Coupled deep-mantle carbon-water cycle: Evidence from lower-mantle diamonds

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Graphical abstract

Public summary

- A novel approach was developed to assess the pressure-temperature conditions of entrapment of inclusions in diamonds
- The viscoelastic relaxation of diamond has a significant effect on the evolution of pressure and temperature
- Ice-VII-bearing diamonds have formed in wet, cool environments at depths down to 800 km
- The coupled recycling of water and carbon is present in the deep mantle
Diamonds form in a variety of environments between subducted crust, lithospheric and deep mantle. Recently, deep source diamonds with inclusions of the high-pressure H₂O-phase ice-VII were discovered. By correlating the pressures of ice-VII inclusions with those of other high-pressure inclusions, we assess quantitatively the pressures and temperatures of their entrapment. We show that the ice-VII-bearing diamonds formed at depths down to 800 ± 60 km but at temperatures 200–500 K below average mantle temperature that match the pressure-temperature conditions of decomposing dense hydrous mantle silicates. Our work presents strong evidence for coupled recycling of water and carbon in the deep mantle based on natural samples.

**Keywords:** diamond; deep mantle; water and carbon cycle; first-principles calculations

**INTRODUCTION**

Decades of effort in geodynamic modeling and seismic observations have confirmed the presence of lateral heterogeneities in the transition zone (TZ) and lower mantle (LM) of Earth.1–3 These heterogeneities are distinguished through reduced seismic velocities and seismic wave reflections and can be generated by the presence of melt or fluid,4 or by thermal and chemical variations in the mantle.4,5 In this context, diamonds provide key information because some of them contain inclusions that were entrapped in the TZ or LM.6,7–10 and, hence, are part of the global deep-carbon cycle. Generally, diamond formation is not bound to subduction. The vast majority of diamonds, including most of the diamonds that we have examined, have formed in the subcontinental lithosphere without direct relation to subduction processes. However, the release of carbonaceous material from subducted slabs can result in the formation of diamond in a reducing mantle through a reaction of enstatite with magnesite12 or at greater depth through disproportionation of carbon from carbonate and carbide.13,14 Iron carbide has been proposed to be an abundant accessory mineral in the mantle at depths where the pressure-induced disproportionation of Fe²⁺ into Fe⁰ plus Fe³⁺ dominates the redox conditions.13 This mechanism finds support in the frequent occurrence of iron and iron carbide inclusions in diamonds from deep mantle.10,15,16

Recently, the discovery of hydrous ringwoodite7 and ice-VII10 as inclusions in diamonds has correlated the question of water storage in the deep mantle with the carbon cycle. It was also shown that some inclusions sustain remnant pressures of several gigapascals (GPa),9,10 high enough to imply formation in the TZ or LM. Hence, these inclusions provide direct mineralogical information about the TZ and LM, whereas products of retrograde transformations of high-pressure minerals15,16 conserve composition but no fully quantifiable information about the pressures and temperatures of their entrapment. Here, we show that diamonds with inclusions of ice-VII and other minerals at high remnant pressure not only represent entrapment in environments rich in carbonaceous aqueous fluid, which permit the formation of diamond13 and ice-VII,10 but that they generally represent very cool environments within the LM, above the solidus of wet carbonated peridotite but below the solidus of wet peridotite, and are in apparent correlation with the decomposition boundary of dense hydrous Mg silicate phase D.

Our approach is based on the in situ observation of µm-to sub-µm scale mineral inclusions in diamonds which bear remnant pressures in the range of 2–14 GPa (Table 1; Figure 1). These remnant pressures define foot points of their P-T paths that these inclusions experienced between the time of their entrapment in growing diamond and presence.9,10,17 Inclusions that were entrapped at the same depth in the Earth have P-T paths intersecting at the same P-T point. Here, we use a new concept of correlating P-T paths of different inclusions in one diamond for assessing the P-T of entrapment (see the materials and methods). This approach is different from earlier assessments which involve a priori assumption about the geotherm.9,10,17 At the same time, we take full account of the viscoelastic relaxation of the host diamond (see the supplementary methods). In our approach, assessment of the P-T paths is in two steps: first through the condition of the equal strain of host diamond and inclusions (isomeke,17 which we call here “elastic paths” to emphasize the abstraction from viscoelastic relaxation) and, second, the role of viscoelastic relaxation of diamond.17 Finally, we show that accounting for viscoelastic relaxation gives temperatures that match the average mantle residence temperatures obtained from nitrogen defects in diamond,17 which give estimates of average residence temperatures as a function of residence time.17 In our approach, P and T are strictly correlated. Thus, independent confirmation of T also confirms that the assessment of P is correct.

**RESULTS**

The information about diamonds investigated in this work is described in detail in the supplementary methods. We conducted X-ray diffraction measurements on the inclusions. The diffraction and X-ray fluorescence data of ilmenite (ilm>95) and taenite (Fe50Ni50) from Diamantina-1 gave the following volumes: 307.9(5) and 44.9(3) Å³, respectively. The Fe/Mg ratio of ilmenite was assessed through Rietveld refinement and the Fe/Ni ratio of taenite through the integrated intensity ratio of the Fe and Ni K fluorescence data. Published composition, volumes, and diffraction data of a garnet-ilmenite-TAP (10 Å phase)-liebermannite inclusion in diamond ON-ZIZ-7425 are included in Table 1 because they provide a cross-check of the present method with conventional garnet geobarometry.26,28,29 In addition, we measured the infrared spectra of the diamonds...
and used the calibrations by Boyd et al.30,31 for estimating the amount of nitrogen in A- and B-type defects, respectively. The amount of D-type defects was found to be less than 10 ppm in any specimen based on the calibration by Clark and Davey32 and was neglected as being within uncertainties of the amounts of A-type and B-type defects. The nitrogen contents from A- and B-type defects range from 52 to 96 ppm and from 49 to 134 ppm, respectively. The corresponding percentage of A-type defects and the approximate age of the diamonds (Table 1) were used to estimate average mantle residence temperatures.25,26 The fitted defect profiles and observed spectra are shown in Figure S1. Nitrogen contents and estimated mantle residence temperatures are presented in Table 1.

Remnant 300 K pressures of inclusions were assessed from their unit cell volumes corrected for the elastic relaxation of diamond at 300 K.17 The corrected pressures were used as foot points for calculations of P-T paths for the inclusions based on the condition of the equilibrated strain of inclusion and diamond (elastic path). In a second step, the paths were corrected for viscoelastic relaxation of the hosting diamond.

### DISCUSSION

We start with discussing the common case of annealed inclusion-diamond systems. Temperatures near the average mantle adiabat are well above the temperatures of viscoelastic relaxation of diamond.25,26 This observation was already made by Anzolini et al.19 for assessing the entrapment pressure of a periclase inclusion in a diamond. Thus, P-T of inclusions and their hosting diamond equilibrate with the surrounding mantle and follow a nearly adiabatic path upon ascent until the temperature drops below the brittle-to-viscous transition in diamonds. This is illustrated in Figure 1A for inclusions in a type IaB diamond from the Diamantina alluvial deposits. The remnant pressures of the inclusions are 1 and 4 GPa, respectively, at 300 K, which are remnant pressure values typically found for the super-deep diamonds from Juina, Brazil, that formed at least within the TZ or deeper.19 The elastic P-T paths of ilmenite and taenite intersect right at the viscoelastic limit (Figure 1B; for further details, see the supplemental methods). As a check, we estimate T independently through the N aggregation state in the diamonds.22 We find that the adiabatic path gives the same temperatures as the N aggregation in their host diamonds within uncertainties (Table 1; Figure 2). Therefore, the adiabatic path provides plausible temperature estimates for the inclusions. In contrast, the elastic paths markedly overestimate T and underestimate P. Along an adiabatic path P and T are correlated. Therefore, with T independently confirmed, our approach also provides reliable estimates of P.

The results are summarized in Figure 2. All P-T points are above the solids of wet carbonated peridotite.35 All diamonds with ice-VII inclusions fall within a P-T range between the solidi of wet and wet carbonated peridotite, but quite below the solidus of dry carbonated or even alkaline-rich peridotite.36 Notably, all P-T points are tied to wet cool environments at depths down to 820 km, and temperatures of 200–500 K below a reference average mantle adiabat.34 This finding is consistent with the formation of these diamonds in the surrounding of cold slabs (Figure 2). Below ~800 km depth the P-T points of entrapment are at the decomposition line of the dense hydrous magnesium silicate phase D,37 suggesting that the presence of H₂O, which is now conserved as ice-VII, and the formation of the hosting diamond

### Table 1. Pressures and temperatures from the adiabatic approach compared with temperatures from nitrogen aggregation (second column from the right) using ages from Chaves et al.19,26 and Timmerman et al.25,33

<table>
<thead>
<tr>
<th>Specimen</th>
<th>Nitrogen aggregation</th>
<th>Adiabatic P-T</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>A (ppm)</td>
<td>B (ppm)</td>
</tr>
<tr>
<td>Orapa GR1507</td>
<td>94 ± 9</td>
<td>49 ± 7</td>
</tr>
<tr>
<td>Orapa GR1519</td>
<td>87 ± 9</td>
<td>53 ± 7</td>
</tr>
<tr>
<td>Orapa M57666</td>
<td>96 ± 6</td>
<td>68 ± 7</td>
</tr>
<tr>
<td>Diamantina</td>
<td>52 ± 12</td>
<td>134 ± 15</td>
</tr>
<tr>
<td>ON-ZIZ74</td>
<td>55 ± 8</td>
<td>13 ± 1</td>
</tr>
</tbody>
</table>

Further details are given in the supplemental methods. *Pressure from elastic P-T paths and temperature from N aggregation. †Unknown age but a residence time of 0.1 Ga corresponds to 1,490 ± 10 K while 3 Ga give 1,410 ± 10 K. ‡P and T were assessed through the intersection of isomel of ilmenite with the geobarometer pressure of coexisting garnet.
are correlated with the decomposition of hydrated mantle silicate. Metallic iron in the same diamonds may be a remnant of the redox-reaction mechanism proposed by Rohrbach and Schmidt,\textsuperscript{13} which, therefore, may be active within the LM. Preservation of high remnant pressure and an overall low-temperature regime and short residence time in the mantle are correlated: the sample with the strongest mantle residence time (from Diamantina, Table 1) has kept no record of a P-T path beyond the elastic deformation regime of diamond. In many deep-source diamonds, long residence at temperatures above the elastic-viscoelastic limit of diamond has removed the record of their origins beyond the observation of transformation products of former high-pressure phases. However, the observation of hydrous minerals,\textsuperscript{8,25,39} taenite, and iron as inclusions in ultradepend-source diamonds\textsuperscript{9,10,11} point toward a common origin at 500–800 km depth but different paths and timescales of ascent (Figure 2). It cannot be excluded that diamonds form at even greater depth. Equally well, remnant water may be kept in the mantle to even greater depth,\textsuperscript{37} but we show that water present at the depth of 800 ± 60 km is still involved in the recycling of water and carbon (as witnessed through the diamonds) (Figure 2). This concept is shown in a cartoon.

Figure 1. P-T paths of high-pressure inclusions in diamonds (A) Inclusions of ilmenite (ilm−95, geik−95) and taenite (Fe50Ni50) observed in a diamond from the Diamantina alluvial deposits (see the supplemental methods). The calculated elastic release paths start to intersect at the diamond viscoelastic limit (hachured area). This indicates that the inclusions were in elastic equilibrium with the host diamond above this limit. Above this limit, P-T is expected to have evolved close to a mantle adiabat (blue line). The ilmenite-lute phase boundary is indicated. (B) Inclusions of ilmenite (ilm=92geik=7) and iron (Fe=95) in a diamond from Orapa, Botswana. The range of foot pressures and P-T paths reflect the uncertainties (see the supplemental methods). Offsets of paths are the results of phase transformations. The blue hachured region indicates the transition from elastic-to-viscoelastic deformation of diamonds. We assess the corresponding T through the intersection of a reference adiabat (blue) with P + ΔP (indicated through dashed lines). This P + ΔP and T gives a lower limit of P-T of entrapment. However, the temperature of this lower limit matches the temperature estimate from nitrogen deficit distribution in this diamond (Table 1). This shows that the lower limit represents the actual P-T path quite closely.

Figure 2. P-T points of entrapment of inclusions in diamonds Blue squares, assessment based on adiabatic approach, hollow diamonds, temperature assessed through nitrogen aggregation. Reference mantle adiabat is from Brown and Shankland,\textsuperscript{10} carbonsaceous, wet, and wet-carbonsaceous solidus of peridotite are from Tsuchauer et al.,\textsuperscript{33} Litasov et al.,\textsuperscript{35} and Ghosh et al.\textsuperscript{36} The decomposition boundary of phases D to bridgmanite (bdm), stishovite (st), and fluid was taken from\textsuperscript{37} All inclusions were entrapped in diamonds which grew in cool wet environments down to 820 km depth. Consistent with experiments, these diamonds grew above the solidus of C-H-O fluid-bearing peridotite.\textsuperscript{37} The formation of these diamonds is tied to local wet areas in the TZ and dehydration of phases B and D\textsuperscript{37} above ~800 km. (Figure 3). This does not imply that all deep-mantle diamonds formed in similarly wet environments or that certain deep layers in Earth are globally wet. Nevertheless, we establish a conjunction between these conditions within the LM, the deep-carbon, and the deep-water cycle.

Conclusion
We have developed a novel approach to assess the entrapment P-T conditions of inclusions with high remnant pressure in diamonds. Similar to Anzolini et al.,\textsuperscript{18} we find that the viscoelastic relaxation of diamond has a significant effect on the evolution of P and T of inclusions. The results show that ice-VII-bearing diamonds have formed in wet, cool environments at depths down to 820 km and temperatures of 200–500 K below the average mantle geotherm. This is consistent with the formation of these diamonds in the surrounding of cold slabs. This work presents evidence for the recycling of water and carbon in the deep mantle, even to the LM.

MATERIALS AND METHODS
X-ray diffraction and X-ray fluorescence analysis
X-ray diffraction data were collected at beamlines 13-IDB, -IDE, and 34-IDE at energies of 30, 19, and 22 keV, respectively. The primary beams were focused by elliptical mirrors to micrometer scale (34-IDE: 0.5 μm) beam diameters. Diffraction data were collected with area detectors, calibrated, and integrated with Diotas. X-ray fluorescence was excited by the same primary beams and collected with a Vortex detector. The diffraction data of the Orapa samples had been reported previously (see online deposition of Tsuchauer et al.\textsuperscript{11}). The diffraction- and X-ray fluorescence data of ilmenite (ilm=95) and taenite (Fe50Ni50) from Diamantinas-1 gave the following volumes: 307.9(5) and 44.9(3) Å\textsuperscript{3}. The Fe-Ni ratio of taenite- and iron-inclusions was assessed using the LARCH program.\textsuperscript{37}

Infrared spectra of the examined diamonds
The spectra of all samples except GRR 1521 were collected in transmission at beamline 1.4, ALS, with a Nicolet Magna 760 FTIR bench and a Nico-Plan IR microscope with a 32× magnification Schwarzschild objective, with 1 cm\textsuperscript{-1} resolution and a HgCdTe detector with a KBr beam splitter. Apertures were set to 20 × 20 to 40 × 60 μm\textsuperscript{2} spatial resolution. The spectrum of the sample Diamantina-1 was obtained from the uncut specimen. The spectrum of GRR1521 was taken from a crushed, clear piece with a Thermo-Nicolet iS50 FTIR at the mineral spectroscopy laboratory at Caltech in transmission with a glow bar source and 2 cm\textsuperscript{-1} resolution. All other spectra
were obtained from laser-cut, polished platelets. A synthetic type II diamond was used for assessing absorption between 1,000 and 1,500 cm\(^{-1}\). Spectra were background subtracted and scaled to an equal thickness of 10 mm. Contributions of A-, B-, and D-type defect bands were assessed by using the pure defect-type spectra reported by Taylor et al.\(^4\) We used the calibrations by Boyd et al.\(^3\) for estimating the amount of nitrogen in A- and B-type defects, respectively. The amount of D-type defects was found to be less than 10 ppm in any specimen based on the calibration by Clark and Davey\(^2\) and was neglected as being within uncertainties of the amounts of A- and B-type defects. The corresponding percentage of A-type defects, and the approximate age of the diamonds (Table 1) were used to estimate average mantle residence temperatures.\(^2,24\) These temperatures are used as comparison with the temperatures obtained from the modeled P-T paths. The N content in the hosting diamonds may be locally lower and such variations cannot be clearly seen in transmission IR spectroscopy but we found that the temperatures obtained from P-T paths are not systematically different from the estimates based on N defects. The fitted defect profiles and observed spectra are shown in Figure S1. These spectra and fits correspond to the results in Table 1.

Ab initio calculations

Computational calculations were conducted using the Quantum Espresso package\(^5\) (ilmenite and liulite\(^6\)), Vienna ab initio simulation package (VASP)\(^7\) plus finite displacement approach\(^8\) for ice-VII, first-principles molecular dynamics simulations (FPMD) on the cubic box containing 210 H\(_2\)O molecules for fluid H\(_2\)O, and equation of state of iron phases from Dorogokupets et al.\(^8\).

For ilmenite and liulite, the local density approximation (LDA) was used for assessing the exchange-correlation. The energy cutoff for electronic wave functions was set at 70 Ry. The oxygen pseudopotential was generated using the Troullier-Martins method\(^9\) with a cutoff radius of 1.45 Bohr and a valence configuration of 2s\(^2\)2p\(^4\). The pseudopotentials for iron (Fe) and titanium (Ti) were generated using the Vanderbilt method\(^10\) with a valence configuration of 3s\(^2\)3p\(^6\)3d\(^2\)4s\(^2\) for iron and a valence configuration 3s\(^2\)3p\(^6\)3d\(^2\)4s\(^2\) for titanium. The cutoff radii for both pseudopotentials are 1.8 Bohr. Due to the existence of large on-site Coulomb interactions among the localized electrons (e.g., 3d electrons),\(^11\) we introduced a Hubbard U correction to the LDA (LDA + U). Hubbard U values for Fe and Ti atoms in ilmenite were non-empirically determined using the linear response method.\(^12\) Crystal structures of ilmenite were well optimized using the damped variable cell shape molecular dynamics at variable pressures on a 6 x 6 x 6 k-point mesh, and vibrational density of state (VDoS) values were calculated using the finite displacement method.\(^13\) However, the vibrational phonon calculations for liulite report some imaginary frequencies, which hampers the calculations of the high-temperature equation of state (EoS). Here, we obtained the 0 K isotherm of liulite\(^14\) from LDA + U calculations and estimated the EoS at different pressures using the thermal expansion of bridgmanite.\(^15\) We assumed that temperature shows a similar effect on the volume changes of FeTiO\(_3\) and MgSiO\(_3\) perovskites.

Due to the failure of LDA in predicting the properties of the H\(_2\)O system,\(^16\) we performed first-principles calculations for ice-VII and H\(_2\)O fluids by adopting the generalized gradient approximation\(^17\) for the exchange-correlation function. All calculations for ice-VII were done using VASP code,\(^18\) and the PBE-type of pseudopotentials for hydrogen and oxygen were used. The energy cutoff for plane waves was set as 700 eV. For solid ice-VII, relaxed crystal structures under different pressures were obtained by optimizing cell parameters and atomic coordinates at an 8 x 8 x 8 k-point mesh grid, and their VDoS values were derived from the finite displacement method.\(^19\) For H\(_2\)O fluids, we conducted FPMD simulations on the cubic box containing 210 H\(_2\)O molecules to determine the EoS. FPMD simulations were propagated in the canonical ensemble (NVT) with a Nose thermostat and the Brillouin zone was sampled at gamma point. All simulations on cubic boxes with variable volumes lasted at least 40,000 steps with a time step of 1.0 fs, and the temperature was set as 600, 900, 1,200, 1,500, 2,000, 2,300, 2,500, 2,700, and 3,000 K. Pressures at different temperatures and volumes can be derived by calculating ensemble averages of the instantaneous pressure after reaching the equilibrium state.

Determination of P-T paths

Remnant 300 K pressures of inclusions were assessed by synchrotron microdiffraction of their unit cell volumes at beamlines 13-IDDIDIE and 34-IDD. Experimental parameters and data are provided in the supplemental information. We used empirical equations of state of the mineral inclusions for the given composition. Subsequently, the elastic relaxation of diamond at 300 K was corrected.\(^20\) The corrected pressures were used as foot points for calculations of pressure-temperature (P-T) paths for the inclusions and the paths were calculated based on the condition of the equilibrated strain of inclusion and diamond (elastic path). We used the variance of pressures for separate inclusions of the same phase as upper and lower bounds for the foot points. Because of the low compressibility, low thermoelastic softening, and low thermal expansivity of diamond, the elastic paths are close to but not identical with isochores.\(^21\) First-order phase transitions were addressed by calculating separate paths for low and high P-T phases, assessment of the pressure difference at the phase boundaries (coexistence range), and subsequent correction for diamond relaxation under isothermal conditions. The required thermoelastic parameters were obtained from ab initio calculations and literature data. Details of these calculations and the correction for minor chemical components are described above. By using empirical foot pressures we largely circumvent the issue of possible overestimation or underestimation of computed volumes from insufficient correction of electron exchange correlation. Consequently, deviations between computed and available empirical high P-T volume data are within the uncertainties of the latter. Generally, we used these deviations and the uncertainties of the foot point pressures in combination to estimate the upper and lower bounds of P-T paths (Figure 1). Uncertainties of intersection points are defined by the upper and lower intersection points of intersecting paths in P-T space.

All data are given in Tables 1 and S1–S3, and are plotted in Figures 1 and S2. Partial relaxation is a time-dependent, therefore, path-dependent process. Thus, changes in pressure, volume, and temperature are path dependent as well. In addition, partial relaxation is expected to differ for different inclusions, depending on their elastic moduli, phase transformations, and their actual sizes and shapes. We constrain this unknown time-dependent P-T path by two non-path-dependent limiting cases (Figure 1B). In case i), the intersection of the elastic P-T paths defines the upper limit of temperature and the lower limit of pressure of their P-T point because it defines the most rigid response of diamond to the stress exerted by the inclusions at a given P-T of the surrounding rock. This is shown in Figure 1B. For all examined specimens, these P-T intersection points are well above the viscoelastic limit of diamond and well above the present mantle geotherm (Figure 1B). In case ii) we look at the pressure differences between these inclusions at the elastic-viscoelastic transition temperature and use an adiabatic path for assessing the P-T of entrapment as a lower T limit (Figure 1B). It turns out that, within uncertainties, the adiabatic P-T paths give the same temperature as the correlation of nitrogen content in the host diamonds with the percentage of A-type defects (Table 1; Figure 2). As a low-temperature limit, we assume...
that an adiabatic path intersects the viscoelastic limit temperature of 1,200–1,300 K at the lowest observed pressure of the inclusions (Figure 1B). In the case of complete relaxation, the inclusion would have the same pressure at this temperature. The observed $\Delta P$ at the diamond elastic-viscoelastic transition quantifies an excess pressure and a corresponding adiabatic $\Delta T$ (Figure 1B). The transition from brittle elastic to visco-elastic behavior of diamond has been examined for single and polycrystals, the latter giving lower bounds. Without discussing the possible effect of Ni and P on the yield strength, we set the viscoelastic limit to the reported temperatures for single and polycrystals. These were calculated from the upper and lower section of the elastic P-T paths with these two limits (Figure 1B) and bracket $\Delta P$ and $\Delta T$. The validity of the adiabatic approach is confirmed through the agreement of the assessed temperatures with the temperatures obtained from N aggregation states (Figure 2; Table 1). A similar finding was reported by Anzolin et al. (1999) for single pericline inclusions from the T2.

REFERENCES


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AUTHOR CONTRIBUTIONS
O.T., S.H., and W.W. conceived and designed this project. W.W. performed the theoretical calculations. W.W. and O.T. wrote the manuscript and all authors contributed to the discussion of the results and revision of the manuscript.

DECLARATION OF INTERESTS
The authors declare no competing interests.

SUPPLEMENTAL INFORMATION
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