## Measurement of Forward-Backward Asymmetry and Wilson Coefficients in $\boldsymbol{B} \rightarrow \boldsymbol{K}^{*} \boldsymbol{l}^{+} \boldsymbol{l}^{-}$

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#### Abstract

We report the first measurement of the forward-backward asymmetry and the ratios of Wilson coefficients $A_{9} / A_{7}$ and $A_{10} / A_{7}$ in $B \rightarrow K^{*} \ell^{+} \ell^{-}$, where $\ell$ represents an electron or a muon. We find evidence for the forward-backward asymmetry with a significance of $3.4 \sigma$. The results are obtained from a data sample containing $386 \times 10^{6} B \bar{B}$ pairs that were collected on the $\Upsilon(4 S)$ resonance with the Belle detector at the KEKB asymmetric-energy $e^{+} e^{-}$collider.


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Flavor-changing neutral current $b \rightarrow s$ processes proceed via loop diagrams in the standard model (SM). If additional diagrams with non-SM particles contribute to such processes, the decay rate and kinematics are modified. Such contributions may change the 12 Wilson coefficients [1] that parametrize the strength of the weak and strong short distance interactions. The $b \rightarrow s \ell^{+} \ell^{-}$amplitude is described by the effective Wilson coefficients $C_{7}, C_{9}$, and $C_{10}$, whose terms have been calculated up to next-to-next-to-leading order (NNLO) [2] in quantum chromodynamics. To evaluate the Wilson coefficients, we use $A_{i}$ which are dominant and $q^{2}$-independent real terms of $C_{i}$. Other small complex terms in $C_{i}$ are fixed to the SM values. Here, $q^{2}$ is the squared invariant mass of the dilepton system.

The magnitude of $A_{7}$ is strongly constrained from measurements of $B \rightarrow X_{s} \gamma[3,4]$, where $X_{s}$ is a hadronic system with an $s$ quark; a large area of the $\left(A_{9}, A_{10}\right)$ plane is excluded by branching fraction measurements of $B \rightarrow$ $X_{s} \ell^{+} \ell^{-}$and $B \rightarrow K^{(*)} \ell^{+} \ell^{-}$[5-8], where $K^{(*)}$ refers to $K$ or $K^{*}$. However, the sign of $A_{7}$ and the values of $A_{9}$ and $A_{10}$ are not yet determined. Measurement of the forwardbackward asymmetry and differential decay rate as functions of $q^{2}$ and $\theta$ for $B \rightarrow K^{*} \ell^{+} \ell^{-}$constrains the relative signs and magnitudes of these coefficients [9,10]. Here $\theta$ is the angle between the momenta of the negative (positive) lepton and the $B(\bar{B})$ meson in the dilepton rest frame. The forward-backward asymmetry is defined using the differential decay width $g\left(q^{2}, \theta\right)=d^{2} \Gamma / d q^{2} d \cos \theta$ [11] as

$$
\begin{equation*}
\mathcal{A}_{\mathrm{FB}}\left(q^{2}\right)=\frac{\int_{-1}^{1} \operatorname{sgn}(\cos \theta) g\left(q^{2}, \theta\right) d \cos \theta}{\int_{-1}^{1} g\left(q^{2}, \theta\right) d \cos \theta} \tag{1}
\end{equation*}
$$

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The numerator in Eq. (1) can be expressed in terms of Wilson coefficients as

$$
\begin{align*}
\int_{-1}^{1} \operatorname{sgn}(\cos \theta) g\left(q^{2}, \theta\right) d \cos \theta= & -C_{10} \xi\left(q^{2}\right) \\
& \times\left(\operatorname{Re}\left(C_{9}\right) F_{1}+\frac{1}{q^{2}} C_{7} F_{2}\right), \tag{2}
\end{align*}
$$

where $\xi$ is a function of $q^{2}$, while $F_{1}$ and $F_{2}$ depend on form factors. (The full expression can be found in Ref. [11].)

In this Letter, we report the first measurement of the forward-backward asymmetry and ratios of Wilson coefficients in $B \rightarrow K^{*} \ell^{+} \ell^{-}$. We use a $357 \mathrm{fb}^{-1}$ data sample containing $386 \times 10^{6} B \bar{B}$ pairs taken at the $\Upsilon(4 S)$ resonance. We also study the $B^{+} \rightarrow K^{+} \ell^{+} \ell^{-}$mode, which is expected to have a very small forward-backward asymmetry even in the presence of new physics [12]. Chargeconjugate modes are included throughout this Letter.

The data were taken at the KEKB collider [13] and collected with the Belle detector [14]. The detector consists of a silicon vertex detector, a central drift chamber, aerogel Cherenkov counters, time-of-flight scintillation counters, an electromagnetic calorimeter, and a muon identification system.

The event reconstruction procedure is the same as described in our previous Letter [5]. The following final states are used to reconstruct $B$ candidates: $K^{* 0} \ell^{+} \ell^{-}$, $K^{*+} \ell^{+} \ell^{-}$, and $K^{+} \ell^{+} \ell^{-}$, with subdecays $K^{* 0} \rightarrow K^{+} \pi^{-}$, $K^{*+} \rightarrow K_{S}^{0} \pi^{+}$and $K^{+} \pi^{0}, K_{S}^{0} \rightarrow \pi^{+} \pi^{-}$, and $\pi^{0} \rightarrow \gamma \gamma$.

Hereafter, $K^{* 0} \ell^{+} \ell^{-}$and $K^{*+} \ell^{+} \ell^{-}$are combined and called $K^{*} \ell^{+} \ell^{-}$.

We use two variables defined in the center-of-mass (c.m.) frame to select $B$ candidates: the beam-energy constrained mass $M_{\mathrm{bc}}=\sqrt{\left(E_{\text {beam }}^{*} / c^{2}\right)^{2}-\left(p_{B}^{*} / c\right)^{2}}$ and the energy difference $\Delta E=E_{B}^{*}-E_{\text {beam }}^{*}$, where $p_{B}^{*}$ and $E_{B}^{*}$ are the measured c.m. momentum and energy of the $B$ candidate, and $E_{\text {beam }}^{*}$ is the c.m. beam energy. When multiple candidates are found in an event, we select the candidate with the smallest value of $|\Delta E|$.

The dominant background consists of $B \bar{B}$ events where both $B$ mesons decay semileptonically. We suppress this background using missing energy and $\cos \theta_{B}^{*}$, where $\theta_{B}^{*}$ is the angle between the flight direction of the $B$ meson and the beam axis in the c.m. frame. These quantities are combined to form signal and background likelihoods $\mathcal{L}_{\text {sig }}$ and $\mathcal{L}_{B \bar{B}}$, respectively, and event selection is then performed using the ratio $\mathcal{R}_{B \bar{B}}=\mathcal{L}_{\text {sig }} /\left(\mathcal{L}_{\text {sig }}+\mathcal{L}_{B \bar{B}}\right)$. The continuum ( $e^{+} e^{-} \rightarrow q \bar{q}, q=u, d, s, c$ ) background is suppressed using a likelihood ratio $\mathcal{R}_{\text {cont }}$ (defined similarly to $\mathcal{R}_{B \bar{B}}$ ) that depends on three variables: a Fisher discriminant [15] calculated from the sum of c.m. energies of the final state particles in each of nine cones along the $B$ candidate c.m. sphericity axis [16] and the normalized second Fox-Wolfram moment [17], the angle between the beam axis and the c.m. sphericity axis, and $\cos \theta_{B}^{*}$. Backgrounds from $B \rightarrow J / \psi X_{s}$ and $B \rightarrow \psi(2 S) X_{s}$ decays, referred to below as $B \rightarrow \psi X_{s}$, are rejected using the dilepton invariant mass. Backgrounds from photon conversions and $\pi^{0}$ Dalitz decays are suppressed by requiring the $e^{+} e^{-}$invariant mass to be above $140 \mathrm{MeV} / c^{2}$.

The signal box is defined as $\left|M_{\mathrm{bc}}-m_{B}\right|<8 \mathrm{MeV} / c^{2}$ for both lepton modes and $-55(-35) \mathrm{MeV}<\Delta E<$ 35 MeV for the electron (muon) mode. We optimize the selections on $\mathcal{R}_{\text {cont }}$ and $\mathcal{R}_{B \bar{B}}$ for each $K^{*}$ decay mode and each lepton mode to maximize sensitivity to events with $q^{2}<6 \mathrm{GeV}^{2} / c^{2}$ assuming the branching fractions in Ref. [18].

To determine the signal yield, we perform an unbinned maximum-likelihood fit to the $M_{\mathrm{bc}}$ distribution for events that lie within the $\Delta E$ signal window. The fit function includes signal, cross feeds, and other background components. The cross feeds are misreconstructed $K^{(*)} \ell^{+} \ell^{-}$
events with correct ("CF") and incorrect ("IF") $B$ meson flavor assignment. The cross feed from $X_{s} \ell^{+} \ell^{-}$events other than $K^{(*)} \ell^{+} \ell^{-}$is negligible. The other backgrounds come from dilepton background, combinatorial $K^{(*)} \ell^{ \pm} h^{\mp}$, $K^{(*)} h^{+} h^{-}$, and $\psi X_{s}$ events, where $h$ represents a pion or a kaon. The dilepton background refers to the sum of all background sources with two leptons where the lepton is from leptonic or semileptonic meson decays, photon conversions, and $\pi^{0}$ Dalitz decays. The $K^{(*)} h^{+} h^{-}$background is from both combinatorial background and $B$ meson decays.

The shape for cross-feed events is parametrized by a sum of an ARGUS function [19] and a Gaussian whose parameters are determined from Monte Carlo (MC) samples. The dilepton background is modeled by an ARGUS function. The shape of each background is determined from a MC sample. (The $K^{(*)} e^{ \pm} \mu^{\mp}$ background shape is found to be consistent between the MC sample and data.) Since the shape for $K^{(*)} \ell^{ \pm} h^{\mp}$ is similar to that for the dilepton background, we use the same parametrizations for both backgrounds. The residual background from $\psi X_{s}$ is estimated from a MC sample of $\psi$ inclusive events and parametrized by the sum of an ARGUS function and a Gaussian. The background from events with misidentified leptons is also parametrized by the sum of an ARGUS function and a Gaussian. In the fit, all background fractions except the dilepton background are fixed while the signal fraction is allowed to float.

Figure 1 shows the fit result. We obtain $113.6 \pm 13.0$ and $96.0 \pm 12.0$ signal events for $K^{*} \ell^{+} \ell^{-}$and $K^{+} \ell^{+} \ell^{-}$, respectively.

We use $B \rightarrow K^{*} \ell^{+} \ell^{-}$candidates in the signal box to measure the normalized double differential decay width. For the evaluation of the Wilson coefficients, the full (partial) NNLO Wilson coefficients $C_{i}[2,7]$ are used for $q^{2} / m_{b}^{2}<0.25(>0.25)$. The value of $A_{7}$ is fixed at the SM value -0.330 or the sign-flipped value +0.330 . The SM values for $A_{9}$ and $A_{10}$ are 4.07 and -4.21 , respectively [7]. We choose $A_{9} / A_{7}$ and $A_{10} / A_{7}$ as fit parameters. To extract these ratios, we perform an unbinned maximum-likelihood fit to the events in the signal box with a probability density function (PDF) that includes the normalized double differential decay width. The PDF used for the fit consists of terms describing the signal, cross feeds, and backgrounds:

$$
\begin{align*}
P\left(M_{\mathrm{bc}}, q^{2}, \cos \theta ; A_{9} / A_{7}, A_{10} / A_{7}\right)= & \frac{1}{N_{\mathrm{sig}}} f_{\mathrm{sig}} \epsilon_{\mathrm{sig}}\left(q^{2}, \cos \theta\right) g\left(q^{2}, \cos \theta\right)+\frac{1}{N_{\mathrm{CF}}} f_{\mathrm{CF}} \epsilon_{\mathrm{CF}}\left(q^{2}, \cos \theta\right) g\left(q^{2}, \cos \theta\right) \\
& +\frac{1}{N_{\mathrm{IF}}} f_{\mathrm{IF}} \epsilon_{\mathrm{IF}}\left(q^{2}, \cos \theta\right) g\left(q^{2},-\cos \theta\right)+\left(1-f_{\mathrm{sig}}-f_{\mathrm{CF}}-f_{\mathrm{IF}}-f_{K^{*} h h}-f_{\psi X_{s}}\right) \\
& \times\left\{\left(f_{K^{*} \ell h} \mathcal{P}_{K^{*} \ell h}\left(q^{2}, \cos \theta\right)+\left(1-f_{K^{*} \ell h}\right) \mathcal{P}_{\mathrm{dl}}\left(q^{2}, \cos \theta\right)\right\}+f_{K^{*} h h} \mathcal{P}_{K^{*} h h}\left(q^{2}, \cos \theta\right)\right. \\
& +f_{\psi X_{s}} \mathcal{P}_{\psi X_{s}}\left(q^{2}, \cos \theta\right) \tag{3}
\end{align*}
$$

Here $\mathcal{P}_{K^{*} \ell h}, \mathcal{P}_{\mathrm{dl}}, \mathcal{P}_{K^{*} h h}$, and $\mathcal{P}_{\psi X_{s}}$ are the probability density functions for $K^{*} \ell h$, dilepton background, $K^{*} h h$, and $\psi X_{s}$, respectively. The quantities $\epsilon_{\mathrm{sig}}\left(N_{\mathrm{sig}}\right), \epsilon_{\mathrm{CF}}\left(N_{\mathrm{CF}}\right)$, and $\epsilon_{\mathrm{IF}}\left(N_{\mathrm{IF}}\right)$ correspond to the efficiency function (normalization) of


FIG. 1. $M_{\mathrm{bc}}$ distributions for (a) $B \rightarrow K^{*} \ell^{+} \ell^{-}$and (b) $B \rightarrow K^{+} \ell^{+} \ell^{-}$samples. The solid and dashed curves are the fit results for the total and background contributions, respectively.
each signal and cross-feed component. Each fraction $f$ is the probability of finding the corresponding component in the data sample for a given $M_{\mathrm{bc}}$ value determined from the $M_{\mathrm{bc}}$ fit, with the exception of $f_{K^{*} \ell h}$, which is the fraction of the $K^{*} \ell h$ events within the background component with misidentification leptons determined from the MC samples. The functions $\epsilon$ and $\mathcal{P}$ for the dilepton background, $K^{*} \ell^{ \pm} h^{\mp}$, and $\psi X_{s}$ are obtained from MC samples. The $K^{*} h^{+} h^{-}$background shape $\mathcal{P}_{K^{*} h h}$ is obtained from $K^{*} h^{+} h^{-}$events and the momentum- and angulardependent hadron to lepton misidentification probability.

The renormalization scale $\mu$ is set to 2.5 GeV as suggested by Ref. [7]. The double differential decay width includes the form factor parameters and the bottom quark mass $m_{b}$. We choose the form factor model of Refs. [7,11] and a bottom quark mass of $4.8 \mathrm{GeV} / c^{2}$.

First, we measure the asymmetry $\tilde{\mathcal{A}}_{\mathrm{FB}}$, which is defined as

$$
\begin{equation*}
\tilde{\mathcal{A}}_{\mathrm{FB}}=\frac{\iint_{-1}^{1} \operatorname{sgn}(\cos \theta) g\left(q^{2}, \theta\right) d \cos \theta d q^{2}}{\iint_{-1}^{1} g\left(q^{2}, \theta\right) d \cos \theta d q^{2}} \tag{4}
\end{equation*}
$$

We determine the yield in five $q^{2}$ bins for $\cos \theta>0$ and $\cos \theta<0$ from a fit to the $M_{\mathrm{bc}}$ distribution. After efficiency correction for each bin, we obtain

$$
\begin{align*}
\tilde{\mathcal{A}}_{\mathrm{FB}}\left(B \rightarrow K^{*} \ell^{+} \ell^{-}\right) & =0.50 \pm 0.15 \pm 0.02 \\
\tilde{\mathcal{A}}_{\mathrm{FB}}\left(B^{+} \rightarrow K^{+} \ell^{+} \ell^{-}\right) & =0.10 \pm 0.14 \pm 0.01 \tag{5}
\end{align*}
$$

where the first error is statistical and the second is systematic. A large asymmetry is measured for $K^{*} \ell^{+} \ell^{-}$with a

TABLE I. $\quad A_{9} / A_{7}$ and $A_{10} / A_{7}$ fit results for negative and positive $A_{7}$ values. The first error is statistical and the second is systematic.

|  | $A_{7}=-0.330$ | $A_{7}=+0.330$ |
| :--- | ---: | ---: |
| $A_{9} / A_{7}$ | $-15.3_{-4.8}^{+3.4} \pm 1.1$ | $-16.3_{-5.7}^{+3.7} \pm 1.4$ |
| $A_{10} / A_{7}$ | $10.3_{-3.5}^{+5.2} \pm 1.8$ | $11.1_{-3.9}^{+6.0} \pm 2.4$ |

significance of $3.4 \sigma$. The result for $K^{+} \ell^{+} \ell^{-}$is consistent with zero as expected.

We fit the $K^{*} \ell^{+} \ell^{-}$candidates with the PDF of Eq. (3). The fit results of ratios of Wilson coefficients are summarized in Table I. Figure 2 shows the fit results projected onto the background-subtracted forward-backward asymmetry distribution in bins of $q^{2}$.

We estimate contributions to the systematic error due to uncertainties in the physics parameters, finite $q^{2}$ resolution, efficiency, and signal probability. We vary the $A_{7}$ value within the range allowed by the branching fraction of $B \rightarrow$ $X_{s} \gamma$ [20]. The bottom quark mass $m_{b}$ is varied by $\pm 0.2 \mathrm{GeV} / c^{2}$. The systematic uncertainty associated with the choice of the form factor model is taken from the deviation in fit results when a model of Ref. [21] is used. The effect of $q^{2}$ resolution is estimated using a toy MC study. The effect due to $\cos \theta$ resolution is found to be negligible. The uncertainty in the efficiency is estimated by changing the efficiency for pions with $p<0.3 \mathrm{GeV} / c$, electrons with $p<0.7 \mathrm{GeV} / c$, and muons with $p<$ $1 \mathrm{GeV} / c$ by $10 \%, 5 \%$, and $10 \%$, respectively, to obtain revised efficiency functions for signal and background PDFs. We change the shape parameters for the signal or background probability functions $f$ and take the difference as an uncertainty in the signal fraction. The parameters are modified by $\pm 1 \sigma$ for signal, dilepton background, and $K^{*} h^{+} h^{-}$. We vary the normalization for cross-feed events and $\psi X_{s}$ by $100 \%$ since we cannot determine these background from data. To assign the systematic error due to the uncertainty in the fraction of $K^{*} \ell^{ \pm} h^{\mp}$, we change the value of $f_{K^{*} \ell h}$ by $20 \%$, which corresponds to the difference between the MC sample and sideband events. Table II summarizes the contributions to the systematic error.

The fit results are consistent with the SM values $A_{9} / A_{7}=-12.3$ and $A_{10} / A_{7}=12.8$. In Fig. 3, we show


FIG. 2. Fit result for the negative $A_{7}$ solution (solid line) projected onto the background-subtracted forward-backward asymmetry and forward-backward asymmetry curves for several input parameters, including the effects of efficiency: $A_{7}$ positive case ( $A_{7}=0.330, A_{9}=4.07, A_{10}=-4.21$ ) (dashed line), $A_{10}$ positive case ( $A_{7}=-0.280, A_{9}=2.42, A_{10}=1.32$ ) (dotteddashed line), and both $A_{7}$ and $A_{10}$ positive cases ( $A_{7}=0.280$, $A_{9}=2.22, A_{10}=3.82$ ) (dotted line) [9]. The new physics scenarios shown by the dotted-dashed and dotted curves are excluded. The blank regions are excluded by the $\psi X_{s}$ veto.

TABLE II. Summary of systematic errors.

|  | $A_{7}=-0.330$ |  |  | $A_{7}=+0.330$ |
| :--- | :--- | :--- | :--- | :---: |
| Source | $A_{9} / A_{7}$ | $A_{10} / A_{7}$ | $A_{9} / A_{7}$ | $A_{10} / A_{7}$ |
| $A_{7}[20]$ | $+0.2-0.0$ | $\pm 0.0$ | $+0.1-0.2$ | $+0.3-0.1$ |
| $m_{b}\left(4.8 \pm 0.2 \mathrm{GeV} / c^{2}\right)$ | $\pm 0.7$ | $\pm 0.5$ | $\pm 0.6$ | $\pm 0.4$ |
| Model dependence | $\pm 0.7$ | $\pm 1.7$ | $\pm 1.0$ | $\pm 2.2$ |
| $q^{2}$ resolution | $\pm 0.3$ | $\pm 0.4$ | $\pm 0.3$ | $\pm 0.4$ |
| Efficiency | $\pm 0.1$ | $\pm 0.0$ | $\pm 0.1$ | $\pm 0.1$ |
| Signal probability | $+0.4-0.5$ | $+0.2-0.3$ | $+0.4-0.5$ | $\pm 0.4$ |
| Total | $\pm 1.1$ | $\pm 1.8$ | $+1.3-1.4$ | $+2.4-2.3$ |

confidence level (C.L.) contours in the $\left(A_{9} / A_{7}, A_{10} / A_{7}\right)$ plane based on the fit likelihood smeared by the systematic error, which is assumed to have a Gaussian distribution. We also calculate an interval in $A_{9} A_{10} / A_{7}^{2}$ at the $95 \%$ C.L. for the allowed $A_{7}$ region,

$$
\begin{equation*}
-14.0 \times 10^{2}<A_{9} A_{10} / A_{7}^{2}<-26.4 \tag{6}
\end{equation*}
$$

From this, the sign of $A_{9} A_{10}$ must be negative, and the solutions in quadrants I and III in Fig. 3 are excluded at the $98.2 \%$ confidence level. Since solutions in both quadrants II and IV are allowed, we cannot determine the sign of $A_{7} A_{10}$. Figure 2 shows the comparison between the fit results for the negative $A_{7}$ value projected onto the forward-backward asymmetry and the forward-backward asymmetry distributions for several input parameters. We exclude the new physics scenarios shown by the dotted and dotted-dashed curves, which have a positive $A_{9} A_{10}$ value.

In summary, we have measured the ratios of Wilson coefficients in $B \rightarrow K^{*} \ell^{+} \ell^{-}$decay for the first time by studying the forward-backward asymmetry in the angular distribution of leptons. We find evidence for a large forward-backward asymmetry with a significance of


FIG. 3. C.L. contours for negative $A_{7}$. Curves show $1 \sigma-5 \sigma$ contours. The symbols show the fit (circle), SM (triangle), and $A_{10}$-positive (star) [9] cases. The $A_{10}$-positive case appears as the dotted-dashed curve of Fig. 2.
$3.4 \sigma$. The fit results are consistent with the SM prediction and also with the case where the sign of $A_{7} A_{10}$ is flipped. We exclude new physics scenarios with positive $A_{9} A_{10}$ at $98.2 \%$ confidence.

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