

Distributed Radar-aided Vehicle-to-Vehicle Communication

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Abstract—Establishing high-rate vehicle-to-vehicle (V2V) links with narrow beamwidth is challenging due to the varying network topology. We propose a distributed method where each vehicle associates local radar detections with GPS information from nearby vehicles. This avoids time-consuming channel estimation and provides high SNR, under the condition that reliable relative and absolute location information is present.

I. INTRODUCTION

Vehicles are expected to rely on wireless communication for several functionalities, including safety-related applications and traffic efficiency applications. Vehicle-to-vehicle (V2V) communication is currently standardized in ITS-G5, relying on WiFi-like protocols [1], [2]. Due to high mobility, intermittent connectivity, and the need for reliably and timely data transfer, as well as safety concerns, V2V communication is extremely challenging [3]. Multi-antenna techniques (MIMO) can help boost reliability, by providing a larger link budget through directional transmission [4]. However, this is only possible when channel state information (CSI) is known at the transmitter [5]. As obtaining such CSI entails additional overhead, directional transmissions are generally not considered and instead omnidirectional approaches are preferred. As a replacement for CSI, context information can be utilized, in particular location information [6]. For instance, the use of location information for directional beamforming was proposed in [7]. Both in-band and out-of-band location information have been considered [8], [9]. Among the sensors that can provide location information, we mention radar and GPS, which are viewed as key enablers for V2V applications. Radar provides relative situational awareness, where backscattered signals are processed to construct a map [10]. Absolute situational awareness is provided by GPS, where signals acquired from satellites and ground stations are used to determine the 3D position of the vehicle on earth. Accuracy for automotive radar varies from 1 cm to 1 m, and for GPS from 10 cm (for RTK GPS) to 10 m (for stand-alone GPS).

Recently, as terrestrial communication systems have started to operate in bands traditionally reserved for radar, there has been a growing interest in the convergence of communication and sensing [11], where communication signals at high carrier frequencies are used for sensing the environment [12], [13] or where radar signals are used for communicating information [14], [15]. Automotive radar, which uses a large bandwidth at high carrier frequencies is an ideal technology for joint

communication and sensing. It is then natural to identify and exploit synergies between the radar and communication functionalities.

The use of radar signals for improving communication has been studied in [16]–[21]. In [16], a BS equipped with a radar and communication sub-system (operating at different frequencies) is considered, where it is verified that the radar and communication channels share the same dominant paths. The paths detected by the radar are then used for directional data transmission. In [17], a similar problem to [16] is considered, but with radar and communication operating over the same band, but using separate waveforms. The radar recovers the angle of arrival (AoA) and angle of departure (AoD) of each path after which beamforming is designed towards those directions. In [18], 801.11ad communication at 60 GHz is considered, where a BS router is configured to send and receive radar signals. This allows determination of vehicle range and velocity, within a certain beamwidth. The communication uses these estimates to beamform for maximum throughput. In [19], the radar at the BS is passive and listens to the vehicle radars. The azimuth power spectrum from the radar is then used for BS-to-vehicle communication. A method to address the lack of synchronization between vehicles and BS is proposed. In [20] an indoor mmWave communication system is developed, where an access point first senses the environment. Once the environment is mapped, communication towards a specific user in a certain location is performed based on predicted propagation paths (including reflected paths). Finally, in [21] a scenario similar to [16] is considered, but with a single joint communication and radar device. No downlink pilots are needed. A tracking algorithm predicts the vehicles' states and utilizes these predictions to perform power allocation for both communication and sensing. Among the above works, only [21] considers the unknown data association between radar detections and vehicles. None of the above works develop solution for the V2V scenario.

In this paper, we propose radar-aided communication for V2V communication, develop a method for exploiting radar detections to steer highly directional communication signals. The method involves transforming radar detections to a global reference frame and then associating these transformed detections to vehicles. We analyze the impact of different accuracies of GPS and radar detections as well as different distance metrics between detected objects and vehicles. Our results

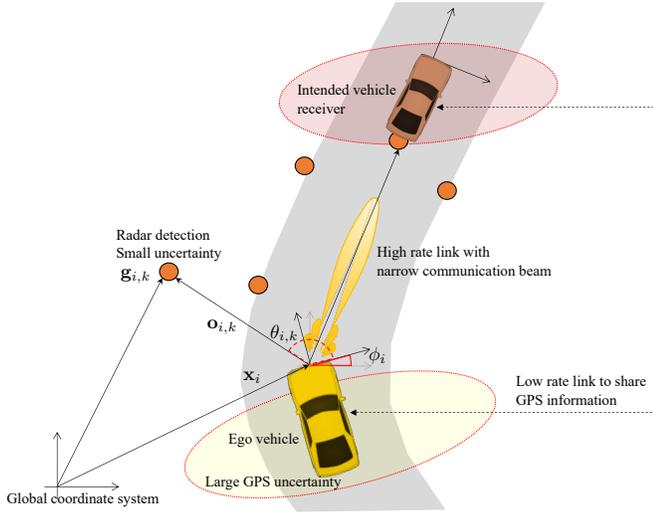


Figure 1. Scenario: the ego vehicle has unknown location and heading. It measures objects using a radar in its local frame of reference.

indicate that radar-aware communication can increase link quality, but only when GPS is sufficiently reliable.

Notation: We denote a multi-variate Gaussian density in variable \mathbf{x} with mean $\boldsymbol{\mu}$ and covariance $\boldsymbol{\Sigma}$ by $\mathcal{N}(\mathbf{x}; \boldsymbol{\mu}, \boldsymbol{\Sigma})$. We define the 2D rotation matrix

$$\mathbf{R}(\phi) = \begin{bmatrix} \cos \phi & -\sin \phi \\ \sin \phi & \cos \phi \end{bmatrix}. \quad (1)$$

II. SYSTEM MODEL

The overall model is visualized in Fig. 1, comprising vehicles and objects. Our focus is on the ego vehicle in yellow.

A. Geometric Model

We consider an environment with multiple vehicles with state in global coordinates of vehicle i denoted by $\mathbf{s}_i = [\mathbf{x}_i^T, \mathbf{v}_i^T, \phi_i]^T$, where \mathbf{x}_i is the 2D position, \mathbf{v}_i is the 2D velocity, and ϕ_i is the heading (measured w.r.t. the front bumper, see Fig. 1). In addition to the vehicles, there are objects in the environment with states \mathbf{g}_k (in global coordinates), comprising position and velocity. As objects have no identifier, we will denote the state of an object seen by vehicle i as $\mathbf{g}_{i,k} = [\mathbf{x}_{i,k}^T, \mathbf{v}_{i,k}^T]^T$. Both vehicles and objects are modeled as point targets, with vehicle locations coinciding with the radar equipment locations. Finally, we will consider a short transmission interval so that we can ignore mobility during the communication.

B. Measurement Model

Each vehicle is equipped with a GPS device, which provides the density $p(\mathbf{s}_i) = \mathcal{N}(\mathbf{s}_i; \bar{\mathbf{s}}_i, \mathbf{S}_i)$ in a global reference frame. Each vehicle also has a front-looking radar, which provides a set of N_i detection objects within the field of view. Each object k has an associated existence probability $\rho_{i,k} \in [0, 1]$ [22] and spatial density $p(\mathbf{o}_{i,k}^{\text{polar}} | \mathbf{s}_i) = \mathcal{N}(\mathbf{o}_{i,k}^{\text{polar}}; \mathbf{o}_{i,k}^{\text{polar}}, \mathbf{S}_{i,k}^{\text{polar}})$ in the vehicle's local frame of reference. Here, $\mathbf{o}_{i,k}^{\text{polar}} = [r_{i,k}, \theta_{i,k}, v_{i,k}]^T$

comprises distance $r_{i,k} = \|\mathbf{x}_i - \mathbf{x}_{i,k}\|$, AoA $\theta_{i,k}$ (measured from the local x -axis), and radial velocity. We assume $\mathbf{S}_{i,k}^{\text{polar}}$ to be a diagonal matrix with measurement variances in range, AoA, and radial velocity.

C. Communication Models

Each vehicle is equipped with two separate communication systems. First of all a standard low rate system (e.g., 4G or ITS-G5 [2]) that provides GPS information from neighboring vehicles. The set of neighbors is denoted by \mathcal{N}_i . The availability of such a system is reasonable, as all modern vehicles are equipped with such communication transceivers to support a variety of services. Secondly, each radar unit can serve as a directional communication transceiver [23], [24]. The direction of beamforming and the azimuth beamwidth can be controlled to achieve high SNR. The goal of vehicle i is to determine $(\theta_{ij}^{\text{beam}}, W_{ij}^{\text{beam}})$ in azimuth, in order to communicate with a neighboring vehicle $j \in \mathcal{N}_i$, without explicit channel estimation, in order to maximize the SNR [18]

$$\text{SNR}_{ij} = \begin{cases} \frac{P_t}{N_0 W} \frac{4\pi\lambda^2}{\|\mathbf{x}_i - \mathbf{x}_j\|^2} \frac{4\pi^2}{W_{ij,\text{el}}^{\text{beam}} W_{ij}^{\text{beam}}} & |\theta_{ij} - \theta_{ij}^{\text{beam}}| \leq W_{ij}^{\text{beam}} \\ 0 & \text{else,} \end{cases} \quad (2)$$

where θ_{ij} is the direction of vehicle j in the frame of reference of vehicle i , $W_{ij,\text{el}}^{\text{beam}}$ is a fixed beamwidth in elevation, P_t is the V2V transmit power, W is the V2V bandwidth, λ is the wavelength at the V2V carrier frequency, and N_0 is the noise power spectral density.

III. V2V LINK ESTABLISHMENT APPROACHES

In this section, we propose two methods to determine $(\theta_{ij}^{\text{beam}}, W_{ij}^{\text{beam}})$ based on location information: one based only on the communicated GPS data, and the second one based on the radar data.

A. GPS-aided Communication

In the frame of reference of vehicle i , the location of vehicle j is $\mathbf{x}_j^i = \mathbf{R}(-\phi_i)(\mathbf{x}_j - \mathbf{x}_i)$. We thus find that

$$\theta_{ij} = \arcsin \frac{[-\sin \phi_i \cos \phi_i]^T (\mathbf{x}_j - \mathbf{x}_i)}{\|\mathbf{x}_j - \mathbf{x}_i\|}. \quad (3)$$

In order to compute the distribution of θ_{ij} , we use a particle approach. We first generate samples $[\mathbf{s}_i^{(p)} \mathbf{s}_j^{(p)}]_{p=1}^{N_p} \sim p(\mathbf{s}_i)p(\mathbf{s}_j)$ and then evaluate $\theta_{ij}^{(p)}$ by computing (3) for each particle. Then, $\theta_{ij}^{\text{beam}} = \mathbb{E}\{\theta_{ij}\} \approx 1/N_p \sum_{p=1}^{N_p} \theta_{ij}^{(p)}$ and $W_{ij}^{\text{beam}} = \alpha \sqrt{1/N_p \sum_{p=1}^{N_p} (\theta_{ij}^{(p)})^2 - (\theta_{ij}^{\text{beam}})^2}$, where $\alpha > 1$ is a constant to ensure that the beam covers the intended receiver.

B. Radar-aided Communication

The proposed process involves three steps: (i) determining the distribution of $\mathbf{g}_{i,k}$ based on the radar measurements and vehicle i 's GPS information; (ii) associating the vehicles to the objects, and (iii) computing the optimal beams.

Remark (On the use of velocity information). Since vehicle i only has access to radial velocity measurements of the detected object, the distribution of $\mathbf{g}_{i,k}$ will have unbounded uncertainty in the velocity component. This is due to the lack of knowledge of the object's tangential velocity component. For that reason, we will drop the velocity from now on. The use of velocity information is possible when we consider explicit cooperation between multiple vehicles, as then the tangential component is also available and radial velocities between two mutually observable vehicles are identical. Such cooperation is out of the scope of the current work.

1) *Coordinate Transformation*: Our focus is on object k , detected by vehicle i . We first transform the object into Cartesian coordinates. If we denote the radial and AoA variances from $\mathbf{S}_{i,k}^{\text{polar}}$ by $\sigma_{r,i}^2$ and $\sigma_{b,i}^2$, respectively, then the object location in Cartesian coordinates $\mathbf{o}_{i,k} = [x_{i,k}^i, y_{i,k}^i]^\top$, in the vehicle frame of reference is $p(\mathbf{o}_{i,k}|\mathbf{s}_i) = \mathcal{N}(\mathbf{o}_{i,k}; \bar{\mathbf{o}}_{i,k}, \mathbf{S}_{i,k})$, where $\bar{\mathbf{o}}_{i,k} = [\bar{x}_{i,k}^i, \bar{y}_{i,k}^i]^\top$, in which

$$\bar{x}_{i,k}^i = \bar{r}_{i,k} \cos \theta_{i,k} \quad (4)$$

$$\bar{y}_{i,k}^i = \bar{r}_{i,k} \sin \theta_{i,k} \quad (5)$$

$$\mathbf{S}_{i,k} = \mathbf{R}^\top(\theta_{i,k}) \text{diag}([\sigma_{r,i}^2, \bar{r}_{i,k}^2 \sigma_{b,i}^2]) \mathbf{R}(\theta_{i,k}). \quad (6)$$

These relations follow from geometry. Then $\mathbf{g}_{ik} = \mathbf{R}(\phi_i) \mathbf{o}_{i,k} + \mathbf{x}_i$, where all variables are random. The distribution of \mathbf{g}_{ik} can be approximated as $\mathbf{g}_{ik} \sim \mathcal{N}(\mathbf{g}_{i,k}; \bar{\mathbf{g}}_{i,k}, \mathbf{\Gamma}_{i,k})$, where $\bar{\mathbf{g}}_{i,k} = \mathbf{R}(\bar{\phi}_i) \bar{\mathbf{o}}_{i,k} + \bar{\mathbf{x}}_{i,k}$ and

$$\mathbf{\Gamma}_{i,k} = \mathbf{F}_{i,k} \begin{bmatrix} \mathbf{S}_i & 0 \\ 0 & \mathbf{S}_{i,k} \end{bmatrix} \mathbf{F}_{i,k}^\top, \quad (7)$$

in which $\mathbf{F}_{i,k}$ is the Jacobian. Since $\nabla_{\phi_i} \mathbf{g}_{ik} = \mathbf{R}(-\phi_i) \mathbf{o}_{i,k}$, $\nabla_{\mathbf{x}_i} \mathbf{g}_{ik} = \mathbf{I}_2$ and $\nabla_{\mathbf{o}_{i,k}} \mathbf{g}_{ik} = \mathbf{R}(\phi_i)$,

$$\mathbf{F}_{i,k} = \begin{bmatrix} \mathbf{I}_2 & \mathbf{R}(-\bar{\phi}_i) \bar{\mathbf{o}}_{i,k} & \mathbf{R}(\bar{\phi}_i) \end{bmatrix}. \quad (8)$$

2) *Data Association*: We now associate the objects k detected by vehicle i , transformed in the global coordinate system with the GPS data from the other vehicles j . In order to perform such an association, we need a similarity measure $D_{jk} \geq 0$ between object k (detected by vehicle i) and vehicle $j \in \mathcal{N}_i$. These have densities $p(\mathbf{g}_{i,k})$ and $p(\mathbf{s}_j)$, respectively. Recall that object also have a corresponding existence probability $\rho_{i,k}$. We propose to use the Kullback-Leibler divergence (KLD), elaborated in the Appendix. Using this metric, we formulate an optimal assignment¹ problem

$$\min_{\mathbf{X}} \sum_{j \in \mathcal{N}_i} \sum_{k=1}^{N_i} x_{jk} D_{jk} \quad (9a)$$

$$\text{s.t. } x_{jk} \in \{0, 1\} \quad (9b)$$

$$\sum_{j \in \mathcal{N}_i} x_{jk} \leq 1, \forall k \quad (9c)$$

$$\sum_{k=1}^{N_i} x_{jk} = 1, \forall j. \quad (9d)$$

¹Alternatively, soft data associations can be considered [25].

Table I
DEFAULT SIMULATION PARAMETERS.

Parameter	Value
V2V bandwidth (W)	100 MHz
Carrier frequency (f_c)	28 GHz
V2V transmit power	0.1 mW
Thermal noise temperature T_0	290 K
Receiver's noise figure	1
Range standard dev. σ_r	0.3 m
Bearing standard dev. σ_b	0.5°
GPS heading standard dev. σ_ϕ	0.57°
Number of particles N_p	500
Beamwidth parameter α	4
Number of objects N_i	20
Number of vehicles	20
Object existence prob. ρ	1.0

After solving the data association problem with the Kuhn-Munkres algorithm [26], we have determined $k^*(j)$, i.e., the best matching object to vehicle j .

3) *Optimal Beams*: The optimal beams are then easily found as

$$\theta_{ij}^{\text{beam}} = \arcsin \left(\frac{[\bar{\mathbf{o}}_{i,k^*(j)}]_2}{\|\bar{\mathbf{o}}_{i,k^*(j)}\|^2} \right) \quad (10)$$

$$W_{ij}^{\text{beam}} = \alpha \sqrt{\mathbf{f}_{i,k,j}^\top \mathbf{S}_{i,k^*(j)} \mathbf{f}_{i,k,j}} \quad (11)$$

in which $\mathbf{f}_{i,k,j}$ is again a Jacobian, $\mathbf{f}_{i,k,j} = \nabla_{\mathbf{o}_{i,k^*(j)}} \theta_{ij}$, so that

$$\mathbf{f}_{i,k,j}^\top \mathbf{S}_{i,k^*(j)} \mathbf{f}_{i,k,j} = \frac{1}{\|\bar{\mathbf{o}}_{i,k^*(j)}\|^2} \mathbf{e}_{i,k,j}^\top \mathbf{S}_{i,k^*(j)} \mathbf{e}_{i,k,j}, \quad (12)$$

where $\mathbf{e}_{i,k,j}$ is a unit length vector, orthogonal to $\bar{\mathbf{o}}_{i,k^*(j)}$.

IV. RESULTS

A. Simulation Setting

We consider an environment of size 50 m by 50 m in front of the ego vehicle. A total of 100 Monte Carlo simulations are run to obtain the results with the parameters summarized in Table I.

B. Discussion

We first evaluate the impact of GPS uncertainty. We set $[\mathbf{S}_i]_{1:2,1:2} = \sigma_{\text{GPS}}^2 \mathbf{I}_2$ and vary the value of σ_{GPS} . The result in terms of average SNR (averaged over all links and over all Monte Carlo simulations) and average beamwidth are shown in Fig. 2. We compare three approaches: the GPS-aided method from Section III-A, the radar-aided method from Section III-B, with and without perfect data association. We observe that for low GPS variance, we achieve high average SNR, due to low beamwidth. With increasing GPS errors, beamwidth necessarily becomes larger, leading to SNR penalties. The radar-aided approach with perfect data association (DA) is not affected by the GPS variance, as it depends only on the radar performance, leading to high average SNR. Finally, with data association according to (9), high SNR is only achievable for low GPS variance. This is because in that case the objects, when transformed to global coordinates, remain well separated, leading to easy data association. When the

GPS errors increase, data association errors occur (see below). These errors have limited impact on the beamwidth (since even under incorrect data association, beams can be narrow), but severely degrades the SNR. A drop of about 10 dB in average SNR is observed. We have also explored alternative distance metrics to the KLD, including Euclidean distance and Riemannian distance, but observed little performance difference.

The performance difference is explained in Fig. 3, showing the data association performance as a function of σ_{GPS} . After about 1 meter standard deviation, about 10 % of the associations are incorrect. After about 10 meter standard deviation, all the associations are incorrect. Hence, the selected beams will be narrow but point towards an incorrect directions. Fig. 3 also includes an investigation of KLD performance for object existence probabilities ($\rho_{i,k}$) of 0.5, whereas the vehicle existence probabilities are 1. Although the data association error decreases marginally for lower object existence probabilities, the effect on beamwidth and SNR turns out to be negligible.

Finally, Fig. 4 shows the impact of the beamwidth parameter α on the average SNR and beamwidth. Unsurprisingly, larger α leads to broader beams, with the GPS-aided beams being about one order of magnitude wider than the radar-aided beams. The performance of the data association has no impact on the average beamwidth in this case. On the other hand, we see interesting behavior in the SNR: the GPS-aided approach generates too narrow beams for $\alpha < 2$, leading to zero SNR. For increasing α , beams cover the intended receiver, but SNR degrades as beams become wider. For the radar-aided approach, too small α leads to low SNR as the beams are unable to hit most of the intended receivers. Around $\alpha = 2$ leads to optimal performance, with beams narrow enough to have high gains, but wide enough to illuminate the intended receiver. Increasing α beyond 2 leads to SNR reductions.

We have also investigated the performance sensitivity to the number of objects and the number of vehicles and found that the performance is reduced with increased number of vehicles.

V. CONCLUSIONS

We have proposed a method for radar-aided communication, which leverages the high accuracy of radar detections to form narrow beams towards intended receivers. To associate radar detections with receivers, we rely on GPS information from those receivers, communicated via an out-of-band technology. The method shows good performance when GPS errors are not too large. Possible extensions include more realistic models for radar performance, as well as extended object models; extending the model with velocities (to improve the data association) but this needs higher-level cooperation; consider soft data association (e.g., using belief propagation).

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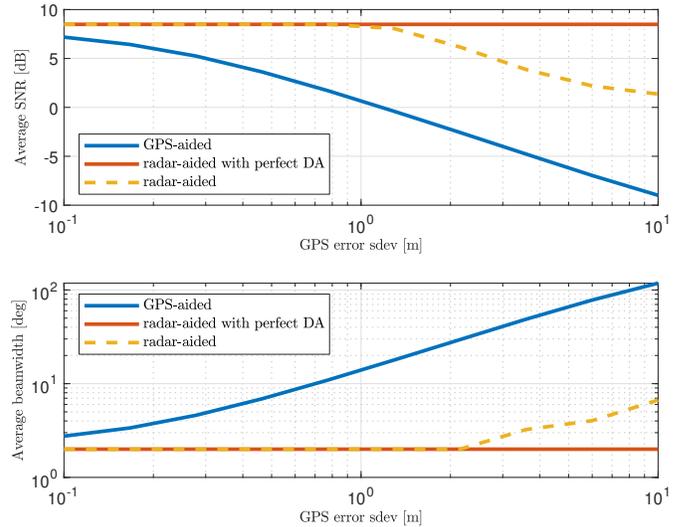


Figure 2. Performance comparison of GPS-aided and radar-aided V2V communication in terms of average SNR and average beamwidth, as a function of GPS standard deviation.

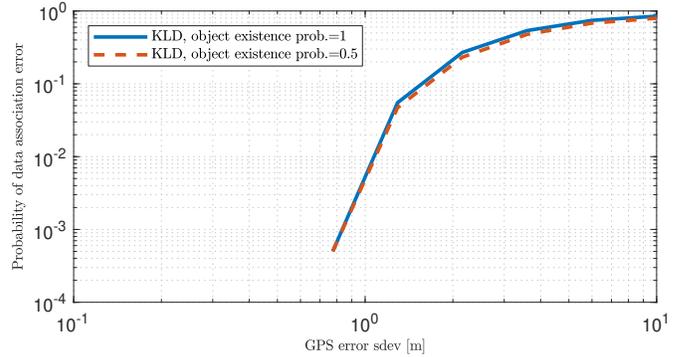


Figure 3. Probability of data association error for the scenario with 20 vehicles and 20 objects for changing GPS error standard deviation.

APPENDIX SIMILARITY MEASURE

Given two Bernoulli set densities $f(\mathcal{X})$ and $g(\mathcal{Y})$, with existence probabilities ρ_f and ρ_g and spatial Gaussian densities $p_f(\mathbf{x}) = \mathcal{N}(\mathbf{x}; \boldsymbol{\mu}_f, \boldsymbol{\sigma}_f)$ and $p_g(\mathbf{y}) = \mathcal{N}(\mathbf{y}; \boldsymbol{\mu}_g, \boldsymbol{\sigma}_g)$. The KLD is then defined as

$$D(f||g) = \int f(\mathcal{X}) \log \frac{f(\mathcal{X})}{g(\mathcal{X})} \delta \mathcal{X} \quad (13)$$

$$= f(\emptyset) \log \frac{f(\emptyset)}{g(\emptyset)} + \int f(\{\mathbf{x}\}) \log \frac{f(\{\mathbf{x}\})}{g(\{\mathbf{x}\})} d\mathbf{x} \quad (14)$$

$$= D(\rho_f||\rho_g) + \rho_f D(p_f||p_g). \quad (15)$$

where $D(\rho_f||\rho_g)$ is the KLD between two Bernoulli distributions, i.e.,

$$D(\rho_f||\rho_g) = (1 - \rho_f) \log \frac{(1 - \rho_f)}{(1 - \rho_g)} + \rho_f \log \frac{\rho_f}{\rho_g}, \quad (16)$$

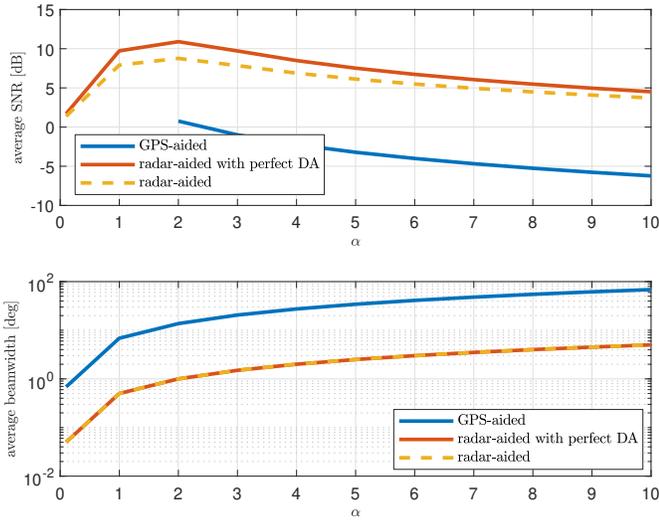


Figure 4. Performance comparison of GPS-aided and radar-aided V2V communication in terms of average SNR and average beamwidth, as a function of the beamwidth parameter α .

and $D(p_f \| p_g)$ is the conventional KLD between two Gaussian densities, i.e.,

$$D(p_f \| p_g) = \frac{1}{2} \text{tr}(\Sigma_g^{-1} \Sigma_f) + \frac{1}{2} \log \left(\frac{\det \Sigma_g}{\det \Sigma_f} \right) + \frac{1}{2} \Delta^T \Sigma_g^{-1} \Delta - \dim/2. \quad (17)$$

where $\Delta = \mu_g - \mu_f$ and \dim is the dimension of the random variable.

In case one of the variables is not a set, we can simply set the corresponding existence probability to 1.

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