

1 **A miniature triaxial apparatus for investigating the micromechanics of**
2 **granular soils with in-situ X-ray micro-tomography scanning**

3
4 Z. Cheng¹, J.F. Wang^{2,3}, M.R. Coop⁴ and G.L. Ye⁵

5
6 ¹ Ph.D., Research Associate

7 Department of Architecture and Civil Engineering,
8 City University of Hong Kong, Tat Chee Avenue, Kowloon, Hong Kong

9
10 ²Associate Professor (Corresponding Author)

11 Department of Architecture and Civil Engineering,

12 City University of Hong Kong, Hong Kong

13 Tel: (852) 34426787, Fax (852) 34420427

14 E-mail: jefwang@cityu.edu.hk

15 Address: B6409, Academic 1, City university of Hong Kong,

16 Tat Chee Avenue, Kowloon, Hong Kong

17 ³Shenzhen Research Institute of City University of Hong Kong, Shenzhen, China

18
19
20 ⁴Professor

21 Department of Civil, Environmental and Geomatic Engineering,

22 University College London, Gower Street, London, UK

23
24 ⁵Professor

25 Department of Civil Engineering,

26 Shanghai Jiaotong University,

27 Dongchuan Road, Minhang District, Shanghai, China

29 **Abstract:** The development of a miniature triaxial apparatus is presented. In conjunction with an
30 X-ray micro-tomography (termed as X-ray μ CT hereafter) facility and advanced image
31 processing techniques, this apparatus can be used for in-situ investigation of the micro-scale
32 mechanical behavior of granular soils under shear. The apparatus allows for triaxial testing of a
33 miniature dry sample with a size of 8×16 mm (diameter \times height). In-situ triaxial testing of a
34 0.4~0.8 mm Leighton Buzzard sand (LBS) under a constant confining pressure of 500 kPa is
35 presented. The evolutions of local porosities (i.e., the porosities of regions associated with
36 individual particles), particle kinematics (i.e., particle translation and particle rotation) of the
37 sample during the shear are quantitatively studied using image processing and analysis
38 techniques. Meanwhile, a novel method is presented to quantify the volumetric strain distribution
39 of the sample based on the results of local porosities and particle tracking. It is found that the
40 sample, with nearly homogenous initial local porosities, starts to exhibit obvious inhomogeneity
41 of local porosities and localization of particle kinematics and volumetric strain around the peak
42 of deviatoric stress. In the post-peak shear stage, large local porosities and volumetric dilation
43 mainly occur in a localized band. The developed triaxial apparatus, in its combined use of X-ray
44 μ CT imaging techniques, is a powerful tool to investigate the micro-scale mechanical behavior of
45 granular soils.

46 **Key words:** Triaxial apparatus; X-ray μ CT; in-situ test; micro-scale mechanical behavior;
47 granular soils

48

49 **1 Introduction**

50 Micro-scale mechanical behavior (e.g., particle crushing and particle rearrangement) plays a very
51 important role in the macro-scale mechanical behavior of granular soils. Evidence has shown that
52 by changing particle size distribution and pore structures, particle crushing and particle
53 rearrangement lead to significant settlement and change of hydraulic conductivity in engineering
54 where stress levels are high; for example, driven piles and high rock-fill dams [1-3]. It has been
55 found that shear-induced dilation and strain softening tend to occur in dense sands under low
56 confining pressures, because of particle rearrangement in the shear band. Meanwhile, shear-
57 induced compression and strain hardening are likely to appear in loose sands under high
58 confining pressures due to particle crushing [4, 5]. The critical state of a loaded sand in which
59 particle crushing takes place can also be interpreted as an equilibrium state between the dilation
60 caused by particle rearrangement and the compression caused by particle crushing [6]. Therefore,
61 investigation into the micro-scale mechanical behavior is of great importance for achieving a full
62 understanding of the macro-scale mechanical behavior, and for developing advanced constitutive
63 models incorporating the corresponding micromechanical mechanisms.

64 Conventional and advanced triaxial apparatuses have been widely used to evaluate the shear
65 strength and stiffness of granular soils. However, because of the inability to distinguish and
66 characterize individual grains inside a sample in triaxial testing, they cannot be used
67 independently to study the micro-scale mechanical behavior (e.g., grain rearrangement and grain
68 morphology change) of granular soils. Recently, advanced apparatuses have been developed to
69 measure the grain-scale friction coefficients and stiffness, which provides important
70 experimental support for the discrete element modeling (DEM) of micro-scale mechanical
71 behavior of granular materials [7, 8]. DEM was first introduced into the geotechnical field by

72 Cundall and Strack [9], who modeled each soil particle with a single circle (or sphere). Their
73 model could reproduce the overall macro-scale mechanical behavior of granular soils but led to
74 over-rotation of particles, because the simplified model did not take into consideration the effects
75 of particle shape. Although the efforts made during the last two decades have helped to achieve
76 more realistic particle rotation in DEM modeling [10-17], the modeling of real particle rotation
77 requires the incorporation of real particle shapes and the development of sophisticated contact
78 models, which makes the calculation highly intensive.

79 The development of optical equipment and imaging techniques (e.g., the microscope, laser-aided
80 tomography, X-ray computed tomography (termed as X-ray CT hereafter) and X-ray μ CT) has
81 provided many opportunities for experimental examination of the micro-scale mechanical
82 behavior of granular soils. Via acquisition and analysis of images of soil samples in triaxial
83 testing, these equipment and techniques have been increasingly used in the investigation of soil
84 microstructures [18-24]. These studies have enhanced the understanding of the micro-scale
85 mechanical behavior of granular soils. However, in most of these studies, images were acquired
86 before and after testing, which only allows for the interpretation of the micro-scale mechanical
87 behavior in two loading states (i.e., prior to and after tests). To capture the full micro-scale
88 mechanical behavior of granular soils, image acquisition should be carried out throughout the
89 tests, which requires the development of an apparatus for in-situ testing. Here, in-situ testing
90 refers to CT scanning and image acquisition at the same time of triaxial testing. In recent years,
91 only a very limited number of triaxial devices have been designed for use in conjunction with X-
92 ray CT (or μ CT) to conduct in-situ triaxial tests [25-32]. These devices have been used for
93 investigating the micro-scale characteristics changes within granular materials throughout tests
94 (e.g., void ratios, strain distribution, particle kinematics and inter-particle contacts). Specifically,

95 in its combined use of advanced image processing and analysis techniques such as digital image
96 correlation (DIC) techniques, in-situ testing allows the experimental measurement of strain
97 distribution of soils [32, 33]. Thus, the in-situ testing triaxial apparatus has become a powerful
98 tool to unravel the micro-mechanism of failure of soils subjected to loading.

99 This paper presents the development of a novel miniature apparatus for in-situ triaxial testing.
100 The detailed design of this apparatus is presented to facilitate the building of such an apparatus to
101 conduct micromechanical experiments on soils. A main advantage of this apparatus, over many
102 of the currently existing apparatuses for in-situ triaxial testing, is its high confining pressure
103 capacity (i.e., up to 2,000 kPa). Meanwhile, a novel method is presented to quantify the strain
104 localization of granular soils. In the following context, we first introduce the principle of X-ray
105 CT (or μ CT) and the main considerations for applying it to in-situ triaxial testing. Subsequently,
106 the detailed design of this apparatus is described. Finally, a demonstration triaxial test is carried
107 out on a uniformly graded sample of Leighton Buzzard sand (LBS). The evolutions of local
108 porosities, particle kinematics and volumetric strain distribution of the sample throughout the test
109 are quantitatively studied, and the results are then presented.

110 **2 X-ray CT (μ CT) and in-situ triaxial test apparatus**

111 X-ray CT (or μ CT) has been widely used to scan 3D CT images of objects. An X-ray CT (or
112 μ CT) facility is generally composed of an X-ray source, a rotation stage and a detector. Fig. 1
113 shows a schematic of a typical parallel beam X-ray μ CT facility used for imaging a sample.
114 During operation of the setup, the sample is rotated by the rotation stage across 180° (or 360°)
115 to acquire a series of 2D projections at different angles. These 2D projections are then used to
116 reconstruct a 3D CT image of the sample.

117 The 3D CT image is determined according to the attenuation coefficient distribution of the
118 sample, based on Beer's law. According to Beer's law, for monochromatic X-rays passing
119 through an object, there is an exponential relationship between the ratio of the emitted X-ray
120 intensity I_0 to the detected X-ray intensity I , and the multiplication of attenuation coefficients u_i
121 with thickness d_i , given by:

$$122 \quad \frac{I_0}{I} = \exp(\sum u_i d_i), \quad (1)$$

123 where d_i is the material thickness (i.e., the thickness of material i within which the attenuation
124 coefficient u_i is constant) of the object along the path of the X-rays.

125 A series of such equations can be obtained according to the 2D projections at different angles. A
126 solution to these equations gives the attenuation coefficient distribution, used to determine the
127 intensity values of a CT image of the sample. Different materials generally have different
128 intensity values in a CT image due to their respective attenuation coefficients, which are closely
129 related to their densities. For example, with respect to intensity values soil particles are higher
130 than water, and water is higher than air.

131 To make use of these properties in in-situ triaxial testing, apparatuses are generally fixed on the
132 rotation stage when they supply loads to samples. A triaxial apparatus for use with an X-ray CT
133 (or μ CT) facility generally differs from the conventional triaxial apparatus as follows. Firstly, the
134 apparatus should be very light so that it falls within the loading capacity of the rotation stage of
135 the X-ray CT (or μ CT) facility. Secondly, the X-ray CT (or μ CT) facility does not allow the
136 triaxial apparatus to have any tie bars around the confining chamber, as these tie bars would
137 obstruct the X-ray beam. Finally, the sample should be small enough to ensure that it remains
138 within the scanning area during the rotation.

139 Because of the particular requirements (e.g., weight limitations due to the loading capacity of the
140 rotation stages, and geometric restrictions) of the X-ray CT (or μ CT) facilities, a light and highly
141 transparent acrylic, Plexiglas or polycarbonate cell is usually used to provide a confining
142 pressure to a sample. For example, Otani and colleagues [29] adopted an acrylic cylindrical cell
143 in their triaxial apparatus which has a spatial resolution of 200 μ m and a confining stress
144 capacity of 400 kPa for samples with a size of 50 \times 100 mm (diameter \times height). To acquire a
145 higher spatial resolution and a full-field scanning of samples, some authors [26, 31] used a
146 smaller-sized cell (high-spatial resolution X-ray μ CT scanners generally have a very small
147 scanning area), in which a much higher confining pressure capacity is also achieved. These
148 features allow the in-situ triaxial testing of granular soils under high confining pressure, and
149 imaging and characterization of their breakage behavior with high spatial resolution. For this
150 purpose, a similar small-sized triaxial cell is adopted in the apparatus presented in the following
151 sections.

152 **3 Triaxial apparatus design**

153 **3.1 Schematic of triaxial apparatus**

154 A miniature triaxial system is specially fabricated to incorporate the features stated in Section 2
155 for use with the X-ray μ CT scanner at SSRF. Figs. 2(a) and 2(b) schematically show the triaxial
156 system and a photograph of the apparatus, respectively. As shown in Fig. 2(a), similar to the
157 conventional triaxial system, this triaxial system comprises an axial loading device (i.e., the
158 stepping motor and the screw jack), a confining pressure offering device (i.e., the chamber and
159 the GDS pressure controller) and a data acquisition and controlling system. Note that the triaxial
160 system is used for testing dry samples, and the back pressure valve is used to create suction

161 inside samples in the sample preparation process. In the current paper, triaxial test of dry samples
162 is used to explore the soil mechanical behavior under drained shear conditions. Meanwhile, the
163 measurement of sample volume change with high-resolution X-ray μ CT also allows the absence
164 of water within the sample. Furthermore, the absence of water will also reduce the technical
165 difficulty of image processing and analysis. For these reasons, dry samples are used. The
166 apparatus shown in Fig. 2(b) is about 520 mm in height and 20 kg in weight. The sample size
167 required for the apparatus is 8×16 mm (diameter \times height), and is dictated by consideration
168 of the use of high spatial resolution and the representativeness of a sample, which requires an
169 adequate number of grains inside. While the X-ray μ CT scanner at SSRF can offer a high spatial
170 resolution of up to several microns (e.g., $6.5 \mu\text{m}$), it has a rather small scanning area (e.g., 11
171 mm in width and 4.888 mm in height). However, the representativeness of a sample requires that
172 the sample-to-size ratio (i.e., the ratio of specimen diameter to maximum particle size) is larger
173 than six [34, 35]. Note that the use of small sample size may influence the macro-scale
174 mechanical response of the material [36, 37]. It was shown in a comprehensive DEM study by
175 Wang and Gutierrez [36] that as long as a uniform shear banding across the entire sample
176 dimension (i.e., no progressive shear failure) occurs, the sample size can be regarded to be
177 acceptable and the boundary-measured stress-strain curve is representative of the true shear
178 strength of the granular material and does not contain artificial lateral boundary effects. There is
179 no clear evidence of progressive failure within the sample in this study, as will be shown in
180 Section 4. Therefore, its boundary effects are not considered to be significant. In fact, such a
181 practice has also been adopted in many other studies for investigating grain-scale kinematics,
182 inter-particle contacts, and fabrics, etc. [38-41]. A more detailed description of the triaxial
183 system is presented in the following sections.

184 **3.2 Axial loading device**

185 The axial loading device is composed of a rotational stepping motor and a made-to-order screw
186 jack driven by a worm and a worm gear. Fig. 3 shows a closer view of the axial loading device.
187 The rotational stepping motor can offer a maximum torque of 117.9 N · cm and a rotation speed
188 ranging from 0.1318 to 5,110 deg/s. In combination with a screw jack having a speed reduction
189 ratio of 16:1, and a worm drive with a speed reduction ratio of 10:1, the stepping motor can
190 provide a maximum axial force of up to 5 kN and an axial loading speed ranging from 1 to 1,000
191 $\mu\text{m}/\text{min}$. Note that in order to resist the reaction forces acting on the worm shaft from the worm
192 along the axial and the radial directions, a pair of axial thrust bearings and radial thrust bearings,
193 respectively, are used.

194 Below the screw jack, a piston shaft is connected to the screw jack via a load cell and two screw
195 adaptors (see Fig. 2(b)). It should be noted that the axial force measured by the load cell
196 incorporates the friction of the piston shaft, and this is assumed to be constant during the
197 movement of piston shaft. A round-ended loading ram (i.e., the piston shaft) contacting a flat top
198 platen (i.e., the cushion plate shown in Fig. 2(a)) is adopted to transfer the motion from the
199 stepping motor to a sample.

200 **3.3 Confining pressure offering device**

201 The confining pressure is transmitted through water and is offered by a GDS pressure controller
202 (see Fig. 2(a)) with a confining pressure of up to 2,000 kPa. In order to supply the sample with a
203 constant pressure, the apparatus requires a good seal performance. Fig. 4 shows a schematic of
204 the seal design of the chamber. The chamber is fabricated with polycarbonate and has an I-
205 shaped section and a thickness of 20 mm. Different sealing types are incorporated to prevent

206 leakage with the use of O-rings. On the interfaces between the chamber and the plates (i.e., the
207 base plate and the chamber top plate), and the interface between the piston shaft and the piston
208 shaft sleeve, radial seals are used. An axial seal is utilized between the chamber top plate and the
209 piston shaft sleeve. Additionally, two sealing gaskets are installed on the chamber to prevent
210 leakage from the two cell pressure valve holes, through which the cell pressure fluid is injected.

211 It is worth noting that the apparatus has no tie bars around the chamber (See Fig. 2(b)). In
212 addition to constant water pressure, the chamber is also subjected to a tensile force along its axis
213 when a deviatoric stress is applied on the sample. This may result in an axially tensile
214 deformation of the chamber. Given that the tensile elastic modulus E_s of the polycarbonate is
215 2,300 MPa, the axially tensile deformation of the chamber can be estimated by:

$$216 \quad \omega_c = \frac{A_s q}{A_c E_s} L_c \delta_A, \quad (2)$$

217 where A_c ($A_c = 2,513.3 \text{ mm}^2$) and A_s ($A_s = 54.7 \text{ mm}^2$) are the section area of the chamber and the
218 designed sample, respectively. L_c ($L_c = 50 \text{ mm}$) is the length of the chamber, while q and δ_A are
219 the deviatoric stress and the sample area expansion factor (i.e., the ratio of the average section
220 area of the deformed sample to A_s), respectively.

221 This deformation is rather small ($\omega_c \leq 5.68 \mu\text{m}$) if the deviatoric stress is lower than 10 MPa.
222 This is negligible when compared to the axial deformation of the sample $\omega_s = 80 \mu\text{m}$ (suppose
223 that the deviatoric stress reaches its peak at the axial strain of 0.5% and $\delta_A = 1.2$).

224 **3.4 Data acquisition and controlling system**

225 Fig. 5 shows a photograph of the data acquisition and controlling system, which comprises a data
226 logger, a micro-computer, a miniature load cell with a capacity of up to 10 kN, and a LVDT with

227 a measurement range of 10 mm. The load cell and the LVDT are connected to the data logger
228 through the port shown in Fig. 5. A specially written code is used to send commands from the
229 computer to the data logger to record the axial force and deformation, and to control the axial
230 loading. Similar data controlling systems have also been used in single particle compression tests
231 [42, 43].

232 **3.5 Sample maker**

233 A sample maker is designed to form samples with a size of $8 \times 16 \text{ mm}$ (diameter \times height), as
234 shown in Fig. 6. The sample maker is constructed from two pieces of stainless steel molds with a
235 semi-cylindrical inner surface, locked by four screws. The two mold parts have the same size,
236 except for a nozzle connected to one half to increase suction inside. The large flat contact surface
237 is polished to improve the seal performance. The conventional air pluviation method is used to
238 prepare the sample as shown in Fig. 7. This process includes the position of a porous stone and a
239 membrane (Fig. 7A), the installation of the sample maker and the fixing of the membrane (Figs.
240 7B and 7C), the filling of sand grains and the installation of a cushion plate (Figs. 7D and 7E),
241 and finally the removal of the sample maker (Fig. 7F).

242 **4 Triaxial test on LBS sand**

243 **4.1 Test material and synchrotron radiation facility setup**

244 An in-situ triaxial compression test is conducted using the developed triaxial apparatus in
245 combination with the synchrotron X-ray μCT scanner at SSRF. The testing material is a
246 uniformly graded LBS with a particle diameter of 0.4~0.8 mm. The LBS sample has an initial
247 porosity of 0.343 (i.e., a relative density of 127.7%), which is measured from the CT image of
248 the sample after the isotropic consolidation under a confining stress of 500 kPa. Figs. 8(a) and

249 8(b) show a photograph of the triaxial apparatus being used in conjunction with the synchrotron
250 radiation facility, and a schematic of the connection between them, respectively. The X-ray
251 source has an energy of 25 Kev, and the detector has a spatial resolution of 6.5 μm . This permits
252 a high contrast between sand grains and air voids in the CT images of the sample. In each scan,
253 four sections are required for the full-field imaging of the 16 mm-high sample, because the
254 scanning window of the detector is 4.888 mm in height, and an overlap between any two
255 consecutive sections is required to stitch them together. This is achieved by adjusting the height
256 of the apparatus for different sections using a motor-controlled lifting device, which is fixed
257 upon the board with an alumina plate and has a load capacity of 50 kg, as seen in Fig. 8(b).
258 Above the lifting device, a tilting table positions the sample rotation plane parallel to the X-ray
259 beam. The rotation stage is placed above the tilting table. It has a load capacity of 60 kg and
260 enables the entire apparatus to be rotated with a constant speed of up to $10^\circ/\text{s}$.

261 During the test, the LBS sample is first compressed isotropically to a stress of 500 kPa by the
262 GDS pressure controller, and then loaded axially at a constant rate of 33.34 $\mu\text{m}/\text{min}$ by the
263 motor. Except for the state prior to shear (i.e., the isotropic compression state), the loading is
264 paused (i.e., the axial displacement is stopped) at different loading states (i.e., axial strains of
265 0.98%, 4.94%, 10.40%, 15.34%) for CT scan. In each loading state, as the rotation stage rotates
266 the whole apparatus at a constant rate across 180° , the X-ray beam and the detector work to
267 record the CT projections of the sample at different angles. About 1,080 projections are recorded
268 for each section. Due to the powerful X-ray source and the use of an exposure time of 0.08s, a
269 full-field scan of the sample at each loading state takes about 15 min.

270 **4.2 Test results**

271 Figs. 9(a) and 9(b) show the stress–strain curves of the tested LBS sample, where the scanning
272 points are marked with circles. As seen in Fig. 9(a), the deviatoric stress (i.e., $\sigma_1 - \sigma_3$) reaches
273 its peak at around the third scan (i.e., at the axial strain of 4.94%). Note that there is a significant
274 drop of the deviatoric stress during each scan. This is due to stress relaxation caused by the pause
275 of loading during a scan. The deviatoric stress increases rapidly to the value before the drop,
276 when the sample is reloaded after the scan. Overall, the sample exhibits a dilation behavior
277 during the shear after a compression in the pre-peak shear increment of 0~0.98%, as shown in
278 Fig. 9(b). Note that the GDS equipment is not used to measure the sample volumetric strain
279 because of the requirement to measure the volume change of the miniature sample with high
280 precision and resolution. The volumetric strain is determined based on image processing and
281 analysis of the CT images at each scan of the sample.

282 Using the synchrotron radiation facility, a raw 3D CT image of the sample at each scan is
283 acquired. Fig. 10 shows vertical slices of the sample at different scans, and indicates the increase
284 of voids in the sample at large shear strains (i.e., from 4.94% to 15.34%).

285 To quantify the porosity and volumetric strain of the sample, the raw 3D CT image is put
286 through a series of image processing and analysis. For illustration, Figs. 11(a)-(f) present the
287 image processing of a 2D horizontal slice to determine the porosity of the LBS sample. Please
288 note that the image processing is performed on 3D images in this study. First, an anisotropic
289 diffusion filter [44, 45] is applied to the raw CT image shown in Fig. 11(a) to remove random
290 noise within it. The anisotropic diffusion filter has the advantage of removing noise from
291 features and backgrounds of the image while preserving the boundaries and enhancing the
292 contrast between them. This is achieved by setting a diffusion stop threshold [45], which is
293 determined by a parametric study. Each voxel in the image is diffused unless the intensity

294 difference between the voxel and its six face-centered neighboring voxels exceeds the threshold
295 value. The resulting image is a grey-scale image shown in Fig. 11(b). Fig. 12 shows the intensity
296 histograms of the raw CT image and filtered CT image, respectively. The filtered CT image
297 shows a higher contrast between grains and air voids than the raw CT image, as seen in Fig. 12.
298 Subsequently, a global threshold (see Fig. 12) is applied to the smoothed grey-scale image to
299 transform it into a binary image shown in Fig. 11(c), where voxel intensities are either 1 or 0.

300 Based on the binary image, the volume of the solid phase (i.e., the sand grains) V_s is calculated
301 as the number of voxels with an intensity value of 1 multiplied by the voxel size (i.e., $6.5 \mu\text{m}^3$).
302 Meanwhile, the sample volume V_T is also determined by implementing a series of morphological
303 operations on the binary image according to a method used by Andò [31]. Specifically, 12
304 episodes of image dilation are firstly implemented to the binary image to acquire another binary
305 image (i.e., the image shown in Fig. 11(d)), which contains a connected solid phase region. This
306 is followed by a ‘filling hole’ operation which replaces all the void phase voxels (i.e., the voxels
307 with an intensity value of 0) within the sample region with solid phase voxels (i.e., the voxels
308 with an intensity value of 1), as shown in Fig. 11(e). Note that while the image dilation decreases
309 the void phase within the sample region, the sample region itself is enlarged (i.e., the sample
310 boundary moves outwards). To alleviate this effect, 12 episodes of image erosion are applied
311 after the ‘filling hole’ operation. The final resulting image shown in Fig. 11(f) is used to
312 calculate the sample volume similar to the calculation of V_s . The morphological operation
313 process may have a tiny influence on the sample boundary shape because of the irreversibility of
314 the dilation and erosion operations. However, its influence on the sample volume results is
315 considered to be negligible due to the much larger number of voxels within the sample than on
316 its boundary. The sample porosity ϕ and volumetric strain ε_v are calculated as $\phi = \frac{V_T - V_s}{V_T}$ and

317 $\varepsilon_v = \frac{\Delta V_T}{V_T}$ (i.e., the decrease of the sample volume during a shear increment divided by the
318 original sample volume), respectively. Note that a positive volumetric strain denotes
319 compression.

320 To study the porosity distribution evolution, the local porosities of the sample (i.e., the local
321 porosities around individual particles) are calculated based on a distance transformation method
322 [46, 47]. Figs. 13(a)-(f) illustrate the image processing process of a horizontal CT slice to
323 determine the local porosities. In the binary image shown in Fig. 11(c), different particles
324 generally contact each other, so a watershed algorithm [48] is applied to separate the attached
325 particles prior to the calculation of local porosities. To this end, a distance transformation is first
326 implemented on the inverted binary image to obtain a distance map, before the watershed
327 algorithm is applied on the inverted distance map to separate the attached particles. Over-
328 segmentation sometimes occurs if the watershed algorithm is directly implemented because of
329 the intensity variations within the distance map [49]. A marker-based approach used in previous
330 studies [42, 50] is adopted to control the over-segmentation. The resulting image is a binary
331 image of separated particles shown in Fig. 13(a). Note that the regions with different colors in
332 the image denote different particles. To determine the local porosity around a particle, the
333 particle should be firstly extracted and stored in a binary image (Fig. 13(b)). Then, a distance
334 transformation is implemented to the binary image of separated particles (Fig. 13(a)) and the
335 binary image of the extracted particle (Fig. 13(b)), respectively. The resulting images are the two
336 images shown in Figs. 13(c) and 13(d), respectively. The local void region of the extracted
337 particle shown in Fig. 13(e) is determined as the region of pixels having an intensity value of 0 in
338 the resulting image of subtraction of the two distance transformation images (i.e., Figs. 13(c) and
339 13(d)). Fig. 13(f) shows the local void region of the extracted particle superimposed on the

340 binary image of separated particles. The local porosity p_i around a particle i is calculated by
341 $p_i = \frac{V_R - V_P}{V_R}$ (where V_P and V_R are the volumes of particle i and the local void region of particle i ,
342 respectively). Note that the volumetric strain of the sample during each shear increment can also
343 be determined according to the distance transformation method (i.e., $\varepsilon_v = \frac{\Delta \Sigma V_R}{\Sigma V_R}$). For
344 comparison, the volumetric strain of the sample calculated using both methods is presented in
345 Fig. 14, indicating that the two methods provide consistent volumetric strain results.

346 Meanwhile, particle kinematics (i.e., particle translation and particle rotation) of the sample
347 during each shear increment are also quantitatively investigated through a particle-tracking
348 approach [50], which uses either particle volume or particle surface area as a particle-tracking
349 criterion to track individual particles within the sample. The centroid coordinates and
350 orientations of tracked particles in CT images from different scans are used to determine their
351 displacements and rotations, respectively. Specifically, a particle motion is decomposed into a
352 translation of the particle mass center and a rotation around a certain axis passing through the
353 mass center. The particle translation (i.e., particle displacement) is calculated as the difference of
354 the particle centroid coordinates at the end and the start of the shear increment. The particle
355 rotation is calculated according a rotation matrix, which is determined based on the orientation
356 matrices of the particle at the end and the start of the shear increment. The readers are referred to
357 literature [50] for the full description of the calculation of particle translation and particle
358 rotation. Additionally, by combing the particle tracking results with the determination of local
359 porosities, the volumetric strain distribution of the sample during each shear increment is
360 investigated. This is achieved by calculating local volumetric strain around each particle, i.e., the
361 volumetric strain of the local void region of the particle. For each shear increment, the local

362 volumetric strain ε_{v_i} of a particle i is determined by the volume change of local void region of
363 the particle during the shear increment (i.e., $\varepsilon_{v_i} = \frac{V'_R - V_R}{V_R}$, where V_R and V'_R are the volume of
364 local void region at the start and the end of the shear increment, respectively). The authors have
365 checked the reliability of the quantification of volumetric strains in this study. It is found that the
366 presented method provides strain results basically consistent with those from a grid-based strain
367 calculation method [51]. The grid-based method calculates volumetric strains of the sample at a
368 shear increment based on particle translations and rotations during the shear increment. In the
369 method, a grid-type discretization is employed over the sample space, in which each grid is
370 associated to a particle based on a criterion. The displacement of each grid is determined
371 according to the kinematics of its associated particle. The grid displacements are used for the
372 strain calculation.

373 Fig. 15 shows a vertical slice of local porosity distributions of the sample at different axial
374 strains. Note that only the porosities at the particles' centroids are calculated, and a linear
375 interpolation is adopted for the porosities between any two particle centroids. As shown in Fig.
376 15, the sample shows a slightly inhomogeneous porosity distribution at the isotropic state (i.e.,
377 the axial strain of 0%) and the axial strain of 0.98%. Particles with large local porosities are
378 disorganized in the sample, and this inhomogeneity increases as the deviatoric stress approaches
379 the peak around the axial strain of 4.94%. The sample exhibits several zones of high porosity in
380 the center. In the post-peak shear stage (i.e., axial strains of 10.40% and 15.34%), a localized
381 band of high porosity is well developed. Overall, the sample experiences an increase of local
382 porosities during the shear from the axial strain of 0.98% to 15.34%.

383 Fig. 16 shows the normalized frequency distributions of local porosity of the sample at different
384 axial strains, and presents the mean value and the standard deviation. From Fig. 16 we can see
385 that from the axial strain of 0% to 0.98%, there is no obvious change of the normalized
386 frequency distribution. From the axial strain of 0.98% to 15.34%, the normalized frequency of
387 particles with high local porosities (e.g., local porosities larger than 0.5) increases, while that
388 with low local porosities (e.g., local porosities smaller than 0.4) decreases. This results in the
389 increase of the mean local porosity value, which indicates a volumetric dilation, during the shear
390 stage. Meanwhile, the standard deviation of local porosity – which reflects the homogeneity of
391 the sample (the sample is completely homogenous when the standard deviation is 0, i.e., all
392 particles have the same porosity) – also experiences an increase during the shear stage, from
393 0.98% to 15.34%. This indicates that the sample becomes increasingly inhomogeneous in the
394 volumetric dilation process.

395 Figs. 17(a)-(d) show the particle displacement and particle rotation of the sample at different
396 axial strain increments. Note that the rotation magnitudes of particles shown in Fig. 17 are the
397 rotation angles of the particles around their own rotation axes. The rotation axis of a particle is
398 determined according to the particle rotation matrix, which is different for different particles. At
399 the early stage of shear (i.e., 0~0.98%) shown in Fig. 17(a), there is no obvious localization of
400 particle displacement (left), or particle rotation (right) occurring within the sample. At the axial
401 strain increment of 4.94~10.40%, the sample experiences clearly localized particle displacement
402 and particle rotation, as shown in Fig. 17(c). Eventually, the sample fails along a well-defined
403 localized displacement band shown in Fig. 17(d). Figs. 18(a)-(d) show volumetric strain
404 distributions of the sample at different shear increments, in which both 3D maps and vertical
405 slices of the volumetric strains are displayed. Note that negative values denote dilation. The

406 sample exhibits no distinct localization of volumetric strain at the early stage of shear, but
407 experiences a strong localized dilation in the post peak stage of shear (i.e., 4.94~15.34%), which
408 is similar to the evolution of particle kinematics.

409 **5 Conclusions**

410 A miniature apparatus is specially fabricated and used for experimental investigation of the
411 micro-scale mechanical behavior of granular soils under triaxial shear. The apparatus is similar
412 to the conventional triaxial apparatus from a structural point of view, and can be used in
413 conjunction with X-ray μ CT for in-situ testing. The detailed design of this apparatus is presented.

414 An experiment of an LBS sample sheared under a confining stress of 500 kPa is demonstrated.
415 The micro-scale characteristic changes of the sample (e.g., the evolutions of local porosities,
416 particle kinematics and volumetric strain distribution), which are otherwise not possible to
417 examine by conventional triaxial tests, are quantitatively studied using image processing and
418 analysis techniques. A novel method is presented to quantify the volumetric strain distribution of
419 the sample throughout the test.

420 The volumetric strains are calculated using two image processing-based methods, which are
421 found to provide consistent results. The sample shows a slight inhomogeneity of local porosities
422 and no apparent localization of particle kinematics or volumetric strain in the early stage of
423 shearing, with high-porosity particles disorganized in the sample. An obvious inhomogeneity of
424 local porosities and a slight localization of particle kinematics and volumetric strain are observed
425 in the middle of the sample around the peak of the deviatoric stress. A localized band of high
426 porosities, particle kinematics and volumetric strain is gradually developed in the sample at the
427 post-peak shear stage.

428 The miniature triaxial apparatus, in conjunction with X-ray μ CT and advanced image processing
429 and analysis techniques, has provided an effective way to unravel the micromechanical
430 mechanism of the failure of granular soils subjected to loading.

431 **Acknowledgement**

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556 tomography: A comparison between a grid-based method and a mesh-based method. Powder
557 Technology 344: 314-334.
- 558

559 **List of Figures**

560 Fig. 1 Schematic of a typical parallel beam X-ray μ CT facility

561 Fig. 2 The triaxial system: (a) schematic of the triaxial system, (b) photograph of the triaxial
562 apparatus

563 Fig. 3 A closer view of the axial loading device

564 Fig. 4 A schematic of the seal design of the apparatus

565 Fig. 5 Data acquisition and controlling system

566 Fig. 6 Photograph of the sample maker

567 Fig. 7 The process of making a sample

568 Fig. 8 The triaxial apparatus being used in conjunction with the synchrotron radiation facility: (a)
569 a photograph, (b) a schematic of the connection between the apparatus and the synchrotron
570 radiation facility.

571 Fig. 9 Stress–strain curves of the LBS sample: (a) deviatoric stress vs. axial strain, (b) volumetric
572 strain vs. axial strain

573 Fig. 10 Vertical slices of the sample at different scans

574 Fig. 11 Illustration of the image processing of a 2D horizontal slice to determine sample porosity:
575 (a) raw CT image, (b) filtered CT image, (c) binary image, (d) after 12 times of dilation of image
576 (c), (e) after filling holes of image (d), (f) after 12 times of erosion of image (e)

577 Fig. 12 Intensity histograms of the CT image before and after image filtering

578 Fig. 13 Illustration of the image processing of a 2D horizontal slice to determine local porosities:
579 (a) a binary image of separated particles, (b) a binary image of an extracted particle, (c) distance
580 transformation of image (a), (d) distance transformation of image (b), (e) extracted local void
581 region, (f) the local void region superimposed on image (a)

582 Fig. 14 Comparison between the volumetric strains of the sample as calculated by two methods

583 Fig. 15 A vertical slice of local porosity distributions of the sample at different axial strains

584 Fig. 16 Normalized frequency distributions of local porosity of the sample at different axial
585 strains

586 Fig. 17 Particle displacement and rotation of the sample during the axial strain increments of (a)
587 0~0.98% (b) 0.98~4.94% (c) 4.94~10.40% (d) 10.40~15.34%

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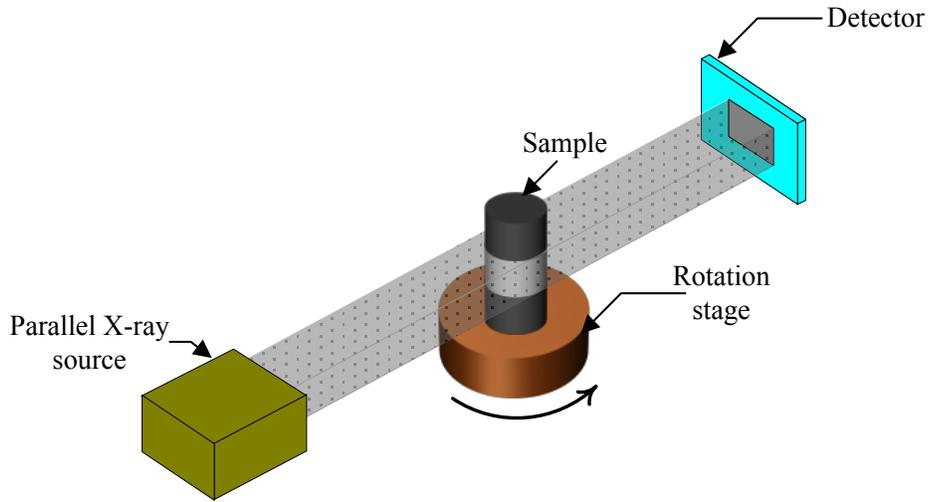
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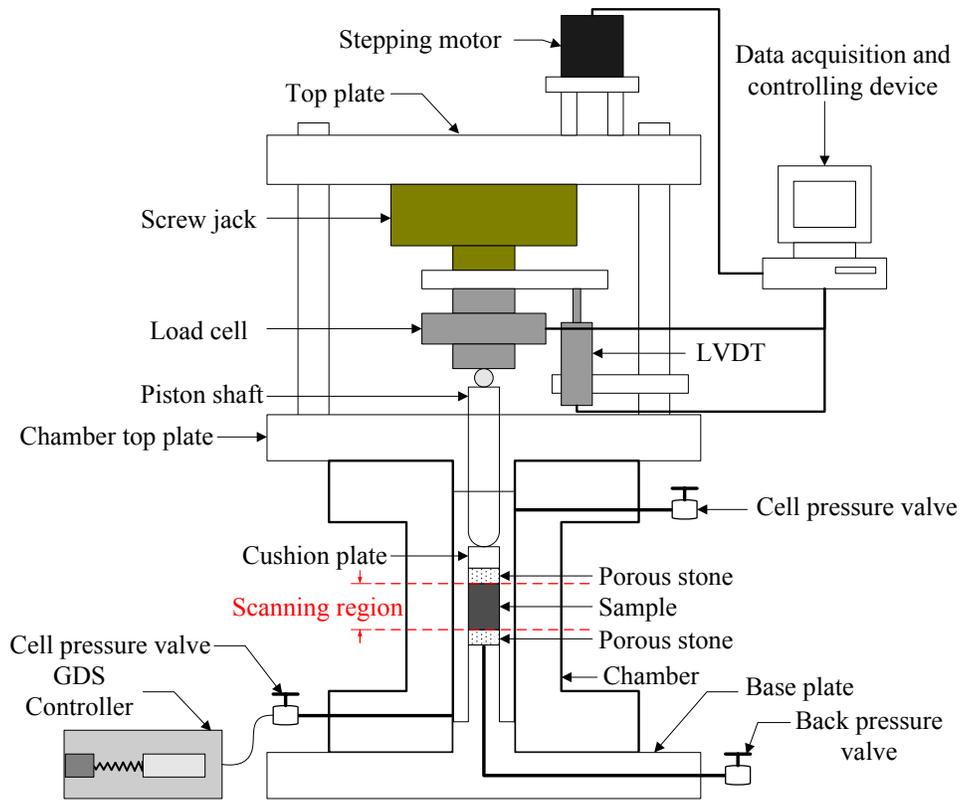


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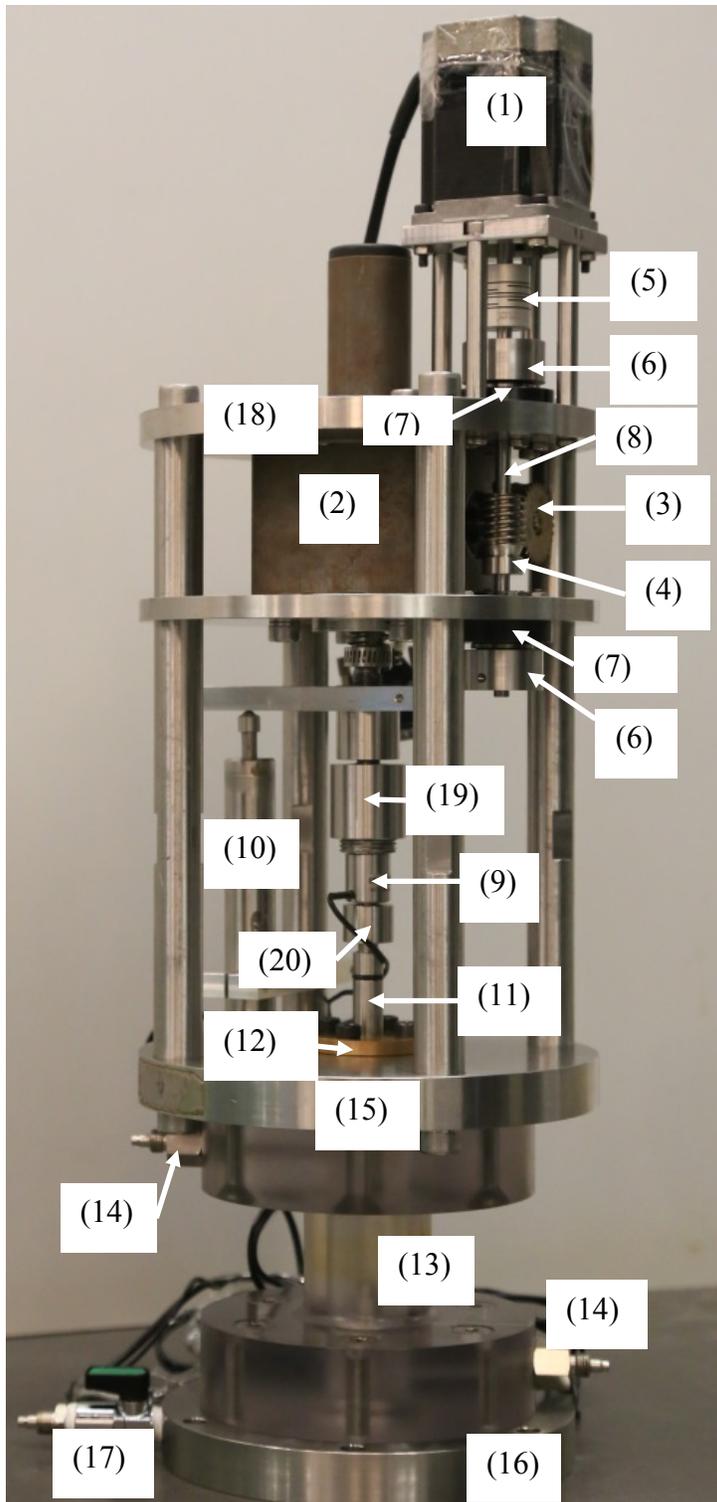
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(a)



- (1) Stepping motor
- (2) Screw jack
- (3) Worm gear
- (4) Worm
- (5) Motor coupling
- (6) Axial thrust bearing
- (7) Radial thrust bearing
- (8) Worm shaft
- (9) Load cell
- (10) LVDT
- (11) Piston shaft
- (12) Piston shaft sleeve
- (13) Chamber
- (14) Cell pressure valve
- (15) Chamber top plate
- (16) Base plate
- (17) Back pressure valve
- (18) Top plate
- (19) and (20) Screw adaptors

(b)

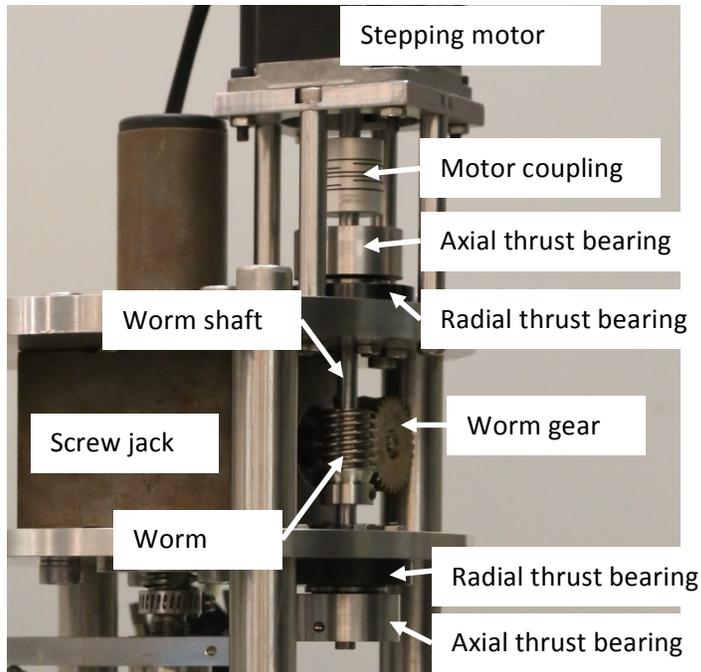
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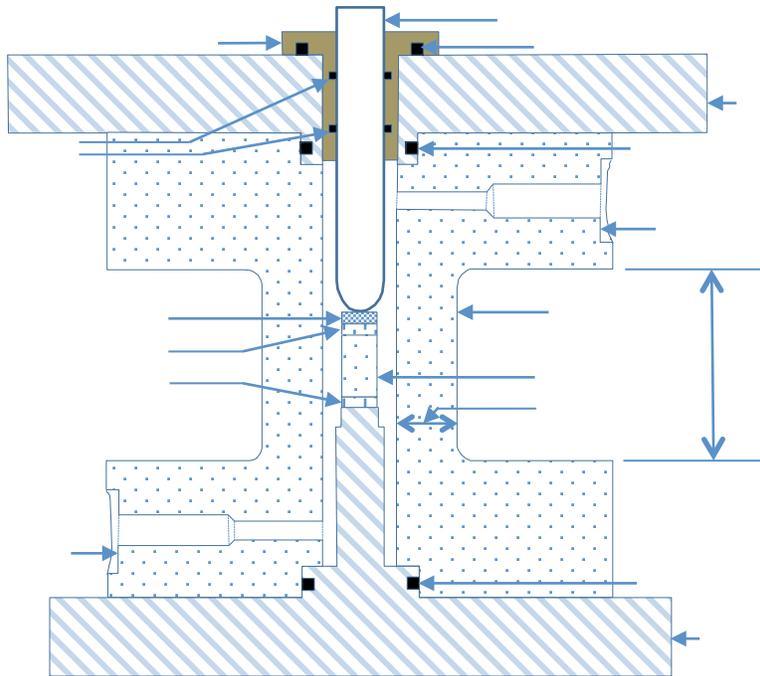
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Fig. 3 A closer view of the axial loading device



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Fig. 4 A schematic of the seal design of the apparatus

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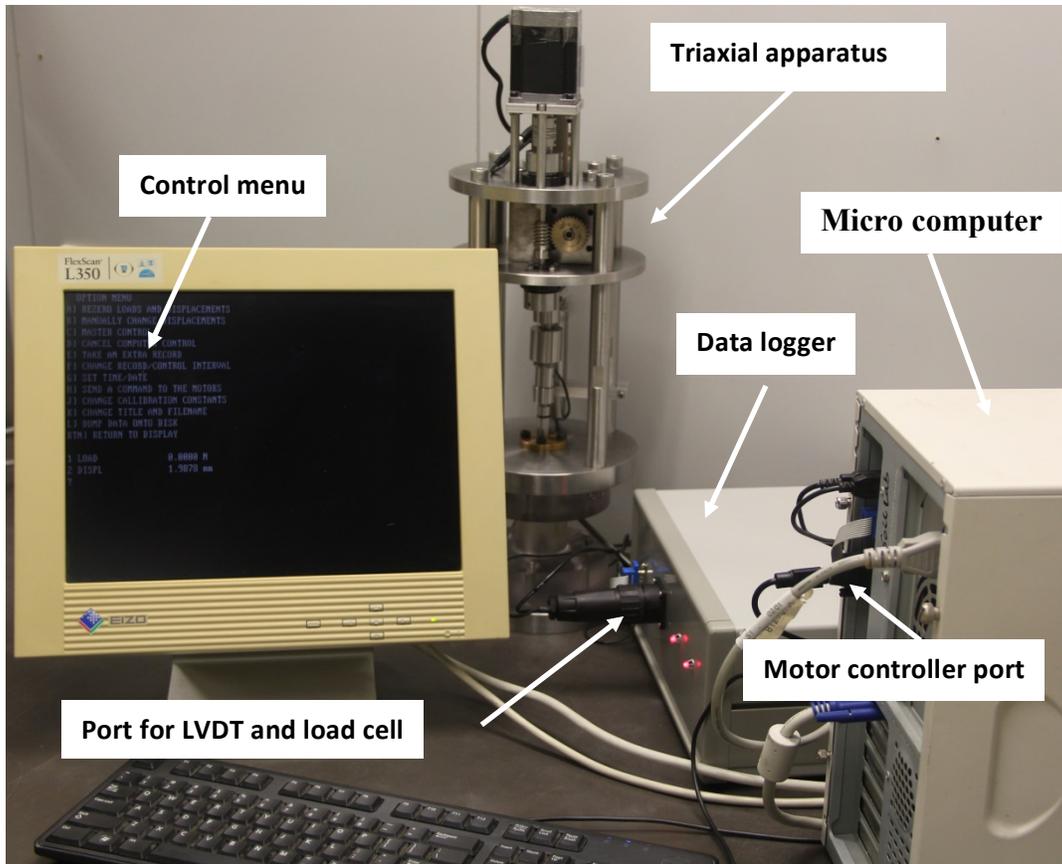
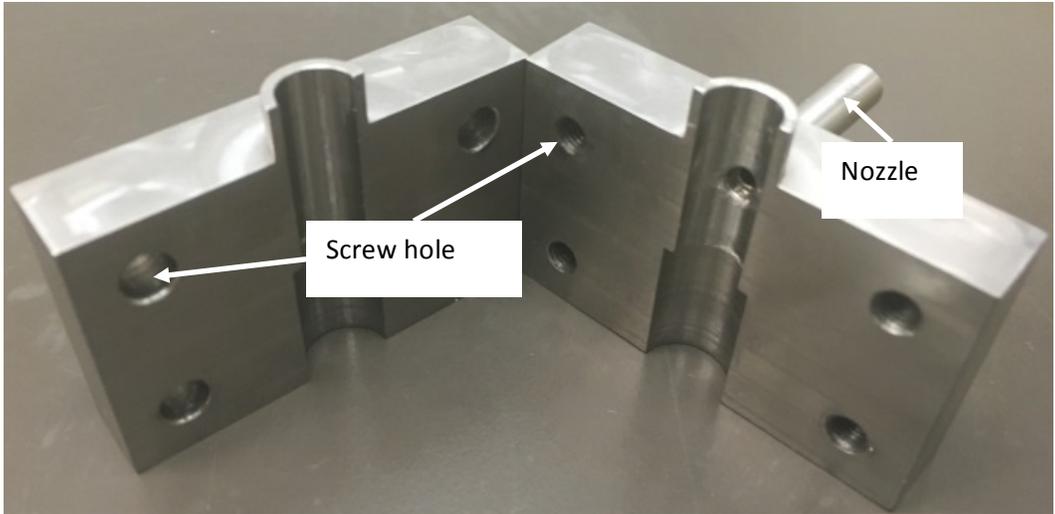


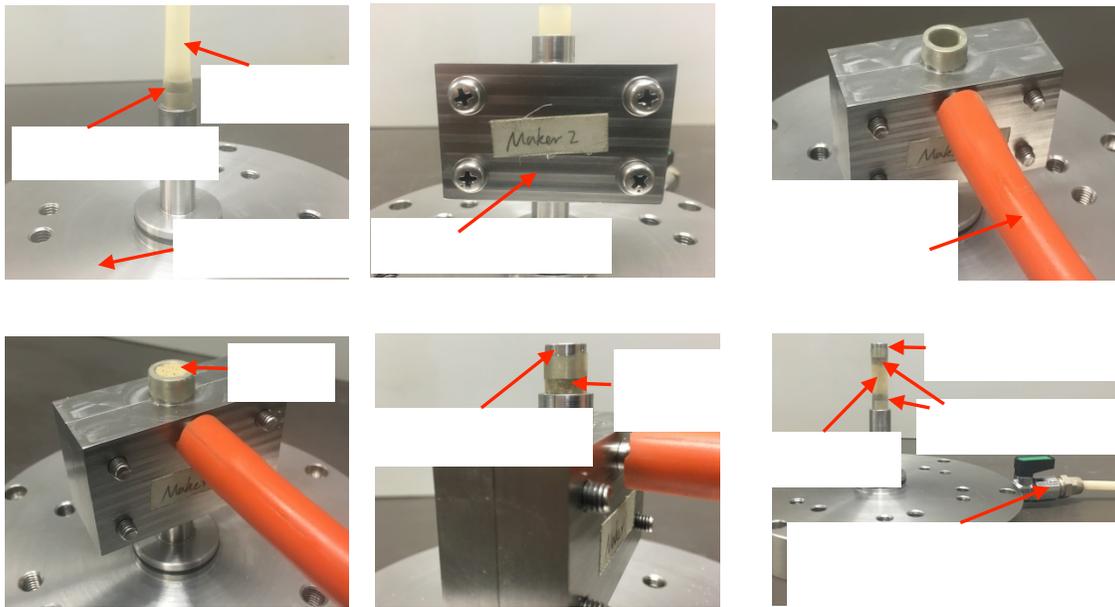
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Fig. 6 Photograph of the sample maker

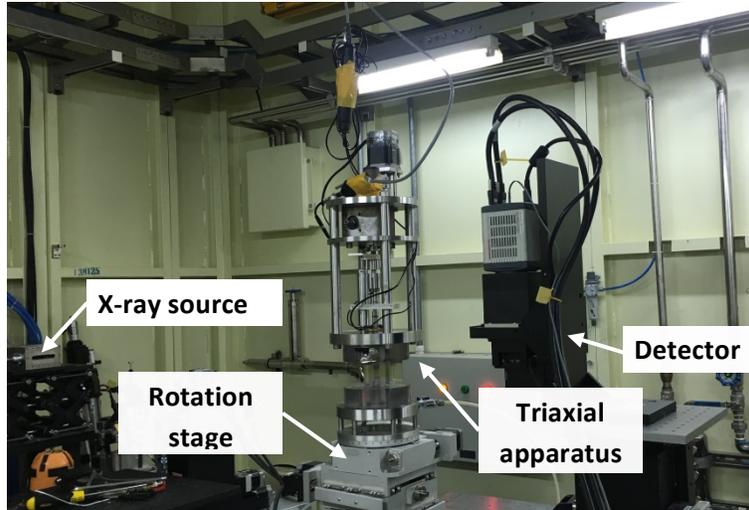


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Fig. 7 The process of making a sample

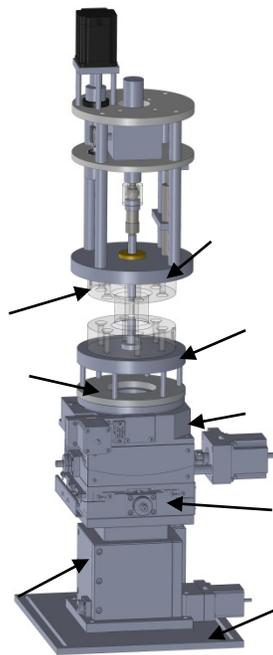
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(a)

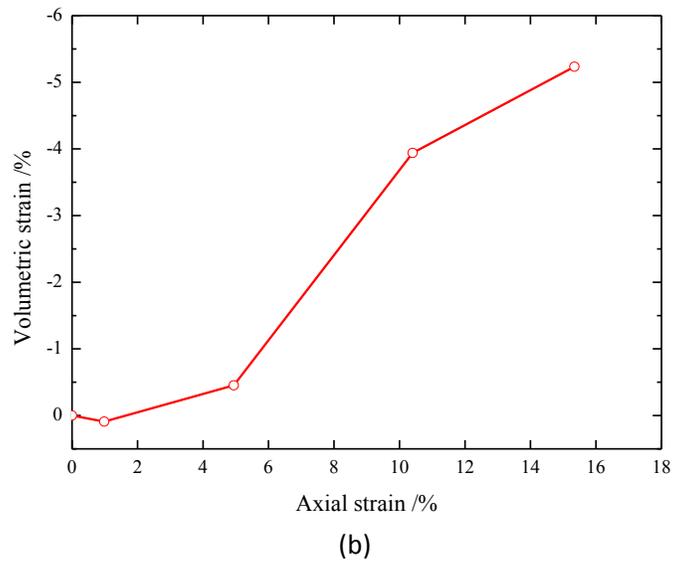
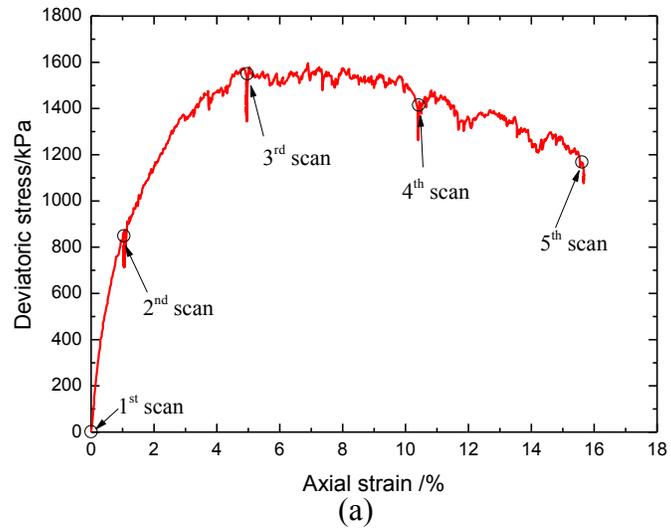


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(b)

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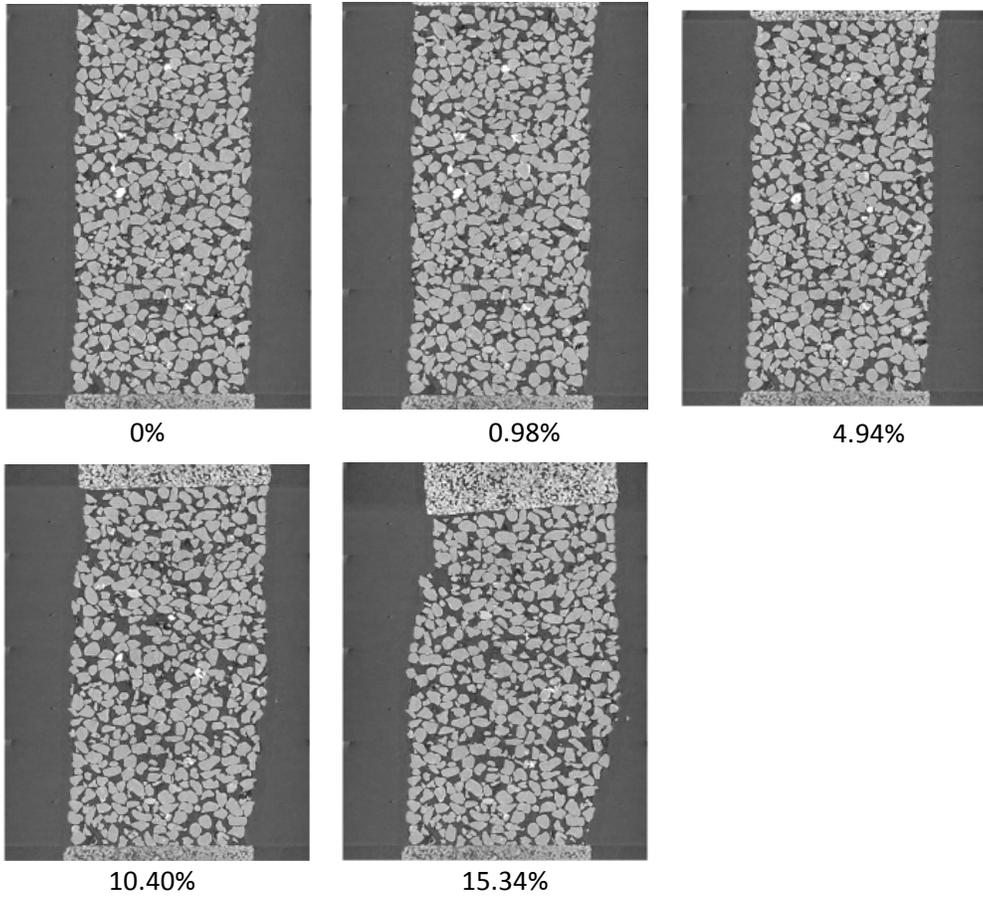
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630 Fig. 9 Stress–strain curves of the LBS sample: (a) deviatoric stress vs. axial strain, (b) volumetric

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strain vs. axial strain

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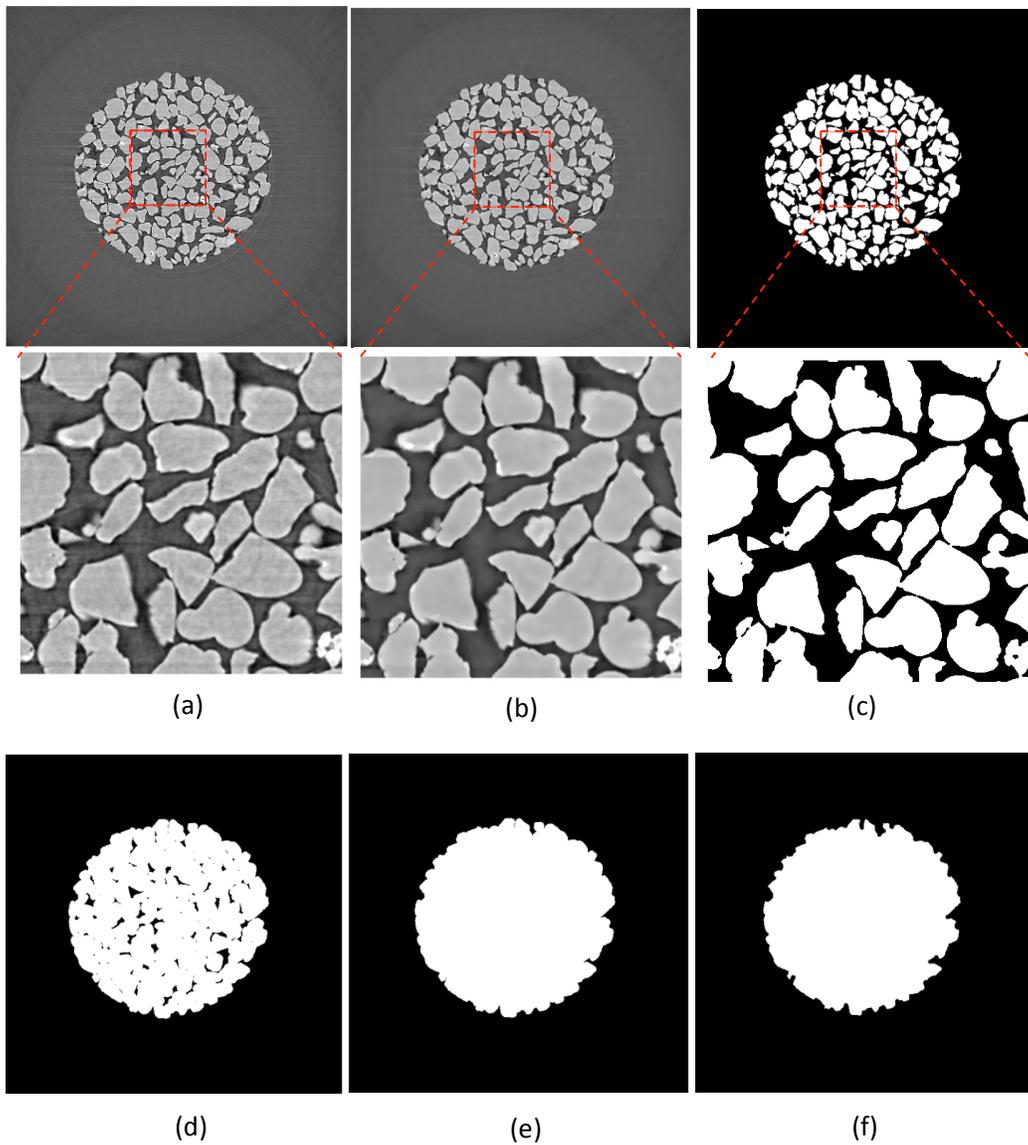


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Fig. 10 Vertical slices of the sample at different scans

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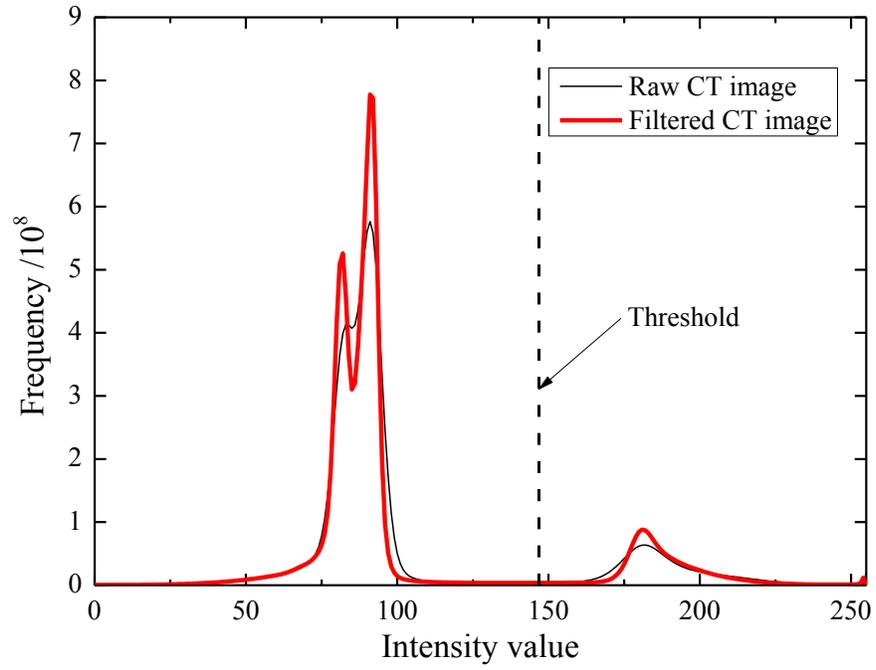
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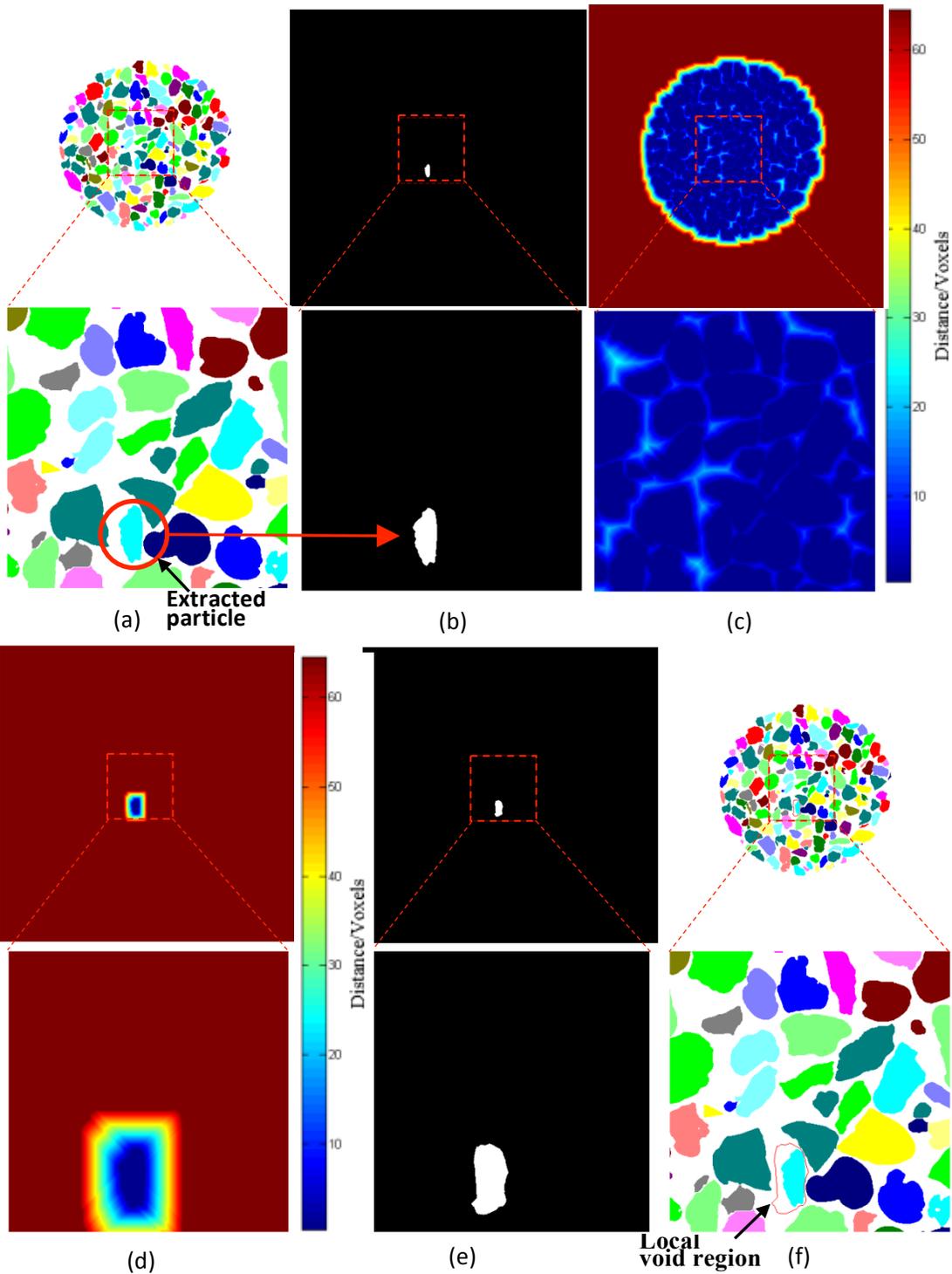


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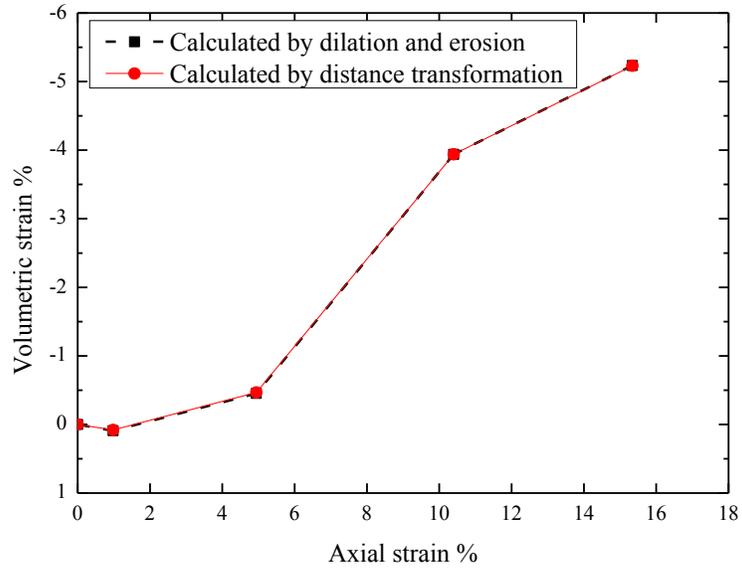
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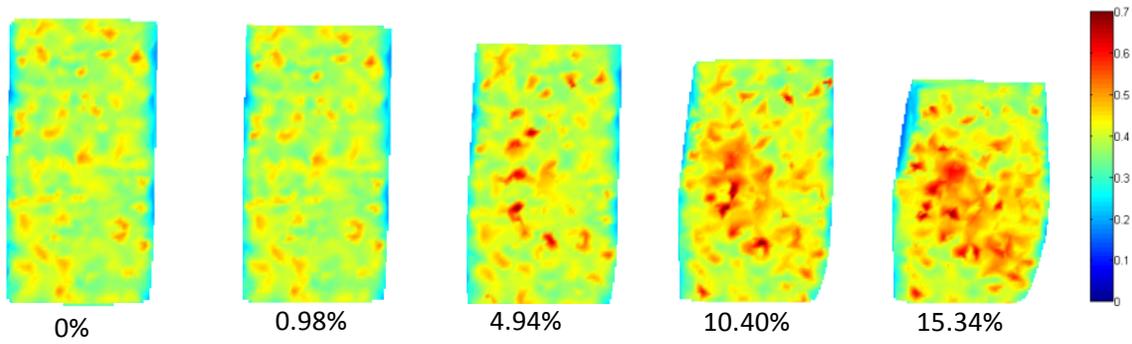
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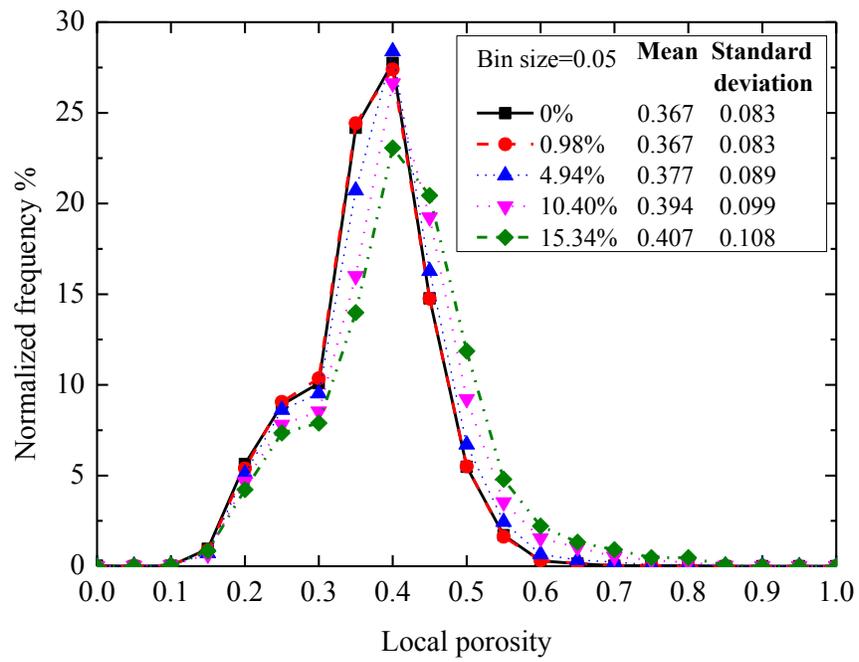


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653 Fig. 15 A vertical slice of local porosity distributions of the sample at different axial strains

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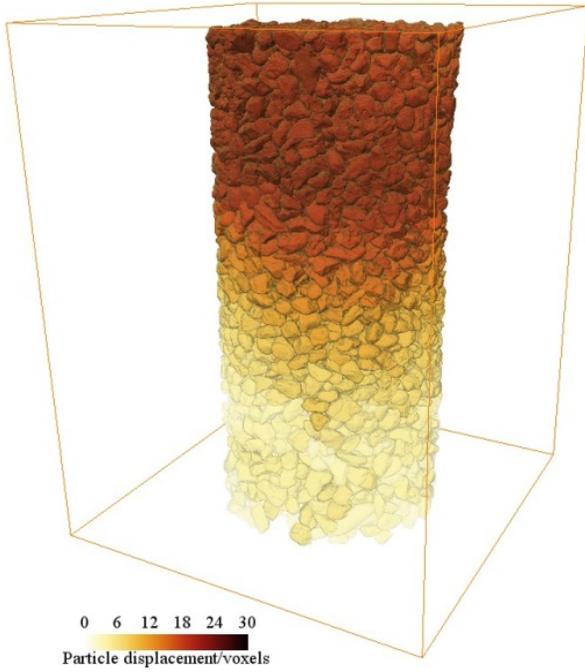
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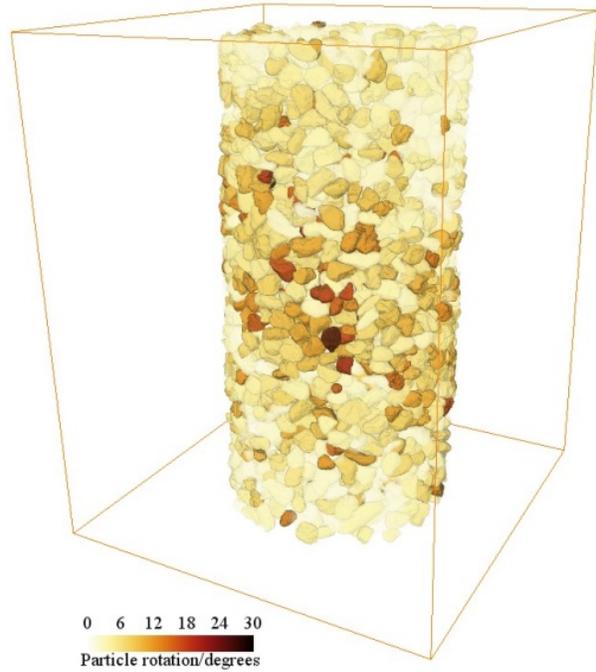
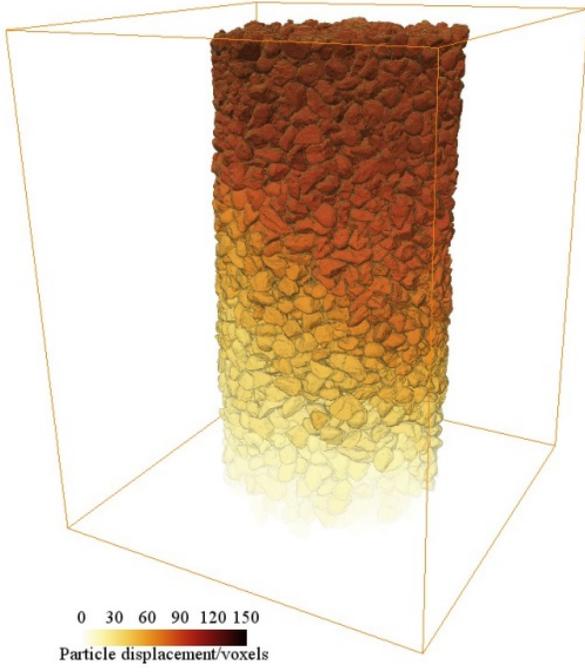
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strains

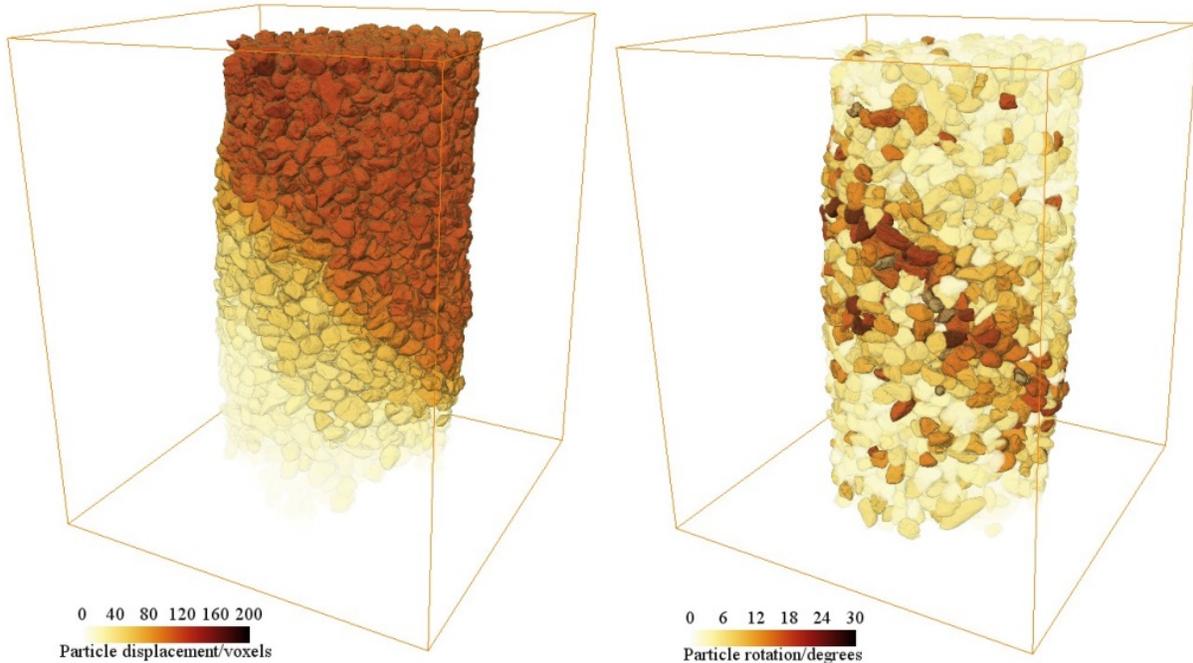
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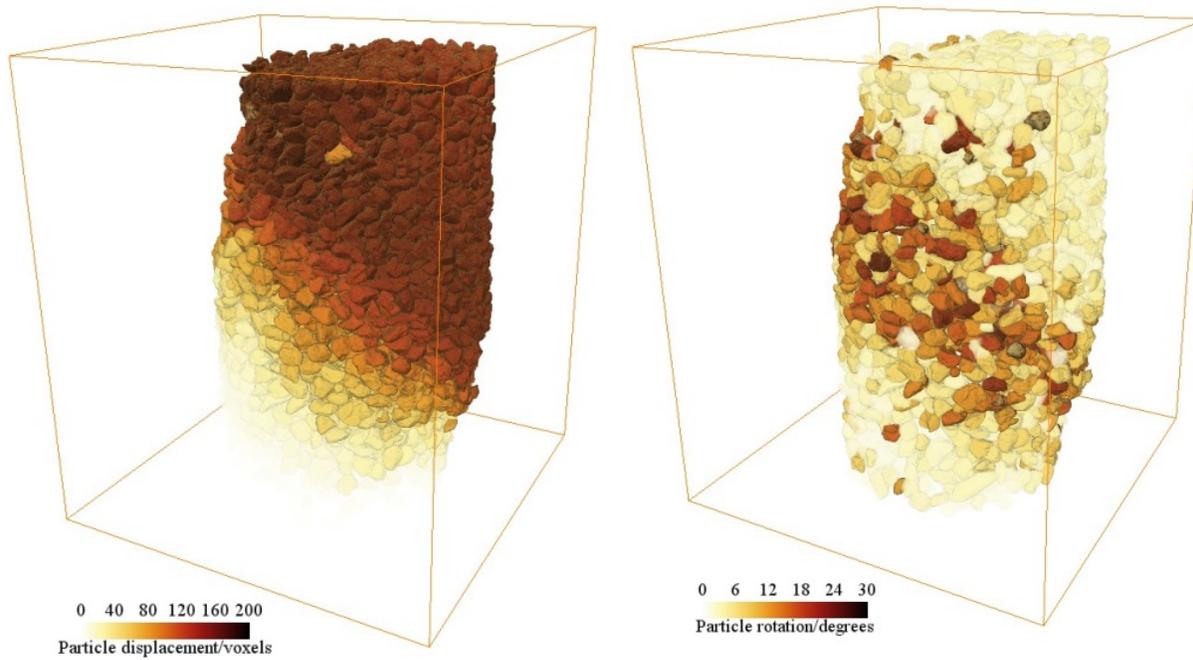
(a)



(b)



(c)



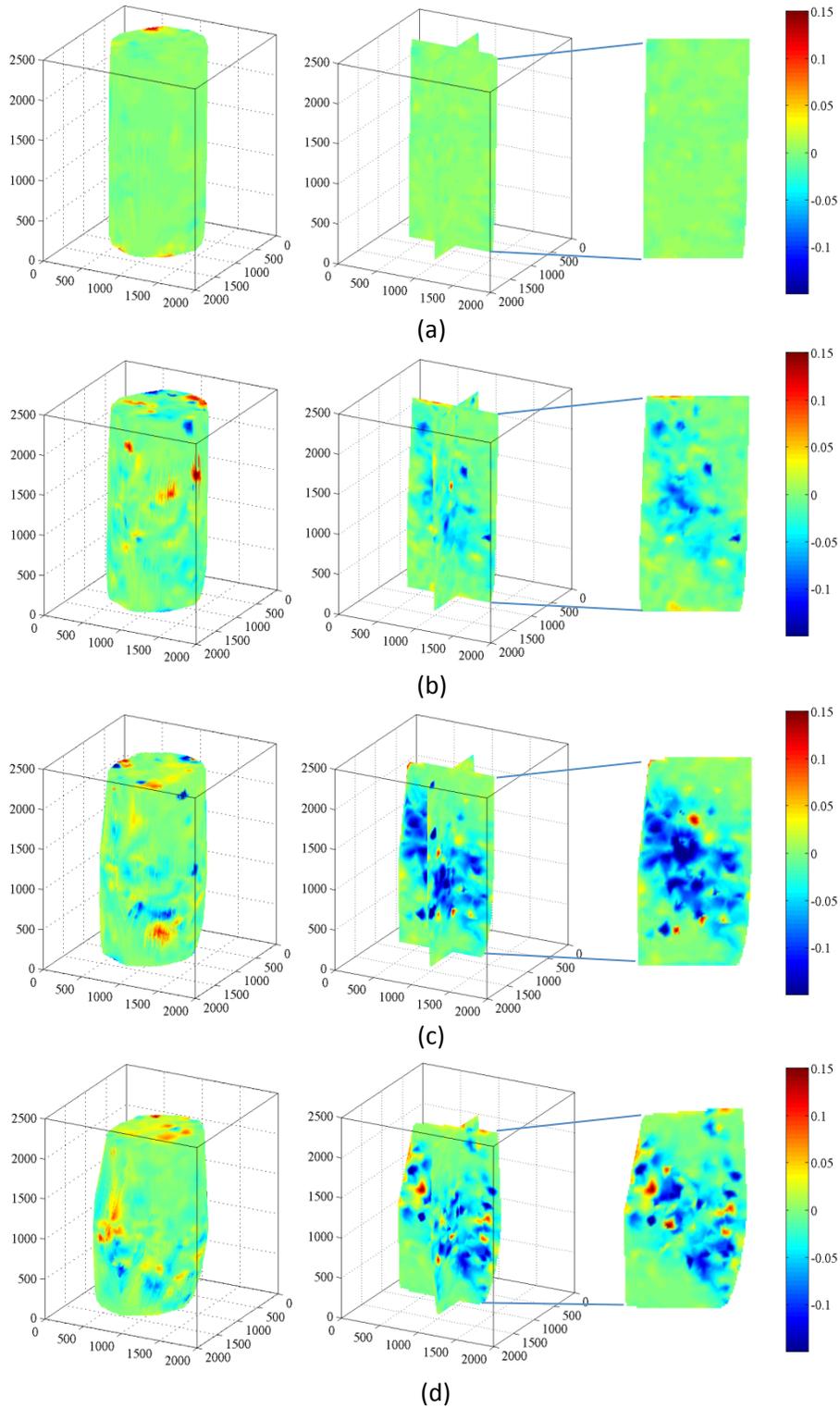
(d)

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662 Fig. 17 Particle displacement and rotation of the sample during the axial strain increments of (a)

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665

Fig. 18 Volumetric strain distributions of the sample during the axial strain increments of (a)

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