# Physical properties of Herschel selected galaxies in a semi-analytic galaxy formation model 

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#### Abstract

We make use of a semi-analytic cosmological model that includes simple prescriptions for dust attenuation and emission to make predictions for the observable and physical properties of galaxies that may be detected by the recently launched Herschel Space Observatory in deep fields such as Great Observatories Origins Deep Survey-Herschel. We compare our predictions for differential galaxy number counts in the Herschel Photodetector Array Camera and Spectrometer (PACS) (100 and $160 \mu \mathrm{~m})$ and Spectral and Photometric Imaging Receiver (SPIRE) (250, 350 and $500 \mu \mathrm{~m}$ ) bands with available observations. We find very good agreement with the counts in the PACS bands, for the overall counts and for galaxies binned by redshift at $z<$ 2. At $z>2$ our model underpredicts the number of bright galaxies in the PACS bands by a factor of 10. The agreement is much worse for all three SPIRE bands and becomes progressively worse with increasing wavelength. We discuss a number of possible reasons for these discrepancies and hypothesize that the effect of blending on the observational flux estimates is likely to be the dominant issue. We note that the PACS number counts are relatively robust to changes in the dust-emission templates, at least for the three sets of templates that we have tested, while the predicted SPIRE number counts are more template dependent especially at low redshift. We present quantitative predictions for the relationship between the observed PACS 160 and SPIRE $250 \mu \mathrm{~m}$ fluxes and physical quantities such as halo mass, stellar mass, cold gas mass, star formation rate and total infrared (IR) luminosity, at different redshifts. We also present predictions for the radial sizes of Herschel-selected discs at high redshift $(z>2)$ and find reasonable agreement with the available observations. Finally, we present quantitative predictions for the correlation between the PACS $160 \mu \mathrm{~m}$ flux and the probability that a galaxy has experienced a recent major or minor merger. Although our models predict a strong correlation between these quantities, such that more IR-luminous galaxies are more likely to be merger driven, we find that a significant fraction (more than half) of all high-redshift IR-luminous galaxies detected by Herschel are able to attain their high star formation rates without enhancement by a merger.


Key words: methods: numerical - galaxies: evolution - galaxies: formation - galaxies: star formation.

## 1 INTRODUCTION

One of the most important discoveries from extragalactic observations in the mid-infrared (IR) and far-IR (FIR) has been the identification of luminous and ultra-luminous IR bright galaxies (LIRGs:

[^0]$L_{\mathrm{IR}}>10^{11} \mathrm{~L}_{\odot}$ and ULIRGs: $L_{\mathrm{IR}}>10^{12} \mathrm{~L}_{\odot}$, respectively). These objects have been studied extensively in the literature (e.g. Rieke \& Low 1972; Harwit et al. 1987; Sanders et al. 1988; Condon et al. 1991; Sanders, Scoville \& Soifer 1991; Auriere et al. 1996; Duc, Mirabel \& Maza 1997; Genzel et al. 1998, 2001; Lutz et al. 1998; Rigopoulou et al. 1999; Rowan-Robinson 2000; Colina et al. 2001; Colbert et al. 2006; Dasyra et al. 2006b; Hernán-Caballero et al. 2009; Magdis et al. 2011) and found to emit more energy at IR
wavelengths ( $\sim 5-500 \mu \mathrm{~m}$ ) than at all other wavelengths combined (e.g. Sanders \& Mirabel 1996). Even though the luminous IR galaxies are rare objects in the local Universe (e.g. Lagache, Puget \& Dole 2005), reasonable assumptions about the lifetime of the IR phase (see e.g. Farrah et al. 2003, and references therein) suggest that a substantial fraction of all massive galaxies pass through a stage of intense IR emission during their lifetime (Sanders \& Mirabel 1996, and references therein). Consequently, the majority of the most luminous galaxies in the Universe emit the bulk of their energy in the FIR. Furthermore, LIRGs and ULIRGs dominate the cosmic star formation rate (SFR) density at $z \sim 1-2$, accounting for 70 per cent of the star formation activity at these epochs (e.g. Floc'h et al. 2005). This makes the IR an extremely interesting wavelength regime to study, especially in the context of the cosmic star formation history, and galaxy formation and evolution.
Understanding IR bright galaxies is especially important because light from bright, young blue stars is often attenuated by dust (for a review see Calzetti 2001). The observed rest-frame ultraviolet (UV) light of a galaxy may therefore provide a biased view of the SFR in the galaxy. For example, the global SFR required to explain the FIR and submillimetre background appears to be higher than that inferred from the data in the UV optical (e.g. Hughes et al. 1998, and references therein). The dust attenuated light from blue stars is however not lost, but is re-radiated at IR wavelengths. As a result, a large fraction of the radiation from star formation is radiated not at UV or optical but at IR rest-frame wavelengths.

The European Space Agency's Herschel Space Observatory (Pilbratt et al. 2010) was launched in 2009 May. It observes the Universe at IR wavelengths, from 60 to $670 \mu \mathrm{~m}$, and opens up a huge region of new parameter space for surveys in area, depth and wavelength. Consequently, a primary goal of Herschel is to explore the evolution of obscured galaxies. With Herschel, we can finally probe the IR light of high-redshift galaxies from 70 to 160 and 250 to $500 \mu \mathrm{~m}$ with the Photodetector Array Camera and Spectrometer (PACS; Poglitsch et al. 2010) and Spectral and Photometric Imaging Receiver (SPIRE; Griffin et al. 2010), respectively. Unfortunately, at such long wavelengths, contamination and crowding, rather than the depth of the observations, often become a limiting factor (e.g. Blain, Ivison \& Smail 1998; Brisbin et al. 2010; Lacey et al. 2010). As a result, the interpretation of IR observations can be less than straightforward. This is especially true when probing galaxies at high redshift. Despite the potential complications, several deep Herschel observations have been performed (e.g. Oliver et al. 2010) since the launch of the observatory and more will likely follow.
Early Herschel observations and studies have already generated some very interesting results, such as the conclusions that the majority of the detected high-redshift galaxies are large and massive spiral galaxies (e.g. Cava et al. 2010) with extremely high SFRs (e.g. Brisbin et al. 2010). Furthermore, the minimum dark matter halo mass of IR bright galaxies was recently constrained to be about $3 \times$ $10^{11} \mathrm{M}_{\odot}$ (Amblard et al. 2011), while the average dust temperature of H-ATLAS sources was found to be $28 \pm 8 \mathrm{~K}$ (Amblard et al. 2010). However, because of the very large beam of the Herschel telescope and the difficulty of making unique associations between optically detected galaxies and the PACS or SPIRE sources, many open questions about the physical nature of the populations detected by Herschel remain: for example, what are their stellar masses, sizes and morphologies (spheroid or disc dominated)? Are they dynamically relaxed galaxies or interacting or merging systems?
One can turn to theoretical modelling to aid in the interpretation of these observations and to make predictions about the nature of the objects that Herschel should detect at various redshifts. In the

IR, all the theoretical models in the literature can be divided into two broad classes: phenomenological models and cosmological models. The phenomenological models (sometimes called 'backwards evolution' models) are based on observed luminosity functions (LFs) and assume simple functional forms to describe the evolution of galaxy LFs or SFR with redshift. Template spectral energy densities (SEDs) based on observed galaxies are used to transform between different wavelengths (e.g. Dale et al. 2001; Dale \& Helou 2002; Lagache, Dole \& Puget 2003). In contrast, in semi-analytic cosmological models, the evolution of galaxy properties is predicted based on the framework of the hierarchical structure formation, or cold dark matter (CDM) theory. In these simulations, the evolution of structure in the dark matter component is characterized via 'merger trees', and simplified prescriptions are used to model the main physical processes such as cooling and accretion of gas, star formation, chemical evolution, stellar, supernovae and active galactic nuclei feedback (e.g. Croton et al. 2006; Somerville et al. 2008). Based on the resulting predicted star formation and chemical enrichment histories, the SED for unattenuated light from stars (which dominates the SED shortwards of about $3 \mu \mathrm{~m}$ ) may be calculated using stellar population synthesis models (e.g. Tinsley \& Gunn 1976; Worthey 1994; Leitherer \& Heckman 1995; Bruzual \& Charlot 2003; Maraston 2005; Conroy, Gunn \& White 2009, and references therein).
Modelling the impact of dust attenuation and computing the SED of the dust emission are less straightforward. A standard assumption is that all energy absorbed by dust is re-radiated. One can then break the problem into two parts: computing the amount of light absorbed (and scattered) by dust as a function of wavelength and computing the amount of re-radiated light emitted by dust as a function of wavelength. One approach is to couple the semi-analytic models with a radiative transfer (RT) code (Granato et al. 2000; Baugh et al. 2005a; Fontanot et al. 2007; Lacey et al. 2008, 2010) to compute the dust attenuation and scattering, and a detailed dust model, which assumes a specific dust composition and set of grain properties, to compute the dust-emission SEDs. Another approach is to use analytic models relating the attenuation to the column density of dust (assumed to be traced by metals in the cold gas) in galactic discs (e.g. Guiderdoni \& Rocca-Volmerange 1987). To compute the dust-emission SED, one can then use empirical dust SED templates based on analytic dust models calibrated to observations or observed galaxies (Guiderdoni et al. 1998; Devriendt, Guiderdoni \& Sadat 1999; Devriendt \& Guiderdoni 2000).
The former approach (full RT+dust model) has the clear advantage of providing more detailed and accurate predictions of the galaxy SEDs, given the input assumptions, and certainly provides a better estimate of galaxy-to-galaxy scatter in the SED properties. It has the disadvantage of being computationally quite expensive, and perhaps not merited given that semi-analytic models do not provide detailed information about the relative geometry of stars and dust in galaxies, nor about the composition or properties of the dust, which may vary with cosmic time or environment. Fontanot et al. (2009a) and Fontanot \& Somerville (2011) have shown that the analytic recipes for predicting dust attenuation and the empirical template approach for dust emission provide reasonably good agreement, in most cases, with statistical quantities such as galaxy LFs and counts as computed with the full RT approach using the GRASIL code (Silva et al. 1998). Moreover, this analytic approach to dust attenuation and emission was adopted by Somerville et al. (2011, hereafter S11) and Gilmore et al. (2011), who showed that it provided good agreement with observed galaxy LFs for rest UV to near-IR (NIR) wavelengths and redshifts $0<z<4$. This approach also produced
fairly good agreement with observational estimates of the total IR LF at $0<z<2$ and with the observed extragalactic background light. However, these models produced poorer agreement at longer wavelengths ( $\lambda \gtrsim 8 \mu \mathrm{~m}$ ), particularly for luminous higher redshift ( $z \gtrsim 2$ ) galaxies. Thus, the limitations of our approach should be kept in mind. Part of the goal of this work is to determine where improvements to this kind of analytic approach must be made by confronting the models with recent observations from Herschel.

In this work we use the semi-analytic galaxy formation model (SAM) introduced in Somerville \& Primack (1999), with significant updates as presented by Somerville et al. (2008), Hopkins et al. (2009) and S11, and undertake a study of galaxies that should be detected by current Herschel surveys both locally and at high redshift. We focus on the populations that can be detected in the relatively deep surveys being carried out with Herschel, in particular the Great Observatories Origins Deep Survey (GOODS)-Herschel project (PI: D. Elbaz). The redshift range $2 \leq z<4$ is of special interest because (1) it spans the peak of the cosmic star formation activity in the Universe, (2) it probes what are probably the earliest epochs for which individual galaxies can be detected with Herschel and (3) many open questions remain about the nature of galaxy populations, especially luminous IR galaxies, at these epochs.

This paper is organized as follows. In Section 2, we provide a brief overview of the SAM used in our study, the model for dust attenuation and emission, how we construct our mock light cone and our sample selection criteria. In Section 3, we present our predictions for the observable properties of Herschel galaxies such as counts and LFs. In Section 4, we show predictions for the physical properties of Herschel-selected galaxies at different redshifts. Finally, we summarize our results and conclude in Section 5.

## 2 THE SEMI-ANALYTIC MODEL

### 2.1 The semi-analytic galaxy formation model

We compute the formation and evolution of galaxies within the $\Lambda$ CDM cosmology using the SAM introduced in Somerville \& Primack (1999) and described in detail in Somerville et al. (2008), hereafter S08. Our model also includes the modified recipe for bulge formation and starburst efficiency described in Hopkins et al. (2009). In summary, the S08 SAM includes the following physically motivated recipes: (1) growth of structure in the dark matter component in a hierarchical clustering framework, as characterized by 'merger trees', (2) the shock heating and radiative cooling of gas, (3) conversion of cold gas into stars according to an empirical 'Kennicutt-Schmidt' relation, (4) the evolution of stellar populations, (5) feedback and metal enrichment of the interstellar and intracluster medium from supernovae explosions, (6) two modes ('quasar' and 'radio' mode) of black hole growth and feedback from active galactic nuclei and (7) starbursts and morphological transformation by galaxy mergers. The SAM can be used to predict physical quantities such as stellar and cold gas masses and metallicities of galaxies, their star formation and merger histories, and their luminosities and sizes.

The merging histories (or merger trees) of dark matter haloes are constructed based on the extended Press-Schechter formalism using the method described in Somerville \& Kolatt (1999), with improvements described in S08. These merger trees record the growth of dark matter haloes via merging and accretion, with each 'branch' representing a merger of two or more haloes. In this work we follow each branch back in time to a minimum progenitor mass of $10^{9} \mathrm{M}_{\odot}$. This mass scale is sufficient to resolve the formation histories of
the relatively bright, massive galaxies that we study in this work, which occupy haloes with masses greater than a few $\times 10^{11} \mathrm{M}_{\odot}$.

In the SAM of S08 the star formation occurs in two modes, a 'quiescent' mode in isolated discs and a merger-driven 'starburst' mode. Star formation in isolated discs is modelled using the empirical Kennicutt-Schmidt relation (Kennicutt 1989), assuming that only gas above a fixed critical surface density is eligible to form stars. The efficiency and time-scale of the merger-driven burst mode is a function of merger ratio and the gas fractions of the progenitors, and is based on the results of hydrodynamic simulations (Robertson et al. 2006; Hopkins et al. 2009).

In this work we have assumed a standard $\Lambda \mathrm{CDM}$ universe and a Chabrier stellar initial mass function (IMF; Chabrier 2003). We adopt the following cosmological parameter values: $\Omega_{\mathrm{m}}=0.28$, $\Omega_{\Lambda}=0.72, H_{0}=70.0, \sigma_{8}=0.81$ and $n_{\mathrm{s}}=0.96$, which are consistent with the five-year Wilkinson Microwave Anisotropy Probe results (Komatsu et al. 2009) and were also adopted by S11. The adopted baryon fraction is 0.1658 .

In the following we summarize the main aspects of the modelling of the dust attenuation and emission. A more detailed account can be found in S11.

### 2.1.1 Model for dust attenuation

Our model for dust extinction is based on the approach proposed by Guiderdoni \& Rocca-Volmerange (1987), combined with the model proposed by Charlot \& Fall (2000). As in the Charlot \& Fall model, we consider extinction by two components, one due to the diffuse dust in the disc and another associated with the dense 'birth clouds' surrounding young star-forming regions. The $V$-band, face-on extinction optical depth of the diffuse dust is given by
$\tau_{V, 0}=\frac{\tau_{\text {dust }, 0} Z_{\text {cold }} m_{\text {cold }}}{r_{\text {gas }}^{2}}$,
where $\tau_{\text {dust }, 0}$ is a free parameter, $Z_{\text {cold }}$ is the metallicity of the cold gas, $m_{\text {cold }}$ is the mass of the cold gas in the disc and $r_{\text {gas }}$ is the radius of the cold gas disc, which is assumed to be a fixed multiple of the stellar scalelength.

To compute the actual extinction we assign a random inclination to each galaxy and use a standard 'slab' model; i.e. the extinction in the $V$ band for a galaxy with inclination $i$ is given by
$A_{V}=-2.5 \log _{10}\left[\frac{1-\exp \left(\frac{-\tau_{V, 0}}{\cos (i)}\right)}{\frac{\tau_{V, 0}}{\cos (i)}}\right]$.
Additionally, stars younger than $t_{\mathrm{BC}}$ are enshrouded in a cloud of dust with optical depth $\tau_{\mathrm{BC}, V}=\mu_{\mathrm{BC}} \tau_{V, 0}$, where we treat $t_{\mathrm{BC}}$ and $\mu_{\mathrm{BC}}$ as free parameters. Finally, to extend the extinction estimate to other wavebands, we assume a starburst attenuation curve (Calzetti 1997, 2001) for the diffuse dust component and a power-law extinction curve $A_{\lambda} \propto(\lambda / 5500 \AA)^{n}$, with $n=0.7$, for the birth clouds (Charlot \& Fall 2000). Our results are insensitive to minor modifications of the underlying extinction curve for the cirrus extinction, e.g., adoption of a Galactic or Small Magellanic Cloud-type extinction curve instead of Calzetti.

### 2.1.2 Dust parameters

There are three free parameters that control the dust attenuation in our model: the normalization of the face-on $V$-band optical depth $\tau_{\text {dust }, 0}$, the opacity of the birth clouds relative to the cirrus component $\mu_{\mathrm{BC}}$ and the time that newly born stars spend enshrouded in
their birth clouds, $t_{\mathrm{BC}}$. We first set $\tau_{\text {dust }, 0}$ by matching the normalization of the observed relationship between $L_{\text {dust }} / L_{\mathrm{UV}}$ and bolometric luminosity $L_{\mathrm{bol}}$ for nearby galaxies, where $L_{\mathrm{dust}}$ is the total luminosity absorbed by dust and re-emitted in the mid- to FIR and $L_{\mathrm{UV}}$ is the luminosity in the far-UV (FUV) ( $\sim 1500 \AA$ ). Using a value of $\tau_{\text {dust }, 0}=0.2$, S11 found good agreement with these observations, and also with the observed optical through NIR LFs in the local Universe. We also adopt this same value, $\tau_{\text {dust }, 0}=0.2$.

The birth cloud parameters $\mu_{\mathrm{BC}}$ and $t_{\mathrm{BC}}$ mainly control the attenuation of UV light relative to longer wavelengths. S11 show that in the local Universe $(z=0)$, the $g$ through $K$-band LFs are insensitive to the birth cloud parameters, while the FUV through $u$ bands are quite dependent on them. S11 adjusted the parameters to match the $z=0$ FUV and near-UV observed LFs, finding good agreement with $\mu_{\mathrm{BC}}=4.9$ and $t_{\mathrm{BC}}=2 \times 10^{7} \mathrm{yr}$, which we also adopt in our study. However, S11 found that it was not possible to reproduce the observed rest UV and optical LFs at high redshift with fixed values of these parameters. Other studies (e.g. Guo \& White 2009; Lo Faro et al. 2009) have reached similar conclusions. Moreover, there is direct observational evidence that galaxies are less extinguished at high redshift for a given bolometric luminosity (Reddy et al. 2010) Following S11, we therefore adopt a simple redshift dependence in all three dust parameters, which is adjusted in order to reproduce the observed rest-frame UV and optical LFs out to $z \sim 5$. Our adopted scalings are $\tau_{\text {dust }, 0}(z)=\tau_{\text {dust }, 0}(1+z)^{-1}$, and both $\mu_{\mathrm{BC}}$ and $t_{\mathrm{BC}}$ scale with $z^{-1}$ above $z=1$.

### 2.1.3 Model for the dust emission

Using the formalism presented above we can compute the total fraction of the energy emitted by stars that is absorbed by dust, over all wavelengths, for each galaxy in our simulation. We then assume that all of this absorbed energy is re-radiated in the IR (we neglect scattering), and thereby compute the total IR luminosity of each galaxy $L_{\mathrm{IR}}$. We then make use of dust-emission templates to determine the SED of the dust emission, based on the hypothesis that the shape of the dust SED is well correlated with $L_{\text {IR }}$. The underlying physical notion is that the distribution of dust temperatures is set by the intensity of the local radiation field; thus, more luminous or actively star-forming galaxies should have a larger proportion of warm dust, as observations (e.g. Sanders \& Mirabel 1996) seem to imply.

There are two basic kinds of approaches for constructing these sorts of templates. The first is to use a dust model along with either numerical or analytic solutions to the standard RT equations to create a library of templates, calibrated by comparison with local prototypes. This approach was pioneered by Desert, Boulanger \& Puget (1990), who posited three main sources of dust emission: polycyclic aromatic hydrocarbons, very small grains and big grains In this approach, the detailed size distributions are modelled using free parameters, which are calibrated by requiring the model to fit a set of observational constraints, such as the extinction or attenuation curves, observed IR colours and the IR spectra of local galaxies.
The second approach is to make direct use of observed SEDs for a set of prototype galaxies and to attempt to interpolate between them (e.g. Chary \& Elbaz 2001; Dale \& Helou 2002; Lagache et al. 2004). In this work we make use of the empirical SED templates recently published by Rieke et al. (2009), hereafter R09. They constructed detailed SEDs from published Infrared Space Observatory (ISO), IRAS and NICMOS data as well as previously unpublished IRAC, MIPS and IRS observations. They modelled the FIR SEDs assuming a single blackbody with
wavelength-dependent emissivity. The R09 library includes 14 SEDs covering the $5.6 \times 10^{9} \mathrm{~L} \odot<L_{\mathrm{IR}}<10^{13} \mathrm{~L}_{\odot}$ range. To explore the sensitivity of our results to the details of the template set, we also present results for the Chary \& Elbaz (2001) templates, hereafter CE01, and for the templates recently presented by Chary \& Pope (2010), hereafter CP11. The latter are calibrated to reproduce the SEDs of high-redshift galaxies, which appear to deviate somewhat from the local templates (for a detailed discussion, see CP11).

### 2.2 The mock light cone

We use the SAM described in Section 2.1 to generate a mock light cone of simulated galaxies. Our simulated light cone is 100 times the size of the GOODS on the northern sky, which covers $\sim 160$ arcmin squared in the sky. We chose to simulate a light cone that covers 100 times larger area than the GOODS North (GOODS-N) to improve the statistics, as luminous IR galaxies are relatively rare. We further limit our light cone of simulated galaxies to range from 0 to 6 in redshift space. This limitation is arbitrary; however, we will show below that the apparent IR flux of simulated galaxies drops steeply as a function of redshift, so it is unlikely that any galaxies beyond this redshift could be detected by Herschel.
Our simulated light cone contains in total 23980599 galaxies. The dark matter halo masses range from $\sim 2.7 \times 10^{9}$ to $\sim 4.5 \times$ $10^{14} \mathrm{M}_{\odot}$. Consequently, our light cone contains a variety of dark matter haloes from light subhaloes to large and massive clustersized haloes. As a result, these simulated dark matter haloes host a variety of different types of galaxies from small dwarf galaxies to giant ellipticals. The stellar masses of our simulated galaxies range roughly five orders in magnitude from $10^{7}$ to $\sim 4.6 \times 10^{12} \mathrm{M}_{\odot}$.

We use the full mock light cone from redshift 0 to 6 when comparing the predicted number counts to observational constraints (Section 3.1) and for predictions of the galaxy LFs (Section 3.2). We also use all galaxies in our full mock light cone when making predictions for physical properties as a function of redshift. However, in some cases we select a subsample that contains only high-redshift IR bright galaxies.

### 2.2.1 Sample of high-redshift luminous IR galaxies

For part of our analysis, we focus on a sample with criteria that are motivated by the desire to compare with high-redshift galaxies in the GOODS-Herschel survey. For this sample, we select all simulated galaxies from our light cone that are in the redshift range $2 \leq z<$ 4 and above the detection limit of either PACS at the $160 \mu \mathrm{~m}$ or SPIRE at the $250 \mu \mathrm{~m}$ bands in the GOODS-N. For simplicity, we assume the limits for both instruments to be $\sim 5 \mathrm{mJy}$ (see e.g. Elbaz et al. 2010), although we note that the actual detection limit in the PACS band may be somewhat lower ( $\sim 3.5-4.5 \mathrm{mJy}$ ). These two bands were chosen to represent the two different instruments and to be close to the peak of the thermal IR emission in our chosen redshift range. No other selection criteria, such as stellar mass or optical flux cut, were applied, except the ones enforced by the mass resolution.

Selected in this way, our high-redshift sample comprises in total 1154 (3948) galaxies when the selection is done using the PACS 160 (SPIRE 250) $\mu \mathrm{m}$ band. Note however that our simulated light cone is 100 times larger than the GOODS-N - hence one may infer that we would expect $\sim 10$ PACS $160 \mu \mathrm{~m}$ and $\sim 40$ SPIRE $250 \mu \mathrm{~m}$ detected galaxies in a field with the size and depth of the GOODSN. However, cosmic variance is probably large for these objects,
and therefore this number is uncertain. We return to this matter in the following sections.

The PACS $160 \mu \mathrm{~m}$ selected high-redshift sample consists of luminous IR galaxies with bolometric IR luminosity ranging from $\sim 1 \times 10^{12}$ to $\sim 2 \times 10^{13} \mathrm{~L} \odot$. The average bolometric luminosity $\bar{L}_{\text {IR }} \sim 2.46 \times 10^{12} \mathrm{~L}_{\odot}$. The SPIRE $250 \mu \mathrm{~m}$ selected high-redshift sample consists of IR bright galaxies with the bolometric IR luminosity ranging from $\sim 5 \times 10^{11}$ to $\sim 2 \times 10^{13} \mathrm{~L} \odot$, while the average bolometric IR luminosity $\bar{L}_{\text {IR }} \sim 1.75 \times 10^{12} \mathrm{~L} \odot$. We can therefore readily conclude that all of the galaxies in the PACS selected sample are ULIRGs, while in the SPIRE selected sample they are at least LIRGs, while most, i.e. more than 90 per cent, can be defined as ULIRGs. The simple single PACS $160 \mu \mathrm{~m}$ or SPIRE $250 \mu \mathrm{~m}$ band selection is a good indicator for the total IR luminosity because in our selected redshift range we are always near the peak of the IR flux. Consequently, our sample of high-redshift galaxies is well suited to study the physical properties of high-redshift (U)LIRGs that are potentially observable in fields such as the GOODS North and South.

Fig. 1 shows the PACS $160 \mu \mathrm{~m}$ flux, $S_{160}$, in mJy as a function of redshift $z$ for all simulated galaxies as well as the comoving number density of simulated galaxies as a function of the PACS $160 \mu \mathrm{~m}$ flux and redshift. The horizontal green dashed line in the scatter
plot is drawn at 5 mJy , which is roughly the same as the detection limit in the GOODS-N. Note, however, that the confusion limit in the GOODS-N and in comparable fields can be higher than the detection limit, especially at longer wavelengths. For example, a confusion limit $\sim 19.1 \pm 0.6 \mathrm{mJy}$ at the $250 \mu \mathrm{~m}$ SPIRE band has been quoted in the literature (Nguyen et al. 2010). Obviously, observations that are of the same depth, but on less crowded fields, could reach down to the mJy level. Moreover, observations in gravitational lensed fields can reach well below the derived confusion limit, as has already been shown by Altieri et al. (2010), thus providing a motivation for our sample selection and the usage of 5 mJy . We note that Fig. 1 would be quantitatively similar if we used the SPIRE $250 \mu \mathrm{~m}$ band instead of the PACS $160 \mu \mathrm{~m}$ flux, although the SPIRE-selected sample extends to slightly higher redshift (a few galaxies are predicted above 5 mJy up to $z \sim 4.0$ ).

Fig. 1 shows that the number density of luminous IR galaxies drops quickly above redshift 3 ; hence, observations comparable to those in the GOODS-N are unlikely to detect galaxies above redshift 4. However, as noted above, these galaxies are likely to be strongly clustered, with a large field-to-field variance, implying that the maximum redshift may also vary from field to field. Unfortunately, due to the fact that we adopt the extended Press-Schechter formalism to generate our merger trees, we do not have information on the spatial


Figure 1. PACS $160 \mu \mathrm{~m}$ flux, $S_{160}$, in mJy as a function of the redshift $z$ for all simulated galaxies. The histograms show projections of the scatter plot. The solid bars in the upper histogram show the comoving number density $\left(\frac{\mathrm{d} N}{\mathrm{~d} z}\right)$ of all galaxies, while the hatched bars show that of simulated galaxies with $S_{160}>$ 5 mJy . The right-hand-side histogram shows the comoving number density $\left(\frac{\mathrm{d} N}{\mathrm{~d} S}\right)$ as a function of the PACS $160 \mu \mathrm{~m}$ flux. The horizontal green dashed line is at 5 mJy , which corresponds roughly to the detection limit in PACS $160 \mu \mathrm{~m}$ observations in the GOODS-N.
locations of our galaxies and therefore we cannot properly quantify the effects of cosmic variance. We defer this to a future study, where we plan to use light cones extracted from $N$-body simulations and will therefore have information on the clustering properties of our galaxies.

## 3 OBSERVABLE PROPERTIES

### 3.1 Number counts and redshift distributions

The most basic statistic describing a galaxy population is the number counts, i.e. the number density on the sky of galaxies as a function of the observed flux. The number counts at FIR and submillimetre wavelengths are well known to exhibit strong evolution (Oliver et al. 2010, and references therein). Unfortunately, the Herschel beam is broad compared to the number density of sources, and thus the maps are often confused. This confusion means that care has to be taken when estimating number counts from Herschel data: observations must in general be corrected for flux boosting and incompleteness (see, e.g., Clements et al. 2010; Oliver et al. 2010, and references therein). For example, the faint flux densities may be overestimated due to the classical flux boosting effect (e.g. Béthermin et al. 2010). In the following sections we therefore compare our model to existing observations and make predictions for higher redshifts and lower flux levels than what the current observations have probed.

### 3.1.1 Number counts in the PACS and SPIRE bands

Figs 2 and 3 show differential galaxy number counts for the PACS 100 and $160 \mu \mathrm{~m}$ bands derived from our simulated light cone after being normalized to a Euclidean slope ( $\mathrm{d} N / \mathrm{d} S \propto S^{-2.5}$ ). In order to investigate the sensitivity of our results to the dust-emission templates, we have shown the predictions using three different sets of templates. The template sets of R09 and CE01 are based on nearby


Figure 2. Predicted galaxy differential number counts (circles) compared to observational estimates of Berta et al. (2010) (shown in cyan) and Altieri et al. (2010) (shown in magenta) in the PACS $100 \mu \mathrm{~m}$ band at different redshift bins. The Berta et al. (2010) observations are based on direct detections, while the Altieri et al. (2010) number counts take advantage of lensing caused by the cluster Abell 2218. The shaded regions correspond to $3 \sigma$ Poisson errors in the model, while the observational errors are $1 \sigma$ limits. The different colours refer to different dust-emission template SEDs that have been used in the semi-analytic model (red: CE01; blue: CP11; green: R09).


Figure 3. Predicted galaxy differential number counts (circles) compared to observational estimates of Berta et al. (2010) (shown in cyan) and Altieri et al. (2010) (shown in magenta) in the PACS $160 \mu \mathrm{~m}$ band at different redshift bins. The Berta et al. (2010) observations are based on direct detections, while Altieri et al. (2010) number counts take advantage of lensing caused by Abell 2218. The shaded region corresponds to $3 \sigma$ Poisson errors in the model, while the observational errors are $1 \sigma$ limits. The different colours refer to different dust-emission template SEDs that have been used in the semi-analytic model (red: CE01; blue: CP11; green: R09).
galaxies. The templates of CP11 incorporate data from distant galaxies and in general predict higher fluxes longwards of the thermal dust peak for IR-luminous galaxies, corresponding to colder dust temperatures. Overplotted are the galaxy differential number counts from the early Herschel observations of Berta et al. (2010) and Altieri et al. (2010). The number counts of Berta et al. (2010), which were derived from GOODS-N data, cover the flux range $3-50 \mathrm{mJy}$ at $100 \mu \mathrm{~m}$ and $5.5-72 \mathrm{mJy}$ at $160 \mu \mathrm{~m}$, while the number counts of Altieri et al. (2010) cover the flux range $\sim 1-35$ and $\sim 1.5-58 \mathrm{mJy}$ at 100 and $160 \mu \mathrm{~m}$, respectively. The general agreement between the galaxy differential number counts of simulated galaxies and observations is excellent at low $(z<2)$ redshift. However, in the highest redshift bin $(2<z \leq 5)$ the agreement is worse. Even though the observational constraints are weaker - only two (four) of the observational constraints at the PACS 100 (160) $\mu \mathrm{m}$ band are not upper limits - this disagreement requires further discussion. We return to this issue later.

A detailed inspection of the differential number counts of the simulated galaxies shows a monotonic rise in the two lowest redshift bins till $\sim 20 \mathrm{mJy}$. This is consistent with a non-evolving population of galaxies. Based on their observations Berta et al. (2010) argue for a drop at $\sim 20 \mathrm{mJy}$, even though the errors in observations are relatively large. The number counts of the simulated galaxies provide some support for such a claim at the $100 \mu \mathrm{~m}$ band; however, at the $160 \mu \mathrm{~m}$ band our model does not show any significant drop. For the PACS $100 \mu \mathrm{~m}$ band our model predicts a reasonably monotonic rise all the way to $\sim 500 \mathrm{mJy}$. Even so, a small (but statistically significant) drop is visible at $\sim 60 \mathrm{mJy}$. Quantitatively the PACS 160 $\mu \mathrm{m}$ band's behaviour is very similar; however, the increase in the Euclidean normalized number counts is shallower after $\sim 20 \mathrm{mJy}$ and seems to reach a plateau. The Euclidean normalized counts seem to rise again at $\sim 200 \mathrm{mJy}$, especially at the PACS $100 \mu \mathrm{~m}$ band.
The redshift evolution of the galaxy differential number counts of the simulated galaxies in both PACS 100 and $160 \mu \mathrm{~m}$ bands is rather modest at $z \lesssim 1$. Even up to redshift 2 the number of
$\sim 10$ mJy IR galaxies seems to evolve only slowly, in contrast to the number of fainter galaxies, which seems to grow as a function of redshift, causing the distribution of the number counts to flatten and eventually to turn over when probing even earlier cosmic times. At $z \gtrsim 2$ our model predicts that the normalized number counts of the faintest ( $S_{160} \sim 0.1 \mathrm{mJy}$ ) galaxies are at the same level as that of the brightest ( $S_{160} \sim 100 \mathrm{mJy}$ ).

Figs 4, 5 and 6 show Euclidean normalized differential galaxy number counts derived from our simulated light cone in the 250, 350


Figure 4. Predicted galaxy differential number counts (circles) compared to observational estimates of Glenn et al. (2010) (shown in cyan) and Clements et al. (2010) (shown in magenta) in the SPIRE $250 \mu \mathrm{~m}$ band in different redshift bins. The number counts of Clements et al. (2010) are direct detections, while Glenn et al. (2010) derived their counts by modelling the $P(D)$ distribution, rather than identifying individual galaxies. The shaded regions correspond to $3 \sigma$ Poisson errors in the models, while the observational errors are $1 \sigma$ limits. Green, red and blue colours show the predictions using different dust-emission templates, as in the previous figures.


Figure 5. Predicted galaxy differential number counts (circles) compared to observational estimates of Glenn et al. (2010) (shown in cyan) and Clements et al. (2010) (shown in magenta) in the SPIRE $350 \mu \mathrm{~m}$ band at different redshift bins. The number counts of Clements et al. (2010) are direct detections, while Glenn et al. (2010) derived their counts by modelling the $P(D)$ distribution, rather than identifying individual galaxies. The shaded regions correspond to $3 \sigma$ Poisson errors in the models, while the observational errors are $1 \sigma$ limits. Green, red and blue colours show the predictions using different dust-emission templates, as in the previous figures.


Figure 6. Predicted galaxy differential number counts (black circles) compared to observational estimates of Glenn et al. (2010) (shown in cyan) and Clements et al. (2010) (shown in magenta) in the SPIRE $500 \mu \mathrm{~m}$ band at different redshift bins. The number counts of Clements et al. (2010) are direct detections, while Glenn et al. (2010) derived their counts by modelling the $P(D)$ distribution, rather than identifying individual galaxies. The shaded regions correspond to $3 \sigma$ Poisson errors in the models, while the observational errors are $1 \sigma$ limits. Green, red and blue colours show the predictions using different dust-emission templates, as in the previous figures.
and $500 \mu \mathrm{~m}$ SPIRE bands, respectively. We show the observational results from the early Herschel observations of Glenn et al. (2010) and Clements et al. (2010) for comparison. At $250 \mu \mathrm{~m}$, our model predicts significantly fewer galaxies at the $5-30 \mathrm{mJy}$ level than are observed. This discrepancy is even larger in the SPIRE 350 and $500 \mu \mathrm{~m}$ bands. The agreement seems better at slightly higher fluxes ( $\sim 100 \mathrm{mJy}$ ), but then the models overpredict sources at the highest flux levels ( $\sim 1 \mathrm{Jy}$ ) in all three bands. Note however that the number of simulated galaxies with $S \gtrsim 400 \mathrm{mJy}$ is very small, as indicated by the large error bars. The actual field-to-field variation will be even larger, as our model error bars do not include the effects of large-scale clustering.

The galaxy differential number count estimates of Glenn et al. (2010) are based on the pixel brightness distribution $P(D)$ method, in which no direct detections are needed. In this method the distribution of pixel brightnesses is used to make statistical interferences about the slope and amplitude of the source counts. Therefore, the $P(D)$ method can be used to derive number counts below the confusion limit (see Glenn et al. (2010) for details). However, we note that Glenn et al. (2010) emphasize that their values are model fits and thus effectively integral constraints over some region surrounding each flux density. However, as the differences between their multiply broken power-law and spline models are relatively small, we choose to show only their results based on the multiply broken power-law model (table 2 of Glenn et al. 2010). This provides a reasonable compromise given the fact that we have added their $1 \sigma$ statistical errors and their estimated systematic uncertainties in quadrature, after which both of their model fits are roughly within the errors shown.

Glenn et al. (2010) note that they clearly detect a break in the number counts at around 20 mJy in all the SPIRE bands at high significance. Our model also shows a break; however, it is at a significantly lower flux ( $\sim 2 \mathrm{mJy}$ ), except for the SPIRE $250 \mu \mathrm{~m}$ channel when adopting the CP11 templates. Glenn et al. (2010) also note that there is possible weak ( $\sim 1 \sigma$ ) evidence for a 'bump'
in the differential counts around 400 mJy at the $250 \mu \mathrm{~m}$ band. The location of such a bump in our models is quite dependent on the adopted dust-emission templates, but our model shows an upturn at high fluxes independent of the templates adopted. However, at the $350 \mu \mathrm{~m}$ band all templates show a bump around 300 mJy , although it is unclear whether this is part of the upturn or a real feature given the relatively large uncertainties at high fluxes.

We are not aware of any published results for SPIRE counts broken into redshift bins; however, we show our theoretical predictions for comparison with future observational results. The predicted redshift evolution of the number counts in all SPIRE bands is qualitatively similar to that of the PACS bands. We note however that in the SPIRE bands the redshift evolution of LIRGs is more modest. Even in the highest redshift bin, the Euclidean normalized galaxy differential number counts of the brightest galaxies are only a factor of a few lower than those in the lower redshift bins.
In summary, our models produce very good agreement for the overall counts in the PACS 100 and $160 \mu \mathrm{~m}$ bands, but this agreement rapidly worsens as we move to longer wavelengths. The overall agreement in the SPIRE bands is quite poor. Moreover, although our model predictions are also in good agreement with the galaxy number counts split by redshift for $z<2$, they do not produce enough IR-luminous galaxies at $z>2$. Although the magnitude of the discrepancy between our theoretical predictions and the observational results is disturbing, the interpretation is also somewhat complex. In what follows we therefore discuss potential theoretical and observational complications that could lead to the noted discrepancies in turn.

We first emphasize that these semi-analytic models have been shown elsewhere (see S11; Fontanot et al. 2009b, and references therein) to reproduce reasonably well-observed LFs from the rest UV to NIR, as well as stellar mass functions and SFR functions, from $z \sim 0$ to 5 , although the agreement does get worse towards higher redshifts. Moreover, the good agreement in the PACS bands up to $z \sim 2$ suggests that many of the basic ingredients of the model must be reasonable. However, a possible explanation for some of these discrepancies is that perhaps the adopted dust-emission templates are not valid at earlier cosmic times. Indeed, there is observational evidence that the correlation between total IR luminosity and dust temperature might be different in high-redshift galaxies (Amblard et al. 2010; Elbaz et al. 2010; Hwang et al. 2010). We attempted to investigate this by testing three different sets of dustemission templates (see also the discussion in CP11), as described at the beginning of this section. The results of adopting the different templates are complex, with some templates producing better results at some wavelengths and redshifts, and others performing better in other regimes. The predictions with the three templates are similar in the PACS bands for the overall counts and at low redshifts $(z<1)$. The CP11 templates predict slightly fewer galaxies in the highest redshift bin ( $2<z<5$ ), which worsens the (already poor) agreement with the observations. However, the CP11 templates produce significantly better agreement for the counts in the SPIRE bands at intermediate fluxes (between about 3 and 100 mJy ). Thus, we conclude that the results are sensitive to the choice of dust-emission templates, but none of the template sets that we investigated can reproduce the observations at all wavelengths. Another potential cause for the noted discrepancy may relate to our simplified modelling of the dust absorption and emission. We tuned our model to reproduce the observed ratio of unattenuated to re-radiated light (UV to FIR) for average galaxies at $z=0$. However, galaxies at high redshift may have more complex geometries, leading to greater scatter or even a breakdown in this approach. As already noted, scatter or evolution
in the dust-emission SEDs could also be important. As noted by CP11, it is not clear whether the observations they used span the entire range of underlying dust temperatures and associated FIR colours.

On the other hand, one likely culprit in the Herschel observations is the impact of flux boosting and blending, which affects the counts more severely at longer wavelengths and may also have a larger effect at high redshifts, where galaxies are strongly clustered and there is a higher probability that the Herschel beam intersects lower redshift objects along the line of sight. Indeed, we have visually checked the Hubble Space Telescope (HST) images at the position of $250 \mu \mathrm{~m}$ detected Herschel sources in the GOODS-N, and it is clear that in many, if not most cases, there are multiple galaxies within the PACS or SPIRE beam. For longer wavelengths such as the SPIRE $500 \mu \mathrm{~m}$ the complications are even worse because of the full width at half-maximum of the beam doubles (from $\sim 18$ at $250 \mu \mathrm{~m}$ to $\sim 36 \operatorname{arcsec}$ ). Moreover, according to the simulations carried out by Rigby et al. (2011), more than half ( $\sim 57$ per cent) of the sources detected at $\geq 5 \sigma$ at $500 \mu \mathrm{~m}$ show a flux boosting by a factor $>1.5$ and more than every fourth ( $\sim 27$ per cent) by a factor $>2$. This is clearly a very serious issue when comparing theoretical predictions with these observations.

Other observational complications include cosmic variance. Particularly the bright counts may be compromised by field-to-field variance, as the areas covered are still not large. Moreover, at long wavelengths, recent results imply that many of the bright sources might be lensed (e.g. Lima, Jain \& Devlin 2010; Lima et al. 2010; Negrello et al. 2010). Finally, the contribution to the dust heating from obscured active galactic nuclei (AGN) is uncertain (e.g. Granato, Danese \& Franceschini 1997; Almaini, Lawrence \& Boyle 1999; Farrah et al. 2007; Sajina et al. 2008), although this is unlikely to contribute significantly particularly at the longer wavelengths. Because we cannot rule out these effects, for the remainder of this work, we therefore caution that the predicted IR fluxes that we quote should not be interpreted as corresponding in a one-to-one fashion with the measured fluxes for individual sources that can currently be detected in a Herschel image, but rather with the idealized flux that one would obtain if flux boosting, blending and cosmic variance could be overcome. This situation is less than ideal, but we feel that it can provide a first step towards providing useful predictions. In future work, we plan to pursue a more rigorous comparison, in which we use the theoretical simulations to produce mock Herschel images and treat them in the same way as the real observations. Moreover, the GOODS-Herschel team and others are also working on a better understanding of the impact of blending on their observations, which will eventually clarify the interpretation of our predictions. In addition, our predictions in this form can be compared directly with other theoretical predictions in the literature, which similarly do not address the effects of blending.

### 3.2 Galaxy luminosity functions

While simple number counts are the most basic statistic of galaxy populations, their predictive power is limited. A step further towards the intrinsic properties of a galaxy population can be taken by studying the galaxy LFs. However, even more knowledge of galaxy evolution can be gathered when the evolution of the rest-frame LFs is studied as a function of redshift.
Fig. 7 shows the rest-frame galaxy LFs in the PACS 100 and 160 $\mu \mathrm{m}$ and SPIRE 250 and $350 \mu \mathrm{~m}$ bands. The rest-frame galaxy LFs are shown in five different redshift bins: $0 \leq z<0.3,1.2 \leq z<$ $1.6,2.0 \leq z<2.4,2.4 \leq z<4.0$ and $4.8 \leq z<5.1$. This enables


Figure 7. Rest-frame galaxy LFs in the PACS 100 and $160 \mu \mathrm{~m}$ bands and SPIRE 250 and $350 \mu \mathrm{~m}$ bands at five different redshifts. Different redshifts are shown in different colours and are noted in the legend. The observed LFs (in a and c) marked with symbols are from Lapi et al. (2011).
the study of the redshift evolution of the galaxy IR LFs between $z \sim 5$ and $z \sim 0$. Unfortunately, the observational constraints in the rest-frame LFs of Herschel bands are still limited, especially at higher redshifts; thus, the comparison between the theoretical predictions and observations is less than robust. However, to provide an initial comparison we show the LFs of Lapi et al. (2011), which have been derived from early Herschel data. The redshift bins of the theoretical LFs have been matched to the ones presented in Lapi et al. (2011) to allow easy comparison. However, the sample of Lapi et al. (2011) is limited to only bright galaxies with $S_{250} \geq 35 \mathrm{mJy}$. Moreover, even though they estimate that the fraction of false identifications is as low as $\sim 6$ per cent (in areas with good Sloan Digital Sky Survey completeness), they warn that some truly high-z sources can be missed by their study leading to incompleteness as high as 20 per cent. Such complications will obviously make the comparison less than robust.

The upper panels of Fig. 7, namely $a$ and $b$, show the predicted galaxy LFs in the PACS 100 and $160 \mu \mathrm{~m}$ bands. Qualitatively these two panels are rather similar, i.e. there are only small differences in the LFs of the rest-frame 100 and $160 \mu \mathrm{~m}$ bands. We do note however that the $160 \mu \mathrm{~m}$ band does not extend to as high luminosities as the $100 \mu \mathrm{~m}$ band. This is true at all redshifts. The rest-frame LF of the lowest redshift bin is the lowest curve, showing that the redshift evolution in the PACS bands is strong. The two panels show that the number density of the PACS bright galaxies is highest at redshifts $z \sim 2$, while the highest number density of the faint galaxies is found at $z \sim 3$. Both PACS bands show that the faint end of the LFs evolves hardly at all between $z \sim 5$ and 2 . Even though
we do not see much evolution in the faint end of the PACS LFs, a clear difference exists between the local and higher redshift galaxies. Our model predicts that the number density of luminous IR galaxies peaks around $z \sim 2-3$, in agreement with other predictions (e.g. Swinbank et al. 2008; Lacey et al. 2010). Furthermore, the total number of IR bright galaxies is highest at $z \sim 2$. Such results are easy to understand if the IR rest-frame flux correlates with dust obscured SFR, as the cosmic SFR density is known to peak around the same cosmic time (e.g. Bouwens et al. 2011). Our model also predicts that the number density of the most luminous IR galaxies (i.e. ULIRGs) increases by a factor of $\sim 5$ between redshifts 5 and 3, while their number density is found to peak at $z \sim 2$. The evolution of the PACS LFs also shows that the number density of luminous IR galaxies drops by a factor of $\sim 10$ between redshifts 2 and 0 . These results emphasize the strong evolution in the number density of (U)LIRGs as a function of cosmic time.

In panel a of Fig. 7 we also compare our theoretical LFs to the LFs of Lapi et al. (2011). Qualitatively similar redshift evolution is seen in both cases. Our prediction for the lowest redshift observed $\mathrm{LF}(1.2 \leq z<1.6)$ is in reasonable agreement with the observations, with a modest overprediction of the highest luminosity sources. Towards higher redshift, and especially in the highest redshift bin, the disagreement grows rather large in the sense that our model predicts fewer galaxies with high luminosities than are reported in the observations. Similar effects as discussed in the case of number counts are likely to contribute. The most striking difference, however, between our model and the LFs of Lapi et al. (2011) is the location of the knee of the LFs. Our predicted LFs turn over at about two orders


Figure 8. Predicted median stellar mass versus flux in the PACS 160 and SPIRE $250 \mu \mathrm{~m}$ bands for galaxies selected at different redshifts. The green dotted vertical line shows a representative flux limit of the GOODS-N observations. The error bars show the 16th and 84th percentiles.
of magnitude higher number densities. One potential explanation is provided by Lapi et al. (2011) who argue that the flattening of their LFs at the lowest luminosities may be, at least in part, due to the overestimate of the accessible volume yielded by the $1 / V_{\max }$ estimator for objects near to the flux limit.
The lower panels of Fig. 7, namely c and d, show the predicted rest-frame galaxy LFs in the SPIRE 250 and $350 \mu \mathrm{~m}$ bands. The redshift evolution of the rest-frame SPIRE band LFs is similar to that of the PACS bands. Again, the number densities of LIRGs and ULIRGs, i.e. the galaxies at the bright end of the LF, are found to peak at $z \sim 2-3$. In agreement with the PACS bands, the highest number densities are found at redshifts 2 and 3 , while the number densities drop by a factor of $\sim 11$ to redshift 0 . Thus, the LFs of the rest-frame SPIRE bands show qualitatively similar evolution as the LFs of the PACS bands. However, we note that the bright end of the LFs in the SPIRE bands appears to drop more steeply than in the PACS bands.
In panel c of Fig. 7 we also compare our theoretical LFs to LFs of Lapi et al. (2011). As in the case of the PACS $100 \mu \mathrm{~m}$ the faint end of the lowest redshift $\mathrm{LFs}(1.2 \leq z<1.6)$ is in good agreement with our prediction, while in the brightest end our model predicts more galaxies than are observed. Towards higher redshift, and especially in the case of the highest redshift bin, the disagreement grows rather large. Again, similar effects as discussed earlier are likely to play a role.
IR LFs have also been derived from other observations (e.g. Kim \& Sanders 1998; Floc'h et al. 2005; Goto et al. 2010) and early Herschel data. Dye et al. (2010) derived SPIRE $250 \mu \mathrm{~m}$ band LFs out to $z=0.5$. They find that the LF exhibits significant evolution out to $z=0.5$ and that at a given luminosity, the comoving space density increases steadily with redshift. The evolution noted in Dye et al. (2010) is qualitatively in agreement with our LFs (see S11), although their evolution is rather strong given the rather narrow redshift range. However, strong evolution, particularly at the bright end, is in agreement with our LFs and also noted by others (e.g. Eales et al. 2009). Also Vaccari et al. (2010) derived LFs for local galaxies in all three SPIRE channels. Their LFs are also in good qualitative agreement with our findings for local galaxies. However, our light cones have very small volumes at low redshift, as they were intended for high redshift comparisons, so a more quantitative
comparison is beyond the scope of this study. A comparison with the $z=0.5$ SPIRE $250 \mu \mathrm{~m}$ LF is shown in S11.

## 4 PHYSICAL PROPERTIES OF IR-LUMINOUS GALAXIES OVER COSMIC TIME

Having explored some of the statistical properties of Herschel detected galaxies, in this section we present predictions for some of the physical properties of these objects at different redshifts. We explore the correlations between 160 and $250 \mu \mathrm{~m}$ flux and many different physical properties of our model galaxies. Here we show some of the strongest and most interesting correlations that we identified, which include stellar mass, dark matter halo mass, cold gas mass, SFR and total IR or bolometric luminosity. The correlations with the other Herschel bands are similar and all qualitative conclusions would remain the same, so we do not show them.
Fig. 8 shows the predicted median stellar mass as a function of 160 and $250 \mu \mathrm{~m}$ flux, along with the 16th and 84th percentiles, for different redshifts. Our model predicts that all galaxies with $S_{160}>5$ or $S_{250}>5 \mathrm{mJy}$ have stellar masses in the range $M_{\star} \sim$ $10^{9}-10^{11} \mathrm{M}_{\odot}$. Furthermore, we predict that high-redshift $(z>2)$ galaxies that can be detected individually in deep Herschel surveys such as the GOODS are quite massive, $M_{\star} \gtrsim 10^{10.5} \mathrm{M}_{\odot}$. This is quite different from the results of Lacey et al. (2010), who predict much smaller stellar masses for galaxies at a given FIR flux - at $z \gtrsim 2$, even their most luminous galaxies are less massive than $M_{\star} \sim$ $10^{10} \mathrm{M}_{\odot}$. This difference probably arises mainly from the fact that Lacey et al. (2010) adopted a top-heavy IMF during starbursts. Therefore, there are fewer long-lived low-mass stars in galaxies at high redshift.
Not surprisingly, as stellar mass is known to be fairly well correlated with dark matter halo mass, we find similar results for the dark matter halo masses. At the lowest redshifts ( $z<0.5$ ), luminous IR galaxies (with $S_{160}$ or $S_{250}>5 \mathrm{mJy}$ ) can be found in dark matter haloes as light as $\log _{10}\left(M_{\mathrm{dm}} / \mathrm{M}_{\odot}\right) \sim 11.1$ (see Fig. 9). However, the bulk of simulated IR bright galaxies with $S_{160}$ or $S_{250}>5 \mathrm{mJy}$, especially at higher redshifts, were found to reside in relatively massive dark matter haloes. To be more precise, our model predicts that the masses of the dark matter haloes of IR bright galaxies can cover a broad range from $\log _{10}\left(M_{\mathrm{dm}} / \mathrm{M}_{\odot}\right) \sim 11.5$ to 13.5 , while the bulk


Figure 9. Predicted median dark matter halo mass $\left(M_{\mathrm{dm}}\right)$ as a function of the IR flux in the PACS 160 and SPIRE $250 \mu \mathrm{~m}$ bands at different redshifts. The green dotted vertical line shows a representative flux limit for the GOODS-N observations. The error bars show the 16th and 84th percentiles.
of luminous IR galaxies can be found to reside in rather typical dark matter haloes with masses $\log _{10}\left(M_{\mathrm{dm}} / \mathrm{M}_{\odot}\right) \sim 12.5$.

These predictions are in good agreement with the recent results of Amblard et al. (2011), which were derived from Herschel data. In this paper the authors find an excess clustering over the linear prediction at arcminute angular scales in the power spectrum of brightness fluctuations at 250,350 and $500 \mu \mathrm{~m}$. From this excess Amblard et al. (2011) infer that IR bright galaxies are located in dark matter haloes with a minimum mass of $\log _{10}\left(M_{\min } / \mathrm{M}_{\odot}\right)=11.5_{-0.2}^{+0.7}$ at $350 \mu \mathrm{~m}$. When the authors average over the three wavelengths the minimum halo mass for their galaxies is at the level of $3 \times$ $10^{11} \mathrm{M}_{\odot}$. All our IR bright galaxies are found to reside in dark matter haloes more massive than this lower limit, except a handful of local galaxies, which reside in haloes only slightly less massive $\left(1 \times 10^{11} \mathrm{M}_{\odot}\right)$ than the minimum mass of Amblard et al. (2011).

Our simulated galaxies show evidence for a weak correlation between the dark matter halo mass and the PACS 160 and SPIRE 250 $\mu \mathrm{m}$ fluxes (Fig. 9). Statistically, galaxies residing in more massive dark matter haloes have a higher median IR flux as was also the case with stellar mass (Fig. 8). However, the trend between the dark matter halo mass and 160 or $250 \mu \mathrm{~m}$ flux is weaker than in the case of stellar mass as indicated by the larger range between the 16th and 84th percentiles in Fig 9. Moreover, for the high-redshift galaxies $(2 \leq z<4)$ with either $S_{160}$ or $S_{250}>5 \mathrm{mJy}$ no statistically significant correlation can be inferred. Instead, galaxies with the highest fluxes are again found to reside in dark matter haloes with a broad range of masses from $\log _{10}\left(M_{\mathrm{dm}} / \mathrm{M}_{\odot}\right) \sim 12$ to 13.5. It is however interesting to note that luminous IR galaxies can also be found in cluster-mass dark matter haloes. This implies that some luminous IR galaxies at high redshift may be the progenitors of present-day brightest cluster galaxies. Moreover, this also implies that the IR bright galaxies at high redshifts may provide a signpost to identify proto-clusters during the epoch of their formation. Note, however, that according to our model, the PACS 160 and SPIRE $250 \mu \mathrm{~m}$ fluxes are almost independent of the dark matter halo mass for high-redshift galaxies that would be detected in Herschel observations comparable to fields such as the GOODS. Consequently, the IR flux at high redshift must be governed primarily by other quantities than the mass of the dark matter halo.

Fig. 10 shows the predicted median mass in cold gas as a function of the PACS 160 and SPIRE $250 \mu \mathrm{~m}$ flux for galaxies selected at
different redshifts. Not surprisingly, our model predicts that at high redshift the luminous IR galaxies directly detectable in Herschel surveys will be the most gas rich. Our simulation shows that the galaxies found in these surveys should typically be gas rich with cold gas masses ranging from $\sim 10^{9}$ up to $\sim 4 \times 10^{11} \mathrm{M}_{\odot}$. The bulk of the high-redshift IR bright galaxies were found to contain a cold gas mass of $\sim 6 \times 10^{10} \mathrm{M}_{\odot}$. Interestingly, as we noted earlier, the bulk of the high-redshift IR bright galaxies have stellar masses $M_{\star} \sim$ $6 \times 10^{10} \mathrm{M}_{\odot}$. Consequently, the high-redshift luminous IR galaxies should be extremely gas rich, with the mass in cold gas comparable to or even higher than the mass in stars for high-redshift luminous IR galaxies. This is a clear prediction for future observatories such as ALMA, which should be able to detect CO emission from the molecular gas in these galaxies.

Fig. 11 shows the predicted median SFR as a function of the PACS 160 and SPIRE $250 \mu \mathrm{~m}$ flux at different redshifts. It is not surprising that this is the strongest correlation seen so far, as the FIR flux is generally assumed to be a good proxy for the SFR, and at some level this correlation is artificially tight because of our assumed one-to-one correspondence between total IR luminosity (light reprocessed by dust) and dust-emission SED. However, this plot provides a convenient guide to what SFR one expects to be able to power galaxies at a given 160 or $250 \mu \mathrm{~m}$ flux at different redshifts, assuming a standard set of templates, as well as an indication of how much scatter can arise from heating of dust by old stars.

Fig. 11 shows that at $z>2$ the galaxies directly detectable in surveys such as the GOODS-N should have median SFRs $>30 \mathrm{M}_{\odot} \mathrm{yr}^{-1}$ according to our model prediction. We find that the average SFR for luminous IR galaxies at a high redshift $(2 \leq z<4)$ is $\sim 155 \mathrm{M}_{\odot} \mathrm{yr}^{-1}$. This is significantly higher than for all galaxies (with $\log _{10}\left(M_{\mathrm{dm}}\right)>$ 9) in the same redshift range, for which our model predicts a mean SFR of merely $\sim 2 \mathrm{M}_{\odot} \mathrm{yr}^{-1}$. The highest SFR predicted by our model for a high-redshift galaxy is as high as $\sim 7800 \mathrm{M}_{\odot} \mathrm{yr}^{-1}$. In the next section, we explore the physical mechanisms that are driving high SFRs in high-redshift galaxies. Clearly, such a high SFR cannot persist for very long periods of time.

Fig. 12 shows the median values for the total IR luminosity ( $L_{\mathrm{dust}}$ ) as a function of flux in the PACS 160 and SPIRE $250 \mu \mathrm{~m}$ bands at different redshifts. This plot illustrates that, at low redshift, only a very few of the brightest galaxies in our (relatively small volume) simulations would not even be considered LIRGs ( $L_{\mathrm{IR}}>10^{11} \mathrm{~L} \odot$ ).


Figure 10. Predicted median cold gas mass versus flux in the PACS 160 and SPIRE $250 \mu \mathrm{~m}$ bands for galaxies selected at different redshifts. The green dotted vertical line shows a representative flux limit of the GOODS-N observations. The error bars show the 16th and 84th percentiles.


Figure 11. Predicted median SFR as a function of the IR flux in the PACS 160 and SPIRE $250 \mu \mathrm{~m}$ bands at different redshifts. The green dotted vertical line shows a representative flux limit for the GOODS-N observations. The error bars show the 16th and 84th percentiles. The hatched lines on the right-hand-side plot (L10) are the predictions from Lacey et al. (2010).

Our simulations do not contain any ULIRGs $\left(L_{\mathrm{IR}}>10^{12} \mathrm{~L}_{\odot}\right)$ at low redshift. At $z>1$, all galaxies above our nominal GOODS-Herschel detection limit would be considered LIRGs or ULIRGs, at $z \sim 2$ all of these galaxies would qualify as very bright LIRGs or ULIRGs, and at $z>3$ all of these galaxies are ULIRGs.

At high redshift ( $2 \leq z<4$ ) our model predicts median SFRs that are a factor of 2 higher than those reported in Lacey et al. (2010), as show in Fig. 11. As already noted, Lacey et al. (2010) assumed a top-heavy IMF in starbursts. With a top-heavy IMF, in a given star formation episode, a larger fraction of the mass goes into massive stars that can efficiently heat the dust. Thus, for a top-heavy IMF, the relationship between SFR and IR luminosity is shifted such that a given SFR results in higher IR luminosities. In the Lacey et al. (2010) model, the fraction of star formation occurring in the burst mode increases with redshift, so the average IMF with which stars are being formed shifts from being close to a solar neighbourhood IMF at the present day to being very top-heavy at high redshift. This helps to explain why our SFR versus $250 \mu \mathrm{~m}$ flux relationship agrees with that of Lacey et al. (2010) in the local Universe ( $z<$
$0.25)$, but differs significantly at earlier cosmic epochs. In addition, the treatment of dust is also different in the Lacey et al. (2010) model. They used results from the RT+dust model calculations of Silva et al. (1998).

### 4.1 Sizes of high-redshift late-type Galaxies

For this subsection we use our 'high-redshift' SPIRE $250 \mu \mathrm{~m}$ selected sample of galaxies selected from our light cones in the redshift range $2 \leq z<4$. We identify disc galaxies using the bulge to stellar mass ratio: galaxies with $M_{\text {bulge }} / M_{\text {total }} \leq 0.4$ are considered as latetype galaxies. We also removed all galaxies that have experienced one or more mergers within the last 500 Myr , because these galaxies have disturbed discs (and morphologies) and thus the size of the stellar disc is ill-defined. Fig. 13 shows a Hess plot of the galaxy's disc size as a function of its stellar mass $M_{\star}$ in physical units for this sample of high-redshift galaxies. For a comparison, we also plot the sizes and stellar masses from Cava et al. (2010) with green squares. The grey shading in both panels of Fig. 13 describes the number


Figure 12. Predicted median total IR luminosity ( $L_{\text {dust }}$ ) as a function of the IR flux in the PACS 160 and SPIRE $250 \mu \mathrm{~m}$ bands at different redshifts. The green dotted vertical line shows a representative flux limit for the GOODS-N observations. The error bars show the 16th and 84th percentiles.


Figure 13. Hess plot of disc sizes ( $R_{\text {disc }}$ ) of the late-type galaxies as a function of stellar masses $M_{\star}$. All galaxies shown are in the redshift range $2 \leq z<4$ and have not experienced a merger within the last 500 Myr . The right-hand panel shows only late-type galaxies that are brighter than 5 mJy in the SPIRE $250 \mu \mathrm{~m}$ band. The red lines show the median and 16th and 84th percentiles for simulated galaxies. The observed late-type galaxies, shown with green squares, are from Cava et al. (2010).
of simulated galaxies in a given two-dimensional bin, while the red lines show the median and 16th and 84th percentiles.

As in the real Universe, our model discs show a positive correlation between stellar mass and radial size. Very few galaxies are predicted to be as large in radial extent as the galaxies presented in Cava et al. (2010). However, the right-hand panel of Fig. 13 shows that when we select galaxies in the same redshift range with $S_{250}>5 \mathrm{mJy}$, the predicted sizes are in good agreement with the observational results. The late-type galaxies in our $S_{250}>5 \mathrm{mJy}$ high-redshift sample have average disc radii of $\sim 2.2 \mathrm{kpc}$. This is significantly larger than the mean disc size $(\sim 0.9 \mathrm{kpc})$ of all latetype galaxies in the same redshift range ( $2 \leq z<4$ ). However, the small mean disc size in the case of all late types is driven by the large number of dwarf galaxies. But even if we use the same stellar mass cut that the SPIRE $250 \mu \mathrm{~m}$ band selection induces, we find that the average size of the stellar discs is almost a factor of 2 smaller
( $\sim 1.3 \mathrm{kpc}$ ) than the mean disc size of the high-redshift sample. Consequently, in our models, the IR bright late-type galaxies that have not experienced a merger within the last 500 Myr are on average larger than galaxies that emit lower SPIRE $250 \mu \mathrm{~m}$ fluxes. We speculate that this is because our models predict that larger galaxies are more gas rich, and we have already seen that there is a correlation between gas mass and IR luminosity. Our high-redshift sample of luminous IR galaxies also contains a few late-type galaxies whose stellar discs are $>7 \mathrm{kpc}$ in size (for similar findings, see Rujopakarn et al. 2011).

### 4.2 Correlation with merger activity

Ultra-luminous galaxies in the local Universe are widely believed to be caused by major galaxy mergers (e.g. Sanders \& Mirabel 1996; Colina et al. 2001; Farrah et al. 2003; Dasyra et al. 2006b; Väisänen et al. 2008). It has also been argued that ULIRGs will evolve into moderate-mass ellipticals (e.g. Genzel et al. 2001; Tacconi et al. 2002; Dasyra et al. 2006b) and/or AGN (Farrah et al. 2003, and references therein) after the merger or interaction. Merger-driven star formation has also been studied using hydrodynamic simulations (e.g. Jog \& Solomon 1992; Mihos \& Hernquist 1996; Cox et al. 2008; Teyssier, Chapon \& Bournaud 2010), which support the picture that massive starbursts could be driven by mergers. It has been argued (e.g. Dasyra et al. 2006a) that the majority of ULIRGs are triggered by almost equal-mass major mergers and that less violent mergers of mass ratio < 1:3 typically do not force enough gas into the nucleus to generate ULIRG luminosities. This is in agreement with simulations [e.g. Cox et al. (2008), but see also Teyssier et al. (2010) and references therein], although other factors (orbit, gas fraction and morphology) are also important. Even though some observations of IR-luminous galaxies have failed to identify evidence for mergers, it has been argued that these highly obscured objects could be the end products of collisions between gas-rich galaxies in a final phase of merger evolution (e.g. Auriere et al. 1996). Although this picture is well supported in the local Universe, the physical origin of ULIRGs at high redshift is less clear. For example, Sturm et al. (2010) identified two galaxies in early Herschel observations that suggest that high-redshift galaxies may be able to achieve LIRG and even ULIRG luminosities without experiencing mergers. Our model assumes that mergers can trigger


Figure 14. Merger fraction as a function of the PACS $160 \mu \mathrm{~m}$ flux at different redshifts. The upper-left plot shows the recent major mergers, while the lower-left plot shows recent minor mergers (see the text for definitions). The upper-right panel shows the merger fractions as a function of the PACS $160 \mu \mathrm{~m}$ flux for all mergers within the past 500 Myr , and the lower-right panel shows the fraction of galaxies that have never merged. The vertical dotted line shows a representative flux limit for GOODS-Herschel ( 5 mJy ).
bursts of star formation, but also incorporates the high gas accretion rates at high redshift predicted by cosmological simulations. It is therefore quite interesting to investigate what our model predicts for the fraction of luminous IR galaxies that are the result of mergers at high and low redshift.

To study the fraction of IR bright galaxies that are powered by mergers we record the time since the last merger $T_{\text {merger }}$ or major merger $T_{\text {majormerger }}$ for each galaxy in our simulation. 'Minor' mergers are defined as those with a mass ratio ${ }^{1}$ greater than 1:10 and 'major mergers' as those with mass ratio greater than 1:4. Our model predicts that about 84 (53) per cent of high-redshift galaxies with $S_{160}>10 \mathrm{mJy}$ have experienced a (major) merger during their lifetime. Note, however, that the fraction drops to about 34 per cent if we concentrate on major mergers that have taken place less than 250 Myr ago, which are the mergers that are most likely to be causally linked to the star formation we are seeing. For the SPIRE $250 \mu \mathrm{~m}$ band, the results are very similar; about 86 (57) per cent of high-redshift galaxies with $S_{250}>20 \mathrm{mJy}$ have experienced a (major) merger. If we again concentrate only on recent mergers in which the major merging event took place less than 250 Myr ago, the merger fraction drops to $\sim 42$ per cent. Thus our model makes an interesting prediction: roughly every second high-redshift ULIRG can achieve ULIRG luminosities without a recent major merger. This prediction differs from the findings of Gonzalez et al. (2011), who used an SAM (Baugh et al. 2005b) to study submillimetre galaxies (SMGs; $S_{850}>5 \mathrm{mJy}$ ). Gonzalez et al. (2011) find that the majority of SMGs seen in current submillimetre surveys are starbursts triggered by major and minor mergers involving gas-rich disc galaxies (see also Baugh et al. 2005b).
We present these results in more detail in Fig. 14, which shows the evolution of merger fractions as a function of the PACS $160 \mu \mathrm{~m}$ flux at different redshifts. The upper-left plot shows that the merger fraction of recent (the latest merger took place less than or equal to

[^1]

Figure 15. The fraction of galaxies that have experienced a merger and that have never merged with another galaxy as a function of the far- to mid-IR flux ratio. The flux ratio is the ratio between the PACS 160 and Spitzer IRAC $4.5 \mu \mathrm{~m}$ bands. The merger events have been divided into recent or young ( $\leq 250 \mathrm{Myr}$ ) and less recent or old ( $250<T_{\text {merger }}<500 \mathrm{Myr}$ ) and to minor and major incidents and are colour coded as given by the legend.

250 Myr ago) major mergers grows as a function of the PACS 160 $\mu \mathrm{m}$ flux. This is truly independent of the studied redshift, although the steepest rise is noted at $z=1$ and 4 . The plot shows that the likelihood of the most luminous ULIRGs being powered by a merger is higher than for those that are less luminous. A similar trend can also be seen for minor mergers. This shows that under the right conditions, minor mergers may also trigger (U)LIRG-like activity. We note that Fig. 14 and the related results are qualitatively similar if instead of the PACS $160 \mu \mathrm{~m}$ flux we use the SPIRE $250 \mu \mathrm{~m}$ band.
We can use our models to attempt to identify observational quantities that could provide interesting indicators of starburst and merger activity for observations that are available or will become available soon. We wish to exploit the availability of extensive multiwavelength data, from the rest UV to the FIR with Herschel, in fields such as GOODS. We focus on the redshift range $2 \leq z<4$ for these experiments and use the high-redshift sample from our light cones. It is reasonable to expect that starbursts will have high values of specific SFR (SSFR), $\dot{M}_{\star} M_{\star}^{-1}$. In a relatively narrow redshift range, we can use the ratio of a FIR flux to a Spitzer IRAC band as a proxy for SSFR.
Fig. 15 shows the fraction of different types of mergers and the fraction of galaxies which have never merged as a function of the far- to mid-IR flux ratio (colour). We choose to use the PACS $160 \mu \mathrm{~m}$ band as our FIR band, because it is relatively close to the peak of the IR flux distribution in the studied redshift range ( $2 \leq$ $z<4$ ), but at the same time it suffers less from confusion than, e.g., the SPIRE $250 \mu \mathrm{~m}$ band. The mid-IR band chosen is channel 2 of the Spitzer IRAC at $4.5 \mu \mathrm{~m}$, which should provide a proxy for the stellar mass of a galaxy. Fig. 15 shows that our models predict that the probability that a galaxy has experienced a recent merger is a strong function of this far- to mid-IR flux ratio. For the most extreme values ( $S_{160} S_{4.5}^{-1} \gtrsim 1300$ ) more than half of the galaxies have experienced a major merger within the last 250 Myr . We note that the results remain if we instead use other bands such as $S_{250} S_{8}^{-1}$ as the flux ratio. It will be interesting to test whether these IR colours are correlated with signatures of recent merger activity in observed galaxies.

Simulated Galaxies: $S_{160}>5 \mathrm{mJy}$


Figure 16. Rest-frame UV-optical colour as a function of the far- to mid-IR flux. The flux ratio is the ratio between the PACS 160 and Spitzer IRAC $4.5 \mu \mathrm{~m}$ bands. The model galaxies have been colour coded by the time since the last merger in Myr. The green dotted line marks the region in which all simulated galaxies are recent mergers.

We can also explore whether the use of a two-colour diagram can provide further information. We expect that the rest-frame UV colours might correlate with the age of the starburst, and thus with the time since the merger event. We consider the filters of the HST's Advanced Camera for Surveys, because such data are available for the GOODS. In Fig. 16 we combine the information on UV-optical colour and far- to mid-IR flux ratio in a colour-colour plot. Again, we choose to use the PACS $160 \mu \mathrm{~m}$ band and IRAC's channel 2 $(4.5 \mu \mathrm{~m})$, because these channels allow the most robust comparison with observations of galaxies in the GOODS field. However, the results would be qualitatively similar with any IRAC channel or with the SPIRE $250 \mu \mathrm{~m}$ band. Fig. 16 shows that in our models, the most recent mergers are all located in the lower-right region of each subplot, that is the region with the most extreme far- to mid-IR flux ratio and the bluest UV-optical colour.

The black contours indicate where the galaxies which have never merged are located and have been drawn using a two-dimensional Gaussian kernel density estimator. Note, however, that this region is also populated by recent mergers so we cannot conclude that the observed galaxies in this region have not experienced a recent merger. However, it is interesting that there is a region of the diagram (shown by a green dotted line) in which all galaxies have experienced a recent merger. The functional form of the green line is as follows:
$(F 775 W-F 850 l p)_{\mathrm{AB}}=A \log _{10} \frac{S_{160}}{S_{4.5}}+B$,
where $A=1$ and $B=-2.4$. Note, however, that this simple selection does not seem to be able to separate recent major mergers from less extreme mergers. If instead of the PACS we had used the SPIRE
$250 \mu \mathrm{~m}$ band, the above equation would remain the same, but with $B=-2.7$.

It will be very interesting to test these predictions using surveys such as GOODS-Herschel, where multiwavelength photometry as well as high-resolution Hubble imaging is available. We plan to pursue this in a future work (Niemi et al., in preparation).

## 5 SUMMARY AND CONCLUSIONS

In this work we made use of the semi-analytic models developed by S 11 , in which attenuation and re-emission of light by dust is modelled with a simple analytic approach, to make predictions for the physical and observable properties of galaxies that may be detected in deep fields by the Herschel Space Observatory. We used the semi-analytic models to generate mock light cones resembling the GOODS but with 100 times the volume.
We first examined the differential number counts for galaxies in the PACS and SPIRE bands. We found very good agreement with the observed number counts derived from Herschel PACS data, for the overall counts and for galaxies binned by redshift at $z<2$. At $z>2$ our model underpredicts the number of more luminous galaxies in the PACS 100 and $160 \mu \mathrm{~m}$ bands. The agreement of our model predictions with the observed counts deteriorates as one moves to longer wavelengths, with increasingly poor agreement seen as one moves from PACS to SPIRE $250 \mu \mathrm{~m}$ and then to the longer SPIRE bands. At $250 \mu \mathrm{~m}$ and longer wavelengths, the models tend to underpredict the number counts of intermediate flux galaxies ( $10 \lesssim S_{250} \lesssim 100 \mathrm{mJy}$ ) and overpredict the counts of brighter galaxies ( $S_{250} \gtrsim 100 \mathrm{mJy}$ ). We presented predictions using three different sets of empirical dust-emission templates and found interesting differences. However, it does not appear that any single simple modification to the dust templates could solve the discrepancies.
We discussed possible reasons for these discrepancies. These include uncertainties due to cosmic variance, possible evolution or scatter in the dust-emission templates, a possible contribution to the IR light from obscured AGN, and the possibility that many of the bright sources are lensed. It is also possible that some of the physical processes in our model need revision, or that the stellar IMF was different in early galaxies, as has been suggested by Baugh et al. (2005b). However, our models produce reasonable agreement with the LFs at rest UV through NIR wavelengths, and with the observationally derived stellar mass functions and SFR functions at high redshift (see S11; Fontanot et al. 2009b, and references therein). Moreover, the top-heavy IMF model of Baugh et al. (2005b) that was developed to explain the observed submillimetre population at $850 \mu \mathrm{~m}$ does not appear to reproduce the SPIRE number counts particularly well (Clements et al. 2010; Lacey et al. 2010), and does not produce enough galaxies with large stellar masses at high redshift (Swinbank et al. 2008). We also discuss the impact of flux boosting and blending on the observationally derived Herschel counts. This would explain why the discrepancy becomes larger with increasing wavelength, and might also be a larger effect for high-redshift galaxies, which are compact and strongly clustered. A quick visual inspection of HST images for high-redshift galaxies makes it clear that many, if not most, Herschel sources probably have contributions from multiple galaxies. Moreover, according to the simulations carried out by Rigby et al. (2011), more than half ( $\sim 57$ per cent) of sources detected at $\geqslant 5 \sigma$ at $500 \mu \mathrm{~m}$ show a flux boosting by a factor $>1.5$ and more than every fourth ( $\sim 27$ per cent) by a factor $>2$. This is clearly a very serious issue when comparing theoretical predictions with these observations. We intend to use our simulations
to create mock Herschel images, carry out the source detection procedure on these and study the predicted effects of blending on the measured fluxes and galaxy counts. In addition, the Herschel team is working hard to better understand and overcome this problem.
With the resulting caveat that one probably cannot interpret our predicted Herschel fluxes as corresponding in a one-to-one fashion with directly observed Herschel fluxes (as currently available), but rather as intrinsic fluxes in the absence of blending, we used our model to make predictions for the physical properties of Herschel detected galaxies. We showed the predicted relationships between PACS 160 and SPIRE $250 \mu \mathrm{~m}$ fluxes and stellar mass, halo mass, cold gas mass, SFR and total IR luminosity as various redshifts. Our models show fairly strong trends between both $S_{160}$ and $S_{250}$ at a given redshift and all of these quantities except halo mass, which is quite flat as a function of both $S_{160}$ and $S_{250}$ at higher redshifts. This may have interesting implications for the clustering properties of these sources (for early observational results in GOODS South, see e.g. Magliocchetti et al. 2011). Our models predict that the galaxies that are likely to be detected in deep Herschel surveys such as GOODS-Herschel ( $S_{160}$ or $S_{250}>5 \mathrm{mJy}$ ) at high redshift $(z>2)$ have fairly large stellar masses ( $M_{\star} \sim 6 \times 10^{10}-3 \times 10^{11} \mathrm{M}_{\odot}$ ) and reside in fairly massive dark matter haloes ( $\gtrsim 10^{11} \mathrm{M}_{\odot}$ ). The latter is in good agreement with the minimum mass derived by Amblard et al. (2011) based on the observed clustering of SPIRE sources.
The simulated IR-luminous galaxies were also found to be gas rich with cold gas masses ranging from $\sim 10^{9}$ up to $\sim 4 \times 10^{11} \mathrm{M}_{\odot}$. The bulk of the high-redshift IR bright galaxies were found to contain $\sim 6 \times 10^{10} \mathrm{M}_{\odot}$ of cold gas. These predictions will soon be able to be tested with radio and millimetre observations such as those that will be obtainable with ALMA.

Our predicted stellar, cold gas and halo masses at a given $250 \mu \mathrm{~m}$ flux are significantly higher than the corresponding predictions from the model of Lacey et al. (2010), which assumes a top-heavy IMF in starbursts. We show a quantitative comparison between our predicted SFR versus $S_{250}$ relation and that of Lacey et al. (2010), finding that although their predictions are similar to ours for low redshift galaxies, at higher redshift ( $z \gtrsim 0.5$ ), their predicted SFRs are lower than ours (at a given FIR flux) by about a factor of 2 .
We investigated the radial sizes of high-redshift $(2 \leq z<4)$ latetype galaxies selected in the SPIRE $250 \mu \mathrm{~m}$ band and compared our predictions with the observations recently presented by Cava et al. (2010). We found that the SPIRE detectable galaxies are on average significantly larger than IR faint galaxies with comparable stellar masses. The mean disc size of IR-luminous late-type galaxies was found to be in good agreement with the observations, although the statistics are extremely limited. We speculate that this is because larger galaxies are more gas rich and therefore more likely to be IR bright.
Finally, we investigated our model predictions for the importance of merger-driven starbursts in producing IR-luminous galaxies at different redshifts. Although there is clear evidence for a connection between merger activity and LIRGs and ULIRGs in the local Universe, the situation at high redshift is less clear. However, it has been suggested that an increasing fraction of LIRGs and ULIRGs at high redshift might not have a merger origin. We present quantitative predictions for the fraction of galaxies that have experienced a major or minor merger within a given time-scale as a function of redshift and $160 \mu \mathrm{~m}$ flux. We find a fairly strong trend between the $160 \mu \mathrm{~m}$ flux and the probability that a galaxy has had a recent merger, indicating that brighter galaxies are more likely to be merger driven. However, we find the interesting result that in our models, a significant fraction (half or more) of IR-luminous galaxies
at high redshift $(z>2)$ have not experienced a recent merger. This implies that the high gas accretion rates and efficient feeding via cold flows predicted by cosmological simulations at high redshift can fuel a significant fraction of the galaxies detected by Herschel. This appears consistent with preliminary observational results (e.g. Sturm et al. 2010), but will be interesting to study and quantify in more detail in the near future.

In order to pursue this question further, we used our model to try to identify some observational photometric signatures associated with galaxies that have experienced recent mergers. We showed that there is a strong correlation between the mid-to-IR colour $S_{160} / S_{4.5}$ (PACS $160 \mu \mathrm{~m}$ to Spitzer IRAC channel 2 ratio) and the probability that a galaxy has had a recent merger. We also investigated a two-colour diagnostic using rest-frame UV colour and the $160 \mu \mathrm{~m}$ to IRAC $4.5 \mu \mathrm{~m}$ ratio. We found that recent mergers occupy a characteristic region of this diagram, suggesting another interesting observational tool to identify probable recent mergers. In a work in progress, we are making use of HST imaging in the GOODS-Herschel survey to study the morphologies of galaxies selected using these multiwavelength diagnostics, in order to test our model predictions and the importance of merger-induced star formation at high redshift (Niemi et al., in preparation).

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[^1]:    ${ }^{1}$ Here, the masses used in the ratio include stars, gas and the dark matter within the optical radius of the galaxy, as in S 08 .

