMn_2O_4 ,² and olivine LiFePO_4 ,³ all of which were first proposed more than two decades ago. Iron-based cathode materials are very attractive as Fe is one of the most abundant transition metal in the upper crust with very low production costs. LIBs with olivine LiFePO_4 cathodes are nowadays used in applications including electric vehicles, but they suffer from relatively low specific energies.⁴ Other iron based polyanion cathodes, such as $\text{Li}_2\text{FeSiO}_4$,^{5,6} LiFeSO_4F ⁷⁻⁹ have also being proposed and shown to have comparable performance to LiFePO_4 . The use

of larger-sized polyanion groups, however, places an upper-limit on the energy density, which in turn offsets some of the benefits of the low cost. On the other hand, iron-oxide based cathodes are held back due to low voltages due to the $\text{Fe}^{2+}/\text{Fe}^{3+}$ redox,¹⁰ while attempts to utilize the $\text{Fe}^{3+}/\text{Fe}^{4+}$ redox often lead to decomposition into other phases upon charging.^{11–13}

Substituting one element with another has been a fruitful strategy for increasing the performance of cathode materials. Over the years, most of the research interests have been focusing on cationic substitution, and materials such as layered $\text{LiNi}_x\text{Mn}_y\text{Co}_z\text{O}_2$ ¹⁴ have improved reversible capacities over LiCoO_2 - only half of the Li can be extracted in the latter. In the meantime, anionic substitution, or mixed anion materials have been largely unexplored until recently.¹⁵ With different sizes, valence charge, electronegativity and polarizability of the anions, hetero-anionic materials are known to form layered structures due to preferential cation-anion bonding.^{16,17} The incorporation of fluorine into oxide has been reported to improve the performance of disordered rock salt type cathodes.¹⁸ It offers another knob for tuning the valence of the transition metal cations and being more electronegative than oxygen leads to higher voltages.^{19,20} Anions that are less electronegative can be oxidised more easily than O^{2-} , which could favour anionic redox and leads to higher capacities.²¹ For chalcogenide anions (S^{2-} and Se^{2-}), the increased polarizability also gives rise to better electronic conductivity than the oxide and polyanion based materials, which often poses limitations for fast and reversible Li cycling.

Recently, an anti-perovskite structured oxysulphide Li_2FeSO ($Pm\bar{3}m$) was synthesised and found to have reasonably good electrochemical performance with a theoretical cationic redox capacity of 223 mAh/g, and a voltage of 2.5 V against graphite electrodes.^{22,23} A subsequent computational study suggests that the anti-perovskite framework provides low lithium-diffusion barriers, and substituting Fe with other transition metal ions could lead to improved performance.²⁴ Replacing half of the Fe by Mn has been reported to enhanced the structural stability but at the cost of reducing the capacity.²⁵ Meanwhile, iron oxysulphide based cathodes have also been explored for applications in sodium-ion batteries.²⁶

These findings beg the question: are there other oxysulphides waiting to be discovered? Computational materials discovery, and in particular, high-throughput screening studies, have previously been applied to many fields including battery cathodes.^{27,28} Those studies, however, rely heavily on existing experimental data, as hypothetical materials are constructed from simple substitutions of the known materials.^{17,29,30} For lithium iron oxysulphides, which remain largely unexplored so far, the available experimental data are scarce. The other way of discovering new materials is to directly search for low energy structures using first-principles calculations, with little or no experimental inputs.³¹ Finding the lowest energy crystal structure is a challenging task, as it requires global optimisation over the high-dimensional configuration space. Many approaches have been developed to tackle the problem, including basin hopping,³² minima hopping,³³ genetic algorithms³⁴ and particle-swarm optimisation.³⁵ In this work, we explore the lithium iron oxysulphide chemical space using *ab initio* random structure searching^{36,37} (AIRSS), which is a simple, efficient and highly parallel method for searching for low energy structures. By sampling the Li-Fe-S-O space in an unbiased way, we have discovered many previously unknown phases that are both predicted to be relatively stable and have good electrochemical performances for cathode applications. Among those phases, two anti-Ruddlesden-Popper structured materials $\text{Li}_2\text{Fe}_2\text{S}_2\text{O}$ and $\text{Li}_4\text{Fe}_3\text{S}_3\text{O}_2$ are particularly attractive due to them being both nearly on the convex hull and have theoretical capacities exceeding that of the Li_2FeSO . Subsequent DFT calculations using the predicted crystal structures show that they have average voltages of 2.9 V and 2.5 V respectively, and band gaps about 2.0 eV. Using the climbing-image nudged elastic band method,^{38,39} we show that both of them contain Li-diffusion networks with low transition state barriers similar to that of Li_2FeSO .

2 Methods

Details about *ab initio* random structure searching (AIRSS) and its application to battery electrode materials can be found in the literature.^{36,37,40,41} Briefly, this method searches for low energy structures by generating random but physically sensible initial structures followed by geometry optimisation using first-principles calculations. Unlike most other structure prediction methods, there is no iterative improvement process involved, hence the search can be parallelized and distributed over the computing resources easily. The plane wave density functional theory code CASTEP⁴² is used for structure searching with a plane wave cut off energy of 340 eV and a k-point spacing of $0.072\pi\text{\AA}^{-1}$ for sampling the reciprocal space. Core-corrected on-the-fly generated ultrasoft pseudopotentials from CASTEP’s built-in QC5 library are used. Further DFT calculations are performed using the VASP^{43,44} code with a plane wave cut off energy of 520 eV and a k-point spacing of $0.042\pi\text{\AA}^{-1}$. The PBE exchange-correlation functional⁴⁵ is used with the Hubbard correction applied for the *d* states of Fe. The *U* value for Fe is set to 4.0 eV based on the fitting of oxide formation energies.⁴⁶ A force-based convergence criteria of 0.03 eV \AA^{-1} is used for all geometry optimisations, except when relaxing the input structure for phonon calculations where a tighter tolerance of $0.0001\text{ eV \AA}^{-1}$ is applied. Ferromagnetic spin states have been assumed during the initial search to avoid complicating the energy landscapes. Enumerating spin arrangements for selected low energy phases shows that imposing anti-ferromagnetic orderings typically reduces the energy by 10 to 20 meV per atom, giving minor changes to the computed thermodynamic stabilities. Hence, the FM ordering is used in all further calculations for oxysulphides. Finite-displacement phonon calculations are performed using the Phonopy package⁴⁷ with an increased cut off energy of 650 eV. Climbing-image nudged elastic band^{38,39} calculations are performed for determining the Li-diffusion barriers using the VTST code. The supercells are constructed such that periodic images of the Li-vacancy are more than 10 Å away in all directions. To avoid hole localisation upon creating a single Li vacancy, which would otherwise complicate the potential energy surface and the

minimum energy pathway, a single electron is added to the supercell with a neutralising background. This resembles the case where the polaron formed is far away from the Li-vacancy. The AiiDA framework is used to automate the DFT calculations and preserve their provenance.^{48,49} The sumo⁵⁰ python package is used for plotting electronic density of states and phonon band structures.

3 Results

New phases in the Li-Fe-O-S space

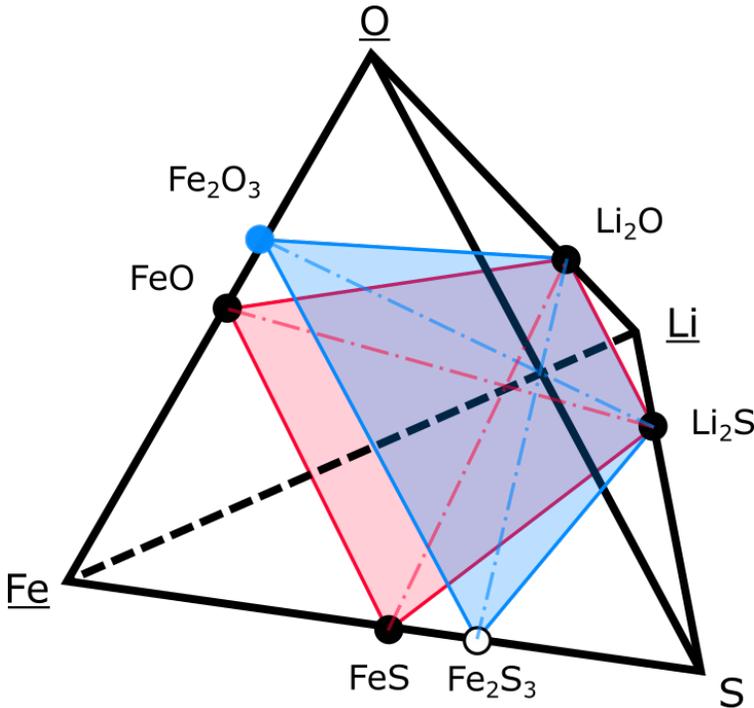


Figure 1: A tetrahedron representing the Li-Fe-S-O chemical space. charge-neutral compositions with formal valences (Fe: +2/+3, Li: +1, S: -2, O: -2) for oxysulphides are located on the two planes with Fe in +3 (red) and +2 (blue) states.

We target our search for fully lithiated phases of potential materials for Li-intercalation cathodes. The Li-Fe-O-S chemical space can be represented as a tetrahedron with vertices being the elemental species, as shown in Fig. 1. In oxysulphides, both oxygen and sulphur typically have the -2 oxidation states. For metal cations, Li is expected to be in the $+1$

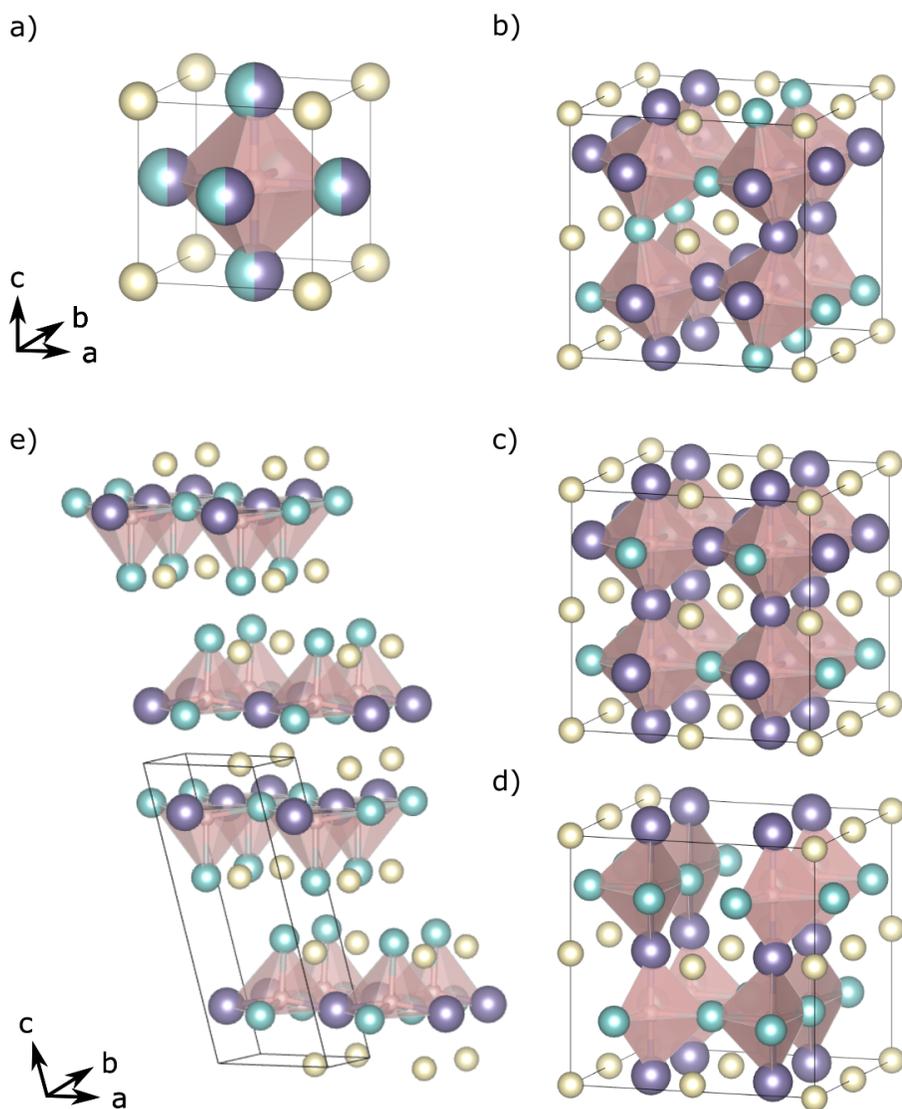


Figure 2: (a) The disordered cubic anti-perovskite unit cell of Li_2FeSO . (b) The Li_2FeSO structure found here. (c) The lowest energy Li_2FeSO reported previously.²⁴ (d) The structure of $\text{Li}_2\text{Fe}_3\text{S}_2\text{O}_2$. (e) The structure of $\text{Li}_2\text{Fe}_4\text{S}_3\text{O}_2$. Colour coding: cream-S, purple-Li, cyan-Fe, pink-O. The coordination polyhedrons drawn are centered on oxygen atoms.

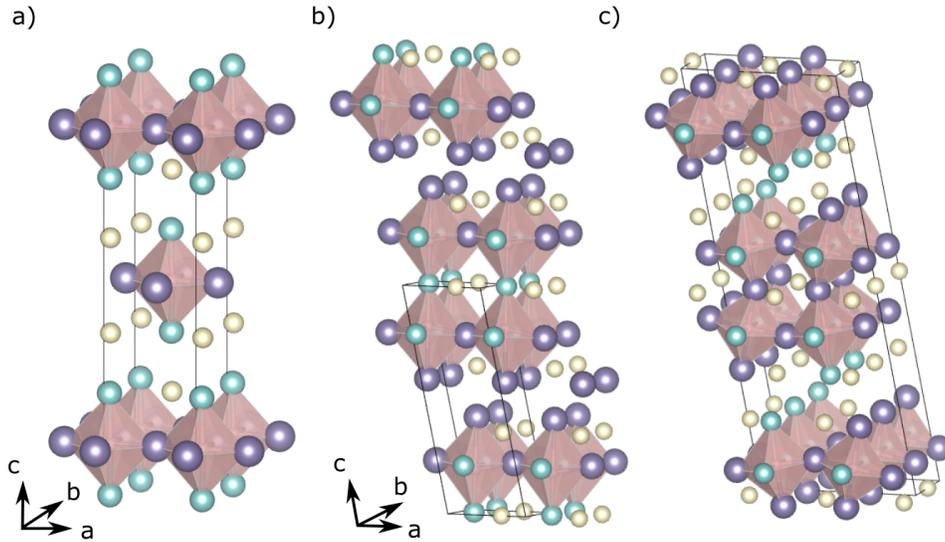


Figure 3: The two anti-Ruddlesden-Popper phases found in the search: (a) $\text{Li}_2\text{Fe}_2\text{S}_2\text{O}$; (b) $\text{Li}_4\text{Fe}_3\text{S}_3\text{O}_2$; (c) $\text{Li}_4\text{Fe}_3\text{S}_3\text{O}_2$ with lower energy obtained by enumerating the Li/Fe orderings. Colour coding: cream-S, purple-Li, cyan-Fe, pink-O. The coordination polyhedrons drawn are centered on oxygen atoms.

state and we limit Fe to be in the $+2$ and $+3$ states. To maintain charge neutrality, the sum of the oxidation states for a given composition should be zero. This means that the compositions to be searched are located on two cross-sectional planes of the full Li-Fe-S-O tetrahedron: one for those with Fe in $+3$ and the other for $+2$, as shown in Fig. 1. Plane wave density functional theory calculations are known to have cubic scaling, to keep the problem tractable, we limit the search to compositions with the number of atoms in the empirical formula ≤ 12 , and the total number of atoms in the full formula ≤ 24 . Even with these constraints applied, there are still 33 candidate compositions to be searched. As a result, we have to perform coarse samplings of the phase space initially, where about 600 random structures generated and relaxed for each composition. Afterwards, compositions that have the lowest energy structure close to the convex are selected for further searching.

The compositions of the phases that are found to be close to the convex hull within a 50 meV per atom range is shown in Table 1, where V_a is calculated average voltage, ΔV is the volume change after delithiation and E_h is the distance to the convex hull, S_c is the

Table 1: Compositions that are close to the convex hull found in the search and their computed average voltages and theoretical capacities. Symbols: V_a is calculated average voltage; ΔV is the volume change after delithiation; E_h is the distance to the convex hull; S_c is the specific capacity; S_e is the specific energy. The $\text{Li}_4\text{Fe}_3\text{S}_3\text{O}_2$ structure obtained from enumeration is marked with the asterisk.

Formula	V_a (V)	ΔV (%)	E_h (meV)	S_c (mAh/g)	S_e (Wh/kg)	Decomposition
Li_2FeSO	2.33	-4.5	0.0	227.5	532.3	N/A
$\text{Li}_2\text{Fe}_4\text{S}_3\text{O}_2$	2.72	-7.3	0.0	146.7	398.5	N/A
$\text{Li}_4\text{Fe}_3\text{S}_3\text{O}_2^*$	2.56	-5.3	3.3	248.6	637.8	$\text{Li}_2\text{FeSO} + \text{Li}_2\text{Fe}_4\text{S}_3\text{O}_2 + \text{Li}_2\text{S}$
$\text{Li}_2\text{Fe}_3\text{S}_2\text{O}_2$	2.56	-10.0	3.4	193.1	496.0	$\text{Li}_2\text{FeSO} + \text{FeO} + \text{Li}_2\text{Fe}_4\text{S}_3\text{O}_2$
$\text{Li}_2\text{Fe}_2\text{S}_2\text{O}$	2.85	-11.7	3.4	260.6	743.6	$\text{Li}_2\text{Fe}_4\text{S}_3\text{O}_2 + \text{Li}_2\text{S}$
$\text{Li}_4\text{Fe}_3\text{S}_3\text{O}_2$	2.55	-3.4	18.1	248.6	633.6	$\text{Li}_2\text{FeSO} + \text{Li}_2\text{Fe}_4\text{S}_3\text{O}_2 + \text{Li}_2\text{S}$
$\text{Li}_4\text{Fe}_3\text{S}_4\text{O}$	2.47	-3.8	30.5	236.8	585.4	$\text{Li}_2\text{Fe}_4\text{S}_3\text{O}_2 + \text{FeS} + \text{Li}_2\text{S}$
$\text{Li}_2\text{Fe}_4\text{S}_4\text{O}$	2.58	-6.9	38.6	140.5	363.4	$\text{Li}_2\text{Fe}_4\text{S}_3\text{O}_2 + \text{FeS} + \text{Li}_2\text{S}$
$\text{Li}_4\text{Fe}_2\text{S}_3\text{O}$	2.09	-5.5	45.8	213.0	445.5	$\text{Li}_2\text{Fe}_4\text{S}_3\text{O}_2 + \text{Li}_2\text{S}$
Li_6FeSO_3	1.90	-10.0	46.3	150.9	287.3	$\text{Li}_2\text{O} + \text{Li}_2\text{FeO}_2 + \text{Li}_2\text{S}$
$\text{Li}_2\text{Fe}_3\text{S}_3\text{O}$	2.44	-7.6	48.8	182.6	446.5	$\text{Li}_2\text{Fe}_4\text{S}_3\text{O}_2 + \text{FeS} + \text{Li}_2\text{S}$
$\text{Li}_6\text{FeS}_3\text{O}$	2.28	1.5	49.9	127.8	291.5	$\text{Li}_2\text{FeSO} + \text{Li}_2\text{S}$

theoretical specific capacity, and S_e is the specific energy computed from on V_a and S_c . The 50 meV distance to hull threshold is chosen because experimentally synthesisable metastable compounds are expected to fall into this range.⁵¹ Our search has also reproduced the anti-perovskite Li_2FeSO phase (Fig. 2a) that was reported previously,²² and it is predicted to be on the convex hull (e.g. thermodynamically stable) at 0 K. A previous DFT study predicts Li_2FeSO to be metastable and would decompose into Li_2FeO_2 , FeS and Li_2S ,²⁴ whereas it is found to be stable here. This difference is likely to be caused by the methodology of treating transition metals in different type of compounds. In that work, the PBE/PBE+U calculations are mixed,⁵² where the Hubbard-correction for Fe is only applied to oxide/oxysulphide phases with the energies adjusted using the correction factors from the Materials Project.²⁸ In this approach, the PBE+U correction factor is supposed to be calibrated for reproducing oxide formation energies involving metallic Fe and O_2 . Applying the same term to oxysulphides would introduce systematic errors and affection the reaction energy of forming oxysulphides from oxide and sulphides. We also find that the standard PBE calculations give

large energy differences between polymorphs of FeS and overly destabilise the troilite phase ($P\bar{6}2c$) for which the experimental thermochemical data is available. More discussion can be found in the supporting information. In this work, the Hubbard correction is applied to all Fe-containing phases including the sulphides (similar to that in the Open Quantum Material Database⁵³). In theory, the U_{eff} calibrated based on oxide formation energies differs from those for sulphides.⁵⁴ Nevertheless, as the distance to hull are computed using the same set of competing phases, phases that are predicted to be close/on the convex hull should have stabilities similar to that of the Li_2FeSO , which has been synthesised experimentally.²²

The Li_2FeSO structure found by the search here (Fig. 2b, space group Pc) contains Li and Fe atoms with substantial displacements from their sites in the cubic disordered anti-perovskite cell (Fig. 2a, space group $Pm\bar{3}m$). This result can be easily rationalised by invoking our knowledge of perovskite tilting, as the O, Li, and Fe atoms have sizes such that the OLi_4Fe_2 network contains tilted octahedra in the $a^0b^0c^+$ pattern using the Glazer’s rotation,⁵⁵ which is consistent the Goldschmidt tolerance factor of 0.85 computed from the ionic radii. This value is computed using a weighted average of Li and Fe radii and the ionic radius of S^{2-} in six-fold coordination. The latter may result in underestimation of the tolerance factor as S^{2-} is in fact under 12-fold coordination in the anti-perovskite structure. The previously reported theoretical ground state structure of Li_2FeSO , which was obtained by enumerating Li and Fe sites (shown in Fig. 2c, space group $P4_2mmc$), does not have any octahedral tilting,²⁴ and it is 6 meV higher in energy compared to our structure obtained using AIRSS. This high-symmetry structure is dynamically unstable (Fig. S4a), and following the imaginary mode at the M point results in $a^-b^-c^0$ tilted octahedra (space group $P2/c$), shown in Fig. S4b. The final energy of this distorted structure is almost identical to the one found with AIRSS. Oxysulphides containing Fe^{3+} are mostly unstable and far from the hull, and all of the phases in Table 1 contain Fe^{2+} instead. This may be attributed to Fe_2O_3 being very stable as one of the competing phases.

Several previously unknown phases have been found to be on or close to the convex

hull. The $\text{Li}_2\text{Fe}_4\text{S}_3\text{O}_2$ (space group $C2$) and $\text{Li}_2\text{Fe}_3\text{S}_2\text{O}_2$ (space group Pm) are shown in Fig. 2d&e respectively. The former is on the convex hull while the latter is only 3 meV (per atom) above it. They can be regarded as cation deficient variants of anti-Ruddlesden-Popper and anti-perovskite structures. In both cases, the oxygen atoms are under square pyramidal coordination by two Li atoms and three Fe atoms, rather than the octahedral coordination in original archetypes. The cation deficiency can be attributed to the reduced Li-to-Fe ratio. Since a Fe^{2+} cation carries more positive charges, fewer cations are needed to balance the negative charge of the anions. Unfortunately, the lower Li-to-Fe ratios result in reduced specific capacities, making them less attractive as cathode materials.

On the other hand, two anti-Ruddlesden-Popper phases, $\text{Li}_2\text{Fe}_2\text{S}_2\text{O}$ and $\text{Li}_4\text{Fe}_3\text{S}_3\text{O}_2$, have been found to be close to the convex hull and more promising for cathode applications with specific capacity higher than that of the Li_2FeSO . The former has a layered structure as shown in Fig. 3a, which resembles the Ruddlesden-Popper (RP) phases with a general formula $\text{A}_{n+1}\text{B}_n\text{X}_{3n+1}$. The RP series consist of alternating perovskite-like (ABX_3) and rock salt like (AX) environments along the z the direction. The number n indicates the number of complete ABX_3 perovskite layers between the rock salt BX layer. In contrast to normal RP phases, such as $\text{Sr}_3\text{Ru}_2\text{O}_7$, where cations take the A and B sites, here they take the anion X sites instead, and S and O occupy the A and B sites respectively. This gives the anti-Ruddlesden Popper structured oxysulphides a general formula $\text{S}_{n+1}\text{O}_n(\text{Fe/Li})_{3n+1}$. The $\text{Li}_2\text{Fe}_2\text{S}_2\text{O}$ phase (space group Pc) has $n = 1$ with one perovskite layer followed by the rock salt layer as shown in Fig. 3a, and it is only about 3 meV from the convex hull. Likewise, the $\text{Li}_4\text{Fe}_3\text{S}_3\text{O}_2$ phase (space group Cm) has two perovskite layers (e.g. $n = 2$) in the unit cell, as shown in Fig. 3b. This phase is slightly less stable with a distance to hull of 18 meV per atom. Different Li/Fe orderings in the primitive cell and supercells of both phases have been enumerated, and twenty structures with the lowest electrostatic energies are further relaxed by DFT for each case. Unlike the cubic perovskite, the base structure of the RP phase is not unique, which can affect the initial rankings based on the electrostatic energies. We used the

experimental structure of Sr_2RuO_4 , $\text{Sr}_3\text{Ru}_2\text{O}_7$ and the structures obtained from the search as the initial templates. For $\text{Li}_2\text{Fe}_2\text{S}_2\text{O}$, performing the enumeration did not generate any structure with lower energy. In fact, using the ideal Sr_2RuO_4 structure as the template would miss the lowest energy structure that is found in the search. On the other hand, repeating the same procedure for $\text{Li}_4\text{FeS}_3\text{O}_2$ has generated many structures with lower energies by up to 14.8 meV per atom (distance to hull is reduced to 3.3 meV). In this case, starting from the ideal structure appears to give better results. The lowest energy structure (space group $C2/m$) contains OLi_4Fe_2 tilted octahedra in a $a^+b^0c^0$ tilt system, as shown in Fig. 3c.

It should be noted that many of the "above-hull" structures are in fact predicted to decompose into phases that are themselves found by the search, as shown in Table 1. If only the ternary and binary compounds in the Li-Fe-S-O chemical spaces are considered, many of them would be regarded as stable. This highlights the importance of performing a sufficient and unbiased sampling of the target chemical space for reliably predicting the thermodynamic stabilities.

To check the dynamic stability of the predicted structures, finite displacement phonon calculations have been carried out. The predicted Li_2FeSO structure was found to have no imaginary frequencies across the first Brouline zone. The $\text{Li}_2\text{Fe}_2\text{S}_2\text{O}$ structure obtained by the search (Fig. 3a) has a highly symmetric perovskite layer as shown in Fig. 4a. However, when we calculate the phonon band structure, it was found to have imaginary frequencies (Fig. 4c). Pushing along the imaginary mode (at $(-0.5, 0.5, 0)$ of the conventional cell) allows us to obtain a structure with tilted OLi_4Fe_2 octahedra in a $a^0b^+c^0$ tilt system with space group $P2_1$ (Fig. 4b). Recomputing the phonon dispersion reveals that the imaginary mode has disappeared, which can be seen in Fig. 4d. The energy per atom is reduced by about 1 meV for this distorted structure. For $\text{Li}_4\text{Fe}_3\text{S}_3\text{O}_2$, the lowest energy structure generated by the enumeration of symmetrically inequivalent structures (Fig. 3c) was found to be dynamically stable. Imaginary frequencies have been also found in $\text{Li}_2\text{Fe}_3\text{S}_2\text{O}_2$ and $\text{Li}_2\text{Fe}_4\text{S}_3\text{O}_2$, which are subsequently eliminated by following the corresponding modes. Their final dy-

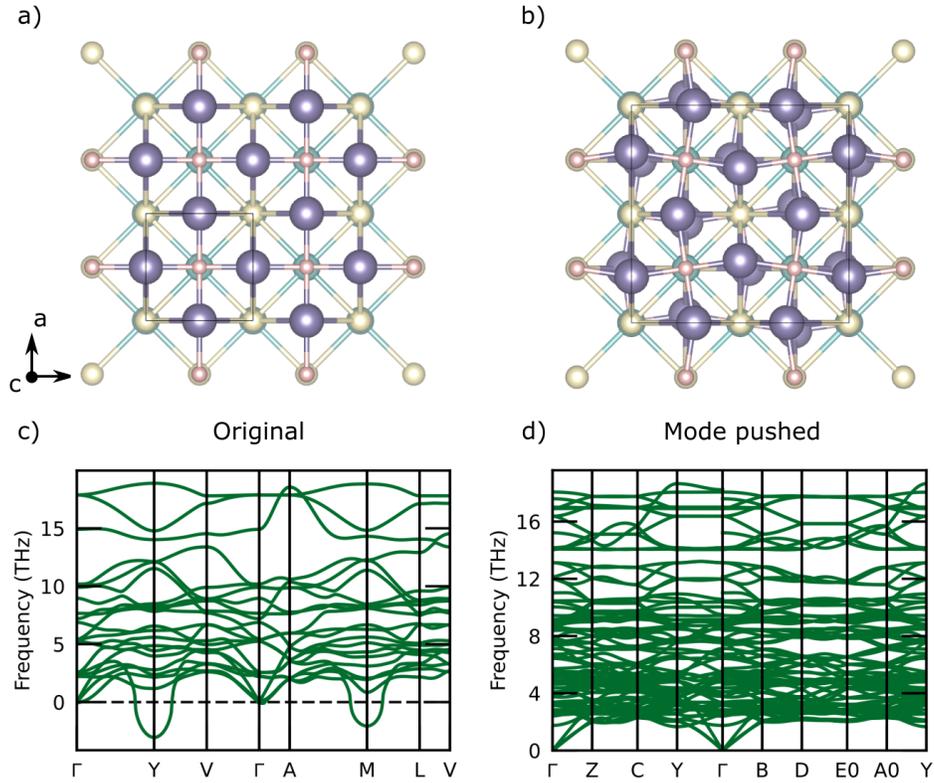


Figure 4: (a) The $\text{Li}_2\text{Fe}_2\text{S}_2\text{O}$ from the search, looking down the z direction. (b) The dynamically stable $\text{Li}_2\text{Fe}_2\text{S}_2\text{O}$ structure with rotated OLi_4Fe_2 octahedra obtained by following the imaginary phonon modes. (c) The phonon band structure of $\text{Li}_2\text{Fe}_2\text{S}_2\text{O}$ with imaginary frequencies. (d) The phonon band structure of mode-pushed $\text{Li}_2\text{Fe}_2\text{S}_2\text{O}$. Colour coding: cream-S, purple-Li, cyan-Fe, pink-O.

namically stable structures have lower energies by 2.6 meV and 0.2 meV compared with the non-distorted structures respectively, giving negligible effects on their thermodynamic stabilities. Since the structure searching was carried out with small unit cells containing symmetry operations, distortions that require increased cell sizes are expected to be missing. Nevertheless, as the typically energy reduction after mode-pushing is small, the structures obtained directly from the search are already sufficiently accurate for evaluating thermodynamic stability. Phonon band structures for the phases mentioned above can be found in the supporting information Fig. S4 and Fig. S5.

Electrochemical properties of the predicted phases

The average voltages, volume changes after delithiation and calculated theoretical capacities of the predicted phases are tabulated in Table 1. For Li-rich phases, only the capacity from the $\text{Fe}^{2+}/\text{Fe}^{3+}$ redox is considered here, and Li orderings in the delithiated structures are enumerated for calculating the voltages. Li_2FeSO is found to have a voltage of 2.3 V, which is in reasonable agreement with the experimentally obtained 2.5 V. We note that for disordered materials, voltages calculated using small ordered unit cell may not be accurate, and more rigorous approaches such as cluster expansion should provide better results. The two anti-RP phases, $\text{Li}_2\text{Fe}_2\text{S}_2\text{O}$ and $\text{Li}_4\text{Fe}_3\text{S}_3\text{O}_2$, are predicted to have voltages 2.9 V and 2.5 V respectively. Compared to the Li_2FeSO phase (223 mAh/g), they have higher theoretical capacities (261 mAh/g and 249 mAh/g) because their Li:Fe ratios are closer to 1:1. The voltage profiles of both materials are computed by enumerating unique configurations with different numbers of Li atoms removed in the primitive cells, including four and two formula units respectively. For both $\text{Li}_2\text{Fe}_2\text{S}_2\text{O}$ and $\text{Li}_4\text{Fe}_3\text{S}_3\text{O}_2$, multiple intermediate phases are found to exist, giving a sloped voltage profile as shown in Fig 5.

The band gaps of the predicted phases are found to range between 1.8 eV and 2.2 eV using the HSE06 functional, which are a lot narrower than that of LiFePO_4 , which has a band gap of 3.8 eV - 4.0 eV measured experimentally.⁵⁶ In comparison, the band gap of

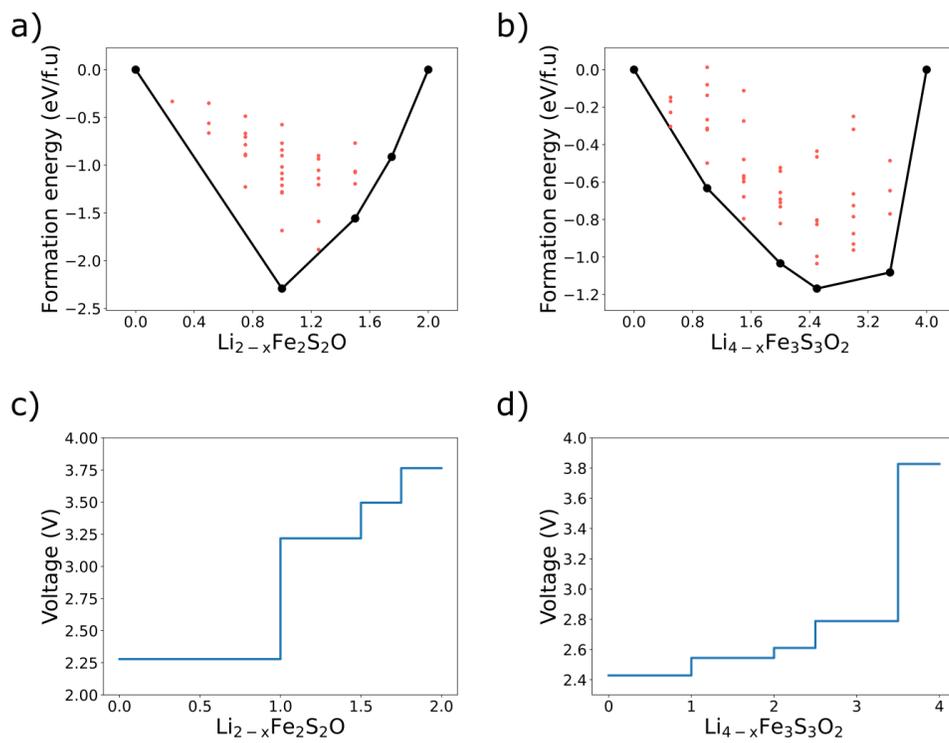


Figure 5: Convex hulls of delithiated structures and voltage profiles for (a,c) $\text{Li}_2\text{Fe}_2\text{S}_2\text{O}$ and (b, d) $\text{Li}_4\text{Fe}_3\text{S}_3\text{O}_2$.

LiCoO₂ has been reported to range from 1.7 eV to 2.7 eV in experimental studies.^{57,58} Hence, the new oxysulphide phases have the potential of being sufficiently electronically conductive as cathodes. The projected density of states of the predicted phases (Fig. S6) suggest that their valence band maxima are mainly composed of Fe d states with some contributions from oxygen and sulphur p states. This confirms that the Fe²⁺/Fe³⁺ is the main contributor to the redox capacity.

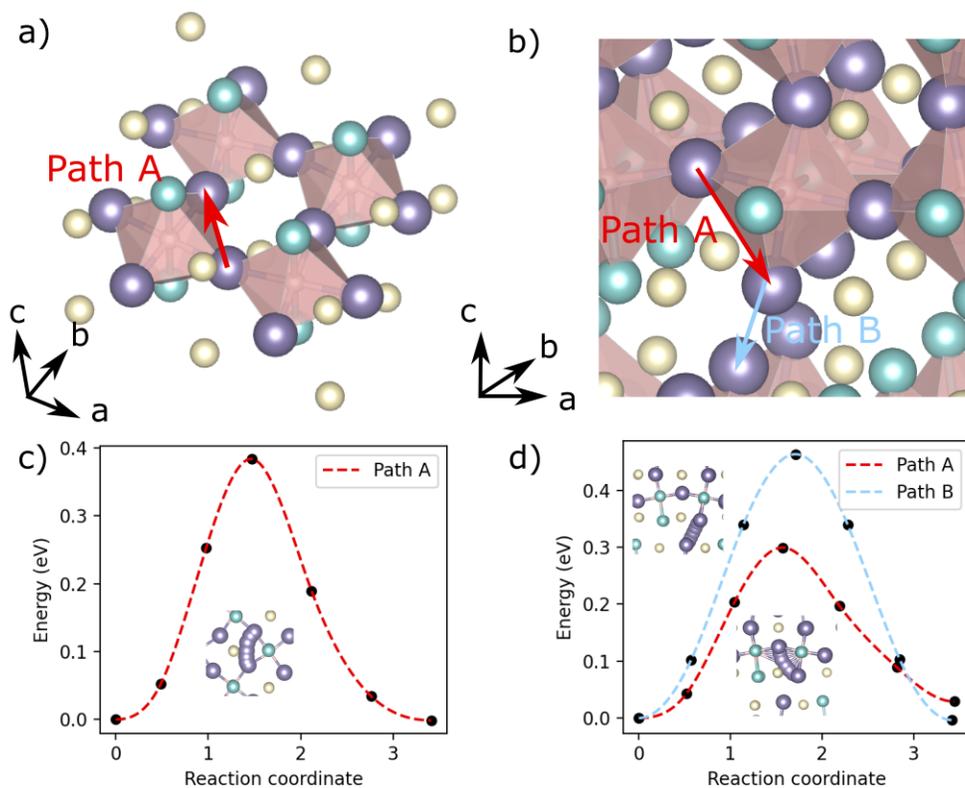


Figure 6: Potential Li diffusion pathways for (a) Li₂Fe₂S₂O (showing only the perovskite layer) and (b) Li₄Fe₃S₃O₂ with their corresponding transition state energies (c,d) calculated using the climbing-image nudged elastic band method. Colour coding: cream-S, purple-Li, cyan-Fe, pink-O. The coordination polyhedrons drawn are centered on oxygen atoms.

In addition to good electronic conductivity, the existence of fast lithium ion conduction pathways is also crucial for cathode materials. For Li₂Fe₂S₂O, the Li atoms only occupy the sites within the Li₂O layer of the perovskite environment as shown in Fig. 6a. Each Li is under octahedral coordination by four S atoms and two O atoms, and it has four nearest neighbour Li atoms and four next-nearest neighbours. The nearest neighbour pathway is

labelled as Path A in Fig. 6a. The climbing-image nudged elastic band (NEB) method has been used to study the minimum energy pathway for a single Li vacancy to migrate. The barrier between the nearest neighbour (NN) sites is found to be 0.38 eV, as shown in Fig. 6c. Multiple symmetrically equivalent routes like this form a percolating network, allowing Li diffusion in the *ab* plane shown in Fig 6a. For the next-nearest neighbour (NNN), the barrier height is increased to 0.95 eV (Fig S7a). The large difference in the barrier heights between the two cases can be understood as the former requires the Li atom to go through the face of the coordination octahedron around it, whereas the latter needs to go squeeze through the edge made of two S atoms with additional repulsion from the nearby Li atoms. In layered cathode materials, the Li atoms are known to take an indirect route through the tetragonal sites going through the faces of LiO_6 octahedra, rather than the direct path through the edges.⁵⁹

The $\text{Li}_4\text{Fe}_3\text{S}_3\text{O}_2$ structure has many inequivalent pathways, and we select representative paths in both the perovskite layer and the rock salt layer, as shown in Fig. 6b. The A and B paths correspond to the NN pathways inside the perovskite and rock salt layers, and they have transition state barriers 0.30 eV and 0.46 eV respectively. We have also considered the potential pathway through the tetrahedral site coordinated by four S^{2-} in analogy to the diffusion in layered Li metal oxides. However, the Li atom is found to be not stable at that intermediate site, since after relaxations the Li atom returns to its starting position. This can be understood as the occupation of the tetrahedral site would in fact result in very short Li-Fe separation with the Fe atom in the perovskite ordered layer above/below, giving rise to increased electrostatic energies. Here, the direct oxygen-dumbbell hop of Path B is already much lower than the counterpart in LiCoO_2 ,⁵⁹ which can be attributed to larger and more polarizable S^{2-} compared with O^{2-} . Similar to $\text{Li}_2\text{Fe}_2\text{S}_2\text{O}$, hopping between the NNN sites is found to have much higher barrier heights. The two pathways calculated, Path C and Path D (Fig S7b), are found to have barrier heights of 1.65 eV and 0.94 eV respectively. Within the rock salt layer, Path B forms a percolating channel along the *b* direction in Fig 6b. A

percolating network also exists in the perovskite layers, which consists of multiple Path A-like segments, permitting the diffusion in both a and c directions. Tilted OFe_2O_4 octahedra result in six inequivalent NN pathways inside the perovskite layer (Fig S7e). To have a more comprehensive coverage of different environments, two more A-like hopping paths are computed, A1 and A2, and found to have barrier heights of 0.40 eV and 0.48 eV respectively (Fig S7c&d). Without exhaustively repeating NEB calculations for all pathways inside the perovskite layer, it is reasonable to conclude that the barrier heights should range from 0.3 to 0.5 eV, which are sufficiently low to allow Li diffusion.

4 Discussion

Our computational exploration of the lithium iron oxysulphides has reproduced the known Li_2FeSO phase and a series of other stable and metastable polymorphs, among which the $\text{Li}_2\text{Fe}_2\text{S}_2\text{O}$ and $\text{Li}_4\text{Fe}_3\text{S}_2\text{O}_2$ have been identified as potential cathode materials. Compositions that are not included in Table 1 are too thermodynamically unstable to be synthesised. Hence they are not investigated further.

The renewed interests in LiFePO_4 and advancement in manufacturing processes have made it the top pick for low-cost and sustainable Li-ion batteries. Compared to polyanion based materials, the oxysulphides have the advantage of increased specific capacities. For example, the theoretical capacity of $\text{Li}_2\text{Fe}_2\text{S}_2\text{O}$, 260 mAh/g, is much higher than that of the LiFePO_4 (170 mAh/g). On the other hand, LiFePO_4 has a higher voltage at 3.5 V, giving a theoretical energy density of 595 Wh/kg, while oxysulphides suffer from relatively low voltages (< 3 V). The theoretical energy densities of $\text{Li}_2\text{Fe}_2\text{S}_2\text{O}$ (2.9 V) and $\text{Li}_4\text{Fe}_3\text{S}_2\text{O}_2$ (2.5 V) are 744 Wh/kg and 633 Wh/kg respectively, which still offer up to 20% increase. Note that due to the poor electrical conductivity of pristine LiFePO_4 , carbon coating on nanometer-sized particles is necessary to achieve good electrical conductivity,^{4,60} which lowers the specific capacity in practice. In comparison, the oxysulphides do not have this problem as they

are expected to have better electric conductivity. Another difference between LiFePO_4 and the oxysulphides is that the existence of intermediate delithiated phases in the latter gives sloped voltage curves similar to other oxides based cathodes, whereas the Li intercalation in the former takes place via two-phase reactions, resulting a flat voltage profile.⁴

The distances to hull of the $\text{Li}_2\text{Fe}_2\text{S}_2\text{O}$ and $\text{Li}_4\text{Fe}_3\text{S}_3\text{O}_2$ (3.4 meV and 3.3 meV) fall into range of the metastability of known quaternary compounds.⁵¹ Nevertheless, having a small distance to hull is not a sufficient condition to infer that experimental synthesis would be straightforward for realising these metastable phases. As our calculations are limited to crystalline phases at 0 K, the effect of disordering is not accounted for. Due to the similar ionic radii of Li^+ and Fe^{2+} , it is possible that the predicted compounds exist in disordered forms. Such entropy contributions from a disordered lattice provide further stabilisation at elevated temperatures. However, this also implies that the competing effect from a disordered Li_2FeSO phase is underestimated in our calculations. Li_2FeSO is found to be stable in calculations, which is not fully consistent with the observed partial decomposition into binary phases at intermediate temperatures.²² This may be attributed to systematic errors in the treatment of transition metals. Effects of finite-temperature on the free energy is also difficult to include directly in theoretical calculations. We use a recently developed machine learned descriptor to estimate the Gibbs free energy and construct convex hulls at finite temperatures,⁶¹ and the results are found to be qualitatively similar to those computed at 0 K. More details can be found in the supporting information. It is likely that direct synthesis of these predicted phases is no easier than that for Li_2FeSO . Adopting indirect routes may be fruitful. For example, ion-exchange can be a potential approach of synthesising $\text{Li}_2\text{FeS}_2\text{O}_2$ from $\text{Na}_2\text{Fe}_2\text{S}_2\text{O}_2$.²⁶

5 Conclusion

The Li-Fe-O-S chemical spaces have been explored using ab initio random structure searching (AIRSS), and a series of potentially synthesisable phases that are close to or on the convex hull have been predicted. Among these candidate phases, two anti-RP structures materials $\text{Li}_2\text{Fe}_2\text{S}_2\text{O}$ and $\text{Li}_4\text{Fe}_3\text{S}_3\text{O}_2$ are particularly promising for cathode applications. Density functional theory calculations show that they have voltages similar to that of the previously reported Li_2FeSO phase, and their theoretical specific capacities exceeds the latter. Fast Li conduction channels are revealed using climbing-image nudged elastic band calculations. If successfully synthesised, they can be good contenders to the commercialised LiFePO_4 cathodes. Even though the low voltages (2.9 V and 2.5 V) are nowhere near that of LiFePO_4 , they are compensated by much increased theoretical gravimetric capacities (~ 250 mAh/g vs ~ 170 mAh/g). Our work also demonstrates that first-principles structure prediction is an effective way to explore complex quaternary chemical spaces where many new materials are waiting to be discovered for battery cathode applications and beyond.

Supporting Information Available

Supporting Information: Detailed comparisons about correction schemes used for formation energies; Discussion on applying a machine learned descriptor for predicting finite-temperature stability; Figures of phonon band structures and electronic projected density of states of the predicted phases; Additional minimum energy pathway plots of Li-diffusion for $\text{Li}_2\text{Fe}_2\text{S}_2\text{O}$ and $\text{Li}_4\text{Fe}_3\text{S}_3\text{O}_2$; A link for accessing the calculation data online.

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TOC Graphic

