Molecular-Dynamics Study of the Crystal Structure of Iron Under the Earth's Inner Core Conditions

Hua Yang[1], Lei Wan[1], Yunguo Li[1,2*], Lidunka Vočadlo[3], John Brodholt[3,4]

[1]*State Key Laboratory of Lithospheric and Environmental Coevolution, School of Earth and Space Sciences, University of Science and Technology of China, Hefei 230026, China*
[2]*Deep Space Exploration Laboratory, Hefei 230026, China*
[3]*Department of Earth Sciences, University College London, Gower Street, London WC1E 6BT, United Kingdom*
[4]*Centre for Planetary Habitability, University of Oslo, Oslo, Norway*

*Corresponding author: Yunguo Li (liyunguo@ustc.edu.cn)

Abstract: The crystal structure of Earth's solid inner core is fundamental to understanding the chemical composition and dynamical evolution of the core. However, despite extensive research, the structure still remains controversial with competing hypotheses regarding the stability of various Fe phases (e.g., bcc, fcc, and hcp). In this paper, we review the studies on the crystal structure of Fe under inner core conditions, and find, in line with previous work, that the main challenges come from the small energy differences between these structures. This has led to a variety of different conclusions across varying theoretical methods and precision, including *ab initio*, force field and machine learning methods. To address this problem, we employ a Bain path thermodynamic integration approach to reach consistent conclusions among different methods; we find that bcc Fe is mechanically stable but thermodynamically less stable under inner core conditions. Using the energetics from the Bain path method as a benchmark, we establish the requirements for converging free energy calculations through a two-phase thermodynamic modelling approach. These calculations confirm that the hcp phase is the most stable, exhibiting the highest melting temperature regardless of the method used. This unified conclusion on the hcp phase as the stable crystal structure provides a robust foundation for future studies on Earth's core.

30 **Plain Language Summary:** Understanding the crystal structure of Earth's solid inner core

31 is crucial for interpreting its chemical composition and dynamical evolution. Despite extensive

32 efforts, the phase stability of iron (e.g., bcc, fcc, hcp) under core conditions remains heavily

33 debated. The extreme *P-T* conditions of the inner core present a significant challenge to

34 experiments, while the difficulty in theoretical studies stems from the minute energy differences

35 among these structures. In this study, we introduce a thermodynamic-integration framework

36 based on the Bain path, which offers enhanced accuracy and serves as a rigorous benchmark

37 for evaluating phase-stability predictions. Applying this approach with stringent convergence

38 criteria, we demonstrate that all commonly used potentials and computational methods

39 uniformly confirm bcc as a metastable phase while hcp as the most stable phase under core

40 conditions. Our findings reconcile previous disparities and establish a solid thermodynamic

41 foundation for future studies of inner-core properties and dynamics.

42

43 **Key Points:**

44 1. Bcc Fe is mechanically stable under inner core conditions from either *ab initio* or force

45   field methods

46 2. The thermodynamic metastability of bcc Fe is independent of the simulation cell size

47 3. Hcp Fe has the highest melting temperature thus being the most stable phase in the Earth's

48   inner core

49

1. Introduction

The Earth's core, located ~2890 km beneath the surface with a radius of ~3480 km, comprises a solid inner core crystallising out from a liquid outer core (Dziewonski & Anderson, 1981). Understanding the composition and structure of the core is essential for comprehending various aspects of Earth's long-term evolution (e.g., Hirose et al., 2021). The crystal structure of the solid inner core is particularly important for determining the partitioning and abundance of light elements between the inner and outer core, as well as the core's temperature profile because of the different chemical potentials, densities and melting temperatures of various iron crystal structures. Previous studies suggest that the solid inner core is primarily composed of an Fe-rich solid solution, which may include substitutional and/or interstitial solid solutions of Fe with alloying elements such as Ni, Si, S, C, and H (Hikosaka et al., 2022; Li et al., 2018; Litasov & Shatskiy, 2016). Fe compounds like Fe_7C_3 and Fe_2S are unlikely to be significant constituents of the inner core as the eutectic points contain high concentrations of light elements and exhibit densities much lower than that of the inner core (Li et al., 2016; Tateno et al., 2019). Although it is well established that the inner core is primarily composed of Fe solid solution, the crystalline structure of the inner core remains debated.

The changes in the crystal structure of Fe at varying pressure and temperature (*P-T*) conditions are a critical scientific issue of interest in high-pressure physics and planetary sciences. At ambient *P-T* conditions, Fe exhibits a body-centred cubic (bcc) structure (α phase, which is not the close-packed with a space utilization rate of 68%); as temperature increases (~1185 K), it transforms into a face-centred cubic (fcc) structure (γ phase, stacking mode of ABCABC, close-packed with the highest space utilization rate of 74%), and at higher temperatures (~1666−1901 K), it reverts to a paramagnetic bcc structure (δ phase); while when the pressure exceeds ~15 GPa, it transitions to a hexagonal close-packed (hcp) structure (ε phase, stacking mode of ABAB with the highest space utilization rate of 74%) (Dewaele et al., 2006; Kraus et al., 2022; Mikhaylushkin et al., 2007; Pushcharovsky, 2019; Shen et al., 1998). Despite considerable efforts which have been made to investigate the phase diagram of Fe and its alloys under high *P-T* conditions, the precise crystalline structure of the inner core still remains controversial (Anzellini et al., 2013; Belonoshko et al., 2003; 2017; Dubrovinsky et al., 2007; Matsui &

79   Anderson, 1997; Ross et al., 1990; Stixrude, 2012; Sun et al., 2024; Tateno et al., 2010; Vočadlo

80   et al., 2003). This has led to discrepancies in the inferred physical and chemical properties of

81   the core, including estimates of core temperature (Alfè, 2009; Belonoshko et al., 2021; Boehler,

82   1993; Li et al., 2020; Sun et al., 2023; Williams et al., 1987), elastic properties (Ikuta et al.,

83   2022; Li et al., 2018; Martorell et al., 2015), seismic anisotropy (Belonoshko, Simak et al.,

84   2022; Sha & Cohen, 2010; Steinle-Neumann et al., 2001; Vočadlo, Wood, Alfè & Price, 2008),

85   transport properties (Belonoshko et al., 2019; Gleason & Mao, 2013; Li & Scandolo, 2022; Xu

86   et al., 2025), and thermal evolution of nucleation processes (Davies et al., 2019; Sun et al., 2022;

87   Wilson et al., 2023).

88   The reason for the continual uncertainty in the correct phase of Fe at inner-core (IC) conditions

89   is that accurately determining the crystal structure of Fe at the extreme *P-T* conditions of the

90   Earth's core is a significant challenge. Early experiments conducted at room temperature by

91   Brown & McQueen (1986) measured the elasticities of Fe under core pressures using shock

92   wave techniques. They revealed discontinuous changes in Fe sound velocities, indicating a

93   possible transition from hcp to fcc structure in the inner core. Subsequent experiments

94   employing laser-heated diamond anvil cell (LHDAC) techniques not only suggested the

95   potential presence of a stable bcc structure in the core (Dubrovinsky et al., 2007; Matsui &

96   Anderson, 1997; Ross et al., 1990), but also demonstrated that the fcc structure could be stable

97   within the *P-T* range of the inner core, exhibiting stability comparable to that of the hcp

98   structure (Mikhaylushkin et al., 2007). Collectively, these previous findings suggested that the

99   actual structure of the core may involve a complex phase with significant stacking faults.

100   Advances in experimental techniques allowed later studies using LHDAC and laser-driven

101   shock waves combined with X-ray diffraction to achieve *in situ* measurements of Fe crystal

102   structures under high *P-T* conditions (Anzellini et al., 2013; Hrubiak et al., 2018; Kraus et al.,

103   2022; Kuwayama et al., 2008; Sinmyo et al., 2019; Tateno et al., 2010; Turneaure et al., 2020;

104   Zhang et al., 2023). However, discrepancies remain regarding the stability of hcp and bcc

105   structures in these experiments. For instance, Hrubiak et al. (2018) reported the stabilisation of

106   bcc, while Tateno et al. (2010) and other groups predominantly observed hcp (Anzellini et al.,

107   2013; Kraus et al., 2022; Kuwayama et al., 2008; Sinmyo et al., 2019; Turneaure et al., 2020;

108   Zhang et al., 2023). These uncertainties are largely due to the challenges of experiments in

109   simultaneously achieving the extreme *P-T* conditions (~330–360 GPa, ~5000–7000 K) of the

110   inner core (Anderson, 2003), making it very difficult to reach a consensus among these

111   experimental results to date.

112   From a theoretical perspective, a major challenge in precisely determining the crystal structure

113   of the Earth's inner core lies in the closely competitive energies—on the order of tens of

114   meV/atom between the various possible Fe phases, including bcc, fcc, and hcp structures

115   (Belonoshko et al., 2011, 2021; Sun et al., 2023; Vočadlo et al., 2003; Vočadlo, Wood, Alfè, &

116   Price, 2008). This energy competition leads to inconsistent conclusions across different

117   methodologies, force fields, system sizes, and levels of computational precision (Belonoshko

118   et al., 2017; Cui et al., 2013; Li & Scandolo, 2024a; Schultz et al., 2018; Stixrude & Cohen,

119   1995; Vočadlo et al., 2000). For instance, discrepancies arise between *ab initio* calculations

120   using small cells and empirical potential simulations employing much larger cells (Belonoshko

121   et al., 2017; Vočadlo et al., 2003). Variations in methodologies, as well as in the precision of

122   vibrational entropy and free energy calculations, can result in contradictory conclusions

123   (Belonoshko et al., 2021; Li & Scandolo, 2024a; Sun et al., 2023), even when identical system

124   sizes and the same methods (EAM) are used (Belonoshko et al., 2017; Schultz et al., 2018).

125   Consequently, these theoretical inconsistencies significantly impede a clear and unified

126   understanding of both the crystalline structure and the associated properties of the Earth's inner

127   core.

128   Indeed, a central theoretical debate on the crystal structure of Fe in the inner core is the stability

129   of the bcc phase, particularly with respect to its mechanical and thermodynamic stabilities,

130   while its dynamic stability at high temperatures has been firmly established (Côté et al., 2010;

131   Luo et al., 2010; Vočadlo et al., 2003). According to density functional theory (DFT)

132   calculations with small simulation cells, the bcc structure of Fe is generally believed to be

133   unstable at IC conditions, mainly because it exhibits mechanical instability when subjected to

134   tetragonal strain at high pressures (Soderlind et al., 1996; Stixrude & Cohen, 1995; Vočadlo,

135   Wood, Gillan, et al., 2008). Even consideration of extremely high temperatures and the

136   incorporation of appropriate amounts of light elements, such as Si and S, cannot overcome this

137   instability (Cui et al., 2013). However, this hypothesis has been recently challenged by studies

138   proposing that the mechanical stability of the bcc structure may be enhanced by self-diffusion

139   (Fe atoms diffusing like liquid, yet preserving all the properties of a solid), as demonstrated by

140   the Born stability criteria through 2000-atom *ab initio* calculations (Belonoshko, Simak, et al.,

141   2022) and 1000-atom deep-learning potential simulations (Li & Scandolo, 2024a). Further

142   clarification is needed to obtain a clearer understanding of the mechanical stability of bcc Fe at

143   IC conditions.

144   However, it is also the case that it has long been considered that the bcc phase is

145   thermodynamically less stable with respect to the hcp and fcc structures, as evidenced by

146   thermodynamic integration (TI) free energy calculations using various force fields, cell sizes,

147   and reference systems (González-Cataldo & Militzer, 2023; Li & Scandolo, 2024b; Sun et al.,

148   2023; Vočadlo et al., 2003; 2008). An alternative perspective has been put forward by

149   Belonoshko et al. (2017), who proposed that the bcc structure may exhibit stability under

150   specific conditions involving a large number of atoms ($N \geq 1024$) and extremely high

151   temperatures (~7000 K). This thermodynamic stability was linked to a cooperative diffusion

152   (collective drifting of Fe atoms) occurring in the <110> direction within an ultra-large system

153   only, accompanied by a substantial increase in vibrational entropy (derived from the power

154   spectrum of the velocity autocorrelation function), which is attributed to size-dependent

155   diffusion effects. However, efforts to replicate this thermodynamic stability (calculated by TI)

156   and the associated size effects using identical force fields, system sizes, and temperature-

157   pressure conditions have proven unsuccessful (Schultz et al., 2018). Moreover, recent *ab initio*

158   simulations (Ghosh et al., 2023) and deep-learning potential calculations (Li & Scandolo, 2024a)

159   have demonstrated that cooperative diffusion behavior in the bcc structure can manifest even

160   within a relatively small unit cell containing as few as 128 atoms. Nonetheless, their findings

161   regarding the thermodynamic stability of the bcc phase and the direction of diffusion are

162   inconsistent (Belonoshko et al., 2017; Ghosh et al., 2023; Li & Scandolo, 2024a). This

163   discrepancy implies that the self-diffusion behavior of bcc Fe is not strongly dependent on the

164   simulation size, whereas the accuracy and convergence of free energy calculations may be

165   significantly influenced by the system size (Belonoshko et al., 2011; 2017), which, in turn, may

166   affect the thermodynamic results.

167   In light of these theoretical challenges and discrepancies, a more precise approach to free energy

168   calculations and a comprehensive understanding of size effects is crucial for resolving the long-

169   standing controversy regarding the stability of competing Fe phases under IC conditions.

170   Generally, all theoretical results should be reproducible; however, thermodynamic calculations,

171   particularly those involving entropy, impose stringent requirements on both simulation cell

172   sizes and durations. Consequently, earlier studies may harbor inherent uncertainties, leading to

173   conflicting conclusions. To address this, we propose using the Bain Path Thermodynamic

174   Integration (BP-TI) technique (Ozolins, 2009; Vočadlo, Wood, Gillan, et al., 2008), which

175   simultaneously evaluates the mechanical and thermodynamic stabilities of the bcc and fcc

176   phases by integrating the differences in internal stress. The BP-TI does not work for bcc-hcp

177   and fcc-hcp since there is no reversible path for these transitions. The BP-TI method eliminates

178   the need for an additional reference system and avoids direct entropy calculations to determine

179   thermodynamic properties. Instead, it calculates the system's free energy by integrating internal

180   stress differences, which converge significantly faster with cell size compared to entropies and

181   energies. This approach provides an ideal tool for testing various theoretical methods with

182   different levels of precision, including *ab initio* calculations, force field models, and machine

183   learning methods. Furthermore, the results may also serve as a benchmark for other free energy

184   calculation methods.

185   Using these techniques, we hope to clarify the factors influencing the stabilities of Fe structures

186   under core conditions and reach a unified consensus on the inner core crystalline structure. The

187   rest of the paper is organized as follows: in Section 2 we introduce the techniques discussed

188   and used in this study; Section 3.1 presents the stability of the bcc and fcc phases using the BP-

189   TI method; Section 3.2 presents the results of free energy calculation for bcc, fcc and hcp Fe

190   using two-phase thermodynamic (2PT) method, building on the results of the BP-TI

191   calculations; in Section 3.3 we present their melting temperatures and discuss their possible

192   occurrence in the core; Section 4 summarises the main findings and conclusions.

193

194   **2. Methods**

195   In this section, we introduce the techniques that will be used and discussed in this study. These

196   include the two widely used EAM potentials and the AIMD method used in earlier work. The

197   BP-TI method was previously used to evaluate the mechanical and thermodynamic stabilities

198   of the bcc and fcc phases under IC conditions (Cui et al., 2013; Vočadlo, Wood, Gillan, et al.,

199   2008). The energetics from the BP-TI method can be used to benchmark the free energy

200   calculation. We also introduce the 2PT method that can treat both the solid and liquid states,

201   allowing direct calculation of the free energies of diffusive system.

202   **2.1 Bain path thermodynamic integration**

203   The bcc↔fcc transformation can be continuously connected through a straightforward

204   tetragonal path, known as the Bain path (Bain, 1924). This transformation is reversible and does

205   not undergo any first-order phase transition. Therefore, in the spirit of the thermodynamic

206   integration technique, the free energy differences can be calculated by integrating the reversible

207   work required to drive the system from the reference state to the target state (Frenkel & Smit,

208   2002). Importantly, integrating along the Bain path corresponds to treating each point on the

209   integral path as the reference frame for the subsequent point, thus eliminating the necessity for

210   introducing additional reference systems. This characteristic is a key factor that enables the BP-

211   TI method to achieve high-precision free energy calculations. Another significant advantage of

212   this approach is that by integrating the work done by internal stresses, the convergence of these

213   stresses is less dependent on the simulation cell size, thereby facilitating more rapid free energy

214   convergence. Consequently, the mechanical and thermodynamic stability between bcc and fcc

215   structures can be accurately determined by calculating the free energy difference during the

216   bcc↔fcc phase transition.

217   The tetragonal strain involves distorting the bcc lattice by altering the c/a ratio while

218   maintaining constant volume. Under this strain, both bcc and fcc structures can transform

219   smoothly into one another, as there are two special cases of the body-centred tetragonal (bct)

220   lattice for these structures: bcc corresponds to c/a = 1 and fcc to c/a = $\sqrt{2}$ (Stixrude & Cohen,

221   1995). To facilitate the integration, as outlined by Ozolins (2009), it is more convenient to

222   introduce a tetragonal distortion parameter τ that is equivalent to the previously mentioned c/a

223   ratio. Then the bct lattice with a volume of a^3 can be described by the vectors $\mathbf{a} = (a/\tau^{1/2}, 0, 0)$,

224    $\mathbf{b} = (0, a/\tau^{1/2}, 0)$, and $\mathbf{c} = (0, 0, a\tau)$. Clearly, $\tau = 1$ for the bcc structure, and $\tau = 2^{1/3}$ for the fcc

225   structure. The work (w) associated with an infinitesimal tetragonal strain can be evaluated using

$$dw = f \cdot du = \sum_\alpha A_\alpha \, \sigma_{\alpha\alpha} du_\alpha \tag{1}$$

227   where f is the force, the summation is taken over $\alpha = x, y, z$. A_α represents the area of the

228   faces of lattice cell perpendicular to the axial, $\sigma_{\alpha\alpha}$ is the principal component of stress tensor

229   (the contributions of non-principal components $\sigma_{\alpha\beta}$ are 0 as they are perpendicular to the

230   displacements of lattice faces), and du_α is the elastic displacement of lattice faces. Since $A_x =$

231    $A_y = a^2 \tau^{1/2}$, $A_z = a^2/\tau$, $u_x = u_y = a/\tau^{1/2}$, and $u_z = a\tau$, Equation (1) can be reduced to

$$dw = a^3[\sigma_{zz} - (\sigma_{xx} + \sigma_{yy})/2]/\tau \, d\tau \tag{2}$$

233   By taking the integral on both sides of Equation (2), we can obtain the Helmholtz free energy

234   difference ΔF_V between the bct and bcc phases along the Bain path when we choose the bcc

235   phase ($\tau = 1$) as the reference system:

$$\Delta F_V = \int dw = \int a^3[\sigma_{zz} - (\sigma_{xx} + \sigma_{yy})/2]/\tau \, d\tau \tag{3}$$

237   The Gibbs free energy of the bct lattice at reference pressure ($G_{\tau \to 1}$) is calculated by integrating

238   its equation of state:

$$G_{\tau \to 1} = F_\tau + P_\tau V_1 + \int_{P_\tau}^{P_1} V \, dP \tag{4}$$

240   where F_τ is the Helmholtz free energy, P_τ is the pressure of the bct phase after applying the

241   tetragonal strain, while P_1 and V_1 are the pressure and volume of the bcc phase, respectively.

242   The third term V represents the equation of state of the bct lattice. The Gibbs free energy of

243   the bcc phase (G_1) is expressed as:

$$G_1 = F_1 + P_1 V_1 \tag{5}$$

245   where F_1 is the Helmholtz free energy of the bcc phase. Then, the Gibbs free energy difference

246    $\Delta G_{P\tau}$ between the bct and bcc phases along the Bain path at isobaric pressure can be evaluated

247   by the following equation:

248
$$\Delta G_{P\tau} = G_{\tau \to 1} - G_1 = \Delta F_V + (P_\tau - P_1)V_1 + \int_{P_\tau}^{P_1} V \, dP \tag{6}$$

249 The shape and position of the free energy difference curves, ΔF_V and $\Delta G_{P\tau}$, decisively

250 indicate the mechanical and thermodynamic stability of bcc and fcc structures.

251 **2.2 Two-phase thermodynamic model**

252 The 2PT model (Lin et al., 2003) was also employed to compute the entropy and free energy of

253 the different Fe phases under inner core *P-T* conditions. This involves decomposing the

254 Velocity Autocorrelation Function (VACF) and its associated Vibrational Density of States

255 (VDoS) into a gas-like diffusion component and a solid-like vibrational component. The

256 vibrational entropies of these two components were calculated using the Hard Sphere (HS)

257 model and the Harmonic Oscillator (HQ) model, respectively (Desjarlais, 2013; Lai et al., 2012).

258 The VACF (Φ), derived from the time evolution of velocities of *N* atoms, and its VDoS (*F*),

259 obtained through the Fourier transform, are the two fundamental quantities in the 2PT model:

260
$$\Phi(t) = \left\langle \frac{\sum_{i=1}^{N} v_i(t) \cdot v_i(0)}{\sum_{i=1}^{N} v_i(0) \cdot v_i(0)} \right\rangle_{T_w} \tag{7}$$

261
$$F(v) = \int_0^\infty \Phi(t) \cos(2\pi v t) dt \tag{8}$$

262 where T_w represents the vibration time, *N* denotes the number of atoms, and $v_i(t)$ signifies

263 the velocity of the *i*-th atom at time *t*. For systems like amorphous liquids or gases where low-

264 frequency modes predominantly influence entropy, it is necessary to partition the total

265 correlation function into solid-like and gas-like components:

266
$$\Phi(t) = (1 - f_g)\Phi_s(t) + f_g\Phi_g(t) \tag{9}$$

267
$$F(v) = (1 - f_g)F_s(v) + f_g F_g(v) \tag{10}$$

268 where F_g and F_s are the gas-like and solid-like contributions to the vibrational density of

269 states, f_g is a fluidity factor to be determined. The vibrational entropy and other

270 thermodynamic properties are then determined by weighting the solid-like and gas-like

271 components with weighting functions:

272
$$S_{vib} = Nk_B \int_0^\infty [f_g F_g(v) W_g + (1 - f_g)F_s(v)W_s] dv \tag{11}$$

273   where W_s and W_g are the solid and gas entropy kernels, respectively. For exact methodology

274   details, we refer to Wilson & Stixrude (2021) as we implemented their formulations of this

275   method.

276   Compared to traditional free energy calculation methods, such as TI (Frenkel & Smit, 2002)

277   and free energy perturbation (FEP) (Zwanzig, 1954), the 2PT model significantly simplifies the

278   calculation of entropy by only requiring the post-processing of a single equilibrium MD

279   trajectory. When the MD simulations are sufficiently large and long enough, a single

280   equilibrium trajectory will contain ample information to fully characterize the entropy of the

281   system (Wilson & Stixrude, 2021). This model has been widely adopted for determining

282   thermodynamic properties across various complex systems (Hernandez et al., 2022; Sun et al.,

283   2017), including those relevant to the Earth's inner core, such as pure Fe and FeH_x alloys with

284   significant self-diffusion components (Yang et al., 2023).

285   **2.3 EAM potentials**

286   There are two EAM potentials developed by Alfè, Gillan, and Price (2002) (EAM-A hereafter)

287   and Belonoshko et al. (2017) (EAM-B hereafter) that have been previously used to study the

288   structure and properties of the Earth's core. In the present study they were used to calculate the

289   thermodynamic properties with BP-TI and 2PT methods across the entire *P-T* range of the inner

290   core. The total energy of the EAM potential has the form:

291
$$E_{tot} = \sum_i E_i \tag{12}$$

292   where E_i is the potential energy of atom *i*, which consists of two parts:

293
$$E_i = E_i^{\text{rep}} + F(\rho_i) = \sum_j \epsilon \left(\frac{a}{r_{ij}}\right)^n - \epsilon C \rho_i^{1/2} \tag{13}$$

294   E_i^{rep} is a purely repulsive function of the interatomic distance r_{ij} and $F(\rho_i)$ is the embedded

295   energy function accounting for the metallic bonding, with the densities $\rho_i = \sum_{j \neq i} \left(\frac{a}{r_{ij}}\right)^m$. The

296   fitting parameters for EAM-A are: $n = 5.93$, $\epsilon = 0.1662$ eV, $C = 16.55$, $a = 3.4714$ Å and $m =$

297   4.788 (Alfè, Gillan, and Price, 2002), and for EAM-B are: $n = 8.7932$, $\epsilon = 0.0220225$ eV, C

298     $= 28.8474$, $a = 3.48501$ Å and $m = 8.14475$ (Belonoshko et al., 2017). The differences between

299   these two EAM potentials can be attributed to the variations in the temperatures and

300 configurations used during their fitting procedures. This may introduce different

301 thermodynamic properties such as entropy, free energy and melting temperatures.

302 **2.4 *Ab initio* calculations**

303 We conducted *ab initio* molecular dynamics (AIMD) simulations and employed the BP-TI

304 technique to examine the mechanical and thermodynamic stability of the bcc structure under

305 tetragonal strain at ~330–360 GPa and 5000–7000 K. Density functional theory (Kohn & Sham,

306 1965) calculations were performed within the generalized gradient approximation (GGA)

307 (Perdew et al., 1996) and the projector-augmented wave (PAW) method (Blöchl, 1994). The

308 calculations were performed by using the Vienna *Ab initio* Simulation Package (VASP) code

309 (Kresse & Furthmüller, 1996). To avoid any overlapping of core states at high pressures and

310 temperatures, we treated fourteen electrons of Fe (Fe-$3p^6 3d^7 4s^1$) as valence. A single Gamma

311 point with a cutoff energy of 550 eV was selected for supercells of 128 atoms ($4 \times 4 \times 4$

312 supercell of the cubic 2-atom box), consistent with the setup used in the previous study (Cui et

313 al., 2013). A dense Gamma-centered $2 \times 2 \times 2$ k-point mesh was adopted for static corrections

314 on 40–100 snapshots extracted every 100–250 steps from the Gamma point MD simulations,

315 and the final stress was obtained by averaging the corrected stresses to achieve higher accuracy

316 in BP-TI calculations. The total energy was converged to 2×10^{-5} eV. These settings are

317 sufficient to converge the stress and total energy within 0.1 GPa and 1 meV/atom, respectively

318 (Table S1). Molecular dynamics trajectories were propagated in the NVT ensemble using the

319 Nosé thermostat (Nosé, 1984) with a time step of 1 fs. The AIMD simulations lasted for 10 ps,

320 and the last 80% were used for statistical sampling. The electronic population was accounted

321 for through the Fermi–Dirac smearing approach (Mermin, 1965). Spin polarization was not

322 considered since the thermal excitation of electrons would essentially destroy the residual

323 magnetic moment at high temperatures (Sun et al., 2024; Vočadlo et al., 2003).

324 **2.5 Computational details**

325 Cell sizes up to 8192 atoms were tested for sufficient convergence using simulations based on

326 the EAM potentials. For the BP-TI method, a system with a 1024-atom cell ($8 \times 8 \times 8$ supercell

327 of the cubic 2-atom box) with a simulation duration of 100–200 ps, was sufficient to converge

328   the Helmholtz free energy difference ($\Delta F_{fcc-bcc}$) between the fcc and bcc phases to within 1

329   meV/atom (Figure S1). For the 2PT method this cell size, with an equilibrium duration of 60

330   ps, provided adequate convergence of the Gibbs free energy (*G*) of the bcc phase to within 2

331   meV/atom (Figure S2). For the fcc phase, a cell size of 864 atoms (6 × 6 × 6 supercell of the

332   cubic 4-atom box) was suitable, while for the hcp phase, a slightly larger1200-atom cell (10 ×

333   6 × 5 supercell of the 4-atom *C*-centred unit cell box) was used, ensuring consistent

334   convergence levels for all free energy calculations using the 2PT model (Table S2).

335   To investigate whether diffusion affects the thermodynamic stabilities of the bcc phase, we

336   tested different cell sizes from 1024 atoms (8 × 8 × 8 supercell) to 65536 atoms (32 × 32 × 32

337   supercell) at 360 GPa and 7000 K, with all simulations maintaining identical densities.

338   Subsequently, the 2PT model was employed to calculate its vibrational entropy as a function of

339   cell size. Additional MD simulations of 500 ps duration were performed to further examine

340   how cooperative diffusion in the bcc phase depends on both system size and simulation time.

341   To verify the phase state (solid or liquid) in the simulations, we retrieved the radial distribution

342   function (RDF), the coordination number (CN), and the mean-square displacement (MSD) from

343   a 15-ps segment of the equilibrium trajectory, with the results depicted in the supporting

344   information Figures S3 and S4. Finally, the thermodynamic properties were evaluated using

345   both the BP-TI technique and the 2PT model, based on these extensive MD simulations. The

346   statistical error was assessed by the blocking method (Flyvbjerg & Petersen, 1989).

347

348   **3. Results and Discussion**

349   **3.1. Mechanical and thermodynamic stabilities of bcc Fe from BP-TI method**

350   As outlined in Section 2.1, the bcc↔fcc transformation can occur along the Bain path via

351   tetragonal strain at constant volume, which does not involve any first-order phase transition.

352   Therefore, the free energy change of this transformation can be determined by integrating the

353   reversible work required to drive the system from the reference state to the target state. The

354   mechanical stability of the bcc phase under tetragonal strain necessitates that its free energy

355   must be at a local minimum. If this is not the case, the bcc phase will spontaneously convert to

356 fcc and as a result, cannot remain stable. It is important to note that some previous studies have

357 focused on the hydrostatic nature of stresses to assess the mechanical stability of the bcc phase

358 (Belonoshko et al., 2011; 2017; Vočadlo et al., 2003). However, hydrostatic equilibrium, as

359 inferred from the stress analysis, does not necessarily correspond to a global free energy

360 minimum. Instead, it may represent a local maximum, with the unit cell being unstable under a

361 finite tetragonal strain (Godwal et al., 2015).

362 The stress anisotropy $(\sigma_{zz} - (\sigma_{xx} + \sigma_{yy})/2)$ and the difference in integrated free energies $(\Delta F_V$

363 and $\Delta G_{P_\tau})$ for various bct lattice structures along the Bain path at inner core *P-T* conditions, as

364 determined from both EAM-A and EAM-B potentials, are illustrated in Figures 1 and 2,

365 respectively. These two potentials show somewhat different behavior, as detailed in the

366 following two paragraphs.

367 For the EAM-A potential, both the bcc ($\tau = 1$) and fcc ($\tau = 2^{1/3}$) phases are found to be in a

368 nearly hydrostatic state, exhibiting only minimal stress variations (Figures 1a and 1d). The

369 stress anisotropy of the bct lattice initially increases from $\tau = 0.948$ to $\tau = 1.052$, then decreases

370 to $\tau = 1.206$, and subsequently increases again with further distortions. The integrated free

371 energy changes suggest that the bcc phase would be mechanically stable, as its free energy is

372 at a local minimum when integrating Equation (2) with respect to tetragonal strain. However,

373 the fcc phase has a lower free energy than the bcc phase at temperatures of 5000 and 6000 K,

374 and so the EAM-A potential predicts that the bcc phase would be metastable under IC

375 conditions relative to fcc. Moreover, the temperature appears to enhance the stability of the bcc

376 phase, while pressure tends to reduce it. The almost overlapping ΔF and ΔG can be attributed

377 to the small volume changes (i.e., the equation of state) during the bcc↔fcc transformation.

378 Notably, at 7000 K, a shift in the relative stability between the bcc and fcc phases becomes

379 evident, as indicated by the positive values of both the ΔF and ΔG. However, according to

380 established melting curves (Alfè, 2009; Anzellini et al., 2013; Sun et al., 2023), Fe is expected

381 to melt at this elevated temperature. The persistence of solid-like states in BP-TI calculations

382 at 7000 K reflects the superheating phenomenon in MD simulations, where crystals can remain

383 metastable above their equilibrium melting temperature until sufficient fluctuations or defects

384 trigger melting. Consequently, the free-energy values obtained for both bcc and fcc at 7000 K

385   correspond to metastable solid-like configurations sustained under superheating conditions.
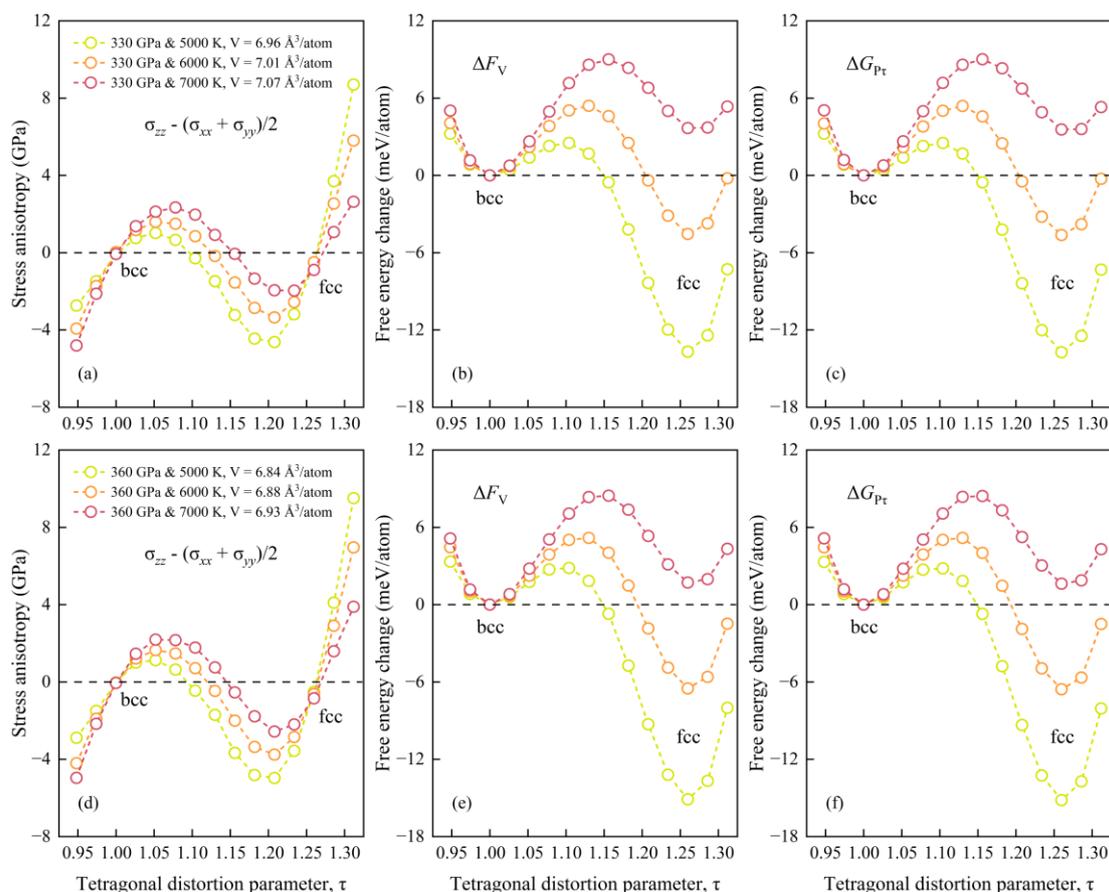
Figure 1. Stress anisotropy (a, d) and integrated free energy change (b-c, e-f) of the bct lattice with respect to tetragonal strain at inner core *P-T* conditions (330 GPa upper, 360 GPa lower), based on the EAM-A potentials (Alfè, Gillan, & Price, 2002). Uncertainty in stress anisotropy is typically less than 0.1 GPa, which is smaller than the symbol size; while uncertainty in the free energy difference accounts for both the error in stress tensor calculations and the integration process, which is less than 2 meV/atom in all cases. The dashed curves serve as guides for the eyes only.

Figure 2 shows the results from the EAM-B potential. At 5000 K, the stress anisotropy of the bct lattice initially decreases from $\tau = 0.948$ to $\tau = 1.182$ before increasing with further distortions. At 6000 K, the stress anisotropy firstly decreases from $\tau = 0.948$ to $\tau = 0.974$ and then increases to $\tau = 1.026$. As shown in Figures 2b–2c and 2e–2f, the free energy of the bcc phase resides at a local minimum, indicating its mechanical stability. At high temperatures of 7000 K, the stress anisotropy and integrated free energy changes for the bct lattice exhibit similar behavior to that observed using the EAM-A potentials, in which the energy of the bcc

400　phase lies clearly at a local minimum, while the fcc phase consistently occupies the global

401　minimum. Consequently, the EAM-B potential also predicts that the bcc phase would be

402　metastable under IC conditions relative to fcc. Note that the abrupt change in stress anisotropy

403　(i.e., $\tau = 1.104$ and 1.156 at 5000 K) observed with the EAM-B potentials corresponds to the

404　formation of a stacking fault on the (101) plane of the bct lattice, with the stacking-fault

405　direction oriented diagonally across this plane (from top left to bottom right), as confirmed by

406　direct visual inspection of the MD trajectories (Figure S5).
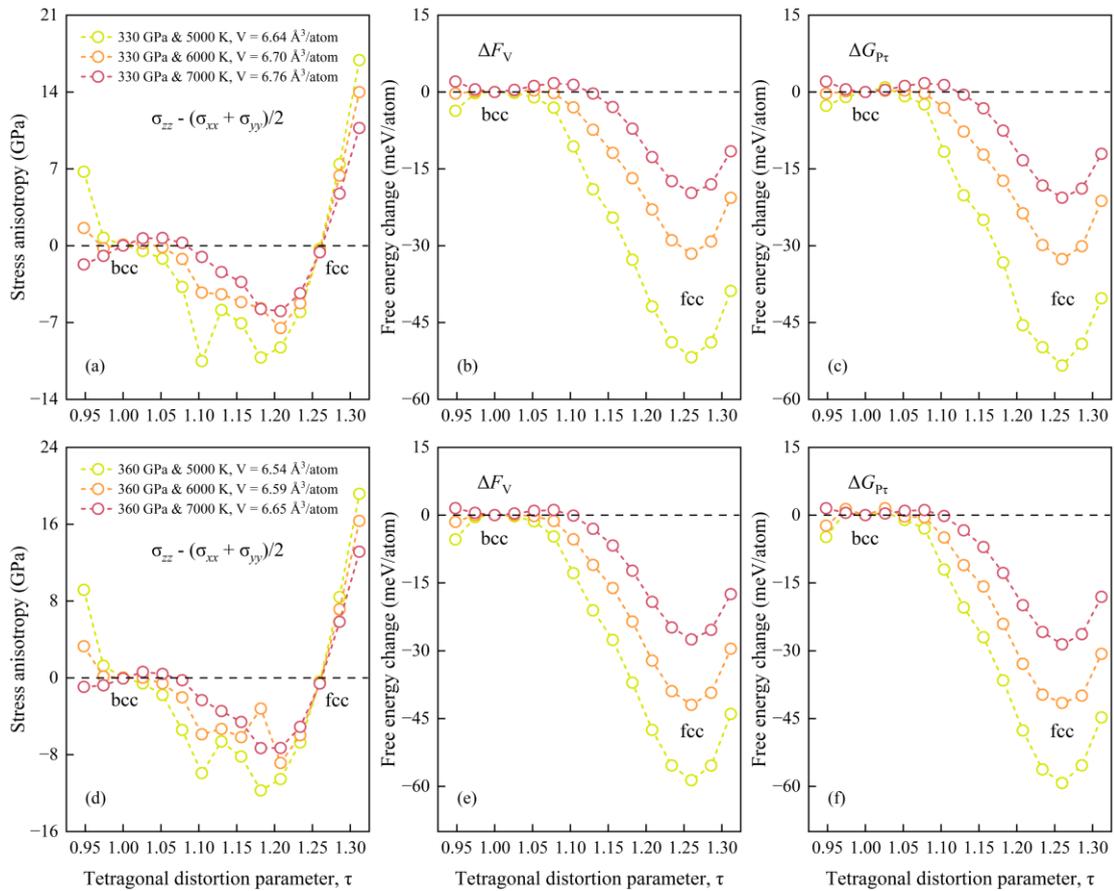
Figure 2. Stress anisotropy (a, d) and integrated free energy change (b-c, e-f) of the bct lattice with respect to tetragonal strain at inner core *P-T* conditions (330 GPa upper, 360 GPa lower), based on the EAM-B potentials (Belonoshko et al., 2017). Uncertainty for the stress anisotropy is typically less than 0.1 GPa, while uncertainty for the free energy difference is less than 2 meV/atom in all cases.

412　Recent studies have reported that the bcc phase can remain stable under conditions involving

413　large cell sizes ($N \geq 1024$ atoms) and extreme *P-T* conditions (360 GPa and 7000 K)

414　(Belonoshko et al., 2017). In contrast, our BP-TI calculation results based on various EAM

415   potentials demonstrate that bcc Fe is metastable under IC conditions with respect to fcc. To

416   further validate the results obtained from the EAM potentials, we carried out AIMD simulations

417   using the same BP-TI techniques at comparable *P-T* conditions. Although with shorter

418   simulation times of 10 ps and smaller system sizes containing 128 atoms, the AIMD results

419   confirm that bcc Fe remains mechanically stable but thermodynamically less stable even up to

420   temperatures of 7000 K (Figure 3), generally consistent with the EAM predictions. Note that at

421   lower temperatures of 5000 K, however, the bcc phase lies near an energy maximum and does

422   not exhibit mechanical stability (Figure 3 and Figure S6). This becomes more apparent in the

423   stress anisotropy, where stability is characterized by negative values at $\tau < 1$ and positive values

424   at $\tau > 1$. Nevertheless, considering that inner core temperatures would exceed 5000 K, both

425   EAM and AIMD calculations now consistently indicate that bcc holds a subtle mechanical

426   stability under IC conditions (Figures 1–3). These findings differ from earlier *ab initio*

427   simulations (Cui et al., 2013; Godwal et al., 2015), where the relatively large distortions applied

428   (e.g., $\tau = 0.052$) may have overlooked the subtle mechanical stability of bcc, particularly at

429   lower temperatures (5000–6000 K). This comparison underscores the importance of employing

430   smaller distortion steps in BP-TI calculations to more accurately capture the weak mechanical

431   stability of the bcc phase under IC conditions (Figure 3 and Figure S6). In addition, our

432   convergence tests indicate that while a Gamma-point mesh was employed in Cui et al. (2013),

433   denser k-point sampling is required to achieve higher accuracy in BP-TI calculations. Our

434   results are consistent with more recent studies at 330–360 GPa (Zhang et al., 2025) and at 400

435   GPa (Ghosh et al., 2023; Li & Scandolo, 2024a).

436
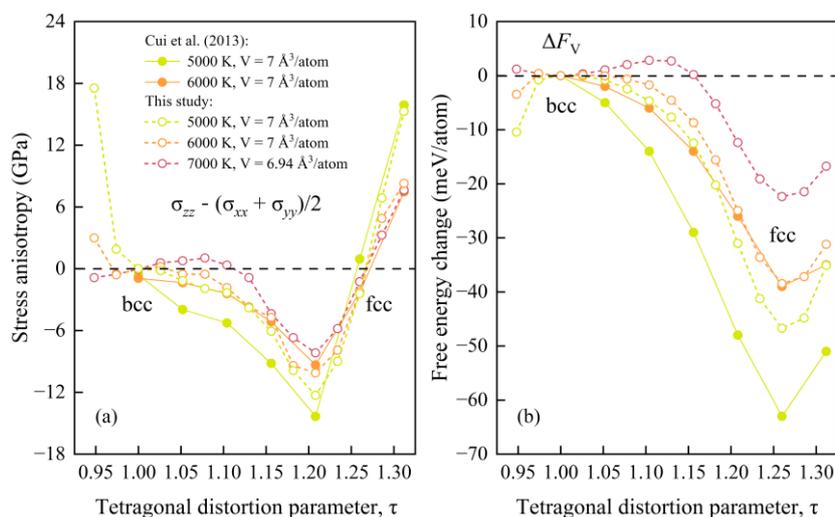
437 **Figure 3.** Stress anisotropy (a) and integrated free energy change (b) of the bct lattice with respect to

438 tetragonal strain at inner core *P-T* conditions, based on *ab initio* calculations. The statistical uncertainty

439 in stress anisotropy, evaluated using the blocking method, is typically less than 0.5 GPa, corresponding

440 to an uncertainty in the free energy difference of no more than 5.5 meV/atom.

441 We also tried to use available Machine Learning (ML) potentials to assess the mechanical and

442 thermodynamic stabilities of the bcc phase. The ML potential developed by Jana & Caro (2023)

443 is suggested to be suitable for simulating Fe phases under IC conditions. However, our

444 calculations show that this ML potential is unable to simulate the bcc↔fcc phase transition

445 along the Bain path, as the simulated structures melted at 6000 K (Figure S7), as well as

446 premelting at 5000 K (Figure S8). As this ML potential was trained on *ab initio* results, it should

447 have the same melting temperature as the *ab initio* simulations. Furthermore, other existing ML

448 potentials have not been publicly released, and discrepancies persist among these potentials in

449 simulating Fe properties, such as the melting temperature (Li & Scandolo, 2024b; Wu et al.,

450 2024; Yuan & Steinle-Neumann, 2023; Zhang et al., 2020). This highlights the critical need for

451 the development of ML-based potentials suitable for long-duration and large-scale MD

452 simulations of core Fe alloys.

453 In summary, we conclude that both EAM potentials and *ab initio* simulations show that the bcc

454 phase is mechanically stable, but remains thermodynamically less stable than the fcc phase

455 under IC conditions. As it is well established that the fcc phase is less stable than the hcp phase

456 (Li & Scandolo, 2024a; Stixrude, 2012; Vočadlo et al., 2000; 1999), it is clear that bcc cannot

457 be the stable phase of pure Fe under core conditions. Nevertheless, it has been suggested that

458 diffusion may stabilise the bcc phase, and that this is only seen in simulations with large

459 numbers of atoms. We examine that next.

460 **3.2. Thermodynamic stabilities of Fe structures from 2PT free energy calculations**

461 **3.2.1 Size effects and self-diffusion**

462 The cooperative diffusion mechanism has been proposed to stabilise the bcc phase of Fe under

463 IC conditions, with large systems being necessary for this stabilisation (Belonoshko et al., 2017).

464 Their analysis of configurations and trajectories unveiled diffusive processes that may

465   contribute to entropy, thereby stabilising the bcc phase (Figure 4). More importantly, it was

466   argued that such diffusion mechanisms cannot be supported in small systems without

467   destroying their structure, emphasising the significant size dependence in the stability of the

468   bcc phase. However, a subsequent study by Schultz et al. (2018) argued that the entropy of bcc

469   Fe exhibits no system size-dependent anomalies, based on their extensive TI thermodynamic

470   calculations. They claimed the accurate free energy calculations for this system can be

471   computed using *ab initio* methods without the need for excessively large atomistic models.

472   Although both studies used identical EAM potentials, cell sizes, and *P-T* conditions, they

473   differed in the approaches employed to determine the entropy and free energy of the system.

474   Schultz et al. (2018) argued that the VACF method used in Belonoshko et al. (2017) does not

475   accurately predict free energies for systems with self-diffusion. This challenges the notion that

476   prohibitively large systems are necessary for proper simulations of bcc Fe. Therefore, further

477   clarification is required regarding the size dependence on the stability of the bcc phase to gain

478   a clear understanding of the inner core structures.

479   Here, we used the 2PT model to examine the discrepancies of size dependence on the bcc phase

480   stabilities, with results presented in Figure 4. The system size modelled for the bcc phase ranged

481   from 1024 to 65536 atoms, consistent with the sizes used in the previous study (Schultz et al.,

482   2018). For the hcp phase under IC conditions, simulations were conducted with system sizes

483   ranging from 256 to 4000 atoms, as previous work has shown that no obvious system-size

484   anomalies in entropy with the system containing more than 1000 atoms (Belonoshko et al.,

485   2017; Schultz et al., 2018; Sun et al., 2018). Our results reveal that the entropy of the bcc phase

486   exhibits negligible size dependence, maintaining a nearly constant value as the system size

487   increases. This can be confirmed from the convergence of the total VDoS versus simulation

488   cell size (Figure S9). The entropy calculated using the 2PT model is systematically larger than

489   that obtained from the TI method of Schultz et al. (2018) (Figure 4). This is likely due to the

490   use of EAM potential. Theoretically, the energy difference between two structures should be

491   identical from different free energy calculation methods. However, the potential may not be

492   well trained to provide accurate description of the phase space explored during simulations.

493   Therefore, variations in methods and integration paths in TI calculations could result in energy

494   shifts. Nevertheless, the entropy difference between the bcc and hcp phases ($\Delta S_{bcc-hcp}$) is

495   estimated to be ~1.2 J/mol/K (0.1443 k_B/atom), which is very close to the value of ~1.3 J/mol/K

496   (0.1564 k_B/atom) reported by Schultz et al. (2018) in their TI calculations. Such an entropy

497   difference is not sufficient to render the bcc structure thermodynamically more stable than the

498   hcp structure, as stability would require $\Delta S_{bcc-hcp} > 1.52$ J/mol/K (0.1831 k_B/atom). This

499   finding is further corroborated by Li & Scandolo (2024a), who, based on the deep-learning

500   potential calculations, suggested that the self-diffusion mechanism is inadequate to stabilise bcc

501   Fe thermodynamically over other competing phases.
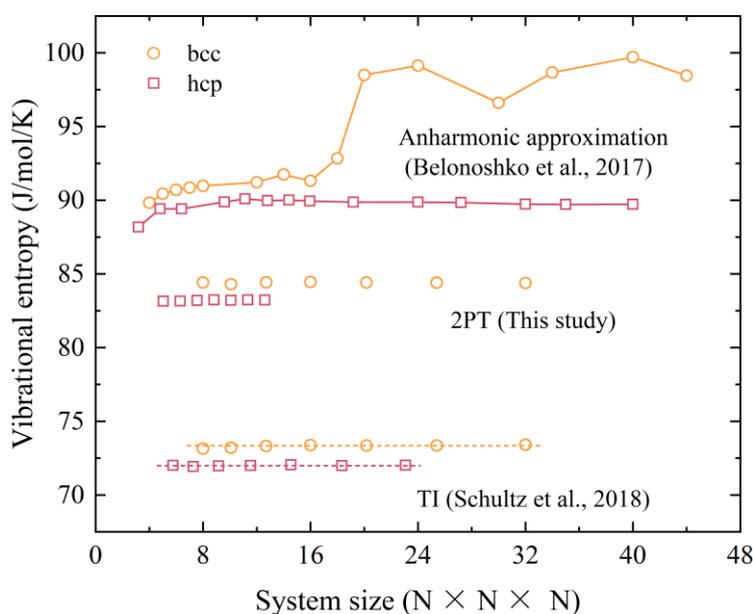
502

503   **Figure 4.** Size dependence of entropy of the bcc and hcp phases computed at 360 GPa and 7000 K using

504   the EAM-B potentials, compared with results from the literature that employed the same potentials.

505   System size is provided in N×N×N unit cells, where each unit cell contains 2 atoms for the bcc phase

506   and a 4-atom *C*-centred unit cell for the hcp phase (normalized to 2 atoms for unified representation).

507   For N = 32, the system consists of 65536 atoms. Although diffusion is observed in large supercell

508   configurations (e.g., with 32768 and 65536 atoms), the entropy difference of the bcc phase is very small

509   and nearly constant, consistent with the TI results reported by Schultz et al. (2018). Dashed lines are the

510   linear fit to the data points.

511   Although our MD trajectory analysis reveals some diffusion in large bcc supercell

512   configurations, as indicated by the MSDs depicted in Figure 5, the calculated entropy does not

513   exhibit a rapid increase as observed by Belonoshko et al. (2017). In their study, cooperative

514   diffusion was found to significantly contribute to low-frequency modes, resulting in a

515   substantial rise in entropy within the bcc phase. However, Schultz et al. (2018) argued that

516   diffusion *per se* does not directly contribute to the free energy, which is an equilibrium

517   thermodynamic quantity that can be defined and computed without any reference to dynamic

518   behavior. They proposed that anomalous entropy scaling can be rigorously demonstrated

519   through precise free energy calculations using various simulation methods, and the presence or

520   absence of diffusion has no effect on the entropy. In contrast, Li & Scandolo (2024a) contend

521   that the existence of self-diffusion invalidates direct TI approaches for free energy calculations

522   by using ideal or Einstein crystals as references. Reconciling these divergences calls for

523   diffusion-aware reference models or advanced sampling methods such as metadynamics or

524   Monte Carlo dynamics that can accommodate atomic mobility without compromising

525   thermodynamic rigor. While the self-diffusion in bcc phase may contribute to entropy, our

526   current study, along with previous works (Li & Scandolo, 2024a; Schultz et al., 2018), suggests

527   that such contributions are likely limited and not scaled significantly with cell size.
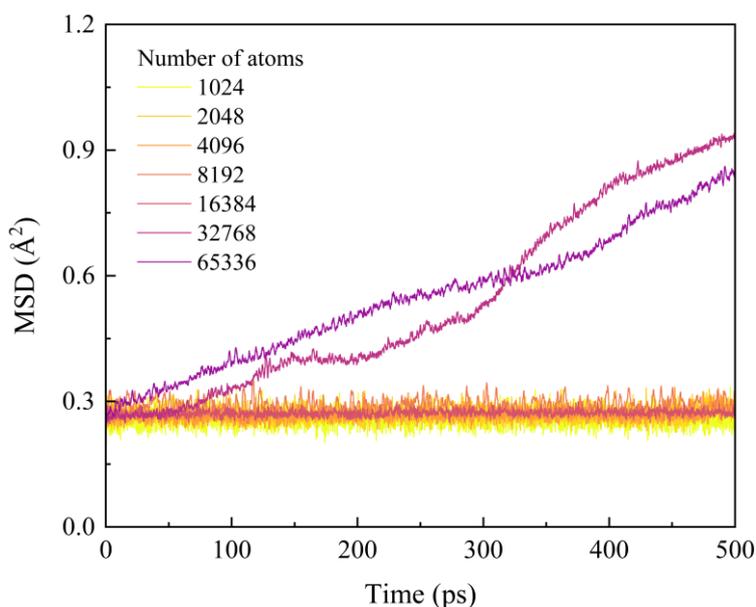

528

529   **Figure 5.** MSDs for different cell sizes in the bcc phase at 360 GPa and 7000 K based on the EAM-B

530   potentials. Self-diffusion is observed in configurations with 32,768 and 65,536 atoms, while smaller

531   systems show no obvious diffusion. This indicates that diffusion is generally more prevalent in larger

532   systems.

533   **3.2.2 Corroborating the BP-TI results with 2PT model**

534   In Section 3.1, we examined the mechanical and thermodynamic stabilities of the bcc phase

535   under tetragonal strain using the TI techniques, incorporating both semi-empirical EAM

536   potentials and *ab initio* simulations. Building on the convergence accuracy of the BP-TI free

537   energy calculations, we now extend our analysis by performing additional thermodynamic

538   calculations using the 2PT model, after clarifying the size effect on the stability of the bcc

539   structure. This approach aims to corroborate the BP-TI results and is expected to be consistent

540   with our previous findings.

541   The VACF and its associated VDoS for the bcc and fcc phases under relevant *P-T* conditions

542   are displayed in Figures 6 and 7, respectively. The reduced number of distinct peaks in the

543   VACF of the fcc phase at 7000 K, as obtained from the EAM-A potentials, suggests that the

544   phase has undergone melting (Figure 6c). This is further supported by the presence of finite

545   VDoS (due to diffusive modes) at zero frequency (Figure 7c). In contrast, when employing the

546   EAM-B potentials, the fcc phase still retains solid phase characteristics, with more peaks in the

547   VACF and its VDoS tends towards zero at the long wavelength limit (Figure 6d). In the case

548   of the bcc phase, it maintains a solid state regardless of the EAM potentials used, as evidenced

549   by the VACF and VDoS shown in Figures 7a and 7b. However, it is worth noting that there is

550   a very slightly diffusive behavior in the bcc phase at 7000 K when using the EAM-A potentials,

551   as indicated by slow, stair-like features in its MSD as the simulation time increases (Figure S4).


552
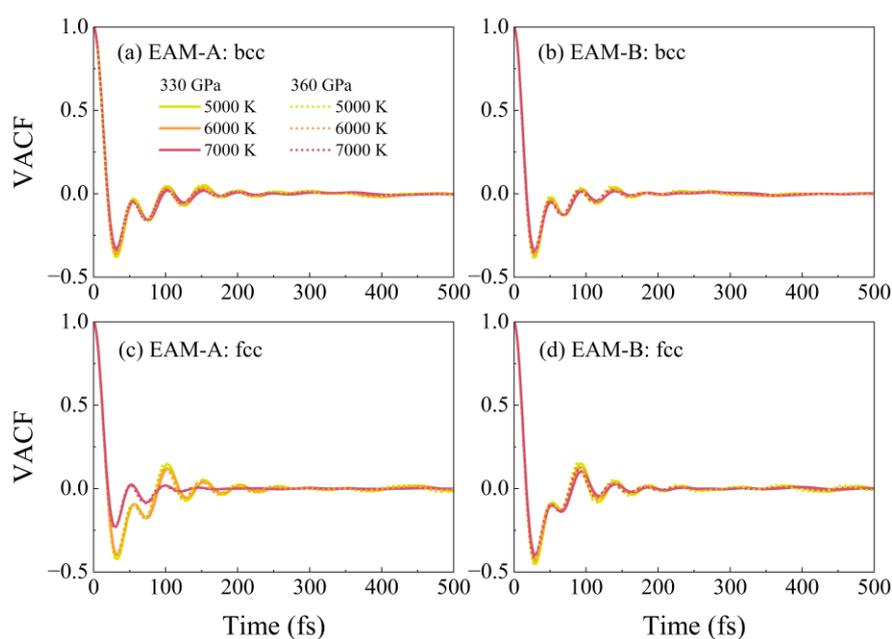
Figure 6. Velocity autocorrelation functions for the bcc (a-b) and fcc (c-d) phases of Fe at different *P-T* conditions as indicated in the legend. Solid lines represent the data at 330 GPa, while dot lines correspond to the data at 360 GPa.
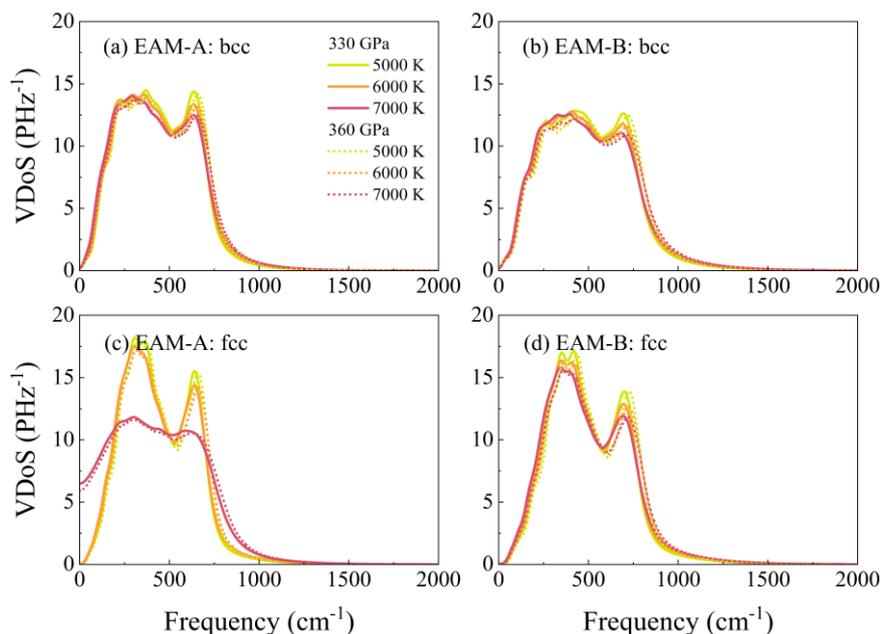
Figure 7. The total vibrational density of states of the bcc (a-b) and fcc (c-d) Fe under different *P-T* conditions. Solid lines represent the data at 330 GPa, while dot lines correspond to the data at 360 GPa.
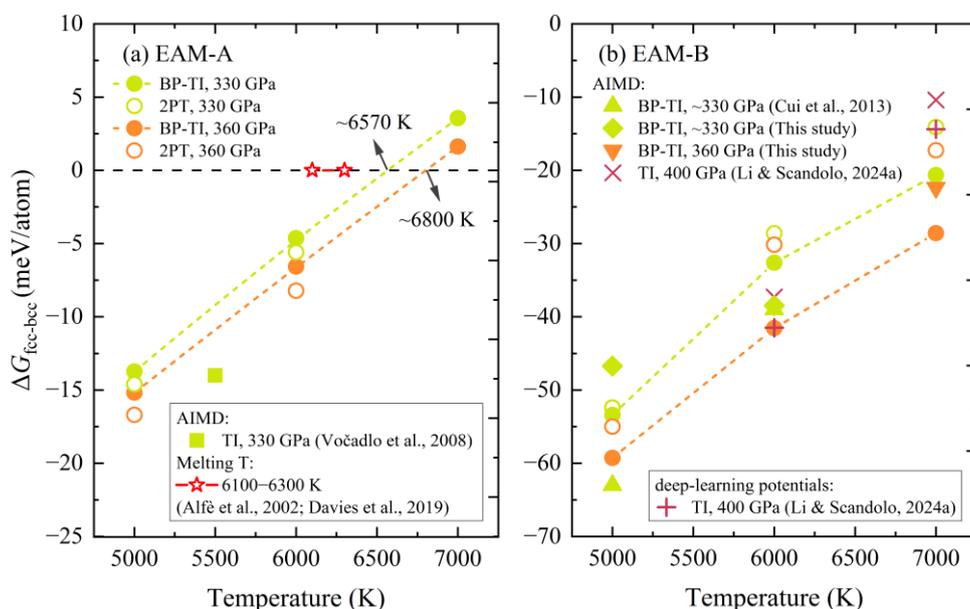
Figure 8. Free energy changes between the fcc and bcc phases of Fe under IC *P-T* conditions based on different force fields and methods. Solid and open circles denote the results from BP-TI and 2PT, respectively. Green represents calculations at 330 GPa while orange represents results at 360 GPa. The square corresponds to *ab initio* data reported by Vočadlo, Wood, Alfè, and Price (2008). Upper triangles

564 indicate *ab initio* results from Cui et al. (2013), while lower triangles represent the *ab initio* results of

565 this study. Additionally, the *ab initio* and deep-learning potential data (shown in purple) explored at 400

566 GPa by Li & Scandolo (2024a) are included for comparison. The melting temperature of bcc Fe

567 (indicated in red) is sourced from Alfè, Gillan, and Price (2002) and Davies et al. (2019).

568 Figure 8 illustrates the free energy changes between the fcc- and bcc-Fe ($\Delta G_{\text{fcc}-\text{bcc}}$) under IC

569 *P-T* conditions, as evaluated through the 2PT model. Remarkably, the results derived from the

570 2PT model demonstrate robust agreement with those obtained from the BP-TI approach,

571 particularly notable in the EAM-A potentials (Figure 8a), where the discrepancy is less than 2

572 meV/atom. Furthermore, these results are in good agreement with previous *ab initio*

573 assessments conducted at ~330 GPa and 5500 K using the coupling parameters TI method

574 (Vočadlo, Wood, Alfè, & Price, 2008), which shows a disparity of only ~4 meV/atom. For the

575 EAM-B potentials (Figure 8b), although marginally larger, the difference remains within 7

576 meV/atom up to temperatures of 7000 K, and the results align well with the *ab initio*

577 computations reported by Cui et al. (2013) as well as close to the recent calculations conducted

578 at 400 GPa based on the *ab initio* and deep-learning potentials (Li & Scandolo, 2024a).

579 According to the EAM-A potentials, the temperatures required to stabilise the bcc phase over

580 fcc phase of Fe at 330 and 360 GPa are estimated to be ~6570 and ~6800 K, respectively (Figure

581 8a). However, using the same EAM potentials, Alfè et al. (2002a) and Davies et al. (2019)

582 determined the melting temperatures of the bcc phase under IC pressure conditions to be in the

583 range of ~6100–6300 K, which are lower than the stabilisation temperatures predicted by the

584 EAM-A potentials. For the EAM-B potentials, the necessary stabilisation temperatures exceed

585 8000 K (Figure 8b). Therefore, while temperature can stabilise the bcc phase, it remains far

586 from completely stable across the entire range of IC temperatures, as the required stabilisation

587 temperatures exceed the melting temperature of Fe under these conditions, irrespective of

588 whether EAM-A or EAM-B potentials are employed.

589 **3.3. Melting temperatures of Fe structures and the inner core**

590 It is well established that the fcc structure is thermodynamically less stable than the hcp

591 structure under IC conditions, primarily due to its larger thermal pressure term (Stixrude, 2012;

592   Vočadlo et al., 2000; 1999). More recent work by Li & Scandolo (2024a), using *ab initio* and

593   deep-learning interatomic potential for Fe at extreme conditions, further supports this

594   hypothesis, although the mechanical stability of the bcc phase under tetragonal strain based on

595   this deep-learning interatomic potential has not been clarified. While the observed *P*-wave

596   anisotropy in the inner core has been attributed to the fcc structure (Vočadlo, Wood, Alfè, &

597   Price, 2008), this alone cannot completely account for the complex anisotropy of the inner core,

598   especially when compared to the hcp and/or bcc structures (Mattesini et al., 2010; Romanowicz

599   et al., 2016; Tateno et al., 2010). Consequently, the fcc structure is not included in this section

600   and the focus is solely on the bcc, hcp, and liquid phases.
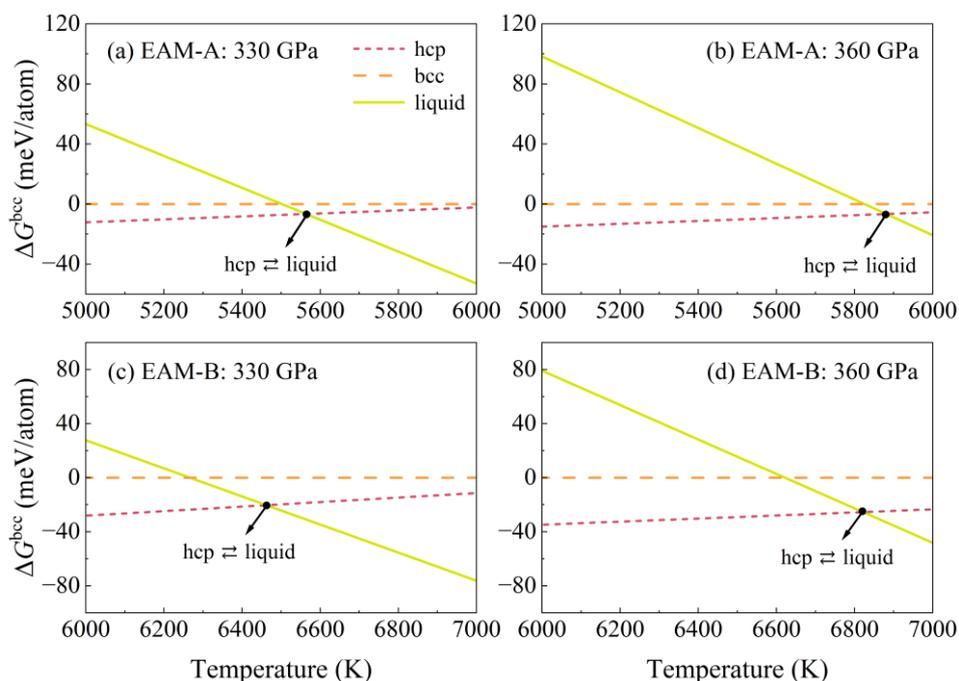
Figure 9. Free energy differences referenced to bcc Fe at 330 and 360 GPa near the melting temperatures.
The black dots indicate the phase transition from hcp to liquid.

604   We calculated the melting temperatures of different Fe structures using the 2PT model based

605   on the EAM potentials by comparing their absolute Gibbs free energies with those of the liquid

606   phase. The VACF and its associated VDoS for the hcp and liquid phases at inner core *P-T*

607   conditions are shown in Figures S10 and S11, respectively. The calculated free energy

608   difference relative to the bcc phase is shown in Figure 9. The free energy difference between

609   hcp and bcc using EAM-A is minimal, generally less than 15 meV/atom (with bcc being higher)

610   under relevant IC conditions. This difference increases when employing EAM-B, reaching ~35

611 meV/atom, which is close to the recent value of ~46 meV/atom (calculated using TI) based on

612 deep-learning potentials at 400 GPa and 6000–7000 K (Li & Scandolo, 2024a). However, the

613 values obtained from EAM potentials are lower than those from *ab initio* calculations, which

614 yield ~60 meV/atom from TI (González-Cataldo & Militzer, 2023) and 170–270 meV/atom

615 from the quasiharmonic approximation, both at 330–360 GPa and 6000 K (Zhang et al., 2025).

616 These discrepancies most likely arise from differences in the employed potentials and free-

617 energy calculation methods.

618 For the EAM-A potentials, the calculated melting temperatures are ~5500 K for bcc and ~5565

619 K for hcp at 330 GPa, while ~5825 K for bcc and ~5900 K for hcp at 360 GPa (Figures 9a and

620 9b). Using the EAM-B potentials, the melting temperatures are determined to be ~6265 K for

621 bcc and ~6460 K for hcp at 330 GPa, while ~6620 K for bcc and ~6820 K for hcp at 360 GPa

622 (Figures 9c and 9d). Generally, a solid phase with the highest melting temperature is considered

623 the most stable phase, while other solid phases remain metastable near the melting temperature.

624 It is evident that the hcp phase consistently exhibits a higher melting temperature than the bcc

625 phase, suggesting it should be the most stable phase in the Earth's inner core. Furthermore, the

626 melting temperature of Fe derived from the EAM-B potentials is ~750–900 K higher than that

627 obtained based on the EAM-A potentials. The different fitting procedures in temperatures and

628 configurations may explain this discrepancy (Alfè, Gillan, & Price, 2002; Belonoshko et al.,

629 2017).

630 The melting temperatures of the bcc and hcp phases obtained from the EAM potentials are

631 compared with available literature values (Figure 10). The data for the hcp phase is abundant,

632 while the bcc phase has a more limited set of values. One *ab initio* data point for the bcc melting

633 point comes from Bouchet et al. (2013), in which the calculation was performed with a 256-

634 atom solid-liquid coexistence (SLC) cell, leading to considerable uncertainties in both pressure

635 and temperature. Another *ab initio* estimate is from Sun et al. (2023), where they determined

636 an *ab initio* melting point using PAW8 and PAW16 pseudopotentials. A more recent data point

637 of ~6480 K for bcc Fe is reported by Wu et al. (2024), derived from the deep potential (DP)

638 model. Our results for the bcc phase, based on the EAM-B potentials, are in good agreement

639 with these studies (Bouchet et al., 2013; Sun et al., 2023; Wu et al., 2024), but ~450 K higher

640   than that of Li & Scandolo (2024a) based on their DP determinations. This discrepancy implies

641   that the current DP model for Fe at IC conditions from different groups still exhibits some

642   inconsistencies (Li & Scandolo, 2024a; Wu et al., 2024). The largest deviation is seen in the

643   bcc phase from Belonoshko, Fu, and Smirnov (2022), showing a melting temperature ~685 K

644   higher than our EAM-B value at 360 GPa. This divergence is particularly notable as it suggests

645   the melting temperature of the hcp phase is much lower than that of the bcc phase at the inner

646   core center. Such deviation could be attributed to the employed semi-empirical potential, which

647   was fitted to 0 K DFT results, and the calculated free energy contained an *ad hoc* correction for

648   the electronic entropy effects (Belonoshko et al., 2021; Belonoshko, Fu, & Smirnov, 2022).
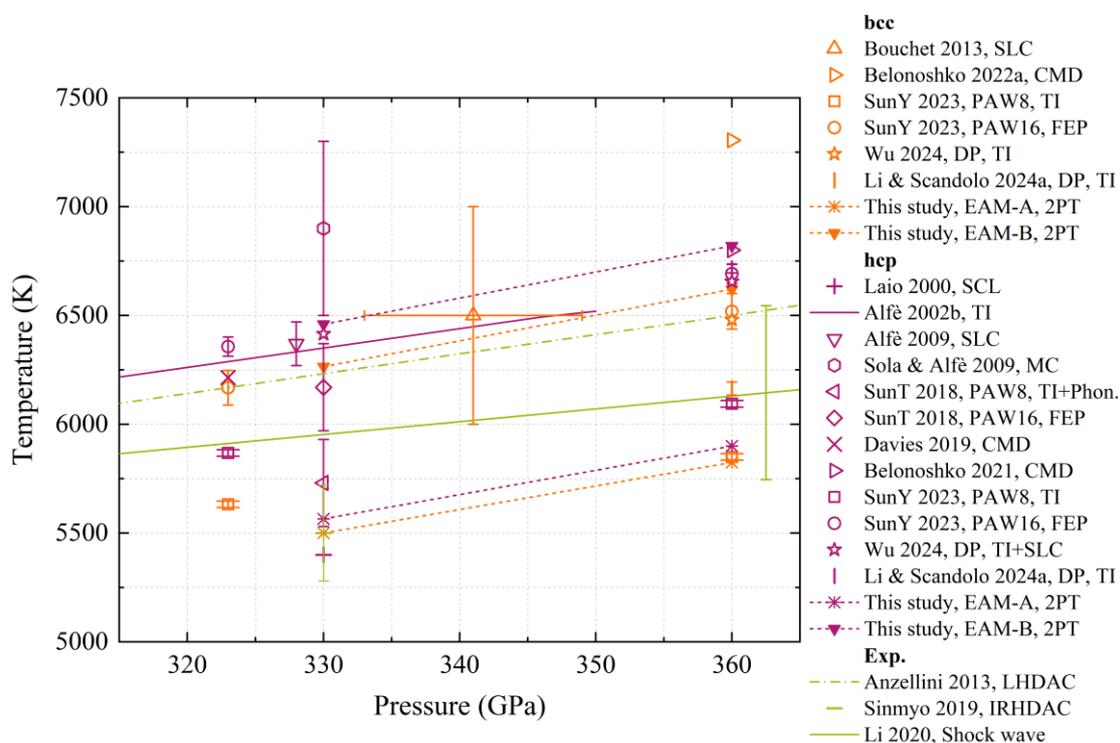
649

650   **Figure 10.** Melting temperatures of the bcc (orange) and hcp (red) phases determined by the 2PT model

651   with EAM potentials, and data from literature is provided for comparison. Literature sources include *ab*

652   *initio* SLC simulations by Laio (2000), Alfè (2009), and Bouchet et al. (2013); *ab initio* TI and SLC

653   simulations by Alfè, Price, and Gillan (2002); *ab initio* TI, phonon quasiparticle, and FEP calculations

654   by Sun et al. (2018; 2023); Monte Carlo (MC) simulations by Sola & Alfè (2009), and classical MD

655   simulations by Davies et al. (2019) and Belonoshko et al. (2021) and Belonoshko, Fu, and Smirnov

656   (2022). Additionally, melting temperatures predicted by the DP model are from Wu et al. (2024) using

657   TI and SLC simulations, and Li & Scandolo (2024a) using TI methods. Experimental melting data (green)

658   are taken from Anzellini et al. (2013), Sinmyo et al. (2019) and Li et al. (2020), based on the extrapolated

659   data from DAC and shock wave experiments, respectively.

660   Our calculated melting temperature for the hcp phase with EAM-A potentials at 330 GPa is

661   reasonably consistent with the data of Sun et al. (2018) using the PAW8 pseudopotential within

662   uncertainties. This data also agrees with recent shock wave experimental results from Li et al.

663   (2020) at 360 GPa, within their margin of error. Note that using the same EAM potential, a

664   higher melting temperature (~6215 K) of the hcp phase at 323 GPa was predicted through SLC

665   simulations (Davies et al., 2019; Gao et al., 2025). The difference in methods for determining

666   the melting point may account for this discrepancy, as the SLC simulations may be susceptible

667   to superheating, leading to an overestimation of the melting point. Nevertheless, the difference

668   in melting temperature between hcp and bcc is nearly the same for both methods: ~70 K (with

669   hcp being higher) for the SLC simulations from previous studies (Davies et al., 2019; Gao et

670   al., 2025), and ~65 K for the free energy calculations in the current work. On the other hand,

671   our melting temperature from the EAM-B at 330 GPa aligns well with the *ab initio* 980-atom

672   SLC simulations conducted by Alfè (2009), and is also close to the values from the DP model

673   determined through TI and SLC by Wu et al. (2024). At the higher pressure of the inner core

674   center (~360 GPa), our EAM-B result is nearly identical to the data examined recently by

675   Belonoshko et al. (2021), with a difference of only ~20 K. Overall, both EAM potentials predict

676   a higher melting temperature for hcp than bcc, indicating that hcp is more stable, which is

677   consistent with previous studies (Li & Scandolo, 2024a; Sun et al., 2023; Wu et al., 2024).

678   These results establish a clear distinction in the relative stability between the hcp and bcc phases

679   under the same level of calculation accuracy.

680

4. Conclusions

682   We have investigated the mechanical stability of the bcc structure under tetragonal strain by

683   employing the high-precision BP-TI technique. Our results, derived from both EAM potentials

684   and *ab initio* simulations, demonstrate that the bcc phase is mechanically stable but

685   thermodynamically less stable relative to fcc under IC conditions, with this metastability being

686 independent of the simulation cell size. Thermodynamic calculations based on the 2PT model

687 further corroborate these results. Although some self-diffusion is observed in bcc cells at

688 elevated temperatures, its contribution to entropy is found to be negligible, which contradicts

689 prior claims suggesting a significant entropy contribution from this diffusion. Furthermore, our

690 melting point calculations reveal that, under IC pressure conditions, the hcp phase consistently

691 exhibits a higher melting temperature than the bcc phase. This suggests that the hcp phase is

692 the most stable phase for pure Fe under these extreme conditions, reinforcing previous

693 methodologies and conclusions regarding the stability of Fe in the Earth's inner core.

694 Nevertheless, the free energy difference between the hcp and bcc phases is minimal, only on

695 the order of tens of meV/atom, which is comparable to the thermal energy ($k_B T$) per atom at

696 room temperatures. Furthermore, alloying with other elements, such as Ni, Si, S, and H, may

697 influence inner core phase stabilities and crystallization processes. Therefore, further

698 investigation is essential to better understand the combined impact of alloying elements on

699 phase behavior and to refine our knowledge of the structures and properties of the Earth's

700 interior.

701

702 **Conflict of Interest**

703 The authors declare no conflicts of interest relevant to this study.

704

705 **Acknowledgments**

713

714 **Open Research**

715 **Data Availability Statement**

716 The data files used in this paper are available at (Yang et al., 2025).

717

References

Alfè, D. (2009). Temperature of the inner-core boundary of the Earth: Melting of iron at high pressure from first-principles coexistence simulations. *Physical Review B*, *79*(6), 060101. https://doi.org/10.1103/PhysRevB.79.060101

Alfè, D., Gillan, M. J., & Price, G. D. (2002). Complementary approaches to the ab initio calculation of melting properties. *The Journal of Chemical Physics*, *116*(14), 6170–6177. https://doi.org/10.1063/1.1460865

Alfè, D., Price, G., & Gillan, M. (2002). Iron under Earth's core conditions: Liquid-state thermodynamics and high-pressure melting curve from ab initio calculations. *Physical Review B*, *65*(16), 165118. https://doi.org/10.1103/PhysRevB.65.165118

Anderson, O. L. (2003). The three-dimensional phase diagram of iron. *Earth's core: Dynamics, structure, rotation*, *31*, 83–103. https://doi.org/10.1029/GD031p0083

Anzellini, S., Dewaele, A., Mezouar, M., Loubeyre, P., & Morard, G. (2013). Melting of iron at Earth's inner core boundary based on fast X-ray diffraction. *Science*, *340*(6131), 464–466. https://doi.org/10.1126/science.1233514

Bain, E. C. (1924). The nature of martensite. *Transactions of the American Institute of Mining and Metallurgical Engineers*, *70*, 25.

Belonoshko, A. B., Ahuja, R., & Johansson, B. (2003). Stability of the body-centred-cubic phase of iron in the Earth's inner core. *Nature*, *424*(6952), 1032–1034. https://doi.org/10.1038/nature01954

Belonoshko, A. B., Arapan, S., & Rosengren, A. (2011). An ab initio molecular dynamics study of iron phases at high pressure and temperature. *Journal of Physics: Condensed Matter*, *23*(48), 485402. https://doi.org/10.1088/0953-8984/23/48/485402

Belonoshko, A. B., Fu, J., Bryk, T., Simak, S. I., & Mattesini, M. (2019). Low viscosity of the Earth's inner core. *Nature communications*, *10*(1), 2483. https://doi.org/10.1038/s41467-019-10346-2

Belonoshko, A. B., Fu, J., & Smirnov, G. (2021). Free energies of iron phases at high pressure and temperature: Molecular dynamics study. *Physical Review B*, *104*(10), 104103. https://doi.org/10.1103/PhysRevB.104.104103

Belonoshko, A. B., Fu, J., & Smirnov, G. (2022). Erratum: Free energies of iron phases at high pressure and temperature: Molecular dynamics study. *Physical Review B*, *105*(5), 059903. https://doi.org/10.1103/PhysRevB.105.059903

Belonoshko, A. B., Lukinov, T., Fu, J., Zhao, J., Davis, S., & Simak, S. I. (2017). Stabilization of body-centred cubic iron under inner-core conditions. *Nature Geoscience*, *10*(4), 312–316. https://doi.org/10.1038/ngeo2892

Belonoshko, A. B., Simak, S. I., Olovsson, W., & Vekilova, O. Y. (2022). Elastic properties of body-centered cubic iron in Earth's inner core. *Physical Review B*, *105*(18), L180102. https://doi.org/10.1103/PhysRevB.105.L180102

Blöchl, P. E. (1994). Projector augmented-wave method. *Phys Rev B*, *50*(24), 17953–17979. https://doi.org/10.1103/PhysRevB.50.17953

Boehler, R. (1993). Temperatures in the Earth's core from melting-point measurements of iron at high static pressures. *Nature*, *363*(6429), 534–536. https://doi.org/10.1038/363534a0

Bouchet, J., Mazevet, S., Morard, G., Guyot, F., & Musella, R. (2013). Ab initio equation of state of iron up to 1500 GPa. *Physical Review B*, *87*(9), 094102.

762   https://doi.org/10.1103/PhysRevB.87.094102

763 Brown, J. M., & McQueen, R. G. (1986). Phase transitions, Grüneisen parameter, and elasticity
764   for shocked iron between 77 GPa and 400 GPa. *Journal of Geophysical Research: Solid*
765   *Earth*, *91*(B7), 7485–7494. https://doi.org/10.1029/JB091iB07p07485

766 Côté, A. S., Vočadlo, L., Dobson, D. P., Alfè, D., & Brodholt, J. P. (2010). Ab initio lattice
767   dynamics calculations on the combined effect of temperature and silicon on the stability
768   of different iron phases in the Earth's inner core. *Physics of the Earth and Planetary*
769   *Interiors*, *178*(1-2), 2–7. https://doi.org/10.1016/j.pepi.2009.07.004

770 Cui, H., Zhang, Z., & Zhang, Y. (2013). The effect of Si and S on the stability of bcc iron with
771   respect to tetragonal strain at the Earth's inner core conditions. *Geophysical Research*
772   *Letters*, *40*(12), 2958–2962. https://doi.org/10.1002/grl.50582

773 Davies, C. J., Pozzo, M., & Alfè, D. (2019). Assessing the inner core nucleation paradox with
774   atomic-scale simulations. *Earth and Planetary Science Letters*, *507*, 1–9.
775   https://doi.org/10.1016/j.epsl.2018.11.019

776 Desjarlais, M. P. (2013). First-principles calculation of entropy for liquid metals. *Physical*
777   *Review E*, *88*(6), 062145. https://doi.org/10.1103/PhysRevE.88.062145

778 Dewaele, A., Loubeyre, P., Occelli, F., Mezouar, M., Dorogokupets, P. I., & Torrent, M. (2006).
779   Quasihydrostatic equation of state of iron above 2 Mbar. *Physical Review Letters*,
780   *97*(21), 215504. https://doi.org/10.1103/PhysRevLett.97.215504

781 Dubrovinsky, L., Dubrovinskaia, N., Narygina, O., Kantor, I., Kuznetzov, A., Prakapenka, V.,
782   Vitos, L., Johansson, B., Mikhaylushkin, A., & Simak, S. (2007). Body-centered cubic
783   iron-nickel alloy in Earth's core. *Science*, *316*(5833), 1880–1883.
784   https://doi.org/10.1126/science.1142105

785 Dziewonski, A. M., & Anderson, D. L. (1981). Preliminary reference Earth model. *Physics of*
786   *the Earth and Planetary Interiors*, *25*(4), 297–356.
787   https://doi.org/10.17611/DP/9991844

788 Flyvbjerg, H., & Petersen, H. G. (1989). Error estimates on averages of correlated data. *The*
789   *Journal of chemical physics*, *91*(1), 461–466. https://doi.org/10.1063/1.457480

790 Frenkel, D., & Smit, B. (2002). Understanding molecular simulation. *Academic Press, San*
791   *Diego*. https://doi.org/10.1016/B978-0-12-267351-1.X5000-7

792 Gao, C., Ho, K.-M., Wentzcovitch, R. M., & Sun, Y. (2025). Understanding the two-step
793   nucleation of iron at Earth's inner core conditions: A comparative molecular dynamics
794   study. *Physical Review B*, *111*(13), 134104.
795   https://doi.org/10.1103/PhysRevB.111.134104

796 Ghosh, M., Zhang, S., Hu, L., & Hu, S. X. (2023). Cooperative diffusion in body-centered cubic
797   iron in Earth and super-Earths' inner core conditions. *Journal of Physics: Condensed*
798   *Matter*, *35*(15), 154002. https://doi.org/10.1088/1361-648X/acba71

799 Gleason, A., & Mao, W. (2013). Strength of iron at core pressures and evidence for a weak
800   Earth's inner core. *Nature Geoscience*, *6*(7), 571–574.
801   https://doi.org/10.1038/ngeo1808

802 Godwal, B. K., González-Cataldo, F., Verma, A. K., Stixrude, L., & Jeanloz, R. (2015).
803   Stability of iron crystal structures at 0.3–1.5 TPa. *Earth and Planetary Science Letters*,
804   *409*, 299-306. https://doi.org/10.1016/j.epsl.2014.10.056

805 González-Cataldo, F., & Militzer, B. (2023). Ab initio determination of iron melting at

806   terapascal pressures and Super-Earths core crystallization. *Physical Review Research*,
807   5(3), 033194. https://doi.org/10.1103/PhysRevResearch.5.033194

808   Hernandez, J. A., Mohn, C. E., Guren, M. G., Baron, M. A., & Trønnes, R. G. (2022). Ab Initio
809   Atomistic Simulations of Ca-Perovskite Melting. *Geophysical Research Letters*,
810   *49*(20), e2021GL097262. https://doi.org/10.1029/2021GL097262

811   Hikosaka, K., Tagawa, S., Hirose, K., Okuda, Y., Oka, K., Umemoto, K., & Ohishi, Y. (2022).
812   Melting phase relations in Fe–Si–H at high pressure and implications for Earth's inner
813   core crystallization. *Scientific Reports*, *12*(1), 10000. https://doi.org/10.1038/s41598-
814   022-14106-z

815   Hirose, K., Wood, B., & Vočadlo, L. (2021). Light elements in the Earth's core. *Nature Reviews*
816   *Earth & Environment*, *2*(9), 645–658. https://doi.org/10.1038/s43017-021-00203-6

817   Hrubiak, R., Meng, Y., & Shen, G. (2018). Experimental evidence of a body centered cubic
818   iron   at   the   Earth's   core   condition.   *arXiv.*,   1804.05109.
819   https://doi.org/10.48550/arXiv.1804.05109

820   Ikuta, D., Ohtani, E., Fukui, H., Sakai, T., Ishikawa, D., & Baron, A. Q. (2022). Sound velocity
821   of hexagonal close-packed iron to the Earth's inner core pressure. *Nature*
822   *communications*, *13*(1), 7211. https://doi.org/10.1038/s41467-022-34789-2

823   Jana, R., & Caro, M. A. (2023). Searching for iron nanoparticles with a general-purpose
824   Gaussian   approximation   potential.   *Physical   Review   B*,   *107*(24),   245421.
825   https://doi.org/10.1103/PhysRevB.107.245421

826   Kohn, W., & Sham, L. J. (1965). Self-Consistent Equations Including Exchange and
827   Correlation   Effects.   *Physical   Review*,   *140*(4A),   A1133–A1138.
828   https://doi.org/10.1103/physrev.140.a1133

829   Kraus, R. G., Hemley, R. J., Ali, S. J., Belof, J. L., Benedict, L. X., Bernier, J., Braun, D.,
830   Cohen, R., Collins, G. W., & Coppari, F. (2022). Measuring the melting curve of iron
831   at   super-Earth   core   conditions.   *Science*,   *375*(6577),   202–205.
832   https://doi.org/10.1126/science.abm1472

833   Kresse, G., & Furthmüller, J. (1996). Efficient iterative schemes for ab initio total-energy
834   calculations using a plane-wave basis set. *Physical Review B*, *54*(16), 11169–11186.
835   https://doi.org/10.1103/physrevb.54.11169

836   Kuwayama, Y., Hirose, K., Sata, N., & Ohishi, Y. (2008). Phase relations of iron and iron–
837   nickel alloys up to 300 GPa: Implications for composition and structure of the Earth's
838   inner   core.   *Earth   and   Planetary   Science   Letters*,   *273*(3-4),   379–385.
839   https://doi.org/10.1016/j.epsl.2008.07.001

840   Lai, P.-K., Hsieh, C.-M., & Lin, S.-T. (2012). Rapid determination of entropy and free energy
841   of mixtures from molecular dynamics simulations with the two-phase thermodynamic
842   model.   *Physical   Chemistry   Chemical   Physics*,   *14*(43),   15206–15213.
843   https://doi.org/10.1039/C2CP42011B

844   Laio, A., Bernard, S., Chiarotti, G., Scandolo, S., & Tosatti, E. (2000). Physics of iron at Earth's
845   core   conditions.   *Science*,   *287*(5455),   1027–1030.
846   https://doi.org/10.1126/science.287.5455.1027

847   Li, J., Wu, Q., Li, J., Xue, T., Tan, Y., Zhou, X., Zhang, Y., Xiong, Z., Gao, Z., & Sekine, T.
848   (2020). Shock melting curve of iron: A consensus on the temperature at the Earth's
849   inner core boundary. *Geophysical Research Letters*, *47*(15), e2020GL087758.

850   https://doi.org/10.1029/2020GL087758

851 Li, Y., Vočadlo, L., Brodholt, J., & Wood, I. (2016). Thermoelasticity of Fe_7C_3 under inner
852   core conditions. *Journal of Geophysical Research: Solid Earth*, *121*(8), 5828–5837.
853   https://doi.org/10.1002/2016JB013155

854 Li, Y., Vočadlo, L., & Brodholt, J. P. (2018). The elastic properties of hcp-Fe alloys under the
855   conditions of the Earth's inner core. *Earth and Planetary Science Letters*, *493*, 118–
856   127. https://doi.org/10.1016/j.epsl.2018.04.013

857 Li, Z., & Scandolo, S. (2022). Elasticity and Viscosity of hcp Iron at Earth's Inner Core
858   Conditions From Machine Learning-Based Large-Scale Atomistic Simulations.
859   *Geophysical Research Letters*, *49*(24), e2022GL101161.
860   https://doi.org/10.1029/2022gl101161

861 Li, Z., & Scandolo, S. (2024a). Competing phases of iron at Earth's core conditions from deep-
862   learning-aided ab-initio simulations. *Geophysical Research Letters*, *51*(19),
863   e2024GL110357. https://doi.org/10.1029/2024GL110357

864 Li, Z., & Scandolo, S. (2024b). Deep-learning interatomic potential for iron at extreme
865   conditions. *Physical Review B*, *109*(18), 184108.
866   https://doi.org/10.1103/physrevb.109.184108

867 Lin, S.-T., Blanco, M., & Goddard III, W. A. (2003). The two-phase model for calculating
868   thermodynamic properties of liquids from molecular dynamics: Validation for the
869   phase diagram of Lennard-Jones fluids. *The Journal of Chemical Physics*, *119*(22),
870   11792–11805. https://doi.org/10.1063/1.1624057

871 Litasov, K. D., & Shatskiy, A. (2016). Composition of the Earth's core: A review. *Russian*
872   *Geology and Geophysics*, *57*(1), 22–46. https://doi.org/10.1016/j.rgg.2016.01.003

873 Luo, W., Johansson, B., Eriksson, O., Arapan, S., Souvatzis, P., Katsnelson, M. I., & Ahuja, R.
874   (2010). Dynamical stability of body center cubic iron at the Earth's core conditions.
875   *Proceedings of the National Academy of Sciences*, *107*(22), 9962–9964.
876   https://doi.org/10.1073/pnas.1004076107

877 Martorell, B., Brodholt, J., Wood, I. G., & Vočadlo, L. (2015). The elastic properties and
878   stability of fcc-Fe and fcc-FeNi alloys at inner-core conditions. *Geophysical Journal*
879   *International*, *202*(1), 94–101. https://doi.org/10.1093/gji/ggv128

880 Matsui, M., & Anderson, O. L. (1997). The case for a body-centered cubic phase (α′) for iron
881   at inner core conditions. *Physics of the Earth and Planetary Interiors*, *103*(1-2), 55–62.
882   https://doi.org/10.1016/S0031-9201(97)00020-4

883 Mattesini, M., Belonoshko, A. B., Buforn, E., Ramírez, M., Simak, S. I., Udias, A., Mao, H.-
884   K., & Ahuja, R. (2010). Hemispherical anisotropic patterns of the Earth's inner core.
885   *Proceedings of the National Academy of Sciences*, *107*(21), 9507–9512.
886   https://doi.org/10.1073/pnas.1004856107

887 Mermin, N. D. (1965). Thermal properties of the inhomogeneous electron gas. *Physical Review*,
888   *137*(5A), A1441–A1443. https://doi.org/10.1103/PhysRev.137.A1441

889 Mikhaylushkin, A. S., Simak, S. I., Dubrovinsky, L., Dubrovinskaia, N., Johansson, B., &
890   Abrikosov, I. A. (2007). Pure iron compressed and heated to extreme conditions.
891   *Physical Review Letters*, *99*(16), 165505.
892   https://doi.org/10.1103/PhysRevLett.99.165505

893 Nosé, S. (1984). A unified formulation of the constant temperature molecular dynamics

methods. *The Journal of chemical physics*, *81*(1), 511–519. https://doi.org/10.1063/1.447334

Ozolins, V. (2009). First-principles calculations of free energies of unstable phases: the case of fcc W. *Physical Review Letters*, *102*(6), 065702. https://doi.org/10.1103/PhysRevLett.102.065702

Perdew, J. P., Burke, K., & Ernzerhof, M. (1996). Generalized Gradient Approximation Made Simple. *Physical Review Letters*, *77*(18), 3865–3868. https://doi.org/10.1103/PhysRevLett.77.3865

Pushcharovsky, D. Y. (2019). Iron and its compounds in the Earth's core: New data and ideas. *Geochemistry International*, *57*, 941–955. https://doi.org/10.1134/S0016702919090088

Romanowicz, B., Cao, A., Godwal, B., Wenk, R., Ventosa, S., & Jeanloz, R. (2016). Seismic anisotropy in the Earth's innermost inner core: Testing structural models against mineral physics predictions. *Geophysical Research Letters*, *43*(1), 93–100. https://doi.org/10.1002/2015GL066734

Ross, M., Young, D. A., & Grover, R. (1990). Theory of the iron phase diagram at Earth core conditions. *Journal of Geophysical Research: Solid Earth*, *95*(B13), 21713-21716. https://doi.org/10.1029/JB095iB13p21713

Schultz, A. J., Moustafa, S. G., & Kofke, D. A. (2018). No system-size anomalies in entropy of bcc iron at Earth's inner-core conditions. *Scientific Reports*, *8*(1), 7295. https://doi.org/10.1038/s41598-018-25419-3

Sha, X., & Cohen, R. (2010). Elastic isotropy of ε-Fe under Earth's core conditions. *Geophysical Research Letters*, *37*(10), L10302. https://doi.org/10.1029/2009GL042224

Shen, G., Mao, H. k., Hemley, R. J., Duffy, T. S., & Rivers, M. L. (1998). Melting and crystal structure of iron at high pressures and temperatures. *Geophysical Research Letters*, *25*(3), 373–376. https://doi.org/10.1029/97GL03776

Sinmyo, R., Hirose, K., & Ohishi, Y. (2019). Melting curve of iron to 290 GPa determined in a resistance-heated diamond-anvil cell. *Earth and Planetary Science Letters*, *510*, 45–52. https://doi.org/10.1016/J.EPSL.2019.01.006

Soderlind, P., Moriarty, J. A., & Wills, J. M. (1996). First-principles theory of iron up to earth-core pressures: Structural, vibrational, and elastic properties. *Physical Review B: Condens Matter*, *53*(21), 14063–14072. https://doi.org/10.1103/physrevb.53.14063

Sola, E., & Alfe, D. (2009). Melting of Iron under Earth's Core Conditions from Diffusion Monte Carlo Free Energy Calculations. *Physical Review Letters*, *103*(7), 078501. https://doi.org/10.1103/PhysRevLett.103.078501

Steinle-Neumann, G., Stixrude, L., Cohen, R., & Gülseren, O. (2001). Elasticity of iron at the temperature of the Earth's inner core. *Nature*, *413*(6851), 57–60. https://doi.org/10.1038/35092536

Stixrude, L. (2012). Structure of iron to 1 Gbar and 40, 000 K. *Physical Review Letters*, *108*(5), 055505. https://doi.org/10.1103/PhysRevLett.108.055505

Stixrude, L., & Cohen, R. E. (1995). Constraintson the crystallinestructure of the inner core: Mechanical instability of BCC iron at high pressure. *Geophysical Research Letters*, *22*(2), 125–128. https://doi.org/10.1029/94GL02742

938 Sun, T., Brodholt, J. P., Li, Y., & Vočadlo, L. (2018). Melting properties from ab initio free
939   energy calculations: Iron at the Earth's inner-core boundary. *Physical Review B*, *98*(22),
940   224301. https://doi.org/10.1103/PhysRevB.98.224301

941 Sun, T., Xian, J., Zhang, H., Zhang, Z., & Zhang, Y. (2017). Two-phase thermodynamic model
942   for computing entropies of liquids reanalyzed. *The Journal of Chemical Physics*,
943   *147*(19), 194505. https://doi.org/10.1063/1.5001798

944 Sun, Y., Mendelev, M. I., Zhang, F., Liu, X., Da, B., Wang, C.-Z., Wentzcovitch, R. M., & Ho,
945   K.-M. (2024). Unveiling the effect of Ni on the formation and structure of Earth's inner
946   core. *Proceedings of the National Academy of Sciences*, 121(4), e2316477121.
947   https://doi.org/10.1073/pnas.2316477121

948 Sun, Y., Mendelev, M. I., Zhang, F., Liu, X., Da, B., Wang, C. Z., Wentzcovitch, R. M., & Ho,
949   K. M. (2023). Ab Initio Melting Temperatures of Bcc and Hcp Iron Under the Earth's
950   Inner Core Condition. *Geophysical Research Letters*, *50*(5), e2022GL102447.
951   https://doi.org/10.1029/2022gl102447

952 Sun, Y., Zhang, F., Mendelev, M. I., Wentzcovitch, R. M., & Ho, K. M. (2022). Two-step
953   nucleation of the Earth's inner core. *Proceedings of the National Academy of Sciences*,
954   *119*(2), e2113059119. https://doi.org/10.1073/pnas.2113059119

955 Tateno, S., Hirose, K., Ohishi, Y., & Tatsumi, Y. (2010). The structure of iron in Earth's inner
956   core. *Science*, *330*, 359–361. https://doi.org/10.1126/science.1194662

957 Tateno, S., Ozawa, H., Hirose, K., Suzuki, T., I-Kawaguchi, S., & Hirao, N. (2019). Fe$_2$S: The
958   Most Fe-Rich Iron Sulfide at the Earth's Inner Core Pressures. *Geophysical Research*
959   *Letters*, *46*(21), 11944–11949. https://doi.org/10.1029/2019GL085248

960 Turneaure, S. J., Sharma, S. M., & Gupta, Y. M. (2020). Crystal Structure and Melting of Fe
961   Shock Compressed to 273 GPa: In Situ X-Ray Diffraction. *Physical Review Letters*,
962   *125*(21), 215702. https://doi.org/10.1103/PhysRevLett.125.215702

963 Vočadlo, L., Alfè, D., Gillan, M. J., Wood, I. G., Brodholt, J. P., & Price, G. D. (2003). Possible
964   thermal and chemical stabilization of body-centred-cubic iron in the Earth's core.
965   *Nature*, *424*(6948), 532–536. https://doi.org/10.1038/nature01829

966 Vočadlo, L., Brodholt, J., Alfè, D., Gillan, M. J., & Price, G. D. (2000). Ab initio free energy
967   calculations on the polymorphs of iron at core conditions. *Physics of the Earth and*
968   *Planetary Interiors*, *117*(1-4), 123–137. https://doi.org/10.1016/S0031-
969   9201(99)00092-8

970 Vočadlo, L., Brodholt, J., Alfè, D., Price, G. D., & Gillan, M. J. (1999). The structure of iron
971   under the conditions of the Earth's inner core. *Geophysical Research Letters*, *26*(9),
972   1231–1234. https://doi.org/10.1029/1999GL900214

973 Vočadlo, L., Wood, I. G., Alfè, D., & Price, G. D. (2008). Ab initio calculations on the free
974   energy and high P–T elasticity of face-centred-cubic iron. *Earth and Planetary Science*
975   *Letters*, *268*(3-4), 444–449. https://doi.org/10.1016/j.epsl.2008.01.043

976 Vočadlo, L., Wood, I. G., Gillan, M. J., Brodholt, J., Dobson, D. P., Price, G. D., & Alfè, D.
977   (2008). The stability of bcc-Fe at high pressures and temperatures with respect to
978   tetragonal strain. *Physics of the Earth and Planetary Interiors*, *170*(1-2), 52–59.
979   https://doi.org/10.1016/j.pepi.2008.07.032

980 Williams, Q., Jeanloz, R., Bass, J., Svendsen, B., & Ahrens, T. J. (1987). The melting curve of
981   iron to 250 gigapascals: A constraint on the temperature at Earth's center. *Science*,

236(4798), 181–182. https://doi.org/10.1126/science.236.4798.181

Wilson, A., & Stixrude, L. (2021). Entropy, dynamics, and freezing of CaSiO$_3$ liquid. *Geochimica et Cosmochimica Acta*, *302*, 1–17. https://doi.org/10.1016/j.gca.2021.03.015

Wilson, A. J., Alfè, D., Walker, A. M., & Davies, C. J. (2023). Can homogeneous nucleation resolve the inner core nucleation paradox? *Earth and Planetary Science Letters*, *614*, 118176. https://doi.org/10.1016/j.epsl.2023.118176

Wu, F., Wu, S., Wang, C.-Z., Ho, K.-M., Wentzcovitch, R. M., & Sun, Y. (2024). Melting temperature of iron under the Earth's inner core condition from deep machine learning. *Geoscience Frontiers*, *15*(6), 101925. https://doi.org/10.1016/j.gsf.2024.101925

Xu, Y., He, Y., Sun, S., Zhang, W., Dai, W., Kim, D. Y., & Li, H. (2025). Viscosities of hcp iron alloys under Earth's inner core conditions. *Geoscience Frontiers*, *16*(1), 101935. https://doi.org/10.1016/j.gsf.2024.101935

Yang, H., Dou, P., Xiao, T., Li, Y., Muir, J. M. R., & Zhang, F. (2023). The Geophysical Properties of FeH$_x$ Phases Under Inner Core Conditions. *Geophysical Research Letters*, *50*(22), e2023GL104493. https://doi.org/10.1029/2023gl104493

Yang, H., Wan, L., Li, Y., Vočadlo, L., & Brodholt, J. (2025). Molecular-Dynamics Study of the Crystal Structure of Iron Under the Earth's Inner Core Conditions (Version 1). *Figshare*. [Dataset]. https://figshare.com/s/18ba3094bc4496753b5d

Yuan, L., & Steinle-Neumann, G. (2023). Hydrogen distribution between the Earth's inner and outer core. *Earth and Planetary Science Letters*, *609*, 118084. https://doi.org/10.1016/j.epsl.2023.118084

Zhang, S., Panjwani, A., Xiao, P., Ghosh, M., Ogitsu, T., Ping, Y., & Hu, S. (2025). Thermally induced structural competitiveness and metastability of body-centered-cubic iron under nonequilibrium conditions. *Physical Review B*, *111*(22), 224106. https://doi.org/10.1103/ws64-kmzr

Zhang, Y., Wang, Y., Huang, Y., Wang, J., Liang, Z., Hao, L., Gao, Z., Li, J., Wu, Q., & Zhang, H. (2023). Collective motion in hcp-Fe at Earth's inner core conditions. *Proceedings of the National Academy of Sciences*, *120*(41), e2309952120. https://doi.org/10.1073/pnas.2309952120

Zhang, Z., Csányi, G., & Alfè, D. (2020). Partitioning of sulfur between solid and liquid iron under Earth's core conditions: Constraints from atomistic simulations with machine learning potentials. *Geochimica et Cosmochimica Acta*, *291*, 5–18. https://doi.org/10.1016/j.gca.2020.03.028

Zwanzig, R. W. (1954). High-temperature equation of state by a perturbation method. I. Nonpolar gases. *The Journal of Chemical Physics*, *22*(8), 1420–1426. https://doi.org/10.1063/1.1740409

1020 **References From the Supporting Information**

1021 Jana, R., & Caro, M. A. (2023). Searching for iron nanoparticles with a general-purpose
1022   Gaussian approximation potential. *Physical Review B*, 107(24), 245421.
1023   https://doi.org/10.1103/PhysRevB.107.245421

1024