



Enhanced sensitivity to a possible variation of the proton-to-electron mass ratio in ammonia

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Numerous accidental near degeneracies exist between the $2\nu_2$ and ν_4 rotation-vibration energy levels of ammonia. Transitions between these two states possess significantly enhanced sensitivity to a possible variation of the proton-to-electron mass ratio μ . Using a robust variational approach to determine the mass sensitivity of the energy levels along with accurate experimental values for the energies, sensitivity coefficients have been calculated for over 350 microwave, submillimeter, and far-infrared transitions up to $J=15$ for $^{14}\text{NH}_3$. The sensitivities are the largest found in ammonia to date. One particular transition, although extremely weak, has a sensitivity of $T = -16\,738$ and illustrates the huge enhancement that can occur between close-lying energy levels. More promising however are a set of previously measured transitions with $T = -32$ to 28 . Given the astrophysical importance of ammonia, the sensitivities presented here confirm that $^{14}\text{NH}_3$ can be used exclusively to constrain a spatial or temporal variation of μ . Thus certain systematic errors which affect the ammonia method can be eliminated. For all transitions analyzed we provide frequency data and Einstein A coefficients to guide future laboratory and astronomical observations.

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I. INTRODUCTION

Molecules are an attractive testing ground for probing two particular dimensionless fundamental constants. Electronic transitions are sensitive to the fine-structure constant α , whilst vibration, rotation, and inversion transitions are sensitive to the proton-to-electron mass ratio $\mu = m_p/m_e$. If any variation did exist it would manifest as observable shifts in the transition frequencies of certain molecular species. Such shifts can be detected by high-precision laboratory experiments over short time scales (years), or from astronomical observation of spectral lines at high redshift. The idea that the fundamental constants of nature may be understood within the framework of a deeper cosmological theory dates back to Dirac [1]. As of yet there is no theoretical justification for the values they assume, or even if they have always had the same values that we measure today.

Research in the field has become more active after claims of a temporal variation in the fine-structure constant, where observations of atomic absorption spectra of distant quasars suggested that α was smaller in the past [2]. A few years later, measurements of H_2 spectra indicated that the proton-to-electron mass ratio was larger by 0.002% up to twelve billion years ago [3]. Numerous studies have followed and these have all produced null results (see Ref. [4] for a detailed review). Any cosmological variation in the fundamental constants would require new physics beyond the standard model and, as such, results are received with caution and must be confirmed, or refuted, with independent studies on different atomic and molecular absorbers.

Ammonia has a large number of rotation-vibration transitions which are particularly sensitive to the proton-to-electron mass ratio [5–7]. The sensitivity coefficient,

$$T_{u,l} = \frac{\mu}{E_u - E_l} \left(\frac{dE_u}{d\mu} - \frac{dE_l}{d\mu} \right), \quad (1)$$

where E_u and E_l is the energy of the upper and lower state, respectively, quantifies the effect that a possible variation of μ would have for a given transition. It is related to the frequency shift of the probed transition through the expression

$$\frac{\Delta\nu}{\nu_0} = T_{u,l} \frac{\Delta\mu}{\mu_0}, \quad (2)$$

where $\Delta\nu = \nu_{\text{obs}} - \nu_0$ is the change in the frequency and $\Delta\mu = \mu_{\text{obs}} - \mu_0$ is the change in μ , both with respect to their present day values ν_0 and μ_0 .

The ammonia method [8] (adapted from van Veldhoven *et al.* [9]) compares inversion transitions in the vibrational ground state of $^{14}\text{NH}_3$ (henceforth referred to as NH_3) with rotational lines from other molecular species. By employing this approach several constraints on a temporal variation of μ have been established from measurements of the object B0218 + 357 at redshift $z \sim 0.685$ [8,10,11], and from the lensing galaxy PKS1830–211 at $z \sim 0.886$ [12]. However, the reliance on other reference molecules, particularly those which are non-nitrogen bearing, is a major source of systematic error (see Refs. [10–12] for a detailed discussion).

Methanol is now preferred because not only is it astrophysically abundant, but it can be used exclusively to place limits on a drifting μ [13–18], circumventing the errors which arise from comparing different molecular species. The most robust constraint to date measured CH_3OH absorption lines in the system PKS1830–211 [18]. The three observed transitions possessed sensitivities ranging from $T = -1.0$

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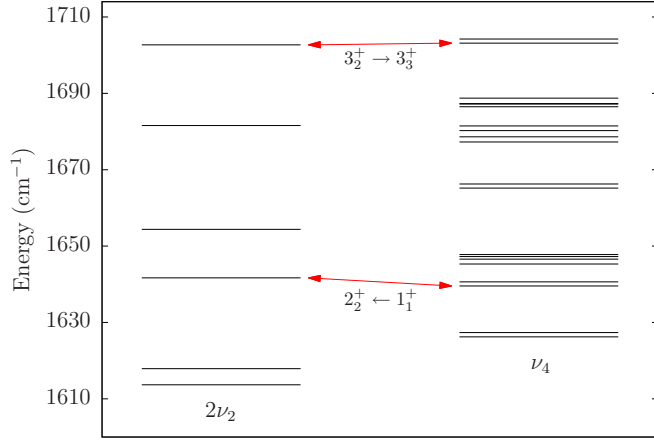


FIG. 1. Accidental near degeneracies between the $2\nu_2$ and ν_4 rotation-vibration energy levels of ammonia. Energy levels are labeled as J_K^\pm . For illustrative purposes only part of the rovibrational manifold is shown.

to -7.4 and were computed using an effective Hamiltonian model [13,19], by far the most common approach used for calculating sensitivity coefficients.

Despite being superseded by methanol, a comprehensive study of $^{14}\text{NH}_3$, $^{15}\text{NH}_3$, $^{14}\text{ND}_3$, and $^{15}\text{ND}_3$ [7] offered perspectives for the development of the ammonia method. Inversion transitions in the ν_4 vibrational state had sensitivities from $T = -4.27$ to 4.67 , whilst the $^{14}\text{NH}_3$ astronomically observed $2_1^+ \leftarrow 1_1^-$ and $0_0^- \leftarrow 1_0^+$ transitions in the ν_2 state [20,21] possessed values of $T = 17.24$ and $T = -6.59$, respectively. Here states are labeled as J_K^\pm , where J is the rotational quantum number, K is the projection onto the molecule-fixed z axis, and \pm denotes the parity of the state. Because of the abundance of NH_3 throughout the Universe and the ease with which its spectrum can be observed, identifying more transitions with large sensitivities in the microwave, submillimeter or far-infrared regions could lead to a much tighter constraint on μ .

A recent analysis of 56 sources of high-resolution $^{14}\text{NH}_3$ spectra utilizing the MARVEL procedure determined 4961 rovibrational energy levels of experimental quality, all labeled using a consistent set of quantum numbers [22]. This has allowed us to investigate transitions of NH_3 and accurately calculate their sensitivity to a possible variation of μ . As shown in Fig. 1, numerous accidental near degeneracies occur between the $2\nu_2$ and ν_4 rovibrational energy levels of ammonia. The strong Coriolis interaction between these two states [23] can give rise to highly anomalous sensitivities. Furthermore, a large number of transitions between these levels have been measured experimentally [24,25].

II. VARIATIONAL APPROACH

To compute sensitivity coefficients the dependence on μ of the energy levels is required, i.e., the derivatives in Eq. (1). Under the assumption that all baryonic matter may be treated equally [26], μ is assumed to be proportional to the molecular mass and it is sufficient to simply compute the mass dependence of the desired energy levels. The variational

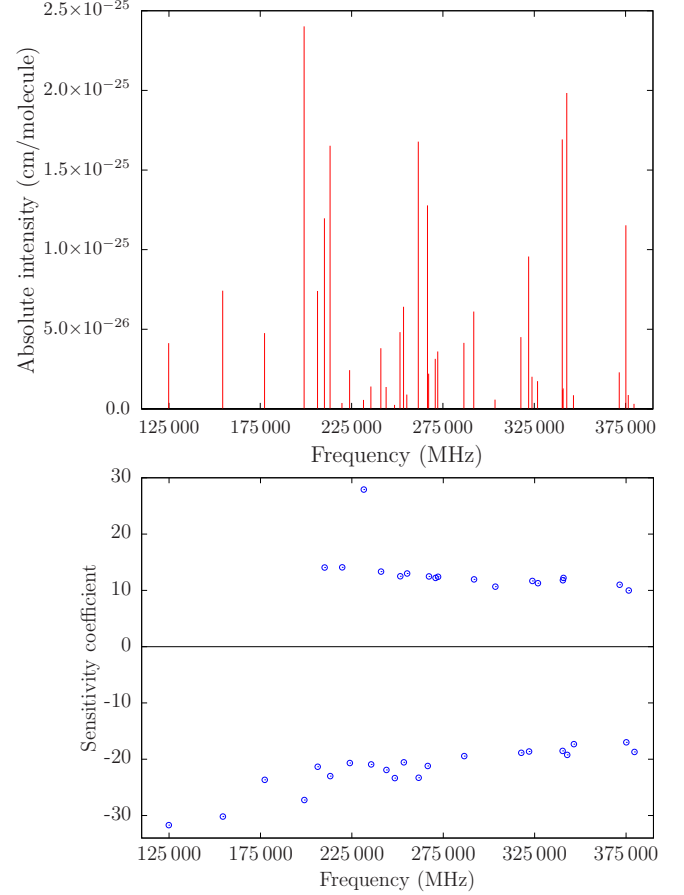


FIG. 2. Observed frequencies [24,25] and simulated intensities at temperature $T = 296$ K (top panel) with the corresponding sensitivities (bottom panel) for transitions between the $2\nu_2$ and ν_4 vibrational states of NH_3 .

approach we employ here is identical to our previous study of ammonia and we refer the reader to Ref. [7] (and references therein) for a detailed description. In short, a series of calculations are performed employing a scaled value for the mass of NH_3 , from which numerical values of the derivatives $dE/d\mu$ are obtained by finite differences. After matching the derivatives with the experimentally determined energy levels from the MARVEL analysis, sensitivities are calculated through Eq. (1). We also compute Einstein A coefficients to determine which transitions could realistically be detected. All calculations were carried out with the nuclear motion program TROVE [27]. Note that sensitivities have been computed for H_3O^+ and D_3O^+ [28] using exactly the same approach.

III. RESULTS AND DISCUSSION

In Fig. 2 we have simulated the intensities at room temperature for 38 previously observed transitions from Refs. [24,25] and plotted their corresponding sensitivity coefficients. The largest difference in sensitivity is $\Delta T = 59.6$, which is over nine times more sensitive than the ΔT of the methanol lines used to establish the most robust constraint to date [18], and over seventeen times larger than the ΔT of the transitions utilized in the ammonia method [8]. As well as being

consistently large, the mixture of positive and negative sensitivities is highly beneficial for detecting a change in μ as transitions are shifted in opposing directions. From Fig. 2, one could imagine scanning this frequency window at two separate instances in time to produce a displaced spectrum if any variation of μ had occurred. In addition to the frequencies of Refs. [24,25], there are 153 transitions with similar Einstein A coefficients and sensitivities from $T = -32.40$ to 17.27 in the frequency range 100 to 900 GHz. We provide comprehensive tables of all investigated transitions as Supplemental Material [29].

The accuracy of the calculated sensitivity coefficients depends on the MARVEL energy levels and the computed TROVE numerical derivatives. The MARVEL analysis offers a rigorous evaluation of high-resolution NH_3 spectra. The $2\nu_2$ energy levels have an average error of 0.0027 cm^{-1} for the 251 levels up to $J = 15$, whilst a similar uncertainty of 0.0026 cm^{-1} is given for the 495 ν_4 energies. As such, the error on the predicted sensitivities is significantly reduced by replacing the computed TROVE energy levels with the corresponding MARVEL values in Eq. (1). This is not to say that the TROVE frequencies are unreliable. As part of the MARVEL procedure the derived experimental energy levels are checked against theoretical predictions using the same potential energy surface (PES) and computational setup [30] as utilized for the present study. This PES is based on extensive high-level *ab initio* calculations [31] and has subsequently been refined to experimental data up to $J \leq 8$ [32]. If we calculate sensitivity coefficients for the 38 transitions shown in Fig. 2 without replacing the energies, the TROVE sensitivities differ on average by 2.5% to the MARVEL substituted sensitivities, the largest difference being 5.5%. Likewise for the additional 153 transitions with similar Einstein A coefficients, the TROVE sensitivities deviate on average by 2.1%. Such small differences reflect the quality of the underlying PES.

However, the variational approach cannot account exactly for all near degeneracies in the $2\nu_2$ and ν_4 rovibrational manifold. A striking example of this is for the extremely weak $5_3^+(\nu_4) \leftarrow 5_2^+(2\nu_2)$ transition. A computed frequency of $\nu_{\text{calc}} = 3540.5 \text{ MHz}$ has a sensitivity of $T_{\text{calc}} = -1843.25$, already the largest known sensitivity coefficient for ammonia. Replacing with MARVEL energy levels gives $\nu_{\text{expt}} = 389.9 \text{ MHz}$ and $T_{\text{expt}} = -16737.52$. The dramatic increase in magnitude occurs because of the inverse dependence on transition frequency [see Eq. (1)] and illustrates the huge enhancement that can happen between close-lying energy levels. Given the difference in predicted sensitivities one could question whether the computed numerical derivatives are still reliable. The change in frequency is just over 3000 MHz ($\approx 0.1 \text{ cm}^{-1}$) so one would expect that they are reasonable. The difficulty is that quantifying the uncertainty of the numerical derivatives is not as straightforward because there are no analogous highly accurate experimental quantities.

To investigate the error of the computed derivatives, sensitivity coefficients were calculated using a purely *ab initio* PES [31]. One can hope to establish a relationship between the difference in $\nu = E_u - E_l$, with the difference in the quantity $dE_u/d\mu - dE_l/d\mu$, by comparing values computed using this and the empirically refined PESs. Whilst no clear general correspondence between the uncertainty on

TABLE I. Highly sensitive weak transitions between the $2\nu_2$ and ν_4 vibrational states of NH_3 . All transitions are of symmetry $E' \leftarrow E''$. Experimental frequencies have been obtained using energy levels from the MARVEL analysis [22].

$\nu' \leftarrow \nu''$	$J_K^{\pm'}$ \leftarrow $J_K^{\pm''}$	ν_{expt} (MHz)	A (s^{-1})	T
$2\nu_2 \leftarrow \nu_4$	$2_2^+ \leftarrow 1_1^+$	61 712.7	1.042×10^{-8}	107.95
$\nu_4 \leftarrow 2\nu_2$	$7_3^- \leftarrow 7_1^+$	110 957.2	9.461×10^{-8}	-54.08
$\nu_4 \leftarrow 2\nu_2$	$10_2^+ \leftarrow 10_1^+$	123 427.8	4.745×10^{-7}	-44.11
$\nu_4 \leftarrow 2\nu_2$	$6_3^- \leftarrow 6_1^+$	169 341.3	2.539×10^{-8}	-37.57

these two quantities emerges, for near-coinciding energy levels separated by 1 cm^{-1} or less, the percentage difference in $dE_u/d\mu - dE_l/d\mu$ is always smaller than the percentage difference in ν . This ranges from 3 to 4 times smaller to several orders of magnitude smaller and suggests that, for extremely close-lying energy levels, the underlying numerical derivatives are relatively stable. Thus the huge amplification in sensitivity we predict is a result of replacing the theoretical frequencies with experimental values.

For the transitions shown in Fig. 2 and those with similar Einstein A coefficients, there is consistent agreement between the TROVE and MARVEL substituted sensitivities and errors in the computed derivatives will be negligible. When the two predictions differ significantly, which occurs for a number of weaker transitions with incredibly large sensitivities ranging from $T = -712.84$ to 509.21 (see Supplemental Material [29]), we are confident that the MARVEL substituted sensitivity coefficients are reliable. In all instances the residual between experiment and computed transition frequency never exceeds 1 cm^{-1} (regarded as spectroscopic accuracy).

IV. OUTLOOK

Finally, we briefly comment on possible experimental tests of our predictions. There are now techniques to produce ultra-cold polyatomic molecules [33], which have rich spectra well suited for testing fundamental physics. Already experiments

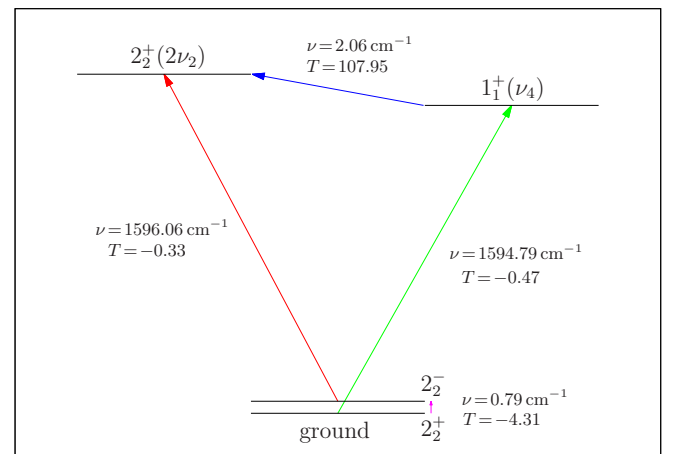


FIG. 3. Use of combination differences involving infrared transitions from the ground vibrational state to the $2\nu_2$ and ν_4 vibrational states of ammonia. Energy levels are labeled as J_K^{\pm} .

TABLE II. Astronomically relevant transitions between the $2\nu_2$ and ν_4 vibrational states of NH_3 . For symmetry of transitions, see Supplemental Material [29]. Experimental frequencies from Refs. [24,25] or obtained using energy levels from the MARVEL analysis [22].

$\nu' \leftarrow \nu''$	$J_K^{\pm'} \leftarrow J_K^{\pm''}$	ν_{expt} (MHz)	A (s^{-1})	T
$\nu_4 \leftarrow 2\nu_2$	$0_0^+ \leftarrow 1_1^+$	379 596.5	4.703×10^{-6}	-18.70
$\nu_4 \leftarrow 2\nu_2$	$1_1^+ \leftarrow 1_0^+$	824 624.2	6.427×10^{-5}	-9.13
$2\nu_2 \leftarrow \nu_4$	$2_1^+ \leftarrow 1_0^+$	231 528.2	1.180×10^{-6}	27.91
$\nu_4 \leftarrow 2\nu_2$	$2_2^+ \leftarrow 2_1^+$	687 852.5	6.318×10^{-5}	-10.70
$2\nu_2 \leftarrow \nu_4$	$3_3^+ \leftarrow 2_2^+$	489 672.2	4.360×10^{-6}	12.72
$\nu_4 \leftarrow 2\nu_2$	$3_3^+ \leftarrow 3_2^+$	557 275.3	7.623×10^{-5}	-12.87
$2\nu_2 \leftarrow \nu_4$	$3_2^+ \leftarrow 2_1^+$	672 644.4	3.223×10^{-5}	8.89
$\nu_4 \leftarrow 2\nu_2$	$3_2^+ \leftarrow 3_1^+$	679 163.4	6.964×10^{-5}	-10.79
$\nu_4 \leftarrow 2\nu_2$	$3_1^+ \leftarrow 3_0^+$	774 889.5	4.660×10^{-5}	-9.59
$2\nu_2 \leftarrow \nu_4$	$3_1^+ \leftarrow 2_0^+$	842 667.6	1.210×10^{-4}	6.91
$\nu_4 \leftarrow 2\nu_2$	$4_4^+ \leftarrow 4_3^+$	441 874.1	7.796×10^{-5}	-15.68
$\nu_4 \leftarrow 2\nu_2$	$4_3^+ \leftarrow 4_2^+$	548 781.8	9.102×10^{-5}	-12.94
$\nu_4 \leftarrow 2\nu_2$	$4_2^+ \leftarrow 4_1^+$	657 787.0	6.078×10^{-5}	-11.07
$\nu_4 \leftarrow 2\nu_2$	$5_5^+ \leftarrow 5_4^+$	342 797.1	7.054×10^{-5}	-19.22
$\nu_4 \leftarrow 2\nu_2$	$5_4^+ \leftarrow 5_3^+$	434 941.1	9.782×10^{-5}	-15.59
$\nu_4 \leftarrow 2\nu_2$	$5_3^+ \leftarrow 5_2^+$	527 333.3	8.219×10^{-5}	-13.31
$\nu_4 \leftarrow 2\nu_2$	$5_2^+ \leftarrow 5_1^+$	618 776.8	4.583×10^{-5}	-11.66
$\nu_4 \leftarrow 2\nu_2$	$5_1^+ \leftarrow 5_0^+$	672 376.5	2.542×10^{-5}	-10.86
$\nu_4 \leftarrow 2\nu_2$	$6_6^+ \leftarrow 6_5^+$	261 535.4	5.745×10^{-5}	-23.29
$\nu_4 \leftarrow 2\nu_2$	$6_5^+ \leftarrow 6_4^+$	340 322.9	9.137×10^{-5}	-18.52
$\nu_4 \leftarrow 2\nu_2$	$6_4^+ \leftarrow 6_3^+$	413 748.1	9.006×10^{-5}	-15.98
$\nu_4 \leftarrow 2\nu_2$	$6_3^+ \leftarrow 6_2^+$	488 661.3	6.308×10^{-5}	-14.12
$\nu_4 \leftarrow 2\nu_2$	$6_2^+ \leftarrow 6_1^+$	559 214.0	3.027×10^{-5}	-12.73
$\nu_4 \leftarrow 2\nu_2$	$7_7^+ \leftarrow 7_6^+$	198 997.4	4.284×10^{-5}	-27.24
$\nu_4 \leftarrow 2\nu_2$	$7_6^+ \leftarrow 7_5^+$	266 541.0	7.700×10^{-5}	-21.20
$\nu_4 \leftarrow 2\nu_2$	$7_5^+ \leftarrow 7_4^+$	321 935.0	8.437×10^{-5}	-18.62
$\nu_4 \leftarrow 2\nu_2$	$7_4^+ \leftarrow 7_3^+$	375 174.5	6.887×10^{-5}	-16.99
$\nu_4 \leftarrow 2\nu_2$	$7_3^+ \leftarrow 7_2^+$	430 468.6	4.113×10^{-5}	-15.29
$\nu_4 \leftarrow 2\nu_2$	$8_8^+ \leftarrow 8_7^+$	154 415.5	3.036×10^{-5}	-30.19

which decelerate, cool, and trap ammonia molecules are being developed to probe a temporal variation of μ [9,34–37]. In Table I we list several highly sensitive transitions which, despite being around two orders of magnitude weaker than the lowest intensity lines displayed in Fig. 2, could possibly be detected in such high-precision studies.

If the transitions in Table I are too weak to be detected directly, the use of combination differences involving

infrared transitions from the ground vibrational state to the $2\nu_2$ and ν_4 vibrational states should be considered. This technique would apply to any two levels provided transitions from a common ground state level can be identified, or for a situation such as that depicted in Fig. 3. Infrared transitions to the respective levels of the $2_2^+(2\nu_2) \leftarrow 1_1^+(\nu_4)$ transition (sensitivity of $T = 107.95$) have been measured experimentally [25], whilst the corresponding ground state pure inversion frequency is well known [38]. Combination differences could be utilized to determine a possible shift in these energy levels provided the sensitivities of the three involved transitions are also known. The large number of potential combination differences prohibits us from carrying out a rigorous evaluation of all possible transitions. However, if particular combination differences could be readily measured in the future, it would be straightforward to compute the required sensitivity coefficients.

Although laboratory experiments have greater control over systematic effects they provide only a local constraint on a drifting constant. It could be argued that even a null result would be limited to the age of the Solar System (around 4.6 billion years) and that a variation of μ could have occurred at earlier stages in the evolution of the Universe. More desirable are molecular systems which are astronomically relevant because observation at different redshifts presents the opportunity to look back to much earlier times in the Universe. Detection in a wide variety of cosmological settings also lends itself to searches for possible spatial variations of μ , for which a number of studies using ammonia have been reported [39–42].

The transitions presented in this work are perhaps more likely to be detected in terrestrial studies given that the rovibrational states involved lie above 1600 cm^{-1} . Astronomical detection is not impossible, however. The energy levels of the $(J, K) = (18, 18)$ inversion transition in the ground vibrational state of $^{14}\text{NH}_3$ reside at 2176.93 and 2178.47 cm^{-1} , respectively, and this line was observed towards the galactic center star forming region Sgr B2 [43]. A number of $2\nu_2 \leftrightarrow \nu_4$ transitions which possess sizable Einstein A coefficients and involve energy levels lower than the $(J, K) = (18, 18)$ energies are listed in Table II. Such highly excited states could effectively be populated by exoergic chemical formation processes [44]. It is hoped that future astronomical observations search for these particularly sensitive transitions.

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