Cosmic variance of $z > 7$ galaxies: prediction from BLUETIDES

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ABSTRACT

In the coming decade, a new generation of telescopes, including JWST and WFIRST, will probe the period of the formation of first galaxies and quasars, and open up the last frontier for structure formation. Recent simulations and observations have suggested that these galaxies are strongly clustered (with large-scale bias $\gtrsim 6$), and therefore have significant cosmic variance. In this work, we use BLUETIDES, the largest volume cosmological simulation of galaxy formation, to directly estimate the cosmic variance for current and upcoming surveys. Given its resolution and volume, BLUETIDES can probe the bias and cosmic variance of $z > 7$ galaxies between magnitude $M_{UV} \sim -16$ and $M_{UV} \sim -22$ over survey areas $\sim 0.1$ arcmin$^2$ to $\sim 10$ deg$^2$. Within this regime, the cosmic variance decreases with survey area/volume as a power law with exponents between $\sim -0.25$ and $\sim -0.45$. For the planned 10 deg$^2$ field of WFIRST, the cosmic variance is between 3 per cent and 10 per cent. Upcoming JWST medium/deep surveys with areas up to $A \sim 100$ arcmin$^2$ will have cosmic variance ranging from $\sim 20$ to 50 per cent. Lensed surveys have the highest cosmic variance $\sim 40$ per cent; the cosmic variance of $M_{UV} \lesssim -16$ galaxies is $\lesssim 100$ per cent up to $z \sim 11$. At higher redshifts such as $z \sim 12$ (14), effective volumes of $\gtrsim 8$ (12 Mpc $h^{-1}$)$^3$ (16 Mpc $h^{-1}$)$^3$ are required to limit the cosmic variance to within 100 per cent. Finally, we find that cosmic variance is larger than Poisson variance and forms the dominant component of the overall uncertainty in all current and upcoming surveys. We present our calculations in the form of simple fitting functions and an online cosmic variance calculator (CV AT COSMIC DAWN) that we publicly release.

Key words: galaxies: high-redshift.

1 INTRODUCTION

The underlying non-linear structure of the Universe and the physics of galaxy formation are imprinted in the abundances of observable galaxies, typically characterized by the galaxy luminosity function (LF) or stellar mass function (SMF). Therefore, a precise measurement of the LF and SMF, and its evolution through cosmic time, is of paramount importance. To this end, there has been significant progress in constraining LFs and SMFs at high redshifts (Duncan et al. 2014; Bouwens et al. 2015; Song et al. 2016; Bouwens et al. 2017; Livermore, Finkelstein & Lotz 2017) using galaxies within the legacy and frontier fields of the Hubble Space Telescope as well as data from Subaru Hyper Suprime Cam. Different parts of the LF can potentially be used to probe different aspects of structure and galaxy formation. For instance, the faint-end ($H \lesssim 33$) measurements coming from lensed surveys can provide constraints on the nature of dark matter (Menci et al. 2016, 2017; Ni et al. 2019). The faint end is also sensitive to modelling of stellar winds (Yung et al. 2019a). On the other hand, the bright end is sensitive to the modelling of active galactic nucleus (AGN) feedback as well as dust extinction (Somerville et al. 2008; Somerville & Davé 2015).

The next generation of infrared surveys such as JWST (Gardner et al. 2006) and WFIRST (Spergel et al. 2015) will reach unprecedented depths, vastly increasing the sizes of high-redshift ($z > 7$) galaxy samples. A major impediment in constraining the LF and SMF comes from the fact that galaxies are not uniformly distributed in space (referred to as galaxy clustering),
2 METHODS

2.1 BLUETIDES simulation

BLUETIDES is a high-resolution cosmological hydrodynamic simulation run until \( z \sim 7.5 \) using the cosmological code MP-GAGDET. With a simulation box size of \((400 \text{ Mpc} h^{-1})^3\) and \(2 \times 7048^3\) particles, BLUETIDES has a resolution comparable to ILLUSTRIS (Nelson et al. 2015), EAGLE (Schaye et al., 2015), and MASSIVEBLACKII (Khandai et al. 2015) but is \( \sim 64 \) times the volume. The cosmological parameters are derived from the 9-yr Wilkinson Microwave Anisotropy Probe (WMAP; Hinshaw et al. 2013) \((\Omega_m = 0.2814, \Omega_r = 0.7186, \Omega_b = 0.0464, c_s = 0.82, h = 0.697, n_s = 0.971)\). The dark matter and gas particles have masses of \(1.2 \times 10^9\) and \(2.36 \times 10^{6}\) M\(_{\odot}\) h\(^{-1}\), respectively. We identify haloes using an FOF Group finder (Davis et al. 1985), and the halo substructure using ROCKSTAR-GALAXIES (Behroozi, Wechsler & Wu 2013). For more details on BLUETIDES, interested readers should refer to Feng et al. (2016).

The various subgrid physics models that have been employed in BLUETIDES include a multiphase model for star formation (Springel & Hernquist 2003; Vogelsberger et al. 2013), molecular hydrogen formation (Krumholz & Gnedin 2011), gas and metal cooling (Katz, Weinberg & Hernquist 1996; Vogelsberger et al. 2014), SNII feedback (Nelson et al. 2015), black hole growth and AGN feedback (Di Matteo, Springel & Hernquist 2005; Springel, Di Matteo & Hernquist 2005), and a model for ‘Patchy’ reionization (Battaglia et al. 2013).

BLUETIDES was targeted towards the high-redshift \((z > 7)\) Universe, with its large volume that captures the statistics of the brightest (rarest) galaxies and quasars. The UV LFs (Feng et al. 2015, 2016; Waters et al. 2016b) are consistent with existing observational constraints (Bouwens et al. 2015). In addition, the predictions are broadly consistent across different hydrodynamic simulations and semi-analytic models (Yung et al. 2019a, b). Clustering properties are also consistent with currently available observations (Bhowmick et al. 2018a). BLUETIDES has also enabled us to build halo occupation distributions (HOD) models for clustering of galaxies in the \(z > 7.5\) regime (Bhowmick et al. 2018b). Photometric properties of high-redshift galaxies and the effect of stellar population synthesis (SPS) modelling as well as dust modelling have been extensively studied in Wilkins et al. (2016a, b, 2018). BLUETIDES has allowed the study of the rare earliest supermassive black holes/first quasars and the role of tidal field in the black hole growth in the early Universe (Di Matteo et al. 2017). Dark matter only realizations have been used to trace their descendants to the present day (Tenneti et al. 2017). We have also been able to make predictions from BLUETIDES (Ni et al. 2018; Tenneti et al. 2019) for the recently discovered highest redshift quasar (Bañados et al. 2018).

The galaxy spectral energy distributions (SEDs) were calculated using the PEGASE-v2 (Fioc & Rocca-Volmerange 1997) SPS models with the stellar initial mass function of Chabrier (2003). The cumulative SED for each galaxy is the sum of the SEDs for each star particle (as a function of stellar age and metallicity). For a complete discussion of the photometric properties of BLUETIDES galaxies, we urge the readers to refer to Wilkins et al. (2016b).

We shall be considering galaxy samples limited by an \(M_{\text{UV}}\) absolute magnitude (denoted by \(M_{\text{UV}}(<)\)), which corresponds to 1600 \(\AA\) in the rest-frame SED of the galaxies. Given its high resolution as well as large volume, BLUETIDES is able to probe the clustering, and therefore the cosmic variance of galaxies with magnitudes ranging from \(M_{\text{UV}} \sim -16\) to \(M_{\text{UV}} \sim -22\). Hereafter, we shall discuss the cosmic variance of galaxies within this magnitude
2.2 Determining cosmic variance

The number of objects $N$ within a field of view with volume $V$ can be described by a probability distribution $P(N|V)$. The cosmic variance ($\sigma_g^2$) can then be defined as

$$\sigma_g^2 = \frac{\langle N^2 \rangle - \langle N \rangle^2 - \langle N \rangle}{\langle N \rangle^2},$$

where the $p$th moment of $P(N|V)$ is given by $\langle N^p \rangle = \sum N^p P(N|V)$. The first two terms in equation (1) represent the total variance in $N$ that includes the contribution from cosmic variance and Poisson variance. The third term represents the Poisson variance that is subtracted to obtain $\sigma_g^2$.

We use the BLUETIDES simulation to determine $\sigma_g^2$ by computing the two-point galaxy correlation function $\xi_{gg}$ of BLUETIDES galaxies and integrating it over the relevant volume, as in Peebles (1980, page 234). $\sigma_g^2$ can be calculated using

$$\sigma_g^2 = \frac{1}{V^2} \int_V \xi_{gg}(r_1, r_2) d^3r_1d^3r_2,$$

where $r_1$ and $r_2$ are position vectors of galaxies integrated over the survey volume. With this approach, we can determine the cosmic variance for survey volumes as large as the BLUETIDES volume. In addition, for survey volumes (e.g. JWST medium/deep surveys and lensed surveys) that are small enough such that a sufficiently large number of them can be extracted from the simulation box, we also determine the full distribution of number counts and analyse the cosmic variance.

We extract a mock survey volume (corresponding to survey Area $A$ and redshift width $\Delta z$) from a single snapshot of BLUETIDES, with median redshift $z_{\text{med}}$. The survey volume $V$ is modelled as a cuboidal box with line-of-sight length determined by the comoving distance between $z \pm \Delta z/2$, and transverse dimensions given by the comoving length subtended by the survey angular size $\sqrt{A}$ at the median redshift.

3 COSMIC VARIANCE OF BLUETIDES GALAXIES

3.1 Clustering of BLUETIDES galaxies

Cosmic variance depends sensitively on how strongly clustered the galaxy population under consideration is; we therefore begin by presenting the clustering power of BLUETIDES galaxies. Fig. 1 shows the two-point correlation functions $\xi(r)$ of galaxies from $r \sim 0.01$ Mpc $h^{-1}$ to $r \sim 400$ Mpc $h^{-1}$. $\xi(r)$ increases with (1) decreasing $M_{UV}$ thresholds (increasing luminosity) at fixed redshift, and (2) increasing redshift at fixed $M_{UV}$ threshold. We note that $\xi(r)$ can be range unless stated otherwise. Note that we do not include a dust correction in the calculation of the magnitudes since its effect is significant only at the very bright end ($M_{UV} \sim -22$ to $\sim -25$) (Feng et al. 2016, fig. 10).
The best-fitting parameters are listed in Table 1. We shall hereafter use these power-law fits to compute the cosmic variance using equation (3).

3.2 Dependence of cosmic variance on survey geometry

Here, we compute the cosmic variance \( \sigma_g \) and study its dependence on the various parameters of the survey.

3.2.1 Survey area

Fig. 2 shows the cosmic variance as a function of survey area. Over areas ranging from \( \sim 1 \) arcmin\(^2\) to \( \sim 1 \) deg\(^2\), the cosmic variance can range from \( \sim 1-2 \) per cent up to \( \geq 100 \) per cent depending on the magnitudes and redshifts of the galaxies. In the next section, we shall discuss in more detail the expected cosmic variance of upcoming surveys.

The dependence of cosmic variance on survey area can be described as a power law

\[
\sigma_g = \Sigma A^\alpha, \tag{4}
\]

where \( \alpha \) is the power-law exponent and \( \Sigma \) is the pre-factor. This is not surprising as the clustering profile of these galaxies could also be described by a power law. The best-fitting values of \( \Sigma \) and \( \beta \) obtained from our results are summarized in Table 1.

We also investigate the dependence on the survey aspect ratio. We report no significant variation of the cosmic variance over aspect ratios ranging from 0.2 to 1 for fixed survey area. However, Moster et al. (2011) showed that for very elongated geometries (survey aspect ratio \(< 0.1\)), the cosmic variance can be reduced by factors \( \sim 5 \). This is due to a larger mean distance between two galaxies detected in such a survey. For a detailed discussion, we refer readers to Moster et al. (2011).

3.2.2 Redshift bin width

Fig. 3 shows the dependence of \( \sigma_g \) on redshift bin width for \( M_{UV} < -16 \) galaxies. As expected, \( \sigma_g \) decreases as \( \Delta z \) increases due to the increase in the comoving volume of the survey. Furthermore, the ratio \( \sigma_g(\Delta z)/\sigma_g(\Delta z_{ref}) \) (where the reference redshift width \( \Delta z_{ref} \) is chosen to be 1 in Fig. 3) has a somewhat universal power-law dependence on \( \Delta z \), independent of magnitude, redshift, and survey type. This behaviour is also reported for \( z < 3 \) galaxies (Moster et al. 2011). We determine the best-fitting power law (shown as the black dashed line) to be

\[
\sigma_g(\Delta z)/\sigma_g(\Delta z_{ref}) = (\Delta z/\Delta z_{ref})^{-0.32}. \tag{5}
\]

3.3 Dependence of cosmic variance on galaxy UV magnitude

We now investigate the dependence of cosmic variance on absolute UV magnitude. We shall present results for survey geometries most relevant to upcoming deep surveys within JWST and WFIRST. They also cover a wide range of existing surveys that are listed in Table 3.

3.3.1 JWST- and WFIRST-like volumes

Fig. 4 shows the cosmic variance \( \sigma_g \) as a function of \( M_{UV} \) threshold at the redshift snapshots 7.5–14. The areas are representative of planned WFIRST (1–10 deg\(^2\)) deep surveys as well as JWST (10–100 arcmin\(^2\)) medium/deep surveys such as JADES and CEERS survey. We show redshift widths \( \Delta z \sim 1 \) as the photometric redshift uncertainties are expected to be significant. For the 1, 10 arcmin\(^2\), and 1 deg\(^2\) survey, we also present the estimates from the full distribution of number counts for an ensemble of simulation subvolumes; we find that these estimates are in reasonable agreement with those computed by integrating the correlation functions.

We see that the cosmic variance increases with decreasing \( M_{UV} \) at fixed redshift, which is expected since brighter galaxies are more strongly clustered (Park et al. 2017; Blomqvist et al. 2018a,b). The scaling of the cosmic variance with respect to \( M_{UV} \) can range from \( \sim |M_{UV}|^2 \) to \( \sim |M_{UV}| \) for \( M_{UV} \) between \( -16 \) and \( -20 \). For the more luminous galaxies with \( M_{UV} \) between \( -20 \) and \( -22 \), the scaling is steeper, particularly at \( z \sim 10–14 \). The redshift dependence (at fixed UV magnitude) of the cosmic variance is driven by the evolution of the galaxy clustering (increases with redshift) as well as comoving survey volume (increases with redshift for fixed survey geometry), wherein the former tends to increase and the latter tends to decrease the cosmic variance; for \( M_{UV} \) between \( -16 \) and \( -20 \) the two effects roughly cancel each other, leading to very marginal redshift dependence. For \( M_{UV} < -20 \), the cosmic variance increases with redshift since the clustering evolution becomes more pronounced, and becomes more important than the redshift dependence of the comoving survey volume.
We now broadly summarize the cosmic variance predictions for the various survey areas. For the 10 and 1 deg$^2$ fields spanning the areas for the planned WFIRST deep surveys, the cosmic variance is $\sim 3$–$10$ per cent for the entire range of $M_{UV}$ at $z = 7.5$–$9$; at higher redshifts ($z \sim 9$–$14$), the cosmic variance is $\sim 3$–$10$ per cent for $M_{UV}$ between $-16$ and $-20$, but can exceed $\sim 10$ per cent for galaxies with $M_{UV} < -20$. The cosmic variance is significantly higher for 100 and 10 arcmin$^2$ fields that span the areas for upcoming JWST medium/deep surveys. For a 100 arcmin$^2$ field, the cosmic variance is between 20 and 50 per cent for UV magnitudes between $-16$ and $-20$. For a 10 arcmin$^2$ field, the cosmic variance ranges from 30 to 70 per cent for $M_{UV}$ between $-16$ and $-18$ up to $z \sim 12$. For $z > 12$, the cosmic variance within a 10 arcmin$^2$ field is $\sim 100$ per cent for the entire range of UV magnitudes between $-16$ and $-22$.

We now cast these results in terms of the overall uncertainties in the expected number counts, which are summarized in Table 2. In a 10 deg$^2$ survey within WFIRST, we predict $\sim 50,000$ galaxies at $z \sim 7.5$ up to depths of $H < 27.5$ ($M_{UV} \lesssim -19.6$) wherein the uncertainty due to cosmic variance amounts to $\sim \pm 2500$ galaxies; at $z \sim 11$, we expect $\sim 170 \pm 7$ galaxies. In a 1 deg$^2$ survey within WFIRST, we predict $\sim 10,000 \pm 800$ galaxies at $z \sim 7.5$ up to depths of $H < 28.5$ ($M_{UV} \lesssim -18.6$); at $z \sim 11$, we predict $\sim 85 \pm 10$ galaxies. For an area of $\sim 100$ arcmin$^2$ that broadly represents the JADES-deep and CEERS surveys, we expect to detect $\sim 2200 \pm 450$ galaxies.
Cosmic variance of $z > 7$ galaxies

Figure 4. Filled circles show the cosmic variance as a function of $M_{UV}$ threshold for various survey areas ($A$) with $\Delta z = 1$. The filled data points are computed by integrating the correlation function. The open data points for $A = 1$ arcmin$^2$, 10 arcmin$^2$, and 1 deg$^2$ are computed from the full distribution of number counts of galaxies for an ensemble of simulation subvolumes (representing survey volumes). The dotted lines are estimates provided by CV AT COSMIC DAWN.

with $M_{UV} < -16$ at $z \sim 7.5$; likewise, at $z \sim 11$, we expect to detect $\sim 150 \pm 45$ galaxies.

Lastly, we also look at the relative importance between the uncertainty due to cosmic variance and Poisson variance. In Fig. 5, we show the ratio between cosmic variance and the Poisson variance, as a function of the number counts of galaxies for a range of redshifts, $M_{UV}$ thresholds, and survey areas. We see that as we increase the number counts, the importance of cosmic variance (relative to Poisson variance) increases. Additionally, at fixed number count, a 1 deg$^2$ survey (star shaped points) has a lower cosmic variance (relative to Poisson variance) compared to the 10, 100 arcmin$^2$ surveys. Most importantly, we find that (apart from the obvious exception of very low galaxy number counts i.e. $N \lesssim 10$), the uncertainty due to cosmic variance largely dominates over the Poisson variance.

**Encountering rare luminous galaxies and environments in upcoming JWST medium/deep surveys:** For the JWST medium/deep surveys (CEERS, JADES-medium/deep), the BLUETIDES volume is large enough to produce $\gtrsim 1000$ realizations. This enables us to construct the full distribution of the predicted number counts of galaxies within these surveys (in addition to the mean and cosmic variance, which only provides the first and second moments of the underlying distributions). We are therefore also able to probe the likelihood of encountering extreme (several standard deviations away from the mean) overdense/underdense regions within these surveys. Fig. 6 shows the normalized probability distributions of overdensity of galaxies. Here, we choose to show galaxies with $M_{UV} < -16$, but the distributions (when presented in the units of the standard deviations) do not significantly change for $M_{UV}$ between $-16$ and $-19$ (approximate range of detection limits of the JWST medium/deep surveys). Also note that there is no significant redshift evolution of these distributions (when presented in the units of the standard deviations). The distributions of JADES deep (lower panel) are slightly broader than that of JADES medium (upper panel); this is expected due to lower volume of JADES deep compared to JADES medium. We find that the likelihood of these surveys to fall on underdense/overdense regions $2\sigma$’s away from the mean is $\sim 5–10$ per cent. BLUETIDES contains no underdense (void) regions with densities lower than $2\sigma$’s away from the mean. On the other hand, the most overdense regions found in BLUETIDES, correspond to $\sim 3\sigma$’s away from the mean; the likelihood of these extremely overdense regions to be encountered by a JWST medium/deep survey, is about 0.1–1 per cent.

The large volume of BLUETIDES also allows us to probe the likelihood of a (chance) detection of rare luminous ($M_{UV} < -22$) galaxies within the JWST medium/deep surveys. We had so far
not discussed these objects in Fig. 2 because their clustering (and cosmic variance) could not be accurately probed due to excessive shot noise. Here, we simply quantify the likelihood of their detection by determining the fraction of survey realizations within BLUETIDES that contain these bright outliers. Fig. 7 shows the overall probability of getting detected for redshifts up to \( \sim 7.5 \) as a function of redshift for absolute UV magnitude thresholds \( M_{\text{UV}} \). Fig. 9 shows the cosmic variance as a function of volume for redshifts 7.5–14 up to UV magnitudes of \( \sim 16 \). We do not focus on galaxies fainter than \( M_{\text{UV}} \sim 16 \) as their statistics may be affected by limited particle resolution; we however note that current and future lensed surveys can reach up to \( \sim 2–3 \) magnitudes fainter.

In order to estimate the cosmic variance for these lensed surveys, we consider simulation subvolumes over the range of \((\sim 6–15 \text{ Mpc} h^{-1})^3\), based on the effective volume \( (V_{\text{eff}}) \) estimates made by Livermore et al. (2017) using lensing models (Bradač et al. 2009; Jauzac et al. 2015; Kawamata et al. 2016 and references therein). Fig. 9 shows the cosmic variance as a function of volume for redshifts 7.5–14 up to UV magnitudes of \( \sim 16 \). We do not focus on galaxies fainter than \( M_{\text{UV}} \sim 16 \) as their statistics may be affected by limited particle resolution; we however note that current and future lensed surveys can reach up to \( \sim 2–3 \) magnitudes fainter. We present the results for two different geometries (at fixed volume) i.e. ‘pencil beam’ like geometries assuming a redshift uncertainty of \( \Delta z = 1 \) (solid lines), and cubic geometries (dashed lines). We see that the cosmic variance is \( \sim 40 \) per cent or higher across the entire range of magnitudes and redshifts. Additionally, there are also conditions (high enough luminosity, redshift, or small enough volume) when the cosmic variance can exceed 100 per cent, in which case the measurements are of limited value for providing constraints on the underlying physics. We therefore identify regimes under which the cosmic variance is contained within \( \sim 100 \) per cent. We primarily focus on \( M_{\text{UV}} < 16 \) (blue line) and \( M_{\text{UV}} < 18 \) (red line) since these surveys are primarily targeting the faint end of the LF. We shall first summarize the results for the pencil beam geometries: for \( M_{\text{UV}} < 16 \), the cosmic variance is below \( \sim 100 \) per cent for the entire range of effective volumes up to \( z \sim 11 \). At higher redshifts, to keep the cosmic variance of \( M_{\text{UV}} < 16 \) galaxies below 100 per cent, the volumes required are \( \gtrsim (8 \text{ Mpc} h^{-1})^3 \) for \( z \sim 12 \), \( \gtrsim (10 \text{ Mpc} h^{-1})^3 \) for \( z \sim 13 \), and \( \gtrsim (12 \text{ Mpc} h^{-1})^3 \) for \( z \sim 14 \). Likewise, for \( M_{\text{UV}} < 18 \) galaxies, the cosmic variance is below...
We use the results of the previous two sections to construct a cosmic variance estimator for $z > 7$ galaxies.

We use the fitting results summarized in Table 1 and equation (5) to compute cosmic variances for $M_{UV} < -21$ galaxies. For the redshifts and $M_{UV}$ thresholds that lie in between those listed in Table 1, we use linear interpolation to estimate the cosmic variance. Cosmic variance estimates made using CV_AT_COSMIC_DAWN are shown as dotted lines in Fig. 4.

We use CV_AT_COSMIC_DAWN to summarize our results as a 2D colour plot (Fig. 9) on the $A - M_{UV}(<)$ plane. We also present our estimates in terms of the apparent magnitude in Appendix A. For $M_{UV}$ thresholds that lie in between those listed in Table 1, the cosmic variance ranges from $\delta \sigma \sim 0.01$ to $\delta \sigma \sim 10$ and is represented by pixels coloured as blue to red, respectively. The solid black lines show contours representing $\delta \sigma \sim 0.1, 0.3, 1, 3,$ and 10. We show all the recent and upcoming surveys listed in Table 3 as various points on the plane positioned approximately by their survey area and depth.

3.5 Implications for galaxy luminosity functions: contribution of cosmic variance to total uncertainty

We now study the impact of cosmic variance on the galaxy LF. In Fig. 10, we compute the LF and the associated cosmic variance and total = cosmic + Poisson variance for various survey areas. The open and black points show current observational constraints. The cosmic variance, shown by the shaded regions, reflects the trends seen in Fig. 4, and is broadly consistent with uncertainties in observational measurements which typically include cosmic variance estimates.

The bottom panels show the fraction ($\delta \sigma$) of the total uncertainty that is contributed by cosmic variance. For fixed magnitude, we see that as survey area decreases, $\delta \sigma$ decreases. Likewise, for fixed survey area, we see that as galaxies become brighter, $\delta \sigma$ decreases. This is expected since number counts decrease with increasing luminosity, which increases the contribution from Poisson variance. Furthermore, we see that $\delta \sigma > 50$ per cent, implying that cosmic variance is the more dominant contribution to the overall uncertainty as compared to Poisson variance, the only exceptions being samples with very small ($\lesssim 10$) number counts (as also seen in Fig. 5).
A. K. Bhowmick et al.

Figure 8. Cosmic variance in lensed surveys: $\sigma_{\text{galaxy}}$ is the cosmic variance as a function of volumes for lensed surveys for various $M_{UV}$ thresholds. We consider a range of volumes ($V_{\text{eff}}$) based on effective volumes of HST Frontier fields surveys (Koekemoer et al. 2017) as computed in fig. 10 of Livermore et al. (2017). The solid and dashed lines have the same total survey volume, but have different geometries. The solid lines correspond to pencil beam like geometries with $\Delta z = 1$. The dashed lines, on the other hand, correspond to cubic geometries.

4 POSSIBLE UNCERTAINTIES IN THE COSMIC VARIANCE ESTIMATES

Our cosmic variance estimates are subject to uncertainties, particularly because the estimates are based on a single hydrodynamic simulation run with a fixed cosmology and galaxy formation modelling. The cosmic variance estimates depend on cosmology due to its effect on the halo bias and matter clustering, as well as the comoving survey volume. For instance, between WMAP (Hinshaw et al. 2013) and PLANCK (Planck Collaboration XIII 2016) cosmologies, the comoving survey volume changes by $\sim 15$ per cent; the matter clustering changes by $\sim 4$–10 per cent (depending on the length-scale) and the halo bias (based on the Tinker et al. 2010 model) changes by $\sim 0.5$–3 per cent (depending on the halo mass scale). Adding these contributions up, we can overall expect a difference of $\sim 25$–30 per cent between cosmic variances $\sigma_{\varepsilon}$ predicted by the WMAP and PLANCK cosmologies. Additionally, uncertainties in the galaxy formation physics can also affect our cosmic variance estimates. In particular, a given sample of galaxies can populate haloes of different masses in different recipes of galaxy formation, thereby affecting the clustering amplitudes. For example, if the star formation within a galaxy sample is extremely ‘bursty’ or ‘episodic’, they may reside within a relatively small fraction of lower mass (more abundant) haloes, compared to a model that does not lead to bursty star formation. This will lead to lower clustering amplitude (for a fixed number density or LF). Finally, we make several approximations in computing the cosmic variance: we use cuboidal volumes through the box with fixed transverse extent, rather than light-cones, and do not include the time evolution across the redshift interval. We expect that the errors due to these approximations will not significantly affect our predictions.

5 SUMMARY AND CONCLUSIONS

In this work, we used the recent BLUETIDES simulation to estimate the cosmic variance for $z > 7$ galaxies to be detected by the planned deep surveys of JWST and WFIRST. Cosmic variance is expected to be a significant, potentially dominant source of uncertainty given the exceptionally strong clustering power (galaxy bias $\gtrsim 6$) of these galaxies seen in recent observations. We express the cosmic variance as an integral of the two-point correlation function over the survey volume, as commonly done in the literature (Peebles 1980; Moster et al. 2011).

The resolution and volume enables BLUETIDES to probe the large-scale bias, and therefore the cosmic variance of $z > 7$ galaxies with $M_{UV} \sim -16$ to $M_{UV} \sim -22$ over survey areas $\sim 0.1$ arcmin$^2$ to $\sim 10$ deg$^2$. Within this regime, the cosmic variance has a power-law dependence on survey volume (with exponent $\sim -0.25$ to $-0.45$). More luminous galaxies have larger cosmic variance than faint galaxies.

The above trends can be put in the context of upcoming deep surveys. The largest planned deep survey will naturally suffer from the least amount of cosmic variance; this corresponds to the 10 deg$^2$ field of WFIRST, which will have a cosmic variance ranging from $\sim 3$ to 10 per cent, except for $M_{UV} < -22$ galaxies at $z > 12$ where the cosmic variance can exceed $\sim 10$ per cent. Upcoming JWST medium/ deep surveys (up to areas of 100 arcmin$^2$) will have a cosmic variance of about 20–50 per cent for $M_{UV}$ between $-16$ and $-20$. At the other end, the smallest surveys are the lensed surveys (Hubble Frontier fields) and are most susceptible to cosmic variance. They have cosmic variance $\gtrsim 40$ per cent over the entire range of magnitudes and redshifts. These are the only existing surveys that can probe the faint ($M_{UV}$ thresholds...
Figure 9. The colour map shows the cosmic variance as a function of threshold $M_{UV}$ magnitude and survey area $A$ as calculated by CVAT COSMIC DAWN. The solid black lines show contours representing $\sigma_g \sim 0.1, 0.3, 1, 3,$ and $10$. We show upcoming (JWST, WFIRST) and current (HUDF, SDF, CANDELS) surveys at various points on the plane positioned approximately by their survey area and limiting $H$-band magnitude (converted to $M_{UV}$). We also show upcoming (JWST lensed) and current (Hubble and Subaru Frontier fields) lensed surveys collectively as ‘Lensed surveys’. The left arrow indicates that the limiting magnitudes for the lensed surveys may be 3–4 magnitudes fainter than the faintest galaxies BLUEFINDES can probe.
Table 3. List of upcoming and current high-redshift surveys using WFIRST, JWST, Hubble space telescope (HST), Hyper Suprime Cam (HSC), and Cosmic Assembly Near infrared Extragalactic Survey (CANDELS). HUDF refers to Hubble Ultra Deep Field and SDF refers to Subaru Deep Field. $H(<)$ is the detection limit in the $H$ band of WFIRST.

<table>
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<td>$\sim$28.5</td>
<td>McCracken et al. (2012)</td>
</tr>
<tr>
<td>JADES-medium</td>
<td>JWST</td>
<td>$\sim$190 arcmin$^2$</td>
<td>$\sim$29.7</td>
<td>JADES survey overview</td>
</tr>
<tr>
<td>JADES-deep</td>
<td>JWST</td>
<td>$\sim$46 arcmin$^2$</td>
<td>$\sim$30.6</td>
<td>JADES survey overviews</td>
</tr>
<tr>
<td>CEERS</td>
<td>JWST</td>
<td>$\sim$100 arcmin$^2$</td>
<td>$\sim$29</td>
<td>Finkelstein et al. (2017)</td>
</tr>
<tr>
<td>HUDF</td>
<td>HST</td>
<td>$\sim$10 arcmin$^2$</td>
<td>$\sim$27</td>
<td>Rafelski et al. (2015)</td>
</tr>
<tr>
<td>GOODS</td>
<td>HST</td>
<td>$\sim$160 arcmin$^2$</td>
<td>$\sim$27.7</td>
<td>Grogin et al. (2011)</td>
</tr>
<tr>
<td>COSMOS</td>
<td>HST</td>
<td>$\sim$2 deg$^2$</td>
<td>$\sim$25.5</td>
<td>Grogin et al. (2011)</td>
</tr>
<tr>
<td>UDS</td>
<td>HST</td>
<td>$\sim$0.8 deg$^2$</td>
<td>$\sim$25</td>
<td>Grogin et al. (2011)</td>
</tr>
<tr>
<td>SDF</td>
<td>HSC</td>
<td>$\sim$34. arcmin$^2$</td>
<td>$\sim$27.5</td>
<td>Kashikawa et al. (2004)</td>
</tr>
</tbody>
</table>

Figure 10. Top panels: $\Phi$ is the rest-frame UV LF. Different colours represent galaxies within simulation sub-volumes corresponding to different survey areas with $\Delta z = 1$. For each colour, the shaded region corresponds to uncertainty due to cosmic variance. For each colour, the dashed lines are upper and lower limits representing the total field to field variance (cosmic variance + Poisson variance). Bottom panels: $\delta_{\sigma}$ is the ratio between the cosmic variance and the total field-to-field variance. Open stars (Livermore et al. 2017), open squares (Ishigaki et al. 2018), open diamonds (Bouwens et al. 2015), open circles (Laporte et al. 2012), filled stars (Bouwens et al. 2015), filled diamonds (McLeod, McLure & Dunlop 2016), and filled squares (Oesch et al. 2018) are observational measurements from current deep and lensed fields.
between $\sim-13$ and $-16$) end of the LF. In order for these measurements to provide useful constraints (e.g. on the nature of dark matter), the cosmic variance must be contained within 100 per cent. For $M_{\text{UV}}$ thresholds up to $-16$, the cosmic variance is within 100 per cent for $z \sim 7$–11 for the entire range of effective volumes between $\sim 6$ and 14 (Mpc$^{-3}$h$^{-3}$). At higher redshifts, effective volumes of $\geq 8$ (Mpc$^{-3}$h$^{-3}$) and $\geq 12$ (Mpc$^{-3}$h$^{-3}$) at $z \sim 12$ and $z \sim 14$, respectively, to keep the cosmic variance within 100 per cent.

Lastly, we study the impact of cosmic variance on the LF and estimate the contribution of cosmic variance to the total uncertainty. We find that across all redshifts and magnitude bins (with the exception of the most luminous bins with number counts $\lesssim 10$ objects), cosmic variance is the more dominant component of the uncertainty, as compared to Poisson variance.

We capture our results in the form of simple fitting functions and encode them in an online cosmic variance calculator (CV_AT_COSMIC_DAWN) that we publicly release.

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APPENDIX A: PRESENTING COSMIC VARIANCE IN TERMS OF TELESCOPE SURVEY PARAMETERS

In addition to presenting cosmic variance as a function of the rest-frame intrinsic UV magnitude, it is also useful (for observers in particular) to present our estimates directly in terms of the apparent magnitude, which is fixed for a given survey. We therefore, in Fig. A1, also present our estimates in terms of the apparent magnitude. We choose the $H$-band magnitude of WFIRST, and present our estimates up to redshift 10.

Figure A1. The colour map shows the cosmic variance as a function of $H$-band (within WFIRST) magnitude and survey area $A$ as calculated by $\text{CV}_{\text{AT}} \cdot \text{COSMICDAWN}$. The solid black lines show contours representing $\sigma_g \sim 0.1, 0.3, 1, 3, 10$. We show upcoming (JWST, WFIRST) and current (HUDF, SDF, CANDELS) surveys at various points on the plane positioned approximately by their survey area and limiting $H$-band magnitude. We also show upcoming (JWST lensed) and current (Hubble and Subaru Frontier fields) lensed surveys collectively as ‘Lensed surveys’. The left arrow indicates that the limiting magnitudes for the lensed surveys may be 3–4 magnitudes fainter than the faintest galaxies BLUETIDES can probe.

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