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## Multi-objective Optimization on Steady-state Thermodynamic Parameters of S-CO<sub>2</sub> Recompression Brayton Cycle Power Generation System for Marine Waste Heat Recovery

--Manuscript Draft--

<b>Full Title:</b>	Multi-objective Optimization on Steady-state Thermodynamic Parameters of S-CO <sub>2</sub> Recompression Brayton Cycle Power Generation System for Marine Waste Heat Recovery
<b>Manuscript Number:</b>	TMAR-2020-0118R1
<b>Article Type:</b>	Original Article
<b>Keywords:</b>	S-CO <sub>2</sub> recompression Brayton cycle; main engine exhaust gas; waste heat recovery; multi-objective optimization; decision making
<b>Abstract:</b>	Analysis of thermodynamic parameters' effects on the S-CO <sub>2</sub> recompression Brayton cycle for recovering the main engine exhaust gas waste heat of an ocean-going 9000 TEU container ship are carried out first in this paper. NSGA-II algorithm-based multi-objective optimizations are conducted to maximize net power output and exergetic efficiency as well as to minimize the levelized cost of energy (LCOE). The final optimal result from Pareto front solutions is decided by decision-making processes. The results show that the LCOE increases along with the enhancement of net power output and exergetic efficiency, and the maximal objectives always appear near the upper boundary of exhaust gas temperature. The final optimal result decided by TOPSIS decision-making has higher rationality and accuracy than that obtained by LINMAP method. Regarding the final optimal results of triple-objective and dual-objective optimizations obtained by TOPSIS method, the former achieved more reasonable results, since its optimal net power output and exergetic efficiency are 1.29% and 5.11% higher than the latter, while its LCOE increased by 2.28% as a result of the increase of the net power output. The recompression Brayton cycle is better for recovering the exhaust gas waste heat in ships compared with the simple recuperative cycle without recompression.
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<b>Response to Reviewers:</b>	List of Responses Note: Revised portions are marked in red in the manuscript. The main corrections and the responds to the reviewers' comments are as follows:  Reviewer #1: This is a well written article. I would recommend it to be accepted, subject to minor comments below. (1) Is the fig. 1 derived by the authors? If not, permission to publish this figure in this journal should be seeked. Same comment applies to other figures. Responds: Thanks for the reviewer's suggestion. The data in Fig.1 was quoted from the published research papers include Singh et al. 2016, Yuan et al. 2018 and Shu et al.2017, but it was plotted by us. And, all the other figures in the whole paper were plotted by us.  (2) Moroz et al. (Moroz et al. 2015) - just mention Moroz et al. (2015). You don't have to mention the name twice. Responds: Thanks for the reviewer's suggestion. We have revised all similar references in the paper according to the reviewer's comments. For example, "Tian et

al. (Tian et al. 2017) presented a systematic multi-objective optimization by GA to optimize the key parameters of carbon dioxide transcritical power cycles to ensure that the system can generate power efficiently and economically."

(3) It was interesting to observe that the LCOE is exponentially increasing with  $W_{net}$  and  $\eta_{ex}$  for the solutions on pareto front. To what would you attribute that?

Responds: Thanks for the reviewer's comments. If the system net power output  $W_{net}$  needs to be further improved, the heat exchanger area per unit power APR will increase significantly, resulting in the increasing of the structural size of the whole system and the increasing of the cost of the whole system.

(4) PIs provide in a short paragraph in conclusions recommendations for future research.

Responds: Thanks for the reviewer's suggestion. A short paragraph in conclusions recommendations for future research was added in the part of Conclusions.

Conclusions recommendations: In this study, the working fluid CO<sub>2</sub> in the system is considered to be always in the supercritical state. However, considering that when the system is shut down and restarted, some of the remaining working fluid CO<sub>2</sub> in the system may not be in its supercritical state. Thus, the influence of the transcritical CO<sub>2</sub> on performance of S-CO<sub>2</sub> recompression Brayton cycle system needs to be further studied.

Reviewer #2: 1- Section 4.2.2, paragraph 1, line 23-24

(1) More clarification needed on the obtained results of TOPSIS and LINMAP. provide an illustration on the mathematical calculations

Responds: Thanks for the reviewer's suggestion. Actually, the obtained results of TOPSIS and LINMAP in section 4.2.2, paragraph 1, line 23-24 were calculated by the deviation index  $R_d$ , calculated as:

(19)

Table 7

Multi-objective optimization results by using LINMAP and TOPSIS decision makings.

Parameters Ideal point Nadir point LINMAP TOPSIS

$W_{net}$  (kW) 313.30 107.50 261.50 272.20

$\eta_{ex}$  (%) 40.19 13.40 33.71 35.04

LCOE (\$/kWh) 0.01080 0.03000 0.02050 0.0219

$x$  0.990 1.00 0.670 0.72

$m_t$  (kg/s) 11.99 12.00 11.99 12.00

$T_g$  (K) 733.05 732.79 732.76 732.53

Deviation index 0.251 0.170 0.1997

Fig.12. The pareto front curve of triple-objective for the presented system.

The deviation index calculation method of the TOPSIS and LINMAP was based on the formula (19).

As can be seen from Fig 12 and Table 7,  $f_j$ \_LINMAP=268.7,  $f_j$ \_TOPSIS=272.20,  $f_j$ ideal=313.3,  $f_j$ nadir=107.5. So, the deviation index of the TOPSIS and LINMAP methods were calculated as:

$R_d$ \_LINMAP=0.2517;

$R_d$ \_TOPSIS=0.1997.

(2) References number 12 & 13 need to be distinguished in text as they appear as same (name and year), however, they are different.

Responds: Thanks for the reviewer's suggestion. We changed the quotation form of Reference 13 (Crespi et al. 2017) to (Sánchez D et al. 2017).

"So far, as a result of the development in the research areas of the turbomachinery and the heat exchanger, S-CO<sub>2</sub> cycles have been successfully applied in the terrestrial power generation industry examples being concentrating solar power generation (Crespi Sánchez et al. 2017; Binotti et al. 2017; Polimeni et al. 2018; Belmonte et al. 2016; Al-Sulaiman et al. 2015), next-generation nuclear reactors (Dostal et al. 2004) and industrial waste heat recovery systems (Li et al. 2017; Yoon et al. 2017)]".

**Table 1**

Principal data of the ocean-going 9000 TEU container ship.

Items	Characteristics	Values
Principal dimension	Length (m)	300
	Moulded Breadth (m)	48.2
	Deadweight/DWT (t)	73125
	Voyage speed (kn)	21.5
Main engine	Engine type	8S90ME-C10.2
	Speed at $MCR_{ME}$ (r/min)	84.0
	$MCR_{ME}$ (kW)	41900
	$SFC_{ME}$ at 75% MCR (g/kWh)	159.61
	$SFC_{AE}$ (g/kWh)	185
	$P_{AE}$ (kW)	1435.75
	Exhaust temperature before turbocharger (°C)	460
	Exhaust temperature after turbocharger (°C)	270
	Exhaust mass flow rate (kg/s)	52.1
	Exhaust gas pressure (MPa)	0.308

**Table 2**The equations for different components of S-CO<sub>2</sub> recompression Brayton cycle.

Components	Energetic equations	Exergetic equations
Main compressor	$\eta_{isen,mc} = (h_{2s} - h_1) / (h_2 - h_1)$	$I_{mc} = W_{mc} / (E_2 - E_1)$
	$W_{mc} = m(h_2 - h_1)$	$\eta_{ex,mc} = (E_2 - E_1) / W_{mc}$
Recompression compressor	$\eta_{isen,rec} = (h_{10s} - h_9) / (h_{10} - h_9)$	$I_{rec} = W_{rec} / (E_{10} - E_9)$
	$W_{rec} = m(h_{10} - h_9)$	$\eta_{ex,rec} = (E_{10} - E_9) / W_{rec}$
HTR	$\varepsilon_{HTR} = (T_7 - T_8) / (T_7 - T_4)$	$I_{HTR} = E_7 - E_8 - (E_5 - E_4)$
	$Q_{HTR} = m(h_5 - h_4) = m(h_8 - h_7)$	$\eta_{ex,HTR} = (E_5 - E_4) / (E_7 - E_8)$
LTR	$Q_{LTR} = m(h_3 - h_2) = m(h_9 - h_8)$	$I_{LTR} = E_8 - E_9 - (E_3 - E_2)$
		$\eta_{ex,LTR} = (E_3 - E_2) / (E_8 - E_9)$
Turbine	$\eta_{isen,t} = (h_6 - h_7) / (h_6 - h_{7s})$	$I_t = E_6 - E_7 - W_t$
	$W_t = m(h_6 - h_7)$	$\eta_{ex,t} = W_t / (E_6 - E_7)$
Gas heat exchanger	$Q_{in} = m(h_6 - h_5)$	$I_{hx} = E_{gas,in} + E_5 - E_{gas,out} - E_6$
		$\eta_{ex,hx} = (E_6 - E_5) / (E_{gas,in} - E_{gas,out})$
Pre-cooler	$Q_{pre} = m(h_9 - h_1)$	$I_{pre} = E_{pre,in} + E_{water,in} - E_{pre,out} - E_{water,out}$
		$\eta_{ex,pre} = (E_{pre,out} - E_{pre,in}) / (E_{water,in} - E_{water,out})$

**Table 3**Economic data and cost function  $C_i$  for the proposed system.

System component	Unit	Cost functions
Main compressor	USD	$71.1 \cdot m_{mc} \cdot (1/0.92 - \eta_{mc}) \cdot p_r \cdot \ln(p_r)$
Re-compressor	USD	$71.1 \cdot m_{rc} \cdot (1/0.92 - \eta_{rc}) \cdot p_r \cdot \ln(p_r)$
Turbine	USD	$479.34 \cdot m_t \cdot (1/0.93 - \eta_t) \cdot \ln(p_t) \cdot (1 + \exp(0.036 \cdot T_{t,in} - 54.4))$
Precooler	USD	$2143 \cdot A^{0.514}_{PRC}$
HTR	USD	$2681 \cdot A^{0.514}_{HTR}$
LTR	USD	$2681 \cdot A^{0.514}_{LTR}$
Exhaust gas heat exchanger	USD	$2681 \cdot A^{0.514}_{hxr}$
Maintenance and operation factor	%	6.0

**Table 4**

Calculation results in the present paper compared with Ref. [37].

$T_{mc,in}$ (°C)	$m_t$ (kg/s) Ref.	$m_t$ (kg/s) Present	$RD$ (%)	$\eta_{th}$ ( % )	$\eta_{th}$ ( % )	$RD$ (%)
				Ref.	Present	
32	98.50	97.69	0.83	47.40	47.00	0.84
50	134.20	134.16	0.03	41.80	41.52	0.67

**Table 5**

Thermodynamic parameters and their initial values for system thermodynamic analysis and performance multi-objective optimization.

Parameters	Values
Ambient temperature (°C)	21
Ambient pressure (MPa)	0.1
Isentropic efficiency of the turbine (%)	70-80
Isentropic efficiency of the main compressor (%)	60-70
Isentropic efficiency of the re-compressor (%)	60-70
Pinch point temperature difference of LTR (°C)	5
Pinch point temperature difference of HTR (°C)	8
Flow split ratio	0.4
LTR effectiveness (%)	90
HTR effectiveness (%)	89

**Table 6**

Thermodynamic parameters for performance multi-objective optimization.

Parameters	Values
Main compressor inlet temperature (°C)	34
Main compressor inlet pressure (MPa)	8.0
Pressure ratio	2.5
Turbine inlet temperature (°C)	420
Turbine isentropic efficiency (%)	75
Re-compressor isentropic efficiency (%)	65
Main compressor isentropic efficiency (%)	65

**Table 7**

Multi-objective optimization results by using LINMAP and TOPSIS decision makings.

Parameters	Ideal point	Nadir point	LINMAP	TOPSIS
$W_{\text{net}}$ (kW)	313.30	107.50	261.50	272.20
$\eta_{\text{ex}}$ (%)	40.19	13.40	33.71	35.04
$LCOE$ (\$/kWh)	0.0108	0.0300	0.0205	0.0219
$x$	0.99	0.10	0.67	0.72
$m_t$ (kg/s)	11.99	12.00	11.99	12.00
$T_g$ (K)	733.05	732.79	732.76	732.53
Deviation index			0.2517	0.1997

**Table 8**Comparison between optimal solutions for dual-objective ( $W_{\text{net}}-LCOE$ ) optimization.

	Decision makings	Design variables		Objectives		Deviation index	
		$x$	$m_t$ (kg/s)	$T_g$ (K)	$W_{\text{net}}$ (kW)	$LCOE$ (\$/kWh)	
NSGA-II	LINMAP	0.67	11.99	732.76	259.90	0.0203	0.2595
	TOPSIS	0.70	11.99	733.15	268.70	0.0214	0.2167

**Table 9**Comparison between optimal solutions for dual-objective ( $\eta_{\text{ex}}-LCOE$ ) optimization.

	Decision makings	Design variables		Objectives		Deviation index	
		$x$	$m_t$ (kg/s)	$T_g$ (K)	$\eta_{\text{ex}}$ (%)	$LCOE$ (\$/kWh)	
NSGA-II	LINMAP	0.68	11.99	733.12	33.25	0.0200	0.2605
	TOPSIS	0.66	12.00	733.14	33.01	0.0190	0.2693

**Table 10**Comparison between optimal solutions for dual-objective ( $W_{\text{net}}\text{-}\eta_{\text{ex}}$ ) optimization.

	Decision makings	Design variables		Objectives		Deviation index
		$x$	$m_t$ (kg/s)	$T_g$ (K)	$W_{\text{net}}$ (kW)	
NSGA-II	LINMAP					
	TOPSIS		0.99	11.99	733.05	313.30
						40.19
						0

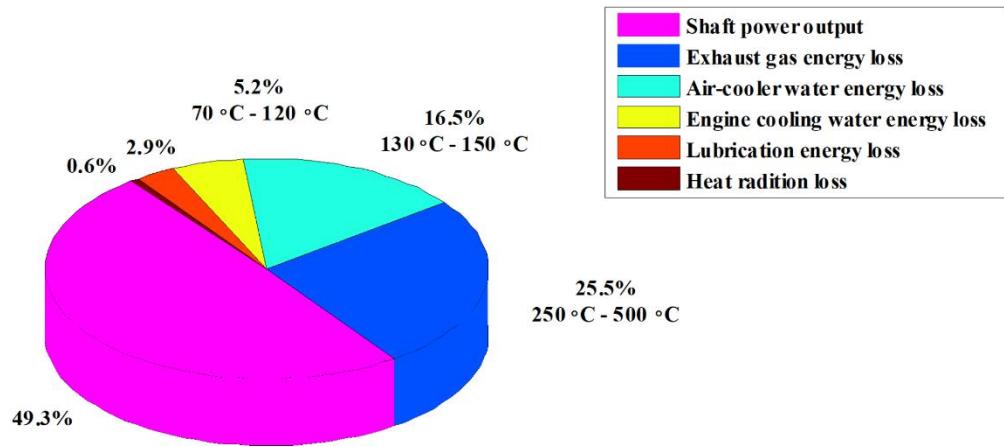


Fig.1. Energy balance of a large-scale low-speed two-stroke marine diesel engine.

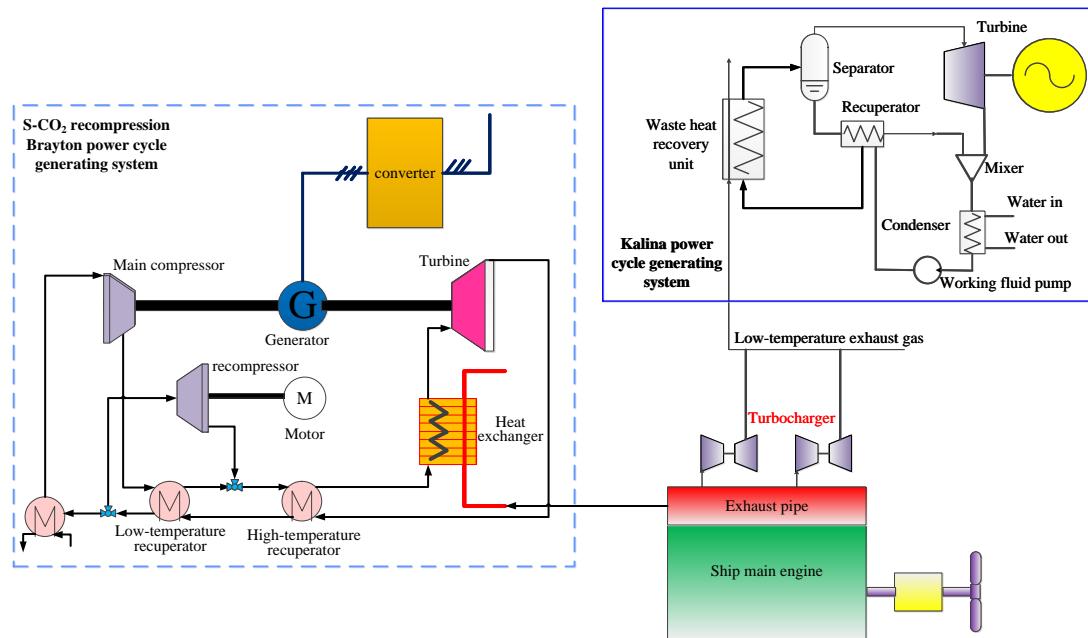


Fig.2. The general schematic diagram of the combined new power cycle generation system.

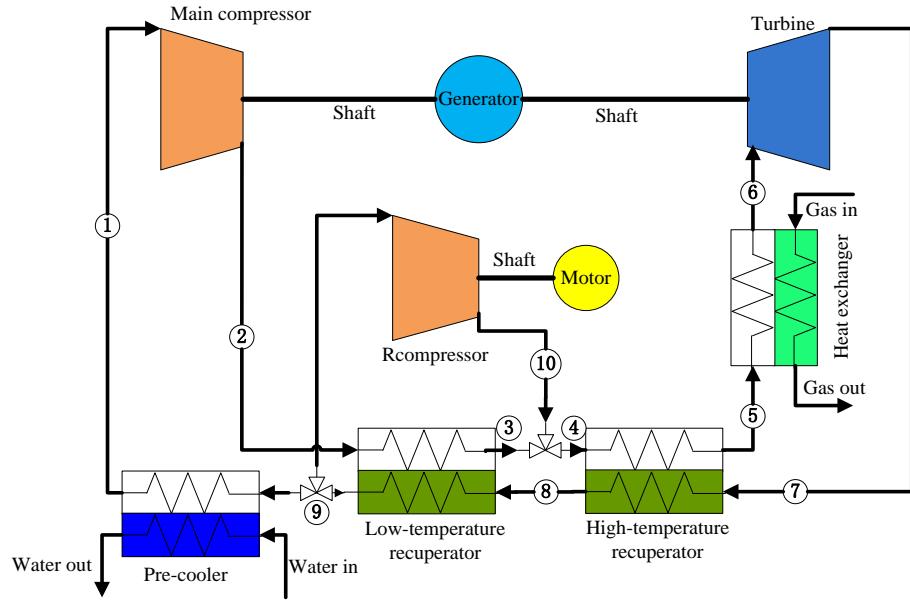


Fig.3. The system configuration of the S-CO<sub>2</sub> recompression Brayton power cycle.

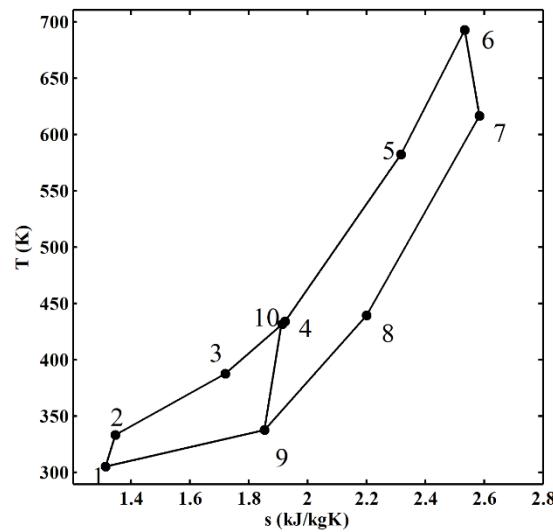


Fig. 4. *T-s* diagram of the S-CO<sub>2</sub> recompression Brayton power cycle.

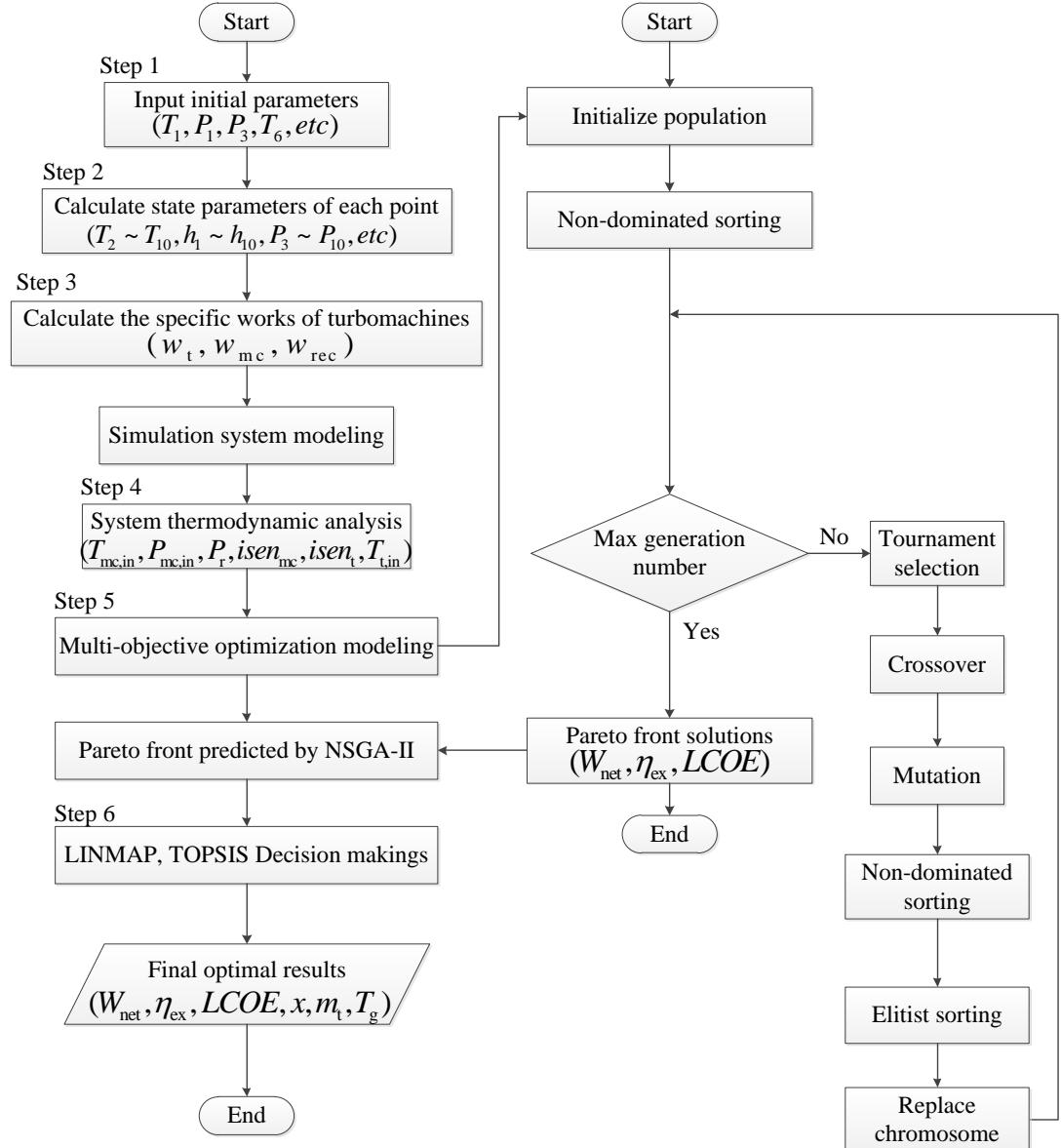


Fig.5. Flow chart of the thermodynamic analysis and parametric optimization.

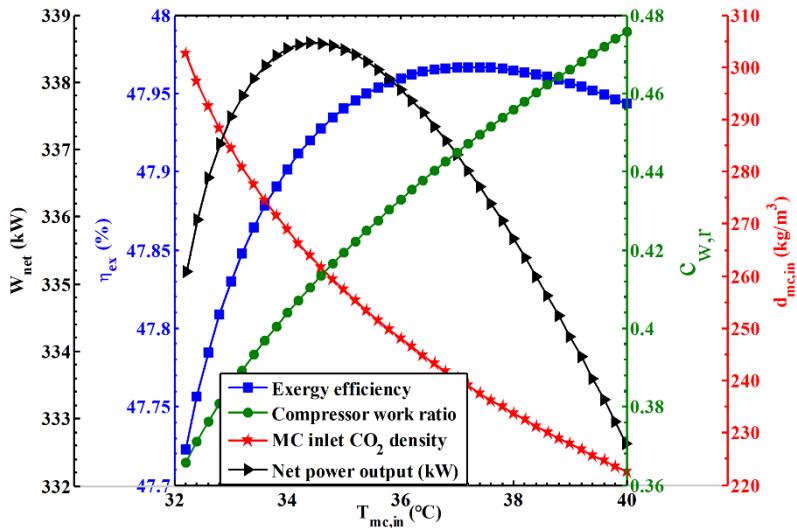


Fig. 6. Variations in different parameters with main compressor inlet temperature.

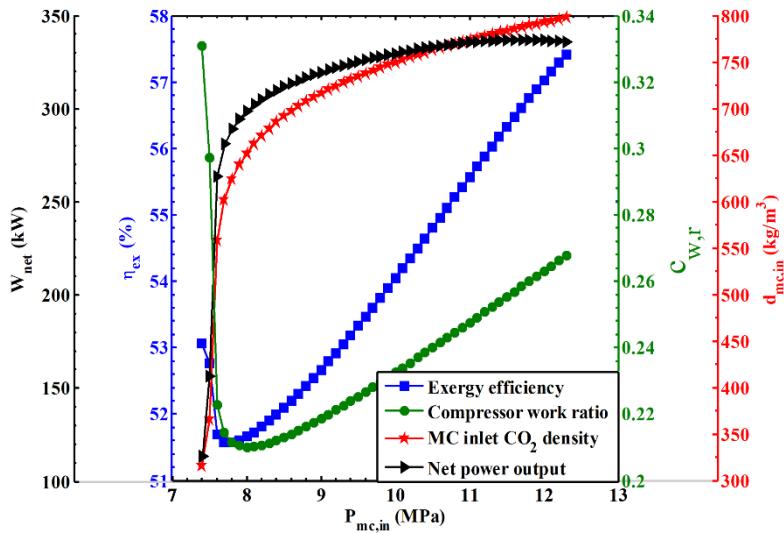


Fig. 7. Variations in different parameters with main compressor inlet pressure.

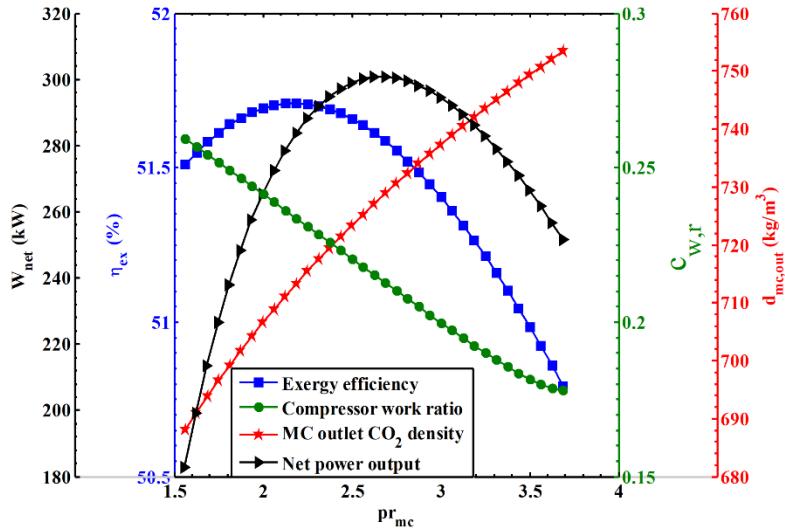


Fig. 8. Variations in different parameters with pressure ratio.

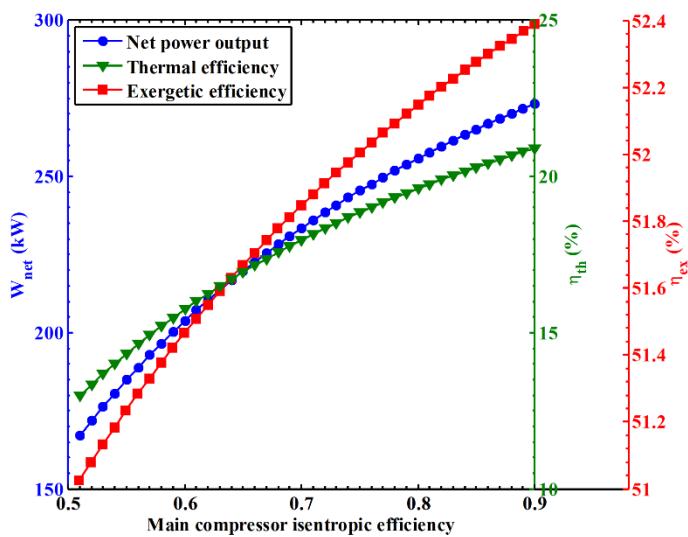


Fig. 9. Variations in system net power output, thermal efficiency and exergetic efficiency with main compressor isentropic efficiency.

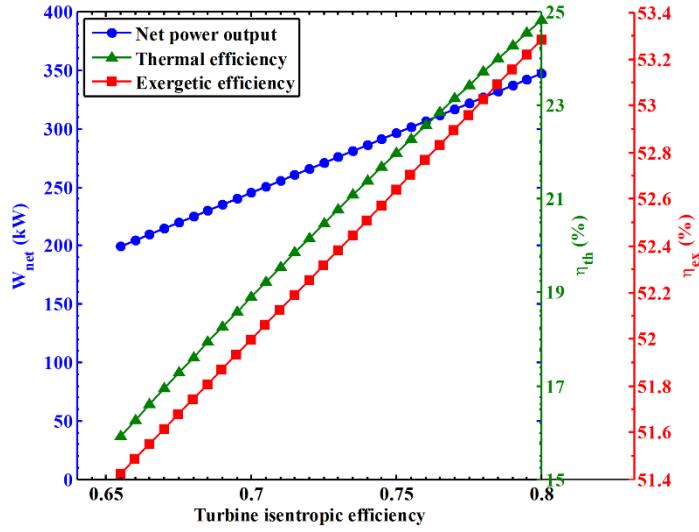


Fig. 10. Variations in system net power output, thermal efficiency and exergetic efficiency with turbine isentropic efficiency.

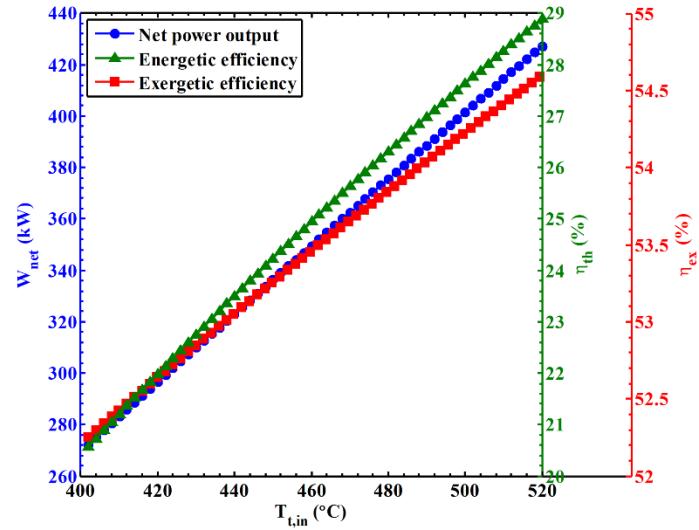


Fig. 11. Variations in system net power output, thermal efficiency and exergetic efficiency with turbine inlet temperature.

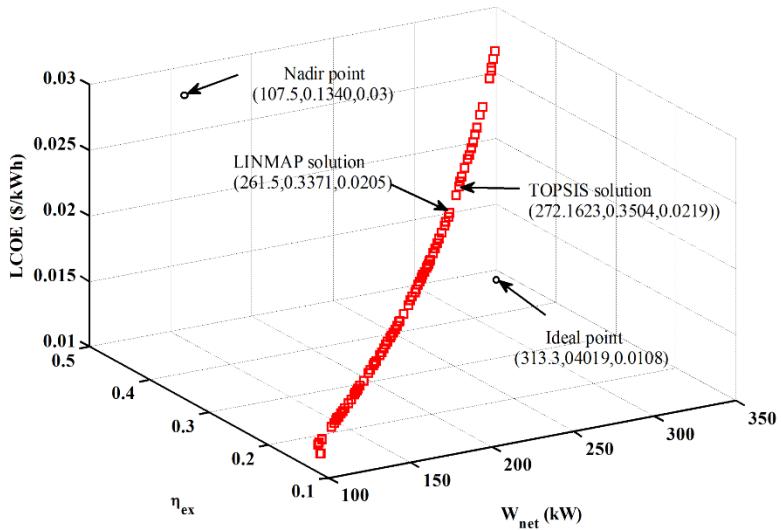


Fig. 12. The pareto front curve of triple-objective for the presented system.

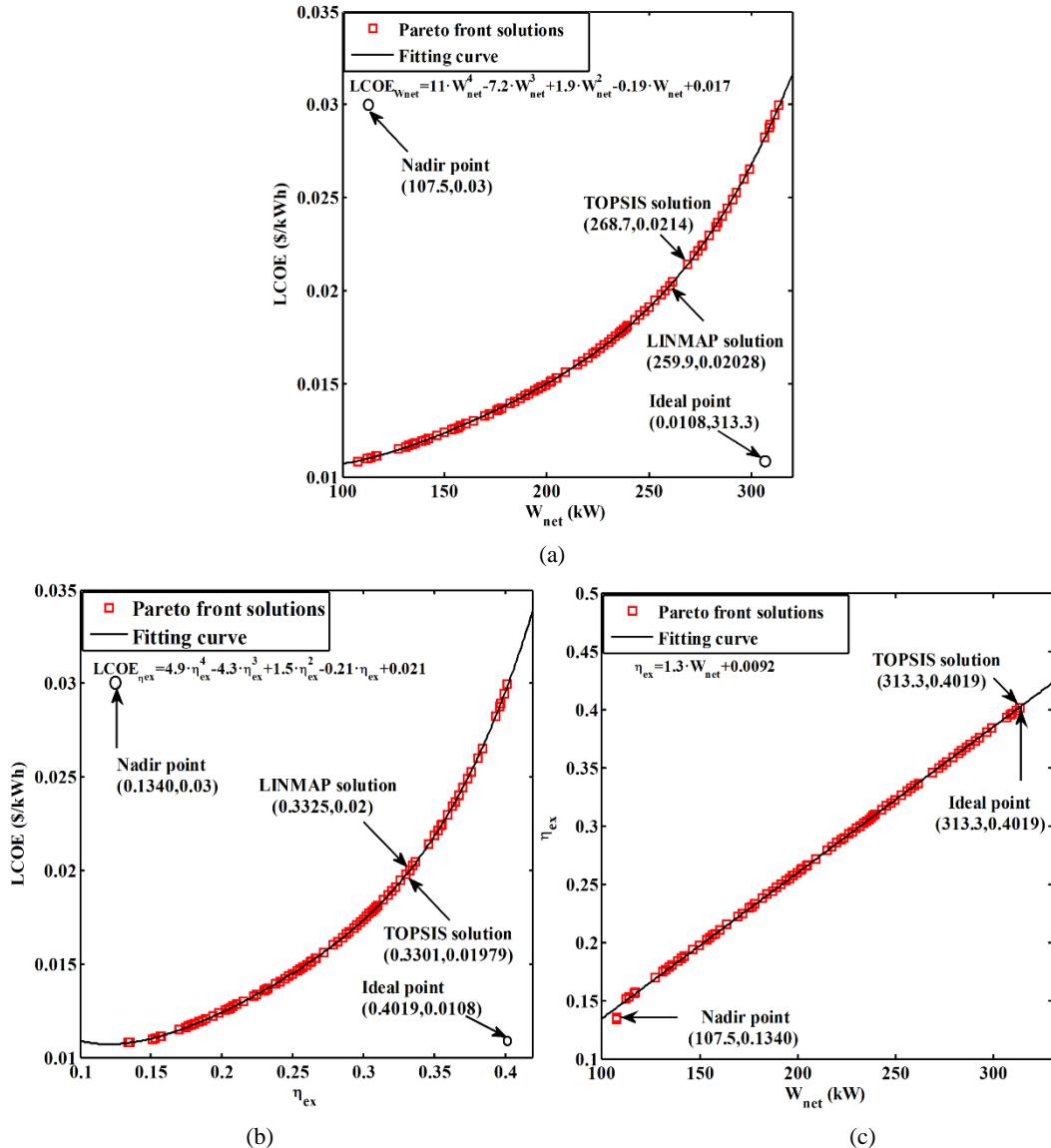
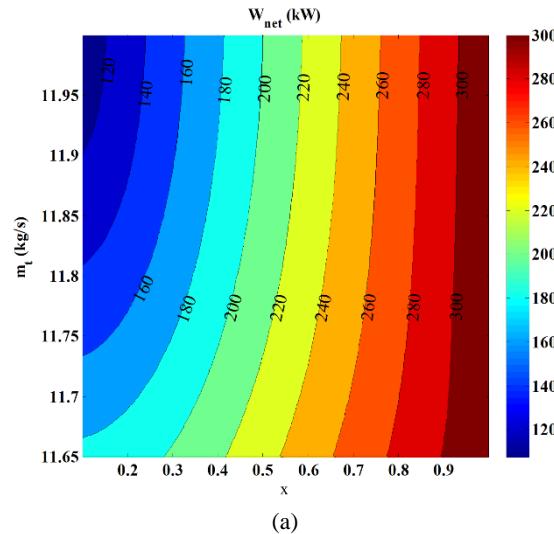


Fig.13. Pareto front solutions fitting curves: (a). Net power output and leveled cost of energy; (b). Exergetic efficiency and leveled cost of energy; (c). Net power output and exergetic efficiency.



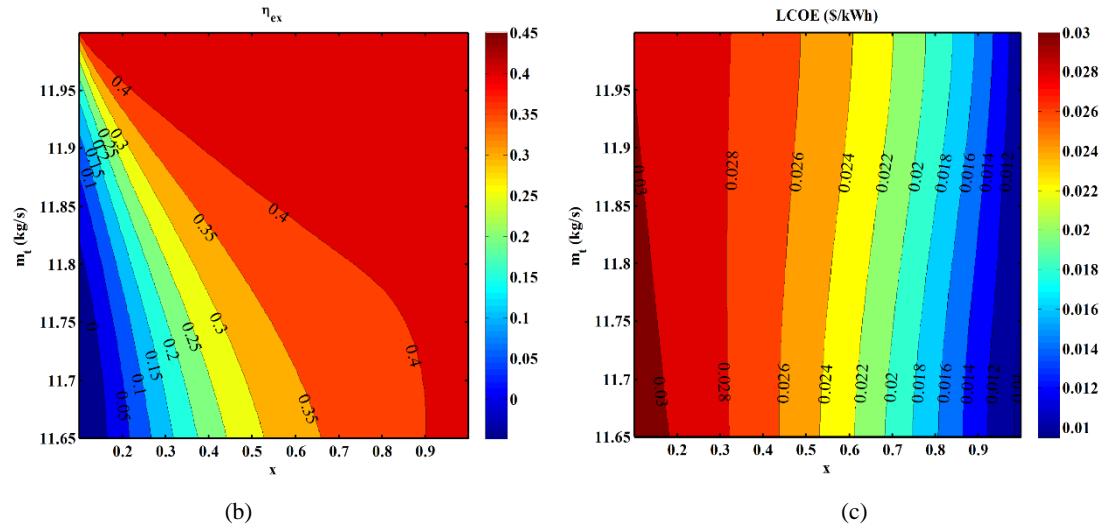


Fig.14. Objectives variations with mass flow rate and flow split ratio: (a). Net power output; (b). Exergetic efficiency; (c). Levelized cost of energy.

1                   **Multi-objective Optimization on Steady-state Thermodynamic**  
 2                   **Parameters of S-CO<sub>2</sub> Recompression Brayton Cycle Power**  
 3                   **Generation System for Marine Waste Heat Recovery**

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11                   **Abstract**

12                   Analysis of thermodynamic parameters' effects on the S-CO<sub>2</sub> recompression Brayton cycle for  
 13                   recovering the main engine exhaust gas waste heat of an ocean-going 9000 TEU container ship are  
 14                   carried out first in this paper. NSGA-II algorithm-based multi-objective optimizations are  
 15                   conducted to maximize net power output and exergetic efficiency as well as to minimize the  
 16                   levelized cost of energy (LCOE). The final optimal result from Pareto front solutions is decided by  
 17                   decision-making processes. The results show that the LCOE increases along with the enhancement  
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 19                   upper boundary of exhaust gas temperature. The final optimal result decided by TOPSIS  
 20                   decision-making has higher rationality and accuracy than that obtained by LINMAP method.  
 21                   Regarding the final optimal results of triple-objective and dual-objective optimizations obtained  
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 25                   cycle is better for recovering the exhaust gas waste heat in ships compared with the simple  
 26                   recuperative cycle without recompression.

27                   **Keywords:** S-CO<sub>2</sub> recompression Brayton cycle; main engine exhaust gas; waste heat recovery;  
 28                   multi-objective optimization; decision making

59                   \* Corresponding Author: Yuwei Sun, 1985-, PhD, Associate professor, Research interests: renewable energy  
 60                   application technology, electric power system and automation, system modeling and simulation.

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## Nomenclature

<i>E</i>	exergy, kJ/kg	hx <sub>r</sub>	gas heat exchanger
<i>h</i>	specific enthalpy, kJ/kg	isen	isentropic
<i>I</i>	exergy destruction, kW	in	input
<i>m</i>	mass flow rate, kg/s	mc	main compressor
<i>P</i>	pressure, MPa	net	net power output, kW
<i>Q</i>	heat transfer rate, kW	out	output
<i>s</i>	specific entropy, kJ/kgK	prc	pre-cooler
<i>T</i>	temperature, K	r	ratio
<i>W</i>	power, kW	rec	recompression compressor
<i>w</i>	specific work, kW	t	turbine
<i>LCOE</i>	Levelized cost of energy (\$/kWh)	th	thermal efficiency
<b>Greek symbols</b>		0	ambient condition
$\eta$	efficiency	1-10	state points
$\varepsilon$	recuperator effectiveness	2s, 7s, 10s	outlet isentropic enthalpy states
<b>Subscripts</b>		<b>Abbreviations</b>	
ex	exergetic efficiency	HTR	high-temperature recuperator
g	exhaust gas	LTR	low-temperature recuperator
		S-CO <sub>2</sub>	Supercritical CO <sub>2</sub>
		TEU	Twenty-foot Equivalent Unit

## 1. Introduction

Shipping is one of the most critical modes of transportation for world trade and accounts for approximately 90% of the global trade (Poulsen et al. 2016; Yuan et al. 2019). The global shipping industry is also one of the main contributors to global greenhouse gas (GHG) emissions, with it currently being responsible for about 3% of the global total (Lee et al. 2013). To restrict and lower the level of GHG emissions from the operation of newly-built ships, the International Maritime Organization (IMO) has formulated regulations such as the Energy Efficiency Design Index (EEDI) and the Ship Energy Efficiency Management Plan (SEEMP) (Beşikci et al. 2016; Perera et al. 2016). In today's global shipping industry, the diesel engine, which relies on fossil fuels, is still the most widely used power plant. However, its average energy efficiency is less than 50%, meaning that more than half of the input thermal energy cannot be exploited. Fig.1 shows the energy balance of a typical large low-speed two-stroke marine diesel engine and the main waste heat sources, temperature ranges and thermal energy loss rates (Singh et al. 2016; Yuan et al. 2018;

1 Shu et al. [2017](#)). It can be seen that heat energy loss from the exhaust gas is the bulk of the energy  
 2 dissipation, which accounts for about 25.5% of the total input fuel thermal energy. This is  
 3 followed by the air cooler (16.5%), jacket cooling water (5.2%), lubricating oil (2.9%) and heat  
 4 radiation (0.6%).

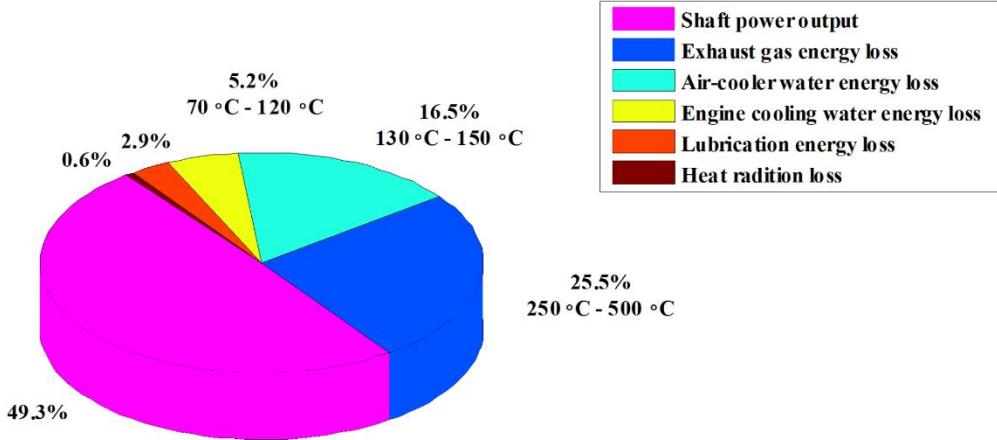


Fig.1. Energy balance of a large-scale low-speed two-stroke marine diesel engine.

From [Fig.1](#), the exhaust gas temperature ranges from 250 °C to 500 °C under normal working conditions. Therefore, the main engine exhaust gas waste heat energy is worth recovering when considering its quality and quantity of heat energy. The commonly used technology to recover the main engine exhaust gas waste heat in a ship is the combined turbocharger and exhaust gas boiler (EGB) system. In this combined waste heat recovery system, the exhaust gas temperature at the outlet of the turbocharger is still relatively high (220 °C~240 °C) in the first conversion stage, so there is potential for further exploitation of this energy source (Yuan et al. [2018](#)). So, the EGB is used as the second stage heat utilization equipment to recover the exhaust gas waste heat energy after the turbocharger. However, from the point view of the thermodynamic exergy analysis, the aforementioned technology cannot make full use of the exhaust gas waste heat. To further improve the utilization rate of the exhaust gas waste heat, alternative power cycle waste heat recovery technologies could offer promising options such as the Organic Rankine cycle (ORC), Rankine cycle (RC) and supercritical CO<sub>2</sub> (S-CO<sub>2</sub>) cycle.

Considering the limited available space and the special working conditions in a ship, the exhaust gas temperature range, operational safety and cost, the S-CO<sub>2</sub> cycle offers significant potential to recover the ship main engine exhaust gas waste heat owing to its advantages of a stable and non-toxic working fluid, compactness of size, relatively high efficiency and lower cost (Crespi et al. [2017](#)).

The first proposed S-CO<sub>2</sub> cycle was a partial condensation Brayton cycle patented by Sulzer in the late 1940s ([1950](#)). During the 1960s, Feher ([1968](#)) and Angelino ([1968](#)) contributed to some

breakthroughs in the research field of the S-CO<sub>2</sub> cycle. Since then, the S-CO<sub>2</sub> cycle continued to develop and has derived various layouts such as inter-cooling, inter-recuperation reheating, pre-compression, partial cooling and preheating (Dostal 2004). Dostal (2004) proposed the S-CO<sub>2</sub> RBC and Kulhánek et al. (2011) proved it has the highest efficiency and best performance over other S-CO<sub>2</sub> cycles. So far, as a result of the development in the research areas of the turbomachinery and the heat exchanger, S-CO<sub>2</sub> cycles have been successfully applied in the terrestrial power generation industry examples being concentrating solar power generation (Sánchez et al. 2017; Binotti et al. 2017; Polimeni et al. 2018; Belmonte et al. 2016; Al-Sulaiman et al. 2015), next-generation nuclear reactors (Dostal et al. 2004) and industrial waste heat recovery systems (Li et al. 2017; Yoon et al. 2017).

Apart from the research into the application of S-CO<sub>2</sub> cycles in terrestrial power generation industries, study on introducing S-CO<sub>2</sub> cycles into ships to recover the main engine waste heat has also been carried out. Moroz et al. (2015) studied the performance of a combined S-CO<sub>2</sub> and a conventional steam cycle to recover a shipboard gas turbine and found that the net power output increased by about 30%. Bella (2015) analyzed the performance of the S-CO<sub>2</sub> Brayton power cycle to recover the ship's gas turbine exhaust gas waste heat, which can lower the fuel consumption by about 22%. Sharma et al. (2017) conducted the parametric optimization of a S-CO<sub>2</sub> regenerative recompression Brayton power cycle to recover a ship's gas turbine exhaust gas waste heat and it was found that the overall energy system efficiency and net power output increased by 10% and 25%, respectively. Hou et al. (2017) stated that the S-CO<sub>2</sub> regenerative recompression cycle system could be used as the backup generator because it can meet 80% of the propulsion power demand of the ship when the gas turbine fails. Furthermore, Choi (2016) studied the thermodynamic performance of a transcritical CO<sub>2</sub> heat recovery system with a 2-stage reheat to recover the internal combustion engine cooling water waste heat in a 6800 TEU container ship. The aforementioned research has proved that the S-CO<sub>2</sub> cycle can be used as waste heat recovery systems in ships to contribute to the goal of energy-saving and emissions reduction in the shipping industry.

Since 2017, researchers from Wuhan University of Technology have devoted themselves to the study of the integrated application of the S-CO<sub>2</sub> cycle with a Kalina cycle for recovering the main engine exhaust gas waste heat of an ocean-going 9000 TEU container ship. The principal parameters of the ship are listed in Table 1. Usually, any available space in the ship's engine room will be limited and the working environment is very harsh. It is therefore a requirement that any proposed waste heat recovery system should offer significant advantages in terms of system structural simplicity, energy efficiency, operational safety, cost and maintenance (Deng et al. 2017).

1 Considering the aforementioned factors, the S-CO<sub>2</sub> recompression Brayton cycle (S-CO<sub>2</sub> RBC)  
 2 could be a reasonable option because it is compact with high efficiency and low cost. It can also  
 3 reduce the amount of compressor work required and avoid the pinch point issue (Deng et al. 2017).  
 4 Fig. 2 shows the structure diagram of the integrated S-CO<sub>2</sub> cycle and Kalina cycle waste heat  
 5 recovery system. As shown in Fig.2, the S-CO<sub>2</sub> RBC system is designed to recover the  
 6 high-temperature exhaust gas waste heat from the main engine exhaust gas before the turbocharger  
 7 and the Kalina cycle used to convert the low-temperature exhaust gas waste heat after the  
 8 turbocharger. The reason for the combination of these two cycles is to further reduce the exhaust  
 9 gas outlet temperature with the overall purpose of using the waste heat in depth. The design power  
 10 output of the S-CO<sub>2</sub> RBC waste heat recovery system is 300 kW. The expected goal of this  
 11 research project is that the ship fuel consumption and the attained EEDI be decreased by at least 2%  
 12 and 3%, respectively.

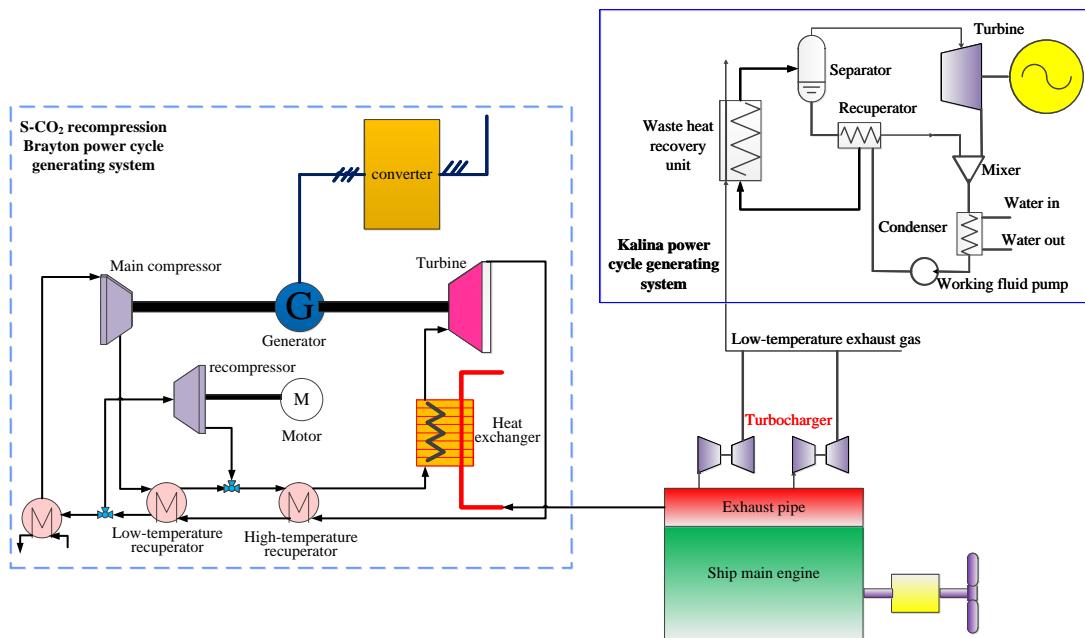


Fig.2. The general schematic diagram of the combined new power cycle generation system.

**Table 1**

Principal data of the ocean-going 9000 TEU container ship.

Items	Characteristics	Values
Principal dimension	Length (m)	300
	Moulded Breadth (m)	48.2
	Deadweight/DWT (t)	73125
	Voyage speed (kn)	21.5
Main engine	Engine type	8S90ME-C10.2
	Speed at MCR <sub>ME</sub> (r/min)	84.0
	MCR <sub>ME</sub> (kW)	41900
	SFC <sub>ME</sub> at 75% MCR (g/kWh)	159.61

1	$SFC_{AE}$ (g/kWh)	185
2	$P_{AE}$ (kW)	1435.75
3	Exhaust temperature before turbocharger (°C)	460
4	Exhaust temperature after turbocharger (°C)	270
5	Exhaust mass flow rate (kg/s)	52.1
6	Exhaust gas pressure (MPa)	0.308

9       1 For the S-CO<sub>2</sub> RBC, its thermodynamic parameters can be divided into design and off-design  
10      2 categories (Cheng et al. [2017](#)). Off-design parameters such as turbomachinery isentropic  
11      3 efficiency and pressure drop can be fixed. Design parameters such as system maximum pressure,  
12      4 mass flow rate and flow split ratio, need to be optimized to ensure that the system can operate  
13      5 safely and efficiently (Cheng et al. [2017](#)). Therefore, for S-CO<sub>2</sub> cycles, study of the effects of  
14      6 thermodynamic parameters on system performance to decide their optimal ranges is very essential  
15      7 to ensure the system can deliver improved performance. Energy, Exergy and Exergoeconomic (3E)  
16      8 analysis methods (Wu et al. [2017](#)) are commonly used to conduct the system thermodynamic  
17      9 analysis. Sharma et al. ([2017](#)) studied the effects of the turbine inlet temperature, main compressor  
18      10 inlet temperature, pressure ratio and pressure drop across the gas turbine on the performance of an  
19      11 S-CO<sub>2</sub> recompression Brayton power cycle waste heat recovery system. Banik et al. ([2016](#)) found  
20      12 that the recompression transcritical CO<sub>2</sub> power cycle can achieve better system performance at  
21      13 higher pressure ratio from 1.9 to 2.4. Furthermore, Sarkar ([2009](#)) revealed that the main  
22      14 compressor inlet temperature effects on optimum pressure ratio and cycle efficiency of the S-CO<sub>2</sub>  
23      15 recompression Brayton power cycle are more predominant than the maximum operating  
24      16 temperature. According to the previous research, it is clear that the thermodynamic parameters not  
25      17 only have comprehensive effects on the system performance but also interact with each other.  
26      18 Even though the same thermodynamic parameter will have inconsistent values for different  
27      19 configurations and specific applications.

20       To ensure that the proposed system can convert energy more efficiently and operate safely, it  
21      is critical to conduct a parametric optimization process of the system design. Artificial Neural  
22      Network (ANN), Genetic Algorithm (GA), Artificial Bee Colony (ABC) algorithm and Particle  
23      Swarm Optimization (PSO) are evolutionary algorithms used to speed up the search process for  
24      optimizing the S-CO<sub>2</sub> cycle system thermodynamic parameters and performance. Wang et al.  
25      ([2010](#)) optimized the simple S-CO<sub>2</sub> cycle turbine inlet pressure and temperature with exergy  
26      efficiency as the objective function by using ANN compared with GA. However, only optimizing  
27      single system performance indicators like exergy efficiency or thermal efficiency may not be  
28      sufficient to obtain reasonable results for system parametric optimization. Multi-objective  
29      optimization is an effective method to overcome the shortcomings of single-objective optimization.

1 Deng et al. (2017) conducted multi-objective optimization based on an NSGA-II algorithm to  
2 study the performance of a gas turbine S-CO<sub>2</sub> RBC waste heat recovery system. Tian et al. (2017)  
3 presented a systematic multi-objective optimization by GA to optimize the key parameters of  
4 carbon dioxide transcritical power cycles to ensure that the system can generate power efficiently  
5 and economically. Similar research has been carried out by using the GA (Cao et al. 2017) and  
6 ABC algorithm (Zhang et al. 2018).

7 The literature review reveals that the system thermodynamic parameters that have significant  
8 effects on the S-CO<sub>2</sub> cycle system performance need to be determined and optimized because their  
9 values are closely affected by the specific applications. Furthermore, it is a strategically  
10 convenient stage to cost effectively evaluate the system performance and economics through the  
11 system's optimal design before introducing the S-CO<sub>2</sub> RBC into the ship. This paper focuses on  
12 the steady-state thermodynamic analysis and performance of multi-objective optimization of the  
13 S-CO<sub>2</sub> RBC, when used to recover the main engine exhaust gas waste heat of an ocean-going  
14 9000 TEU container ship. First, thermodynamic analysis is conducted to determine the variation  
15 trends of the system's performance with change of thermodynamic parameters and decide their  
16 initial values, including main compressor inlet temperature and pressure, pressure ratio,  
17 turbomachinery isentropic efficiency and turbine inlet temperature. Then, performance  
18 multi-objective including dual-objective ( $W_{\text{net}}\text{-LCOE}$ ,  $\eta_{\text{ex}}\text{-LCOE}$ ,  $W_{\text{net}}\text{-}\eta_{\text{ex}}$ ) and triple-objective  
19 ( $W_{\text{net}}\text{-LCOE-}\eta_{\text{ex}}$ ) optimizations are carried out by using the elitist non-dominated sorting genetic  
20 (NSGA-II) algorithm, using flow split ratio, turbine mass flow rate and exhaust gas waste heat  
21 temperature as decision variables. Finally, LINMAP and TOPSIS decision-making methods are  
22 employed to decide the final optimal result from the Pareto front solutions obtained by the  
23 NSGA-II algorithm.

## 41 24 **2. System description and mathematical models**

### 42 25 **2.1. System description**

46 The main components of the S-CO<sub>2</sub> RBC system are the main compressor, re-compressor,  
47 turbine, LTR, HTR and pre-cooler. The pre-cooler is deployed to ensure that the thermodynamic  
48 conditions of the working fluid CO<sub>2</sub> are close to its critical point before entering the main  
49 compressor. Fig.3 and Fig.4 show the system configuration diagram and its *T-s* diagram. In the  
50 proposed system, a splitter divides the working fluid CO<sub>2</sub> into two parts before entering the  
51 pre-cooler. A part of the working fluid flows into the bypass loop to be pressurized in the  
52 recompression compressor, and then joins the cold stream cycle from the entry point between the  
53 LTR and HTR. By lowering the mass flow rate through the cold side of the LTR, the bypass loop  
54 can balance the capacitance rates of the cold stream and hot stream, which results in higher  
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1 efficiency compared with a simple recuperated cycle without recompression (Dyreby. [2014](#)). In  
 2 spite of the higher compression work, the thermal efficiency is improved compared to the single  
 3 recuperated cycle due to the heat input at a higher temperature level and the reduction of the heat  
 4 of CO<sub>2</sub> rejected to the ambient (Manente et al. [2019](#)). The details of the proposed system  
 5 thermodynamic processes are as follows:

6 Process 1-2 and 9-10: isentropic compression in the main compressor and recompression  
 7 compressor.

8 Process 2-3 and 8-9: isobaric heat exchange between the cold working fluid and hot working  
 9 fluid in the LTR.

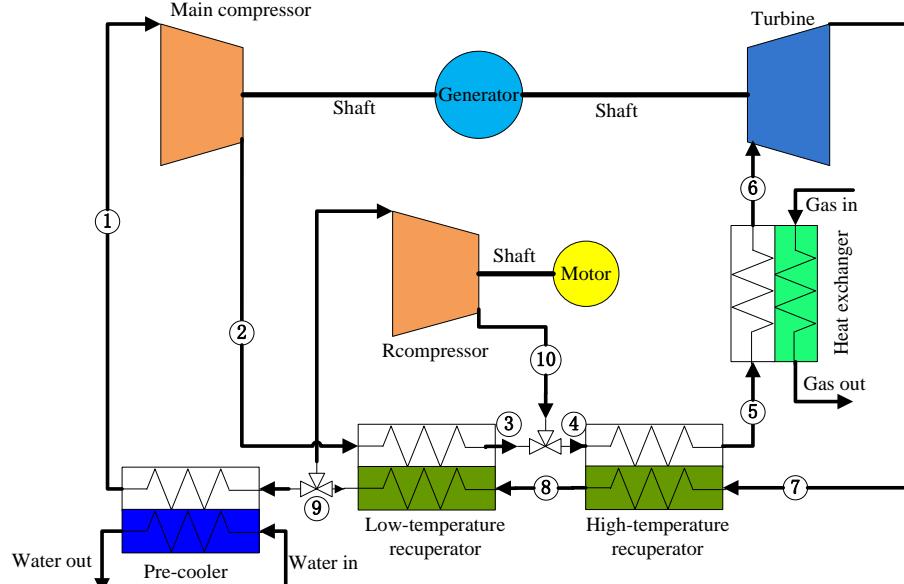
10 Process 4-5 and 8-7: isobaric heat exchange between the cold working fluid and hot working  
 11 fluid in the HTR.

12 Process 3-4 and 10: mixed flow.

13 Process 5-6: isobaric heat absorption process in the heat exchanger between the cold working  
 14 fluid and the ship main engine exhaust gas.

15 Process 6-7: isentropic expansion in the turbine.

16 Process 9-1: heat rejection process in the pre-cooler.



17 Fig.3. The system configuration of the S-CO<sub>2</sub> recompression Brayton power cycle.  
 18

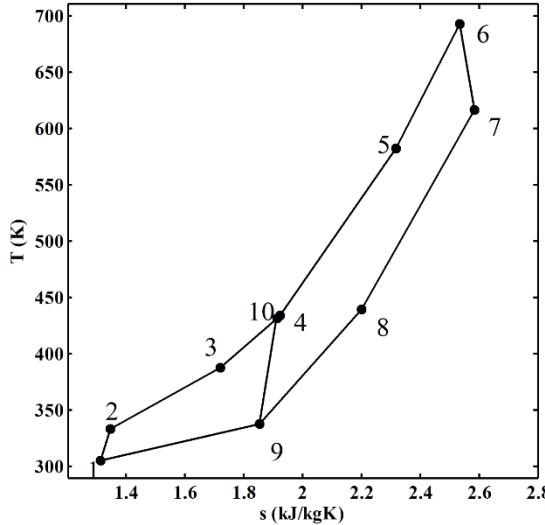


Fig. 4.  $T$ - $s$  diagram of the S-CO<sub>2</sub> recompression Brayton power cycle.

## 2.2. Mathematical model

Certain assumptions are made to simplify the system thermodynamics for analysis, modeling and calculation in this work (Sarkar et al. 2009; Akbari et al. 2014).

(1) The closed-loop system operates under the steady-state condition without any leakage of the working fluid CO<sub>2</sub>.

(2) Pressure drops and heat losses in the pipes are neglected.

(3) Only physical exergy of the working fluid CO<sub>2</sub> is considered, while the chemical exergy, kinetic exergy and potential exergy changes in all components are neglected.

### 2.2.1. Energetic analysis

The thermodynamic models of the S-CO<sub>2</sub> RBC main components are presented in [Table 2](#) (Zhao et al. 2016).

The net power output  $W_{\text{net}}$  of the proposed system is defined as:

$$W_{\text{net}} = W_{\text{t}} - W_{\text{mc}} - W_{\text{rec}} \quad (1)$$

The thermal efficiency  $\eta_{\text{th}}$  is defined as the ratio of net power output  $W_{\text{net}}$  to the heat absorbed from the heat exchanger  $Q_{\text{in}}$ :

$$\eta_{\text{th}} = \frac{W_{\text{net}}}{Q_{\text{in}}} \quad (2)$$

The main compressor specific work  $w_{\text{mc}}$ , re-compressor specific work  $w_{\text{rec}}$  and turbine specific work  $w_{\text{t}}$  are defined as follows:

$$w_{\text{mc}} = h_2 - h_1 \quad (3)$$

$$w_{\text{rec}} = h_{10} - h_9 \quad (4)$$

$$w_t = h_6 - h_7 \quad (5)$$

The LTR effectiveness depends on the heat capacity. If the heat capacity of the high-pressure fluid is greater than that of low-pressure fluid, then Eq. (6-1) is applicable. Eq. (6-2) is applicable for the reverse case (Sarkar 2009; Sarkar et al. 2009):

$$\varepsilon_{\text{LTR}} = (T_8 - T_9) / (T_8 - T_2) \quad (6-1)$$

$$\varepsilon_{\text{LTB}} = (T_3 - T_2) / (T_8 - T_2) \quad (6-2)$$

### 2.2.2. Exergetic analysis

The ambient environment pressure  $P_0$  and temperature  $T_0$  are set as the reference state values. In this study, the working fluid chemical exergy is ignored and only its physical exergy is considered. The exergy of the  $i_{th}$  steady-state point  $E_i$  can be defined as:

$$E_i = m[(h_i - h_0) - T_0(s_i - s_0)] \quad (7)$$

The component exergy loss  $I$  can be calculated by:

$$\sum E_{\text{in}} - \sum E_{\text{out}} = I \quad (8)$$

The system total exergy loss  $\sum I$  is defined as:

$$\sum I = I_{\text{hxr}} + I_{\text{prc}} + I_{\text{HTR}} + I_{\text{LTR}} + I_{\text{t}} + I_{\text{mc}} + I_{\text{rec}} \quad (9)$$

The exergetic efficiency  $\eta_{\text{ex}}$  of the whole system can be calculated as:

$$\eta_{\text{ex}} = \frac{E_{\text{in}} - \sum I}{E_{\text{in}}} \quad (10)$$

The exergetic efficiency of the S-CO<sub>2</sub> RBC can also be defined as (Zhang et al. 2018):

$$\eta_{\text{ex}} = \frac{\eta_{\text{th}}}{(1 - T_0/T_{\text{e}})} \quad (11)$$

Table 2

The equations for different components of S-CO<sub>2</sub> recompression Brayton cycle.

Components	Energetic equations	Exergetic equations
Main compressor	$\eta_{\text{isen,mc}} = (h_{2s} - h_1) / (h_2 - h_1)$	$I_{\text{mc}} = W_{\text{mc}} - (E_2 - E_1)$
	$W_{\text{mc}} = m(h_2 - h_1)$	$\eta_{\text{ex,mc}} = (E_2 - E_1) / W_{\text{mc}}$
Recompression compressor	$\eta_{\text{isen,rec}} = (h_{10s} - h_9) / (h_{10} - h_9)$	$I_{\text{rec}} = W_{\text{rec}} - (E_{10} - E_9)$
	$W_{\text{rec}} = m(h_{10} - h_9)$	$\eta_{\text{ex,rec}} = (E_{10} - E_9) / W_{\text{rec}}$
HTR	$\varepsilon_{\text{HTR}} = (T_7 - T_8) / (T_7 - T_4)$	$I_{\text{HTR}} = E_7 - E_8 - (E_5 - E_4)$
	$Q_{\text{HTR}} = m(h_5 - h_4) = m(h_8 - h_7)$	$\eta_{\text{ex,HTR}} = (E_5 - E_4) / (E_7 - E_8)$
LTR	$Q_{\text{LTR}} = m(h_3 - h_2) = m(h_9 - h_8)$	$I_{\text{LTR}} = E_8 - E_9 - (E_3 - E_2)$
		$\eta_{\text{ex,LTR}} = (E_3 - E_2) / (E_8 - E_9)$
Turbine	$\eta_{\text{isen,t}} = (h_6 - h_7) / (h_6 - h_{7s})$	$I_t = E_6 - E_7 - W_t$

	$W_t = m(h_6 - h_7)$	$\eta_{ex,t} = W_t / (E_6 - E_7)$
1	Gas heat exchanger	$Q_{in} = m(h_6 - h_5)$
2		$I_{hxr} = E_{gas,in} + E_5 - E_{gas,out} - E_6$
3		$\eta_{ex,hxr} = (E_6 - E_5) / (E_{gas,in} - E_{gas,out})$
4	Pre-cooler	$Q_{prc} = m(h_9 - h_1)$
5		$I_{prc} = E_{prc,in} + E_{water,in} - E_{prc,out} - E_{water,out}$
6		$\eta_{ex,prc} = (E_{prc,out} - E_{prc,in}) / (E_{water,in} - E_{water,out})$

### 2.2.3. Economic analysis

The levelized cost of energy (LCOE, \$/kWh) defined as the average cost per unit of energy produced by the proposed system, is used to evaluate the economics of the S-CO<sub>2</sub> RBC waste heat recovery system in this work.

$$LCOE = \sum_{i=1}^N c_i / W_{net} \quad (12)$$

The cost rate for the  $i_{th}$  component  $c_i$  is calculated by considering the purchase cost, operating and maintenance cost which can be defined as follows:

$$c_i = \left( \frac{CRF + \gamma_k}{t} \right) \cdot C_i \quad (13)$$

Where  $\gamma_k$  is the maintenance factor (0.06);  $t$  is the annual operation hours (7200 h);  $C_i$  is the initial investment component (\$);  $CRF$  is the capital recovery factor which can be calculated by:

$$CRF = \frac{k(1+k)^n}{(1+k)^n - 1} \quad (14)$$

Where  $k$  is the interest rate (12%);  $n$  is the system operation life cycle (20 years).

To estimate the area of the heat exchangers, constant values of the overall heat transfer coefficient are introduced for the purpose of simplicity. The constant value of the LTR and exhaust gas heat exchanger is 1.6 kW/m<sup>2</sup>K. The values of HTR and pre-cooler are selected as 3.0 kW/m<sup>2</sup>K and 2.0 kW/m<sup>2</sup>K, respectively (Zhang et al. 2018). The economic data and cost functions are listed in [Table 3](#).

**Table 3**

Economic data and cost function  $C_i$  for the proposed system (Zhang et al. 2018; Liu et al. 2018).

System component	Unit	Cost functions
Main compressor	USD	$71.1 \cdot m_{mc} \cdot (1/0.92 - \eta_{mc}) \cdot p_r \cdot \ln(p_r)$
Re-compressor	USD	$71.1 \cdot m_{rc} \cdot (1/0.92 - \eta_{rc}) \cdot p_r \cdot \ln(p_r)$
Turbine	USD	$479.34 \cdot m_t \cdot (1/0.93 - \eta_t) \cdot \ln(p_r) \cdot (1 + \exp(0.036 \cdot T_{t,in} - 54.4))$
Precooler	USD	$2143 \cdot A^{0.514}_{PRC}$
HTR	USD	$2681 \cdot A^{0.514}_{HTR}$
LTR	USD	$2681 \cdot A^{0.514}_{LTR}$
Exhaust gas heat exchanger	USD	$2681 \cdot A^{0.514}_{hxr}$

Maintenance and operation factor	%	6.0
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### 2.3. Model validation

2 The relative deviation  $RD$  is defined as:

$$RD = \frac{|ref - rel|}{ref} \times 100\% \quad (15)$$

4 Where  $ref$  represents the reference value and  $rel$  is the real value calculated by the simulation  
5 model in this paper.

6 The verification of the model of the proposed system was conducted by comparing the  
7 turbine mass flow rate and thermal efficiency in the present paper to those in Ref. (Dyreby [2014](#))  
8 under the consistent initial conditions. [Table 4](#) compares the results between the Ref. (Dyreby  
9 [2014](#)) and the simulation model present in this study. The deviations are less than 1.0% which  
10 indicates that the proposed system thermodynamic simulation model is validated for use in this  
11 study.

25 **Table 4**

26 Calculation results in the present paper compared with Ref. (Dyreby [2014](#)).  
27

$T_{mc,in}$ (°C)	$m_t$ (kg/s) Ref.	$m_t$ (kg/s) Present	$RD$ (%)	$\eta_{th}$ ( % )	$\eta_{th}$ ( % )	$RD$ (%)
				Ref.	Present	
32	98.50	97.69	0.83	47.40	47.00	0.84
50	134.20	134.16	0.03	41.80	41.52	0.67

### 3. Methodology

12 [Fig.5](#) is the solution process flow chart of the thermodynamic analysis and parametric  
13 optimization.

- 14 (1) Input the initial parameters including main compressor inlet temperature  $T_1$ , pressure  $P_1$   
15 and outlet pressure  $P_2$  as well as turbine inlet temperature  $T_6$ .
- 16 (2) Calculate the working conditions from state point 1 to state point 10, including  
17 temperatures ( $T_2 \sim T_{10}$ ), pressures ( $P_3 \sim P_{10}$ ), entropies ( $E_1 \sim E_{10}$ ) and enthalpies ( $h_1 \sim$   
18  $h_{10}$ ).
- 19 (3) Compute the main compressor specific work  $w_{mc}$ , re-compressor specific work  $w_{rec}$  and  
20 turbine specific work  $w_t$ .
- 21 (4) After completing the aforementioned steps, the whole system simulation model can be  
22 established based on the system mathematical models, and the initial values (including  
23 main compressor inlet temperature  $T_{mc,in}$ , main compressor inlet pressure  $P_{mc,in}$ , pressure  
24 ratio  $P_r$ , main compressor isentropic efficiency  $isen_t$ , turbine isentropic efficiency  $isen_{mc}$

1 and turbine inlet temperature  $T_{t,in}$ ) of thermodynamic parameters that decide the system  
 2 performance characteristics can be investigated through thermodynamic analysis.  
 3 (5) The NSGA-II algorithm is used to optimize the system net power output  $W_{net}$ , exergetic  
 4 efficiency  $\eta_{ex}$  and leveledized cost of energy  $LCOE$ , using the flow split ratio  $x$ , turbine  
 5 mass flow rate  $m_t$  and exhaust gas waste heat temperature  $T_g$  as decision variables.  
 6 (6) The LINMAP and TOPSIS decision making methods are employed to select the final  
 7 optimal result from the Pareto front solutions obtained by NSGA-II.

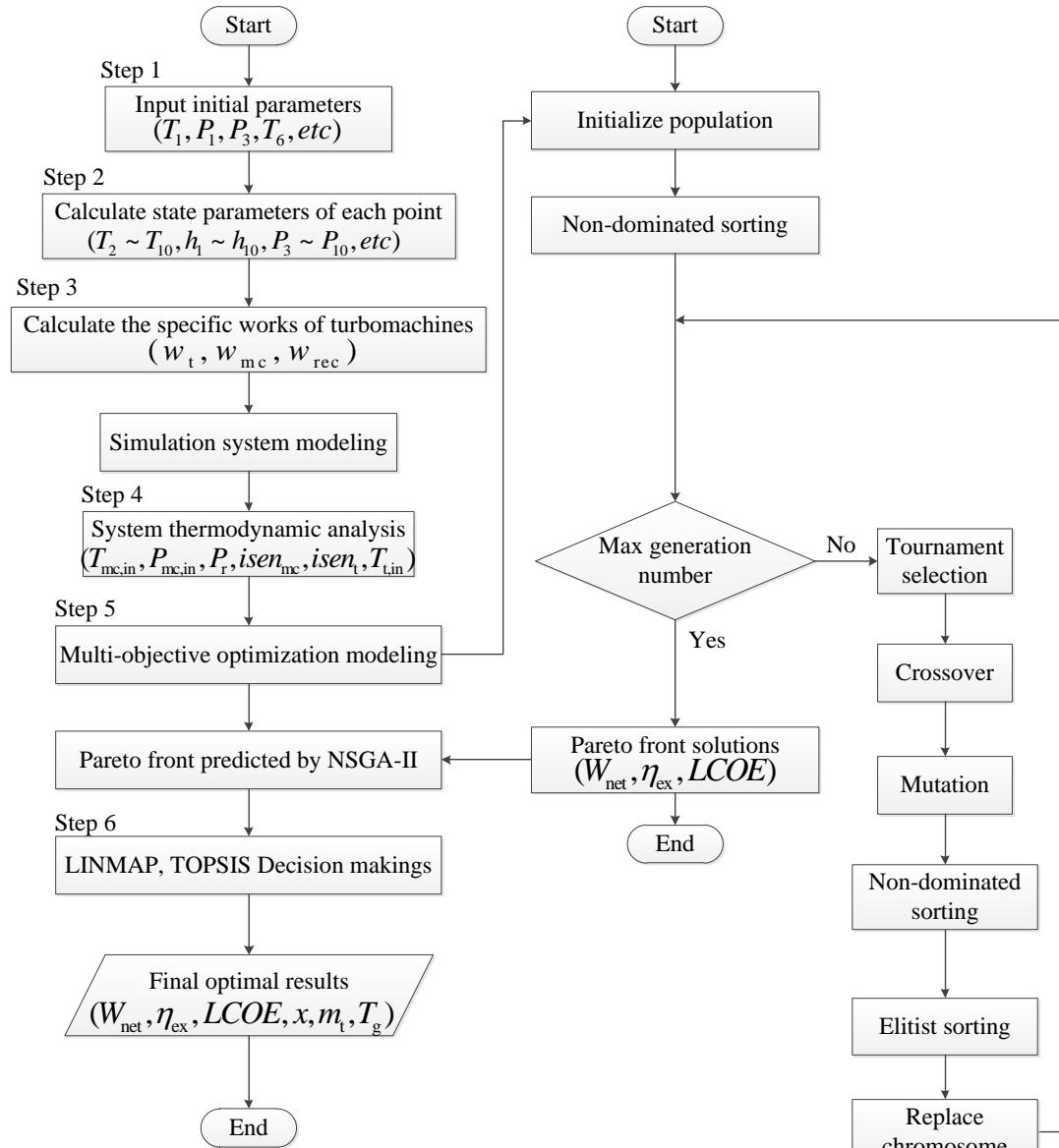


Fig.5. Flow chart of the thermodynamic analysis and parametric optimization.

### 3.1. NSGA-II algorithm

The NSGA-II algorithm was first proposed by Deb et al. (2002) and Shi et al. (2010) concluded that it is one of the best methods to solve multi-objective optimization issues. The algorithm calculation flow chart is shown in Fig. 5.

1    **3.2. Decision-making process**

2        Pareto front solutions are considered equally good in the multi-objective optimization  
3        processes. So, a final optimal solution needs to be decided from the Pareto front solutions, which  
4        is the trade-off solution between the conflict objective functions. In this study, the most recognized  
5        and common type of decision-making methods include LINMAP and TOPSIS, and are used to  
6        decide the final optimal result from the Pareto front solutions obtained by the NSGA-II algorithm.

7    **3.2.1. LINMAP decision-making**

8        The basic principle of the LINMAP decision-making is to calculate the Euclidean distance  
9        from each Pareto front solution to the ideal point, and the solution with the minimum distance is  
10       selected as the final optimal result (Moghimi et al. [2018](#)). The ideal point is optimum with respect  
11       to all of the objective functions. The Euclidean distance is calculated as follows (Li et al. [2015](#)):

$$21 \quad 12 \quad D_{i+} = \sqrt{\sum_{j=1}^n (f_{ij} - f_j^{\text{ideal}})^2} \quad (16)$$

25        13        Where  $f_j^{\text{ideal}}$  is the ideal solution point of the  $j^{\text{th}}$  objective in a single-objective optimization  
26        14        calculation.

29    **3.2.2 TOPSIS decision making**

31        16        TOPSIS is a decision-making method which was first developed by Hwang and Yoon ([1981](#)).  
32        17        In TOPSIS decision-making process, the ideal point and nadir point are considered simultaneously.  
33        18        Therefore, the Euclidean distances of each Pareto front solution to the ideal point and the nadir  
34        19        point should be calculated. The Euclidian distance of each solution to the nadir point can be  
35        20        defined as (Li et al. [2015](#); Sianaki [2015](#)):

$$40 \quad 21 \quad D_{i-} = \sqrt{\sum_{j=1}^n (f_{ij} - f_j^{\text{nadir}})^2} \quad (17)$$

45        22        The maximum  $d_i$  will help to decide the final optimal solution, which is defined as follows:

$$47 \quad 23 \quad d_i = \frac{D_{i+}}{D_{i+} + D_{i-}} \quad (18)$$

50        24        To evaluate the final optimal solutions obtained by these two decision-making methods, the  
51        25        deviation index  $Rd$  is introduced (Li et al. [2015](#)):

$$54 \quad 26 \quad Rd = \frac{\sqrt{\sum_{j=1}^n (f_j - f_j^{\text{ideal}})^2}}{\sqrt{\sum_{j=1}^n (f_j - f_j^{\text{ideal}})^2} + \sqrt{\sum_{j=1}^n (f_j - f_j^{\text{nadir}})^2}} \quad (19)$$

## 4. Results and discussions

### 4.1 Thermodynamic analysis

Both thermodynamic analysis and performance multi-objective optimization of the proposed system are conducted by simulation models established in MATLAB. The thermodynamic properties of the CO<sub>2</sub> are calculated based on the REFPROP (NIST standard reference database 23 2019) database developed by the National Institute of Standards and Technology of the United States.

In this work, the pressure drops of the main components and the temperature differences in the LTR and HTR can be decided based on the previous research. The pressure drops of the cold stream and hot stream in the HTR and LTR are set to 0.15 MPa and 0.08 MPa, the pressure drop values in the gas heat exchanger and pre-cooler are set to 0.08 MPa (Dyreby 2014). The effectiveness of the HTR and LTR are assumed to 95% and 89% (Park et al. 2018). Considering system operational safety and manufacturing technologies, the maximum pressure in the proposed system is set at 20 MPa. The initial values of the thermodynamic parameters to conduct thermodynamic analysis and performance multi-objective optimization are listed in [Table 5](#).

**Table 5**

Thermodynamic parameters and their initial values for system thermodynamic analysis and performance multi-objective optimization.

Parameters	Values
Ambient temperature (°C)	21
Ambient pressure (MPa)	0.1
Maximum pressure (MPa)	20
HTR effectiveness (%)	93
LTR effectiveness (%)	89
Flow split ratio	0.4

#### 4.1.1. Effects of the main compressor inlet temperature

The main compressor inlet temperature is defined as the minimum temperature in the S-CO<sub>2</sub> RBC system in this work. The main compressor initial inlet pressure is fixed at 7.38 MPa to analyze the effects of inlet temperature on the system performance due to the working fluid CO<sub>2</sub> requiring lower compression work near the critical zone (31.1 °C, 7.38 MPa), which can contribute to the system achieve better system performance (Guo et al. 2018). The compressor work ratio is defined as the ratio of compression work (shaft power) to the turbine work (shaft work). [Fig.6](#) shows the effects of the main compressor inlet temperature on the net power output, exergetic efficiency, compressor work ratio and the CO<sub>2</sub> density at the inlet of the main compressor. [Fig.6](#)

1 shows that the net power output continues to increase to a maximum of 338.50 kW as the inlet  
 2 temperature approaches 34 °C, and then decreases. Increasing the main compressor inlet  
 3 temperature results in the reduction of the CO<sub>2</sub> density at the inlet of the main compressor as  
 4 shown in [Fig. 6](#). Therefore, the main compressor needs to consume more turbine output work to  
 5 compress the working fluid to maintain the mass flow rate required for the turbine. Before the  
 6 inlet temperature reaches 34 °C, the system net power output increases because the turbine output  
 7 shaft power increases at a higher rate than the increase in the shaft work required to drive the  
 8 compressor. However, when the inlet temperature exceeds 34 °C, incremental increase of the main  
 9 compressor compression work leads to the decreasing of the net power output. To ensure the  
 10 proposed system has a better performance, the main compressor inlet temperature is fixed at 34 °C  
 11 to conduct the following analysis.

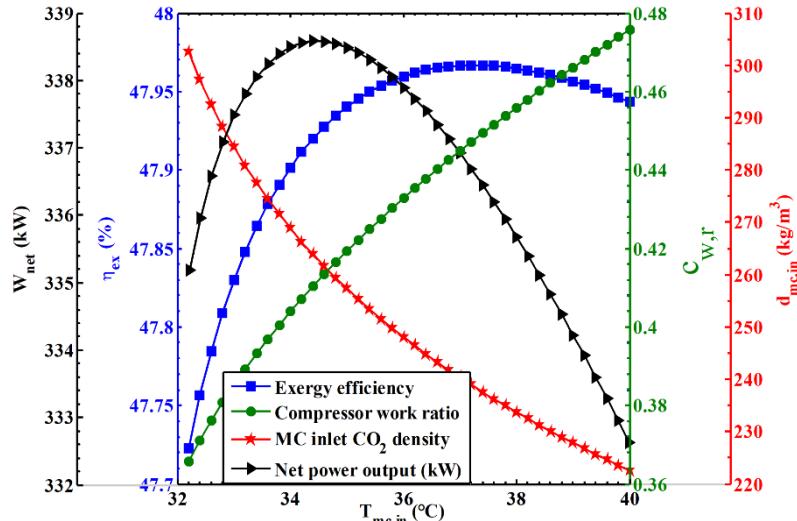


Fig. 6. Variations in different parameters with main compressor inlet temperature.

#### 4.1.2. Effects of the main compressor inlet pressure

The main compressor inlet pressure is defined as the minimum pressure in the proposed system in this paper. As shown in [Fig. 7](#) the main compressor inlet pressure has significant effect on the thermal properties of the working fluid CO<sub>2</sub>, especially its density. From [Fig. 7](#), before the inlet pressure approaches 8.0 MPa, the net power output increases sharply due to the decrease in compression work caused by the dramatic increase of CO<sub>2</sub> density. Then, the effect of the main compressor inlet pressure on the system net power output becomes less significant because density of the CO<sub>2</sub> gradually stabilizes. The values of net power output are 302.30 kW at  $P_{mc,in} = 8.0$  MPa and 335.70 kW at  $P_{mc,in} = 11$  MPa. Only a 9.95% average increase of the system net power output when the main compressor inlet pressure is raised by 27.27% (From 8 MPa to 11 MPa). Although the results show that a higher main compressor inlet pressure contributes to more power, higher inlet pressure in turbomachinery components requires thicker piping and casing that will cause an

1 increase in cost (Guo et al. 2018). Therefore, considering the aforementioned reasons, the main  
 2 compressor inlet pressure is fixed at 8.0 MPa.  
 3

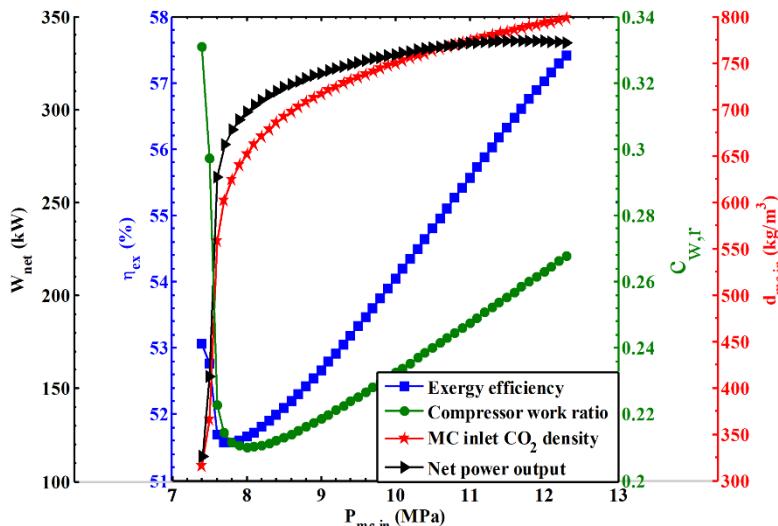


Fig. 7. Variations in different parameters with main compressor inlet pressure.

#### 4.1.3. Effects of the pressure ratio

The pressure ratio in this study is defined as the ratio of the main compressor outlet pressure to its inlet pressure. As shown in Fig. 8, the net power output and exergetic efficiency continue to increase to a maximum, and then decrease. Each of the system performance metrics have their own optimal pressure ratio. The maximum net power output is 311.90 kW when  $pr_{mc} = 2.7$ , and the corresponding exergetic efficiency is about 52.82%. If the pressure ratio is set to 2.7, then the maximum main compressor outlet pressure is 21.60 MPa, which is higher than the constraint condition of 20 MPa as mentioned above. Compared with the net power output of 309.30 kW at a  $pr_{mc}$  of 2.7, the net power output at a  $pr_{mc}$  of 2.5 only decreases by approximately 0.83%. Therefore, it is acceptable for the pressure ratio to be fixed at 2.5 in this work, which can guarantee the maximum pressure does not exceed the upper safety limit while still allowing the system to deliver improved performance.

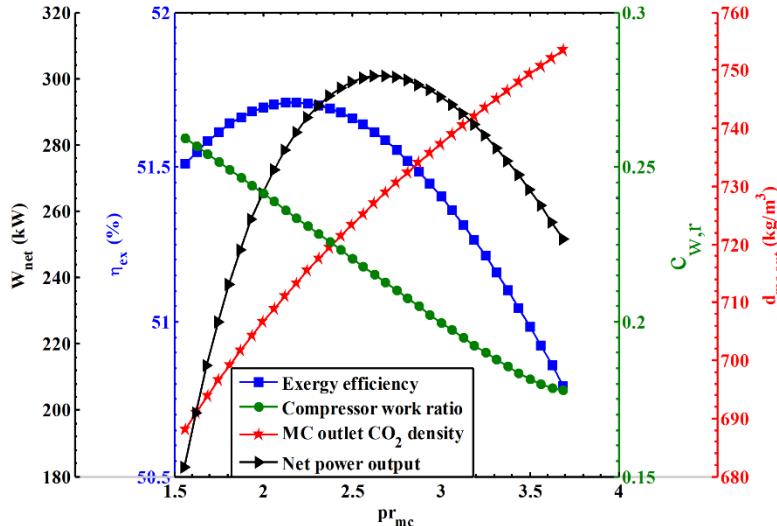


Fig. 8. Variations in different parameters with pressure ratio.

#### 4.1.4 Effects of the main compressor isentropic efficiency

The main compressor efficiency is decided by its isentropic efficiency. Fig. 9 shows the effects of the main compressor's isentropic efficiency on system performance. As can be seen, the main compressor isentropic efficiency has a positive influence on the net power output, thermal efficiency and exergetic efficiency. If the main compressor isentropic efficiency increases by 10%, the system net power output, thermal efficiency and exergetic efficiency are raised approximately 8.51%, 8.24% and 0.46%. It is clear that the effects of the main compressor isentropic efficiency on the system performance is limited. Although higher main compressor isentropic efficiency contributes to improve the system performance, the main compressor isentropic efficiency is set to 65% when the present mechanical process technic level of the turbomachinery is taken into consideration.

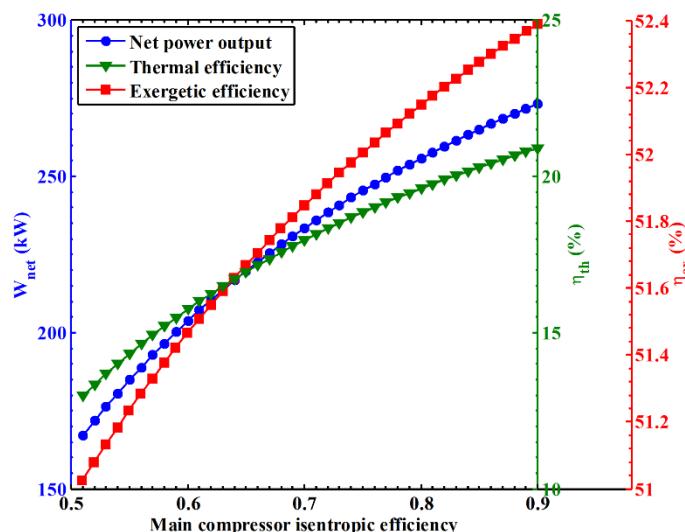


Fig. 9. Variations in system net power output, thermal efficiency and exergetic efficiency with main compressor isentropic efficiency.

#### 4.1.5 Effects of the turbine isentropic efficiency

The turbine's isentropic efficiency determines its mechanical efficiency, which has a direct effect on the system net power output because the turbine output shaft power is used to drive the generator. [Fig.10](#) shows the effects of the turbine isentropic efficiency on the system performance. The system net power output, thermal efficiency and exergetic efficiency all increase linearly with increase of the turbine isentropic efficiency. It is clear that the turbine's isentropic efficiency has greater effect on the system performance compared with that of the main compressor. Higher turbine isentropic efficiency leads to increased power and improves the system energy efficiency. The turbine isentropic efficiency is taken to be 75% in this study owing to current manufacturing limitations.

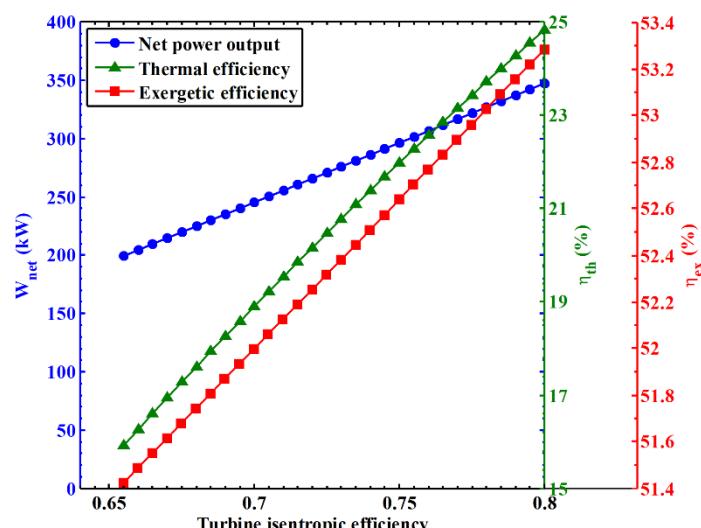


Fig. 10. Variations in system net power output, thermal efficiency and exergetic efficiency with turbine isentropic efficiency.

#### 4.1.6. Effects of the turbine inlet temperature

The maximum temperature of the whole system is the outlet temperature of the gas heat exchanger which is also equal to the turbine inlet temperature. In [Fig.11](#), the system net power output, thermal efficiency and exergetic efficiency all increase almost proportionally to the increase of the turbine inlet temperature. The increase in the turbine inlet temperature by 50 °C results in an increase in the net power output, thermal efficiency and exergetic efficiency by approximately 18%, 14% and 2.0%, respectively. It is clear that increasing the turbine inlet temperature is the most straightforward way to improve the system performance, and this confirms that the S-CO<sub>2</sub> recompression Brayton power cycle is suitable for exploiting the high-temperature heat source. In this study, the turbine inlet design temperature is about 420 °C based on the ship main engine exhaust gas maximum temperature (460 °C).

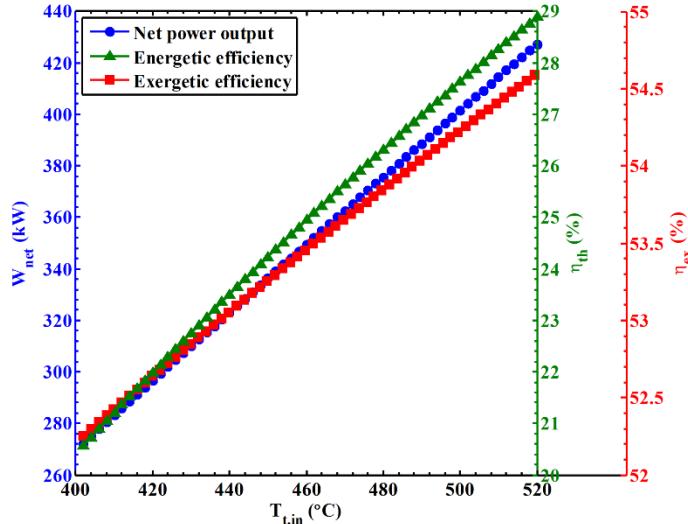


Fig. 11. Variations in system net power output, thermal efficiency and exergetic efficiency with turbine inlet temperature.

According to the results of thermodynamic analysis, values of the thermodynamic parameters to conduct the following performance multi-objective optimizations are listed in [Table 6](#).

**Table 6**

Thermodynamic parameters for performance multi-objective optimization.

Parameters	Values
Main compressor inlet temperature (°C)	34
Main compressor inlet pressure (MPa)	8.0
Pressure ratio	2.5
Turbine inlet temperature (°C)	420
Turbine isentropic efficiency (%)	75
Re-compressor isentropic efficiency (%)	65
Main compressor isentropic efficiency (%)	65

## 4.2. Multi-objective optimization

For a thermodynamic system like the S-CO<sub>2</sub> cycle, system performance optimization can involve two or more conflicting objectives. The multi-objective optimization provides an effective method by which such issues may be resolved, but the issue that must be addressed is that it is difficult to get a feasible solution when the maximization and minimization objective is conflicted during the calculation process of the multi-objective optimization, especially since both objectives are indispensable considerations (Li et al. [2015](#)). In this work, NSGA-II is used to get the Pareto front solutions of the objective functions, then LINMAP and TOPSIS decision-making methods are employed to determine the final optimal result from the Pareto front solutions.

### 4.2.1. Problem formulation

The purpose of system performance multi-objective optimization is to maximize net power

1 output  $W_{\text{net}}$  and exergetic efficiency  $\eta_{\text{ex}}$  as well as to minimize the levelized cost of energy  $LCOE$   
 2 by investigating the decision variables of flow split ratio  $x$ , mass flow rate  $m_t$  and exhaust gas  
 3 waste heat temperature  $T_g$ . The multi-objective optimization model is established according to the  
 4 proposed system energetic, exergetic and economics models described in Section 2, which can be  
 5 expressed as follows:

$$\begin{cases} \max f_1(m_t, x, T_g) = W_{\text{net}} \\ \max f_2(m_t, x, T_g) = \eta_{\text{ex}} \\ \min f_3(m_t, x, T_g) = LCOE \end{cases} \quad (20)$$

7 According to the working principle of the S-CO<sub>2</sub> RBC, the flow split ratio  $x$  is defined as the  
 8 proportion of the working fluid's mass flow rate into the recompression compressor divided by the  
 9 total working fluid's mass flow rate, and ranges from 0 to 1.0 for this study. The design net power  
 10 output of the proposed system is 300 kW, based on an estimation that the mass flow rate  $m_t$  ranges  
 11 from 10.0 kg/s to 12.0 kg/s. Based on the ship main engine working conditions, the temperature  
 12 range of the exhaust gas waste heat  $T_g$  is 400 °C to 460 °C

#### 4.2.2. Optimization results and discussions

14 [Fig.12](#) shows the Pareto front solutions and the final optimal results decided by LINMAP and  
 15 TOPSIS decision-making methods of the triple-objective ( $W_{\text{net}} - LCOE - \eta_{\text{ex}}$ ) optimization. As can  
 16 be seen the  $LCOE$  increases with the increase of net power output and exergetic efficiency. The  
 17 optimal solutions for the net power output, exergetic efficiency and levelized cost of energy are  
 18 within the ranges of 107.50 kW to 313.30 kW, 13.40% to 40.19% and 0.01 \$/kWh to 0.03 \$/kWh,  
 19 respectively. [Table 7](#) lists the final optimal results of the triple-objective optimization determined  
 20 by LINMAP and TOPSIS decision makings in detail. It is observed that the final optimal solutions  
 21 always occur at the upper limit of the heat source temperature, which indicates that higher exhaust  
 22 gas temperatures have a positive effect on the system performance. The final optimal result  
 23 deviation index for the triple-objective optimization obtained by TOPSIS (0.2517) is less than that  
 24 of LINMAP (0.1997). Therefore, the final optimal result decided by the TOPSIS decision making  
 25 is deemed as being more realistic in the triple-objective optimization. To reveal the relationship  
 26 between the three objectives, the mathematical expression obtained by fitting the Pareto front  
 27 solution is given by:

$$LCOE = -68.14 \cdot W_{\text{net}}^2 - 0.29 \cdot W_{\text{net}} - 40.77 \cdot \eta_{\text{ex}}^2 + 0.11 \cdot \eta_{\text{ex}} + 105.80 \cdot W_{\text{net}} \cdot \eta_{\text{ex}} + 0.02 \quad (21)$$

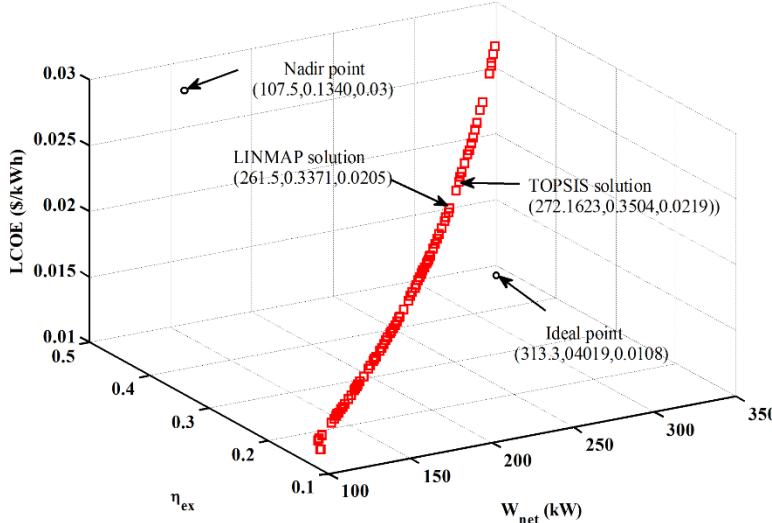


Fig.12. The pareto front curve of triple-objective for the presented system.

**Table 7**

Multi-objective optimization results by using LINMAP and TOPSIS decision makings.

Parameters	Ideal point	Nadir point	LINMAP	TOPSIS
$W_{\text{net}}$ (kW)	313.30	107.50	261.50	272.20
$\eta_{\text{ex}}$ (%)	40.19	13.40	33.71	35.04
$LCOE$ (\$/kWh)	0.0108	0.0300	0.0205	0.0219
$x$	0.99	0.10	0.67	0.72
$m_t$ (kg/s)	11.99	12.00	11.99	12.00
$T_g$ (K)	733.05	732.79	732.76	732.53
Deviation index			0.2517	0.1997

Three 2D figures detailing the Pareto front solutions and curve fitting for dual-objective ( $W_{\text{net}} - LCOE$ ,  $\eta_{\text{ex}} - LCOE$ ,  $W_{\text{net}} - \eta_{\text{ex}}$ ) optimizations are shown in Fig.13 which provide better understanding of the relationships between net power output, exergetic efficiency and levelized cost of energy. As can be seen from Fig.13 (a), the levelized cost of energy increases with the increase of net power output. Under the given conditions, the proposed system can deliver a maximum net power output of 313.30 kW with a maximum levelized cost of energy of 0.03 \$/kWh. The relationship between these two objectives is expressed as:

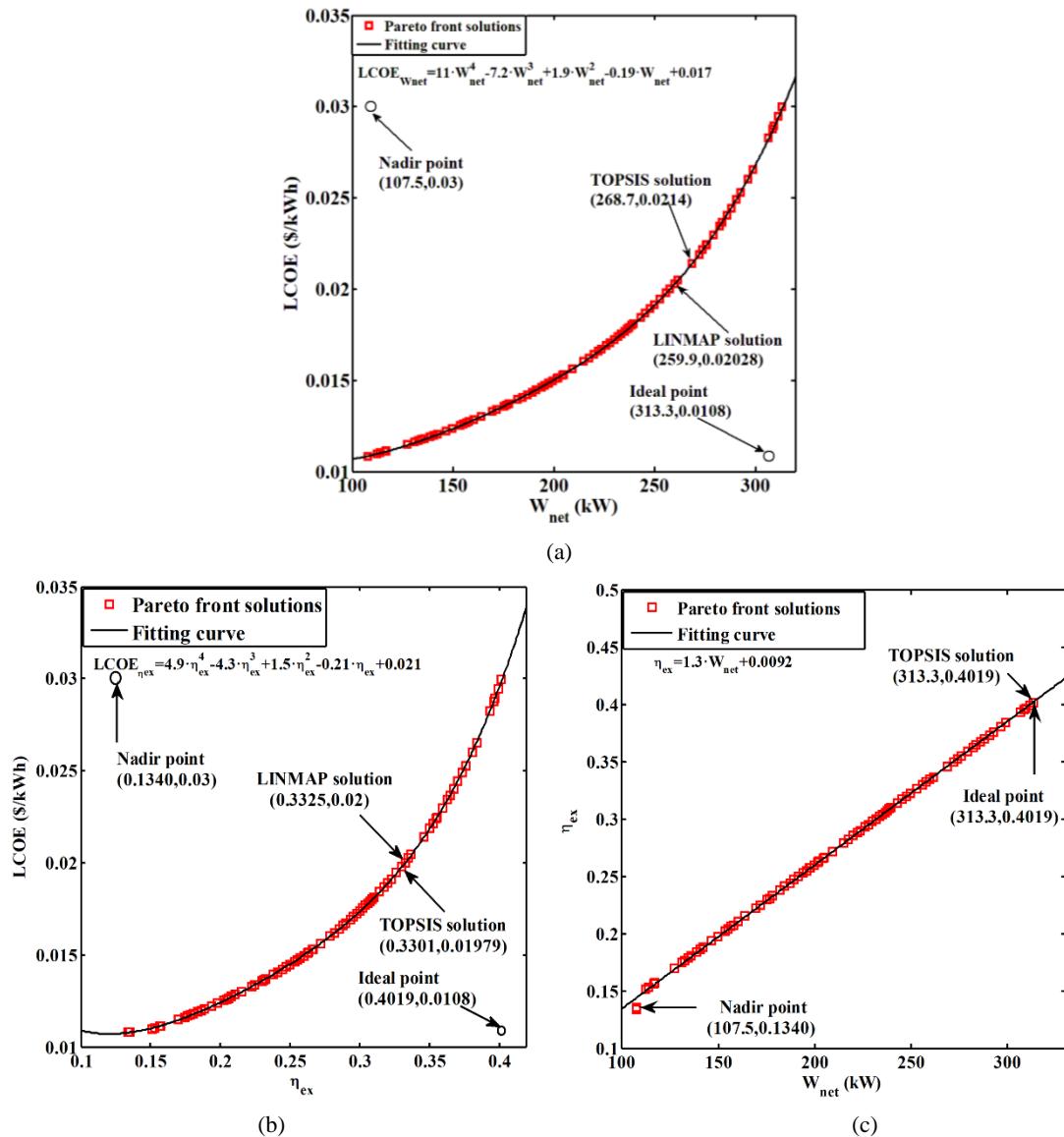
$$LCOE_{W_{\text{net}}} = 11 \cdot W_{\text{net}}^4 - 7.2 \cdot W_{\text{net}}^3 + 1.9 \cdot W_{\text{net}}^2 - 0.19 \cdot W_{\text{net}} + 0.017 \quad (22)$$

The increase of exergetic efficiency leads to an increase in the levelized cost of energy as shown in Fig. 13 (b). Fig.13 (c) shows that the exergetic efficiency increases linearly with the increase of net power output. The mathematical expressions to describe the relationships between levelized cost of energy and exergetic efficiency, exergetic efficiency and net power output are given as follows:

$$LCOE_{\eta_{\text{ex}}} = 4.9 \cdot \eta_{\text{ex}}^4 - 4.3 \cdot \eta_{\text{ex}}^3 + 1.5 \cdot \eta_{\text{ex}}^2 - 0.21 \cdot \eta_{\text{ex}} + 0.021 \quad (23)$$

1  $\eta_{ex} = 1.3 \cdot W_{net} + 0.0092$  (24)

2



7 Fig.13. Pareto front solutions fitting curves: (a). Net power output and leveled cost of energy; (b). Exergetic  
8 efficiency and leveled cost of energy; (c). Net power output and exergetic efficiency.

9 The final optimal results for these dual-objective optimizations decided by LINMAP and  
10 TOPSIS decision makings as well as their deviation indexes are listed in [Tables 8 to 10](#). In [Table 8](#),  
11 the deviation index for the final optimal result decided by TOPSIS (0.2167) is less than that from  
12 LINMAP (0.2595), which is consistent with the result in the triple-objective optimization decision  
13 making processes. The deviation index for the final optimal result decided by the TOPSIS (0.2693)  
14 in [Table 9](#) is higher than that from LINMAP (0.2605). The inconsistency of the deviation index in  
15 [Table 9](#) with that in [Table 7](#) and [Table 8](#) indicates that there is no clear standard to decide which  
16 method is suitable to conduct the multi-objective decision making for the S-CO<sub>2</sub> RBC system

1 performance. However, by comprehensively comparing the optimization results, TOPSIS decision  
 2 making is deemed the better choice to determine the final optimal result in this research project.  
 3 Owing to the linear relationship between net power output and exergetic efficiency, the final  
 4 optimal result of the dual-objective ( $W_{\text{net}} - \eta_{\text{ex}}$ ) is obtained at the ideal point, at which the  
 5 deviation index is 0 (Table 10). By analyzing the final optimal results of the multi-objective  
 6 optimizations, the deviation indexes of the final optimal results decided by TOPSIS and LINMAP  
 7 methods for dual-objective optimizations are higher than that of the triple-objective optimization.  
 8 In addition, the final optimal net power output and exergetic efficiency decided by the TOPSIS  
 9 decision making in the triple-objective optimization are higher than those calculated by the  
 10 dual-objective optimizations by approximately 1.29% and 5.11%, and the leveled cost of energy  
 11 calculated by the dual-objective optimization is 2.28% lower than that of the triple-objective  
 12 optimization. In summary, triple-objective optimization can produce more reliable optimization  
 13 results than dual-objective or even single-objective optimization.

**Table 8**

Comparison between optimal solutions for dual-objective ( $W_{\text{net}} - LCOE$ ) optimization.

Decision makings		Design variables		Objectives		Deviation index
	$x$	$m_t$ (kg/s)	$T_g$ (K)	$W_{\text{net}}$ (kW)	$LCOE$ (\$/kWh)	
NSGA-II	LINMAP	0.67	11.99	732.76	259.90	0.0203
	TOPSIS	0.70	11.99	733.15	268.70	0.0214

**Table 9**

Comparison between optimal solutions for dual-objective ( $\eta_{\text{ex}} - LCOE$ ) optimization.

Decision makings		Design variables		Objectives		Deviation index
	$x$	$m_t$ (kg/s)	$T_g$ (K)	$\eta_{\text{ex}}$ (%)	$LCOE$ (\$/kWh)	
NSGA-II	LINMAP	0.68	11.99	733.12	33.25	0.0200
	TOPSIS	0.66	12.00	733.14	33.01	0.0190

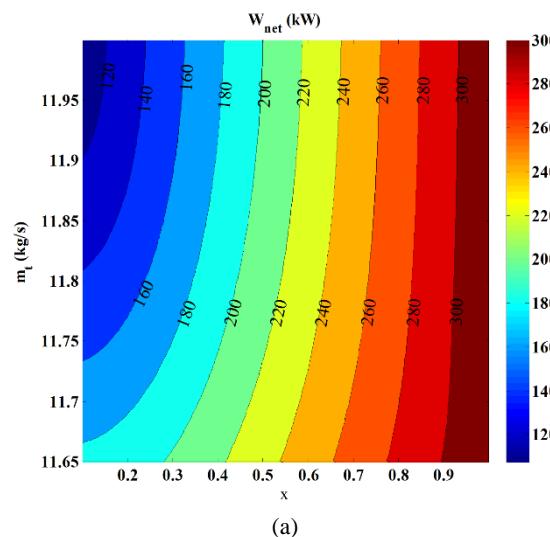
**Table 10**

Comparison between optimal solutions for dual-objective ( $W_{\text{net}} - \eta_{\text{ex}}$ ) optimization.

Decision makings		Design variables		Objectives		Deviation index
	$x$	$m_t$ (kg/s)	$T_g$ (K)	$W_{\text{net}}$ (kW)	$\eta_{\text{ex}}$ (%)	
NSGA-II	LINMAP	0.99	11.99	733.05	313.30	40.19
	TOPSIS	0.99	11.99	733.05	313.30	40.19

14 The effects on the three objective functions by flow split ratio and mass flow rate as decision  
 15 variables were analyzed. The contour plots in Fig. 14 show the variations of  $W_{\text{net}}$ ,  $\eta_{\text{ex}}$  and  $LCOE$

1 along with flow split ratio  $x$  and mass flow rate  $m_t$ . As can be seen from the contour plot in [Fig. 14 \(a\)](#), the maximum net power output is obtained close to the upper limit of the flow split ratio. According to the definition of flow split ratio, it indicates that as more working fluid  $\text{CO}_2$  flows into the re-compressor it produces more power from the proposed system. It is clear that the recompression cycle has the ability to produce more power than that of the simple recuperated cycle without recompression ( $x=0$ ). The effects of flow split ratio and mass flow rate on the exergetic efficiency and levelized cost of energy are shown in [Fig. 14 \(b\)](#) and [Fig. 14 \(c\)](#), respectively. From [Fig. 14 \(b\)](#), the peak exergetic efficiency occurs at the upper limit of the flow split ratio. That is because the heat energy in the working fluid can be further exploited in the recompression loop instead of being released to the environment through the pre-cooler, which can more fully exploit the waste heat to reduce the exergy loss and improve system exergetic efficiency. Therefore, compared with the simple recuperated cycle without recompression, the recompression Brayton cycle can improve the utilization of the waste heat. As can be seen from [Fig. 14 \(c\)](#), it is much more economic for the recompression Brayton cycle if it has a higher flow split ratio. Since the recompression Brayton cycle produces more power, this results in decrease of the levelized cost of energy. Compared with the simple recuperated cycle without recompression, the recompression Brayton cycle has advantages in system net power output, exergetic efficiency and levelized cost of energy. Considering the system performance and economics simultaneously, the recompression Brayton cycle is a better choice to exploit the ship's main engine exhaust gas waste heat recovery for this research project.



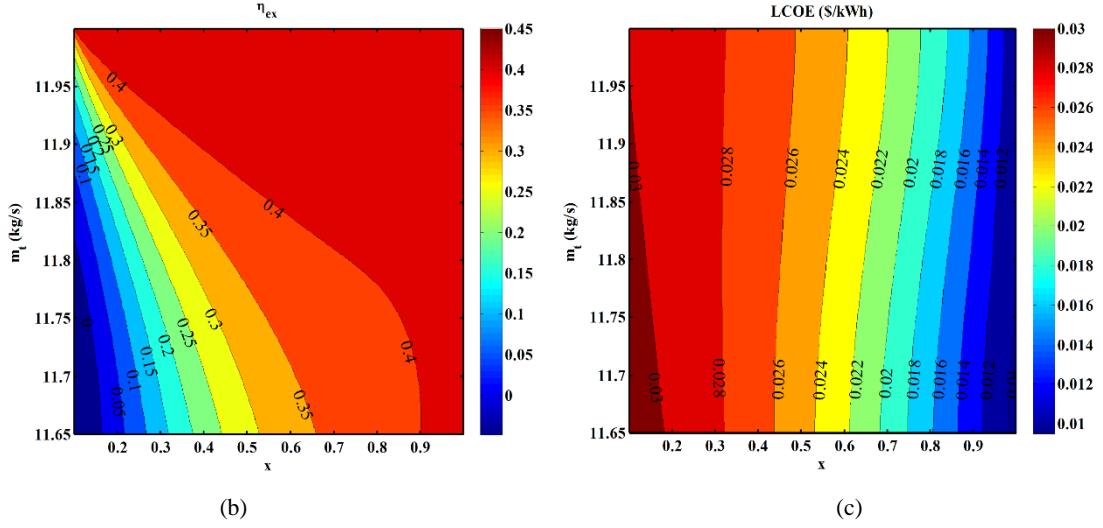


Fig.14. Objectives variations with mass flow rate and flow split ratio: (a). Net power output; (b). Exergetic efficiency; (c). Levelized cost of energy.

## 5. Conclusions

The thermodynamic models of the S-CO<sub>2</sub> recompression Brayton cycle for recovering the main engine exhaust gas waste heat from an ocean-going 9000 TEU container ship are established to evaluate the potential performance from both thermodynamic and economic perspectives by thermodynamic analysis and multi-objective optimization. A theoretical analysis is conducted to determine the effects of thermodynamic parameters on the steady-state system performance and decide their initial values, including main compressor inlet temperature, main compressor inlet pressure, pressure ratio, turbine inlet temperature and turbomachinery isentropic efficiency. For the purpose of maximizing the net power output and exergetic efficiency as well as minimizing the leveled cost of energy triple-objective ( $W_{\text{net}} - \eta_{\text{ex}} - LCOE$ ) and dual-objective ( $W_{\text{net}} - \eta_{\text{ex}}$ ,  $\eta_{\text{ex}} - LCOE$ ,  $W_{\text{net}} - LCOE$ ) optimizations were conducted using the NSGA-II algorithm-based multi-objective optimization, where flow split ratio, mass flow rate and exhaust gas waste heat temperature were considered as decision variables. To determine the final optimal result from Pareto front solutions, LINMAP and TOPSIS decision-making methods were employed. The main conclusions were as follows:

- (1) The results of the thermodynamic analysis reveal that the thermodynamic parameters have significant and comprehensive effects on the system's overall performance. Specifically, higher main compressor inlet temperature has a negative effect on system performance. The proposed system achieved better system performance at the relatively low main compressor inlet temperature of approximately 34 °C. The main compressor

1 inlet pressure brings positive effects on the system exergetic efficiency, while its effect  
2 on the system's net power output is no longer so significant when it exceeds 8.0 MPa.  
3 When the pressure ratio is in the range of 2.0 ~ 3.0, there is a positive effect on the  
4 system net power output and exergetic efficiency, but the net power output and exergetic  
5 efficiency all have their own optimal pressure ratios. Higher turbomachinery isentropic  
6 efficiency contributes to better system performance, but such benefits will be restricted  
7 by the manufacturing technologies. So, on the basis of the thermodynamic analysis, the  
8 initial thermodynamic parameters are fixed at  $T_{mc,in} = 34^{\circ}\text{C}$ ,  $P_{mc,in} = 8.0 \text{ MPa}$ ,  $P_r = 2.5$ ,  
9  $isen_{mc} = 0.65$  and  $isen_t = 0.75$ .

10 (2) The Pareto front results showed that the leveled cost of energy increased with the  
11 increase of net power output and exergetic efficiency, which were in the ranges of 0.01  
12 \$/kWh to 0.03 \$/kWh, 107.50 kW to 313.30 kW and 13.40% to 40.19%, respectively.  
13 The maximized system performance solution occurs close to the upper limit of the  
14 exhaust gas waste heat temperature, which indicates that higher exhaust gas waste heat  
15 temperature can produce a positive effect on the system performance. In addition, the  
16 curve fits and mathematical expressions to demonstrate the relationships between the  
17 objective functions based on Pareto front solutions were plotted and obtained, which  
18 could be used to assist the S-CO<sub>2</sub> recompression Brayton cycle waste heat recovery  
19 system's optimal design.

20 (3) By comparing the deviation indexes of the final optimal results decided by LINMAP  
21 and TOPSIS decision-making methods, the TOPSIS decision making was deemed the  
22 reasonable choice. In addition, the final optimal net power output and exergetic  
23 efficiency obtained by triple-objective optimization were higher than the results  
24 calculated by dual-objective optimizations by 1.29% and 5.11%, while the leveled cost  
25 of energy calculated by dual-objective optimization was 2.28% lower than that from the  
26 triple-objective. Therefore, the triple-objective optimization provided more reasonable  
27 results than that from dual-objective optimization or even single-objective optimization.

28 (4) The results of the flow split ratio and mass flow rate effects on the net power output,  
29 exergetic efficiency and leveled cost of energy confirmed that the recompression  
30 Brayton cycle is an acceptable choice to be used to recover the ship main engine exhaust  
31 gas waste heat compared with the simple recuperated cycle without recompression.

32 (5) In this study, the working fluid CO<sub>2</sub> in the system is considered to be always in the  
33 supercritical state. However, considering that when the system is shut down and  
34 restarted, some of the remaining working fluid CO<sub>2</sub> in the system may not be in its

supercritical state. Thus, the influence of the transcritical CO<sub>2</sub> on performance of S-CO<sub>2</sub> recompression Brayton cycle system needs to be further studied.

## Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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