Theoretical Rationalization of the Dual Photophysical Behavior of $\text{C}_{60}^+$

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ABSTRACT. Interest in fullerenes has been renewed recently in astrophysics as a consequence of their detection in circumstellar environments. In particular, $\text{C}_{60}^+$ was detected in the diffuse interstellar medium and its presence has been related to some diffuse interstellar bands (DIBs) whose origin was previously unknown. A single recent laboratory experiment ($J. \text{Phys. Chem. A}$ 2017, 121, 7356–7361) shows that upon laser excitation at 785 nm, $\text{C}_{60}^+$ in neon matrices exhibits a radiative decay at 965 nm, while UV photoexcitation does not lead to any significant luminescence. To rationalize this original dual photophysical behavior, we have performed time-dependent density functional theory (TD-DFT) calculations on $\text{C}_{60}^+$ to investigate the potential energy surfaces of the relevant electronic states, completed by the simulations of vibrationally-resolved absorption and emission spectra. The proposed photophysical pathways shed light on the experimental measurements: The near-IR laser excitation populates the eleventh doublet excited state ($D_{11}$) that decays to the lowest first bright excited state $D_5$, from which photoluminescence is predicted. Indeed, $D_5$ is largely separated from the lower electronic states ($D_0$-$D_4$). Thus, $D_5$ behaves effectively as the first excited state, while the $D_0$-$D_4$ set of states act as the electronic
ground state. In addition, there are no low-lying conical intersections between D$_5$ and lower excited states energetically accessible upon near-IR excitation that can provide efficient nonradiative decay channels for this state, leaving radiative decay as the most likely deactivation pathway. However, a sloped conical intersection between D$_5$ and D$_4$ was located around 2.9 eV above D$_0$. While it is too high in energy to be accessible upon near-IR excitation, it provides a funnel for efficient nonradiative decay down to the ground state (D$_0$) accessible upon UV light excitation. Thus, the photophysics of C$_{60}^+$ is controlled by the ability to access this funnel: Upon near-IR excitation, the system fluoresces because the funnel for nonradiative decay cannot be reached, while UV irradiation provides a different route by opening up a radiationless decay channel via this funnel accounting for the absence of fluorescence.

**INTRODUCTION**

Fullerenes are fascinating carbon allotropes which are used in a large amount of applications in nanotechnology, material sciences, electronics and biomedicine.$^{1,2,3,4,5,6,7,8}$ In addition, these molecules have important implications in astrophysics. Like polycyclic aromatic hydrocarbons (PAHs), these carbonaceous species are believed to be present in the interstellar medium (ISM) and responsible for the observation of diffusive interstellar bands (DIBs).$^{9,10,11,12}$ Not surprisingly then, fullerenes have attracted considerable interest both in astronomy and in astrophysics research fields. One major breakthrough came with the assignment of previously unidentified DIBs$^{13}$ to the C$_{60}^+$ radical cation.$^{14,15,16,17}$ The buckminsterfullerene cation has thus motivated numerous laboratory measurements of its optical absorption spectra.$^{16,18,19,20,21,22,23}$ However, no information about the photophysics of C$_{60}^+$ had been reported until a very recent laboratory experiment investigated the photoluminescence of this cation.$^{24}$ The luminescence measurements show that
$C_{60}^+$ trapped in a neon matrix at 5 K emits in the near-infrared (NIR) region at 964.5 nm upon excitation in the NIR at 785 nm but no detectable luminescence is obtained upon UV excitation at 405 and 375 nm. This study thus suggests to look for the characteristic NIR emission features of $C_{60}^+$ in astronomical environments, where either $C_{60}/C_{60}^+$ has already been detected or fullerenes are likely to be present.

The photophysical behavior observed for $C_{60}^+$ differs substantially from the one of small compact PAH cations (e.g., naphthalene, anthracene and pyrene) for which ultrafast nonradiative decay is observed and explained by the presence of easily accessible low-lying sloped conical intersections. The only known PAH cation displaying a similar emissive behavior is the perylene radical cation for which no low-lying conical intersection is accessible accounting for the observed luminescence in this cation. It is therefore important to provide a consistent mechanistic picture for the photophysics of this type of system. To do this, it is necessary to understand the excited-state mechanisms involved in the photophysical processes such as ground-state regeneration either by nonradiative decay or photon emission. Very useful insights can be obtained from quantum chemical calculations exploring the potential energy surfaces (PESs) of the relevant electronic states involved in these photophysical processes. In particular, the identification of the excited-state minimum corresponding to the luminescent species and the location of PES crossings, i.e., minimum energy conical intersections (MECIs) that provide ultrafast nonradiative decay channels, are paramount to the rationalization of such photophysical behavior. This type of study has already been conducted for small planar radical cations such as benzene, naphthalene, pyrene and perylene, but to our knowledge, it has never been attempted on the buckminsterfullerene radical cation. The aim of this study is to present a photophysical mechanism for $C_{60}^+$ that rationalizes the experimental evidence, i.e. the observed
photoluminescence upon NIR excitation and the absence of radiative decay upon UV excitation of C₆₀⁺, based on the exploration of relevant potential energy surfaces with reliable quantum chemical calculations. After a short presentation of the computational strategy, we first discuss the absorption spectra computed with two different approaches. Then, we identify the species believed to be responsible for the observed NIR emission and compare the simulated vibrationally-resolved emission spectrum with the experimental one. Finally, we propose a simple explanation for the absence of photoluminescence upon UV excitation and summarize the mechanism for the photophysics of C₆₀⁺ in conclusion.

**COMPUTATIONAL DETAILS**

The ground state (D₀) calculations were performed using density functional theory (DFT) in an unrestricted self-consistent field formalism, while time-dependent-DFT (TD-DFT) was used to compute the electronic excited states. The UHF wavefunction stability was checked for D₀. TD-DFT has become a very efficient tool to investigate excited-state processes and to model optical spectra of large systems, otherwise not feasible with accurate wave function-based ab initio methods. Errors for vertical transition energies of valence states are typically in the order of 0.25 eV with hybrid functionals. The standard B3LYP functional was used throughout this study. This functional provides reliable structures and accurate transition energies for the perylene cation, with C–C bond lengths and transition energies not exceeding 0.016 Å and 0.2 eV deviations, respectively, of the restricted active space self-consistent field (RASSCF) results. It has also been largely used to study the optical properties of PAH cations. In addition, the D₀ PES topology of C₆₀⁺ was also investigated with B3LYP. The 6-31G* orbital basis set was chosen as it
includes polarization \(d\)-functions on the carbon atoms and it has been shown to be flexible enough to give a good qualitative description of the covalent excited states of organic molecules.

The ground-state \((D_0)\) geometry optimization was performed using the appropriate \(D_{5d}\) symmetry,\(^{40,43}\) while the excited-state \((D_5)\) geometry optimization was carried out starting from a slightly distorted \(D_0\) minimum structure without any symmetry restrictions first. When symmetry was recognized, subsequent geometry optimizations were performed with the appropriate symmetry constraints. Numerical frequency calculations were then evaluated within the harmonic approximation to determine the nature of the stationary points found on the respective PESs (i.e., minima vs. saddle points). PES crossings between relevant excited states were optimized without symmetry restrictions at the TD-DFT level using a penalty-constrained algorithm. Here again, the geometry optimization was refined using symmetry constraints upon detection of symmetry point groups.

Vertical transition energies have been computed at the \(D_0\) optimized structure considering up to 80 states. Vibrationally-resolved absorption and emission spectra were simulated in the framework of the Franck-Condon\(^{44}\) (FC) and nuclear ensemble\(^{45}\) (NE) approaches. The two methods differ in the way vibrational contributions are taken into account. Within the FC principle, the optimized geometries and normal mode analysis are required for both the initial (i.e., ground-state minimum for absorption and excited-state minimum for emission) and final (i.e., excited-state minimum for absorption and ground-state minimum for emission) states. As mentioned above, these data are obtained from DFT and TD-DFT calculations. The electronic transition dipole moment between the initial and final states is considered to be a constant and the vibronic spectrum results mainly from the calculation of overlap integrals (known as FC integrals) between the vibrational harmonic wave functions of the electronic states involved in the transition. For the NE simulation, these
overlap integrals are not explicitly computed. Only the optimized geometry and normal mode analysis of the initial state is needed as input. A number of nonequilibrium geometries are produced and, for each structure, a single point TD-DFT calculation is performed, providing transition energies and electronic transition dipole moments. The spectrum is then integrated over these distinct vertical absorptions. In this way, the spectral band shape results mainly from the initial-state nuclear geometry distribution. For both methods, a phenomenological Gaussian broadening was used to account for the convolution of the spectral lines. This factor was chosen to visually reproduce the experimental band shapes. In the NE simulations, an ensemble of 240 geometries were prepared and the first fifteen excited states were considered for simulating the absorption spectrum in the spectral range of interest ($\lambda > 785$ nm, the excitation wavelength). This spectrum was simulated varying the number of nonequilibrium geometries to test the convergence of the results (Figure S1 in Supp. Info.). For the FC absorption spectrum, only the D$_5$ state was considered, as no minimum on the D$_6$ PES could be located. For the NE emission spectrum, only the D$_5$ state was considered to contribute to the emission at very low temperature and the spectrum was generated using the same number of sampling geometries. All spectra were simulated at 0 K.

DFT and TD-DFT calculations, including geometry optimizations of stationary points and harmonic frequency analyses, were performed with Gaussian09. This program was also used for the FC simulations. Q-Chem 5.0 was used to perform the MECI optimizations. The NE simulations were carried out using the software Newton-X.

**RESULTS AND DISCUSSION**

**Ground-State Structure and Absorption Spectrum.** It is well known that the neutral buckminsterfullerene C$_{60}$ has a ground-state structure belonging to the icosahedral symmetry.
After removal of an electron from the fivefold degenerate highest occupied molecular orbital (HOMO) of the $h_u$ irreducible representation, the resulting radical cation is stabilized due to Jahn-Teller effects leading to a species with reduced $D_{5d}$ symmetry.\textsuperscript{40,43} Our $D_0$ geometry optimization along with the harmonic frequency analysis confirm that the ground-state structure corresponds to a minimum of $D_{5d}$ symmetry with a $^2A_{1u}$ electronic configuration. The singly occupied molecular orbital (SOMO) is the delocalized $\pi$-MO $6a_{1u}$ shown in Figure 1.

**Figure 1.** Relevant molecular orbitals for $C_{60}^+$ at its minimum $D_0$ structure of $D_{5d}$ symmetry.

The lowest thirteen doublet excited states are mainly obtained by $\pi-\pi$ electronic transitions from the thirteen lowest lying $\pi$-MOs to the $6a_{1u}$ SOMO (see Table 1). The higher excited states above $D_{13}$ are due to $\pi-\pi^*$ transitions. Vertical transition energies for the lowest thirteen doublet excited states are provided in Table 1. It shows that the excited states $D_1$ to $D_4$ are close in energy to $D_0$. This is not surprising as the $D_0$-$D_4$ set of states all arise from the fivefold degenerate $^1H_u$ state of the neutral $C_{60}$. The first bright state is $D_5$ and is degenerate with $D_6$. The excitation energy between $D_0$ and $D_5/D_6$ is 1.39 eV (892 nm). The second state with a non-zero oscillator strength ($f$) is also a degenerate state ($D_{11}/D_{12}$) with an excitation energy of 1.55 eV (801 nm), but this state is 16
times less intense than the D5/D6 pair of states. Since no other bright state has an energy close to the experimental laser excitation at 785 nm, we expect that this NIR laser excitation is actually populating D11/D12 pair of states.

**Table 1.** Lowest thirteen vertical transition energies computed at TD-DFT/6-31G* level at the minimum D0 structure of D5d symmetry.

<table>
<thead>
<tr>
<th>Transitions</th>
<th>States</th>
<th>ΔE (eV)</th>
<th>λ (nm)</th>
<th>f</th>
</tr>
</thead>
<tbody>
<tr>
<td>36e1u→6a1u</td>
<td>D1</td>
<td>0.206</td>
<td>6032</td>
<td>0.000</td>
</tr>
<tr>
<td>35e1u→6a1u</td>
<td>D2</td>
<td>0.206</td>
<td>6032</td>
<td>0.000</td>
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<tr>
<td>36e2u→6a1u</td>
<td>D3</td>
<td>0.208</td>
<td>5974</td>
<td>0.000</td>
</tr>
<tr>
<td>35e2u→6a1u</td>
<td>D4</td>
<td>0.208</td>
<td>5974</td>
<td>0.000</td>
</tr>
<tr>
<td>36e1g→6a1u</td>
<td>D5</td>
<td>1.391</td>
<td>892</td>
<td>0.032</td>
</tr>
<tr>
<td>35e1g→6a1u</td>
<td>D6</td>
<td>1.391</td>
<td>892</td>
<td>0.032</td>
</tr>
<tr>
<td>36e2g→6a1u</td>
<td>D7</td>
<td>1.514</td>
<td>819</td>
<td>0.000</td>
</tr>
<tr>
<td>35e2g→6a1u</td>
<td>D8</td>
<td>1.514</td>
<td>819</td>
<td>0.000</td>
</tr>
<tr>
<td>34e2g→6a1u</td>
<td>D9</td>
<td>1.537</td>
<td>807</td>
<td>0.000</td>
</tr>
<tr>
<td>33e2g→6a1u</td>
<td>D10</td>
<td>1.537</td>
<td>807</td>
<td>0.000</td>
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<tr>
<td>34e1g→6a1u</td>
<td>D11</td>
<td>1.548</td>
<td>801</td>
<td>0.002</td>
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<tr>
<td>33e1g→6a1u</td>
<td>D12</td>
<td>1.548</td>
<td>801</td>
<td>0.002</td>
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<tr>
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<td>D13</td>
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<td>789</td>
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</table>

Figure 2 provides the simulated absorption spectrum using the NE approach based on the lowest fifteen excited states and a comparison between the FC and NE formalisms for the high-resolution spectrum in the NIR spectral range is presented in the inset. The absorption spectrum shows two
intense bands in the 900-1000 nm range attributed to the \(D_0 \rightarrow D_5\) and \(D_0 \rightarrow D_6\) transitions. The experimental excitation energy at 785 nm coincides with the \(D_0 \rightarrow D_{11}\) and \(D_0 \rightarrow D_{12}\) transitions. Comparing the simulated high-resolution NIR absorption spectra with the recorded experimental absorption spectrum of \(C_{60}^+\) in the gas phase,\textsuperscript{15} the two observed absorption bands at 963.2 nm and 957.7 nm are well reproduced by our simulations with peaks at 959 nm and 951 nm for the NE spectrum and peaks at 958 nm and 950 nm for the FC spectrum. This is also in good agreement with the absorption spectrum of \(C_{60}^+\) trapped in a neon matrix at 5 K.\textsuperscript{24} Note that the relative intensity of these two peaks is in better agreement with the NE simulated spectrum (compare with Figure 3b in Ref. [24]). This is probably due to the fact that in the FC simulated spectrum the absorption only results from the \(D_0 \rightarrow D_5\) transition (with a total spectral progression of the simulated spectrum reaching \(\sim 94\%\)), while the NE spectrum also includes contributions from \(D_0 \rightarrow D_6\). We expect therefore a more accurate description of the absorption spectrum with the NE approach, as both \(D_5\) and \(D_6\) strongly contribute to the absorption of \(C_{60}^+\) in the NIR range. This could also possibly explain the better agreement with the next absorption peaks observed between 910-930 nm in Ref. [24].
Figure 2. Convoluted absorption spectrum of C_{60}^{+} and spectrum decomposition simulated using the first fifteen excited states within the NE approach (see Figure S2 in Supp. Info. for the error due to the statistical sampling). The inset shows the high-resolution absorption spectrum in the NIR region with the FC (green line) and NE (red line) approaches.

Near-IR Photoluminescence. Because the experimental NIR laser excitation at 785 nm used is in good agreement with the D_{0}→D_{11}/D_{12} transition energy (see Table 1 and Figure 2), we assume that the initial photoexcited states are D_{11}/D_{12}. As shown in Table 1, the energy gaps with lower electronic states down to D_{5} are pretty small with all the states from D_{5} to D_{12} found within 0.16 eV. Then, a large energy gap is found with the next lower excited state D_{4}, with a D_{5}–D_{4} energy gap of 1.18 eV. Thus, D_{5} can be considered effectively as “D_{1}”, while the D_{0}–D_{4} set of states play the effective role of “D_{0}”. As a consequence, we expect efficient nonradiative decay to take place from the initially excited D_{11}/D_{12} states down to D_{5}, from which luminescence is expected to take place, provided no easily accessible conical intersections are available for efficient nonradiative decay from D_{5}. To verify this scenario, we have optimized the D_{5} structure and searched for D_{5}/D_{4}
MECIs. At the end of the D₅ geometry optimization, the excited radical cation has no longer D₅d symmetry because an electron has been removed from a degenerate e₁g MO and, as a consequence of a Jahn-Teller instability, the symmetry is reduced to C₁. This Jahn-Teller effect is rather weak with a relaxation energy in the D₅ state between the D₅d and C₁ structures of 0.063 eV and C–C bond lengths modifications not exceeding 0.02 Å. At this D₅ minimum geometry, the vertical emission energy is computed at 1.242 eV, corresponding to an emission wavelength of 999 nm, in good agreement with the experimental value of 964.5 nm²⁴ (963.2 nm in the gas phase¹⁵). An excellent agreement is obtained when considering the 0–0 transition energy, which is computed at 1.294 eV (958 nm). Note that this agreement is beyond expectation, as typical errors for TD-DFT transition energies are typically within 0.3 eV for covalent singly-excited transitions. In addition, a D₅/D₄ MECI was located at an energy above that provided by NIR excitation (see next subsection), making this funnel for nonradiative decay not accessible.

Figure 3 shows the vibrationally-resolved emission spectra computed both with FC and NE approaches. The FC simulated emission spectrum displays the most intense band exactly at the 0–0 transition, in agreement with the experimental observations.¹⁵,²⁴ A second less intense emission band is observed shifted by 265 cm⁻¹ to lower energy with respect to the 0–0 transition, in very good agreement with the experimental spectrum,²⁴ which shows a secondary band at 262 cm⁻¹ at lower energies. This band was assigned experimentally to the first vibrationally excited level of the electronic ground state, corresponding to a radial a₁g vibrational mode of C₆₀⁺. Our FC simulation confirms this assignment from the analysis of the vibrational progression. This a₁g vibrational mode at 267 cm⁻¹ corresponds to a breathing motion of C₆₀⁺ with a contraction along one direction of the ball and an expansion along two orthogonal directions (see animated movie in Supp. Info.). The NE spectrum is slightly red-shifted (by 423 cm⁻¹) compared to the FC spectrum.
However, the spectrum envelop reproduces very nicely the experimental one, with two shoulders occurring at higher energies than the 0–0 maximum.

**Figure 3.** Simulated emission spectra of $C_{60}^+$ within the FC (black line) and NE (red line) approaches. The vertical dashed line marks the computed 0–0 transition. The dashed blue line is the experimental spectrum digitalized from Ref. [24].

**UV Photostability.** Unlike the NIR photophysical pathway which leads to radiative decay, UV excitation at 405 and 375 nm does not lead to any detectable fluorescence. Although we have computed up to 80 vertical transition energies, the excited states with an excitation wavelength lower than 500 nm suffer from a large spin contamination and are thus unreliable. Based on our TD-DFT calculations, it is therefore not possible to identify the electronic states that are initially populated by these UV excitations. However, due to the high density of electronic states in that region of the spectrum, it can be assumed that efficient nonradiative decay will take place down to the $D_5$ state, in a similar way that we have assumed efficient decay from $D_{11}$ to $D_5$ in NIR
photophysical pathway. Of course, upon UV excitation, the D₅ state produced will have a lot more vibrational kinetic energy available.

To account for the lack of luminescence from D₅ upon UV excitation, we have searched for MECIs between D₅ and D₄. If such a crossing exists and is energetically accessible, then it would provide a nonradiative decay path that would be responsible for luminescence quenching. As explained in the previous subsection, we found a D₅/D₄ MECI. It that has a C₁ symmetry structure like the D₅ minimum structure. It is located 2.869 eV above the ground state D₅d minimum and 1.541 eV above the D₅ excited-state C₁ minimum. The high activation energy necessary to reach this MECI from the D₅ minimum is the result of substantial structural deformations involving changes in the C–C bond lengths up to 0.08 Å. Because the UV excitation at 405 nm and 375 nm provides 3.061 eV and 3.306 eV above D₀, respectively, whereas the NIR excitation at 785 nm only provides 1.579 eV, this D₅/D₄ MECI is unreachable upon NIR excitation but becomes energetically accessible upon UV excitation. Thus, our results suggest that the hot D₅ state produced upon UV irradiation has enough vibrational kinetic energy available to access this funnel for nonradiative decay down to D₄. The topology of this MECI is sloped⁵⁰,⁵¹ (Figure S3 in Supp. Info.) and will favor the photostabilization⁵²,⁵⁳ of C₆₀⁺. Following UV excitation and radiationless decay to D₄, the system can easily relax down to D₀, as the D₀-D₄ manifold of states are coupled via the symmetry-enforced (Jahn-Teller) icosahedral conical intersection.

**CONCLUSION**

The present theoretical investigation described two distinct photophysical pathways corresponding to NIR and UV irradiation of C₆₀⁺, respectively. These pathways are schematically summarized in Figure 4. In the first case, C₆₀⁺ is fluorescent in the NIR range. Upon excitation to
the D_{11} excited state, the system can decay nonradiatively to the lower D_5 excited state, which has been identified as the electronic state responsible for the observed emission. The predicted fluorescence maximum (at 0 K) is attributed to the 0–0 transition between the D_5 and D_0 states and computed at 958 nm, in excellent agreement with the experimental 0–0 transition values of 964.5 nm in a Ne matrix at 5 K and 963.2 nm in the gas phase at 5.8 K. The vibrationally-resolved emission spectra reproduce beautifully the band structures of the experimental fluorescence spectrum, in particular the second most intense band shifted by 265 cm\(^{-1}\) to lower energies, which is assigned to the first vibrational excited state of a radial \(a_{1g}\) normal mode of \(\text{C}_{60}^+\). In the case of UV irradiation, \(\text{C}_{60}^+\) is excited to higher excited states that are assumed to decay rapidly to the lower D_5 state. The excess of vibrational kinetic energy available is then sufficient to access a sloped D_5/D_4 MECI responsible for the internal conversion to D_4. This state can then decay down to D_0 via interstate couplings in the region of the symmetry-induced conical intersection found in the icosahedral symmetry.

To summarize, the photophysics of \(\text{C}_{60}^+\) is controlled by the accessibility of a sloped conical intersection. Upon NIR excitation this crossing is not accessible and the system decays radiatively, whereas upon UV excitation this funnel allows for efficient nonradiative decay back to the ground electronic state of \(\text{C}_{60}^+\). This simple mechanistic picture provides a rationale behind the experimental observations. These findings may be interesting to astrophysicists who are looking for the origin of some diffuse interstellar bands and of unidentified IR emission bands observed in the interstellar medium.
**Figure 4.** Schematic representation of the NIR radiative (in red) and of the UV nonradiative (in green) photophysical pathways.

ASSOCIATED CONTENT

**Supporting Information.** The following files are available free of charge. Tables S1-S3 for the Cartesian coordinates of all the optimized structures. Figure S1 for the effect of the number of sampling geometries on the simulated NE absorption spectrum. Figure S2 for the error due to the statistical sampling for the simulated NE absorption spectrum reported in Figure 2. Figure S3 for the D₄ and D₅ gradients at the D₅/D₄ MECI. (PDF file) A movie file showing the radial $a_{1g}$ vibrational mode of C₆₀⁺. (GIF file)

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Notes

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