

Computational Intelligence-Assisted Understanding of Nature-Inspired Superhydrophobic Behavior

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In recent years, state-of-the-art computational modeling of physical and chemical systems has shown itself to be an invaluable resource in the prediction of the properties and behavior of functional materials. However, construction of a useful computational model for novel systems in both academic and industrial contexts often requires a great depth of physicochemical theory and/or a wealth of empirical data, and a shortage in the availability of either frustrates the modeling process. In this work, computational intelligence is instead used, including artificial neural networks and evolutionary computation, to enhance our understanding of nature-inspired superhydrophobic behavior. The relationships between experimental parameters (water droplet volume, weight percentage of nanoparticles used in the synthesis of the polymer composite, and distance separating the superhydrophobic surface and the pendant water droplet in adhesive force measurements) and multiple objectives (water droplet contact angle, sliding angle, and adhesive force) are built and weighted. The obtained optimal parameters are consistent with the experimental observations. This new approach to materials modeling has great potential to be applied more generally to aid design, fabrication, and optimization for myriad functional materials.

1. Introduction

Superhydrophobic surfaces have attracted much attention from the scientific community and captured the imagination of the public due to their various useful applications including anti-corrosion,^[1] anti-icing,^[2] oil–water separation,^[3] and so on. Among these, self-cleaning is one of the most significant applications.^[4] The lotus leaf is an excellent example of a superhydrophobic surface found in nature, upon which water droplets will exist in a spherical form rather than wetting the leaf by spreading out or staining the surface of the leaf; when such superhydrophobic surfaces are tilted slightly, sessile water

droplets will roll off easily without leaving any trace of wetting, while the rolling motion of the droplet collects dirt from the surface, in such a way that lotus leaves can be described as “self-cleaning.”^[5] To achieve superhydrophobicity, the lotus leaf surface has micrometer-scale morphology combined with nanoscaled waxy fibrils to enable an extremely low affinity to water droplets.^[6] On such surfaces water droplets are able to bounce, and the contact time between bouncing water droplets and superhydrophobic surfaces becomes a key factor of their dynamic characterization.^[7] The water bouncing motion is well studied by physicists and the contact time can be further reduced by tuning the surface micromorphology and droplet Weber number to achieve “nonaxisymmetric bouncing,”^[8] “pancake bouncing,”^[9] and “sausage bouncing”^[10] of water droplets.

In the static characterization of superhydrophobic surfaces, the three most important measurements are water contact

angle (CA), sliding angle (SA), and adhesive force.^[11] As shown in Figure S1 (Supporting Information), imagining a side-on view of a superhydrophobic surface, a water droplet coming into contact with the solid surface creates an angle between the flat region of surface contact at the base of the droplet and a tangent drawn along the outer edge of the droplet at the point where liquid, solid, and air meet; this angle is widely identified as the water droplet contact angle and provides a quantifiable metric for the wettability of a solid substrate. Usually, a larger water contact angle correlates with a greater degree of superhydrophobicity.^[12] Meanwhile, the droplet sliding angle quantifies the mobility of a water droplet on a given surface, defined as

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the maximum angle at which a level surface can be tilted before a sessile water droplet will begin to slide.^[13] The sliding angle is also referred to as the rolling angle or tilting angle in some literature.^[14] Last, the water adhesive force defines the strength of interaction between a water droplet and a solid surface; it is measured at the instance when a water droplet separates from the surface, while the adhesive force is observed to vary with the distance that the droplet/substrate travels.^[15] To achieve self-cleaning, the water contact angle is expected to be larger than 150° to minimize wetting, while the sliding angle and the adhesive force ought to be as small as possible so that water droplets can easily roll off the surface.^[16]

The measurements of water contact angle, sliding angle, and adhesive force (the “objectives”) are generally considered standard characterization for a superhydrophobic surface. However, in practice the outcome of these measurements is subject to experimental variables such as the degree of nanostructure within the hierarchical surface morphology,^[17] water droplet volume, and the distance that the droplet or the surface travels when measuring the adhesive force (the “parameters”).^[18] For example, larger droplets are usually selected in sliding angle measurements for their ease of mobility, resulting in a smaller sliding angle; however, the details of the relationship between sliding angle and droplet size are not well understood, and it is unclear what effect a changing droplet size will have on the other objectives. Similar such uncertainties arise with the selection of parameters in the determination of the other objectives; increasing the degree of nanostructure reduces the contact angle, but what effect will this have on sliding angle or adhesive force? Complications arise in obtaining a conclusive characterization when all of said parameters and objectives are involved at the same time. It is observed that multiple experimental parameters tend to influence the determination of each objective, as such it is important to find out to what degree each parameter influences each objective, which parameter dominates in each instance and whether the experimental objectives conflict with each other. With limited experimental data and no analytical model available, approaching the problem using traditional mathematical tools presents difficulties.

Computational intelligence (CI), as a major branch of artificial intelligence, has been widely applied to solving complex real-world problems^[19] and designing functional materials in fields such as energy science^[20] and catalysis.^[21] Computational techniques which are constructed using in-depth physical and chemical theory are limited in their applicability to the wider design of other functional materials and processes where theory is cumbersome or less well-understood, such as superhydrophobic surfaces. In such instances, the adoption of nature-inspired CI where artificial neural networks and evolutionary algorithms enable location of optimal minima in multivariable systems has shown itself to be a promising alternative in solving global optimization problems.

In this work, SiO₂ nanoparticles and polyvinyl chloride (PVC) were used to prepare

biomimetic superhydrophobic surfaces with varying SiO₂ nanoparticle content. Water contact angle, sliding angle, and adhesive forces were measured on these surfaces with varying droplet volumes. Adoption of CI related techniques was sought in order to investigate the relationship between experimental parameters, such as water droplet size, weight percentage of nanoparticles in the polymer composite and distance moved by the substrate in the measurement of droplet adhesive force, and experimental objectives, such as water contact angle, sliding angle, and the droplet adhesive force. In the computational process, artificial neural networks and evolutionary computation were applied in analyzing the experimental data. The artificial neural networks are inspired by the biological neural networks within the brains of animals and have been widely applied to learning and prediction tasks,^[22] while the evolutionary computation is inspired by natural evolution and has been widely applied to optimization tasks.^[23] First, a computational model is formulated to demonstrate the relationship between the experimental parameters and objectives. Second, artificial neural networks are adopted in building the surrogate models to estimate the functional mapping between the experimental parameters and objectives. Finally, evolutionary computation carries out multiobjective optimization on those surrogate models, leading to an optimal set of solutions to the experiments. Potential conflicts between the experimental objectives are likewise sought via the evolutionary multiobjective optimization. This method does not require large data sets and could potentially be applied more broadly to aid in the design, fabrication, and optimization of myriad functional materials.

2. Results and Discussion

Superhydrophobic samples were prepared by introducing hydrophobic silica (SiO₂) nanoparticles into micrometer-structured PVC. The hydrophobic SiO₂ nanoparticles were obtained using a previously reported technique.^[24] The hydrophobic SiO₂ nanoparticles showed high repellence to water and water-based liquids, such as juice, milk, and coffee droplets as shown in Figure 1a–c. The dispersibility of these SiO₂ nanoparticles in

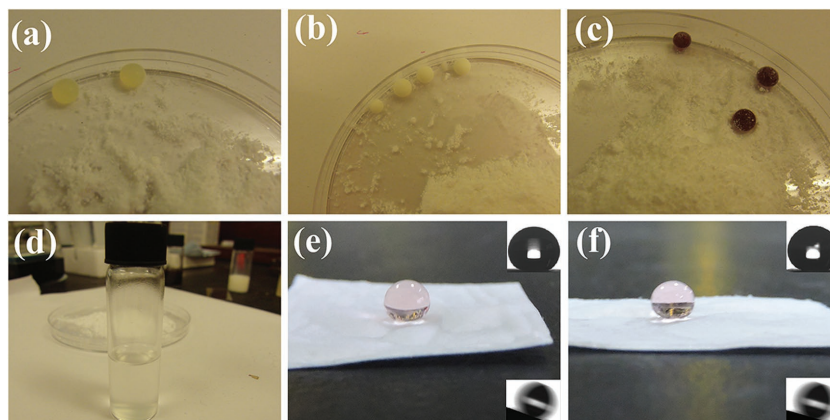


Figure 1. a) Juice, b) milk, and c) coffee droplets formed spheres on hydrophobic SiO₂ powder. d) SiO₂ powder dispersed in n-hexane solution. e, f) Sessile water droplet on superhydrophobic SiO₂/PVC surfaces: e) Sample S1; f) Sample S2, with inset contact angle (upper right) and sliding angle (lower right) measurements.

Table 1. The ratio of hydrophobic silica nanoparticles and PVC, defining Samples S1–S5. SiO_2 wt% = $m(\text{SiO}_2) / [m(\text{SiO}_2) + m(\text{PVC})] \times 100\%$.

Weight content	Sample 1 (S1)	Sample 2 (S2)	Sample 3 (S3)	Sample 4 (S4)	Sample 5 (S5)
PVC (/g)	1.2	1.1	1.0	0.9	0.8
SiO_2 (/g)	0.3	0.4	0.5	0.6	0.7
SiO_2 wt%	20%	26.7%	33.3%	40%	46.7%

organic media is illustrated in Figure 1d, in which the hydrophobic SiO_2 nanoparticles form a stable dispersion in n-hexane. The hydrophobic SiO_2 nanoparticles were then mixed with PVC at five different ratios as shown in Table 1, defining Samples S1–S5. The spherical form of water droplets on contact with Samples S1 and S2 is displayed in Figure 1e,f respectively. To create microscaled morphology, a lotus leaf was used as a template to transfer its micrometer structures onto the SiO_2 /PVC coatings as shown in Figure S2 (Supporting Information). Polydimethylsiloxane (PDMS) solution was poured onto a lotus leaf; after curing, the lotus leaf was removed leaving a negative topography on the PDMS template. The SiO_2 /PVC dispersion was poured onto the negative PDMS template; after the SiO_2 /PVC dispersion had dried, the PDMS was removed to yield the finished SiO_2 /PVC composite. Figure 2 shows the field emission scanning electron microscopy (FESEM) images of (a,b) the negative PDMS template and (c–h) the SiO_2 /PVC surfaces. It is evident that the microscopic structure of the lotus leaf was successfully transferred to the SiO_2 /PVC surfaces. Figure 2c–h compared the surface morphologies of Samples S1, S3, and S5; the micrometer structures on these samples are of the similar sizes as they all “copy” the same topographies from the lotus leaf. However, Samples S1, S3, and S5 show different ratios of nanoscaled structures due to the varying ratios of SiO_2 nanoparticles added to the PVC, where Sample S5 had the highest degree of nanoscaled structure (SiO_2 : 46.7 wt%) while Sample S1 had the least (SiO_2 : 20 wt%).

X-ray photoelectron spectroscopy (XPS) was employed to investigate the chemical composition of the samples as shown in Figure S3 (Supporting Information). Only Si, O, C, and Cl were detected indicating the purity of the obtained SiO_2 /PVC film. From Samples S1–S5, it is clear that the amount of Si increased with the increasing addition of SiO_2 nanoparticles.

To characterize the wettability of Samples S1–S5, CA and SA were measured using water droplets at different volumes. Figure 3a shows the plot of water contact angle as the droplet size increased for Samples S1–S5. The contact angle did not significantly change as the droplet size increased, while Sample S5 exhibited the highest contact angle correlating with the greatest addition of SiO_2 nanoparticles among the five samples. Figure 3b illustrates the relationship between sliding angles and water droplet size. The sliding angle decreased as the increase of water droplet volume from 2 to 10 μL . Sample S5 achieved the lowest sliding angle among the five samples for all droplet volumes. Therefore, Sample S5 is considered to be the most superhydrophobic among the five samples under the evaluation of water contact angles and sliding angles. However, the influence of SiO_2 nanoparticles and the droplet size on contact angle and sliding angle measurements has not been directly quantified.

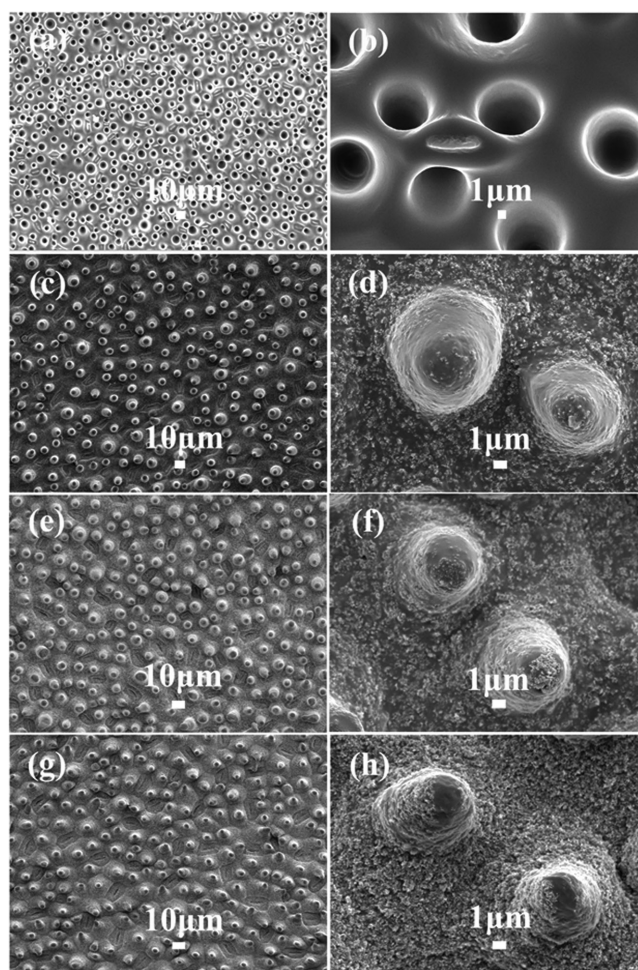


Figure 2. FESEM images of a,b) the obtained PDMS surface with negative biomimetic lotus topography and SiO_2 /PVC surface: c,d) Sample S1, e,f) Sample S3, and g,h) Sample S5.

To investigate the strength of interaction between water and the superhydrophobic coatings, a high-sensitivity microelectromechanical balance system was used to measure the adhesive force between the surfaces of Samples S1–S5 and water droplets with different volumes. As shown in Figure S4 (Supporting Information), the water droplet was suspended by a copper ring, and the samples were positioned onto a stage under the water droplet. In the measurements, the stage moved up toward the suspended droplet at a rate of 0.03 mm s^{-1} , then upon contact with the droplet, the stage moved downward at the same rate. Like so, the microelectromechanical balance collected data measuring the adhesive force of the droplet on the substrate. Figure 4 shows the adhesive force–distance curves for Samples S1–S5, respectively. Here, the distance refers to the travel distance of the stage. The force measurement process can be understood in three steps: in Step 1, there is zero adhesive force measured while the sample is moved upward toward the suspended droplet. The beginning of Step 2 is marked by the instance at which the droplet makes contact with the sample. During this step, samples on the stage were moved away from the

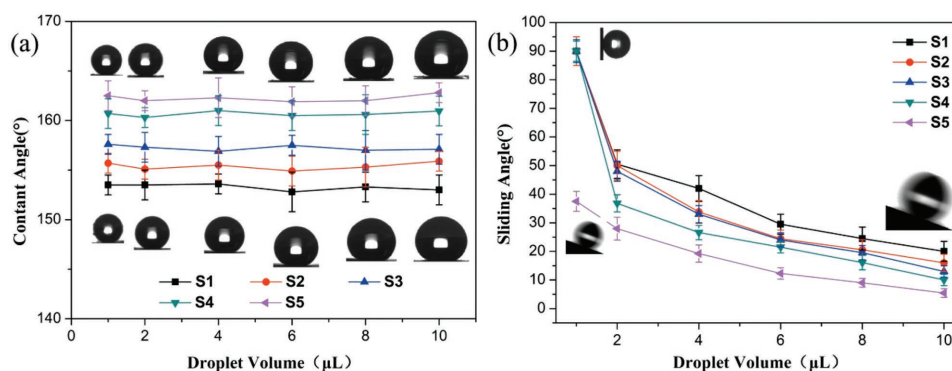


Figure 3. The relationship between water droplet volume and the a) contact angle and b) sliding angle for Samples S1–S5.

droplet, enabling the collection of adhesive force data. Step 3 is marked by the separation of the sample from the droplet, at which point the measured adhesive force drops to 0. It can be seen that a smaller droplet volume tended to yield a greater adhesive force. Figure 4f shows the relationship between adhesive force and droplet size for Samples S1–S5, where Sample S5 exhibited the lowest adhesive force at each droplet volume. However, illustrating the multidimensional relationship between droplet volume, distance moved by the substrate in the adhesive force measurement, quantity of SiO₂ nanoparticles incorporated into the polymer composite and the measured adhesive force is nontrivial, and optimization of this as well as other such multiparameter problems points toward assistance by CI techniques.

3. Computational Intelligence-Assisted Analyses

Although it has been shown possible to plot “one to one” relationships between objectives such as water droplet contact angle, sliding angle, adhesive force, and experimental parameters, such as the nanoparticle-to-polymer weight ratio in the synthesis, water droplet size, and force measurement distance, it is clear that the current approach encounters difficulty with quantifying the influence of each factor. In addition, when attempting to gauge the simultaneous effect of two or more parameters such as nanoparticle ratio and droplet size, using the current approach it is impossible to determine a weighted contribution from each parameter on an objective such as droplet sliding angle. Here, computational intelligence-assisted analysis was employed to understand the correlation between each experimental parameter and objective, based on data from the measurements carried out in Section 2. All computational analysis is performed in the Matlab software platform.

3.1. Problem Formulation

To achieve the best superhydrophobicity and self-cleaning ability, the objectives to be optimized are defined in the computation such that the maximum contact angle, minimum sliding

angle, and minimum adhesive force are obtained. The computational model is constructed as follows

$$\begin{cases} \max_{x_1, x_2} Y_1 = f_1(X_1, X_2) \\ \min_{x_1, x_2} Y_2 = f_2(X_1, X_2) \\ \min_{x_1, x_2, x_3} Y_3 = f_3(X_1, X_2, X_3) \end{cases} \quad (1)$$

where, as summarized in Table 2, Y_1 , Y_2 , and Y_3 , as the experimental objectives to be optimized, denote the contact angle, sliding angle, and adhesive force respectively, for which the functional mappings f_1 , f_2 , and f_3 are constructed using the input variables X_1 , X_2 , and X_3 , which represent the experimental parameters: nanoparticle-to-polymer weight percentage, water droplet volume, and distance travelled in the adhesive force measurement, respectively.

In order to quantify the correlations between the experimental parameters and objectives, namely X_1 , X_2 , X_3 , Y_1 , Y_2 , and Y_3 , statistical correlation analysis is performed on the experimental data obtained in Section 2. The correlation coefficient r_{xy} between any experimental parameter X and any experimental objective (or parameter) Y is calculated as

$$r_{xy} = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_{i=1}^n (x_i - \bar{x})^2 \sum_{i=1}^n (y_i - \bar{y})^2}} \quad (2)$$

where n is the number of experimental data points obtained in Section 2 for X and Y , while \bar{x} and \bar{y} are the mean values of X and Y , respectively. As a result, the three correlation matrices for the functional mappings f_1 , f_2 , and f_3 for the optimization of Y_1 , Y_2 , and Y_3 respectively are obtained

$$R_1 = \begin{bmatrix} 1 & 0 & 0.99 \\ 0 & 1 & 0.02 \\ 0.99 & 0.02 & 1 \end{bmatrix} \quad (3)$$

$$R_2 = \begin{bmatrix} 1 & 0 & -0.50 \\ 0 & 1 & -0.83 \\ -0.50 & -0.83 & 1 \end{bmatrix} \quad (4)$$

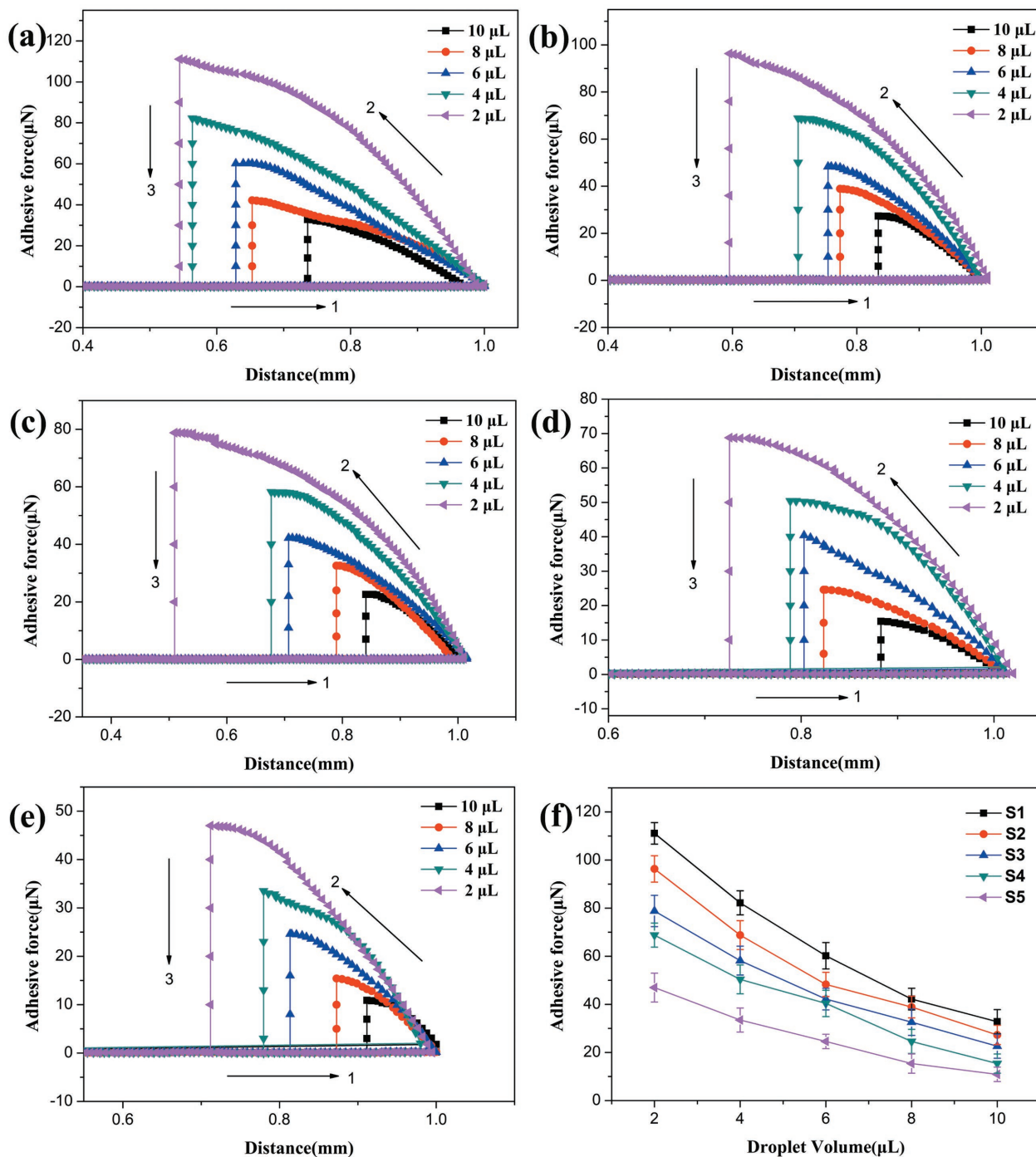


Figure 4. Adhesive force–distance curves with various water droplet volumes for Samples a) S1, b) S2, c) S3, d) S4, and e) S5. f) Adhesive force of water droplet on surface as a function of droplet volume.

$$R_3 = \begin{bmatrix} 1 & -0.05 & 0.27 & -0.30 \\ -0.05 & 1 & 0.34 & -0.58 \\ 0.27 & 0.34 & 1 & -0.88 \\ -0.30 & -0.58 & -0.88 & 1 \end{bmatrix} \quad (5)$$

where each element r_{ij} in R_k is either, when $i \leq j < D$ (with D denoting the size of the matrix), the correlation coefficient between experimental parameters X_i and X_j , or when $j = k$,

between the experimental parameter X_i and experimental objective Y_k .

According to R_1 , the correlation coefficient for X_1 and X_2 is 0, which means that those two experimental parameters, namely the weight percentage of SiO_2 in the polymer and the water droplet volume, are independent of each other, which means that adjusting one in an experiment should not affect measurements made in which the other is the measured variable.

Table 2. Symbols, denotations, and their scales in the problem formulation.

Symbol	Meaning	Range
X_1	Percentage of SiO ₂ in SiO ₂ /PVC mixture	20–46.7 wt%
X_2	Water droplet volume	2–10 μ L
X_3	Distance	0–1.0 mm
Y_1	Contact angle	$\leq 180^\circ$
Y_2	Sliding angle	0–90°
Y_3	Adhesive force	> 0 μ N

Another interesting observation is that nanoparticle quantity X_1 is also strongly positively correlated with the water droplet contact angle Y_1 , as indicated by the correlation coefficient 0.99, while the water droplet volume X_2 is virtually independent of its observed contact angle Y_1 , indicated by a correlation coefficient of 0.02.

Those experimental parameters X_1 and X_2 remain uncorrelated according to R_2 . By contrast, both X_1 and X_2 show negative correlations to the sliding angle Y_2 , indicated by the correlation coefficients of -0.50 and -0.83 , respectively.

While R_1 and R_2 involve only two experimental parameters, R_3 , which involves X_1 , X_2 , and X_3 , is more complicated. As indicated by the correlation coefficients of -0.30 , -0.58 , and -0.88 in R_3 , all of X_1 , X_2 , and X_3 are negatively correlated with the experimental objective Y_3 , namely, the adhesive force. This means that the measured adhesive force is changed by adjusting any of those three experimental parameters, while adjusting the distance moved has the most significant impact.

3.2. Artificial Neural Network-Based Surrogate Modeling

In order to obtain surrogate models for the functional mappings f_1 , f_2 , and f_3 , artificial neural networks were trained by the experimental data obtained in Section 2. As shown in Figure S5 (Supporting Information), the neural networks adopted for building the surrogate models for f_1 , f_2 , and f_3 are the classic two-layer feed-forward networks with sigmoid hidden neurons $S_{\text{sigmoid}}(z)$ and linear output neurons $S_{\text{linear}}(z)$ ^[25]

$$S_{\text{sigmoid}}(z) = \frac{1}{1 + e^{-z}} \quad (6)$$

$$S_{\text{linear}}(z) = z \quad (7)$$

where $z = \mathbf{w}\mathbf{x} + \mathbf{b}$ is the weight sum of the input \mathbf{x} , and \mathbf{w} and \mathbf{b} are known as the weight matrix and bias vector, respectively.

In order to train the neural networks as per Figure S5 (Supporting Information), the experimental data obtained in Section 2 is used as training data, and the Bayesian regularization is used as the training function. As shown in Figure S6 (Supporting Information), all three neural networks returned small training errors, indicating a high degree of accuracy for the regressions. For further assessment, functional mapping landscapes of f_1 and f_2 using the surrogate models obtained by the neural networks have been plotted in Figure 5. It can be observed that the correlations between X_1 , X_2 and f_1 , f_2 are consistent with the correlation analysis performed in Section 3.1. Using the surrogate models of f_1 , f_2 , and f_3 obtained by the neural networks, numerical optimization is performed to obtain the optimal experimental parameter settings in the following subsection.

3.3. Evolutionary Computation-Based Multiobjective Optimization

Since there are three objective functions f_1 , f_2 , and f_3 in the model formulated in Section 3.1, it is a typical multiobjective optimization problem,^[26] where there are more than one (conflicting) objectives to be optimized simultaneously.

In order to obtain solutions to such a problem, the evolutionary multiobjective optimization technique is applied.^[26] The state-of-the-art reference vector-guided evolutionary algorithm (RVEA)^[27] is employed, which has previously been successfully applied to other real-world applications such as the optimization of hybrid electric vehicle control.^[28]

As shown in Figure 6a, RVEA has obtained a number of “nondominated” solutions by optimizing the surrogate models from Section 3.2. There are two important observations to

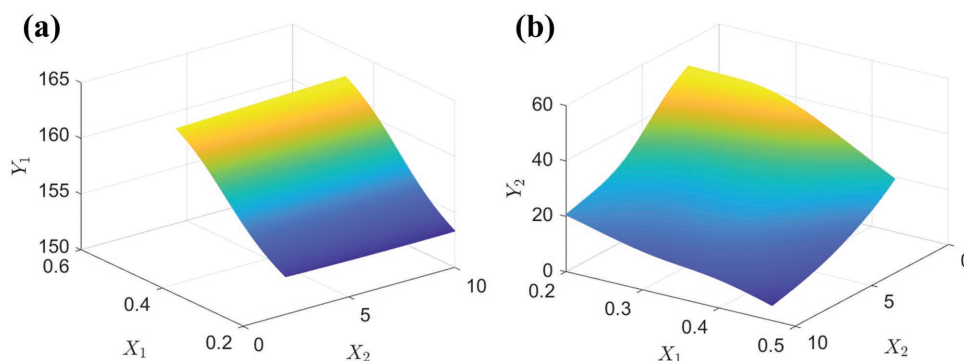


Figure 5. The functional mapping landscapes of a) f_1 and b) f_2 obtained by the surrogate models built by artificial neural networks. [X_1 , percentage of SiO₂ in SiO₂/PVC mixture (wt%); X_2 , water droplet volume (μ L); Y_1 , water contact angle ($^\circ$); Y_2 , sliding angle ($^\circ$)].

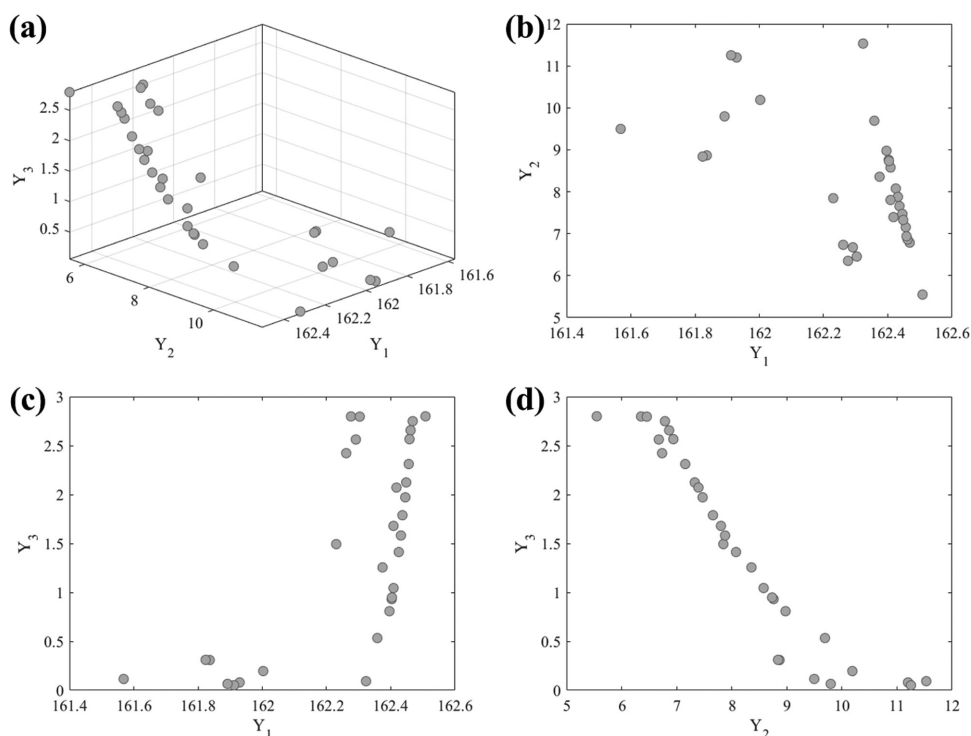


Figure 6. The final solution set obtained by optimising the surrogate models from Section 3.2 by using the state-of-the-art RVEA. [Y_1 , water contact angle ($^\circ$); Y_2 , sliding angle ($^\circ$); Y_3 , adhesive force (μN)].

make. First, as shown in Figure 6b,c, f_1 can be always optimized regardless of the specific values of f_2 and f_3 , resulting in an optimal value around $Y_1 = 162$, which means that the contact angle is independent from sliding angle or adhesive force. Second, as shown in Figure 6d, f_2 and f_3 are conflicting with each other since an optimum cannot be reached simultaneously, thus resulting in a set of trade-off solutions distributed in the range between $Y_2 \in (5, 12)$ and $Y_3 \in (0, 3)$, which means that the sliding angle and adhesive force are directly at odds and cannot coexist in a mutually optimal state. As such, the optimal experimental parameters obtained by RVEA are $X_1 \in (0.44, 0.47)$, $X_2 \in (8.2, 10)$, and $X_3 \approx 1$, which is consistent with the experimental results in Section 2. This yields a set of values which can be used to achieve the optimal synthesis and characterization of a superhydrophobic surface.

4. Conclusion

A lotus leaf was used as a template in patterning SiO_2/PVC coatings in order to make biomimetic superhydrophobic surfaces. The degree of nanoscaled structure was varied by the weight percentage of SiO_2 nanoparticles in the SiO_2/PVC mixture. Water droplet contact angles, sliding angles, and adhesive forces were measured on these superhydrophobic surfaces using droplets of various known volumes. Computational intelligence techniques including artificial neural networks and evolutionary computation were applied to analyze the relationship between experimental parameters (weight percentage of SiO_2 nanoparticles in the polymer, water droplet volume, and

distance between the pendant droplet and the superhydrophobic surface in adhesive force measurements) and experimental objectives (water droplet contact angle, sliding angle, and adhesive force). Within the parameter ranges investigated, the following conclusions can be drawn:

- [1] The percentage of hierarchical nanoscaled structure on the micrometer-scaled surface pattern is positively correlated with the water droplet contact angle, with a correlation coefficient as high as 0.99. This conclusion is widely in agreement with the literature.^[29]
- [2] The water droplet volume has virtually no bearing on its contact angle, with a correlation coefficient of 0.02. This suggests that any error in the droplet volume dispensed during contact angle measurements for a superhydrophobic material should not significantly influence the outcome of the measurement.
- [3] Both the percentage of nanoscaled structure incorporated into the polymer and the water droplet volume exhibit negative correlations with droplet sliding angles, with correlation coefficients of -0.50 and -0.83 , respectively. Of the two parameters, water droplet volume has the greater impact on its sliding angle.
- [4] The adhesive force of water droplets on the superhydrophobic materials is negatively correlated with all experimental parameters investigated, including the percentage of nanoscaled structure in the polymer, water droplet volume, and droplet-surface separation distance in the force measurements, with correlation coefficients of -0.30 , -0.58 , and -0.88 , respectively. The outcome of this observation is that the observed adhesive force can be varied by adjusting

any of those three experimental parameters, while the distance used in the measurement has the most significant impact on its outcome.

- [5] Water droplet contact angle is independent from its sliding angle or adhesive force.
- [6] Water droplet sliding angle and adhesive force are conflicting properties and cannot be optimized simultaneously.
- [7] To achieve the optimal synthesis and characterization of a superhydrophobic self-cleaning surface with the maximum water droplet contact angle, minimum droplet sliding angle and minimum adhesive force between the surface and the droplet, the quantity of SiO₂ nanoparticles used in the polymer composite should be between 44 and 47 wt%, droplet size should be between 8.2 and 10 μL and the separation distance used in the measurement of the adhesive force should be about 1.0 mm.

The use of artificial neural networks and evolutionary computation here does not require large sets of experimental data or any detailed physicochemical theoretical background in order to predict and optimize experiments, so that it can be generalized and broadly applied to tackle problems in other research fields and industrial processes. Computational networks and optimization can be further trained to enhance accuracy and expanded to encompass a wider numerical range for each variable and output (for example, increasing the droplet size investigated to 100 μL) when larger data sets are obtained and input into the system. This system has great potential to be generally applied to aid design, fabrication, and optimization for myriad functional materials.

5. Experimental Section

Preparation of Hydrophobic Silica Powder: Na₂SiO₃ was dissolved in DI water (50 mL) to form a 0.15 M solution (defined as Solution A). Then hydrochloric acid (25 mL, 0.18 M) was added into the stirred Solution A. After half of the hydrochloric acid had been added, hexamethyldisilazane (25 mL, 12.5×10^{-3} M) was added dropwise to Solution A together with the remaining hydrochloric acid. The resulting suspension was heated to 60 °C with stirring for 4 h. The suspension was separated into two phases upon cooling to room temperature, with white foam floating atop the liquid phase. The foam was purified by filtration and washed repeatedly using a solution containing DI water and ethanol until Cl⁻ could not be detected by silver nitrate solution by visual examination. The filter cake was redispersed into a solution containing DI water and ethanol at a volume ratio of 1:1 to form an emulsion. The emulsion was then spray dried and hydrophobic SiO₂ nanoparticles were obtained.

Fabrication of Biomimetic SiO₂/PVC Coatings: Lotus leaf was used as a template to fabricate hierarchical SiO₂/PVC surface comprising hierarchical micro- and nanoscaled structures, as shown in Figure S2 (Supporting Information). In order to first create a negative mould, PDMS precursors and cross-linking agent were mixed (10:1 weight ratio) and degassed in a desiccator at room temperature for ≈ 3 h to release air bubbles from the mixture. Then, the PDMS mixture was poured onto the lotus leaf templates. After curing at 70 °C for 10 h, the PDMS was solidified and then peeled off from the template, forming a negative replica of the lotus leaf template. The PDMS negative mould was then used to create the microstructure for the SiO₂/PVC composite, while the nanoscaled features were provided by the incorporated nanoparticles. In this process, SiO₂ powder and PVC were dispersed in tetrahydrofuran (10 mL) then the mixed solution was poured onto the PDMS negative template. After drying at room temperature, the PDMS template

was removed and thus the SiO₂/PVC superhydrophobic coating was obtained.

Characterization: The surface morphology of the sample was characterized by FESEM (JSM-6701F). XPS (Thermo Scientific ESCALAB 250Xi) was used to characterize the surface chemical compositions. Sessile water CA was acquired using a DSA-100 optical contact-angle meter (Kruss Company, Ltd, Germany) at room temperature (22 °C). The average CA value was determined by measuring the same sample at five different positions. SA was measured at five different positions on a sample to determine the average. The image of the water droplet on the surface was captured with a digital camera (NIKON, P600). The adhesive force was measured by a high-sensitivity microelectromechanical balance (Data- physics DCAT 11, Germany). A water drop was first suspended with a metal cap which was fixed to the balance, and the substrate was placed on the balance stage. The stage was moved upward at a constant speed of 0.03 mm s⁻¹, until the surface contacted the droplet. Then the stage was moved down. The water droplet was stretched from the spherical to the elliptical, and the force increased gradually up to maximum. When the surface broke away from the water droplet, the water droplet changed back to spherical and the force reduced down to zero quickly. The force when the droplet is just leaving, the surface is defined as the maximum adhesive force.

Supporting Information

Supporting Information is available from the Wiley Online Library or from the author.

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Conflict of Interest

The authors declare no conflict of interest.

Keywords

artificial neural networks, computational intelligence, evolutionary computation, superhydrophobic behavior

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- [1] a) T. Rezayi, M. H. Entezari, *Surf. Coat. Technol.* **2017**, 309, 795; b) E.-C. Cho, C.-W. Chang-Jian, H.-C. Chen, K.-S. Chuang, J.-H. Zheng, Y.-S. Hsiao, K.-C. Lee, J.-H. Huang, *Chem. Eng. J.* **2017**, 314, 347.
- [2] a) Y. Liu, X. Li, J. Jin, J. Liu, Y. Yan, Z. Han, L. Ren, *Appl. Surf. Sci.* **2017**, 400, 498; b) Y. Wang, J. Xue, Q. Wang, Q. Chen, J. Ding, *ACS Appl. Mater. Interfaces* **2013**, 5, 3370.
- [3] a) Z. Xue, S. Wang, L. Lin, L. Chen, M. Liu, L. Feng, L. Jiang, *Adv. Mater.* **2011**, 23, 4270; b) Y. Lu, S. Sathasivam, J. Song, F. Chen, W. Xu, C. J. Carmalt, I. P. Parkin, *J. Mater. Chem. A* **2014**, 2, 11628.

- [4] a) Y. Lu, S. Sathasivam, J. Song, C. R. Crick, C. J. Carmalt, I. P. Parkin, *Science* **2015**, 347, 1132; b) S. Sutha, S. Suresh, B. Raj, K. R. Ravi, *Sol. Energy Mater. Sol. Cells* **2017**, 165, 128; c) P. Wang, M. Chen, H. Han, X. Fan, Q. Liu, J. Wang, *J. Mater. Chem. A* **2016**, 4, 7869.
- [5] a) W. Barthlott, C. Neinhuis, *Planta* **1997**, 202, 1; b) I. P. Parkin, R. G. Palgrave, *J. Mater. Chem.* **2005**, 15, 1689.
- [6] a) T. Onda, S. Shibuichi, N. Satoh, K. Tsujii, *Langmuir* **1996**, 12, 2125; b) R. Nishimura, K. Hyodo, H. Sawaguchi, Y. Yamamoto, Y. Nonomura, H. Mayama, S. Yokojima, S. Nakamura, K. Uchida, *J. Am. Chem. Soc.* **2016**, 138, 10299.
- [7] a) C. Hao, Y. Liu, X. Chen, J. Li, M. Zhang, Y. Zhao, Z. Wang, *Small* **2016**, 12, 1825; b) Y. Lu, S. Sathasivam, J. Song, W. Xu, C. J. Carmalt, I. P. Parkin, *J. Mater. Chem. A* **2014**, 2, 12177; c) D. Richard, C. Clanet, D. Quéré, *Nature* **2002**, 417, 811.
- [8] J. C. Bird, R. Dhiman, H.-M. Kwon, K. K. Varanasi, *Nature* **2013**, 503, 385.
- [9] a) Y. Liu, L. Moevius, X. Xu, T. Qian, J. M. Yeomans, Z. Wang, *Nat. Phys.* **2014**, 10, 515; b) J. Song, M. Gao, C. Zhao, Y. Lu, L. Huang, X. Liu, C. J. Carmalt, X. Deng, I. P. Parkin, *ACS Nano* **2017**, 11, 9259.
- [10] Y. Liu, M. Andrew, J. Li, J. M. Yeomans, Z. Wang, *Nat. Commun.* **2015**, 6, 10034.
- [11] a) Y. C. Jung, B. Bhushan, *Nanotechnology* **2006**, 17, 4970; b) S. Wang, Y. Li, X. Fei, M. Sun, C. Zhang, Y. Li, Q. Yang, X. Hong, *J. Colloid Interface Sci.* **2011**, 359, 380.
- [12] a) T. Young, *Philos. Trans. R. Soc. London* **1805**, 95, 65; b) R. Wang, K. Hashimoto, A. Fujishima, M. Chikuni, E. Kojima, A. Kitamura, M. Shimohigoshi, T. Watanabe, *Nature* **1997**, 388, 431.
- [13] L. Feng, S. Li, Y. Li, H. Li, L. Zhang, J. Zhai, Y. Song, B. Liu, L. Jiang, D. Zhu, *Adv. Mater.* **2002**, 14, 1857.
- [14] a) K. Koch, B. Bhushan, Y. C. Jung, W. Barthlott, *Soft Matter* **2009**, 5, 1386; b) W. Ming, D. Wu, R. van Benthem, G. De With, *Nano Lett.* **2005**, 5, 2298.
- [15] a) M. Liu, L. Jiang, *Adv. Funct. Mater.* **2010**, 20, 3753; b) Z. Cheng, M. Du, H. Lai, N. Zhang, K. Sun, *Nanoscale* **2013**, 5, 2776; c) M. Jin, X. Feng, L. Feng, T. Sun, J. Zhai, T. Li, L. Jiang, *Adv. Mater.* **2005**, 17, 1977.
- [16] a) I. Sas, R. E. Gorga, J. A. Joines, K. A. Thoney, *J. Polym. Sci., Part B: Polym. Phys.* **2012**, 50, 824; b) O.-U. Nimitrakoolchai, S. Supothina, *J. Eur. Ceram. Soc.* **2008**, 28, 947.
- [17] Y. Su, B. Ji, K. Zhang, H. Gao, Y. Huang, K. Hwang, *Langmuir* **2010**, 26, 4984.
- [18] S. Ma, Q. Ye, X. Pei, D. Wang, F. Zhou, *Adv. Mater. Interfaces* **2015**, 2, 1500257.
- [19] a) A. P. Engelbrecht, *Computational Intelligence: An Introduction*, John Wiley & Sons, West Sussex, England **2007**; b) R. Kruse, C. Borgelt, C. Braune, S. Mostaghim, M. Steinbrecher, *Computational Intelligence: A Methodological Introduction*, Springer, London **2016**.
- [20] G. He, X. Han, R. Zou, T. Zhao, Z. Weng, S. Ho-Kimura, Y. Lu, H. Wang, Z. X. Guo, I. P. Parkin, *Adv. Funct. Mater.* **2017**, 27, 1604903.
- [21] a) B. Zhang, X. Zheng, O. Voznyy, R. Comin, M. Bajdich, M. García-Melchor, L. Han, J. Xu, M. Liu, L. Zheng, *Science* **2016**, 352, 333; b) C. Sotelo-Vazquez, R. Quesada-Cabrera, M. Ling, D. O. Scanlon, A. Kafizas, P. K. Thakur, T.-L. Lee, A. Taylor, G. W. Watson, R. G. Palgrave, J. R. Durrant, C. S. Blackman, I. P. Parkin, *Adv. Funct. Mater.* **2017**, 27, 1605413.
- [22] a) H. B. Demuth, M. H. Beale, O. De Jess, M. T. Hagan, *Neural Network Design*, Martin Hagan, USA **2014**; b) Y. LeCun, Y. Bengio, G. Hinton, *Nature* **2015**, 521, 436.
- [23] a) D. B. Fogel, *Evolutionary Computation: Toward a New Philosophy of Machine Intelligence*, John Wiley & Sons, Hoboken, NJ **2006**; b) A. E. Eiben, J. Smith, *Nature* **2015**, 521, 476.
- [24] D. Zhi, Y. Lu, S. Sathasivam, I. P. Parkin, X. Zhang, *J. Mater. Chem. A* **2017**, 5, 10622.
- [25] D. Svozil, V. Kvasnicka, J. Pospichal, *Chemom. Intell. Lab. Syst.* **1997**, 39, 43.
- [26] K. Miettinen, *Nonlinear Multiobjective Optimization*, Springer Science & Business Media, New York **2012**.
- [27] R. Cheng, Y. Jin, M. Olhofer, B. Sendhoff, *IEEE Trans. Evol. Comput.* **2016**, 20, 773.
- [28] R. Cheng, T. Rodemann, M. Fischer, M. Olhofer, Y. Jin, *IEEE Trans. Emerging Top. Comput. Intell.* **2017**, 1, 97.
- [29] M. Miwa, A. Nakajima, A. Fujishima, K. Hashimoto, T. Watanabe, *Langmuir* **2000**, 16, 5754.