

1 **Fatigue life sensitivity of monopile-supported offshore wind turbines to** 2 **damping**

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7 8 **Abstract**

9 Offshore wind energy is an important renewable electricity source in the UK and Europe.
10 Monopiles are currently the most commonly used substructures to support offshore wind
11 turbines. The fatigue life of offshore wind turbines is directly linked to the oscillatory bending
12 stresses caused by wind and wave loading. The dynamic response of the structure is highly
13 dependent on the combined aerodynamic, hydrodynamic, structural, and soil damping present.
14 The fatigue life sensitivity of a reference 5MW wind turbine under operational and non-
15 operational conditions has been investigated using time-domain finite element simulations. The
16 model uses beam elements for the monopile and tower and includes nonlinear p-y curves for
17 soil-structure interaction. The effects of the wind turbine operation, environmental loads, and
18 variable damping levels on the fatigue life were investigated systematically. The fatigue life
19 increases significantly as a result of reductions in the bending stress caused by increased
20 damping. From a practical point of view, significant cost-savings could be achieved in the
21 design of a wind turbine by fitting supplemental damping devices. An efficient approximate
22 method is proposed to assess the influence of damping, by scaling the vibration amplitudes
23 around the first natural frequency of the system.

24 **Keywords:** Offshore wind turbine; Fatigue life calculation; Vibration analysis; Renewable
25 energy

26 **1 Introduction**

27 Offshore wind electricity generation has become one of the fastest growing renewable energy
28 technologies. Europe has focused extensively on the development of offshore wind energy, to
29 the extent that almost 90% of the largest offshore wind farms in the world are located there
30 [1,2]. Monopiles are currently the most common type of support structure for offshore wind
31 turbines. The fatigue life of offshore wind turbines (OWT) is directly linked to the stress
32 induced by the structural vibrations due to environmental (wind and wave) loading. As a
33 dynamic system, the magnitude of the response of an OWT depends on the amplitude of the
34 applied forces, the proximity of the natural frequencies to the dominant forcing frequencies
35 and the damping. As wind turbines are lightly damped structures, a good estimate of the
36 damping is crucial to predicting their dynamic response accurately. The overall damping in
37 offshore wind turbines is mostly comprised of aerodynamic, hydrodynamic, structural and soil
38 damping, and damping due to supplemental damping devices such as tuned-mass dampers.
39 There is significant uncertainty about each of these contributions. Soil damping depends on the
40 soil type and is particularly difficult to measure directly. Different values for soil damping
41 ratios in offshore wind turbines mounted on monopiles have been suggested in literature [3-6],
42 varying from 0.17% [4] up to 1.3% of critical damping [6]. Aerodynamic damping is the
43 highest contributor to the overall damping, but it mostly acts in the fore-aft direction when the
44 turbine is in operation. In parked conditions, good agreement is found for the side-side and
45 fore-aft damping levels reported in literature [7–9]. In this case, the overall damping is reported
46 to be about 1% of critical damping in the fore-aft direction and 1.5% for the side-side mode. In
47 the operational range, the aerodynamic damping is known to be variable and the levels
48 proposed in the literature vary from 2% to 8%, depending on the wind speed, size and operation
49 of the wind turbine [10–12].

50 Offshore wind turbines are generally designed for a minimum of 20 years of service life [13]
51 and the predicted fatigue life of the system has to match this [14,15]. Four methods of fatigue
52 assessment for structures are commonly used; simplified method, spectral method, time-
53 domain method and deterministic method [16]. As the aerodynamic loading has a wide
54 bandwidth, damage calculation methods in the frequency domain lead to very conservative
55 estimates [17]. Time-domain approaches are considered the most reliable for the prediction of
56 fatigue life as nonlinear and stochastic load effects caused by the environmental loads and soil-
57 structure interaction can be taken into account [18]. In addition, various hybrid frequency/time-
58 domain fatigue analysis methods have been proposed [17–21], typically using transfer
59 functions to obtain the response in the frequency-domain [17,18,22–25]. However, in general
60 predictions of fatigue life are considered less accurate than using time-domain methods.

61 The influence of damping on the fatigue damage of offshore wind turbines has been mostly
62 considered in parked/non-operational conditions in the literature. The fatigue assessment of
63 OWT is usually carried out by simulating and analysing the stress at critical locations such as
64 the tower base [25, 26] or the mudline [27]. The effect of damping in a parked condition was
65 studied and it was demonstrated that the maximum bending moment could increase by 20% as
66 a result of a 50% change in damping [6]. It was further shown that the mudline bending moment
67 during an extreme wind and wave event is decreased by 5% if damping is increased by 1% [4].
68 The effect of soil damping has been studied and up to 47% reduction in fatigue damage due to
69 a 4% increase in soil damping has been reported [26]. It was also suggested that a complete
70 lifetime simulation including damping effects could clarify the influence on the fatigue life of
71 OWTs, which has not been reported in literature.

72 This paper investigates systematically the effects of damping on the fatigue life of offshore
73 wind turbines. The study is based on time-domain finite element (FE) simulations carried out
74 on a reference offshore wind turbine supported by a monopile, including soil-structure

75 interaction. The fatigue life was calculated by adding the damage contributions from
76 representative environmental states in the operational wind speed range. The methodology is
77 described in section 2. Section 3 discusses the relevant features of the wind and wave loads. In
78 section 4, the effects of variable damping and operational state (shutdowns) are studied
79 systematically. The contribution of increased damping on increased fatigue life is investigated.
80 A novel approximate method is proposed, significantly reducing the computational costs
81 associated with time-domain simulations for multiple damping levels (requiring only one full
82 time-domain analysis for one level of damping with little additional computational effort for
83 other damping levels), while allowing accurate predictions of the effect of increased damping
84 on prolonged fatigue life.

85 **2 Methodology**

86 2.1 Modelling approach

87 As fatigue affects mostly structural details (e.g. welds), it must be assessed using a
88 comprehensive and realistic structural model. Following other researchers [26, 28–31], this
89 study is based on a reference 5MW case study wind turbine model mounted on a monopile, for
90 which the US National Renewable Energy Laboratory (NREL) has provided a significant
91 amount of data [32]. According to initial design reports [33], it was due to be constructed at a
92 location approximately 10 km off the Dutch coast in the North Sea. The complete fatigue
93 analysis was carried out in different stages using a combination of software packages. The
94 process is shown schematically in Fig. 1. The wave and wind loads were calculated based on
95 available meteorological data for the proposed site. Wave load time-series were obtained in
96 MATLAB by inverse-Fourier Transform of the JONSWAP spectrum [34]. Wind load time
97 histories were calculated using FAST, a software package provided by NREL, which includes
98 a validated model of the turbine chosen here. FAST simulates an incoming turbulent wind field
99 (TurbSim module) and then computes the aerodynamic interaction of the flow with the blades

100 using Blade Element Momentum theory. FAST also provides an estimate of the aerodynamic
 101 damping, which is otherwise difficult to obtain. As FAST has limited capabilities for modelling
 102 soil-structure interaction and only allows for a basic structural model of the tower/monopile,
 103 the wind loads obtained from FAST and wave loads from Matlab were used as input to an FE
 104 model (ABAQUS) of the OWT which comprised the tower, monopile and soil system.
 105 Response stress time histories were computed and recorded in ABAQUS at critical locations
 106 for various load time series.

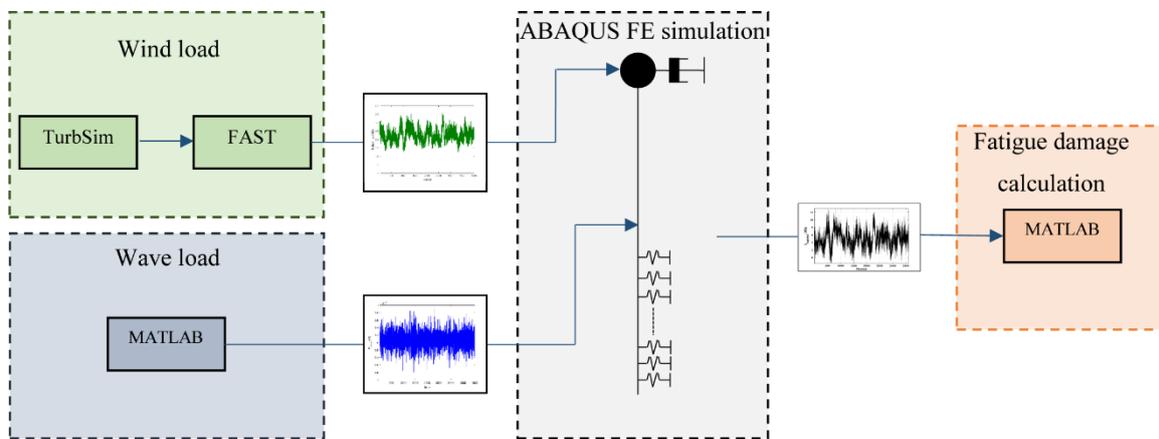


Figure 1. Schematic of simulation software packages for fatigue life calculation.

107 2.2 Geometry and properties of the OWT and monopile

108 The reference wind turbine is a 3-bladed wind turbine, shown schematically in Fig. 2 with key
 109 dimensions. The rotor diameter is 126m, and the hub height at 92m above mean sea level. The
 110 monopile embedded depth is 45m for a water depth of 21m. The NREL 5MW wind turbine
 111 uses a Repower 5M machine. The rotor blades are based on a LM-Glasfiber Holland design
 112 with a length of 62.7m [35]. A slight modification to the blades adopted here was suggested in
 113 reference [32], which truncated the length of the blades by 1.1m to be similar to those suggested
 114 for the Repower 5M machine. The operational range of wind speeds for this turbine is between
 115 3m/s to 25m/s, with the rated rotor speed at 12.1 rpm.

116 The pile has a 6m diameter with a constant thickness, while the tower has a tapered section
 117 with the diameter decreasing linearly from 6m at the bottom to 3.87m at the top (Fig. 2). In this

118 study, the thickness of the pile and tower sections were modified from the original documents
119 [32] to ensure that the natural frequency of the wind turbine lies between the 1P (rotor) and 3P
120 (blade passing) frequencies with a margin of 10%. A pile thickness of 80mm and linearly
121 varying tower thickness of 28-38mm were used to ensure that the first natural frequency of the
122 system lies at 0.25Hz.

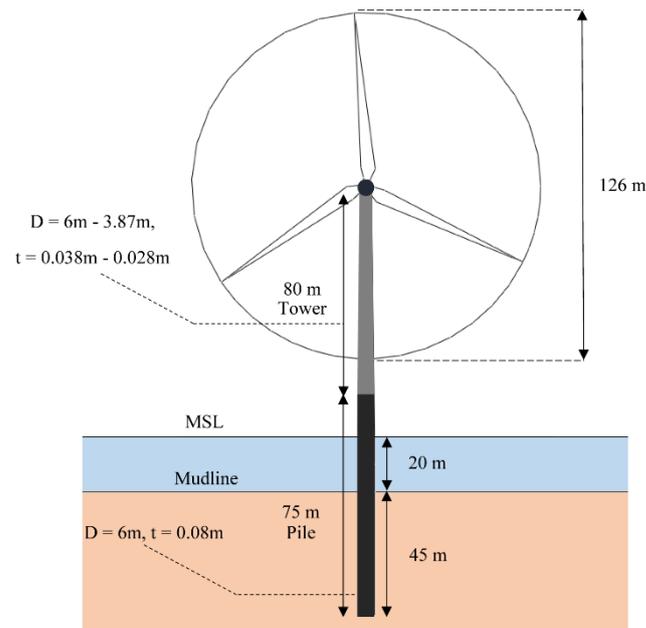


Figure 2. Reference 5MW wind turbine dimensions.

123 The steel used for the monopile is assumed to have an elastic modulus of 210GPa, a Poisson
124 ratio of 0.3 and a density of 7850 kg/m³. A higher density steel ($\rho=8500\text{kg/m}^3$) was used for
125 the tower section to take into account the added mass of secondary steel [32].

126 2.3 Numerical simulation

127 The OWT time response due to the combined non-periodic aerodynamic and wave loading was
128 simulated using the FE software ABAQUS. The equation of motion of the structure was
129 implicitly solved for small amplitude vibrations. The FE Model comprises the tower and
130 monopile, modelled using linear Timoshenko beam elements (ABAQUS: B21 element). The
131 rotor was modelled as a lumped mass located at the top of the tower. The soil-structure
132 interaction was modelled with nonlinear horizontal springs (p-y curves) connecting the

133 monopile to a fixed reference (see section 2.4). A preliminary study showed that 0.5m length
134 elements produced sufficiently converged results, with less than 0.5% change in the results
135 when the element size was reduced from 1m in length. Good agreement with relevant reports
136 on the 5MW NREL wind turbine was obtained [32]. The dynamic analysis for fatigue
137 calculations was done using implicit simulations with time increments of 0.1s. Following
138 recommended practice, a one-hour simulation length was used throughout this paper. A
139 preliminary study of fatigue damage sensitivity to simulation time confirmed that this was
140 acceptable. Four hundred seconds were added at the start of the load time series and the
141 corresponding simulation data was later discarded to avoid any potential initial transient
142 effects. Numerical damping is normally applied by default in ABAQUS to stabilise the
143 numerical scheme. This was set to zero as damping is a key factor for this study that needs to
144 be controlled carefully. The stabilisation of the solution was achieved by applying damping in
145 the model. Offshore wind turbines can be considered as lightly damped structures (overall
146 damping ratios typically lower than 10% of critical damping). Therefore, the energy dissipation
147 processes can be linearized, with the amplitude of dynamic response only depending on the
148 correct overall amount of damping. The model accuracy was checked for different
149 implementations of the damping (e.g. Rayleigh & dashpot damping), and the same response
150 was obtained for the same overall damping ratio. The structural, hydrodynamic and soil
151 damping were combined and modelled as Rayleigh damping, which is common practice [7, 11,
152 26]. The aerodynamic damping was simulated through a dashpot at the top of the monopile in
153 the direction of the wind load [36]. This provides a spatial distribution closer to the real system
154 and allows this damping contribution to be varied independently. The Rayleigh damping was
155 kept constant throughout as 2% of critical damping, incorporating structural (1%),
156 hydrodynamic (0.2%) and soil (0.8%) damping contributions based on literature [3, 6]. The

157 aerodynamic damping was varied independently from 4% to 9% based on literature values
158 [10], as described in the following sections.

159 2.4 Soil structure interaction modelling

160 In the FE model, the bottom of the monopile was supported vertically on a roller while 30
161 horizontal springs were distributed every 1.5m along the embedded height of the pile to model
162 the lateral soil-structure interaction. Following DNV [14] and API [37], non-linear p-y curves
163 were used to define the stiffness of the springs following the soil properties listed in Table 1.
164 P-y curves are further described in references [38, 39] for homogeneous and layered soils. For
165 the actual loads in an offshore wind turbine, most of the soil-structure interaction occurs on the
166 initial, linear part of the p-y curves. This has been employed for the approximate method
167 (section 4.4), which effectively linearizes the soil-structure interaction. Due to the lack of data
168 for the planned location, the soil profile used here was based on an interpolation of available
169 data from neighbouring sites whose soil profile mostly consists of medium-dense to dense sand,
170 as used in reference [40].

171

Table 1. Soil profile for proposed location, modified according to data from [40]. γ_{sat} is the saturated unit weight, and ϕ' is the angle of friction of the soil layers.

Soil layer	Layer description	γ_{sat} (kN/m ³)	ϕ'
0m to -15m	Loose sand	17	27.5
-15m to -20m	Firm clay	19	20
-20m to -25m	Fine to medium sand	19	32.5
-25m to -65m	Fine to medium sand	19	35

172

173 2.5 Environmental load calculation

174 Aerodynamic and hydrodynamic loads are the driving dynamic forces in the fatigue of offshore
175 wind turbines. The relative directionality of wave and wind loads has been the subject of
176 research [6]. For this study, the wind and wave loads are assumed to be in the same direction
177 as a likely worst case scenario. In reference [25], 3D scatter diagrams of wind speed (V_w),
178 significant wave height (H_s) and zero-crossing wave periods (T_z) were used to create a set of
179 environmental states, which were applied in this research. Wind speeds ranging from 4m/s to
180 24m/s were grouped into 2m/s bins. Wave heights and periods were grouped in 0.5m and 1s
181 bins, respectively. Environmental states (ES) were defined by correlated wind and wave bins.
182 The environmental states were classified into 22 states as shown in Table 2 [25], in line with
183 other studies that used a similar number of ES [41, 42]. As expected, the ES with higher wind
184 and wave intensities have a significantly lower probability of occurrence, while the majority of
185 ES occur with wave heights of below 2m, wave period of less than 4.5s and wind speeds of
186 less than 15m/s. The operational ES (Table 2) account for 91% of probability of occurrence,
187 with most of the remaining 9% corresponding to wind speeds below the cut-in speed and thus
188 low contribution to fatigue damage.

Table 2. Environmental states, based on data from [25].

State	V _w (m/s)	T _Z (s)	H _s (m)	P _{State} (%)
1	4	3	0.5	3.95
2	4	4	0.5	3.21
3	6	3	0.5	11.17
4	6	4	0.5	7.22
5	8	3	0.5	11.45
6	8	4	1.0	8.68
7	10	3	0.5	5.31
8	10	4	1.0	11.33
9	12	4	1.0	5.86
10	12	4	1.5	6.00
11	14	4	1.5	4.48
12	14	5	2.0	3.26
13	16	4	2.0	1.79
14	16	5	2.5	3.10
15	18	5	2.5	1.74
16	18	5	3.0	0.80
17	20	5	2.5	0.43
18	20	5	3.0	1.14
19	22	5	3.0	0.40
20	22	6	4.0	0.29
21	24	5	3.5	0.15
22	24	6	4.0	0.10

189

190 Mann [43] and Kaimal [44] spectra are the main turbulent wind models suggested in practice.
191 In this study, the Kaimal spectrum was used to model the wind turbulence. The wind speeds
192 for the selected ES are all within the operational range of the reference wind turbine. However,
193 in this paper, the turbine will be considered in three possible states: (i) in operation, (ii)
194 stationary and blades feathered (least drag) and (iii) stationary and pitched-out blades
195 (maximum drag). In operation, a constant blade pitch and rotor speed were considered for a
196 given mean wind speed at hub height. The rotor thrust was calculated using FAST by
197 constraining the tower and monopile to be rigid. These thrust time series were then used as the
198 input wind load in ABAQUS. This approach, where the separately calculated wind and wave

199 loads are combined in an FE software, has been used in various references [25,31]. The wind
200 and wave loads were calculated using 0.1s time increments to match the FE time steps.

201 The random nature of the wave load for the North Sea conditions is most commonly captured
202 through the JONSWAP [34] spectrum, a modified version of the Pierson-Moskovitz (P-M)
203 [45] spectrum. The surface velocities and accelerations were defined according to linear (Airy)
204 wave theory. Wheeler stretching was applied to the velocity and acceleration terms to account
205 for the variation of the mean sea surface. The wave force on the vertical pile was calculated
206 using Morison's equation. The effect of currents on the wave force was considered by adding
207 the mean current velocity to the water particle velocities in the drag component of the wave
208 load, as the current results in a static transverse force on the pile. The resultant hydrodynamic
209 pressure was applied as a point load at the mean sea level.

210 2.6 Fatigue life calculation

211 Design guidelines provide a recommended practice for the fatigue life calculation of offshore
212 wind turbines that is followed here. DNV [46] proposes various S-N curves to assess the fatigue
213 capacity of details in offshore structures. S-N curves are defined by Eq. (1), where N refers to
214 the number of cycles to failure, $\log(\bar{a})$ corresponds to the intercept of $\log(N)$ axis, $\Delta\sigma$ is the
215 stress range, m is the negative inverse slope of the curve and SCF is the stress concentration
216 factor. t and t_{ref} are the thickness through which the crack is likely to grow (i.e. thickness of the
217 monopile) and a reference thickness, respectively. In the current study a bi-linear S-N curve
218 class E, which is suggested for piles, is used and the parameters for the considered location of
219 circumferential welding are shown in Table 3.

$$\log(N) = \log(\bar{a}) - m \log\left(\Delta\sigma(SCF) \left(\frac{t}{t_{ref}}\right)^k\right) \quad (1)$$

220

Table 3. S-N curves parameters, according to [46].

$N \leq 10^6$		$N \geq 10^6$		Thickness component	Hot-spot consideration
Log(\bar{a}_1)	m_1	Log(\bar{a}_2)	m_2	k	SCF
11.61	3.0	15.35	5.0	0.2	1.13

221

222 The fatigue damage was calculated at the location of maximum stress at an assumed welding
 223 point. The location of maximum stress in the monopile was investigated and it was found to be
 224 approximately 8m below the seabed and sensitive to changes in the seabed condition (for
 225 instance due to scour).

226 The random nature of the loading results in variable amplitude stress outputs. Rainflow
 227 counting was used to bin the stress amplitudes into multiple stress levels and count the number
 228 of cycles in every stress bin. Once the stress output was rainflow-counted, the results were used
 229 to find the damage caused by every stress bin and then added together to obtain the total damage
 230 in the monopile for a given stress time-history. The damage D in the pile for a given ES j was
 231 calculated using the Palmgren-Miner (PM) sum rule as shown in Eq. (2)

$$D_j = \sum_{i=1}^{N_C} \frac{n_i}{N_i}, \quad (2)$$

232 where n_i is the number cycles counted within a given stress bin, N_i is the number of cycles to
 233 fatigue failure [47] for the nominal stress cycle amplitude i , and N_C is the total number of bins
 234 counted over the one hour time history. Denoting D_{ref}^{1hr} the damage required in one hour of
 235 simulation time that would lead to a total damage of 1 (failure according to PM sum rule) over
 236 20 years. D_{ref}^{1hr} is used to normalise the damage calculated for each ES.

237 As each ES j has a different probability of occurrence p_j , the normalised contribution of ES j
238 to the total fatigue damage is $DC_j = \frac{D_j}{D_{ref}^{1hr}} p_j$ and the total fatigue damage is obtained by
239 summing each damage contribution according to Eq. (3), with $20 \text{ years}/D$ the resultant fatigue
240 life of the monopile:

$$D = \sum_{j=1}^{N_j} DC_j . \quad (3)$$

241 Fatigue damage calculation was verified using harmonic loading simulation. The fatigue
242 damage at the mudline was calculated using the rainflow counting and fatigue life calculation
243 MATLAB scripts and compared and verified with the analytically calculated damage. Using
244 this methodology, the fatigue life of the reference turbine system was predicted for various
245 levels of aerodynamic damping and operational regimes.

246 **3 Influence of operational regime on loads**

247 The operational regime of the wind turbine determines the aerodynamic forces and damping
248 on the structure. Figure 3(a) shows the mean resultant wave loads and their standard deviation
249 for the sea states considered. The mean and standard deviation of the aerodynamic and
250 hydrodynamic loads were used to quantify their static and dynamic (varying) components.
251 With increasing wave height and period, the static component of the wave load increases only
252 slightly, whereas the dynamic component increases significantly. Figure 3(b) and (c) show the
253 mean and standard deviation of the operational and non-operational wind loads for each ES.
254 For the non-operational wind turbine, feathered and pitched-out blades are considered
255 separately. As one would expect, the aerodynamic load is significantly higher when the blades
256 are pitched-out than when they are feathered. As the ‘intensity’ of the ES increases, so do the
257 mean and standard deviation of the rotor thrusts. When the wind turbine is in operation, the
258 mean wind load peaks at the rated wind speed and then decreases (as blades are increasingly
259 feathered), whereas the standard deviation of the load shows a continuous increase with the
260 wind speed due to turbulence. The mean rotor thrust for the operational wind turbine is
261 normally higher than for the non-operational feathered wind turbine. In the case of pitched out
262 blades, the mean wind thrust for very high wind speeds (environmental states 22 and 24) is
263 greater than during operation, where blades are turned out of the wind. Significantly lower load
264 turbulence is present for the non-operational wind turbine compared to that experienced by the
265 pitch-controlled operational wind turbine as the rotor is stationary.

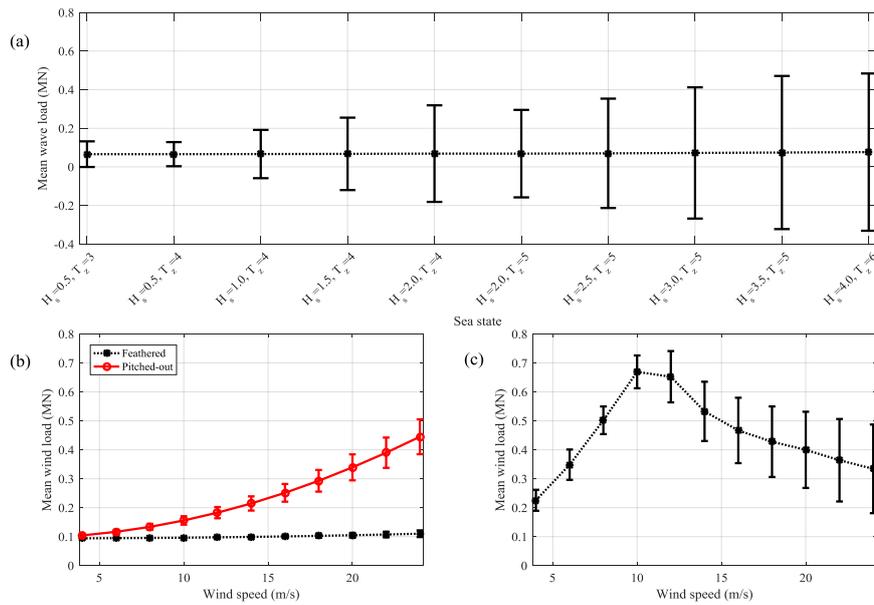
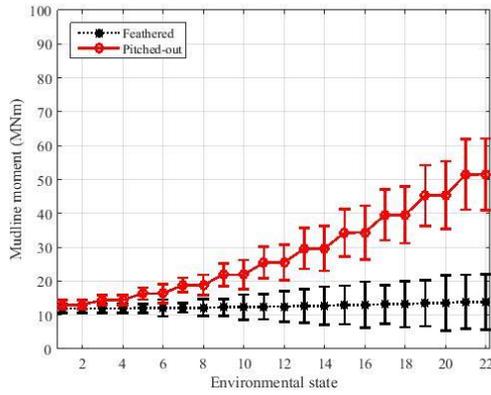
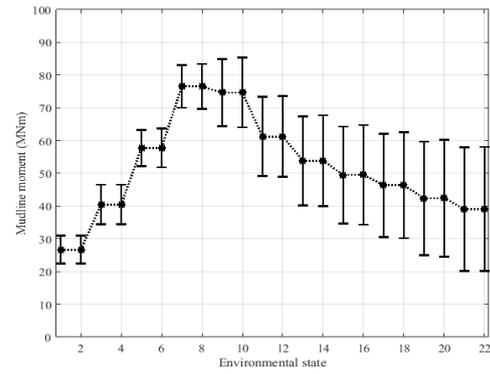


Figure 3. Mean (static component) and standard deviation (variable component) of the environmental loads: (a) wave load; (b) non-operational wind load (feathered and pitched-out); (c) operational wind load.

266 As a wind turbine is a cantilevered structure, the highest bending moment and stresses occur
 267 close to the bottom, with a significantly higher lever arm and thus bending moment contribution
 268 from the wind load during operation. Figure 4(a) shows the mean and standard deviation of the
 269 mudline bending moment for the non-operational wind turbine, calculated from the combined
 270 wind and wave forces. When the blades are feathered, the wind load is approximately constant
 271 and the mean and standard deviation of the mudline bending moment is mainly driven by the
 272 increase in the variable component of the hydrodynamic loads. However, when the blades are
 273 pitched-out, the higher lever arm of the wind thrust leads to an increasing mean mudline
 274 bending moment. The standard deviation of the bending moment at mudline increases as both
 275 wind and wave loads have increasing dynamic components. Figure 4(b) shows the mean and
 276 standard deviation of the mudline bending moment for the operational wind turbine. The mean
 277 value peaks at the ES corresponding to the rated wind speed and then slowly decreases,
 278 following the wind speed pattern observed in Figure 3(c).



(a)



(b)

Figure 4. Mean (static component) and standard deviation (dynamic component) of mudline bending moment for (a) non-operational wind turbine; (b) operational wind turbine.

279 As the soil stiffness is not infinite, the location of the maximum longitudinal stress in the
 280 monopile (relevant for fatigue) is not at the mudline. Figure 5 shows the variation of the
 281 bending moment along the depth of the monopile caused by applying 1MN wind and wave
 282 loads. For the soil conditions considered, the maximum bending moment in the reference
 283 monopile occurs approximately 8m below the mudline. Assuming the maximum stress occurs
 284 at the mudline instead of its actual location could result in an error of approximately 15% in
 285 the stress amplitudes in the monopile, significantly underestimating fatigue damage. Note that
 286 the location of this maximum stress is specific to the geometry considered here and could shift
 287 depending on the soil properties, water depth, scour depth and the respective magnitudes of the
 288 loads.

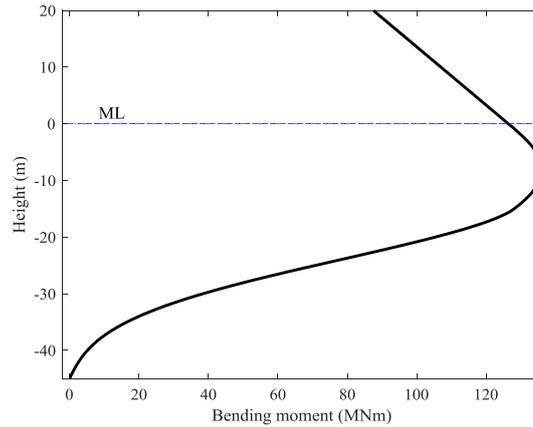


Figure 5. Bending moment in the reference monopile for 1MN wind and wave loads.

289 4 Fatigue analysis results

290 4.1 Effect of variable damping

291 In this section, the effect of the variation of damping with wind speed is investigated by
 292 comparing the fatigue life of the OWT when damping is assumed variable or constant. Variable
 293 aerodynamic damping values with respect to wind speed were taken from [48], ranging from
 294 3.7% to 5.4% depending on the wind speed (Table 4), with the maximum value close to the
 295 rated operational wind speeds. These values are realistic, but only used for illustrative purposes
 296 as they are based on a smaller wind turbine. The average value of damping of approximately
 297 4.5% was used as a constant value for comparison.

Table 4. Aerodynamic damping ratio contributions at different wind speeds, based on data from [48].

Wind speed (m/s)	4	6	8	10	12	14	16	18	20	22	24
Aerodynamic damping (%)	4	4	3.7	4.4	4.6	5.4	5.3	4.9	4.7	4.5	4.3

298

299 Simulation results (not presented graphically) showed that considering a variable aerodynamic
 300 damping had mixed effects on fatigue damage. For ES where the variable damping is
 301 appreciably higher than average (e.g. states 11-14), the fatigue damage contribution was

302 reduced by up to 16%. For other ES, the variable damping values are close to the average and
303 the ES probabilities of occurrence are low enough that the effect on fatigue damage
304 contribution was minimal. Overall, the fatigue life was calculated as 31 years for the constant
305 damping case and 33 years for the variable damping case – a 7% increase in the predicted
306 fatigue life of the system. Given that the values of varying aerodynamic damping are difficult
307 to obtain and come with significant uncertainty [48], this rather small difference in fatigue life
308 suggests that in practice assuming a constant aerodynamic damping for all wind speeds leads
309 to acceptable fatigue life estimates. Therefore, a constant aerodynamic damping is assumed
310 throughout the remainder of the paper.

311 4.2 Operational versus non-operational wind turbine

312 Although the environmental loads considered are in the operational range of the wind turbine,
313 this section investigates the long-term effects on the fatigue life of wind turbine shut-downs.
314 As they cause both a decrease in load and in damping, their overall effect is difficult to assess
315 without a complete fatigue life calculation. Approximately 5% of aerodynamic damping for
316 the operational wind turbine was suggested in reference [12], and as described in the
317 introduction, structural damping is reported to be approximately 1-2%. Therefore, a reference
318 damping of 2% for the non-operational and 7% for the operational wind turbine was assumed
319 in this section.

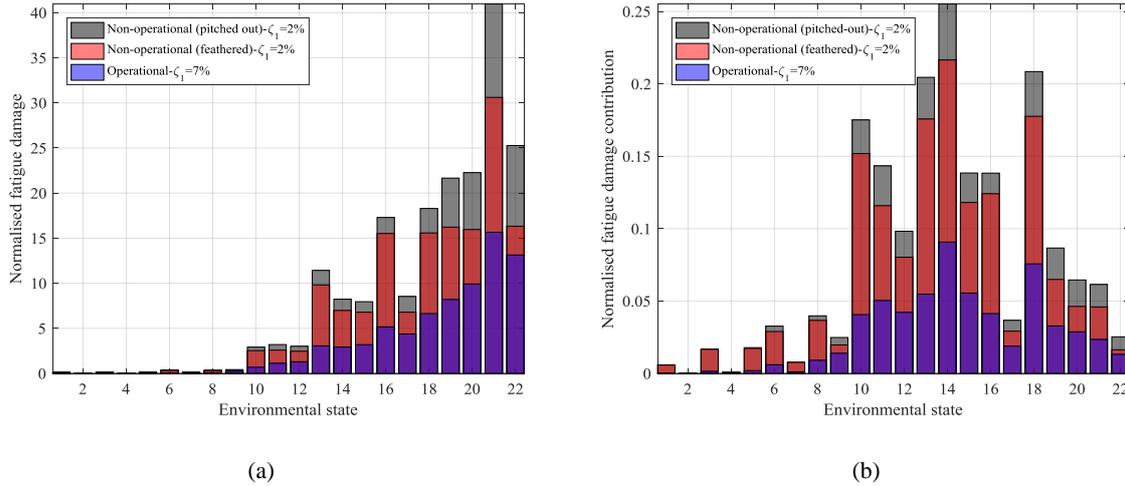


Figure 6. (a) Normalised damage and; (b) normalised fatigue damage contribution of the environmental states for operational and non-operational (feathered and pitched-out) wind turbines. Bars are overlaid (i.e. all start from zero).

320 Figure 6(a) shows the normalised damage for each ES, comparing the operational turbine with
 321 non-operational (feathered and pitched-out) loads and damping. The environmental loads and
 322 resulting bending moments for the operational and non-operational wind turbine can be seen
 323 in Figs. 3 and 4. Figure 6(b) shows the contribution of the ES to the fatigue damage of the wind
 324 turbine, taking the probability of occurrence of each state (Table 2) into account. Figure 6(a)
 325 shows that the fatigue damage increases in general with increasing wind speed and wave height,
 326 with slight variations due to the dynamic amplification from the forcing frequencies. The lower
 327 ES (up to #8) do not lead to significant fatigue damage. The ES that are above the rated wind
 328 speed of the operational wind turbine lead to a significantly higher fatigue damage. This
 329 confirms that the wind load has a high contribution to the fatigue damage of operational
 330 systems. In non-operational mode, the fatigue damage is dominated by the dynamic wave load.
 331 Feathered blades lead to lower damage than pitched-out blades due to the lower aerodynamic
 332 load component. Figure 6(a) shows that in spite of the lower aerodynamic loads in the non-
 333 operational cases, the fatigue damage is significantly higher due to the absence of aerodynamic
 334 damping.
 335 Figure 6(b) shows that fatigue life is dominated by the contribution of the ES around the rated
 336 wind speed. The predicted fatigue life of the operational wind turbine is approximately 33

337 years, as opposed to 11 years for the pitched-out and 14 years for the feathered non-operational
338 cases. The importance of the aerodynamic damping is clearly demonstrated by the fact that the
339 higher operational damping compensates for the higher rotor loads and results in a fatigue life
340 that is more than twice the fatigue life of the non-operational case. ES are paired up such that
341 odd-numbered states have the same wind speed as the following even-numbered state, so
342 damage variation within each pair can be attributed only to different wave loading. For
343 instance, in Fig. 6(a) environmental states 21 and 22 have the same wind speed of 24m/s but
344 different wave loads (Table 2). The difference in the fatigue damage of these environmental
345 states are approximately 40% for the non-operational wind turbine, but considerably lower for
346 the operational case. These large variations, due to the differences in wave loading, are a feature
347 characteristic of ES with above-rated wind speed (see also ES 15-16 and 17-18) and can be
348 explained by a combination of the higher magnitude of wave loads and the proximity of the
349 wave peak frequency to the first natural frequency of the wind turbine.

350 4.3 Damping influence

351 In this section, a set of damping levels is considered to examine their effect on the fatigue
352 damage in the wind turbine. The levels of damping applied to the operational wind turbine
353 model range from 4% to 11%, including 2% applied in the form of Rayleigh damping to
354 account for structural, hydrodynamic and soil damping. The standard deviation of the
355 longitudinal stress (at 8m below the seabed) shows a reduction of approximately 7%, 13%, and
356 17% for an increase of 2%, 5%, and 7% in the overall damping of the system. These reductions
357 are higher than those reported in reference [26] in the operational range of the wind turbine
358 (value of the aerodynamic damping not stated).

359 Figure 7(a) shows the normalised fatigue damage and Fig. 7(b) shows the contribution of the
360 normalised damage of each ES at various damping levels while the turbine is in operation. As
361 expected, the fatigue damage observed with 4% overall damping is the highest. Higher

362 damping levels lead to a reduction in fatigue damage, but the reduction varies to some degree
 363 depending on the wind and wave loading for each ES.

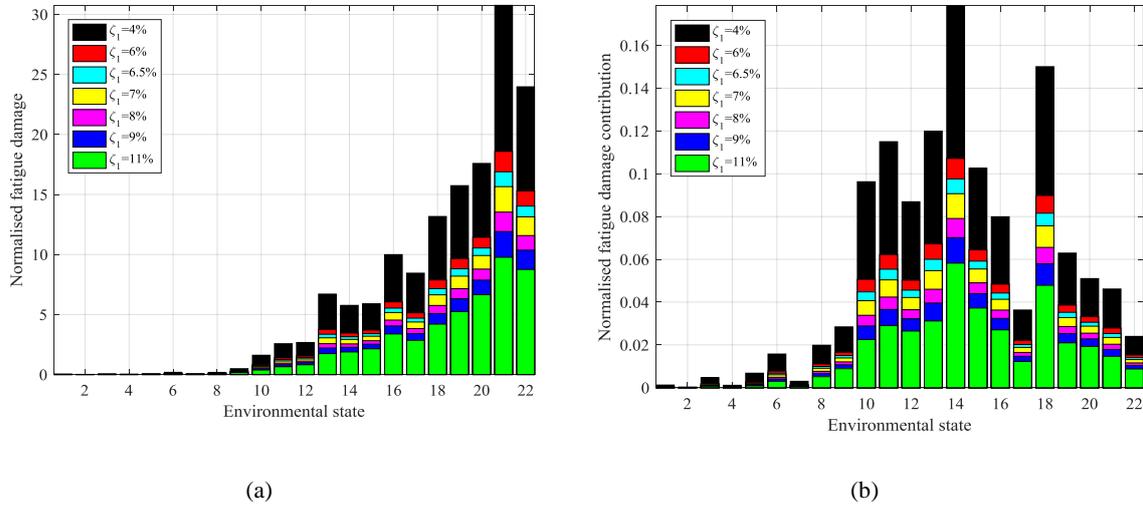


Figure 7. (a) Fatigue damage, and (b) fatigue damage contribution for every environmental state at different levels of total damping.

364 The lower ES show a larger reduction, while the damage reductions for ES above the rated
 365 wind speed converge to similar levels. Compared to the values for 4% overall damping, the
 366 fatigue damage for 6% total damping reduces by an average of approximately 45%. This
 367 decrease is even more pronounced and reaches 75% when 11% total damping is considered.
 368 The contribution of an ES to the overall fatigue of the structure depends on the combination of
 369 its probability of occurrence and absolute damage. In general, the higher ES have lower
 370 probabilities of occurrence but cause more damage. ES 1 to 9 have a low contribution to the
 371 fatigue of the system due to their low normalized fatigue damage (Fig. 7(a)). The most
 372 damaging environmental states are at and above the rated wind speed, with ES 14 and 18
 373 contributing the most damage due to the combination of normalised fatigue damage and
 374 probability of occurrence (Table 2). The combined contribution of fatigue damage from ES 10
 375 to 18 is more than 70% of the overall damage.

376 Figure 8 shows the projected fatigue life of the wind turbine (100% operational) based on the
 377 damage contributions obtained for the different damping values shown in Fig. 7(b). The design

378 fatigue life of 20 years is marked as a reference. An almost linear increase in fatigue life is
 379 observed when damping increases, from 16 years at 4% overall damping to 53 years at 11%
 380 damping. The changes in the overall fatigue life are consistent with the average reductions in
 381 the ES damages as shown in Fig. 7(a) and demonstrate the potential fatigue life extension of a
 382 wind turbine structure with additional damping, e.g. in the form of a tuned-mass damper or
 383 other structural modifications. Wind turbines are regularly shut down for short maintenance
 384 and inspection periods, but breakdowns can lead to longer non-operational periods during
 385 operational ES until repairs can be carried out. In a hypothetical scenario where the turbine is
 386 left parked for an extended period, the fatigue damage is increased, as was shown in section
 387 4.2 from the comparison of operational and non-operational wind turbines. Assuming
 388 respectively 5% and 10% downtime (95% and 90% operational) and summing the proportional
 389 damage, a reduction in the fatigue life of the wind turbine of approximately 2% and 4% is
 390 predicted, indicating a potential danger of prolonged downtime.

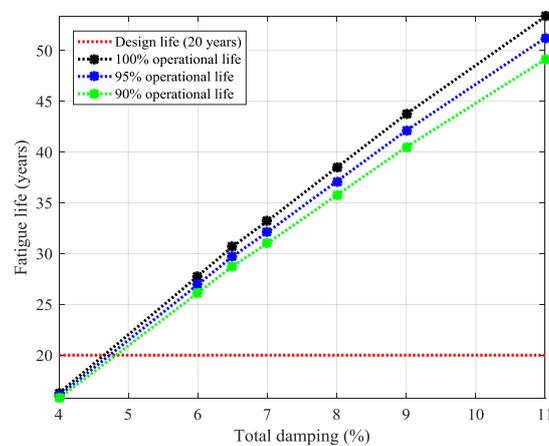


Figure 8. Fatigue life comparison for various levels of damping and operational life.

391 4.4 Approximate method for the prediction of fatigue life

392 In this section, a hybrid time-domain approach is proposed, which only requires the full time-
 393 domain analysis for one level of damping and uses it to predict the fatigue life at other damping
 394 levels with little additional computational effort. The outline of the simplified fatigue analysis
 395 is shown in Fig. 9. In this method, the output stresses from the time-domain simulations of a

396 reference damping level are transformed into the frequency-domain. The dynamic
 397 amplification factor (DAF) of an equivalent single degree of freedom system (SDoF), which
 398 can be easily obtained from the dynamic properties of the wind turbine, is used as a substitute
 399 for the transfer function of the FE model. The reference stresses are scaled by the frequency-
 400 dependent ratio of amplification of the response between each damping level and the reference.
 401 The scaled stresses are then converted back into the time domain and rainflow counted to
 402 determine the fatigue damage in the wind turbine structure.

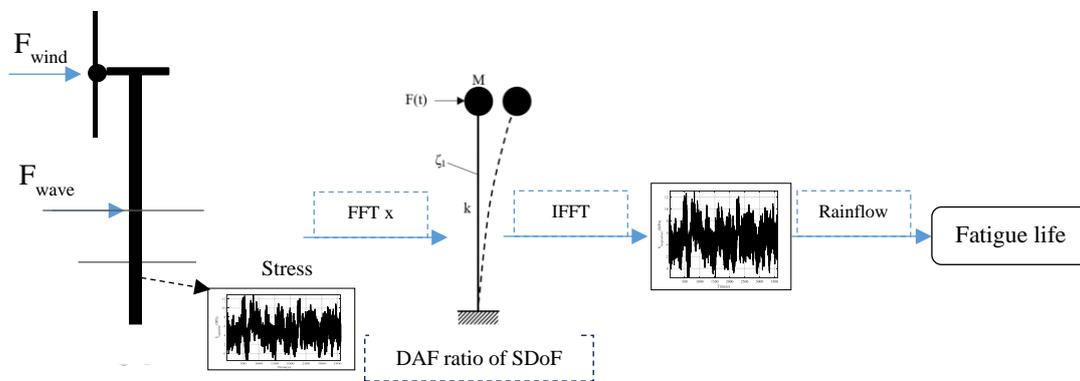


Figure 9. Schematic flow chart of the simplified fatigue analysis method.

403 The mass of the equivalent single degree of freedom system is the first modal mass (M_1) and
 404 the stiffness (k) was chosen so that the first natural frequency of the turbine (0.25 Hz) is
 405 identical to that of the SDoF system. The influence of damping was studied by choosing as a
 406 reference damping a mid-level value of $\zeta_l=7\%$ (comprising 5% aerodynamic and 2% structural,
 407 soil and hydrodynamic damping). To test the accuracy using the DAF of a SDoF instead of the
 408 actual transfer function, a set of idealised harmonic wind and wave loads with identical
 409 amplitudes of 0.5MN and frequencies $\Omega_1 = 0.2Hz$, $\Omega_2 = 0.25Hz$ and $\Omega_3 = 0.3Hz$ were
 410 applied in the time-domain with different damping levels. Subsequently, the steady-state
 411 portions of the maximum longitudinal stress in the monopile at 8m below seabed were
 412 compared for each force frequency. The stresses calculated using the DAF were compared to
 413 the stress time histories from the full time simulations. A close match was observed,

414 approximately within 1% for almost all damping values tested. Comparison of the fatigue life
 415 showed a maximum deviation of 2% between the approximate analysis and full simulations.
 416 To test the influence of the reference damping level, an alternative damping level of $\zeta_I=11\%$
 417 was selected as reference and the comparison of the stress ratios showed approximately 2%
 418 deviation. Thus, the selection of reference damping level is considered to have only a minor
 419 influence on this analysis.

420 Actual aerodynamic and hydrodynamic loads are stochastic with broadband frequency content.
 421 Using those as input, longitudinal stress time histories at the reference damping of $\zeta_I=7\%$ were
 422 obtained from the FE simulations for each ES, to obtain the fatigue damage. Figure 10
 423 compares the normalised damage contributions calculated using the simplified fatigue analysis
 424 with those from the time-domain analysis for the highest damping level of $\zeta_I=11\%$ (using 7%
 425 damping as reference). As can be seen, the normalised damage contributions obtained from the
 426 two methods show a close match, with a slight underestimation of the fatigue damage for some
 427 ES by up to 2% with the approximate method.

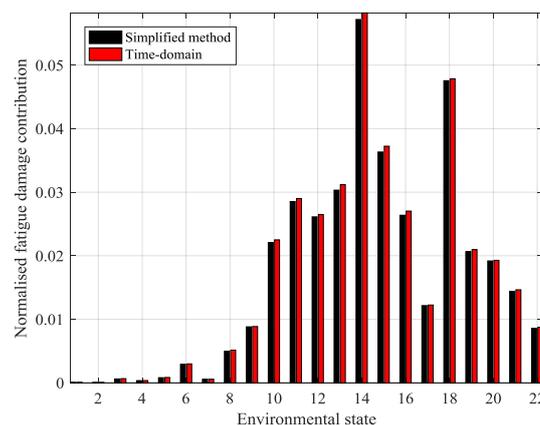


Figure 10. Comparison of the normalised damage contribution in the simplified fatigue analysis method with the time-domain results.

428 Figure 11 shows the fatigue lives predicted using the simplified method against those predicted
 429 using full time-domain simulations. As can be seen, the fatigue life predictions show a very
 430 good match with a largest difference of 2% for 11% damping. The hybrid time-domain

431 approach requires only a full time-domain analysis for one level of damping with little
432 additional computational effort, e.g., for the 6 damping levels shown in Fig. 11 the simulation
433 time was reduced by approximately 75%.

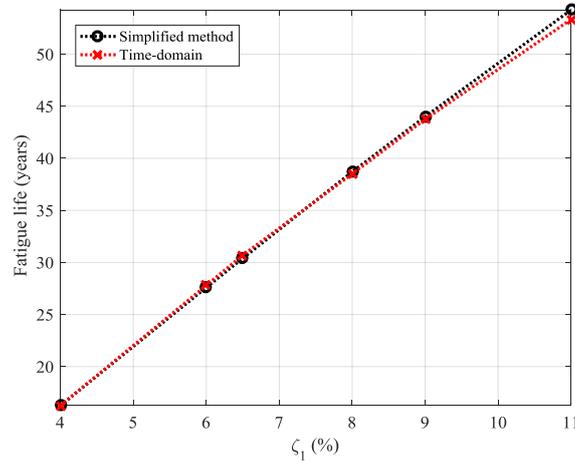


Figure 11. Fatigue life predictions from the simplified and the time-domain fatigue analyses of the wind turbine.

434 For the loads experienced at this intermediate water depth, the small differences found in the
435 fatigue life prediction show that dynamic amplification factors can be used to quickly assess
436 the influence of damping on the fatigue life of the wind turbine with good accuracy and little
437 extra effort. This can be particularly useful at a preliminary design stage.

438 **5 Conclusions**

439 The effects of damping on the fatigue life of an offshore wind turbine structure were
440 investigated systematically for the detailed FE model of a 5MW case study wind turbine.
441 Fatigue damage is mainly driven by the bending stresses caused by the vibrations due to wind
442 and wave loads. Assuming a constant average aerodynamic damping for all wind speeds was
443 found to lead to accurate fatigue life estimations compared to allowing aerodynamic damping
444 to vary with wind speeds. Normal or unforeseen shutdowns of the wind turbine during
445 operational environmental states can result in increased fatigue damage of up to 60%, as the
446 significant reduction in aerodynamic damping has a larger influence than the reduced loading.

447 Prolonged maintenance or shut-down periods could reduce the fatigue life to an unsafe level,
448 therefore this scenario should be included as part of the fatigue limit state analysis.

449 Moderate damping increases were shown to effectively reduce fatigue damage by up to 67%.
450 The predicted fatigue life of offshore wind turbines showed an almost linear increase with the
451 level of damping, from 16 years at 4% overall damping to 53 years at 11% damping. Therefore
452 significant cost-savings could be achieved in OWT design by incorporating damping devices
453 (e.g. tuned-mass-dampers), reducing the levelized electricity costs of the renewable energy
454 system. An approximate hybrid time-domain method was developed, significantly reducing the
455 computation time required to accurately assess the influence of damping on fatigue (requiring
456 only a full time-domain FE analysis for one level of damping with little additional
457 computational effort for other damping levels). In this paper, only unidirectional wind and
458 wave loads were considered. The consideration of the directionality of wave and wind loads
459 and their influence on fatigue life is recommended for further research.

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