Synchrotron tomographic quantification of the influence of Zn concentration on dendritic growth in Mg-Zn alloys

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Abstract

Dendritic microstructural evolution during the solidification of Mg-Zn alloys was investigated as a function of Zn concentration using *in situ* synchrotron X-ray tomography. We reveal that increasing Zn content from 25 wt.% to 50 wt.% causes a Dendrite Orientation Transition (DOT) from a six-fold snow-flake structure to a hyper-branched morphology and then back to a six-fold structure. This transition was attributed to changes in the anisotropy of the solid-liquid interfacial energy caused by the increase in Zn concentration. Further, doublon, triplon and quadruplon tip splitting mechanisms were shown to be active in the Mg-38wt.%Zn alloy, creating a hyper-branched structure. Using the synchrotron tomography datasets, we quantify, for the first time, the evolution of grain structures during the solidification of these alloys, including dendrite tip velocity *in the mushy zone*, solid fraction, and specific surface area. The results are also compared to existing models. The results demonstrate the complexity in dendritic pattern formation in hcp systems, providing critical input data for the microstructural models used for integrated computational materials engineering of Mg alloys.

**Keywords:** magnesium alloys; zinc; 4D imaging; dendrite orientation transition; morphology transition.
As the lightest structural metal widely used for automotive and aerospace applications, Mg alloys have tremendous opportunity for lightweighting vehicles and improving fuel efficiency[1][2][3]. Due to their excellent fluidity[2], most components made from Mg are generally cast into a near-net-shape mould. At the scale of the microstructure, the casting process refers to the formation of dendrites, eutectic, and precipitate constituents as the metal evolve from the liquid to the solid state[4][5][6]. The morphology and size distribution of these features significantly affects other phenomena – micro-segregation, intermetallic precipitation, semisolid rheology, and grain texture – and thus determines the in-service mechanical properties[7].

The formation of dendrites during solidification is largely controlled by the underlying crystalline structure, diffusion (both heat and solute), and anisotropy in the solid/liquid interfacial energy[4][8]. In metallic systems, a variety of dendritic morphologies and growth patterns have been observed, from the expected cubic/hexagonal morphology to feathery and seaweed grains, hyperbranched structures, and dendrite orientation transitions. These observations were made post-mortem, historically in 2D (via metallography, scanning electron microscopy[9][10][11]) and more recently in 3D (via serial sectioning and X-ray tomography[12][13][14]), on samples quenched from the semi-solid regime to “freeze-in” the microstructure. In a comprehensive study on Mg alloys, Yang et al.[15] performed post-mortem X-ray tomography to examine the effect of solute content on dendrite morphology and orientation selection using Sn, Ba, Al, Y, Gd, and Zn.
elements. In particular, for Mg-Zn, a dendrite orientation transition was observed in which seaweed-like $\alpha$-Mg structures grew for Zn content between 20-45 wt.%, while 18-branch (<20 wt.%Zn) and 12-branch (>45 wt.%Zn) morphologies were observed outside this range. In a similar post-mortem X-ray tomography study, Shuai et al.[11] also observed a dendrite orientation transition, however the seaweed structure was not seen until 38 wt.%Zn. These studies showed the possibility to control the dendritic formation patterns of Mg alloys through alloy additions.

Recently, due to advances in high-speed synchrotron X-ray radiography and tomography, in situ studies of microstructure evolution during the processing of metallic materials have been reported[16][17][18][19][20][21][22][23]. Real-time radiographic experiments at ultrafast frame rates have been largely carried out on Al-based alloys (Al-Cu[24][25][26], Al-Ni[27], Al-Si[28][29]) with thin plate-like (100-200 $\mu$m) samples, in order to study solidification phenomena including dendrite coarsening, columnar-to-equiaxed transition, crystal fragmentation [26], and crystallographic misorientation [30]. In situ tomographic experiments, known as 4D imaging, have also been performed on similar cubic alloy systems (but at a much slower frame rate) to elucidate the corresponding 3D evolution in solidification microstructure[9][31][32][33][34]. For the case of Mg, with hcp crystallography and high affinity for oxygen, direct 2D and 3D observations of dendritic morphology evolution during solidification are limited[19][35][36]. Using radiography, Wang et al.[19] investigated the effect of cooling rate on dendritic growth dynamics of Mg-Gd alloy in a fixed thermal gradient. Using tomography, Shuai et al.[35] quantified the
effect of the cooling rate on 3D dendritic morphology evolution in a Mg-Sn alloy while Guo et al. [37] examined the influence of cooling rate and solute concentration on the coarsening kinetics of Mg-Zn alloys.

Collectively, these studies have greatly advanced our understanding of solidification microstructure evolution in complex hcp structures. In addition, they demonstrate the need for further research to reveal the dynamics of microstructural evolution and the underlying mechanisms by which solute elements alter the dendritic structures of hcp Mg alloys.

In the present study, the effect of Zn content on $\alpha$-Mg dendritic growth patterns was investigated using 4D synchrotron X-ray tomography, X-ray diffraction (XRD) and electron back-scattered diffraction (EBSD). This research goes beyond the post-mortem tomography studies of Yang et al. [15] and Shuai et al. [11] to quantify in situ the evolution in solid fraction ($f_s$), dendrite tip velocity in the mushy zone ($V_{tip}$), and specific surface area ($S_v$) in alloys having 25 to 50 wt.%Zn, and qualitatively capture the influence of Zn on dendrite growth kinetics in hcp Mg alloys. By providing the first quantitative kinetic data, the results both inform and validate numerical solidification models of hcp metals.

2 Materials and experimental methods

Three hypoeutectic Mg-Zn alloys with 25, 38 and 50% weight percent of Zn were selected for this study, to determine zinc’s influence on the dendritic structure. The solidification ranges of the three alloys are $\sim 209^\circ$C (550-341$^\circ$C), $\sim 134^\circ$C (475-341$^\circ$C)
and ~59°C (400–341°C), respectively. The methodology for sample preparation and
encapsulation enabling 4D imaging of Mg alloy solidification is the same as that in
ref.[35]. Note that these are nominal alloy compositions, as evaporative loss may have
resulted in a reduction in the Zn content.

The X-ray tomography experiment was carried out at the Diamond-Manchester
Beamline (I13), Diamond Light Source (DLS, UK). Each sample was heated to 30°C
above the liquidus temperature, held for 30 min to ensure complete melting, and then
cooled at a rate of 3°C/min. During cooling, tomographic images were acquired
continuously until solidification was complete. The acquisition time was 14 s per
tomogram at a voxel size of 1.6 μm followed by a 22 s delay for system
re-initialization, giving a cycle time of 36 s. Subsequently, each set of 3D datasets was
processed using the Avizo software (ThermoFisher FEI) to visualize the process of
solidification in Mg-Zn alloys and segment the solid and liquid phases. The
experimental set-up, beam parameters and image processing procedures are the same
as those utilized previously[35]. Please note that it was assumed that the melt
temperature reached the liquidus temperature in the tomogram prior to the one where
the dendrites were first observed irrespective of the thermocouple readout value.

Further, based on the cycle time and cooling rate, the temperature difference between
each subsequent tomogram was 1.8°C and thus this value was also assumed to be the
uncertainty in temperature.

The XRD and EBSD specimens were prepared by heating cylindrical Mg-Zn
alloys to ~30°C above the melting point, cooled down at the same rate as the X-ray
tomography experiments to 30 °C below the liquidus, and then quenched into liquid metal coolant (Ga-In-Sn). The XRD was conducted on a Bruker AXS-D8 Advance system (10° to 90°, 3°/min). For EBSD, metallography was then performed on a Struers automated grinding and polish machine following the standard procedure. After final polish with OP-S (0.04µm), the specimens were etched for 2-3s with a solution of 5ml nitric acid, 15ml acetic acid, 20ml distilled water and 60ml ethanol. The EBSD was conducted using a Zeiss Crossbeam 540 equipped with NordlysMax2 detector and HKL Channel 5 data analysis system.

3 Results and discussion

3.1 Qualitative analysis

3.1.1 Dendritic morphology evolution during solidification

Fig. 1 and supplementary videos V1, V2 and V3 show the dendritic morphology evolution of three different Mg-Zn alloys at different temperatures within the mushy zone as 2D cross-sectional slices extracted from the middle of each tomogram. As can be seen, distinctive dendritic morphologies were observed at each of the different Zn contents. Specifically, a coarse and globular-like dendritic structure was obtained at Mg-25wt.%Zn, a hyper-branched structure was obtained at Mg-38wt.%Zn, and a dendritic structure with branched arms around the trunk was obtained at Mg-50wt.%Zn.

For all the alloys, it appears that the majority of the grains nucleated on the sample wall and grew towards the sample center. This is potentially due to the MgO
skin on the surface acting as heterogeneous nucleation sites for the $\alpha$-Mg grains[38][39]. With increased solid fraction, an increase in the image contrast was observed. This was a result of Zn being rejected from the growing dendrites to the liquid phase. Finally, for the images b4 (Mg-38wt.%Zn) and c4 (Mg-50wt.%Zn), increased attenuation in the interdendritic region was observed, suggesting that this region has solidified forming eutectic (i.e. the eutectic temperature was reached), showing as darker in the image due to the solid’s increased density and additional scattering of x-rays[25]. This final feature is best seen in supplementary videos V1, V2 and V3. Note that the final $\Delta T$ in Fig. 1 (a4, b4, c4) does not correspond perfectly to the solidification range for the three alloys from the phase diagram, but instead is $\sim 15$ °C less. This may be due to either evaporative loss of Zn changing the composition during multiple melting/solidification experiments, and/or a change in the furnace temperature distribution resulting from latent heat evolution. This inaccuracy in the solidification range does not affect the dendritic growth observations, but may shift the Zn concentration at which they occur.
Fig. 1: 2D image sequence showing dendritic morphology evolution as a function of solid fraction and temperature in Mg-25wt.%Zn (a1-a4), Mg-38wt.%Zn (b1-b4) and Mg-50wt.%Zn (c1-c4) alloys ($\Delta T$ indicates the temperature below $T_{\text{liquidus}}$). All the figures share the same scale bar; the dark grey areas on the margin represent the gap between the sample and graphite tube.
Fig. 2: 3D dendritic morphology evolution for Mg-25wt.%Zn (a1-a4), Mg-38wt.%Zn (b1-b4) and Mg-50wt.%Zn (c1-c4) alloys (ΔT indicates temperature below $T_{\text{liquidus}}$; all the figures share the same scale bar).

To examine the 3D growth of dendrites during solidification, isolated representative dendrites were extracted from each acquired tomogram. Fig. 2 and supplementary videos V4, V5 and V6 show the morphological evolution of the three Mg-Zn alloys tested. From the earliest growth stage onwards, the microstructures of all three alloys are seen to be dendritic from a 3D perspective[35]. For the case of Mg-25wt.%Zn, Fig. 2 (a1-a4), it would appear that dendritic growth and coarsening occurred concurrently. For the cases of Mg-38wt.%Zn and Mg-50wt.%Zn, dendritic growth is evident but coarsening is more difficult to clearly observe. As coarsening is a time-dependent process, the decreasing solidification interval occurring with
increasing Zn content results in shorter time for the structure to coarsen and thus its effects are difficult to quantify. It can also be seen from Fig. 2 that, with an increasing Zn content, the morphology of primary \( \alpha \)-Mg grains became more complex with a higher number of dendritic branches, and an increase in the number of secondary dendrite arms. In other words, as the Zn concentration increases, dendrites in Mg-Zn alloys appear to produce finer branches that split more frequently. This is best seen by comparing Figs. 2 a1, b1, and c1.

Fig. 3 plots the local mean curvature distribution for each of the three dendrites shown in Fig. 2 at a time when the average solid fraction in the tomogram was 0.15. Mean curvature, \( H \), is defined as \( (1/R_1 + 1/R_2)/2 \), where \( 1/R_1 \) and \( 1/R_2 \) are the two principal curvatures at any point on the dendrite. Along with the distribution, images of the three dendrites are shown. In these images, a red colour indicates large positive values of \( H \), and thus local regions with large positive mean curvature / dendrite arms having the finest tip radii, while a green colour indicates neutral values of \( H \). As can be seen, with increasing Zn concentration, the dendritic surface area having a large mean curvature also increases. This experimental result agrees well with the experimental finding in succinonitriile-acetone alloys where an increase in dendrite tip curvature was observed with an increase in acetone concentration [40].
Fig. 3: Mean curvature ($H$) distribution of separated dendrites in Mg-25/38/50wt.%Zn alloys at a solid fraction of 0.15. The scale bar has a length of 300 µm.

3.1.2 Dendritic morphology transition with increasing Zn concentration

Dendrites in Mg alloys generally evolve as a six-fold hcp symmetric snowflake-like structure[10][41][42][43]. However, due to the weak anisotropy between symmetric growth directions, the preferential growth orientations of $\alpha$-Mg dendrite are influenced by many factors. These include alloying elements and solute concentrations, as well as imposed thermal conditions, resulting in a diversity of $\alpha$-Mg dendrite morphologies possessing both six-fold symmetrical structures and those with abnormal structures formed during solidification[10][11][44][45][46].

As shown in Fig. 2, the dendritic morphologies in the studied alloys were found to transform from a six-fold snowflake-like structure in Mg-25wt.%Zn to a hyper-branched structure in Mg-38wt.%Zn and then subsequently back to a six-fold symmetry morphology in Mg-50wt.%Zn alloy. In Mg-25wt.%Zn a typical six-fold structure was present from the view of the basal plane. However, the dendritic arms were found to split on the basal plane and tended to grow along the direction of the
prismatic plane. In contrast, while a six-fold structure was also observed in Mg-50wt.%Zn from the perspective of basal plane, only 4 branches were present on the prismatic plane, and the branch arms on the basal plane disappeared and grew along a direction between the basal plane and prismatic plane[11].

In order to further confirm the dendrite orientation transition, XRD and EBSD measurements were performed on the quenched samples. From the XRD patterns shown in Fig. 4, three different phase constituents, α-Mg (P63/mmc, a=b=3.209Å, sc=5.211Å, c/a=1.624, α=β=90°, γ=120°), Mg7Zn3 (I, a=b=c=14.170Å, α=β=γ=90°), Mg2Zn11 (Pm3(200), a=b=c=8.552Å, α=β=γ=90°) were observed and the <11\̅20> direction of α-Mg on the basal plane can be observed in Mg-25wt.%Zn alloy, while in Mg-50wt.%Zn, it is clear that <11\̅20> disappeared and only <11\̅21> was found. In Mg-38wt.%Zn, some anomalous diffraction peaks were observed. This is further clarified by the EBSD results, shown in Fig. 5. Specifically, the preferred growth direction of α-Mg for Mg-25wt.%Zn was found to be <11\̅20> (Fig. 5 a2) and in Mg-50wt.%Zn alloy, the preferential orientation was observed to be <11\̅21> (Fig. 5 c2). The results for Mg-38wt.%Zn (Fig. 5 b) show that the branching structure and growth orientation of these dendrites were much more complicated than in either the Mg-25wt.%Zn and Mg-50wt.%Zn.
Fig. 4: XRD patterns of Mg-25/38/50wt.%Zn alloys showing the orientation selection in these three alloys.

Fig. 5: EBSD measurement showing the preferential growth direction in: (a-a2) Mg-25wt.%Zn, (b-b3) Mg-38wt.%Zn, and (c-c2) Mg-50wt.%Zn

In general, the preferential growth direction of dendrites is known to be determined by the anisotropy in interfacial free energy and thus the transition in dendrite growth orientation can be attributed to changes in this quantity [4]. There are
a variety of factors that might affect the anisotropy in solid-liquid interfacial free energy during the growth of a dendrite: including (i) lattice defects (lattice distortions and/or stacking faults), (ii) the formation of twin grains, (iii) fast cooling rates, and (iv) an increase in the concentration of a solute element with high anisotropy in solid-liquid interfacial free energy.

Of these, the first can be discounted in Mg-Zn because although lattice distortions and stacking faults are likely induced when Zn forms a solid solution in Mg, all three alloys are above the solid solubility limit. Hence, a similar number of lattice defects would be expected to form.

The second is seen as unlikely because the investigated system is binary while twins are frequently seen in ternary systems. As reported by Kurtuldu et al.[46], a trace addition of Cr (typically 200 to 1000 ppm) in Al-20wt.%Zn alloy was shown to drastically modify the alpha-Al dendrite growth direction from <100> to <110>; this was correlated in [46] to the formation of a surprisingly large number of twinned grains. However, from the EBSD results shown in Fig. 5 and previous EBSD studies in Mg-Zn alloys[11][44][47], no obvious twin grains were observed to initiate this mechanism.

The third can be eliminated since similar hyperbranched/seaweed microstructure was observed in Mg-Zn alloys when cooled under a range of cooling rates (3°C/min (this study), 6°C/min[11] and quick quench[15]).

Thus, based on the results obtained in this study, it is likely that the observed dendrite orientation transition is caused by the increase in solute content as Zn is
known to have a very strong anisotropy in solid/liquid interfacial energy. Because of
the low solubility of Zn in Mg, we hypothesize that the structural changes occur on
the liquid side, perhaps by a concentration-dependent atom cluster that forms adjacent
to the dendrite growth front and changes continually the surface energy.

This hypothesis that Zn content is modifying the anisotropy in solid/liquid
interfacial energy in the Mg-Zn system to cause the change in growth directions is
supported by the molecular dynamics (MD) simulations of Sun et al.[45]. In these
simulations, it was found that the anisotropy between different symmetric directions
in pure magnesium was rather small, therefore, the interface free energy anisotropy of
α-Mg could be easily changed through the addition of a solute with high anisotropy.

Due to present limitations of MD calculations in binary systems[47], the community
cannot yet perform realistic simulations for the interfacial free energy anisotropy in
Mg-Zn alloys. It is hoped that the present study and similar studies will encourage
experts in MD to focus their attention on developing methods to help explain the
phenomenon observed in this work.

The dendrite morphologies presented in this study can be used to validate the
numerical simulations, i.e. phase-field models, that are currently being used for
predicting dendrite growth patterns in engineering metals. However, the phase-field
simulation results will only match experimental results if the anisotropy function is
properly accounted for. To give an example, although the Mg-Zn phase field
simulations of Wang et al. [10] did show hyper- branched dendrite morphology at
intermediate compositions, they used an anisotropy function having the preferred
orientations of <1120> and <2245> based on [48]. These simulation results do not agree very well with the experimental results in this study where the dendrite orientation transitioned from <1120> to <1121>. Thus, in hcp systems, it is clear that a combination of simulations and experiments is needed to accurately quantify anisotropy in interfacial free energy.

3.1.3 3D evolution of hyper-branched structures in Mg-Zn alloy

Through analysis of the 3D datasets, it appears that three tip-splitting mechanisms are responsible for the formation of hyper-branched structures at Mg-38wt.%Zn. These are shown in Fig. 6: doublon (Fig. 6 a1-a4 and d1-d4), triplon (Fig. 6 b1-b4) and quadruplon (Fig. 6 c1-c4), respectively. These hyper-branched structures are similar to ones displayed in succinonitrile–camphor under microgravity condition (Fig. 6 a1, b1, c1) by Bergeon et al.[49]. However, only the final shapes (doublon, triplon or quadruplon) were obtained in that study due to the limited temporal resolution of the experiment; the evolution of seaweed structure and the tip splitting mechanisms were not captured. In the present study, the mechanisms of tip splitting were directly captured. Specifically, (i) for the doublon, the dendrite tip was observed to split in two parts about its central axis with a narrow liquid groove in between (Fig. 6 a2-a4) and it is similar to what was observed in directionally solidified Al-4wt.%Cu[50] and pure Cu[51] metals in previous studies; (ii) for the triplon, the dendrite tip was observed to split into three small tips simultaneously during growth (Fig. 6 b2-b4); (iii) for the quadruplon, the tip dendrite was observed to first split into two tips (doublon) and then each doublon split again into two tips making four tips in total (Fig. 6 c2-c4)
through a “doubling doublons” mechanism rather than quadruplon branches forming simultaneously. It is worth noting that although the doublon structure was present in both Mg-38wt.%Zn and Mg-50wt.%Zn alloy, triplon and quadruplon structures were only observed in the Mg-38wt.%Zn alloy.

Fig. 6: Dendrite tip splitting mechanisms during the solidification of (a1, b1, c1) bulk transparent (succinonitrile–camphor) alloy (after ref.[9]), (a2-a4, b2-b4, c2-c4) Mg-38wt.% alloy and (d1-d4) Mg-50wt.%. $\Delta T$ indicates the temperature below liquidus. Figures (a2-a4, b2-b4, c2-c4, d1-d4) share the same scale bar. Note no scale
Seaweed-like microstructures usually form under various situations like isotropic or weakly anisotropic conditions or with increased undercooling[52][53]. In the current study, the sample was solidified under a relatively low cooling rate, and it is unlikely that the hyper-branched structures resulted from large undercooling. Instead, we hypothesize that the formation of seaweed-like hyper-branched microstructure is a result of the Zn addition and the corresponding modification of the interfacial free energy anisotropy of α-Mg dendrites. This phenomenon correlates well to that observed in Al-(10–90)wt.%Zn alloys where a dendritic orientation transition occurred with an increase in Zn content and a hyper-branched structure formed at interim Zn concentration (e.g. Al-55wt.%Zn)[4]. Abnormal and complex dendritic growth morphologies were also previously observed in a number of transparent systems[51][54] and metallic alloys[4][45][50]; the observations of dendrite growth in Figure 4 help to explain the development of such structures.

3.2 Quantitative analysis

3.2.1 Evolution of dendrite solid fraction with temperature

The overall evolution in volume fraction of primary α-Mg dendrites with temperature was calculated from the 3D datasets, and is shown in Fig. 7 along with the corresponding lever rule and Scheil predictions. For the Scheil equation, the partition coefficient was assumed to be constant with a value of $k_0=0.146[55]$. As can be seen, the measured results for all three alloy systems, except during the later stages, were generally in agreement with the Lever rule and far from the Scheil model. In the
case of Mg-50wt.%Zn, the rapid increase in solid fraction at ~360°C is a result of eutectic solidification and thus the Lever rule no longer applies. Although it is widely recognized that the partition coefficient varies with solutal concentration in a binary system, varying \( k_0 \) for the three alloys did not provide any meaningful difference in the position of the Scheil model fraction solid relative to the experimentally-collected data.

Interestingly, in the previous work for Mg-15wt.%Sn alloys under the similar cooling rate[35], the measured evolution in solid fraction matched the Scheil predictions and not the Lever rule. The difference in the solid fraction evolution with temperature between Mg-Zn and Mg-Sn alloys may result from the underlying thermodynamic parameters of the alloying elements (solute diffusion and solute partition coefficient) as either analytic curve can be shifted to fit the experimental data depending on these values. Note that the dendrite morphology will also influence the distribution of solute concentration during solidification and hence influence the evolution of solid fraction.

**Fig. 7:** Measured evolution of solid fraction together with values determined via the
lever rule and Scheil Equation. (Note, change from filled to hollow symbols
denotes an increase in the cooling rate near the end of experiment.)

3.2.2 Influence of zinc on dendrite tip velocity in the mushy zone during
solidification

The evolution in dendrite tip velocity \( V_{\text{tip}} \) in the mushy zone was characterized in each of the three alloys in order to provide insight into the effect of solute concentration on dendrite growth kinetics. This was carried out by segmenting several representative equiaxed dendrites and then measuring the evolving dendrite arm length \( L \) during the solidification process. As can be seen in Fig. 8, \( V_{\text{tip}} \) in the mushy zone was observed in all three alloys to decrease continuously with time and then arrest at the end of solidification. The gradual decrease of dendrite tip growth rate was mainly ascribed to the rejection of solute ahead of the growing grains, hindering the growth of dendrite arms. As demonstrated in an Al-Cu alloy by Bogno et al.[24] (Fig. 4a and b) the decelerating regime emerges when the far-field solute concentration ahead of the dendrite tip starts to increase because of an overlap between the solute fields of adjacent grains. It must be stated that the initial accelerating growth stage of dendrites are not captured due to a limited temporal resolution between tomograms; this phenomenon can only be captured using ultrafast 2D radiography which which will be on the order of 1000 times faster than tomography[56].

Fig. 8 also shows that all three curves reach a plateau at about 220s after the initial solidification. The duration of the decelerating growth stage as a fraction of total solidification time for each of the Mg-25/38/50wt.%Zn alloys is estimated to be
about 5%, 11% and 20%, respectively. This indicates that the dendrite morphology
evolution was dominated by tip growth only at the early stage of solidification and
then solidification occurred through lengthening and thickening of secondary arms.

As plotted in Fig. 8, the fraction of the dendrite tip growth period with respect to
the total solidification time increases continuously with increasing Zn content. The
experimental results therefore indicate that the amount of Zn influences dendritic
growth kinetics during solidification. This effect can be considered in terms of growth
restriction factor (GRF)[57]. Specifically, the addition of solute elements generates
constitutional undercooling within a diffusion layer ahead of the solid/liquid interface,
restricting dendritic growth and thus limiting the overall growth rate. As suggested by
Lipton et al.[40], the dendrite tip growth velocity in the mushy zone was closely
related to solute concentration and dendrite morphology (tip radius). The dendrite tip
radius in Mg-Zn alloys was demonstrated to decrease with the increasing zinc
concentration, as shown in Fig. 3. Therefore, the difference of dendrite tip velocity in
the mushy zone might also be attributed to the diversity of dendrite morphologies and
growth orientations.
Fig. 8 Average dendrite tip velocity in the mushy zone as a function of solidification time for Mg-25/38/50wt.%Zn alloys. A few dendrites were measured for each composition. The error bars in the figure indicate the standard deviation of the measured values.

### 3.2.3 Effect of solute concentration on specific surface area evolution

The microstructure evolution during dendritic growth and coarsening can be assessed through analysis of the change in specific surface area ($S_v$) with solidification time or solid volume fraction. Voorhees et al. [13] reported that the inverse of specific surface area usually follows a $S_v^{-1} \sim t^{1/3}$ power law during isothermal coarsening of both equiaxed and directionally solidified dendrites. Further research has shown that the temporal exponent is not exactly 1/3 but varies based on solidification conditions[59]. A more general law is thus,

$$\frac{S_v}{S_{v_0}} = [1 + k \times (S_{v_0})^n \times t]^{-1/n}$$

(Eq. 2)

or

$$S_v^{-n} - S_{v_0}^{-n} = kt$$

(Eq. 3)

where $S_{v_0}$ is the initial value of $S_v$ (1/µm), $t$ is the solidification time, and $n$ and $k$ are fitting parameters. $k$ (µm$^n$/s) is generally known as the coarsening rate constant.

Although Equation (3) was derived for isothermal conditions with constant values of interfacial energy and diffusion coefficient, it will also provide a good fit during non-isothermal conditions if one assumes that the temperature variation in the interfacial energy and diffusion coefficient are small[60]. Researchers are working to overcome this limitation, as recently demonstrated by Beckermann et al. [61] who
proposed a more general equation for specific surface evolution during solidification.

Fig. 9 shows the plots of $S_v/S_{v0}$ as a function of time for the three Mg-Zn alloys, along with the fitted curves at the early growth stage. As can be seen in the figure, the specific surface area for all three alloys decreases continuously with solidification time, as expected. The specific surface area at the final stage of solidification is also seen to increase with increased Zn content. As the lines show, Eq. (3) provides a reasonable fit to the experimental data, assuming different fitting parameters are used. With increasing Zn concentration, the exponent $n$ increases slightly, while the coarsening rate $k$ decreases dramatically. The increasing $n$ and decreasing $k$ indicate a slower coarsening process. This is consistent with the qualitative results shown in Figure 2, where coarsening was clearly evident in the Mg-25wt.%Zn alloy, but hardly visible in the Mg-50wt%Zn alloy. The results are also consistent with results of isothermal coarsening experiments conducted on this alloy system [37].
an increased cooling rate near the end of the experiment, and hollow data was not
used for fitting.)

To comprehensively reveal the evolution of a specific surface area, especially in
relation to growing dendrites during solidification, it is imperative to quantify the
specific surface area of dendrites by temperature or solid fraction, as described in a
model proposed by Cahn[62] and further developed by Rath[63]. This model links the
specific surface area ($S_v$) of the dendrite, to its solid fraction ($f_s$) during solidification
and is expressed as follows:

$$S_v = K \times (f_s)^m \times (1 - f_s)^n$$

(Eq. 4)

where $K$, $m$ and $n$ are constants, $f_s$ is the volume fraction of solid phase and
$m=n=2/3$ according to[62] or $0 < (m,n) < 1$ based on the fitting value from results
described in[63]. Fig. 10 illustrates the variations of $S_v$ with solid fraction ($f_s$), along
with the fitted curves. As can be seen, the curves are able to match the experimental
data although $m$ and $K$ must both be taken as fitting parameters. Interestingly, the
exponent $m$ has a negative value. Cahn and Rath’s model assumes the initial grain
shape is globular, hence the specific surface area initially increases with solid fraction
and then continually decreases when $f_s$ exceeded ~0.5. However, in this study, as Figs.
1-3 show, the initial growing grains are already dendritic-like with hierarchical
branches. Therefore, due to the interaction of solute rejected by adjacent solidifying
dendrites and the limitation and restriction of solute diffusion at higher solid fraction,
it is reasonable that the coarsening process tends to decelerate with increasing solid
fraction, causing the value of $m$ to be negative, i.e. we are not capturing the very
initial stages of spherical growth and it’s degeneration, which is happening on a very fine scale and/or a very short time period.

Fig. 10 Specific surface area evolution as a function of solid fraction, and fitted curves using modified Rath and Cahn's model. (Note, change from filled to hollow symbols denotes an increased cooling rate near the end of the experiment, and hollow data was not used for fitting).

4 Conclusions

Using 4D synchrotron X-ray tomography, the dendritic growth dynamics of primary α-Mg grains during the solidification of Mg-Zn alloys with various Zn concentrations was investigated both qualitatively and quantitatively. These in situ observations demonstrate conclusively that a dendritic morphology transition occurs in Mg-Zn alloys. This finding, along with prior similar findings in fcc Al, strongly supports the hypothesis that Zn modifies the anisotropy in interfacial energy in alloy systems that have inherently weak anisotropy in interfacial energy (e.g. Mg, Al).

Synchrotron tomography revealed the mechanisms by which hyper-branched
structures form, i.e. via doublon, triplon and quardrulon (or doubling doublons). The dynamic formation of these structures was captured and quantified, revealing new tip-splitting mechanisms.

Analysis of the time resolved 3D images allowed the first quantification of the microstructural evolution of Mg-Zn alloys during solidification, including: solid fraction ($f_s$), dendrite tip growth velocity ($V_{tip}$), and specific surface area ($S_v$). The $f_s$ variations with temperature were found to correlate well with lever rule. Dendrite tip growth was found to decelerate continuously with solidification time, and dendrite tip growth as a mechanism of dendrite morphology evolution was found to dominate only at a very early stage of solidification. The evolution of $S_v$ during dendritic growth compared well with Poirer’s model[59], demonstrating the rate of dendritic coarsening decreases with increasing Zn concentration. The data was also fit to Cahn and Rath’s equation to reveal the evolution of $S_v$ with $f_s$ during solidification.

These 4D observations provide both the first quantification of dendritic growth dynamics during the solidification of these magnesium alloys, providing a method for both informing and validating numerical models of microstructural evolution, e.g. phase field simulations and cellular automata methods.

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Data statement

Representative samples of the research data are given in the figures and supplementary data. Other datasets generated and/or analysed during this study are not publicly available due to their large size but are available from the corresponding authors on reasonable request.

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