Modelling accretion disc emission with generalized temperature profile and its effect on AGN spectral energy distribution

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ABSTRACT

The broad-band spectral energy distribution (SED) of active galactic nuclei (AGNs) is investigated for a well-selected sample composed of 23 Seyfert 1 galaxies observed simultaneously in the optical/ultraviolet (UV) and X-ray bands with the Neil Gehrels Swift Observatory. The optical to UV continuum spectra are modelled, for the first time, with emission from an accretion disc with a generalized radial temperature profile, in order to account for the intrinsic spectra which are found to be generally redder than the model prediction of the standard Shakura–Sunyaev disc (SSD, $F_\nu \propto \nu^{+1/3}$). The power-law indices of the radial temperature profile ($T_{\text{eff}}(R) \propto R^{-p}$, $R$ is the radius of the accretion disc) are inferred to be $p = 0.5–0.75$ (a median of 0.63), deviating from the canonical $p = 0.75$ for the SSD model as widely adopted in previous studies. A marginal correlation of a flatter radial temperature profile (a smaller $p$-value) with increasing the Eddington ratio is suggested. Such a model produces generally a lower peak of accretion disc emission and thus a smaller bolometric luminosity in some of the AGN, particularly those with high Eddington ratios, than that based on the SSD model by a factor of several. The broad-band SED, the bolometric correction factors, and their dependence on some of the AGN parameters are revisited. We suggest that such non-standard SSD discs may operate in AGN and are at least partly responsible for the reddened optical/UV spectra as observed. One possible explanation for these flattened temperature profiles is the mass-loss process in form of disc winds/outflows.

Key words: accretion, accretion discs – black hole physics – galaxies: active – galaxies: Seyfert.

1 INTRODUCTION

The study of the broad-band energy distributions (SEDS) of active galactic nuclei (AGNs) is important for understanding the central engine and the physical processes in supermassive black holes (SMBHs, e.g. Elvis et al. 1994; Richards et al. 2006; Jin, Ward & Done 2012; Krawczyk et al. 2013; Jin et al. 2017). The SED of radio-quiet AGN is mainly dominated by two wavebands, i.e. the optical/ultraviolet (UV) and the X-ray band. The former is believed to originate from a geometrically thin and optically thick accretion disc, and the latter from a hot, optically thin corona. In the study of the AGN SED, the modelling of the optical/UV spectra is crucial since, as a common practice, the fitted model is used to determine the bolometric luminosity by extrapolating it to the extreme-UV (EUV) band, where the peak of typical AGN emission is located but can not be observed due to strong absorption by interstellar medium in the Galaxy.

Conventionally, the standard accretion disc (or Shakura–Sunyaev disc, SSD) (Shakura & Sunyaev 1973; Pringle 1981) model is widely utilized to fit the optical/UV spectra. This model predicts a specific dependence of the disc effective temperature on radius $T_{\text{eff}}(R) \propto R^{-0.75}$ and consequently a hump of a power-law spectrum $F_\nu \propto \nu^\alpha$ ($\alpha = +1/3$) with a high energy cutoff throughout much of the optical-to-EUV waveband. This emission is generally thought to account for the observed ‘big blue bump’ (BBB) feature in AGN (e.g. Shields 1978; Shang et al. 2005). On the contrary, however, continua with softer power laws in optical/UV band are often observed in AGN ($\alpha \approx -0.7$ to $-0.3$) (e.g. Vanden Berk et al. 2001; Scott et al. 2004; Davis, Woo & Blaes 2007; Shull, Stevans &...
Danforth 2012; Stevans et al. 2014; Jun et al. 2015; Selsing et al. 2016; Lawther et al. 2017), showing much redder optical/UV spectra than the theoretical model prediction.

The optical/UV spectra with shallower slopes ($\alpha < +1/3$), as observed in many AGN, may result from a number of factors (see Koratkar & Blaes 1999, for a detailed review). First, host galaxy starlight can contribute to the optical spectra especially at the red end (e.g. Bentz et al. 2006, 2009). Secondly, the dust extinction effect can also redden the spectra by scattering the UV and optical photons (e.g. Xie et al. 2016; Gaskell 2017). The latter has been widely advocated to explain the observed redder optical/UV spectra in AGN, assuming the emission is from an accretion disc of the SSD-type (e.g. Vasudevan et al. 2009; Marchese et al. 2012). However, the amount of the dust extinction intrinsic to the source is hard to measure independently. One way is to make use of the broad-line Balmer decrement measured from optical spectroscopy, which is suggested to be a good indicator for dust extinction in the broad-line region (e.g. Dong et al. 2008; Schnorr-Müller et al. 2016; Gaskell 2017). There have been efforts made in recent years to carefully assess the contributions from these two effects in order to recover the intrinsic optical/UV spectra in AGN. As examples, Vasudevan et al. (2009) employed 2D optical image decomposition to exclude host galaxy contamination for a sample of 29 AGNs with black hole masses determined from reverberation mapping. On the other hand, Grupe et al. (2010) tried to correct for the dust extinction effect using the Balmer decrement for a sample of 92 soft-X-ray-selected Seyfert 1 galaxies.

Alternatively, the reddening of the optical/UV spectra can also be explained as an intrinsic emission feature of an accretion disc (e.g. Gaskell et al. 2004). For instance, observations of NGC 5548 show a significantly reddened optical/UV spectra even after removing the host galaxy starlight and correcting for dust extinction (Gaskell, Klimke & Nazarova 2007). Theoretically, the canonical radial temperature profile $T_{\text{eff}} (R) \propto R^{-0.75}$ in the SSD solution is only valid under the assumption that mass is accreted from the outer disc all the way to the inner part without mass loss or gain of the accretion flow, and the accretion energy is solely dissipated into the disc and radiated away efficiently throughout the course of mass accretion. However, in reality this may not be true since there are likely other processes involved during the accretion process such as the disc-wind/outflow (e.g. Tombesi et al. 2013; King & Pounds 2015; Done & Jin 2016), disc evaporation and condensation (e.g. Liu & Tama 2009; Qiao et al. 2013; Liu et al. 2015), energy advection into the BH (the ‘advection-dominated accretion flow, e.g. Ichimaru 1977; Narayan & Yi 1994, 1995a,b; Yuan & Narayan 2014) and photon trapping effect (the ‘slim’ disc, e.g. Abramowicz et al. 1988; Watarai & Mineshige 2001).

In particular, the temperature distribution for a ‘slim’ disc model is much flatter ($T_{\text{eff}} (R) \propto R^{-0.5}$, e.g. Wang et al. 1999; Watarai & Fukue 1999) than that of the SSD (in this paper a temperature profile with the power-law index less than 0.75 is referred to as ‘flat’ or ‘flattened’, and those with smaller power-law indices as ‘flatter’). Other factors, such as the general relativity effects (e.g. Yamada & Fukue 1993) and irradiation from the central object (e.g. Sanbuichi, Yamada & Fukue 1993; Czerny, Goosmann & Janiuk 2008), may also alter the radial temperature profile. In order to take these possible effects into account, a generalized disc model has been proposed in Mineshige et al. (1994) by parametrizing the disc radial temperature profile as a power law $(T_{\text{eff}} (R) \propto R^{-p})$ with the slope $p$ being a free parameter, different from the SSD solution which has $p = 0.75$. It should be noted that even a small deviation of $p$ from 0.75 can make a noticeable difference in the slope of the power-law regime of the disc spectrum ($\alpha = 3 - 2p$, e.g. Pringle & Rees 1972; Frank, King & Raine 2002; Kato, Fukue & Mineshige 2008), which, falls into the optical/UV band in the case of AGN. Gaskell (2008) pointed out that an optical/UV spectral slope of $\alpha = -0.5$ implies a radial temperature profile of $T_{\text{eff}} (R) \propto R^{-0.57}$. The idea of changing the radial temperature profiles has been adopted to generate a reddened optical/UV spectrum in various studies, either by radially changing the mass flow rate inside the accretion disc through disc wind (e.g. Slone & Netzer 2012; Laor & Davis 2014), or introducing an additional irradiating (heating) term mostly to the outer disc region (e.g. Soria & Puchnarewicz 2002; Loska, Czerny & Szcerba 2004).

The appropriate modelling of the observed optical/UV emission in AGN is essential for constructing the broad-band SED. This is because the EUV emission, which is thought to be the peak of the AGN continuum (in the $\log v F_v - \log v$ manifestation), is completely obscured due to Galactic absorption and is usually estimated by extrapolating the optical/UV spectral model obtained from data fitting. This has become a common practice in recent studies of AGN SED (e.g. Vasudevan & Fabian 2007, 2009; Vasudevan et al. 2009; Jin et al. 2012; Marchese et al. 2012). However, in most of these studies the SSD model was employed, and any spectral deviation is presumably attributed to some external processes, such as dust extinction. Clearly, if the actual disc radial temperature profile is indeed flattened compared to the SSD solution, the bolometric luminosities $L_{\text{bol}}$ may have been largely overestimated, especially in sources with strong optical/UV emission. For instance, Slone & Netzer (2012) argued that in such a case the estimated disc luminosity can differ by a factor of as large as 2, and so is the estimated bolometric luminosity $L_{\text{bol}}$ and the Eddington ratio $\lambda_{\text{Edd}}$ (defined as $L_{\text{bol}}/L_{\text{Edd}}$ where $L_{\text{Edd}} = 1.3 \times 10^{38}(M/M_\odot)\operatorname{erg\ s}^{-1}$ is the Eddington luminosity). As such, there is a possibility that some of the bolometric correction factors $\kappa_\nu$ (defined as $L_{\text{bol}}/\nu L_\nu$, $\nu L_\nu$ is the monochromatic luminosity at frequency $\nu$) obtained in previous work may be subject to systematic uncertainties. Some of these factors have been widely used in the literature to estimate the bolometric luminosities of AGN from luminosity measurement in a single waveband.

In this work, we study the broad-band SED of AGN using a well-selected sample composed of 23 Seyfert 1 galaxies with simultaneous optical/UV and X-ray data obtained by the Neil Gehrels Swift Observatory (Gehrels et al. 2004). The sample objects are selected in such a way that they are subject to no or at most mild dust extinction (as estimated from the Balmer decrement); for the latter, the extinction effect is also corrected. Furthermore, the host galaxy starlight is eliminated by applying 2D image decomposition, as also did in Vasudevan et al. (2009). We model the optical to UV spectra by adopting, for the first time, an accretion disc model with a generalized radial temperature profile. The X-ray spectra of the sample objects from simultaneous observations are also modelled. We derive the bolometric correction factors for both the optical and X-ray bands and investigate their dependence on some of the AGN parameters.

The paper is organized as follows. A brief description of the sample selection and multiwaveband data reduction are presented in Sections 2 and 3, respectively. In Section 4, we describe the spectral modelling in optical/UV band. The X-ray spectral analysis,
broad-band SEDs and bolometric corrections are investigated in Section 5. The main results are discussed in Section 6, followed by a summary in Section 7. A flat universe model with a Hubble constant of $H_0 = 75 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_M = 0.27$, and $\Omega_{\Lambda} = 0.73$ is adopted throughout the paper.

2 SAMPLE

For the study of AGN broad-band SED, it is essential to use simultaneous observational data in both the optical/UV and X-ray bands, in which AGN radiate most of their energy. At present, there are two space telescopes capable of achieving this goal, i.e. Swift and XMM–Newton. In this work, we draw our sample from the published AGN catalogue on Vizier observed with Swift. We choose the Swift database for two reasons. First, the data provided by UV and optical telescope (UVOT, Roming et al. 2005) onboard Swift are generally in a better quality compared to those of optical mirror (OM, Mason et al. 2001) equipped on XMM–Newton: (1) the data images are less influenced by the scattered light, which may lead to an unpleasant background noise and ghost image, and (2) the effective areas of the detectors for two UV filters (uvw2, uvw2) are larger than those in OM, which makes the UV throughput a factor of 10 higher than that of the OM instrument. Secondly, the X-ray spectra obtained by its X-ray telescope (XRT, Burrows et al. 2005) are sufficient for our SED study as long as the exposure is long enough (a few kiloseconds). The sample is compiled of AGN with simultaneous observations with data from both the UVOT and XRT instruments. We consider only type 1 AGN classified as radio quiet in the literature. The modelling of the optical/UV spectra with an accretion disc model requires the knowledge of the black hole masses and the amount of dust extinction along the line of sight (see Section 3.4). We therefore limit our sample to those having optical spectroscopic data from the Sloan Digital Sky Survey (SDSS, York et al. 2000), based on which both the broad-line Balmer decrements and black hole masses can be estimated in a reliable and homogeneous way. This leads to 103 objects in total. Among these sources, 29 objects are abandoned since there are no distinguishable H$\beta$ broad-line components in the SDSS spectra. 18 objects are abandoned since the UVOT observations are operated in less than two filters (the disc model employed in our work have two free parameters, see Section 4.2). Two sources (SDSS J165430.72+0.709, OM 614) are abandoned as they lie on the edge of UVOT image, which can introduce large uncertainties to the photometric measurements. Two sources (2MASX J11475508+0.702284, and 2MASX J15550531+0.521119) are abandoned since their XRT spectra have less than 50 source counts, which cannot be fitted to determine the X-ray spectral slope (see Section 5.1).

Next, we discard 20 sources suffering from substantial dust extinction, which is indicated by their broad-line Balmer decrements. We assume a zero-point H$\alpha$/H$\beta = 3.06$ for AGN having no intrinsic dust extinction (Dong et al. 2008, see Section 3.4), and regard those sources with H$\alpha$/H$\beta > 3.4$ as substantial reddening (also adopted in Grupe et al. 2010). Since 2D imaging AGN–host galaxy decomposition is required in this work, we also discard the following objects: (1) six faint AGNs embedded within a dominant bulge of the host galaxy, and (2) three sources too close to a nearby star. In these 29 sources only the data in three optical filters (for the former 20 sources) or three UV filters (for the latter nine sources) can be used for spectral modelling. However, this may lead to uncertainties in the determination of the optical/UV spectral slope and model parameters. We perform simple tests to the uncertainty caused by using photometric data in only three optical or UV filters and find that the spectral slope and SED parameters can differ a lot. For instance, in PG 1138 + 222, the optical/UV spectral slopes derived are $-0.32$ (using $u$, $b$, and $r$ filters), $+0.70$ (using uvw1, uvw2, and uvw2 filters), and $+0.02$ (using all the six filters), and the difference in the fitted model parameters leads to a difference in the Eddington ratio by a factor of $\sim 10$ (0.221, 1.952, and 0.352). This is because in actual cases the spectral shapes in optical and UV bands may not be the same. Therefore, in order to get a more accurate estimation of the optical/UV spectral shape as well as a more convincing result of the spectral modelling, we do not include the above sources in our final sample. The final sample is composed of 23 sources, whose basic data are listed in Table 1.

3 DATA REDUCTION

The reduction procedures of the optical/UV photometric data, the X-ray data, and the optical SDSS spectroscopic data are described in this section. We download the pipeline-processed ‘Level 2’ UVOT and XRT FITS files from ASI Science Data Center. For sources with multiple observations, we utilize the data with the maximum exposure time. The SDSS optical spectra are downloaded from SDSS Science Archive Server.

3.1 UV data

All the sources in our sample have six UVOT filter photometric measurements in the optical ($u$, $b$, and $r$) and UV (uvw1, uvw2, and uvw2) bands. We follow the UVOT reduction threads for data reduction. The ‘Level 2’ UVOT FITS files for each of the filters are summed together by using the procedure uvotimsum, and source magnitudes are extracted by using uvotsource. We use a circle source region with a radius of 5 arcsec centring on the source, and a background region with a radius of 20 arcsec selected from a source-free region close-by. At the UV wavelengths, the starlight contribution within the aperture is negligible, and we simply consider the measurement as being dominated by the AGN radiation. For the $v$, $b$, and $u$ magnitudes, contamination from the host galaxy starlight may not be negligible, and we thus perform 2D image decomposition on the obtained images to decompose the AGN from the host galaxy. Such a procedure was also adopted in a similar work by Vasudevan et al. (2009) for UVOT data.

We use the GALFIT software developed by Peng et al. (2002) to perform 2D image decomposition. For each of the image, a point spread function (PSF) is constructed from nearby stars in the field of view (USNO A2.0 catalogue, Monet 1998) with count rates comparable to that of the target AGN. The background is calculated by selecting a source-free region near the source and is always included. The AGN is modelled with the point-like source (an instrumental PSF), with an initial magnitude and position from the results of uvotsource. A potential galaxy component is added in, as either an exponential or a Sérsic model, whichever results in a better fit. Such a model is fitted to the image data of the three optical filters, resulting in good fits in all but one object (PG 1138 + 222), which is judged by visually examining the residual images. Among these, eight objects can be well fitted with a point-like source model in all of the three filters (i.e. the host galaxy starlight contribution is

\[ \text{http://www.asdc.asi.it/mmia/index.php?mission=swiftmastr} \]

\[ \text{http://dr13.sdss.org/home} \]

\[ \text{http://www.swift.ac.uk/analysis/uvot/index.php} \]
negligible), while in the remaining 14 objects an additional galactic component (exponential) is needed to improve the fits for at least two filters. An example of the 2D imaging fitting results is shown in Fig. 1. For PG 1138 + 222, no good fit can be achieved due to the poor data quality of the UVOT images. Since no host galaxy is seen apparently in the images, we consider them to be dominated by AGN emission, and simply use the 5 arcsec aperture photometric measurements as the AGN magnitudes.

Finally, with the PSF magnitudes derived from GALFIT, we perform correction for coincidence-loss (the phenomenon when two or more photons arrive at a similar location on the detector within the same CCD readout interval, see Poole et al. 2008; Breekel et al. 2010) in the optical filters. The best-estimated optical-to-UV magnitudes of the AGN for each of the filter bands are listed in Table 2, along with the magnitudes of the host galaxies in the UVOT images. The magnitudes are corrected for the Galactic extinction by employing the Galactic reddening from Schlegel, Finkbeiner & Davis (1998).

Table 1. Basic information of our sample AGN.

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Notes: † Galactic reddening from Schlegel, Finkbeiner & Davis (1998).

Figure 1. An example of 2D image decomposition results for Mrk 1310. The rows from top to bottom represent the results in $v$, $b$, and $u$ bands, respectively. In each row, the first column shows the data image, the second column shows the best-fitting model (including the background component), and the third column shows the residual image derived by subtracting the model from the original data.
3.2 XRT data

Of 23 XRT observations of the sample objects, 22 were performed in the photon counting (PC) mode and one in the windowed timing (WT) mode (Mrk 705). We follow the XRT analysis threads\(^2\) starting with ‘Level 2’ clean event FITS files and employ xselect procedure to extract the source spectra. For the PC mode observation, the source photons are selected by using a circular region centred on the target with a radius determined from \(r = 188\) arcsec. For the WT mode, we use two circular regions with \(r = 47\) arcsec for the source and background selection, respectively. We perform pile-up correction for sources with count rates larger than \(0.5\) counts s\(^{-1}\) observed in PC mode by excluding a small region in the centre with a radius determined from ximage procedure. For Mrk 705, the observed count rate (\(\sim 0.6\) counts s\(^{-1}\)) is much less than the threshold of pile-up (100 counts s\(^{-1}\)) for WT mode. X-ray events with grades 0–12 are extracted to produce the X-ray spectra for the full energy range of the XRT (about 0.2–10 keV). For the extracted X-ray spectra, we use xrtmkarf to build the ancillary response files. The response matrix functions (RMFs) are determined individually by using quzcf. The source spectra are rebinned to have a minimum of 25 photons in each energy bin by using grppha (version 3.0.1). The information on the XRT data reduction is given in Table 3.

3.3 SDSS optical spectra

The SDSS optical emission line spectra are used to derive the Balmer decrements, as well as to estimate the masses of the black holes. The spectral analysis follows the procedure developed in our previous series work on SDSS AGN spectroscopic studies, as described in Zhou et al. (2006), Dong et al. (2008), and Liu et al. (2018). For all the sources of the sample, the SDSS spectra are clearly dominated by emission from the AGN. We fit simultaneously the AGN continuum, the Balmer lines and the Fe\(\text{II}\) emission lines. A broken power law with a break frequency at 5600 Å is adopted to fit the AGN continuum in the H\(\alpha\) and H\(\beta\) region. The optical Fe\(\text{II}\) multiplets are modelled by two separate templates built by Dong et al. (2008) based on the results of Véron-Cetty, Joly & Véron (2004). The Balmer lines are deblended into a broad and a narrow component. The broad components are fitted with one or two Gaussians assuming their redshifts to be the same, while the narrow lines are fitted with one Gaussian except for the [O\(\text{III}\)] lines. The [O\(\text{III}\)] \(\lambda 4959, 5007\) doublets are fitted with one or two Gaussians for each assuming that they have the same profiles and redshifts, with the flux ratio fixed to the theoretical value. Fig. 2 illustrates one example of the spectral fittings. Table 4 lists the results of SDSS spectral fitting for the sample objects, including the full width at half-maximum (FWHM) and the luminosities of H\(\alpha\) and H\(\beta\) broad components and the 5100 Å monochromatic luminosities \(L_{\lambda 5100}\).

3.4 Estimation of intrinsic dust extinction and black hole mass

The intrinsic dust extinction in our sample AGN is estimated from the broad-line Balmer decrement, which is derived from the flux ratio of the broad components of H\(\alpha\) and H\(\beta\). The intrinsic value of H\(\beta\)/H\(\alpha\) of AGN with no dust reddening has been a topic of debate (e.g. Dong et al. 2005; La Mura et al. 2007; Dong et al. 2008; Schnorr-Müller et al. 2016; Gaskell 2017). In this work, we adopt an intrinsic H\(\beta\)/H\(\alpha\) value of 3.06 derive by Dong et al. (2008) based

\(^{1}\)http://www.swift.ac.uk/analysis/xrt/index.php

\(^{2}\)\(\text{http://sgr.astro.psu.edu/xrt/xyout/\text{Analysis\_threads.html}}\)
Table 3. Log of XRT data reduction.

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Figure 2. Illustration of the spectral fitting for Mrk 290. The black solid line denotes the rest-frame SDSS spectrum. Purple and green lines represent the broad and narrow components of H$\alpha$ and H$\beta$, respectively. Red solid line shows the overall model.

on a sample of 446 blue AGNs, which is verified later by Baron et al. (2016) with a much larger AGN sample and has been employed in various studies (e.g. Wang et al. 2009b; Grupe et al. 2010; Liu et al. 2016). The colour excess is derived as $E(B-V) = 2.12 log \frac{L_{H\beta}}{L_{H\alpha}} = 3.06$ (1) by using the Small Magellanic Cloud (SMC) extinction curve, which is suggested to be applicable in AGN (e.g. Hopkins et al. 2004; Czerny 2007; Li 2007; Krawczyk et al. 2015, see Section 6.1 for the discussion of using other extinction curves). The derived broad-line Balmer decrements $L_{H\beta}/L_{H\alpha}$ are listed in Table 4, and their distribution is plotted in Fig. 3. The Balmer decrements are around 2.2–3.4, indicating little or no dust extinction in most of the sample objects ($H\alpha/H\beta \leq 3.06$), except for a few cases where some moderate extinction might be present. For the six objects with $H\alpha/H\beta > 3.06$, the intrinsic continuum fluxes at the six UVOT filters are derived by correcting for the excess reddening effect from the $E(B-V)$ derived above, using the IDL code ssmc.unred.pro.8

The BH masses of AGN can be estimated using the spectral measurements based on the virial method (e.g. Kaspi et al. 2000; Wang et al. 2009a). In this work, the BH masses are estimated using the FWHMs of the H$\beta$ broad component and monochromatic luminosity at 5100 Å (equation 5 in Vestergaard & Peterson 2006). It should be noted that the black hole mass estimated in this way is indirect and subject to systematics as large as ∼0.3 dex (e.g. Gebhardt et al. 2000; Greene & Ho 2006; Grier et al. 2013, the effect on our results is discussed in Section 4.2). The values of the black hole masses are also listed in Table 4, and the distribution is shown in Fig. 4. The black hole masses lie in the range of $10^7$–$10^9 M_\odot$ with a median around $10^8 M_\odot$.

4 MODELLING THE OPTICAL/UV CONTINUUM

4.1 Optical/UV spectral slopes

Assuming the optical/UV continuum of an AGN (at a redshift $z$) is radiated from a geometrically thin, optically thick disc, the rest-frame luminosity at the frequency $\nu$ is calculated as $\nu L_\nu = \nu F_\nu \times \frac{2\pi d^2}{c^2} \frac{z^2}{0.4}$, (2)

$\nu = \nu_0 (1 + z)$, (3)

8http://users.ynao.ac.cn/xbdong/
Table 4. SDSS spectral fitting results.

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Notes: Column (1): identification number assigned in this paper. Column (2): NED name of the sample objects. Column (3): FWHM of the $H\alpha$ broad component. Column (4): FWHM of the $H\beta$ broad component. Column (5): logarithmic of the luminosity of the $H\alpha$ broad component in units of erg s$^{-1}$. Column (6): logarithmic of the luminosity of the $H\beta$ broad component in units of erg s$^{-1}$. Column (7): logarithmic of the 5100 Å monochromatic luminosity in units of erg s$^{-1}$. Column (8): broad-line Balmer decrement derived from $L_{H\alpha}/L_{H\beta}$. Column (9): logarithmic of Black hole mass $M_{BH}$ derived from FWHM($H\beta$) and $L_{5100}$ (Vestergaard & Peterson 2006) in units of $M_\odot$. 

Figure 3. The distribution of the broad-line Balmer decrements for the sample.

Figure 4. The distribution of the black hole masses for the sample.

where $F_\nu_0$ is the flux density (in units of erg cm$^{-2}$ s$^{-1}$ Hz$^{-1}$) observed at a frequency $\nu_0$ in the observer’s frame. $d_L$ is the luminosity distance. $i$ is the viewing angle to the norm of the accretion disc ($i = 0^\circ$ for face-on). In this work, we assume $i = 30^\circ$, a typical value for type 1 AGN as commonly adopted and also consistent with polarization measurement (Marin 2014). It should be noted that the optical/UV continuum spectral shapes derived below are independent of the assumption of the disc inclination. The effect of varying the inclination on our results is also discussed below.

First, a simple power-law model is used to fit the optical/UV spectra. The fitted slopes $\alpha_{opt-UV}$ are listed in Table 6. Fig. 5 shows the distribution, which lie in the range of $-1.0$ to $+0.3$ with a median of $-0.39$. It shows that most of the sources have a shallower $\alpha_{opt-UV}$ than that of the SSD (+1/3), consistent with most of the previous results. Considering that the host galaxy contamination and possible dust reddening have been largely eliminated in this work, their effects on the observed spectral slopes are considered to be small, and hence cannot account for the reddening of the optical/UV spectra (see Section 6.1 for discussion on the systematics). Here, we consider that the derived continua are intrinsic emission from the AGN. As mentioned above, a shallower optical/UV spectral slope is at odds with that predicted from the SSD model.
4.2 Accretion disc model with non-standard radial temperature profile

In this work, an alternative approach is adopted as an attempt to reconcile the observation with theoretical models of accretion discs. We consider that the observed optical/UV spectra originate intrinsically from a realistic accretion disc whose radial profile of the effective temperature deviates from the SSD solution. For this purpose, a generalized radial profile of the effective temperature is assumed,

\[ T_{\text{eff}}(R) = T_{\text{eff}}(R_{\text{in}}) \times \left( \frac{R}{R_{\text{in}}} \right)^{-p} \]  

(4)

where \( T_{\text{eff}}(R_{\text{in}}) \) is the effective temperature at the inner disc radius \( R_{\text{in}} \) and the index \( p \) a free parameter. Such a model is sometimes dubbed as \( p \)-free disc model in the literature (e.g. Kubota & Makishima 2004; Kubota et al. 2005; Ai et al. 2011). This model was first introduced in the studies of black hole X-ray binaries (XRBs) to verify the disc solution in outbursts (Mineshige et al. 1994; Hirano et al. 1995). Other values of \( p \) deviating from the SSD value 0.75 have physical meanings. For instance, under the assumption of local thermodynamic equilibrium (LTE), \( T_{\text{eff}}(R) \propto M_{\text{BH}}^{1/4} M^{1/4} R^{-3/4} \) (e.g. Frank et al. 2002; Kato et al. 2008), a non-standard radial temperature profile may result from a radius-dependent mass flow rate distribution \( M(R) \propto R^{3-4p} \), where \( p \neq 0.75 \), in contrast to the constant (\( R \)-independent) \( M \) in the standard disc formalism \( (p = 0.75) \). In reality, this may well be the case for an realistic accretion disc with mass evaporation/outflow or condensation.

The total disc luminosity at a frequency \( \nu \) can be calculated as the integral of the local blackbody radiation from the inner disc radius \( R_{\text{in}} \) to the outmost disc \( R_{\text{out}} \)

\[ L_{\nu} = 2 \int_{R_{\text{in}}}^{R_{\text{out}}} \frac{\pi B_{\nu}(R) 2\pi R dR}{c^2} \]

(5)

in which

\[ B_{\nu}(R) = \frac{2\nu^3}{c^2} \frac{1}{e^{\nu/kT(R)} - 1} \]  

(6)

\[ T(R) = f_{\text{col}} T_{\text{eff}}(R) \]  

(7)

where \( T(R) \) is the color temperature and \( f_{\text{col}} \) represents the electron scattering correction to the pure local blackbody radiation (also refer to hardening factor, e.g. Shimura & Takahara 1995; Salvesen et al. 2013; Davis & EI-Abd 2019). For XRBs, a typical value of \( \sim 1.7 \) is often used (Shimura & Takahara 1995). Little is known for the hardening factor for AGN, however. The characteristic disc temperature in AGN is about two orders of magnitude lower than that in XRBs and the colour correction is suggested to be 1.0–1.6 in some studies (e.g. Czerny et al. 2011; You et al. 2016). Here, we adopt \( f_{\text{col}} = 1 \), as in some similar previous studies (e.g. Vasudevan & Fabian 2007, 2009). For a disc extending all the way to the innermost stable circular orbit, the inner disc radius \( R_{\text{in}} \) is determined by the black hole spin \( (a_*) \), from \( R_{\text{g}} \approx GM_{\text{BH}} c^2 \) is the gravitational radius) for a corotating disc around an extremely spinning BH \( (a_* = 0.99) \) to \( 3R_{\text{g}} \) \((R_g = 2M_c)\), the Schwarzschild radius) for a non-spinning BH \( (a_* = 0) \), and \( 9R_g \) for a retrograde-rotating disc around an extremely spinning BH \( (a_* = -1) \). As a common practice here a non-spinning BH is assumed following Vasudevan & Fabian (2007) and thus \( R_{\text{in}} \approx 6R_g \). \( R_{\text{in}} \) is the outer radius of the disc, which is determined by the self-gravity of the accretion disc (Laor & Netzer 1989) and set to a typical value 3000\( R_g \).\(^9\) The black hole masses derived from the optical spectral parameters (see Section 3.4) are used to calculate \( R_g \).

In this model, the inner disc temperature \( T_{\text{eff}}(R_{\text{in}}) \) and index \( p \) in equation (4) are free parameters. The value of \( p \) allowed in the fitting is set to a reasonable range of \([0.45, 0.85]\), considering the limits in the classical accretion theory \((p = 0.5 \text{ in ‘slim’ disc and 0.75 in SSD})\) and possible uncertainty in the spectral fitting procedure caused by other parameters such as black hole mass (see below). The \( \chi^2 \) routine \( \chi^2 \) (Markwardt 2009), which employs the Levenberg–Marquardt least-squares method, is used to fit the optical/UV spectra obtained above with the \( p \)-free disc model. For most of the objects, the model can fit the optical/UV data reasonably well. The best-fitting values of \( p \) and \( T_{\text{eff}}(R_{\text{in}}) \) are listed in Table 6. The measured AGN optical/UV luminosities and the best-fitting disk models are shown in Fig. 6.

The above fitted \( p \) and \( T_{\text{eff}}(R_{\text{in}}) \) values are obtained by assuming a specific set of parameters of the BH and the accretion disc, which might deviate in reality. Moreover, the black hole masses estimated in Section 3.4 from the single-epoch optical spectra are subject to systematic uncertainties as large as \( \sim 0.3 \text{ dex} \). To investigate the systematics of the fitted \( p \) and \( T_{\text{eff}}(R_{\text{in}}) \) values caused by these uncertainties, the above fitting procedure is repeated for \( 5000 \) times using various combinations of the values of these parameters which are drawn randomly from reasonable ranges in the parameter space of \( M_{\text{BH}}, a_*, \text{ and } i \). Specifically, \( M_{\text{BH}} \) is drawn from a Gaussian distribution of \( \log (M_{\text{BH}}) \) with a standard deviation \( \sigma = 0.3 \), and \( i \) and \( a_* \) from a uniform distribution in the \([0^\circ–60^\circ]\) and \([-0.99 \text{ to } +0.99]\) ranges, respectively. The 1\( \sigma \) error of \( p \) and \( T_{\text{eff}}(R_{\text{in}}) \) is derived from the simulated distribution and given in Table 6.

Fig. 7 shows the distribution of the best-fitting indices of \( p \). The majority lie between 0.5 and 0.75 with a median of 0.63, suggesting a flatter radial temperature profile than that of the SSD model (0.75) in most of the sample objects. Theoretically, the slope of the power-law regime of an emergent disc spectrum in optical/UV band can be determined by the radial temperature profile of the disc, and thus a relation between the two can be predicted, as \( \alpha_{\text{opt-UV}} = 3 - 2/p \) (e.g. Gaskell 2008). The relationship between the obtained \( p \) values and \( \alpha_{\text{opt-UV}} \) is shown in Fig. 8, which is found to be consistent with

\[^9\text{Generally, } R_{\text{out}} \gtrsim 1000R_g \text{ for a black hole with a mass of } 10^8 M_{\odot}. \text{ Considering that the temperature in lower mass black holes (} M_{\text{BH}} \approx 10^3 M_{\odot} \text{) is relative higher and the emission from outer radius can have a contribution to the emission in optical band, we take a commonly adopted value 3000R_g.}\]
Figure 6. The SEDs for our sample, including the measured luminosities and spectral models in optical/UV and X-ray bands. Red dots represent the measured luminosities in the six UVOT filters. Black crosses represent the X-ray luminosities obtained by XRT instrument. The spectral model components are denoted by dashed lines in different colours. The red dashed line represents the $p$-free disc model. The green dashed line represents the blackbody model (if required). The blue dashed line represents the power-law model, which is extrapolated by an exponential cutoff at both ends. The sum of all models is represented by a pink solid line. The data and models are in the source rest-frame.
The distribution of the radial temperature power-law index $p$, obtained from the optical/UV spectral fitting using the $p$-free disc model. The two black dotted lines represent $p = 0.5$ (‘slim’ disc solution) and $p = 0.75$ (SSD solution). The red dotted line represents $p = 0.63$ (the median).

Fig. 8 also reveals a few outliers with rather redder spectra. By examining, the spectral fits it is clear that for these sources the UVOT data sampled mostly the Wien rather than the power-law regime of the spectrum (this also leads to a strong dependence of the theoretical relation for most of the objects. In these sources, the UVOT data mainly sampled the power-law portion of the emergent disc spectra. The value of $p$ is mainly determined by $\alpha_{\text{opt-UV}}$ and has a weak dependence on the black hole mass (thus has a small uncertainty). The Spearman’s rank test confirms a strong correlation between these two parameters ($\rho_s = 0.63$ and $P = 1.320 \times 10^{-3}$).
5 Broad-band SED and bolometric correction factors

It has been shown above that the optical/UV spectra in most of our AGN can well be reproduced by emission from accretion discs with a flattened radial temperature profile. As a result, such a disc produces relatively lower emission in the EUV band than that previously predicted for an SSD model with the $F_\nu \propto N_\lambda^{1/3}$ spectrum. This energy band is thought to be where the disc emission peaks, and thus contains a substantial fraction of the bolometric luminosity. In the rest of the paper, we investigate the broad-band SED for our sample AGN assuming that a non-SSD radial temperature profile may operate in accretion discs.

Aside from the optical/UV band, another dominant emission bandpass is X-ray. In this section, we first model the X-ray emission by making use of the simultaneous Swift/XRT observations. Then, the broad-band SEDs are constructed and the bolometric luminosities are derived. Finally, the bolometric correction factors are studied for the X-ray and optical bands.

5.1 The 0.3–10 keV X-ray band

We make use of the XSPEC software (Arnaud 1996, version 12.9.1) to model the XRT spectra of our sample objects in the observed 0.3–10 keV energy band. An absorbed power-law model ($\text{wabs}\times\text{powerlaw}$) with a free absorption column density ($N_H$) is fitted to the spectra at first, and the fitted $N_H$ do not show evidence for excess absorption above the Galactic value. We thus fix the absorption column densities at the Galactic value for better constraining of the spectral parameters. The spectra of six AGN can be well fitted with a simple absorbed power-law model. In other 16 sources, a possible soft excess component below 2 keV is indicated in the fitting residuals when the model is fitted to the 2–10 keV data and is extrapolated below 2 keV. We thus add a blackbody component in the model ($\text{wabs}\times(\text{bbody}+\text{powerlaw})$), whose addition is justified by using the $F$-test and an acceptance $P$-value of $P < 0.05$ is adopted. For these objects, an absorbed power-law plus a soft X-ray excess model is found to better describe the X-ray spectra. The temperature of the soft excess is found to be $T_b \approx 0.1$–0.2 keV, consistent with the typical values in AGN. In the remaining source RX J1209.8 + 3217, a distinct feature is noticed, with a possible absorption around 1–2 keV. A power-law model plus an ionized absorption component ($\text{wabs}\times\text{absori}\times\text{powerlaw}$) with their photon indices tied with each other gives a satisfactory fit. The results of the X-ray spectral analysis are summarized in Table 5 (the errors are given in 90 per cent confidence interval). We note that the reflection component which is often observed in Seyfert galaxies should have a negligible effect to the determination of X-ray power-law continuum in this work, as the practical energy range of the XRT spectra for our sample objects are all below 8 keV.

5.2 Broad-band spectral energy distributions

Based on the spectral fitting results in both the optical/UV and X-ray bands, we construct the broad-band SED by integrating the spectral models from the optical to X-ray band. For the optical to EUV band, the emergent spectrum from an accretion disc model with the best-fitting $p$ and $T_{\text{eff}}(R_{\text{in}})$ parameters is calculated from equations (4)–(7). For the X-ray band, the power-law continuum, which is thought to originate from a hot corona, is extrapolated to both the lower and higher energy bands. At the lower energy end (EUV to soft X-rays), an operational cut-off energy is applied, as often adopted in the literature (e.g. Grupe et al. 2010; Fanale et al. 2013), since the corona emission does not contribute significantly to the UV band. The $\epsilon$-folding energy is determined for each object individually based on the consideration of Compton scattering of the disc emission.10 It should be noted that the exact value of this cut-off energy within a reasonable range has almost no effect on the calculation of bolometric luminosity. At the higher energy end, observations have revealed an exponential cutoff in the power-law spectra of AGN in the hard X-ray band, with a cut-off energy $E_{\text{cut}} = 150$–250 keV for Seyfert galaxies (e.g. Dudina 2008; Malizia et al. 2014). We note that the choice of the exact $E_{\text{cut}}$ value within this range has only little effect on the bolometric luminosities, causing a scatter of only 0.05 dex. We thus assume a uniform high energy exponential cut-off $E_{\text{cut}} = 200$ keV for all the objects.

We overplot the derived broad-band SED models for our sample in Fig. 6, along with the measured luminosities and the best-fitting spectral models in the optical/UV and X-ray bands. Some of the parameters of the SED are summarized in Table 6 (the errors are given in 1σ). The effective optical-to-X-ray spectral index $\alpha_{\text{OX}}$ is calculated by measuring the luminosity densities at 2500 Å and 2 keV ($\alpha_{\text{OX}} = -0.384\log L(2\text{keV})/L(2500\text{Å})$, Tananbaum et al. 1979). $L_{5100}$ is the monochromatic luminosity at 5100 Å. $L_{2-10}$ is the rest-frame 2–10 keV bolometric luminosity. The bolometric luminosity $L_{\text{bol}}$ is defined as the integral of the SED within the energy range of 0.001–300 keV. The Eddington ratios $\lambda_{\text{Edd}}$, defined as $L_{\text{bol}}/L_{\text{Edd}}$, are derived. The errors of $p$, $T_{\text{eff}}(R_{\text{in}})$, $L_{5100}$, and $\alpha_{\text{OX}}$,\tablefootnote{The power-law model drops toward low energies as an exponential decay $\exp(-E_{\text{cut}}/E_{\text{in}})$ in EUV band. The $E_{\text{cut}}$ is determined for each individual source as (1) $4E_{\text{cut}}$ is the minimum scattered energy after inverse Compton scattering; and (2) the peak of the continuum is determined by the fitted accretion disc model above.} are derived from the Monte Carlo simulations in the optical/UV band (see Section 4.2). The error of $L_{2-10}$ is derived by using XSPEC command cflux. The error of $L_{\text{bol}}$ is derived from a simulated distribution (A group of 5000 simulated X-ray luminosities is obtained by drawing them randomly from a Gaussian distribution, with a standard deviation $\sigma$ derived by using cflux). The luminosities are added to 5000 Monte Carlo-simulated disc luminosities to generate a group of 5000 simulated bolometric luminosities ($L_{\text{bol}}$). The errors of other parameters which are dependent on $L_{\text{bol}}$, such as $\lambda_{\text{Edd}}$, $\kappa_{2-10}$ (see Section 5.3), are also derived.

The averaged SED is often used to study the dependence of the SED shape on some key parameters, as it can minimize the intrinsic dispersions among individual objects. The sample objects are divided into three groups according to their Eddington ratio $\lambda_{\text{Edd}}$, i.e. low-, $\lambda_{\text{Edd}} \lesssim 0.03$ (eight objects), intermediate-, $0.03 \lesssim \lambda_{\text{Edd}} \lesssim 0.09$ (eight objects), and high-, $\lambda_{\text{Edd}} \gtrsim 0.09$ (seven objects).
SEDs are all normalized at 1 eV and the average of their logarithms are calculated in each $\lambda_{\text{Edd}}$ bin. The three averaged SEDs are plotted in Fig. 9, together with the 68 per cent scatter. It shows clearly that, as $\lambda_{\text{Edd}}$ increases, the optical/UV (disc) emission gradually dominates the overall energy budget, with the peak luminosity shifts to higher frequencies in EUV band; meanwhile, the X-ray continuum (corona emission) becomes softer in higher-$\lambda_{\text{Edd}}$ objects. These results are generally consistent with previous findings (e.g. Shimmer et al. 2006; Vasudevan & Fabian 2009).

5.3 Bolometric corrections

The bolometric luminosities obtained above are used to derive bolometric correction factors at a specific luminosity or band,

$$\kappa_b = \frac{L_{\text{bol}}}{\lambda_{5100}}$$

Here, we focus on two frequently used factors, $\kappa_{2-10}$ for the 2–10 keV X-ray band and $\kappa_{5100}$ at the optical 5100 Å wavelength, respectively.

5.3.1 2–10 keV bolometric correction

The 2–10 keV bolometric correction reflects the relative contribution of the corona X-ray emission in the total radiation power of AGN. Previous studies suggested dependences of $\kappa_{2-10}$ on a few parameters including $\lambda_{\text{Edd}}$, $\Gamma_X$, and $\chi_{\text{ox}}$. Vasudevan & Fabian (2007) found that $\kappa_{2-10}$ increases with $\lambda_{\text{Edd}}$, which was confirmed later in various studies (e.g. Lusso et al. 2010; Jin et al. 2012; Fanali et al. 2013). The distribution of the derived $\kappa_{2-10}$ for our sample AGN is shown in Fig. 10, spanning a wide range $\sim$10–100 with a median of $\sim$19. There is a correlation between $\kappa_{2-10}$ and $\lambda_{\text{Edd}}$ ($\rho = 0.74$ and $P = 6.4 \times 10^{-5}$), consistent with those found in previous studies. The $\kappa_{2-10}$ versus $\lambda_{\text{Edd}}$ is plotted in Fig. 11. A bisector regression analysis using the ordinary least-squares algorithm yields a linear relationship equation (9), which is overplotted in Fig. 11.

$$\log \kappa_{2-10} = (0.473 \pm 0.068) \log \lambda_{\text{Edd}} + (1.922 \pm 0.105)$$

The averaged bolometric correction factors are also obtained for the above groups of the Eddington ratios (low-$\lambda_{\text{Edd}}$, $\lambda_{\text{Edd}} \lesssim 0.03$; intermediate-$\lambda_{\text{Edd}}$, $0.03 < \lambda_{\text{Edd}} \lesssim 0.09$; and high-$\lambda_{\text{Edd}}$, $\lambda_{\text{Edd}} \gtrsim 0.09$), $\kappa_{2-10}$ is found to be $8 \pm 15$ for $\lambda_{\text{Edd}}$ $\lesssim 0.03$, $15 \pm 30$ for $0.03 < \lambda_{\text{Edd}} \lesssim 0.09$, and $20 \pm 70$ for $\lambda_{\text{Edd}} \gtrsim 0.09$. As in previous work, the SSD model was adopted in fitting the optical/UV spectra of AGN, it is of interest to compare our result with previous ones. In Fig. 11, the results from Vasudevan & Fabian (2009) and Fanali et al. (2013) are overplotted for comparison. It can be seen that objects with low- and intermediate-$\lambda_{\text{Edd}}$ in our sample have similar $\kappa_{2-10}$ values to those in Vasudevan & Fabian (2009), while the high-$\lambda_{\text{Edd}}$ objects have lower $\kappa_{2-10}$ values in general. The slope of the linear regression is

**Notes:** Column (1): identification number assigned in this paper. Column (2): NED name of the sample objects. Column (3): the XSPEC models used: (a) wabs×powerlaw (b) wabs×(bbbody + powerlaw) (c) wabs×absor×powerlaw. Column (4): the neutral hydrogen column density $N_H$ used in wabs in units of $10^{20}$ cm$^{-2}$. Column (5): the hard X-ray photon index $\Gamma_X$ in powerlaw. Column (6): the blackbody temperature in units of keV in bbbody. Column (7): logarithmic of the observed 2–10 keV flux in units of erg cm$^{-2}$ s$^{-1}$. Column (8): the goodness of fit for the model. Column (9): the XRT count rates in the observed 0.3–10 keV band in units of counts s$^{-1}$. The errors are given in 90 per cent confidence interval.
A marginal correlation is found (\(\rho = 0.59 \) and \(P = 3.3 \times 10^{-3}\)). Using a bisector regression analysis gives

\[
\log \kappa_{2-10} = (0.932 \pm 0.151)\log \Gamma_X - (0.417 \pm 0.278)
\]
Figure 11. Hard X-ray bolometric correction factor $\kappa_{2-10}$ versus Eddington ratio $\lambda_{\text{Edd}}$. The black dots represent the sources in our sample, and the errors are given in 1σ. The black solid line is the bisector regression line. The green dashed line is the best-fitting regression line obtained in Fanali et al. (2013). The yellow crosses are the binned data points in Vasudevan & Fabian (2009).

Figure 12. Hard X-ray bolometric correction factor $\kappa_{2-10}$ versus hard X-ray photon index $\Gamma_X$. The black dots represent the sources in our sample. The error of $\Gamma_X$ is given in 90 per cent confidence interval, and the error of $\kappa_{2-10}$ is given in 1σ. The black solid line represents the best-fitting regression. The green dashed line is the result in Jin et al. (2012).

The $\kappa_{2-10}$ versus $\alpha_{\text{OX}}$ distribution is plotted in Fig. 13, along with the relations reported in previous studies. Our fitted curve generally agrees with those derived in Lusso et al. (2010) and Marchese et al. (2012), but lower than that in Jin et al. (2012). Our result confirms that, compared to $\lambda_{\text{Edd}}$ and $\Gamma_X$, $\alpha_{\text{OX}}$ appears to be a better indicator for $\kappa_{2-10}$. We note that the above correlations ($\kappa_{2-10}$-$\lambda_{\text{Edd}}$, $\kappa_{2-10}$-$\Gamma_X$, and $\kappa_{2-10}$-$\alpha_{\text{OX}}$) can also be inferred from the study of the averaged SED (see Fig. 9).

5.3.2 Optical 5100 Å bolometric correction

Early studies suggested a constant 5100 Å bolometric correction factor, e.g. $\kappa_{5100} = 9.0$ (Kaspi et al. 2000) and $\kappa_{5100} = 10.3 \pm 2.1$ (Richards et al. 2006), with weak or no dependence of $\kappa_{5100}$ on $\lambda_{\text{Edd}}$. Vasudevan & Fabian (2007) suggested a positive correlation similar to $\kappa_{2-10}$, which was confirmed by Jin et al. (2012) using a high-$\lambda_{\text{Edd}}$ AGN sample. The distribution of $\kappa_{5100}$ in our work is shown in Fig. 14, within a range of $8-20$ for most of the AGN. The median value of 12 is broadly consistent with $10.3 \pm 2.1$ given by Richards et al. (2006) for quasars. However, no correlation is found between $\kappa_{5100}$ and $\lambda_{\text{Edd}}$ for our sample ($r_s = -0.031$ and $P = 0.89$, see Fig. 15), which is in contrary to the results in Vasudevan & Fabian (2007) and Jin et al. (2012). Similar to the case in $\kappa_{2-10}$, this is also due to the flatter radial temperature profiles in high-$\lambda_{\text{Edd}}$ objects than those with low- and intermediate-$\lambda_{\text{Edd}}$ (see Section 6.4 for a detailed discussion).

6 DISCUSSION

6.1 Optical/UV spectral slope

The optical/UV spectrum is of great importance to the determination of the broad-band SED of AGN. The power-law spectral slopes $\alpha_{\text{opt-UV}}$ have been measured for many AGN in large samples in numerous studies using photometric and spectroscopic data from various surveys, e.g. SDSS (Vanden Berk et al. 2001; Davis et al. 2007), Far Ultraviolet Spectroscopic Explorer (FUSE, Scott et al. 2004), Cosmic Origins Spectrograph onboard Hubble Space Telescope (HST/COS, Shull et al. 2012; Stevans et al. 2014), AKARI Space Telescope (Jun et al. 2015), X-shooter onboard Very Large Telescope (VLT/X-shooter, Selsing et al. 2016), and UVOT.
The errors are given in $\kappa_{5100}$ from that of the host galaxy by using the 2D image decomposition may not be negligible. We try to separate the AGN (nuclear) flux of 1 arcsec for AGN photometry the host galaxy contamination wavelengths. Bentz et al. (2006) pointed out that even for an aperture source of uncertainty in measuring AGN optical emission at long discussed below.

The contamination of the host galaxy starlight is the main source of uncertainty in measuring AGN optical emission at long wavelengths. Bentz et al. (2006) pointed out that even for an aperture of 1 arcsec for AGN photometry the host galaxy contamination may not be negligible. We try to separate the AGN (nuclear) flux from that of the host galaxy by using the 2D image decomposition algorithm GALFIT, as commonly done in previous work (e.g. Bentz et al. 2009; Vasudevan et al. 2009; Koss et al. 2011), even though the spatial resolution of the UVOT images is not high (a typical FWHM of ~2 arcsec). To check the reliability of our image decomposition analysis, we compare our results with the previous ones for the seven objects which were also studied for image decomposition by Koss et al. (2011) using the SDSS images with a better resolution. The magnitudes of the galactic component derived in this work are broadly consistent with those derived in Koss et al. (2011) with differences in the fluxes around 10–20 per cent. We consider the uncertainties to be small and our results to be reliable.

As commonly adopted in AGN studies, we assume that the dust extinction of the optical/UV continuum can well be represented by that in the broad-line region, which can be estimated from the broad-line Balmer decrement. There is good observational basis for this argument (e.g. Dong et al. 2008; Gaskell 2017). Our sample is selected in such a way that the dust extinction effect is negligible or minor at most. For most (17/23) of our sample objects, the Balmer decrements are consistent with the value for which little or no dust extinction is present. For the remaining six sources, there may be a minor effect and the amount of dust reddening is derived by assuming an SMC-like extinction curve in the analysis. The effect of using different extinction curves is also investigated, including the extinction curves of the MW, the average curves of the Large Magellanic Cloud (LMC) and the LMC2 supershell (Gordon et al. 2003). For these objects, the optical/UV photometric data are corrected for the reddening effect by assuming the above curves. The resulting spectra are fitted with a power-law model as well as the p-free disc model, respectively. This results in typical changes in the optical/UV slopes of ~5 per cent only and ~2 per cent in the index p. We thus conclude that the use of different extinction curves does not affect our results significantly for those objects in which minor dust reddening might occur. Therefore, in the rest of this work, the SMC-like extinction curve is adopted.

6.2 Accretion discs with non-standard radial temperature profile

It has been demonstrated that the shallower spectral slopes in our sample AGN cannot be attributed mainly to starlight contamination or dust reddening. We consider such spectral shapes intrinsic to the emission from the AGN, which can well be produced by an accretion disc with a radial temperature profile flatter than the canonical $T_{\text{eff}}(R) \propto R^{-0.75}$ for the standard SSD model. Theoretically, the spectral slope $\alpha$ of the power-law regime of an accretion disc spectrum and the effective temperature power-law index $p$ are related via $\alpha = 3 - 2/p$ (e.g. Pringle & Rees 1972; Kato et al. 2008). For SMBHs, the power-law regime of the spectra falls into the optical/UV waveband for a wide range of $M_{\text{BH}}$ and $\lambda_{\text{Edd}}$, and the slope $\alpha_{\text{opt,UV}}$ can be reddened depending on the exact value of $p$. Gaskell (2008) suggested that $p \approx -0.57$ can explain the typical spectral slopes of $\alpha \approx -0.5$ observed in AGN. In this work, we apply this model, for the first time, to fit the optical/UV spectra for a sample of AGN with simultaneous multi-band photometric data. It is found that, the inferred radial effective temperature profile indices $p$ fall within a range of 0.5–0.75 for most of the sample objects in order to explain the observed spectra, flatter than $p = 0.75$ for the SSD widely assumed in previous studies.

Accretion discs with a non-standard radial temperature profile ($p \neq 0.75$) may operate if one or more of the assumptions underlying the standard SSD break down. For instance, the local thermal equilibrium condition may not hold, if the dissipated accretion energy cannot be radiated away efficiently locally, and consequently the energy/photons are advected into the black hole. Alternatively, the assumption of mass conservation may not hold as, for instance, part of the accreted mass is lost in the accretion process due to various mechanisms (e.g. disc winds/outflows).

To gain an insight into the cause of the non-standard radial temperature profiles, the relationship is examined between $p$ and the Eddington ratio $\lambda_{\text{Edd}}$, which is considered to be the most possible dominant quantity that governs the accretion process of AGN. A marginal correlation is found ($\rho_1 = -0.41$, and $P = 5.0 \times 10^{-2}$), as shown in Fig. 16, where the results derived using different dust extinction curves for the sources with intrinsic reddening are marked in different colours. The correlation becomes more prominent when only the sources having no intrinsic dust reddening are used ($\rho_1 = -0.71$, and $P = 1.4 \times 10^{-3}$). Such a correlation is qualitatively consistent with the above physical explanations. For instance, when the accretion rate is well below the Eddington limit, the radiative diffusion time-scale in the disc is much faster than the accretion time-scale. Such an accretion flow is radiatively efficient and has a radial temperature distribution of SSD type ($T_{\text{eff}}(R) \propto R^{-0.75}$). However, when the accretion rate approaches the Eddington limit ($\lambda_{\text{Edd}} \gtrsim 0.3$, e.g. Abramowicz et al. 1988; Mineshige et al. 2000), the photon trapping effect in the disc becomes appreciable and the disc becomes a ‘slim’ disc. In this case, the radiation energy is trapped and advected inward rather than locally radiated away, resulting in a much flatter radial temperature profile ($T_{\text{eff}}(R) \propto R^{-0.5}$, e.g. Wang et al. 1999; Watarai & Fukue 1999). Given the distribution of the Eddington ratio of our sample, the flat temperature profiles in most of the sources can hardly be induced by the photon trapping.  

![Figure 15. Optical (5100 Å) bolometric correction factor $\kappa_{5100}$ versus Eddington ratio $\lambda_{\text{Edd}}$. The black dots represent the sources in our sample. The errors are given in 1σ. The red dotted line represents $\kappa_{5100} = 12$ (the median). The black dotted line represents $\kappa_{5100} = 9.0$ (Kaspi et al. 2000). (Lawther et al. 2017). Despite large scatter, the optical/UV spectra are found to have shallower slopes in most of the studies. The spectral slopes obtained in our work, with elimination of the effects of the host galaxy contamination and dust extinction, are broadly consistent with previous results. Yet, there may be uncertainties inherent in these measurements which may bias the results, as discussed below. The contamination of the host galaxy starlight is the main source of uncertainty in measuring AGN optical emission at long wavelengths.
Nevertheless, we suggest that this effect may operate in some of the high-\(\lambda_{Edd}\) sources and be partly responsible for the observed \(p-\lambda_{Edd}\) correlation.

Another possible physical explanation is offered by the mass-loss process in form of outflows/disc winds, as a power-law radial temperature profile with an index \(p \neq 0.75\) implies a non-stationary mass inflow rate \(M(R) \propto R^{3-p}\) under the LTE assumption. In fact, observations suggest that outflows may be prevalent or even ubiquitous in bright AGN, and are likely stronger in higher-\(\lambda_{Edd}\) sources (e.g. Laor & Brandt 2002; Ganguly et al. 2007; Zhang et al. 2014). In this picture, the \(p-\lambda_{Edd}\) relation found in our work can thus be understood, as the \(p\)-value is determined by the amount of mass loss, i.e. a smaller \(p\)-value (a steeper mass flow rate distribution and thus a stronger mass loss) tends to be found in higher-\(\lambda_{Edd}\) sources.

Interestingly, Gofford et al. (2015) studied the properties of highly ionized outflows for a sample of 51 AGN observed with Suzaku and found that the mass-loss rate of the outflow (\(M_{\text{loss}}\)) is well correlated with the bolometric luminosity (\(L_{\text{bol}}\)) of the source. Recently, it has been well interpreted under the mechanism of the line-driven disc wind by numerical simulations (e.g. Nomura & Ohsuga 2017; Nomura, Ohsuga \\& Done 2018). In this work, by assuming that the deviation of the radial temperature profile is caused by the mass-loss process, we can also investigate the \(M_{\text{loss}}-L_{\text{bol}}\) relation from the spectral fitting results.

In order to calculate the mass-loss rate for the sample AGN, the mass flow rate profile \(M(R)\) for each object is obtained from the best-fitting radial temperature distribution \(T_{\text{eff}}(R)\) (see Section 4.2) under the LTE assumption (\(T_{\text{eff}}(R) = f(M(R), M_{\text{Bol}}, R) \propto M(R)^{1/4} M_{\text{Bol}}^{1/4} R^{-3/4}\), e.g. Frank et al. 2002; Kato et al. 2008). With this accretion rate profile, the mass-loss rate is calculated by

\[
M_{\text{loss}} = M(\text{Russell}) - M(R) \tag{12}
\]

We note that the mass-loss rate is positive when \(p < 0.75\) and negative when \(p > 0.75\). For the latter case, this indicates an ‘inflow’ instead of ‘outflow’. In this work, we do not take this ‘inflow’ explanation for the sources with \(p \gtrsim 0.75\), considering the uncertainties inherent in our spectral fitting procedure. The accretion discs in these sources are regarded to be the SSD-type. We also note that although the mass-loss rate formally depends both on \(p\) and \(\lambda_{Edd}\), the dependence on \(p\) is decisive as it appears in the power-law index of the accretion rate formula thus determines the steepness of the distribution. In other words, no matter how large \(T_{\text{eff}}(R)\) (the accretion rate at \(R_{\text{in}}\)) is, a \(p\)-value close to 0.75 (the SSD solution) stands for a weak/negligible outflow solution (\(M_{\text{loss}} \approx 0\)).

The bolometric luminosity \(L_{\text{bol}}\) is derived by integrating the SED model within the energy range of 0.001–300 keV. We note that \(L_{\text{bol}}\) depends mainly on \(T_{\text{eff}}(R_{\text{in}})\), and the relation can roughly be a fourth power when \(L_{\text{bol}} \approx L_{\text{bol}}\) under high-\(\lambda_{Edd}\) condition. The dependence on \(p\), however, is inconspicuous (there is no statistical correlation between \(L_{\text{bol}}\) and \(p\)). One should keep in mind that the two free parameters \(p\) and \(T_{\text{eff}}(R_{\text{in}})\) is not correlated (the former is determined by the optical/UV spectral slope, and the latter by the observed flux).

Fig. 17 shows the obtained relation between \(M_{\text{loss}}\) (in units of g s\(^{-1}\)) and the bolometric luminosity \(L_{\text{bol}}\) for 17 sources with \(p < 0.75\) in our sample (in other six sources, the stationary disc solution \(p = 0.75\) can be satisfied considering the uncertainties). It is clear that the resulting relation is in agreement with the observational result obtained by Gofford et al. (2015). Since the mass-loss rate and bolometric luminosity derived in our work can be regarded as irrelevant to each other, as we showed above, the relation obtained here is an independent proof that verifies the results in their work. This also suggests that the observed reddened optical/UV spectra in the AGN of our sample are likely a result of the flatter radial temperature profiles of their accretion discs than the standard SSD profile. Such a flat temperature profile may be caused by mass loss in the form of outflows as the mass is accreted inward.

Apart from these two scenarios, the deviation of the radial temperature profile could also result from an accretion disc illuminated by an external radiation source (e.g. Czerny et al. 2008), or the irradiation of the outer areas by its inner part (e.g. Sanbuichi et al. 1993). By introducing an additional heating term which is more pronounced in the outer areas of the AGN disc, a flattened radial temperature profile can be obtained and lead to a reddened optical/UV spectra (e.g. Soria \\& Puchnarewicz 2002; Loska et al. 2004). However, this usually requires the disc to be warped (\(H_{\text{z}} \approx R\), \(H_{\text{z}}\) is the vertical height of the disc at radius \(R\), e.g. Pringle 1997). In our work, we only consider flat (geometrically thin) accretion discs (\(H_{\text{z}} \ll R\)). In this case, the irradiating disc gives a radial...
dependence of the temperature identical to the one derived for the SSD (see Netzer 2013, chapter 4.2.2).

6.3 Implication to the SED modelling of AGN

In the modelling of the AGN optical/UV continuum in previous studies, the spectrum from the SSD model is mostly adopted and assumed to be subject to dust reddening with $E(B - V)$ as a free-fitting parameter (e.g. Vasudevan & Fabian 2009; Vasudevan et al. 2009; Capellupo et al. 2016; Castelló-Mor, Netzer & Kaspi 2016). While such a model can reproduce the optical/UV spectra reasonably well, it implies an enormous energy budget of the intrinsic source luminosity in the far- and extreme-UV regime, where the multitemperature blackbody from the accretion disc peaks (the so-called ‘BBB’). On the other hand, the $p$-free disc model with a flat radial temperature profile leads to a less prominent EUV bump and a lower peak energy (due to lower $T_{\text{eff}}$ in the inner disc), and thus lower energy output. Given that the bolometric luminosity is dominated by the energy in this regime, the two models may result in somewhat different bolometric luminosities. In another word, if in reality, the accretion disc is indeed better described by a non-standard radial temperature profile, the bolometric luminosities calculated assuming the SSD model must be overestimated systematically to some extent.

As a demonstration, a quantitative comparison between the broadband SED based on the two models is carried out for two selected objects in our sample with shallower spectral slopes, SBS 1136 + 594 ($\alpha_{\text{opt-UV}} = -0.2$) and Mrk 493 ($\alpha_{\text{opt-UV}} = -0.12$). Their optical/UV spectra can be fitted equally well with the SSD model which is reddened using the SMC extinction curve with $E(B - V)$ as a free parameter. The fitted broadband SED model is plotted in Fig. 18, together with those obtained assuming the $p$-free disc model above in this work. An excess dust reddening of $E(B - V)$ (0.08 and 0.12, respectively) is required to reproduce the observed optical/UV spectra in both sources, albeit their Balmer decrements ($<3.06$) indicate no reddening. The overall disc luminosities based on the SSD model is higher than that for the $p$-free disc model by a factor of 3.4 and 5.9, respectively. The differences are comparable to those derived in Slone & Netzer (2012), in which the accretion energy carried away by disc winds is considered in calculating the emergent radiation of the accretion disc, effectively similar to the approach adopted in this work. This results in an overestimation of the bolometric luminosity $L_{\text{bol}}$ by a factor of 2.1 and 5.0, respectively. The difference would be even more pronounced for sources with even more flatter radial temperature profiles (for instance, for RX J1702.5 + 3247 in which $p \approx 0.54$ the difference in $L_{\text{bol}}$ is around 8.0).

We note that the uncertainties inherent in our method should be considered when assessing the significance of this difference. In this work, we implement the estimation of the uncertainties in two ways. For the optical/UV band, we employ the Monte Carlo method to estimate the uncertainty in $L_{\text{disc}}$, which is caused by the systematics of various physical parameters in the $p$-free disc model ($M_{\text{BH}}, i, \alpha_0$). As for the X-ray (corona) luminosity, the statistical error is calculated using XSPEC/eflux. By the combination of these two methods, the 1σ uncertainty in $L_{\text{bol}}$ is found to be 0.1–0.3 dex for the sample objects (see Table 6). In this sense, the differences in $L_{\text{bol}}$ obtained in a moderate fraction of the sample (8/23) are somewhat significant as they exceed the uncertainties (the differences are somewhat by a factor of 4–8). However, we should keep in mind that there are certainly other contributions to the uncertainty in $L_{\text{bol}}$ which are not considered in this estimation. For instance, the contribution of the soft excess below the lower end of the Swift/XRT bandpass is difficult to be robustly constrained by the blackbody model. In fact, there are various physical models in describing this mystical component, such as the thermal comptonization model (e.g. Magdziarz et al. 1998; Done et al. 2012) and the blurred ionized reflection model (e.g. Crummy et al. 2006). As a pilot test, we attempt the thermal comptonization model optxagnf (Done et al. 2012) to some of the sample AGN in which a strong soft X-ray excess exists (e.g. Mrk 142, RX J1355.2+5612, RX J1702.5 + 3247) and find that the derived bolometric luminosities are higher than those derived in this work by a factor of 3–4. This indicates that alternative models of the soft excess may also lead to an overestimation of $L_{\text{bol}}$. As a first study of the effects caused by using the $p$-free disc model, we mainly pay our attention to the distinction in the optical/UV band. Further investigations including a more physical model in describing the soft excess will be implemented in future work.

Our results show that the traditional way in modelling the optical/UV spectra (the SSD model subject to an additional dust reddening) could indeed lead to an overestimation of the disc luminosity when the intrinsic spectra are found to be redder than that of the SSD. As the redder-than-SSD spectra have been widely observed in the literature and the disc luminosity usually dominates...
the overall energy budget, this also suggests that the bolometric luminosities and hence the Eddington ratios for many AGN may have been overestimated in some of the previous studies (probably by a factor of several).

6.4 Bolometric correction factors

The bolometric correction factor $\kappa_\nu$ is a convenient quantity used to derive the bolometric luminosity $L_{\text{bol}}$ (representing the accretion rate $M$) of an AGN based on photometric measurement in a specific waveband. The commonly used factors are $k_{2-10}$ for the X-ray band and $k_{5100}$ for the optical. There have been studies on $k_{5100}$ and $k_{2-10}$ in the literature, which are found to be dependent on some other parameters in some of the studies. For instance, a strong correlation between $k_{2-10}$ and $\lambda_{\text{Edd}}$ was reported (e.g. Vasudevan & Fabian 2007, 2009; Vasudevan et al. 2009; Lusso et al. 2010). The hard X-ray photon index $\Gamma_X$ (e.g. Jin et al. 2012) and the optical-to-X-ray effective index $\alpha_{\text{OX}}$ (e.g. Lusso et al. 2010; Marchese et al. 2012) were also suggested to correlate with $k_{2-10}$. As for the optical band, a correlation between $k_{5100}$ and $\lambda_{\text{Edd}}$ was reported in Vasudevan & Fabian (2007) and later confirmed by Jin et al. (2012). These correlations were mostly derived from the broadband SED analysis assuming the SSD model in the optical/UV and EUV bands. As discussed above, for those sources with reddened optical/UV spectra the employment of the p-free disc model implies a much lower EUV bump and hence a smaller $L_{\text{bol}}$ compared to the SSD model. It is therefore of interest to re-investigate the bolometric correction factors and their dependence on some of the key parameters.

Compared to Vasudevan et al. (2009), the increase of $k_{2-10}$ with $\lambda_{\text{Edd}}$ is found to be less steep in our work (see Section 5.3.1). This is because a large fraction of the high-$\lambda_{\text{Edd}}$ sources ($\lambda_{\text{Edd}} > 0.1$) have a relatively lowered $k_{2-10}$ values compared to Vasudevan et al. (2009), while the $k_{2-10}$ values are similar for the objects with low- and intermediate-$\lambda_{\text{Edd}}$ (see Fig. 11). Since the spectral modelling in the X-ray band is not affected by that in the optical/UV band, the decrease in $L_{\text{bol}}$ by using the p-free disc model leads to a decrease in $L_{\text{bol}}$, and hence $k_{2-10}$ and $\lambda_{\text{Edd}}$ which are both proportional to $L_{\text{bol}}$. This effect, although present in nearly all AGN of our sample, affects mostly the high-$\lambda_{\text{Edd}}$ sources since they have much flatter radial temperature profiles (smaller $p$ values) than the low- and intermediate-$\lambda_{\text{Edd}}$ objects (see Fig. 16). Compared to the results obtained based on the SSD model, this results in a lower $k_{2-10}$ for the same $\lambda_{\text{Edd}}$ at the higher $\lambda_{\text{Edd}}$ end and thus flatten the $k_{2-10}, \lambda_{\text{Edd}}$ relation.

The optical correction factor $k_{5100}$ is found to be independent of $\lambda_{\text{Edd}}$ in our work, which differs from previous studies (e.g. Vasudevan & Fabian 2007; Jin et al. 2012). The correlations reported in those studies were mainly due to an increase of $k_{5100}$ at the higher $\lambda_{\text{Edd}}$ end (there is little or no correlation among low- and intermediate-$\lambda_{\text{Edd}}$ objects). In our case, however, this trend is weakened since the high-$\lambda_{\text{Edd}}$ objects have significantly lowered $k_{5100}$ (while the values of $k_{5100}$ in low- and intermediate-$\lambda_{\text{Edd}}$ objects are similar). Unlike $k_{2-10}$, the effect on $k_{5100}$ by using different disc models is more complex since both $L_{\text{bol}}$ and $L_{\text{bol}}$ are inherent to the model and changed (see Fig. 18). To understand the difference in the high-$\lambda_{\text{Edd}}$ regime between the two models, we calculate the theoretical $k_{5100}$ values for the same range of black hole mass $M_{\text{BH}} (10^{7}–10^{8} M_\odot)$ and Eddington ratio $\lambda_{\text{Edd}} (0.1–1.0)$ in the framework of the SSD model (the fraction of corona emission in the total luminosity is assumed to be 5 per cent, as estimated from the hard X-ray bolometric correction for high-$\lambda_{\text{Edd}}$ sources in Vasudevan & Fabian 2009). The theoretical values of $k_{5100}$ lie between 30–80, which are much larger than the values derived based on the p-free disc model in our work (9–20). This is caused by the enormous difference in the radiative energy in the EUV band from the inner disc region ($L \propto R_{\text{in}} R_{\text{in}}^{2}$), where the two models have very different temperatures. We note that the median value of $k_{5100} \approx 12$ obtained in our work is generally consistent with those given in some of the previous studies (e.g. Richards et al. 2006).

7 SUMMARY

We present a study on the broad-band SED for a well-selected sample of Seyfert 1 galaxies, by taking advantage of their simultaneous optical, UV, and X-ray observations with the Neil Gehrels Swift Observatory. Their SDSS spectrometric data are also used to derive the optical spectral parameters in order to determine their BH masses and Balmer decrements. The sample is selected in a way that there is little or no intrinsic dust reddening as indicated by the Balmer decrement of the broad emission lines. The starlight contamination of the host galaxies is eliminated to a large extent by performing 2D nuclear-galaxy image decomposition.

The main feature of this work that differs from previous studies is that we employ, for the first time, an accretion disc model with a generalized radial temperature profile (rather than the standard SSD profile with the emergent spectra modified by dust reddening) to fit the observed optical/UV spectra of AGN. That is, the power-law index of the radial temperature distribution is treated as a free parameter ($T(\text{rad}) \propto R^{-p}$, i.e. the p-free disc model), which is a special case when $p = 0.75$ as commonly adopted in previous studies. The underlying physics of such a model concerns possible breakdown in reality of the assumptions on which the SSD model is based, e.g. the mass conservation of the inward accretion flow or the effective radiative cooling of the disc.

It is found that the majority of our sample AGN show a shallower optical/UV spectral slope ($F_{\nu} \propto \nu^{\alpha}$, $\alpha = -1.0$ to +0.3 with a median of −0.39) after correcting for host galaxy starlight and dust reddening wherever applicable. This is broadly consistent with previous results and at odds with the prediction by the SSD solution ($\alpha = +1/3$), implying in general flatter radial temperature profiles than the latter. By fitting the p-free disc model to the optical/UV spectra, the radial temperature power-law indices are derived, $p = 0.5–0.75$ (median 0.63), smaller than the SSD value $p = 0.75$ for most of our sample objects. We suggest that the reddened optical/UV spectra as observed in many AGN are at least in part determined by the intrinsically reddened spectral shape of the disc emission.

The broad-band SED of our sample AGN is constructed by integrating the p-free disc model in the optical/UV band and the X-ray radiation model derived from the simultaneous X-ray observations. The averaged SEDs are also presented, whose shapes are found to be dependent strongly on the Eddington ratio. The bolometric luminosities and the bolometric correction factors in the optical $\lambda_{5100}$ and X-ray band $k_{2-10}$ are derived. It is found that, for sources with reddened optical/UV spectra typical of AGN, the SSD plus dust reddening model as commonly adopted in previous work can lead to disc luminosities higher than those derived from the p-free disc model by a factor of several, as well as the bolometric luminosities. The difference is more pronounced in AGN with higher Eddington ratios. Consequently, the values of $k_{2-10}$ and $k_{5100}$ as well as their relations with $\lambda_{\text{Edd}}$ are affected. The hard X-ray bolometric correction factor $k_{2-10}$ is found to be 8–15 for $\lambda_{\text{Edd}} \lesssim 0.03$ and 15–30 for $0.03 \lesssim \lambda_{\text{Edd}} \lesssim 0.09$, which is similar to previous
results, $\kappa_{2-10}$ at high $\lambda_{\text{Edd}}$ values ($\lambda_{\text{Edd}} \gtrsim 0.1$) are relatively lower (20–70) than previous results. The optical bolometric correction factor $\kappa_{1000}$ is found to be independent of the Eddington ratio $\lambda_{\text{Edd}}$, with a median value of $\sim 12$.

The physical origin of the flattened temperature profile in an accretion disc is complicated and far from fully understood. In this work, we suggest that some kind of mass-loss process in form of disc winds/outflows could be a possible scenario for this issue. A thorough test of this hypothesis will be needed in future work.

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