¹ A joint model for stated choice and best-worst scaling data using

² latent attribute importance: application to rail-air intermodality

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8 ABSTRACT

This paper looks at modelling choices in the presence of a new mode of transport, 9 where there is need to understand the sensitivities to a number of new attributes. 10 Stated choice (SC) data and two types of Best-worst scaling (BWS) data (i.e. case 1 11 and case 2) are collected from the same respondents. We mix survey methods rather 12 than using a longer SC survey to better understand choice behaviour whilst reducing 13 the boredom caused by one very long set of SC choices. Although BWS data has been 14 increasingly collected alongside stated choice (SC) data, little is known about the 15 relationships between BWS responses and SC responses at the level of individual 16 respondents. Also, little effort has been made to jointly exploit the behavioural 17 information from BWS data and SC data to improve the understanding of choices. 18 This paper proposes a joint model which links the BWS and SC data through 19 the notion of latent attribute importance. The modelling results show that people 20 21 perceive attribute importance in a relatively consistent way across different survey methods, i.e. a person who perceives higher importance from an attribute is likely to 22 show stronger sensitivity to that attribute in SC tasks, give more weight to the same 23 attribute in BWS1 tasks and exhibit a wider gaps in terms of attractiveness between 24 25 levels for the same attribute - in comparison with other individuals. This consistency shows that the additional behavioural information can be gained by using a joint 26 model estimated on BWS1 and BWS2 data alongside more traditional SC data, 27 28 helping us to improve the explanation of the choices and the role of the attributes. Our results however do not find a one-to-one relationship between different survey 29 methods and analysts thus need to be mindful that there remain some differences 30 in how attributes are evaluated between SC, BWS1 and BWS2 surveys. 31

32 KEYWORDS

- 33 Stated choice, Best-worst scaling, Attribute importance, MaxDiff model,
- 34 Integrated Choice and Latent Variable model

1 1. Introduction

Many new travel modes have emerged in recent years. Studies aimed at understand-2 ing individuals' choice behaviour and the travel demand for novel alternatives have 3 predominantly relied on stated-choice (SC) data, where a respondent chooses his/her most preferred alternative in each hypothetical scenario. A new travel mode is usually 5 characterised with some new attributes which individuals are not familiar with. There-6 fore, a key role of the surveys is to gain more information on how these new attributes are valued by respondents. These attributes are often not continuous in nature and 8 the reliable estimation of their impact can thus require substantial amounts of data. 9 However, increasing the number of tasks of a SC survey might lead to respondents 10 feeling greater boredom to process a repeated same type of choice tasks. Thus, it can 11 be useful to gain additional behavioural information through other types of prefer-12 ence elicitation methods to help us better understand how people make choices in the 13 context of new modes and the role that these new attributes play. This combination 14 of data sources can be helpful to improve the robustness of policy recommendations. 15 This can especially be the case when the number of tasks that can be used in an SC 16 experiment is limited due to the increasing boredom brought on by a longer set of re-17 peated SC tasks. Moreover, respondents may experience fatigue in a SC survey where 18 many attributes are presented all at the same time (Pullman, Dodson, and Moore 19 1999; Carlsson 2003; Collins, Bliemer, and Rose 2014). 20

Recently, a limited number of travel behaviour studies have adopted best-worst 21 scaling (BWS) approaches as alternative preference elicitation methods (e.g. Dumont, 22 Giergiczny, and Hess 2015; Hensher, Mulley, and Rose 2015; Beck and Rose 2016; 23 Beck, Rose, and Greaves 2017). The BWS approaches originate in marketing and the 24 majority of its applications can be found in the marketing and health literature. In 25 BWS, respondents are asked to in each task select the best and the worst option. Dif-26 ferent formats of this exist. BWS Case 1 surveys ask respondents to identify, in each 27 choice screen, the most and the least important attribute per se without a focus on the 28 actual levels (e.g. Finn and Louviere 1992; Auger, Devinney, and Louviere 2007; Marti 29 2012). BWS Case 2 surveys ask respondents to identify the most and the least im-30 portant attribute level (e.g. Coast et al. 2006; Dyachenko, Reczek, and Allenby 2014). 31 While BWS Case 1 measures the relative weight of attributes, BWS Case 2 measures 32 the relative attractiveness of attribute levels across different attributes.¹ Like SC sur-33 veys, BWS Case 3 surveys also look at comparisons amongst different alternatives, 34 each described by a combination of attribute levels; but BWS Case 3 surveys require 35 respondents to identify both the most and the least preferred alternative in each choice 36

¹In this presented paper, we use *weight* to describe the influence of an attribute in decision making in BWS Case 1 tasks and use *attractiveness* to describe the influence of an attribute level in decision making in BWS Case 2 tasks. Greater *weight* of an attribute or *attractiveness* of an attribute level means higher probability of this attribute or attribute level being chosen as the best and lower probability of it being chosen as the worst.

occasion. Comparisons between SC and BWS case 3 data can be found in the work of
Giergiczny et al. (2017) and Petrolia, Interis, and Hwang (2018).

This research is conducted in the context where a new travel mode, i.e. high-speed 3 rail(HSR)-air intermodality, is introduced. Since our interest is in predicting choices 4 (i.e. first preferences only), we adopt a traditional SC survey as it allows us to analyse 5 how respondents make trade-offs between attributes and forecast travel demand within 6 multi-alternative settings. A BWS Case 3 survey is not adopted for this purpose as it 7 combines both the best and the worst where existing studies show diverging views on 8 how consistent people are in choosing the best and the worst. Some found differences in 9 both utility parameters and scales between the two stages (Rose 2014; Giergiczny et al. 10 2017), notwithstanding contrary findings in Hawkins, Islam, and Marley (2018) that 11 suggested that the same utility parameters drive individuals' best and worst choices 12 despite a scale difference between best choices and worst choices. In addition to the 13 SC survey, BWS Case 1 and BWS Case 2 surveys are used as these two methods can 14 reflect how individuals are influenced by different attributes in relatively more direct 15 manners in single-alternative settings. As such, BWS Case 1 and BWS Case 2 data 16 serves as additional behavioural information to help in better explaining the role of 17 specific attributes in these choice decisions.² 18

This paper aims at exploring approaches to synthesise SC, BWS Case 1 and Case 2 19 data within a same modelling framework to understand their relationships at the level 20 of individual respondents and to improve the explanation of choices with the help of 21 the supplementary information obtained from BWS Case 1 and Case 2 data. A key 22 question in achieving this target, which has not been addressed in the literature, is 23 whether the extent to which respondents weight attributes in a BWS Case 1 survey 24 and rank attribute levels in a BWS Case 2 survey is consistent with how those same 25 attributes and levels influence the choices in a SC survey. A higher level of corre-26 spondence between the different data sources would imply greater exploitation of the 27 auxiliary BWS Case 1 and Case 2 data in enhancing the explanation of stated choices 28 and building a more robust evidence base for policy recommendations. 29

The majority of studies comparing SC data and BWS Case 1 and (or) Case 2 data 30 have been conducted at the sample level (e.g. Louviere and Islam 2008; Potoglou 31 et al. 2011). Only Balbontin, Ortúzar, and Swait (2015) and Beck, Rose, and Greaves 32 (2017) have jointly analysed SC and BWS Case 2 data. However, there are some 33 remaining limitations associated with these two joint estimation studies. The former 34 lacks flexibility in model specifications as it assumes the impact of an attribute level 35 in the SC tasks to be equal (or a function of) to the impact of the same attribute 36 level revealed in the BWS Case 2 data. The latter directly incorporates the average 37

 $^{^2}$ BWS approaches outweigh rating or ranking methods as BWS can take advantage of respondents' tendency of responding more consistently and accurately to extreme options on an underlying scale from a relatively small choice set(Marley and Louviere 2005). Thus conventional rating or ranking tasks are not used to help explain choices in our study.

impact over different attribute levels from BWS Case 2 data to help explain choices in
SC data and thereby exposes itself to potential endogeneity biases. Meanwhile, joint
analyses of SC data with BWS Case 1 data have not yet been explored.³

In this paper, we put forward a flexible approach to jointly estimate SC, BWS Case 1 and BWS Case 2 data at the individual level while overcoming the shortcomings in 5 the literature. This approach is based on the assumption that responses to BWS Case 6 1, BWS Case 2 and SC tasks are all driven by a common underlying factor of perceived 7 attribute importance. We develop an Integrated Choice and Latent Variable (ICLV) 8 model (Ben-Akiva et al. 2002) where each attribute is associated with a specific latent 9 variable of *attribute importance*. The notion of *attribute importance* has previously 10 been put forward to challenge the decision heuristic of attribute non-attendance (Hen-11 sher, Rose, and Greene 2005; Hensher 2006; Hensher and Rose 2009), arguing that 12 some people actually perceive reduced importance for an attribute in making stated 13 choices rather than completely ignoring it even if the respondents stated that they 14 did not take the associated attribute into account (Hess and Hensher 2010; Camp-15 bell, Hensher, and Scarpa 2011; Hess et al. 2013). Our work adopts a similar strategy 16 as Hess and Hensher (2013), who use latent attribute importance to simultaneously 17 explain the responses to SC tasks and the responses to selected indicators, including 18 binary stated attribute attendance and stated attribute rankings. In our proposed 19 model, the indicators are replaced by BWS Case 1 and Case 2 data. 20

We apply the proposed model in the context of a new HSR-air intermodal service 21 in China. This new service facilitates people's long-distance travel by allowing passen-22 gers to jointly take HSR trains and flights to make a journey without the hassle of 23 purchasing train tickets and flights separately. As expected, we find a certain degree 24 of correspondence among the behaviour in the stated choice scenarios, BWS Case 1 25 exercises and BWS Case 2 exercises. That is, for a given attribute, people who perceive 26 stronger importance of an attribute derive higher marginal utility from that attribute 27 in SC tasks, attach higher weight to that attribute in BWS1 tasks, and are more 28 sensitive to changes in level values of that attribute in BWS2 tasks - in comparison 29 with other people. This correlation suggests that the supplementary BWS1 and BWS2 30 tasks can indeed bring about desired additional information and help better explain 31 the role of attributes. There is, however, not a one-to-one relationship between the 32 different survey methods. This implies that researchers, while being keen to explore 33 the additional insights provided by BWS data, should not treat SC and BWS survey 34 methods as equivalent and interchangeable. 35

The remainder of this paper is organised as follows. Section 2 explains the methodology of the joint model. The survey design and the data is described in section 3. The

 $^{^{3}}$ BWS Case 1 and SC data is often collected at different moments of the survey design and collection process. Outcomes of the former are for example regularly used to determine which attributes from a larger pool of attributes need to be included in the SC experiment.

¹ case study is analysed in section 4, which is followed by a conclusion section.

² 2. Methodology

In this section, we look at the individual components of our model framework before
discussing estimation results. For the sake of brevity, we use "BWS1" and "BWS2" to

- ⁵ represent "BWS Case 1" and "BWS Case 2" respectively.

6 2.1. Model framework

As mentioned in the Introduction, our model is developed based on the assumption of correlation between SC responses and BWS1/2 responses. Latent variables are introduced to capture the correlation and to simultaneously explain different types of responses within a single ICLV framework. We follow the adoption of the notion *attribute importance* from Hess and Hensher (2013) to represent latent variables for each attribute as SC, BWS1 and BWS2 surveys all reveal people's preferences towards various attributes in the decision-making process.⁴

Fig. 1 illustrates our joint modelling framework, where items in rectangulars are 14 observable to researchers while items in ellipses are unobserved. Brief descriptors of 15 each notation used in section 2, including those appeared in Fig. 1, are shown in the 16 Appendix. The model has three components, explaining the SC responses y, BWS1 17 responses $(b, w)_{|1}$ and BWS2 responses $(b, w)_{|2}$ respectively. The latter two form the 18 measurement model components. All three components are influenced and connected 19 by the attribute-specific latent variable of *attribute importance*. As such, we do not im-20 pose restrictions on how an attribute (or attribute level) is evaluated between BWS1/221 data and SC data as in the work by Balbontin, Ortúzar, and Swait (2015). We also 22 do not directly feed the BWS1 and BWS2 responses as explanatory variables into the 23 choice model component as Beck, Rose, and Greaves (2017) did. Thereby, the pro-24 posed model has greater flexibility in recovering the correlations between BWS and 25 SC responses, and data collected through different methods can be synthesised without 26 the risk of introducing endogeneity bias or measurement error. 27

More precisely, the attribute-specific latent variables of *attribute importance* are used as explanatory variables for each elicitation procedure. For each specific attribute, we assume that the corresponding *attribute importance* scales the marginal utility of that attribute in the SC component, hence influencing the utilities of alternatives in the utility functions which are also affected by some socioeconomic characteristics. Meanwhile, the latent *attribute importance* also determines the same attribute's weight

⁴Please refer to the definition of *weight* and *attractiveness* in footnote 1. It also needs to be noted that our definition of *attribute importance* is not equivalent to the *importance* defined by Marley, Flynn, and Louviere (2008), and we do not have the same identifiability problem as discussed in that paper as we are not trying to separate the impact of an attribute and a specific level on that attribute in BWS2 tasks.

in the BWS1 component as well as the attractiveness of attribute levels of the same
attribute in the BWS2 component. Different coefficients are specified to capture the
different impact of a same latent attribute importance in different methods. In what
follows, we discuss how each component is constructed and the role of latent attribute *importance* in detail.



Figure 1.: Framework of the joint model.

6 2.2. Structural equations for latent variables

⁷ We denote the attribute-specific latent variables of *attribute importance*, as perceived ⁸ by respondent *n*, by the vector $\alpha_n = (\alpha_{n1}, \ldots, \alpha_{nK})'$, where *K* describes the total ⁹ number of attributes. Selected socio-demographic characteristics Z_n are used to explain ¹⁰ the latent variables in the structural equations:

$$\alpha_{nk} = \omega'_k Z_n + \eta_{nk}, \quad (k = (1, \cdots, K)), \tag{1}$$

¹¹ where η_{nk} is a standard Normal error term and where the estimated vector of param-¹² eters ω_k measures the impact of the socio-demographic characteristics on the latent ¹³ variable. Note that Z_n is centred on 0, such that the latent variable α_{nk} has a mean ¹⁴ of 0.

15 2.3. Stated choice model component

The model is constructed under the Random Utility Maximisation (RUM) theory, where it is presumed that a decision-maker can derive some utility from choosing a particular alternative and that the probability of choosing an alternative increases with its utility.

Let U_{int} in Eq. 2 represent the utility of alternative *i* for respondent *n* in stated

¹ choice task t. U_{int} consists of a deterministic portion V_{int} (i.e. systematic utility), and ² an unobserved error term ε_{int} which is independently and identically distributed (IID)

³ extreme value type I.

$$U_{int} = V_{int} + \varepsilon_{int} = \delta_i + \beta'_n x_{int} + \varepsilon_{int}.$$
 (2)

⁴ The term δ_i is an estimated alternative-specific constant (ASC) while $x_{int} = (x_{int1}, \cdots, x_{intK})'$ is a vector of explanatory variables representing the K attributes ⁶ of alternative *i* as shown to respondent *n* in SC task *t*, where the estimated vector ⁷ $\beta_n = (\beta_{n1}, \cdots, \beta_{nK})'$ captures the marginal utilities of these attributes. Hence, it is ⁸ assumed that each attribute contributes to the utility of an alternative in an addi-⁹ tive manner, and that the marginal utility for each attribute is kept generic across ¹⁰ alternatives.

¹¹ Marginal utility varies across respondents due to the role of the latent *attribute* ¹² *importance*, as well as additional observed and unobserved preference heterogeneity ¹³ that is independent of the latent variable. For an attribute where we assume a positive ¹⁴ marginal utility, we specify β_{nk} such that:

$$\beta_{nk} = e^{\tau_k \alpha_{nk}} \cdot e^{\kappa_k Z_n} \cdot e^{\mu_{\ln \beta_k} + \sigma_{\ln \beta_k} \cdot \xi_{nk}},\tag{3}$$

where, for an attribute with an expected negative marginal utility, we instead work
with the negative exponential such that:

$$\beta_{nk} = -e^{\tau_k \alpha_{nk}} \cdot e^{\kappa_k Z_n} \cdot e^{\mu_{\ln(-\beta_k)} + \sigma_{\ln(-\beta_k)} \cdot \xi_{nk}}.$$
(4)

Latent attribute importance is accommodated in an exponential form to act as 17 a positive scalar on marginal utility where τ_k captures the degree of scaling (Hess 18 and Hensher 2013). To avoid overstating the role of latent attribute importance in 19 explaining heterogeneity in the SC data (Vij and Walker 2016), we let the socio-20 demographics Z_n which explain the latent variable α_{nk} in the structural equations also 21 directly enter the marginal utility, where the vector κ_k measures the direct impacts 22 from socio-demographics Z_n on the scaling of marginal utility. Additional random 23 heterogeneity that is not linked to the latent variable is accommodated by specifying 24 the underlying parameter, net of the influence of socio-demographics and the latent 25 variable, to follow a Lognormal distribution. We then have that $\mu_{\ln\beta_k}$ and $\sigma_{\ln\beta_k}$ (or 26 $\mu_{\ln(-\beta_k)}$ and $\sigma_{\ln(-\beta_k)}$ if we work with a negative exponential) denote the mean and 27 standard deviation of the underlying Normal distribution, where ξ_{nk} follows a standard 28 Normal distribution across respondents for attribute k. It can be observed that as 29

- $e^{\tau_k \alpha_{nk}}$ itself follows a Lognormal distribution, β_{nk} does too as it is formed by a product of Lognormals.
- The probability of alternative s being chosen out of I alternatives by respondent nin SC task t is then written as:

$$P(y_{nt} = s) = \frac{e^{\delta_s + \sum_{k=1}^{K} \beta_{nk} x_{sntk}}}{\sum_{i=1}^{I} e^{\delta_i + \sum_{k=1}^{K} \beta_{nk} x_{intk}}},$$
(5)

⁵ where this is dependent on a specific realisation of the vector of random coefficients.

6 2.4. Measurement model components

In explaining BWS1 and BWS2 data, we develop models based on the MaxDiff model 7 (Marley and Louviere 2005; Marley, Flynn, and Louviere 2008), attempting to explain 8 the choice for the observed pair of best and worst attributes $(b, w)_{|1}$, and attribute 9 levels $(b, w)_{|2}$, respectively. MaxDiff models explain the choice of the combination of 10 attributes or attribute levels with the largest difference in "utility" between them. In 11 the remainder of this paper, we use "utility" to refer to the weight of an attribute 12 in the BWS1 component and the attractiveness of an attribute level in the BWS2 13 component, for the sake of brevity.⁵ 14

Let $B_{qnm|c}$ denote the "utility" of q for respondent n as shown in BWS task m and BWS type c, where c = 1 stands for BWS1 and c = 2 for BWS2. We thus define:

$$BW_{(q,j)nm|c} = B_{qnm|c} + W_{jnm|c} + \nu_{qjnm|c},\tag{6}$$

where $B_{qnm|c}$ and $W_{jnm|c}$ give the "utility" of the two attributes or attribute levels that would be used to create the combination (q, j) while $\nu_{qjnm|c}$ denotes a standard extreme value type I error term operating at the level of the attribute (level) pairs allowing us to operate within the Multinomial Logit (MNL) framework when deriving the probability of a given pair being the one with the largest difference in "utility". Rather than simply assuming symmetry between the "utilities" for the best and the worst levels, we set:

$$W_{jnm|c} = -\lambda_{j|c} B_{jnm|c},\tag{7}$$

thus accounting for scale difference between the "best" and the "worst" stage and allowing this difference to be attribute-specific, while still assuming that the driving factors of making an attribute (level) important/attractive or unimportant/unattractive are the same across the two stages. Hence this specification is different from the original

 $^{^{5}}$ The quoted term "utility" is used for precision as *utility* by definition can only be derived from an alternative (McFadden et al. 1973; McFadden 2001), rather than from a single attribute or attribute level.

¹ MaxDiff model proposed by (Marley and Louviere 2005; Marley, Flynn, and Louviere ² 2008), where scale parameters were not included (i.e. $\lambda_{j|c} = 1$). We thereby refer to ³ our models for the BWS1/2 data as *MaxDiff models with scale difference*.

Due to the experimental design, the choice set varies over respondents and tasks, and this thus affects what is possible for a respondent to select as the combination 5 of best and worst attributes or attribute levels in a given scenario. We use $\mathbb{D}_{nm|c}$ to 6 define the set containing all the available items presented to respondent n in BWS 7 task m and type of BWS data c. The items in $\mathbb{D}_{nm|c}$ allow the formation of the set 8 $\mathbb{S}_{nm|c}$ containing all the possible best-worst pairs of the available attributes or attribute levels, respectively. Similar to other MNL models with a RUM assumption, the best-10 worst choice probabilities of respondent n selecting h as the best and r as the worst 11 $(h, r \in \mathbb{D}_{nm|c}, r \neq h, (h, r) \in \mathbb{S}_{nm|c})$ in BWS task m can then be written as: 12

$$P\left((b,w)_{nm|c} = (h,r)\right) = \frac{e^{B_{hnm|c} + W_{rnm|c}}}{\sum_{(q,j) \in \mathbb{S}_{nm|c}} \left(e^{B_{qnm|c} + W_{jnm|c}}\right)},\tag{8}$$

¹³ making use of the appropriate combinations of Eqs. 9 - 11 discussed in what follows.

14 2.4.1. BWS1 data

In the BWS1 setting, we work with attributes rather than attribute levels. The "utility" function is specified to represent the weight placed on an attribute k by respondent n in task m in decision-making. Thus we have a single "utility" for a given attribute k to be "best" attribute, which is given by:⁶

$$B_{knm|1} = \delta_{k|1} + \zeta_{k|1}\alpha_{nk},\tag{9}$$

where this is generic across BWS1 tasks as the attribute levels are not used. In Eq. 9, we have a constant $\delta_{k|1}$ and a sensitivity $\zeta_{k|1}$ with respect to the latent variable, where these two parameters are to be estimated. Since α_{nk} is centred on 0, $\delta_{k|1}$ captures the mean weight of attribute k in the BWS1 data, while $\zeta_{k|1}$ captures the variation in the weight of the attribute in the sample due to latent attribute importance. Respondents who perceive a higher importance to an attribute are expected to care more about that attribute in the BWS1 data.

²⁶ For normalisation purpose, one attribute in the MaxDiff model with scale difference

⁶In an ICLV model, it is common practice to use the latent variable solely to capture heterogeneity in the measurement component, and only a limited number of studies have also directly included additional randomness irrelevant from the latent variable in the measurement model. We have tried to estimate models with such direct random component in the measurement model for the BWS1 data. However, log-likelihood ratio test suggests accounting for such randomness cannot bring about significant improvement in fit or help better explain choices in our case. The interpretation of the estimation results are nevertheless quite similar to the old model, indicating that our findings about the correlation among different survey methods are relatively consistent across different model specifications. This also applies to the specification for BWS2 data in Eqs. 10 and 11.

for BWS1 data needs to be selected as the base by fixing the associated parameters
to 0.

3 2.4.2. BWS2 data

⁴ In the BWS2 data, we work with multiple levels across attributes. The BWS2 "utility" ⁵ function describes the attractiveness of an attribute level (or value) k perceived by ⁶ respondent n in task m. The specification for a given attribute level k now depends ⁷ on whether this attribute is treated as continuous or categorical. We explicitly here ⁸ do not allow for scenarios in which multiple values for the same attribute are shown ⁹ on one screen, i.e. only allowing for screens where each element is from a different ¹⁰ attribute.

Let us define $x_{knm|2}$ to be the value of continuous variable k as shown in BWS2 task m for respondent n. We then define $B_{knm|2}$ to be equal to:

$$B_{knm|2} = \delta_{k|2} + \gamma_{k|2} \cdot e^{\zeta_{k|2}\alpha_{nk}} x_{knm|2}.$$
 (10)

¹³ Here, we assume that the attractiveness of a level depends in a linear fashion on the ¹⁴ actually presented value $x_{knm|2}$, $\delta_{k|2}$ captures the constant associated with attribute k¹⁵ and $\gamma_{k|2}$ captures the baseline marginal attractiveness of the attribute level on $B_{qnm|2}$. ¹⁶ This marginal attractiveness is then affected by the latent variable, where $\zeta_{k|2}$ scales ¹⁷ the level spacing based on latent attribute importance.

The treatment is different if attribute k is a categorical variable. In that case, a specific level will apply. Let us assume that attribute k takes L_k possible values in a survey. We would then have:

$$B_{knm|2} = \phi_{k_1|2} \left(x_{knm|2} == 1 \right) + \sum_{l=2}^{L_k} \phi_{k_l|2} \left(e^{\zeta_{k|2}\alpha_{n_k}} \right) \left(x_{knm|2} == l \right).$$
(11)

In this specification, we have a sum over all the possible levels that could apply for 21 attribute k, where only one of these will apply in a given BWS2 scenario, and where 22 the bracket $(x_{knm|2} == l)$ will be equal to 1 for that specific level. We now estimate 23 the baseline attractiveness of each level for the categorical attribute through $\phi_{k_l|2}$. The 24 baseline attractiveness parameter $\phi_{k_l|2}$ is then further re-scaled by the corresponding 25 latent attribute importance through $\zeta_{k|2}$, where this impact of the latent variable is 26 attribute rather than attribute-level specific. We do not scale the base level (i.e. l = 1) 27 to avoid the situation where an individual with higher *attribute importance* derives 28 higher attractiveness from the base level of attribute k than other individuals. Under 29 the current specification, respondents with higher attribute importance then exhibit a 30

wider gap in terms of attractiveness between a higher level and the lowest (base) level
for that attribute than others do.

For normalisation purpose, one attribute level across all attributes in the MaxDiff model with scale difference for BWS2 data needs to be selected as the base by fixing

⁵ the associated parameters to 0.

6 2.5. Log-likelihood

The unconditional probability of observing the sequence of stated choices y_n and bestworst responses $(b, w)_n$ can be expressed as the integral of the multiplication of the conditional stated choice probabilities and the conditional best-worst choice probabilities over the distribution of η_n , the random component of the latent variables α_n , and over the distribution of ξ_n , the random component of the unobserved preference heterogeneity irrelevant from α_n , such that the log-likelihood is given by:

$$LL(y, (b, w)) = \sum_{n=1}^{N} ln \int_{\xi_n} \int_{\eta_n} \left(\prod_{t=1}^{T_n} P(y_{nt} \mid \beta_n) \prod_{m|1=1}^{M_{n|1}} P((b, w)_{nm|1} \mid \alpha_n) \prod_{m|2=1}^{M_{n|2}} P((b, w)_{nm|2} \mid \alpha_n) \right),$$

$$f(\eta_n) g(\xi_n) d\eta_n d\xi_n$$
(12)

where T_n , $M_{n|1}$ and $M_{n|2}$ give the total numbers of the SC tasks, the BWS1 tasks, and the BWS2 tasks shown to respondent n. Meanwhile, choice observations y_{nt} , $(b, w)_{nm|1}$, $(b, w)_{nm|2}$ refer to the chosen alternative in a SC task, the chosen best-worst pair of attributes in a BWS1 task, and the best-worst pair of attribute levels selected in a BWS2 task, respectively. Since the resulting LL does not have closed-form expression, the value of the log-likelihood needs to be approximated through simulation (Train 2009).

20 2.6. Hypothesis

A hypothesis is put forward with respect to the correlations among stated choices, BWS1 responses and BWS2 responses as well as the role of latent *attribute importance* in the joint model. Providing that a higher value of the latent variable is associated with stronger *attribute importance*, we expect the signs of the impact factors of *attribute importance* in the choice model and measurement models (i.e. $\tau, \zeta_{|1}, \zeta_{|2}$) to all be positive. That is, respondents who perceive higher importance from an attribute would have a higher probability to:

• be more sensitive (i.e. higher marginal utility) to the attribute in SC tasks;

- give more weight to the same attribute per se in BWS1 tasks;
- experience a wider gap in terms of attractiveness between a higher level and the
- lowest level (i.e. higher marginal attractiveness) for the attribute concerned in
 BWS2 tasks.

Of course, the same result also applies if all signs are negative, i.e. a higher latent 5 variable leads to lower sensitivities in SC, lower weights in BWS1 and narrower at-6 tractiveness gaps in BWS2. In that case, the latent variable would be interpreted as 7 reduced attribute importance. Opposite signs for the different effects or insignificance 8 indicate a lack of consistency for the associated attribute across datasets. If fixing all 9 the impact factors to 0, the joint ICLV model would be equivalent in specification to 10 a model which pools all the three datasets but ignores any correlations in between. 11 In this sense, our model can identify to what extent the choices made and the role of 12 attributes played are consistent across different types of tasks, and explore whether 13 the behavioural information contained in BWS1 and BWS2 data could help improve 14 the understanding of SC data. 15

It is worth noting that the latent variables of *attribute importance* are not used to show the influence on an attribute in comparison with other attributes, but instead to explain part of the variation across individuals. That is, if the hypothesis can be confirmed, ceteris paribus, a higher value of the latent attribute importance α_{nk} would mean individual n is relatively more strongly influenced by attribute k in different tasks than other individuals, rather than indicating perceiving more importance from attribute k than from other attributes.

23 3. Case study: Survey and data

24 3.1. Survey background

Our research is conducted in the context of HSR (high-speed rail)-air intermodality in China. This integrated HSR-air service has been put into practice since 2011 in Shanghai with an aim to enhance the connectivity of Shanghai and its non-airport catchment area by enabling passengers to jointly travel by HSR and air on a single trip with a convenient and even seamless transfer between the two different modes and without the need of purchasing HSR and flight tickets separately.

³¹ Since collecting data from real passengers at an airport terminal is very difficult,⁷

- ³² we tried to gain more behavioural and preference information from each respondent.
- ³³ Concerning this, we used SC, BWS1 and BWS2 tasks in the survey to understand how

⁷A preliminary pilot survey conducted at Shanghai Hongqiao Airport where the HSR-air intermodal service was available suggested low chance of intercepting transfer passengers, low willingness of outbound passengers to participate in the survey, and little knowledge about HSR-air intermodality of the participants. This also explains why we instead collected data at Pudong International Airport for the formal survey as it was much easier to approach transfer passengers there.

¹ people react to the relatively new integrated HSR-air mode.

² We collected data at Pudong International airport in Shanghai in January 2017. A

 $_3$ total of 123 respondents answered 8 SC tasks, 7 BWS1 tasks and 8 BWS2 tasks. The

⁴ SC component repeatedly asked participants to choose the most favourable alternative

5 including the new HSR-air alternative. The BWS1 tasks examined the relative weight

⁶ of all the 7 attributes involved in the SC tasks. The BWS2 tasks focused on the relative

7 attractiveness of 14 attribute levels across 4 attributes of interest.

A detailed description of survey background, socio-demographic composition, SC experimental design, and descriptive analysis on the SC data can be found in Song, Hess, and Dekker (2018). All the respondents were shown tasks in the order of SC, BWS1 and BWS2, thus any ordering effects cannot be addressed in our study. We did so to ensure that respondents would be aware of the choice scenarios and the meaning of attributes involved in the SC tasks when they responded to the BWS1 and BWS2 tasks.

15 **3.2.** SC tasks

¹⁶ The context of the SC tasks is framed in the following way:

• a passenger is travelling from a domestic origin O to an overseas destination D;

• direct flights from O to D are unavailable;

• a passenger from O to D needs to travel via Shanghai;

• a passenger can only travel by air between Shanghai and D.

Four alternatives were shown to respondents, namely car-air, air-air, separated HSR-21 air and integrated HSR-air. As shown in Fig. 2, we denote the first leg between O and 22 Shanghai as the "minor leg" on which various modes are available, and the second leg 23 between Shanghai and D as the "major leg" where air is the only option. Car-air means 24 using car on the minor leg and using flight on the major leg; air-air means taking a 25 connecting flight; separated HSR-air refers to the traditional way of purchasing air 26 and HSR tickets separately; integrated HSR-air refers to the new HSR-air intermodal 27 service. 28



Figure 2.: Illustration of choice scenarios in the SC survey.

²⁹ The SC survey was generated through a *D*-efficient design (Rose and Bliemer 2007)

in Ngene (Metrics 2012). Each respondent was presented with 8 SC tasks in a ran-1 domised order, giving a total of 984 stated choice observations. Fig. 3 shows an example 2 of the SC tasks. A total of 7 attributes were incorporated, including minor time, con-3 nection time, transfer time, delay protection, ticket integration, luggage integration 4 and travel cost. Minor time gives the time spent on the minor leg; transfer time de-5 notes the time spent on transferring between the minor leg and the major leg;⁸ and 6 connection time means the time spent on waiting and going through various proce-7 dures (e.g. security check-in, luggage check-in) at the departure airport of the major 8 leg. Travel cost gives the total expenditure for the journey, and delay protection in-9 dicates to what extent a respondent would be compensated in case of delay on the 10 minor leg. Ticket integration and luggage integration are two attributes describing the 11 extent of integration of the ticketing systems and luggage-handling systems between 12 the HSR side and the air side, of which the detailed levels can be found in Table 2. 13

	Car-air	Air-air	Separated HSR-air	Integrated HSR-air
Travel cost	¥1,250	¥1,050	¥1,150	¥1,250
Minor time	5h	1.5h	2.5h	2.5h
Transfer time	0h	0h	1.5h	1.5h
Connection time	1.5h	4h	1.5h	2.5h
Delay protection	None	Free flight change	None	50% discount on changing flight
Ticket integration	-	 Book together Fixed-time flight on minor leg Easy collection 	 Book separately Fixed-time train on minor leg No easy collection 	 Book together Fixed-time train on minor leg Easy collection
Security check and luggage integration	-	 Two security checks No integrated luggage handling system 	 Two security checks No integrated luggage handling system 	 One security check Integrated luggage handling system available

Figure 3.: Example of SC tasks.

From the SC observations, we find that the integrated HSR-air alternative was most frequently chosen (41.57%), followed by the separated HSR-air alternative (26.42%), whereas car-air was selected for the least number of times (9.35%), which indicates relatively strong attractiveness of the integrated service and its potential market.

 $^{^{8}}$ Transfer time has three levels: it takes a value of 0min to indicate a seamless transfer in the same transport hub and takes the level of either 45min or 90min to suggest a transfer between two different hubs.

1 3.3. BWS Case 1 tasks

The BWS1 section required respondents to choose the attributes that they weighted the most and the least in each task. A balanced incomplete block design (BIBD) was adopted to generate the BWS1 experiment which could ensure each attribute occurred the same number of times and co-occurred with any other attribute the same number of times across all the choice tasks (Louviere, Flynn, and Marley 2015). In our survey, 7 attributes were assigned into 7 randomly-displayed BWS1 tasks, each with 4 attributes. Consequently, each attribute was shown to each respondent 4 times and 9 each pair of attributes occurred twice. Fig. 4 shows an example of the BWS1 tasks.

Most	If you are going to buy an integrated HSR-air service, what factors do you consider as the most important and least important?	Least
	Minor time	
	Delay protection	
	Connection time	
	Travel cost	

Figure 4.: Example of BWS1 tasks.

An easy way to analyse BWS data is to compute the simple best-minus-worst (B-10 W) scores for each attribute.⁹ Table 1 summarises the simple B-W score for each 11 attribute averaged across respondents in a descending order as well as the standard 12 deviation (s.d.) of individual-level simple B-W scores for each attribute. A higher B-13 W score means greater weight to the corresponding attribute in deciding whether to 14 buy an integrated HSR-air option. These scores provide a straightforward implication 15 that minor time and ticket integration mattered the least, whereas connection time 16 and travel cost are the two attributes that mattered the most by the sample. The 17 standard deviations of B-W scores suggest that respondents gave more diverse weight 18 to the time-unrelated attributes than to time-related attributes. Minor time has the 19 lowest B-W scores and is the attribute with the second lowest standard deviation of 20 B-W scores, indicating that it was universally considered of limited importance. This 21 is understandable as our survey was based in Shanghai and its nearby regions which 22 could be reached by HSR or air from Shanghai within a relatively short period of time. 23

⁹Simple best-minus-worst scores can be obtained by subtracting the total count of an item being chosen as the worst from the total count the same item being chosen as the best across all BWS choice tasks and across all respondents (Louviere, Flynn, and Marley 2015). Since each attribute appeared 4 times per person in our case, the simple B-W score averaged at the individual-level is between -4 and 4.

Attribute	B-W score	s.d.	Score ranking
CT (connection time)	0.37	2.00	1
TC (travel cost)	0.33	2.49	2
DP (delay protection)	0.29	2.35	3
TT (transfer time)	0.23	1.77	4
LI (luggage integration)	0.16	2.61	5
TI (ticket integration)	-0.47	2.27	6
MT (minor time)	-0.90	1.77	7

Table 1.: Average simple B-W scores and standard deviation for BWS1 data

1 3.4. BWS Case 2 tasks

The BWS2 section consisted of 8 tasks, each comprising the attribute levels which 2 constituted the profile of the integrated HSR-air alternative in each SC task. Our 3 BWS2 survey focused on four attributes, i.e. connection time, delay protection, ticket 4 integration and luggage integration, such that each BWS2 task required respondents 5 to select the most appealing and the least appealing from 4 available attribute levels.¹⁰ 6 We did not include the full set of attributes in the BWS2 tasks as in the SC or BWS1 7 tasks for the sake of reducing cognitive burden and zooming in on those relatively 8 new attributes of HSR-air. As the latent attribute importance is not used to show the 9 influence of an attribute in comparison with other attributes, but to explain part of 10 the inter-individual preference heterogeneity, not presenting levels for the remaining 11 three attributes would not affect the distributions or the impact of the latent *attribute* 12 *importance* across individuals for the four attributes involved in the BWS2 tasks. 13 Fig. 5 gives an example of the BWS2 tasks, where different levels across different 14 attributes were evaluated on a common scale rather than being compared within an 15

¹⁶ attribute, such that a respondent might prefer "having 50% off on a flight change"

17	over	"having	an	integrated	luggage	-handling	system	and	one	security	check"	'.
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Most	Given that the integrated HSR-air service costs 1250RMB, takes 2.5h on the minor (HSR) leg, and requires a transfer between Hongqiao HSR station and Pudong airport, which of the following are the most and the least appealing?	Least
	Connection time: 2.5h	
	50% off on changing flight	
	Book together, fixed-time train on the minor leg and easy collection	
	Integrated luggage-handling and one security check	

Figure 5.: Example of BWS2 tasks.

¹⁰The levels were always shown in the order of connection time, delay protection, ticket integration and luggage integration to reduce cognitive burden. Comparisons between levels within a same attribute were not allowed.

1			Table 2.: Summary of the attri	ibute levels in BWS2	tasks		
	#	Attribute	Meaning	Numbers of re-	Times avail-	Times as	Times as
		level		spondents shown	able	the best	the worst
	1	conn150	Connection time is 2.5h	123	235	32	53
	2	conn180	Connection time is 3h	111	172	15	83
	3	conn210	Connection time in 3.5h	123	280	25	97
	4	conn270	Connection time is 4.5h	74	162	2	93
	5	conn 330	Connection time is 5.5h	87	135	1	103
	6	delay0	No delay protection	123	320	20	155
	7	delay1	50% off on changing flight should missing major-leg	123	319	80	64
			flight due to the delay on minor leg				
	8	delay2	Changing flight for free should missing major-leg flight	123	345	131	39
2			due to the delay on minor leg				
2	9	tick1	Booking tickets together, no easy collection, fixed-time	123	379	96	64
			train on the minor leg				
	10	tick2	Booking tickets together, easy ticket collection available,	123	324	76	56
			fixed-time train on the minor leg				
	11	tick3	Booking tickets together, eash ticket collection available,	111	281	91	38
			flexible train on the minor leg				
	12	lugg0	No luggage integration, security checks required on both	99	138	2	67
			minor and major legs				
	13	lugg1	Integrated luggage-handling system available, security	110	448	179	54
			checks required on both minor and major legs				
	14	lugg2	Integrated luggage-handling system available, one security check required	123	398	234	18

Overall, 14 different attribute levels were included in the BWS2 survey as listed in Table 2, including 5 levels of connection time, 3 levels of delay protection, 3 levels of ticket integration and 3 levels of luggage integration.

It should be noted that each item was not necessarily presented to all of the 123 respondents and did not occur with a same frequency. Thus, we calculate analytical B-5 W scores¹¹ to show relative attractiveness of the attribute levels among the sample. As 6 shown in Table 3, we can see an increase in the analytical B-W scores as the level goes 7 up for delay protection and luggage integration. However, for ticket integration, the 8 scores are generally low and close to each other, indicating that the three levels of ticket 9 integration were almost equally attractive to the respondents. One interesting thing is 10 that connection time appears to be generally considered less attractive, regardless of 11 which actual value it takes. This is understandable as connection time was considered 12 as the most important factor in the BWS1 tasks, so that the respondents felt all the 13 values of connection time presented in the BWS2 tasks to be unattractive. 14 The scores are used for descriptive analysis for better understanding the BWS1 and 15

¹⁶ BWS2 data. All in all, we wish to study the correlation across the different datasets. ¹⁷ The B-W scores themselves do not allow us to do so because we can only calculate the ¹⁸ scores for BWS1 and BWS2 data independently, regardless of the calculation method ¹⁹ we adopt. We need the joint model to simultaneously estimate on SC, BWS1 and ²⁰ BWS2 data and to explore the correlations among them.

Attribute level	Analytical B-W score	Score ranking
conn150	-0.18	8
conn180	-0.84	10
conn210	-0.53	9
conn270	-1.27	13
conn 330	-1.97	14
delay0	-0.90	11
delay1	0.10	7
delay2	0.55	3
tick1	0.17	5
tick2	0.12	6
tick3	0.38	4
lugg0	-1.02	12
lugg1	0.57	2
lugg2	1.22	1

Table 3.: Analytical B-W scores for BWS2 data at the sample level

¹¹Analytical B-W scores can be obtained by $\ln \left(\frac{1+\frac{N_b-N_w}{N_x}}{1-\frac{N_b-N_w}{N_x}}\right)$, where $N_b - N_w$ is the simple B-W score and N_x is the total times of the item being available, such that the score can rule out the impact of uneven occurrence of each attribute (Lipovetsky and Conklin 2014; Marley, Islam, and Hawkins 2016).

1 4. Case study: Model estimation

2 4.1. Model specification

The models in this paper were estimated in R using the flexible choice modelling 3 package Apollo (Hess and Palma 2019), and 1000 MLHS draws (Hess, Train, and 4 Polak 2006) were used in simulation. We used likelihood ratio tests to gradually improve the model specification and select the model offering the best fit while also 6 taking into account the risk of over-fitting as well as behavioural interpretation of the 7 modelling results. We also removed some insignificant variables due to small sample 8 size and continuously checked the impact on willingness-to-pay estimates. This section 9 describes the final specification of the joint ICLV model we have found with the 10 best information criterion (i.e. Akaike Information Criterion and Bayesian Information 11 Criterion), which can best balance between log-likelihood and behavioural insights 12 while keeping the risk of over-fitting at a relatively low level.. 13

14 4.1.1. Structural equations

¹⁵ After regressing the BWS1 individual-specific simple B-W scores of each attribute on ¹⁶ different socio-demographic characteristics, the adopted structural equations for the 7

¹⁷ latent variables of attribute importance α_{nk} in Eq. 1 are defined as:¹²

 $\alpha_{n,MT} = \eta_{n,MT}, \ (k = \text{Minor Time})$ $\alpha_{n,CT} = \eta_{n,CT}, \ (k = \text{Connection Time})$ $\alpha_{n,TT} = \eta_{n,TT} + \omega_{TT,age>45} \cdot Z_{age>45}, \ (k = \text{Transfer Time})$ $\alpha_{n,DP} = \eta_{n,DP} + \omega_{DP,male} \cdot Z_{male}, \ (k = \text{Delay Protection}) \quad , \qquad (13)$ $\alpha_{n,TI} = \eta_{n,TI} + \omega_{TI,age>35} \cdot Z_{age>35}, \ (k = \text{Ticket Integration})$ $\alpha_{n,LI} = \eta_{n,LI} + \omega_{LI,age>45} \cdot Z_{age>45}, \ (k = \text{Luggage Integration})$ $\alpha_{n,TC} = \eta_{n,TC} + \omega_{TC,reimbursed} \cdot Z_{reimbursed}, \ (k = \text{Travel Cost})$

where η_{nk} follows a standard Normal distribution among respondents. All sociodemographic variables used are rescaled to be centred on 0. We have not found suitable socio-demographics for the determinants of the latent attribute importance of minor time and connection time. Thus $\alpha_{n,MT}$ and $\alpha_{n,CT}$ are assumed to be purely random.

¹²For the sake of consistency, in section 4, parameters on attributes are notated with subscripts of the capital initials of the attributes as shown in Table 1, and parameters on attribute levels are represented with subscripts of the abbreviation of the attribute levels in lower case as listed in Table 3.

1 4.1.2. Choice model for SC data

For normalisation purposes, the alternative-specific constant δ_i for the integrated HSRair alternative is fixed to 0 while the other 3 alternative-specific constants are estimated. We assume $\tau_{MT} = 0$ to avoid over-specification since minor time acts as the base in the measurement model for BWS1 data and was not included in the BWS2 survey.

Minor time, connection time and travel cost are treated as continuous variables. The
remaining four attributes are treated as categorical variables, with the lowest level of
each being the base in dummy coding. The sensitivity coefficients for these attributes
in the stated choice component in Eq. 3 are denoted in detail as:

$$\beta_{n,MT} = -e^{\mu_{ln(-\beta_{MT})} + \sigma_{ln(-\beta_{MT})}\xi_{n,MT}}$$

$$\beta_{n,CT} = -e^{\tau_{CT}\alpha_{n,CT}} \cdot e^{\mu_{ln(-\beta_{CT})} + \sigma_{ln(-\beta_{CT})}\xi_{n,CT}}$$

$$\beta_{n,tran45\&90min} = -e^{\tau_{TT}\alpha_{n,TT}} \cdot e^{\kappa_{TT,age>45}Z_{age>45}} \cdot e^{\mu_{ln(-\beta_{tran45\&90min})} + \sigma_{ln(-\beta_{TT})}\xi_{n,TT}}$$

$$\beta_{n,delay1\&2} = e^{\tau_{DP}\alpha_{n,DP}} \cdot e^{\kappa_{DP,male}Z_{male}} \cdot e^{\mu_{ln(\beta_{delay1\&2})} + \sigma_{ln(\beta_{DP})}\xi_{n,DP}},$$

$$\beta_{n,lugg1\&2} = e^{\tau_{LI}\alpha_{n,LI}} \cdot e^{\kappa_{LI,age>45}Z_{age>45}} \cdot e^{\mu_{ln(\beta_{lugg1\&2})} + \sigma_{ln(\beta_{LI})}\xi_{n,LI}}$$

$$\beta_{n,TC} = -e^{\tau_{TC}\alpha_{n,TC}} \cdot e^{\kappa_{TC,reimbursed}Z_{reimbursed}} \cdot e^{\mu_{ln(-\beta_{TC})} + \sigma_{ln(-\beta_{TC}x67)}\xi_{n,TC}}$$

$$(14)$$

such that $\beta_{n,MT}$, $\beta_{n,CT}$ and $\beta_{n,TC}$ measure the marginal utilities, while $\beta_{n,tran45\&90min}$, 11 $\beta_{n,delay1\&2}$, and $\beta_{n,lugq1\&2}$ give the relative utility against the corresponding base lev-12 els, which are tran0min, delay0, and lugg0 in respective. The higher two levels for each 13 are merged for estimation in our final specification as they are found not significantly 14 different from each other. The final specification excludes the attribute of ticket inte-15 gration from the utility function for the SC data, as it is found to contribute little to 16 the utility functions. However, ticket integration is still used in the measurement mod-17 els. Finally, parameters of $\kappa_{DP,male}$, $\kappa_{TC,reimbursed}$ and τ_{DP} are set to zero in the final 18 specification as they were insignificant. Besides, although we have found suitable socio 19 to explain transfer time (i.e. $Z_{age>45}$), the model with the indirect impact of $Z_{age>45}$ 20 becomes insignificant once the direct impact is added. Hence, in the final specification, 21 we drop the indirect impact by fixing $\omega_{TT,age>45} = 0$ and keep the direct impact of 22 age on transfer time by estimating $\kappa_{TT,aqe>45}$. 23

24 4.1.3. Measurement models for BWS1 data and BWS2 data

For the BWS1 data, all the 7 attributes shown in the SC survey are examined, i.e. minor time, connection time, transfer time, delay protection, ticket integration, luggage integration and travel cost. Minor time acts as the base, with relevant parameters $\delta_{MT|1}$ and $\zeta_{MT|1}$ normalised to 0. For the BWS2 data, connection time, delay pro¹ tection, ticket integration and luggage integration are the four attributes of interest.

² Connection time is treated as a continuous variable and $x_{CT,nm|2}$ can take the value

³ of 150min, 180min, 210min, 270min or 330min. The remaining three attributes are

⁴ regarded as categorical variables, with level delay0, tick1 and lugg0 being the lowest

⁵ (base) levels for delay protection, ticket integration and luggage integration in respec-

 $_{6}$ tive. The attribute level delay0 is selected as the base in the measurement model for

⁷ BWS2 data, with the baseline attractiveness $\phi_{delay0|2}$ fixed to 0 for normalisation.

8 4.2. Estimation results

⁹ For comparison, we estimated the corresponding reduced form mixed multinomial logit ¹⁰ (MMNL) model for the SC data alone, i.e. setting $\tau = 0$, $\forall k$ (Vij and Walker 2016). ¹¹ The estimates of the MMNL model are shown alongside the estimates of the choice ¹² model component of the joint ICLV model in Table 4. In both models, the travel cost ¹³ variable was scaled by 6.9, such that the value-of-time is expressed in the $/min^{13}$.

Since the ICLV model explains three different types of responses, the log-likelihood 14 for the whole model in ICLV model (LL(total) = -4445.339) is much lower than the 15 log-likelihood of the SC component alone. Meanwhile, the log-likelihood of the choice 16 model component on the SC data of the ICLV model (LL(SC) = -1060.453) is slightly 17 inferior to that of the MMNL model (LL = -1057.396), which is consistent with the 18 discussions by Vij and Walker (2016). Indeed, the ICLV model needs to explain not 19 only the SC data but also the extra BWS1 and BWS2 data, and it is then impossible 20 for the ICLV model to outperform the reduced form MMNL model. Notwithstanding 21 this, our joint ICLV model appears to provide more behavioural explanations than 22 the reduced form MMNL model does. The τ estimates suggest significant roles of 23 the latent variables of *attribute importance* in scaling sensitivities for all the non-cost 24 attributes where applicable. 25

The MMNL model and the ICLV model show similar preference patterns towards 26 attributes. As shown in the upper part of Table 4, the most negative δ_{ca} implies that 27 the car-air alternative is the least preferred option, all else being equal, whereas the 28 air-air alternative (δ_{aa}) and the separated HSR-air alternative (δ_{sha}) are both slightly 29 less preferred compared to the base alternative, i.e. the integrated HSR-air mode. Since 30 Lognormal distributions are used, the more negative the underlying mean parameter 31 $\mu_{\ln|\beta_k|}$ is, the smaller in magnitude the median of marginal utility is, which translates 32 into a lower sensitivity to that attribute in the SC tasks. As to the standard deviations 33 $\sigma_{\ln|\beta_k|}$, both models detect statistically significant random heterogeneity in sensitivities 34 to all of the attributes. Regarding the direct impacts of socio-demographics in the 35 utility functions, we can see from both models that $\kappa_{TT,age>45}$ is significant at the 95% 36 confidence interval, suggesting that older respondents are more sensitive to transfer 37

 $^{^{13}\}mathrm{USD/CNY} \approx$ 6.9 during the period of data collection.

	\mathbf{M}	MNL		\mathbf{CLV}
Log likelihood	LL	1057 396	LL (total	l): -4445.399
Log inkcillioou	<u>пп</u>	1007.000	LL (SC)	: -1060.453
	\mathbf{est}	t-rat(0)	est	t-rat(0)
δ_{ca}	-3.210	-7.49	-3.081	-6.91
δ_{aa}	-0.411	-1.73	-0.439	-2.04
δ_{sha}	-0.622	-3.30	-0.738	-3.60
$\mu_{ln(-\beta_{MT})}$	-5.243	-16.51	-5.441	-14.26
$\mu_{ln(-\beta_{CT})}$	-4.527	-37.69	-4.596	-38.62
$\mu_{ln(-\beta_{tran45\&90min})}$	-0.900	-2.44	-1.009	-1.85
$\mu_{ln(\beta_{delay1\&2})}$	-1.342	-2.29	-2.157	-2.42
$\mu_{ln(\beta_{lugg1\&2})}$	-0.729	-2.32	-1.096	-2.10
$\mu_{ln(-\beta_{TC})}$	-4.181	-22.02	-4.265	-14.51
$\sigma_{ln(-\beta_{MT})}$	-0.558	-4.02	-0.881	-3.62
$\sigma_{ln(-\beta_{CT})}$	-0.517	-6.11	-0.409	-5.02
$\sigma_{ln(-\beta_{TT})}$	1.327	5.01	1.028	4.08
$\sigma_{ln(\beta_{DP})}$	-1.203	-2.12	-1.818	-3.71
$\sigma_{ln(\beta_{LI})}$	-1.331	-6.35	-1.246	-5.25
$\sigma_{ln(-\beta_{TC})}$	-0.622	-3.75	-0.486	-2.81
$\kappa_{TT,age>45}$	$\bar{1}.\bar{6}\bar{6}\bar{9}$	3.73	1.468	2.54
$\kappa_{DP,male}$	0.000	-	0.000	-
$\kappa_{LI,age>45}$	0.947	1.57	1.252	2.18
$\kappa_{TC,reimbursed}$	0.000		0.000	
$ au_{CT}$			$0.2\bar{3}\bar{3}$	2.37
$ au_{TT}$			0.335	2.59
$ au_{DP}$			0.000	-
$ au_{LI}$			0.701	4.49
$ au_{TC}$			0.334	1.21

Table 4.: Estimates for the reduced form MMNL model and the choice model component of the ICLV model

time and dislike long transfer time more than young people do. Meanwhile, although $\kappa_{LI,age>45}$ in the MMNL model is only significant at the 80% confidence interval, we can still infer from $\kappa_{LI,age>45}$ in the ICLV model, which is significant at the 95% confidence interval, that older passengers can derive higher utility from better luggage integration than young people do.

In the left part of Table 5, the constant $\delta_{|1}$ represents the mean of the weight to the 6 associated attribute among the sample in the BWS1 data. It could be noticed that, 7 with minor time normalised to 0, connection time, delay protection and transfer time 8 are positioned at the higher end of the underlying weighting scale, followed by travel 9 cost and luggage integration. Regarding the scalars in the worst choice stage shown in 10 the down left of Table 5, $\lambda_{CT|1}$ (t-rat(1)=-4.27) is the only one which is significantly 11 different from 1, suggesting that scaling difference between the worst choice stage and 12 the best choice stage only exists for the attribute of connection time. Since $\lambda_{CT|1}$ is 13 much lower than 1, it suggests that the model has less noise in explaining the choices 14 in the best choice stage than in the worst choice stage for the attribute of connection 15 time. 16

Table 5.: Estimates of the measurement models for the BWS1 and BWS2 data using the MaxDiff models with scale difference

	В	WS1			BV	WS2	
	\mathbf{est}	t-rat(0)	t-rat(1)		\mathbf{est}	t-rat(0)	t-rat(1)
$\delta_{MT 1}$	0 (base)	-	-	$\delta_{CT 2}$	4.151	4.06	-
$\delta_{CT 1}$	1.271	5.23	-	$\gamma_{CT 2}$	-0.015	-3.86	-
$\delta_{TT 1}$	0.920	4.22	-	$\phi_{delay0 2}$	0 (base)	-	-
$\delta_{DP 1}$	1.071	3.21	-	$\phi_{delay1 2}$	2.008	5.54	-
$\delta_{TI 1}$	0.311	1.29	-	$\phi_{delay2 2}$	2.601	6.25	-
$\delta_{LI 1}$	0.738	2.37	-	$\phi_{tick1 2}$	1.956	4.86	-
$\delta_{TC 1}$	0.899	3.44	-	$\phi_{tick2 2}$	2.201	5.34	-
				$\phi_{tick3 2}$	2.536	5.93	-
				$\phi_{luqq0 2}$	-0.102	-0.33	-
				$\phi_{luqq1 2}$	2.437	5.75	-
				$\phi_{lugg2 2}$	3.432	7.60	
$\lambda_{MT 1}$				$\lambda_{MT 2}$			
$\lambda_{CT 1}$	0.255	-	-4.27	$\lambda_{CT 2}$	0.992	4.11	-0.03
$\lambda_{TT 1}$	0.600	-	-1.17	$\lambda_{TT 2}$	-	-	-
$\lambda_{DP 1}$	0.751	-	-0.98	$\lambda_{DP 2}$	0.815	7.18	-1.63
$\lambda_{TI 1}$	1.171	-	0.48	$\lambda_{TI 2}$	0.691	5.41	-2.42
$\lambda_{LI 1}$	1.018	-	0.06	$\lambda_{LI 2}$	0.755	6.59	-2.13
$\lambda_{TC 1}$	1.411	-	0.95	$\lambda_{TC 2}$	-	-	-

The right part of Table 5 shows estimates for the baseline attractiveness of each attribute level in the BWS2 data. Focusing on $\phi_{|2}$, it can be inferred that compared to ticket integration, delay protection and luggage integration are associated with overall larger steps in attractiveness when moving from a poorer level to a better level, which implies that respondents might be indifferent to variations in ticket integration. This is $_{1}$ $\,$ in line with the discoveries in the SC data and the BWS1 data as well as the preliminary

² findings in the normalised B-W scores in the BWS2 data. As to the attribute-specific

- ³ scalars shown in the down right of Table 5, only ticket integration $\lambda_{TI|2}$ (t-rat(1)=-
- 4 2.42) and luggage integration $\lambda_{LI|2}$ (t-rat(1)=-2.13) are significantly different from 1.
- ⁵ Being smaller than 1, $\lambda_{TI|2}$ and $\lambda_{LI|2}$ suggest stronger random error in the worst choice

⁶ stage for these two attributes than in the best choice stage.

Now we turn to Table 6 to jointly examine all the impact factors of latent attribute 7 importance in the choice model (i.e. τ) as well as in the two MaxDiff-based measure-8 ment models (i.e. ζ_{11} and ζ_{12}). The estimation results confirm our hypothesis. Except 9 for τ_{TC} , all the impact factors in the choice model and the measurement models are 10 positive and significant where applicable. Thus, choices are made in a consistent way 11 across different types of surveys. An increase in the latent variable would result in a 12 stronger sensitivity to the associated attribute in the SC data, an increased probability 13 that the attribute of interest is positioned to the higher end on the weighting scale 14 in the BWS1 data, and a wider attractiveness gap between levels of the concerned 15 attribute in the BWS2 data. 16

An exception arises for travel cost, where τ_{TC} is insignificant (est=0.334, t-17 rat(0)=1.21), whereas the same latent attribute importance plays a strong and sig-18 nificant role in BWS1 tasks (est=2.210, t-rat(0)=5.66). It is also worth noting that 19 delay protection is related to cost as well, and that positive and significant impact 20 of the corresponding latent attribute importance is found in both the BWS1 and 21 BWS2 data, but not in the SC data, i.e. as mentioned earlier, τ_{DP} is fixed to 0 in 22 this final specification as little influence from the latent attribute importance could 23 be found on scaling the sensitivity to delay protection in the SC data. This implies a 24 lack of consistency for the attributes related to cost between SC and BWS1/2 data, 25 which is in accordance with and complements the findings in Balbontin, Ortúzar, and 26 Swait (2015), where the sensitivity of an attribute related to cost, i.e. rent, was es-27 timated to be inconsistent between the SC and BWS2 data. It might be due to the 28 fact that choices in the SC experiment were made based on detailed choice contexts 29 and level values of different attributes of each alternative in multi-alternative settings, 30 while this information was not available in the BWS1 experiment where respondents' 31 awareness and past experience of each attribute would influence their evaluation of 32 the attributes (Louviere and Islam 2008; Mueller, Lockshin, and Louviere 2010). In 33 this context, compared to the other non-cost attributes, it might be more difficult to 34 assess the importance of the cost-relevant attributes and to trade off between cost and 35 the other non-cost attributes without knowing the actual levels for all the available 36 options in the choice set. Consequently, the role of the latent *attribute importance* is 37 not significant in explaining the preference variations for cost-related attributes across 38 individuals in the SC data, but is more prominent in the BWS1/2 data. 39

40 Combining the estimates ω in the structural equations and the impact factors for

Structur	al equati	ons		SC da	ta		BWS1 dat	ta	I	BWS2 d	ata
	est	t-rat(0)		est	t-rat(0)		est	t-rat(0)		est	t-rat(0)
ω_{MT}	-	-	τ_{MT}	-	-	$\zeta_{MT 1}$	0 (base)	-	$\zeta_{MT 2}$	-	-
ω_{CT}	-	-	τ_{CT}	0.233	2.37	$\zeta_{CT 1}$	0.659	2.03	$\zeta_{CT 2}$	0.373	9.37
$\omega_{TT,age>45}$	0.000	-	τ_{TT}	0.335	2.59	$\zeta_{TT 1}$	1.211	4.50	$\zeta_{TT 2}$	-	-
$\omega_{DP,male}$	-0.863	-2.71	τ_{DP}	0.000	-	$\zeta_{DP 1}$	2.067	3.40	$\zeta_{DP 2}$	0.519	3.25
$\omega_{TI,age>35}$	0.868	3.97	τ_{TI}	-	-	$\zeta_{TI 1}$	1.683	4.34	$\zeta_{TI 2}$	0.371	3.94
$\omega_{LI,age>45}$	1.191	2.66	τ_{LI}	0.701	4.49	$\zeta_{LI 1}$	2.160	5.29	$\zeta_{LI 2}$	0.530	4.80
$\omega_{TC,reimbursed}$	-0.625	-3.36	τ_{TC}	0.334	1.21	$\zeta_{TC 1}$	2.210	5.66	$\zeta_{TC 2}$	-	-

Table 6.: Estimates in the structural equations and impact factors of latent attribute importance in the choice model and the BWS1/2 measurement models

latent attribute importance, the positive $\omega_{TI,aqe>35}$ and $\omega_{LI,aqe>45}$ and the negative 1 $\omega_{TC,reimbuised}$ show that older people think ticket integration and luggage integration 2 to be of greater importance than young people do, while passengers who get reimbursed 3 perceive lower importance for travel cost than those who need to pay for the travel 4 on their own. The negative and significant $\omega_{DP,male}$ suggests that male passengers 5 find delay protection less important than female passengers do. Parameter $\omega_{TT,age>45}$ 6 are fixed to 0 and not estimated in the final specification because of its very low 7 significance. We can further look back into Table 4, where $\kappa_{TT,age>45}$ and $\kappa_{LI,age>45}$ 8 are the only two statistically significant κ parameters. We can therefore deduce that 9 respondents' age mainly plays an independently direct role in scaling the marginal 10 utility of transfer time, whereas age affects the marginal utility of luggage integration 11 both directly and indirectly via the latent variable. The remaining socio-demographic 12 characteristics involved in ω influence stated choice behaviour mainly through the 13 latent variables of attribute importance. 14

Finally, we shed some light on willingness-to-pay (WTP) in the SC data with and 15 without the additional information gained from the BWS1 and BWS2 data in Table 16 7. We first calculated the distributions of marginal utilities for all the attributes. 17 taking into account of the roles of latent attribute importance and socio-demographic 18 characteristics in the ICLV model and the role of socio-demographic characteristics in 19 the reduced form MMNL model, i.e. marginal utilities β_{nk} are given by $e^{\tau_k \alpha_{nk}} e^{\kappa_k Z_n} \beta_{nk}^{\star}$ 20 in the ICLV model and by $e^{\kappa_k Z_n} \beta_{nk}^{\star}$ in the MMNL model, where $\beta_{nk}^{\star} = e^{\mu_{\ln\beta_k} + \sigma_{\ln\beta_k} \cdot \xi_{nk}}$. 21 We then calculated the ratio against the marginal utility of travel cost for each of the 22 remaining attributes for each draw, which is taken from the distributions of marginal 23 utilities used in the estimation procedure, enabling us to obtain the WTP distributions 24 for all the attributes except for travel cost through simulation (Hensher and Greene 25 2003; Sillano and de Dios Ortúzar 2005; Daly, Hess, and Train 2012). 26

We see some differences between the two models here, where we would argue that the ICLV findings are more realistic especially for transfer time. Indeed, in the ICLV model, going from a transfer time of 45 or 90 minutes to a seamless transfer has the same benefit as a reduction in connection time by 81.6 minutes at the mean. In the MMNL model, this would be 122.58 minutes, which seems unrealistic if we assume

that transfer time should at best be as important as connection time. In addition, 1 the standard deviations of the three categorical attributes, i.e. transfer time, delay 2 protection, and luggage integration are relatively large in both models. This can be 3 mainly attributed to the long tails of the Lognormal distributed WTP distributions 4 as the marginal utilities for all the attributes follow Lognormal distributions. Hence, 5 apart from regular statistics of mean and standard deviation, we also show the median 6 and interquartile range of each WTP distribution. We can see an overall reduction in 7 the median values, and a decrease in the interquartile range for all the attributes except 8 for minor time when we move from the MMNL model to the ICLV model. This means 9 that the spread of the distribution is smaller and and the values are more squeezed to 10 the median for the ICLV model. 11

1		Table 7.: W'	TP estin	nates of	f the join	t ICLV	model an	d the reduced form	MMNL	model.		
-	models	attributes	sensitiv	ities β	mean	and perc	centiles of	WTP distribution		WTP c	hanges ag	ainst MMNL
-			mean	s.d.	mean	s.d.	median	interquartile range	mean	s.d.	median	interquartile range
		Minor Time	-0.006	0.007	0.54	0.78	0.31	0.48	10%	59%	-11%	17%
		Connection Time	-0.011	0.006	0.96	0.85	0.72	0.77	-2%	-9%	1%	-5%
	ICIV	Transfer Time_45&90min	-0.738	1.429	62.72	146.51	25.47	50.34	-32%	-55%	-2%	-22%
	ICLV	Delay Protection_lv1&2	0.606	2.981	52.62	359.14	8.18	27.75	23%	252%	-52%	-23%
2		Luggage Integration_lv1&2	1.231	5.119	104.63	509.18	23.01	62.19	8%	78%	-27%	-17%
2		Travel Cost	-0.017	0.011	-	-	-	-	-	-	-	-
		Minor Time	-0.006	0.004	0.49	0.49	0.35	0.41	-	-	-	-
		Connection Time	-0.012	0.007	0.98	0.93	0.71	0.81	-	-	-	-
	MMNI	Transfer Time_45&90min	-1.160	3.581	91.80	328.10	26.08	64.19	-	-	-	-
		Delay Protection_lv1&2	0.539	0.975	42.87	101.98	16.99	35.81	-	-	-	-
		Luggage Integration_lv1&2	1.221	2.833	97.05	285.32	31.44	75.02	-	-	-	-
		Travel Cost	-0.019	0.013	-	-	-	-	-	-	-	-

Table 7.: WTP estimates of the joint ICLV model and the reduced form MMNL model.

¹ 5. Conclusions

This research has looked at potential travel behaviour in the context of the introduction 2 of a new travel mode, i.e. HSR-air intermodality. The need for better understanding the 3 role of attributes (especially the new ones) in the new context entails collecting more behavioural information from each individual. Compared with adopting a longer SC 5 survey, synthesising data from multiple types of preference elicitation approaches can 6 reduce boredom caused by additional SC tasks and provide more robust explanation 7 of the role that attributes play. The growing interest in BWS data has presented 8 the potential of such data synthesis. Specifically, SC data allows us to analyse how 9 respondents trade off between attributes and forecast demand, whereas BWS1 and 10 BWS2 data helps in providing more behavioural insights about the role that attributes 11 play. It needs to be noted that it is not the objective of this research to conclude which 12 type of preference elicitation method is more correct. 13

Informed by the work of Hess and Hensher (2013), we adopt the notion of *attribute* 14 *importance* and treat it as a latent variable, which acts as the connection amongst 15 all the three types of data. The attribute-specific latent variable scales the marginal 16 utility of the associated attribute in the choice model for the SC data. Meanwhile, it 17 explains the weight of the attribute and scale the marginal attractiveness of attribute 18 levels in the measurement models for the BWS1 data and the BWS2 data respectively. 19 This research has for the first time collected SC data together with more than one 20 type of BWS data from the same respondents. Our work can provide researchers with 21 practical guidance on applying BWS1 and (or) BW2 approaches in travel behaviour 22 contexts, and insights of choice behaviour in different types of surveys. By simulta-23 neously estimating on the SC, BWS1 and BWS2 data through the latent constructs 24 of attribute importance in the ICLV model, we are able to examine the correlations 25 of choice behaviour among these three different types of tasks at the individual level, 26 which was not addressed in Balbontin, Ortúzar, and Swait (2015), without inducing 27 the risk of endogeneity bias or measurement error which arose in Beck, Rose, and 28 Greaves (2017). The use of BWS1 and BWS2 data in the measurement models of the 29 ICLV model also provides richer behavioural information than the earlier work by Hess 30 and Hensher (2013), where stated attribute attendance and attribute rankings were 31 used. 32

Overall, our joint model shows that attribute importance can link the SC, BWS1 and BWS2 data, indicating the benefit of improving behavioural explanation by combining the BWS data with SC data. We found a high level of consistency with respect to the impact of the underlying perceived *attribute importance* on decision-making in different tasks is significantly demonstrated. The estimation results imply that an increase in attribute importance results in a stronger sensitivity to that attribute in the SC tasks, more overall weight to that attribute in the BWS1 tasks, and also wider attractiveness

gaps between levels for that attribute in the BWS2 tasks. This is particularly true for 1 non-cost attributes, including connection time, transfer time and luggage integration 2 in our case. We have not found similar consistency for cost-relevant attributes, i.e. 3 delay protection and travel cost, as the corresponding latent variables only impose 4 significant impacts in the BWS1/2 data but not in the SC data. That is, we have not 5 discovered a one-to-one relationship between different survey methods. As such, there 6 remain some differences in how attribute importance is evaluated between SC, BWS1 7 and BWS2 data. We therefore think treating different survey methods as equivalent 8 and interchangeable - for example using BWS1 method to determine which attributes 9 to include in SC survey - can be risky. 10

The lack of one-to-one consistency between different types of data is understandable 11 as SC tasks were conducted in multi-alternative settings. Meanwhile, the detailed 12 information of attribute levels and (or) the information of other competing alternatives 13 were not available in BWS1 tasks, and the competing alternatives were also not shown 14 to respondents. Thus respondents would be more capable to make trade-offs among 15 attributes based on the presented information in SC tasks, whereas their perceived 16 importance of a given attributes in a BWS1/2 survey is more affected by personal 17 experience etc. (Louviere and Islam 2008; Mueller, Lockshin, and Louviere 2010). 18

The finding that there is not a one-to-one relationship between the different types 19 of data can also be due to the fact that selecting the best is different from selecting 20 the worst, i.e. best choices are made under positive frames whereas worst choices are 21 made within negative frames (Rose 2014; Giergiczny et al. 2017). Given these results, 22 we suggest that researchers should not see BWS data as a replacement for SC data in 23 preference elicitation research. It is of course feasible to use BWS tasks alongside SC 24 tasks for better explanation of choices made in SC tasks, and this may be especially 25 beneficial if the number of respondents is low. We acknowledge that Hawkins, Islam, 26 and Marley (2018) suggested that the conclusion of best choices and worst choice 27 being made in different ways in many studies were due to the inadequate data. They 28 argued that respondents made best choices and worst choices in a same way (i.e. same 29 utility parameters), while worst choices were usually associated with greater variance 30 in the error term (i.e. scale heterogeneity existed between best choice stage and worst 31 choice stage). In our paper, the best choice stage and worst choice stage share the 32 same specification but with attribute-specific scale parameters imposed on the worst 33 stage. This means that our model is more generic and flexible, enabling us to detect 34 whether and which attribute has different scales between best and worst stages. The 35 results suggested that only a subset of attributes influence decision-making differently 36 on the worst stage in comparison to the best stage. Besides, we were using only a 37 small sample of data, which in turn makes it difficult to adopt more complex model 38 specification or to validate the conclusion raised by Hawkins, Islam, and Marley (2018). 39 Regarding this, it is necessary and beneficial to replicate different methods in more 40

¹ research contexts.

The present work also has some limitations. Firstly, systematic order effects were 2 not accounted for in our case study as respondents were all presented with choice tasks 3 in the order of SC, BWS1 and BWS2. Secondly, due to the restriction of sample size, 4 all the preference variations in the BWS1 and BWS2 tasks were attributed to latent 5 attribute importance, and we did not incorporate random heterogeneity irrelevant to 6 latent variables in out final specification. It would be worth applying our method on 7 other larger joint datasets with more complicated specification of random heterogene-8 ity, while at the same time achieving a balance with higher computational burden. 9 Furthermore, we could test the non-linearity in sensitivity parameters on the utility 10 functions for alternatives in the SC data. 11

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¹ Appendix A. The descriptors of the notations used in section 2.

α	Matrix, giving the latent <i>attribute importance</i> of each attribute per-
	ceived by each respondent.
α_n	Vector, giving the latent <i>attribute importance</i> of each attribute per- ceived by respondent n
	Consider the second se
$lpha_{nk}$	Scalar, giving the latent <i>attrioute importance</i> of attribute κ perceived
	by respondent n .
eta	Matrix, describing the marginal utility of each attribute for each re- spondent.
ßm	Vector describing the marginal utility of each attribute for respon-
$ ho_n$	dent n .
β_k	Vector, describing the marginal utility of attribute k for each respon-
	dent.
β_{nk}	Scalar, describing the marginal utility of attribute k perceived by
1 1010	respondent <i>n</i> .
$(h w)_{1}$	Matrix giving the choice (i.e. pair of the best attribute h and the
$(0, w) _{1}$	worst attribute w) for each respondent in each BWS1 choice task.
$(h w)_{10}$	Matrix giving the choice (i.e. pair of the best attribute level b and
$(0, \omega)_{ 2}$	the worst attribute level w) for each respondent in each BWS2 choice
	task.
B_{anmle}	Scalar, denoting the "utility" (i.e. weight of an attribute or attractive-
$B_{qnm c}$	Scalar, denoting the "utility" (i.e. weight of an attribute or attractive- ness of an attribute level) of item a in the "best" stage for respondent
$B_{qnm c}$	Scalar, denoting the "utility" (i.e. weight of an attribute or attractive- ness of an attribute level) of item q in the "best" stage for respondent n as shown in BWS task m and BWS type c (i.e. $c = 1$ stands for
$B_{qnm c}$	Scalar, denoting the "utility" (i.e. weight of an attribute or attractive- ness of an attribute level) of item q in the "best" stage for respondent n as shown in BWS task m and BWS type c (i.e. $c = 1$ stands for BWS1 and $c = 2$ stands for BWS2)
$B_{qnm c}$	Scalar, denoting the "utility" (i.e. weight of an attribute or attractive- ness of an attribute level) of item q in the "best" stage for respondent n as shown in BWS task m and BWS type c (i.e. $c = 1$ stands for BWS1 and $c = 2$ stands for BWS2).
$B_{qnm c}$ $BW_{(q,j)nm c}$	Scalar, denoting the "utility" (i.e. weight of an attribute or attractive- ness of an attribute level) of item q in the "best" stage for respondent n as shown in BWS task m and BWS type c (i.e. $c = 1$ stands for BWS1 and $c = 2$ stands for BWS2). Scalar, denoting the "utility" difference between item q and item j
$B_{qnm c}$ $BW_{(q,j)nm c}$	Scalar, denoting the "utility" (i.e. weight of an attribute or attractive- ness of an attribute level) of item q in the "best" stage for respondent n as shown in BWS task m and BWS type c (i.e. $c = 1$ stands for BWS1 and $c = 2$ stands for BWS2). Scalar, denoting the "utility" difference between item q and item j for respondent n as shown in BWS case c task m , with q standing for
$B_{qnm c}$ $BW_{(q,j)nm c}$	Scalar, denoting the "utility" (i.e. weight of an attribute or attractive- ness of an attribute level) of item q in the "best" stage for respondent n as shown in BWS task m and BWS type c (i.e. $c = 1$ stands for BWS1 and $c = 2$ stands for BWS2). Scalar, denoting the "utility" difference between item q and item j for respondent n as shown in BWS case c task m , with q standing for the best and j standing for the worst in the pair (q, j) .
$B_{qnm c}$ $BW_{(q,j)nm c}$ δ_i	Scalar, denoting the "utility" (i.e. weight of an attribute or attractive- ness of an attribute level) of item q in the "best" stage for respondent n as shown in BWS task m and BWS type c (i.e. $c = 1$ stands for BWS1 and $c = 2$ stands for BWS2). Scalar, denoting the "utility" difference between item q and item j for respondent n as shown in BWS case c task m , with q standing for the best and j standing for the worst in the pair (q, j) . Scalar, a constant in the utility function for alternative i in SC tasks,
$B_{qnm c}$ $BW_{(q,j)nm c}$ δ_i	Scalar, denoting the "utility" (i.e. weight of an attribute or attractive- ness of an attribute level) of item q in the "best" stage for respondent n as shown in BWS task m and BWS type c (i.e. $c = 1$ stands for BWS1 and $c = 2$ stands for BWS2). Scalar, denoting the "utility" difference between item q and item j for respondent n as shown in BWS case c task m , with q standing for the best and j standing for the worst in the pair (q, j) . Scalar, a constant in the utility function for alternative i in SC tasks, which is generic across respondents and tasks.
$B_{qnm c}$ $BW_{(q,j)nm c}$ δ_i $\delta_{k 1}$	Scalar, denoting the "utility" (i.e. weight of an attribute or attractive- ness of an attribute level) of item q in the "best" stage for respondent n as shown in BWS task m and BWS type c (i.e. $c = 1$ stands for BWS1 and $c = 2$ stands for BWS2). Scalar, denoting the "utility" difference between item q and item j for respondent n as shown in BWS case c task m , with q standing for the best and j standing for the worst in the pair (q, j) . Scalar, a constant in the utility function for alternative i in SC tasks, which is generic across respondents and tasks. Scalar, capturing the mean weight of attribute k in BWS1 tasks,
$B_{qnm c}$ $BW_{(q,j)nm c}$ δ_i $\delta_{k 1}$	Scalar, denoting the "utility" (i.e. weight of an attribute or attractive- ness of an attribute level) of item q in the "best" stage for respondent n as shown in BWS task m and BWS type c (i.e. $c = 1$ stands for BWS1 and $c = 2$ stands for BWS2). Scalar, denoting the "utility" difference between item q and item j for respondent n as shown in BWS case c task m , with q standing for the best and j standing for the worst in the pair (q, j) . Scalar, a constant in the utility function for alternative i in SC tasks, which is generic across respondents and tasks. Scalar, capturing the mean weight of attribute k in BWS1 tasks, which is generic across respondents and tasks.
$B_{qnm c}$ $BW_{(q,j)nm c}$ δ_i $\delta_{k 1}$ $\delta_{k 2}$	Scalar, denoting the "utility" (i.e. weight of an attribute or attractive- ness of an attribute level) of item q in the "best" stage for respondent n as shown in BWS task m and BWS type c (i.e. $c = 1$ stands for BWS1 and $c = 2$ stands for BWS2). Scalar, denoting the "utility" difference between item q and item j for respondent n as shown in BWS case c task m , with q standing for the best and j standing for the worst in the pair (q, j) . Scalar, a constant in the utility function for alternative i in SC tasks, which is generic across respondents and tasks. Scalar, a constant associated with attribute k in BWS2 tasks (only
$B_{qnm c}$ $BW_{(q,j)nm c}$ δ_i $\delta_{k 1}$ $\delta_{k 2}$	Scalar, denoting the "utility" (i.e. weight of an attribute or attractive- ness of an attribute level) of item q in the "best" stage for respondent n as shown in BWS task m and BWS type c (i.e. $c = 1$ stands for BWS1 and $c = 2$ stands for BWS2). Scalar, denoting the "utility" difference between item q and item j for respondent n as shown in BWS case c task m , with q standing for the best and j standing for the worst in the pair (q, j) . Scalar, a constant in the utility function for alternative i in SC tasks, which is generic across respondents and tasks. Scalar, capturing the mean weight of attribute k in BWS1 tasks, which is generic across respondents and tasks. Scalar, a constant associated with attribute k in BWS2 tasks (only apply to the situation where k is a continuous variable).
$B_{qnm c}$ $BW_{(q,j)nm c}$ δ_i $\delta_{k 1}$ $\delta_{k 2}$ η_{nk}	Scalar, denoting the "utility" (i.e. weight of an attribute or attractive- ness of an attribute level) of item q in the "best" stage for respondent n as shown in BWS task m and BWS type c (i.e. $c = 1$ stands for BWS1 and $c = 2$ stands for BWS2). Scalar, denoting the "utility" difference between item q and item j for respondent n as shown in BWS case c task m , with q standing for the best and j standing for the worst in the pair (q, j) . Scalar, a constant in the utility function for alternative i in SC tasks, which is generic across respondents and tasks. Scalar, a constant associated with attribute k in BWS1 tasks, which is generic across respondents and tasks. Scalar, a constant associated with attribute k in BWS2 tasks (only apply to the situation where k is a continuous variable). Describing the standard Normal error term for respondent n and
$B_{qnm c}$ $BW_{(q,j)nm c}$ δ_i $\delta_{k 1}$ $\delta_{k 2}$ η_{nk}	Scalar, denoting the "utility" (i.e. weight of an attribute or attractive- ness of an attribute level) of item q in the "best" stage for respondent n as shown in BWS task m and BWS type c (i.e. $c = 1$ stands for BWS1 and $c = 2$ stands for BWS2). Scalar, denoting the "utility" difference between item q and item j for respondent n as shown in BWS case c task m , with q standing for the best and j standing for the worst in the pair (q, j) . Scalar, a constant in the utility function for alternative i in SC tasks, which is generic across respondents and tasks. Scalar, capturing the mean weight of attribute k in BWS1 tasks, which is generic across respondents and tasks. Scalar, a constant associated with attribute k in BWS2 tasks (only apply to the situation where k is a continuous variable). Describing the standard Normal error term for respondent n and attribute k .
$B_{qnm c}$ $BW_{(q,j)nm c}$ δ_i $\delta_{k 1}$ $\delta_{k 2}$ η_{nk} $\gamma_{k 2}$	Scalar, denoting the "utility" (i.e. weight of an attribute or attractive- ness of an attribute level) of item q in the "best" stage for respondent n as shown in BWS task m and BWS type c (i.e. $c = 1$ stands for BWS1 and $c = 2$ stands for BWS2). Scalar, denoting the "utility" difference between item q and item j for respondent n as shown in BWS case c task m , with q standing for the best and j standing for the worst in the pair (q, j) . Scalar, a constant in the utility function for alternative i in SC tasks, which is generic across respondents and tasks. Scalar, capturing the mean weight of attribute k in BWS1 tasks, which is generic across respondents and tasks. Scalar, a constant associated with attribute k in BWS2 tasks (only apply to the situation where k is a continuous variable). Describing the standard Normal error term for respondent n and attribute k .
$B_{qnm c}$ $BW_{(q,j)nm c}$ δ_i $\delta_{k 1}$ $\delta_{k 2}$ η_{nk} $\gamma_{k 2}$	Scalar, denoting the "utility" (i.e. weight of an attribute or attractive- ness of an attribute level) of item q in the "best" stage for respondent n as shown in BWS task m and BWS type c (i.e. $c = 1$ stands for BWS1 and $c = 2$ stands for BWS2). Scalar, denoting the "utility" difference between item q and item j for respondent n as shown in BWS case c task m , with q standing for the best and j standing for the worst in the pair (q, j) . Scalar, a constant in the utility function for alternative i in SC tasks, which is generic across respondents and tasks. Scalar, capturing the mean weight of attribute k in BWS1 tasks, which is generic across respondents and tasks. Scalar, a constant associated with attribute k in BWS2 tasks (only apply to the situation where k is a continuous variable). Describing the standard Normal error term for respondent n and attribute k .
$B_{qnm c}$ $BW_{(q,j)nm c}$ δ_i $\delta_{k 1}$ $\delta_{k 2}$ η_{nk} $\gamma_{k 2}$	Scalar, denoting the "utility" (i.e. weight of an attribute or attractive- ness of an attribute level) of item q in the "best" stage for respondent n as shown in BWS task m and BWS type c (i.e. $c = 1$ stands for BWS1 and $c = 2$ stands for BWS2). Scalar, denoting the "utility" difference between item q and item j for respondent n as shown in BWS case c task m , with q standing for the best and j standing for the worst in the pair (q, j) . Scalar, a constant in the utility function for alternative i in SC tasks, which is generic across respondents and tasks. Scalar, capturing the mean weight of attribute k in BWS1 tasks, which is generic across respondents and tasks. Scalar, a constant associated with attribute k in BWS2 tasks (only apply to the situation where k is a continuous variable). Describing the standard Normal error term for respondent n and attribute k . Scalar, capturing the baseline marginal attractiveness of the attribute levels of attribute k (only apply to the situation where k is a contin- uous variable)

κ	Matrix, describing the impact of each socioeconomic variable on each
14	Vector describing the impact of each socia demographic variable on
κ_k	the marginal utility of attribute k
) .	Scalar conturing the scale difference between the "best" and the
$\lambda_j _c$	"worst" stage for item <i>i</i> in BWS case <i>c</i> tasks
Τ.	Scalar giving the total number of possible values that attribute k
L_k	scalar, giving the total number of possible values that attribute κ
lln o	Scalar capturing the mean of the underlying Normal distribution for
$\mu_{\mathrm{In}}\beta_k$	Section, capturing the mean of the underlying iterment distribution for β_k .
$\nu_{qjnm c}$	Describing a standard extreme value type I error term operating at
15	the level of the attribute (level) pair of (q, j) for respondent n in BWS
	case c task m .
ω	Matrix, describing the impact of each socio-demographic variable on
	each attribute's corresponding latent attribute importance.
ω_k	Vector, measuring the impact of each socio-demographic variable on
	the latent <i>attribute importance</i> for attribute k .
$\phi_{k_l 2}$	Scalar, denoting the baseline attractiveness of level l for attribute k
	in BWS2 tasks (only apply to the situation where k is a categorical
	variable).
$\sigma_{\mathrm{ln}eta_k}$	Scalar, capturing the standard deviation of the underlying Normal
	distribution for β_k .
au	Vector, describing the impact of each latent <i>attribute importance</i> on
	the corresponding attribute's marginal utility in the SC component.
$ au_k$	Scalar, describing how the marginal utility of attribute k is affected
	by the corresponding <i>attribute importance</i> in the SC component.
U_{int}	Scalar, representing the utility of alternative i derived by respondent
	n in SC task t.
V_{int}	Scalar, representing the systematic utility of alternative i for respon-
	dent n in SC task t .
ε_{int}	Describing the unobserved type I extreme value error of U_{int} .
x_{int}	Vector, explanatory variables representing the K attributes of alter-
	native i as shown to respondent n in SC task t .
x_{intk}	Scalar, the explanatory variable representing attribute k of alterna-
	tive <i>i</i> as shown to respondent <i>n</i> in SC task <i>t</i> .
$x_{knm 2}$	Scalar, denoting the level value that attribute k takes for respondent
Ċ	11 III DW 52 task 11.
ζnk	dente for ettribute k taken by regrendent v
	denot for attribute κ taken by respondent n .

$W_{jnm c}$	Scalar, denoting the "utility" (i.e. weight of an attribute or attractive-
	ness of an attribute level) of item j in the "worst" stage for respondent
	n as shown in BWS type c task m .
y	Matrix, giving the choice for each respondent in each stated choice
	task.
y_{nt}	Scalar, giving the choice by respondent n in stated choice task t .
$\zeta_{ 1}$	Vector, describing the impact of each latent $attribute importance$ on
	the corresponding attribute's weight in the BWS1 component.
$\zeta_{k 1}$	Scalar, describing how the weight of attribute k is affected by the
	corresponding latent <i>attribute importance</i> in the BWS1 component.
$\zeta_{ 2}$	Vector, describing the impact of each latent $attribute importance$ on
	the corresponding attribute levels' attractiveness in the BWS2 com-
	ponent.
$\zeta_{k 2}$	Scalar, describing how the level spacing for attribute \boldsymbol{k} in terms of
	attractiveness is affected by the corresponding latent $attribute impor-$
	tance in the BWS2 component.
Z	Matrix, giving the value of each socio-demographic variable for each
	respondent.
Z_n	Vector, giving the value of each socio-demographic variable for re-
	spondent n .

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