## Measurement of Polarization and Triple-Product Correlations in $\boldsymbol{B} \rightarrow \boldsymbol{\phi} \boldsymbol{K}^{*}$ Decays

K.-F. Chen, ${ }^{25}$ K. Abe, ${ }^{8}$ K. Abe, ${ }^{39}$ H. Aihara, ${ }^{41}$ Y. Asano, ${ }^{45}$ V. Aulchenko, ${ }^{1}$ T. Aushev, ${ }^{12}$ S. Bahinipati, ${ }^{4}$ A. M. Bakich, ${ }^{36}$ I. Bedny, ${ }^{1}$ U. Bitenc, ${ }^{13}$ I. Bizjak, ${ }^{13}$ S. Blyth, ${ }^{25}$ A. Bondar, ${ }^{1}$ A. Bozek, ${ }^{26}$ M. Bračko, ${ }^{8,19,13}$ J. Brodzicka, ${ }^{26}$ T. E. Browder, ${ }^{7}$ M.-C. Chang, ${ }^{25}$ P. Chang, ${ }^{25}$ Y. Chao, ${ }^{25}$ A. Chen, ${ }^{23}$ W. T. Chen, ${ }^{23}$ B. G. Cheon, ${ }^{3}$ R. Chistov, ${ }^{12}$ S.-K. Choi, ${ }^{6}$ Y. Choi, ${ }^{35}$ A. Chuvikov, ${ }^{48}$ J. Dalseno, ${ }^{20}$ M. Danilov, ${ }^{12}$ M. Dash, ${ }^{46}$ A. Drutskoy, ${ }^{4}$ S. Eidelman, ${ }^{1}$ Y. Enari, ${ }^{21}$ F. Fang, ${ }^{7}$ S. Fratina, ${ }^{13}$ N. Gabyshev, ${ }^{1}$ A. Garmash,,$^{48}$ T. Gershon, ${ }^{8}$ G. Gokhroo, ${ }^{37}$ B. Golob,,${ }^{18,13}$ A. Gorišek, ${ }^{13}$ J. Haba, ${ }^{8}$ N. C. Hastings, ${ }^{41}$ K. Hayasaka, ${ }^{21}$ H. Hayashii, ${ }^{22}$ M. Hazumi, ${ }^{8}$ L. Hinz, ${ }^{17}$ T. Hokuue, ${ }^{21}$ Y. Hoshi, ${ }^{39}$ S. Hou, ${ }^{23}$ W.-S. Hou, ${ }^{25}$ Y. B. Hsiung, ${ }^{25}$ T. Iijima, ${ }^{21}$ A. Imoto, ${ }^{22} \mathrm{~K}$. Inami, ${ }^{21}$ A. Ishikawa, ${ }^{8} \mathrm{H}$. Ishino, ${ }^{42}$ R. Itoh, ${ }^{8}$ M. Iwasaki, ${ }^{41}$ Y. Iwasaki, ${ }^{8}$ J. H. Kang, ${ }^{47}$ J. S. Kang, ${ }^{15}$ P. Kapusta, ${ }^{26}$ N. Katayama, ${ }^{8}$ H. Kawai, ${ }^{2}$ T. Kawasaki, ${ }^{28}$ H. R. Khan, ${ }^{42}$ H. Kichimi, ${ }^{8}$ H. J. Kim, ${ }^{16}$ S. K. Kim, ${ }^{34}$ S. M. Kim, ${ }^{35}$ K. Kinoshita, ${ }^{4}$ S. Korpar, ${ }^{19,13}$ P. Križan, ${ }^{18,13}$ P. Krokovny, ${ }^{1}$ S. Kumar, ${ }^{31}$ C. C. Kuo, ${ }^{23}$ A. Kuzmin, ${ }^{1}$ Y.-J. Kwon, ${ }^{47}$ J. S. Lange, ${ }^{5}$ G. Leder, ${ }^{11}$ S. E. Lee, ${ }^{34}$ Y.-J. Lee, ${ }^{25}$ T. Lesiak, ${ }^{26}$ J. Li, ${ }^{33}$ S.-W. Lin, ${ }^{25}$ D. Liventsev, ${ }^{12}$ J. MacNaughton, ${ }^{11}$ F. Mandl, ${ }^{11}$ T. Matsumoto, ${ }^{43}$ A. Matyja, ${ }^{26}$ Y. Mikami, ${ }^{40}$ W. Mitaroff, ${ }^{11}$ K. Miyabayashi, ${ }^{22}$ H. Miyake, ${ }^{30}$ H. Miyata, ${ }^{28}$ R. Mizuk, ${ }^{12}$ D. Mohapatra, ${ }^{46}$ G. R. Moloney, ${ }^{20}$ T. Nagamine, ${ }^{40}$ Y. Nagasaka, ${ }^{9}$ E. Nakano, ${ }^{29}$ M. Nakao, ${ }^{8}$ H. Nakazawa, ${ }^{8}$ Z. Natkaniec, ${ }^{26}$ S. Nishida, ${ }^{8}$ O. Nitoh,,${ }^{44}$ T. Nozaki, ${ }^{8}$ S. Ogawa, ${ }^{38}$ T. Ohshima, ${ }^{21}$ T. Okabe, ${ }^{21}$ S. Okuno, ${ }^{14}$ S. L. Olsen, ${ }^{7}$ W. Ostrowicz, ${ }^{26}$ H. Ozaki, ${ }^{8}$ P. Pakhlov, ${ }^{12}$ H. Palka, ${ }^{26}$ C. W. Park, ${ }^{35}$ N. Parslow, ${ }^{36}$ L. S. Peak, ${ }^{36}$ R. Pestotnik, ${ }^{13}$ L. E. Piilonen, ${ }^{46}$ N. Root, ${ }^{1}$ M. Rozanska, ${ }^{26}$ H. Sagawa, ${ }^{8}$ Y. Sakai, ${ }^{8}$ T. R. Sarangi, ${ }^{8}$ N. Sato, ${ }^{21}$ T. Schietinger, ${ }^{17}$ O. Schneider, ${ }^{17}$ J. Schümann, ${ }^{25}$ C. Schwanda, ${ }^{11}$ A. J. Schwartz, ${ }^{4}$ K. Senyo, ${ }^{21}$ M. E. Sevior, ${ }^{20}$ T. Shibata, ${ }^{28}$ H. Shibuya, ${ }^{38}$ B. Shwartz, ${ }^{1}$ V. Sidorov, ${ }^{1}$ J. B. Singh, ${ }^{31}$ A. Somov, ${ }^{4}$ N. Soni, ${ }^{31}$ R. Stamen, ${ }^{8}$ S. Stanič, ${ }^{45}, *$ M. Starič, ${ }^{13}$ K. Sumisawa, ${ }^{30}$ T. Sumiyoshi, ${ }^{43}$ O. Tajima, ${ }^{8}$ F. Takasaki, ${ }^{8}$ K. Tamai, ${ }^{8}$ N. Tamura, ${ }^{28}$ M. Tanaka, ${ }^{8}$ Y. Teramoto, ${ }^{29}$ X. C. Tian, ${ }^{32}$ K. Trabelsi, ${ }^{7}$ T. Tsukamoto, ${ }^{8}$ S. Uehara, ${ }^{8}$ T. Uglov, ${ }^{12}$ K. Ueno, ${ }^{25}$ S. Uno, ${ }^{8}$ P. Urquijo, ${ }^{20}$ Y. Ushiroda, ${ }^{8}$ G. Varner, ${ }^{7}$ K. E. Varvell, ${ }^{36}$ S. Villa, ${ }^{17}$ C. C. Wang, ${ }^{25}$ C. H. Wang, ${ }^{24}$ M.-Z. Wang, ${ }^{25}$ M. Watanabe, ${ }^{28}$ Y. Watanabe, ${ }^{42}$ Q. L. Xie, ${ }^{10}$ B. D. Yabsley, ${ }^{46}$ A. Yamaguchi, ${ }^{40}$ Y. Yamashita, ${ }^{27}$ M. Yamauchi, ${ }^{8}$ Heyoung Yang, ${ }^{34}$ J. Ying, ${ }^{32}$ J. Zhang, ${ }^{8}$ L. M. Zhang, ${ }^{33}$ Z. P. Zhang, ${ }^{33}$ V. Zhilich, ${ }^{1}$ D. Žontar, ${ }^{18,13}$ and D. Zürcher ${ }^{17}$
(Belle Collaboration)
${ }^{1}$ Budker Institute of Nuclear Physics, Novosibirsk
${ }^{2}$ Chiba University, Chiba
${ }^{3}$ Chonnam National University, Kwangju
${ }^{4}$ University of Cincinnati, Cincinnati, Ohio 45221
${ }^{5}$ University of Frankfurt, Frankfurt ${ }^{6}$ Gyeongsang National University, Chinju
${ }^{7}$ University of Hawaii, Honolulu, Hawaii 96822
${ }^{8}$ High Energy Accelerator Research Organization (KEK), Tsukuba
${ }^{9}$ Hiroshima Institute of Technology, Hiroshima
${ }^{10}$ Institute of High Energy Physics, Chinese Academy of Sciences, Beijing
${ }^{11}$ Institute of High Energy Physics, Vienna
${ }^{12}$ Institute for Theoretical and Experimental Physics, Moscow
${ }^{13}$ J. Stefan Institute, Ljubljana
${ }^{14}$ Kanagawa University, Yokohama
${ }^{15}$ Korea University, Seoul
${ }^{16}$ Kyungpook National University, Taegu
${ }^{17}$ Swiss Federal Institute of Technology of Lausanne, EPFL, Lausanne
${ }^{18}$ University of Ljubljana, Ljubljana
${ }^{19}$ University of Maribor, Maribor
${ }^{20}$ University of Melbourne, Victoria
${ }^{21}$ Nagoya University, Nagoya
${ }^{22}$ Nara Women's University, Nara
${ }^{23}$ National Central University, Chung-li
${ }^{24}$ National United University, Miao Li
${ }^{25}$ Department of Physics, National Taiwan University, Taipei
${ }^{26}$ H. Niewodniczanski Institute of Nuclear Physics, Krakow
${ }^{27}$ Nihon Dental College, Niigata
${ }^{28}$ Niigata University, Niigata

${ }^{29}$ Osaka City University, Osaka<br>${ }^{30}$ Osaka University, Osaka<br>${ }^{31}$ Punjab University, Chandigarh<br>${ }^{32}$ Peking University, Beijing<br>${ }^{33}$ University of Science and Technology of China, Hefei<br>${ }^{34}$ Seoul National University, Seoul<br>${ }^{35}$ Sungkyunkwan University, Suwon<br>${ }^{36}$ University of Sydney, Sydney NSW<br>${ }^{37}$ Tata Institute of Fundamental Research, Bombay<br>${ }^{38}$ Toho University, Funabashi<br>${ }^{39}$ Tohoku Gakuin University, Tagajo<br>${ }^{40}$ Tohoku University, Sendai<br>${ }^{41}$ Department of Physics, University of Tokyo, Tokyo<br>${ }^{42}$ Tokyo Institute of Technology, Tokyo<br>${ }^{43}$ Tokyo Metropolitan University, Tokyo<br>${ }^{44}$ Tokyo University of Agriculture and Technology, Tokyo<br>${ }^{45}$ University of Tsukuba, Tsukuba<br>${ }^{46}$ Virginia Polytechnic Institute and State University, Blacksburg, Virginia 24061<br>${ }^{47}$ Yonsei University, Seoul<br>${ }^{48}$ Princeton University, Princeton, New Jersey 08545<br>(Received 6 March 2005; published 8 June 2005)


#### Abstract

We present measurements of decay amplitudes and triple-product correlations in $B \rightarrow \phi K^{*}$ decays based on $253 \mathrm{fb}^{-1}$ of data recorded at the $\mathrm{Y}(4 S)$ resonance with the Belle detector at the KEKB $e^{+} e^{-}$ storage ring. The decay amplitudes for the three different helicity states are determined from the angular distributions of final-state particles. The longitudinal polarization amplitudes are found to be $0.45 \pm$ $0.05 \pm 0.02$ for $B^{0} \rightarrow \phi K^{* 0}$ and $0.52 \pm 0.08 \pm 0.03$ for $B^{+} \rightarrow \phi K^{*+}$ decays. $C P$ - and $T$-odd $C P$-violating triple-product asymmetries are measured to be consistent with zero.


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The vector-vector $B \rightarrow \phi K^{*}$ decay processes provide clear insights into the underlying $b \rightarrow s$ transition by virtue of their clear experimental signatures and relatively unambiguous theoretical interpretation, especially of the many angular correlations that can be formed among the final-state particles. The decays are described by second order penguin diagrams, the first order $b \rightarrow s$ transition being forbidden in the standard model (SM). The angular information allows the $C P$-even and $C P$-odd states that comprise the $B^{0} \rightarrow \phi K^{* 0}$ decay to be distinguished. Our previous measurement [1] and a recent report by $B A B A R$ [2] both suggest that the longitudinal polarization component differs from predictions based on the factorization assumption.

In this Letter we report on a further study of this anomaly that is based on a larger data sample and uses observables that are expected to be sensitive to the effects of new physics. We present the first full three-dimensional angular analysis for $B^{+} \rightarrow \phi K^{*+}$ and an extended study for $B^{0} \rightarrow$ $\phi K^{* 0}$. The decay modes $\phi \rightarrow K^{+} K^{-}, K^{* 0} \rightarrow K^{+} \pi^{-}$, $K^{*+} \rightarrow K_{S}^{0} \pi^{+}$, and $K^{*+} \rightarrow K^{+} \pi^{0}$ are considered. Charge conjugate modes are implied everywhere unless otherwise specified. We report measurements of direct $C P$ asymmetries, triple-product correlations and related $T$-odd $C P$-violating asymmetries [3], and other observables that are sensitive to new physics (NP) [4].

This analysis uses a data sample that contains $275 \times 10^{6}$ $B \bar{B}$ pairs collected on the $\Upsilon(4 S)$ resonance by belle detector [5] at the KEKB $e^{+} e^{-}$collider [6]. The Belle detector is a general purpose magnetic spectrometer equipped with a 1.5 T superconducting solenoid magnet. Charged tracks are reconstructed in a central drift chamber (CDC) and a silicon vertex detector (SVD). Photons and electrons are identified using a $\operatorname{CsI}(\mathrm{Tl})$ electromagnetic calorimeter (ECL) located inside the magnet coil. Charged particles are identified using specific ionization ( $d E / d x$ ) measurements in the CDC as well as information from aerogel Cherenkov counters (ACC) and time of flight counters (TOF).

Event reconstruction is performed as described in Ref. [1]. Candidate $B$ mesons are reconstructed from $\phi$ and $K^{*}$ candidates and are identified by the energy difference $\Delta E=E_{B}^{\text {cms }}-E_{\text {beam }}^{\text {cms }}$, the beam constrained mass $M_{\mathrm{bc}}=\sqrt{\left(E_{\text {beam }}^{\text {cms }}\right)^{2}-\left(p_{B}^{\text {cms }}\right)^{2}}$, and $K^{+} K^{-}$invariant mass ( $M_{K^{+} K^{-}}$), where $E_{\text {beam }}^{\text {cms }}$ is the beam energy in the center-of-mass (c.m.) system, and $E_{B}^{\mathrm{cms}}$ and $p_{B}^{\mathrm{cms}}$ are the c.m. energy and momentum of the reconstructed $B$ candidate. The $B$-meson signal region is defined as $M_{\mathrm{bc}}>$ $5.27 \mathrm{GeV} / c^{2},|\Delta E|<45 \mathrm{MeV}$, and $\left|M_{K^{+} K^{-}}-M_{\phi}\right|<$ $10 \mathrm{MeV} / c^{2}$. The invariant mass of the $K^{*} \rightarrow K \pi$ candidate is required to be less than $70 \mathrm{MeV} / c^{2}$ from the nominal $K^{*}$ mass. The signal region is enlarged to
$-100 \mathrm{MeV}<\Delta E<80 \mathrm{MeV}$ for $B^{+} \rightarrow \phi K^{*+}\left(K^{*+} \rightarrow\right.$ $K^{+} \pi^{0}$ ) because of the effects of shower leakage on the $\Delta E$ resolution. An additional requirement $\cos \theta_{K^{*}}<0.8$ is applied to reduce low momentum $\pi^{0}$ background, where $\theta_{K^{*}}$ is the angle between the direction opposite to the $B$ and the daughter kaon in the rest frame of $K^{*}$. These requirements do not affect our results based on a MC study. In the signal region, about $1 \%$ of the events have multiple candidates. The candidate with the smallest $\chi^{2}$ value from $B$ vertex finding and the best $\pi^{0}$ mass in the $K^{*+} \rightarrow K^{+} \pi^{0}$ decay is used.

The dominant background is $e^{+} e^{-} \rightarrow q \bar{q} \quad(q=$ $u, d, c, s)$ continuum production. Several variables including $S_{\perp}$ [7], the thrust angle, and the modified Fox-Wolfram moments defined in Ref. [8] are used to exploit the differences between the event shapes for continuum $q \bar{q}$ production (jetlike) and for $B$ decay (spherical) in the c.m. frame of the $\mathrm{Y}(4 S)$. These variables are combined into a single likelihood ratio $\mathcal{R}_{s}=\mathcal{L}_{s} /\left(\mathcal{L}_{s}+\mathcal{L}_{q \bar{q}}\right)$, where $\mathcal{L}_{s}\left(\mathcal{L}_{q \bar{q}}\right)$ denotes the signal (continuum) likelihood. The selection requirements on $\mathcal{R}_{s}$ are determined by maximizing the value of $N_{s} / \sqrt{N_{s}+\overline{N_{b}}}$ in each $B$-flavor-tagging quality region [9], where $N_{s}\left(N_{b}\right)$ represents the expected number of signal (background) events in the signal region.

Backgrounds from other $B$ decay modes such as $B \rightarrow$ $K^{+} K^{-} K^{*}, \quad B \rightarrow f_{0}(980) K^{*}\left(f_{0} \rightarrow K^{+} K^{-}\right), \quad B \rightarrow \phi K \pi$, $B \rightarrow K^{+} K^{-} K \pi$, and cross feed between the $\phi K^{*}$ and $\phi K$ decay channels are studied. The contributions from $B \rightarrow K^{+} K^{-} K^{*}$ and $B \rightarrow f_{0} K^{*}$ are estimated from a fit to $\Delta E, M_{\mathrm{bc}}$, and $M_{K^{+} K^{-}}$distributions. The $M_{K^{+} K^{-}}$distribution for $B \rightarrow K^{+} K^{-} K^{*}$ is determined from Monte Carlo (MC) simulations. The $f_{0}(980)$ line shape is obtained from MC, where an $S$-wave Breit-Wigner with a $61 \mathrm{MeV} / c^{2}$ intrinsic width [10] is assumed. The uncertainty in the $f_{0}(980)$ width $\left(40-100 \mathrm{MeV} / c^{2}\right)$ [11] is taken as a source of systematic error. The contributions from $B \rightarrow$ $K^{+} K^{-} K^{*}\left(B \rightarrow f_{0} K^{*}\right)$ are estimated together with the $\phi K^{*}$ signal and are found to be $1 \%$ to $7 \%$ ( $1 \%$ to $3 \%$ ) [12] of the signal yield. The background from $B \rightarrow \phi K \pi$ decays is evaluated with fits to the $K \pi$ invariant mass and is found to be about $1 \%$. The contamination from fourbody $B \rightarrow K^{+} K^{-} K \pi$ decays is checked by performing fits to the events in the $\phi \rightarrow K^{+} K^{-}$and $K^{*} \rightarrow K \pi$ mass sidebands and is found to be less than $1 \%$. To remove the

TABLE I. Number of events observed in the signal region $\left(N_{\mathrm{ev}}\right)$, signal yields $\left(N_{s}\right)$, and the direct $C P$ asymmetries $\left(A_{C P}\right)$ obtained in the fits, with statistical and systematic uncertainties.

| Mode | $N_{\mathrm{ev}}$ | $N_{s}$ | $A_{C P}$ |
| :--- | :---: | :---: | :---: |
| $\phi K^{* 0}$ | 309 | $173 \pm 16$ | $0.02 \pm 0.09 \pm 0.02$ |
| $\phi K^{*+}$ | 173 | $85_{-11}^{+12}$ | $-0.02 \pm 0.14 \pm 0.03$ |
| $K^{*+}\left(K_{S}^{0} \pi^{+}\right)$ | 76 | $37.9_{-7.0}^{+7.0}$ | $-0.14 \pm 0.21 \pm 0.04$ |
| $K^{*+}\left(K^{+} \pi^{0}\right)$ | 97 | $47.3_{-8.1}^{+9.1}$ | $0.09 \pm 0.19 \pm 0.04$ |

contamination from $\phi K$ decays, these decays are explicitly reconstructed and rejected.

The signal yields $\left(N_{s}\right)$ are extracted by extended unbinned maximum-likelihood fits performed simultaneously to the $\Delta E, M_{\mathrm{bc}}$, and $M_{K^{+} K^{-}}$distributions. Reconstructed $B$ candidates with $|\Delta E|<0.25 \mathrm{GeV}$, $M_{\mathrm{bc}}>5.2 \mathrm{GeV} / c^{2}$, and $M_{K^{+} K^{-}}<1.07 \mathrm{GeV} / c^{2}$ are included in the fits. The signal probability density functions (PDFs) are a single Gaussian in $M_{\mathrm{bc}}$, a core Gaussian plus a bifurcated Gaussian (Gaussian with different widths on either side of the mean) as the tail in the $\Delta E$ distribution, and a Breit-Wigner shape in $M_{K^{+}} K^{-}$. The means and widths of $\Delta E$ and $M_{\mathrm{bc}}$ are verified using $B \rightarrow J / \psi K^{*}$ decays. The mean and width of the $\phi$ mass peak are determined using an inclusive $\phi \rightarrow K^{+} K^{-}$data sample.

The PDF shapes for the continuum events are parametrized by an ARGUS function [13] in $M_{\mathrm{bc}}$, a linear function in $\Delta E$, and a sum of a threshold function and a BreitWigner function in $M_{K^{+} K^{-}}$. The parameters of the functions are determined by a fit to the events in the sideband. The signal and background yields are allowed to float in the fit while other PDF parameters are fixed. The direct $C P$ asymmetries, $A_{C P}=\frac{N(\bar{B} \rightarrow \bar{f})-N(B \rightarrow f)}{N(\bar{B} \rightarrow \bar{f})+N(B \rightarrow f)}$, are also studied. The measured signal yields and direct $C P$ asymmetries are summarized in Table I. The distributions of $\Delta E, M_{\mathrm{bc}}$, and $M_{K^{+} K^{-}}$are shown in Fig. 1.

The decay angles of a $B$-meson decaying to two vector mesons $\phi$ and $K^{*}$ are defined in the transversity basis [14]. The $x-y$ plane is defined to be the decay plane of $K^{*}$ and the $x$ axis is in the direction of the $\phi$ meson. The $y$ axis is perpendicular to the $x$ axis in the decay plane and is on the same side as the kaon from the $K^{*}$ decay. The $z$ axis is perpendicular to the $x-y$ plane according to the right-hand rule, $\theta_{\mathrm{tr}}\left(\phi_{\mathrm{tr}}\right)$ is the polar (azimuthal) angle with respect to the $z$ axis of the $K^{+}$from $\phi$ decay in the $\phi$ rest frame, and $\theta_{K^{*}}$ is defined earlier.


FIG. 1 (color online). Distributions of the $\Delta E, M_{\mathrm{bc}}$, and $M_{K^{+} K^{-}}$for $B^{0} \rightarrow \phi K^{* 0}$ (a), (b), (c), and for $B^{+} \rightarrow \phi K^{*+}$ (d), (e), (f), with other variables in signal region. Solid curves show the fit results. The continuum background components are shown by the dashed curves. The dark shaded areas represent the contributions from $B \rightarrow K^{+} K^{-} K^{*}$ and $B \rightarrow f_{0} K^{*}$ decays.

The distribution of the angles, $\theta_{K^{*}}, \theta_{\mathrm{tr}}$, and $\phi_{\mathrm{tr}}$ is given by [15]

$$
\begin{align*}
\frac{d^{3} R_{\phi K^{*}}\left(\phi_{\mathrm{tr}}, \cos \theta_{\mathrm{tr}}, \cos \theta_{K^{*}}\right)}{d \phi_{\mathrm{tr}} d \cos \theta_{\mathrm{tr}} d \cos \theta_{K^{*}}}= & \frac{9}{32 \pi}\left[\left|A_{\perp}\right|^{2} 2 \cos ^{2} \theta_{\mathrm{tr}} \sin ^{2} \theta_{K^{*}}+\left|A_{\|}\right|^{2} 2 \sin ^{2} \theta_{\mathrm{tr}} \sin ^{2} \phi_{\mathrm{tr}} \sin ^{2} \theta_{K^{*}}+\left|A_{0}\right|^{2} 4 \sin ^{2} \theta_{\mathrm{tr}} \cos ^{2} \phi_{\mathrm{tr}} \cos ^{2} \theta_{K^{*}}\right. \\
& +\sqrt{2} \operatorname{Re}\left(A_{\|}^{*} A_{0}\right) \sin ^{2} \theta_{\mathrm{tr}} \sin 2 \phi_{\mathrm{tr}} \sin 2 \theta_{K^{*}}-\eta \sqrt{2} \operatorname{Im}\left(A_{0}^{*} A_{\perp}\right) \sin 2 \theta_{\mathrm{tr}} \cos \phi_{\mathrm{tr}} \sin 2 \theta_{K^{*}} \\
& \left.-2 \eta \operatorname{Im}\left(A_{\|}^{*} A_{\perp}\right) \sin 2 \theta_{\mathrm{tr}} \sin \phi_{\mathrm{tr}} \sin ^{2} \theta_{K^{*}}\right] \tag{1}
\end{align*}
$$

where $A_{0}, A_{\|}$, and $A_{\perp}$ are the complex amplitudes of the three helicity states in the transversity basis with the normalization condition $\left|A_{0}\right|^{2}+\left|A_{\|}\right|^{2}+\left|A_{\perp}\right|^{2}=1$, and $\eta=$ $+1(-1)$ corresponds to $B(\bar{B})$ mesons and is determined from the charge of the kaon or pion in the $K^{*}$ decay. The longitudinal polarization component is denoted by $A_{0}$; $A_{\perp}\left(A_{\|}\right)$is the transverse polarization along the $z$ axis ( $y$ axis). The value of $\left|A_{\perp}\right|^{2}\left(\left|A_{0}\right|^{2}+\left|A_{\|}\right|^{2}\right)$ is the $C P$-odd ( $C P$-even) fraction in the decay $B \rightarrow \phi K^{* 0}$ [15]. The presence of final-state interactions (FSI) results in phases that differ from either 0 or $\pm \pi$.

The complex amplitudes are determined by performing an unbinned maximum-likelihood fit to the $B \rightarrow \phi K^{*}$ candidates in the signal region. The combined likelihood is given by

$$
\begin{equation*}
\mathcal{L}=\prod_{i}^{N_{\mathrm{ev}}} \epsilon\left(\phi_{\mathrm{tr}}, \cos \theta_{\mathrm{tr}}, \cos \theta_{K^{*}}\right) \sum_{j} f_{j} R_{j}\left(\phi_{\mathrm{tr}}, \cos \theta_{\mathrm{tr}}, \cos \theta_{K^{*}}\right) \tag{2}
\end{equation*}
$$

where $j$ denotes the contributions from $\phi K^{*}, q \bar{q}$, $K^{+} K^{-} K^{*}$, and $f_{0} K^{*} ; R_{j}$ is the angular distribution function (ADF). The ADF $R_{q \bar{q}}$ is determined from sideband data, and $R_{K^{+} K^{-} K^{*}}$ from events with $1.04 \mathrm{GeV} / c^{2}<M_{K^{+} K^{-}}<$ $1.075 \mathrm{GeV} / c^{2} ; R_{f_{0} K^{*}}$ is obtained from $B \rightarrow f_{0} K^{*} \mathrm{MC}$ events. The detection efficiency $(\boldsymbol{\epsilon})$ is determined using


FIG. 2 (color online). Projected distributions of the three transversity angles for $B^{0} \rightarrow \phi K^{* 0}$ (a), (b), (c), and for $B^{+} \rightarrow \phi K^{*+}$ (d), (e), (f). Solid lines show the fit results. The points with error bars show the efficiency corrected data after background subtraction. The two $K^{*+}$ decay modes are combined in (d), (e), (f). The discontinuity in (d) is due to the requirement of $\cos \theta_{K^{*}}<$ 0.8 in $B^{+} \rightarrow \phi K^{*+}\left(K^{*+} \rightarrow K^{+} \pi^{0}\right)$.

MC simulations assuming a phase space decay. The fractions $f_{j}$ are parametrized as a function of $\Delta E, M_{\mathrm{bc}}$, and $M_{K^{+} K^{-}}$. The value of $\arg \left(A_{0}\right)$ is set to zero and $\left|A_{\|}\right|^{2}$ is calculated from the normalization condition. The four parameters $\left[\left|A_{0}\right|^{2},\left|A_{\perp}\right|^{2}, \arg \left(A_{\|}\right)\right.$, and $\left.\arg \left(A_{\perp}\right)\right]$ are determined from the fit. There is a twofold ambiguity in the solutions for the phases; the chosen set of solutions is the one suggested in Ref. [16]. Figure 2 shows the angular distributions with projections of the fit superimposed. The obtained amplitudes are summarized in Table II.

The systematic uncertainties on the amplitudes are dominated by the efficiency modeling ( $4 \%-5 \%$ ), continuum background (3-4\%), slow pion efficiency ( $2 \%-3 \%$ ), and $K^{+} K^{-} K^{*}$ ADF ( $1 \%-2 \%$ ). The remaining possible systematic errors, such as the angular resolution, signal yields, background from higher $K^{*}$ states, and width of the $f_{0}$, are estimated to be less than $1 \%$.

The triple product for a $B$ meson decay to two vector mesons takes the form $\vec{q} \cdot\left(\vec{\epsilon}_{1} \times \vec{\epsilon}_{2}\right)$, where $\vec{q}$ is the momentum of one of the vector mesons, and $\overrightarrow{\boldsymbol{\epsilon}}_{1}$ and $\overrightarrow{\boldsymbol{\epsilon}}_{2}$ are the polarizations of the two vector mesons. The following two $T$-odd [3,17] quantities

$$
\begin{equation*}
A_{T}^{0}=\operatorname{Im}\left(A_{\perp} A_{0}^{*}\right), \quad A_{T}^{\|}=\operatorname{Im}\left(A_{\perp} A_{\|}^{*}\right) \tag{3}
\end{equation*}
$$

provide information on the asymmetry of the triple products. The SM predicts very small values for $A_{T}^{0}$ and $A_{T}^{\|}$. The comparison of these triple-product asymmetries $\left(A_{T}^{0}\right.$ and $\left.A_{T}^{\|}\right)$with the corresponding quantities for the $C P$-conjugate decays ( $\bar{A}_{T}^{0}$ and $\bar{A}_{T}^{\|}$) provides an observable sensitive to $T$-odd $C P$ violation.

Additional variables that can be accessed by angular analyses are suggested in Ref. [4] and are given by

TABLE II. The decay amplitudes obtained for $B^{0} \rightarrow \phi K^{* 0}$ and $B^{+} \rightarrow \phi K^{*+}$. The first uncertainties are statistical and the second are systematic.

| Mode | $\phi K^{* 0}$ | $\phi K^{*+}$ |
| :--- | :---: | :---: |
| $\left\|A_{0}\right\|^{2}$ | $0.45 \pm 0.05 \pm 0.02$ | $0.52 \pm 0.08 \pm 0.03$ |
| $\left\|A_{\perp}\right\|^{2}$ | $0.30 \pm 0.06 \pm 0.02$ | $0.19 \pm 0.08 \pm 0.02$ |
| $\arg \left(A_{\\|}\right)(\mathrm{rad})$ | $2.39 \pm 0.24 \pm 0.04$ | $2.10 \pm 0.28 \pm 0.04$ |
| $\arg \left(A_{\perp}\right)(\mathrm{rad})$ | $2.51 \pm 0.23 \pm 0.04$ | $2.31 \pm 0.30 \pm 0.07$ |

TABLE III. The measured decay amplitudes and tripleproduct correlations in the $B^{0}$ and $\bar{B}^{0}$ samples.

| Mode | $B^{0}$ | $\bar{B}^{0}$ |
| :--- | :---: | :---: |
| $\left\|A_{0}\right\|^{2}$ | $0.39 \pm 0.08 \pm 0.03$ | $0.51 \pm 0.07 \pm 0.02$ |
| $\left\|A_{\perp}\right\|^{2}$ | $0.37 \pm 0.09 \pm 0.02$ | $0.25 \pm 0.07 \pm 0.01$ |
| $\arg \left(A_{\\|}\right)(\mathrm{rad})$ | $2.72_{-0.38}^{+0.46} \pm 0.14$ | $2.08 \pm 0.31 \pm 0.04$ |
| $\arg \left(A_{\perp}\right)(\mathrm{rad})$ | $2.81 \pm 0.36 \pm 0.11$ | $2.22 \pm 0.35 \pm 0.05$ |
| $A_{T}^{0}$ | $0.13_{-0.14}^{+0.11} \pm 0.04$ | $0.28 \pm 0.08 \pm 0.01$ |
| $A_{T}^{\Pi}$ | $0.03 \pm 0.08 \pm 0.01$ | $0.03 \pm 0.06 \pm 0.01$ |

$$
\begin{array}{ll}
\Lambda_{\perp i}=-\operatorname{Im}\left(A_{\perp} A_{i}^{*}-\bar{A}_{\perp} \bar{A}_{i}^{*}\right), & \Lambda_{\| 0}=\operatorname{Re}\left(A_{\|} A_{0}^{*}+\bar{A}_{\|} \bar{A}_{0}^{*}\right), \\
\Sigma_{\perp i}=-\operatorname{Im}\left(A_{\perp} A_{i}^{*}+\bar{A}_{\perp} \bar{A}_{i}^{*}\right), & \Sigma_{\| 0}=\operatorname{Re}\left(A_{\|} A_{0}^{*}-\bar{A}_{\|} \bar{A}_{0}^{*}\right), \\
\Lambda_{\lambda \lambda}=\frac{1}{2}\left(\left|A_{\lambda}\right|^{2}+\left|\bar{A}_{\lambda}\right|^{2}\right), \quad \Sigma_{\lambda \lambda}=\frac{1}{2}\left(\left|A_{\lambda}\right|^{2}-\left|\bar{A}_{\lambda}\right|^{2}\right), \tag{4}
\end{array}
$$

where the subscript $\lambda$ is either $0, \|$, or $\perp$, and $i$ is 0 or $\|$. The variables $\Lambda_{\perp 0}$ and $\Lambda_{\perp \|}$ are sensitive to $T$-odd $C P$-violating new physics. The following equations should hold in the absence of NP:

$$
\begin{equation*}
\Sigma_{\lambda \lambda}=0, \quad \Sigma_{\| 0}=0, \quad \Lambda_{\perp i}=0 \tag{5}
\end{equation*}
$$

By separating $B^{0}$ and $\bar{B}^{0}$ samples and rearranging fitting parameters in the unbinned maximum-likelihood fit, we measured the decay amplitudes for the $B^{0}$ and $\bar{B}^{0}$, the triple-product correlations, and the other NP-sensitive observables as given in Tables III and IV. The $T$-odd $C P$-violating variables $\Lambda_{\perp 0}$ and $\Lambda_{\perp \|}$ are measured to be $0.16_{-0.14}^{+0.16} \pm 0.03$ and $0.01 \pm 0.10 \pm 0.02$, respectively, consistent with the SM predictions.

In summary, improved measurements of the decay amplitudes for $B \rightarrow \phi K^{*}$, based on fits to angular distributions in the transversity basis, are presented. The results are consistent with our previous measurements [1] with improved precision. The measured value of $\left|A_{\perp}\right|^{2}$ shows that $C P$-odd $\left(\left|A_{\perp}\right|^{2}\right)$ and $C P$-even $\left(\left|A_{0}\right|^{2}+\left|A_{\|}\right|^{2}\right)$ components are present in $\phi K^{*}$ decays in a ratio of about 1:2. Phases of both $A_{\perp}$ and $A_{\|}$differ from zero or $-\pi$ by 4.3 standard deviations $(\sigma)$, which provides evidence for the presence of final-state interactions. The measured direct $C P$ asymmetries in these modes are consistent with zero; the corresponding $90 \%$ confidence level limits are $-0.14<A_{C P}\left(\phi K^{* 0}\left(K^{+} \pi^{-}\right)\right)<0.17 \quad$ and $\quad-0.25<$ $A_{C P}\left(\phi K^{*+}\right)<0.22$. Measurements of the $T$-odd $C P$-violation sensitive differences between triple-product asymmetries, $A_{T}^{0}-\bar{A}_{T}^{0}$, and $A_{T}^{\|}-\bar{A}_{T}^{\|}$, indicate no significant deviations from zero, consistent with $B A B A R$ measurements [2]. Our data show no significant deviations from the expectations: $\Sigma_{\lambda \lambda}=0, \Sigma_{\| 0}=0$, and $\Lambda_{\perp i}=0$, indicating no evidence for new physics.

TABLE IV. $\Lambda$ and $\Sigma$ values obtained from the decay amplitudes measured for $B^{0}$ and $\bar{B}^{0}$ separately.

| $\Lambda_{00}=0.45 \pm 0.05 \pm 0.02$ | $\Sigma_{00}=-0.06 \pm 0.05 \pm 0.01$ |
| :---: | :---: |
| $\Lambda_{\\| \\| \\|}=0.24 \pm 0.06 \pm 0.02$ | $\Sigma_{\\| \\| \\|}=-0.01 \pm 0.06 \pm 0.01$ |
| $\Lambda_{\perp \perp}=0.31 \pm 0.06 \pm 0.01$ | $\Sigma_{\perp \perp}=0.06 \pm 0.05 \pm 0.01$ |
| $\Sigma_{\perp 0}=-0.41_{-0.14}^{+0.16} \pm 0.04$ | $\Lambda_{\perp 0}=0.16_{-0.14}^{+0.16} \pm 0.03$ |
| $\Sigma_{\perp \\|}=-0.06 \pm 0.10 \pm 0.01$ | $\Lambda_{\perp \\|}=0.01 \pm 0.10 \pm 0.02$ |
| $\Lambda_{\\| 0}=-0.45 \pm 0.11 \pm 0.01$ | $\Sigma_{\\| 0}=-0.11 \pm 0.11 \pm 0.02$ |

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*On leave from Nova Gorica Polytechnic, Nova Gorica.
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