

1 Different reactor configurations for enhancement of CO₂ 2 methanation

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18 **Abstract**

19 Greenhouse gas emissions are a massive concern for scientists to minimize the effect of global
20 warming in the environment. In this study, packed bed, coated wall, and membrane reactors
21 were investigated using three novel nickel catalysts for the methanation of CO₂. CFD
22 modelling methodologies were implemented to develop 2D models. The validity of the model
23 was investigated in a previous study where experimental and simulated results in a packed bed
24 reactor were in a good agreement. It was observed that the coated wall reactor had poorer
25 performance compared to the packed bed, approximately 30 % difference between the results,
26 as the residence time of the former was lower. In addition, two membrane configurations were
27 proposed, including a membrane packed bed and membrane coated wall reactor. Additional
28 studies were performed in the coated wall reactor revealing that lower flow rates lead to higher
29 conversion values. As for the bed thickness the optimum layer was found to be 1 mm. In both
30 membrane reactor configurations, the effect of the thickness of M₁ membrane, which indicates
31 the membrane for the removal of H₂O, didn't show difference while the reduction of the
32 thickness of M₂ membrane, which indicates the membrane for the removal of CO₂, H₂ and H₂O,
33 showed better results in terms of conversion.

34 **Keywords**

35 CO₂ methanation; packed bed reactor; coated wall reactor; membrane reactor; CFD modelling.

36 1. Introduction

37 The global mean temperature increase is required to be stabilized to 1.5 – 2 °C relative to the
38 preindustrial era. In order to achieve that, the global yearly emissions must be net-zero or net-
39 negative before 2100 [1,2]. The link between the carbon emissions with the globalization,
40 economic growth and consumption of coal is positive with significant co-movements [3].
41 Carbon capture and utilization (CCU) technologies have attracted the interest of many
42 scientists [4,5] as they can achieve reductions in CO₂ emissions along with sustainable energy
43 technologies and technologies with negative or zero emissions [2]. It is important to reduce the
44 cost and improve the performance of this technology in order to be utilized in large scales [6].
45 The generation of an energy carrier, CH₄, is creating a power-to-gas platform and a circular
46 carbon economy [7–9]. The power-to-gas technology can be involved and contribute in the
47 intermittent power production from renewable energy sources (RES) [10]. The firsts who
48 proposed the CO₂ conversion to CH₄ were Sabatier and Senderens in 1902 [11] and it is
49 described as [12]:



50 The side-reactions that occur in parallel are the reverse water-gas shift (RWGS) and the
51 CO methanation reactions and are involved in the methanation reaction, described by Eq. 2 and
52 Eq. 3, respectively [12].



53 The utilization of CH₄ in industries is promising as it will reduce their energy demands
54 and CO₂ emissions [13]. A plethora of studies have investigated different types of catalyst
55 particles in an effort to optimize and enhance the conversion and selectivity of CO₂
56 methanation reaction over the time [14–22]. It is noted that these studies have been mostly
57 carried out in packed bed reactors [23–26]. We note an earlier work from our group [27], in
58 which we reviewed the CO₂ hydrogenation to valuable chemicals, including the CH₄ generation
59 pathway, according to the challenges faced and the limitations between the convectional units
60 and microreactors.

61 Coated wall reactors constitute a development of packed bed reactors where the solid
62 catalyst particles are loaded and packed in a layer attached to the wall of the reactor. Coated

63 wall reactors provide lower pressure drops over the length of reactors cause of the form of drag,
64 ease of the manufacturing [28], and faster heat exchange with the wall due to their intimate
65 contact. Also, the approach of coated wall reactor would have been better for faster and more
66 exothermic reactions rather than a traditional fixed bed reactor in order to obtain isothermal
67 conditions. The gradients of radial concentrations might be considered as a potential drawback
68 of coated wall reactors gradients by dispersion [29]. Danaci et al. [30], examined in a packed
69 bed reactor 3D-structured catalysts prepared by deposition of fiber and coated with Ni/Al₂O₃
70 suspension, and compared them with powder Ni/Al₂O₃. The 3D-structured catalysts showed
71 improvements in conversion and catalytic stability at higher temperatures. Huynh et al. [31],
72 recently investigated bimetallic NiFe catalysts prepared. Temperature profiles along the reactor
73 were derived from experimental results and computational fluid dynamics (CFD) studies. The
74 packed bed configuration that was used in the study (low-high activity monolithic bed)
75 achieved approximately 80% CH₄ yield at 250 °C. Moreover, Gruber et al. [32], optimized a
76 coated wall reactor for CO₂ methanation. Both the 1D and 3D reactor models developed
77 revealed the importance of external heat transfer. Adjustment in the layer of the catalyst by
78 increasing its thickness revealed that the release of heat from the layer is increased while the
79 heat transfer is reduced. Generally, the majority of studies use packed bed reactors during their
80 investigations due to their economic efficiency. However, the coated wall reactor design for
81 the CO₂ methanation reaction still lacks information, even though it can help optimize heat
82 transfer and eliminate the pressure drop along the reactors.

83 Membrane reactors are a continuously developed technology with many advantages as
84 they can operate the separation of various components and reactions in one system [33]
85 reducing significantly the cost of a process. Moreover, reaction's yield can be improved as the
86 selective separation of species can shift the equilibrium of a reaction. The Le Chatelier's
87 principle is applied in order to restore the equilibrium [7]. Ohya et al. [34], used a membrane
88 reactor in order to selectively remove the H₂O. Results revealed that the improvement in
89 conversion was about 18% when a membrane reactor was used. Iwakiri et al. [35], used a non
90 isothermal membrane reactor for the methanation of CO₂. The studied reactor and a fixed-bed
91 reactor were compared using MATLAB; showing that the membrane reactor can achieve the
92 same results, but at milder conditions. Another CFD study including the production of CH₄
93 using a heat-exchange membrane reactor was performed by Farisabadi et al. [36] and under
94 optimal conditions a 99% CO₂ conversion was achieved.

95 The presence of CO₂ at industrial scale processes may cause corrosion or increase the
96 volume of the gas transported in the pipelines, so the removal of CO₂ is a desired process.
97 There are a lot of membrane types such as, polymeric, inorganic, metal-organic framework,
98 zeolite and mixed-matrix membranes (MMMs) [37]. MMMs are combining the benefits of two
99 types of membranes, the polymeric and inorganic, for the CO₂ removal from different gas fluids
100 [38]. Wang et al. [39], investigated the separation CO₂/CH₄ using ZIF-301 filler in polyimide
101 MMM revealing that the filler tended to improve the CO₂/CH₄ selectivity and the CO₂
102 permeability. Widiastuti et al. [40], aimed to enhance the CO₂ and H₂ removal efficiency from
103 CH₄ with PSF/ZTC MMM. They showed the temperature effect and the TMOS concentration
104 on membrane's performance by the reduction of pore size.

105 In this work, we carried out a theoretical investigation of different reactor designs, i.e.,
106 coated wall and membrane reactor configurations and compared their performance to a
107 previous work published by our group for packed bed reactor [41]. Main goal was to assess
108 their performance during CO₂ methanation and improve the conversion and selectivity of the
109 reaction. CFD modelling studies offer better understanding of parameter optimization for
110 different reactor systems [27], [42–49].

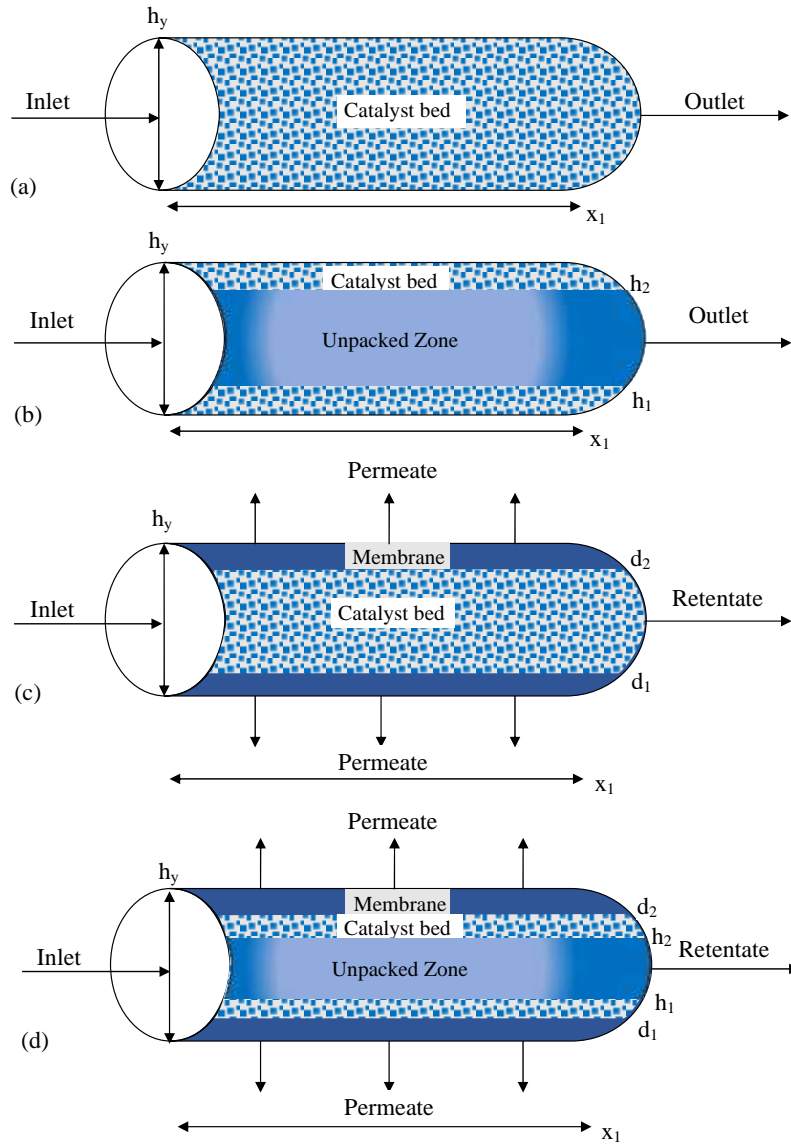
111 **2. Modelling Methodology**

112 A packed bed reactor was used for the experimental investigation of novel nickel catalysts
113 on Pr-CeO₂ support synthesized using three different preparation methods. The catalyst's mass
114 was 0.24 g and the space velocity was 25,000 ml g_{cat}⁻¹ h⁻¹, while the reaction temperature varied
115 between 200 and 450 °C. A theoretical investigation based on the experimental results was
116 performed revealing the validation of the designed model. The full specifics of the previous
117 experimental and theoretical work can be found in our previous work [41].

118 The theoretical investigation is an alternative solution to the experimental work as it
119 requires less effort and expense. CFD models can determine the transport phenomena of
120 heterogeneous flows within a reactor as well as important information of space-time variations
121 in species flows, concentrations, and temperatures. Thus, CFD is a beneficial tool to predict
122 parameters and to perform investigation of the physicochemical processes involved.

123 The reactor configurations presented by Figure 1 were designed as 2D configurations
124 assuming that the gradients of concentrations and temperatures take place only in the radial
125 and axial directions. Table 1 shows the geometrical properties of the reactor configurations that

126 were used in this work. Plug flow type is the overall flow transport mechanism that is operating
127 in the axial direction. Additional assumptions that were incorporated in the model design are:
128 (a) the solution of the study was stationary and temperature distribution was isothermally over
129 the reactor, (c) all the gases behaved as ideal gases, (d) the transport coefficients and physical
130 properties of the constant axial fluid velocity were uniform, and (e) the catalytic material in the
131 reaction zone is in the form of powder. The investigation of internal and external limitations
132 from the mass transfer resistance was occurred at a previous published work of our team.
133 Experimentally and theoretically, the limitations of pressure drop, and heat transfer were found
134 negligible. The reactor's height and length are 0.9 cm and 30 cm, respectively. The membrane
135 materials that were used for the separation of gases are ZSM-5 and PDMS [50–52]. The
136 membrane materials that were used in this work where: (i) the ZSM-5 membrane is selective
137 to remove only H₂O; and (ii) the PDMS membrane is selective to remove CO₂, H₂ and H₂O
138 from the gas mixture. The catalysts used herein are Ni-based supported catalysts, whose Pr-
139 doped CeO₂ supports were prepared through different synthesis methods, i.e., citrate sol-gel
140 synthesis (CSG), Pechini synthesis (PC) and modified Pechini synthesis (MPC). The Ni phase
141 (10 wt%) was subsequently introduced into the prepared supports via wet impregnation and,
142 as such, the corresponding catalysts were labelled as Ni/CSG, Ni/PC and Ni/MPC.



143

144 **Figure 1.** Reactor configurations designed for the CFD modelling study: (a) packed bed, (b)
 145 coated wall, (c) membrane packed bed, and (d) membrane coated wall reactors.

146 **Table 1.** Geometrical properties of the reactor configurations.

Item	Value
Length of reactor (x_1)	30 cm
Packed bed reactor diameter (h_y)	0.9 cm
Each catalyst layer thickness	0.1 cm
Unpacked zone thickness (h_1, h_2)	0.7 cm
Each membrane layer thickness (d_1, d_2)	7 mm

147

148 2.1 Reaction rates

149 The kinetic model of CO₂ methanation reaction was firstly proposed by Xu and Froment
 150 [53], considering all three reactions for the methanation process (Eqs 1-3). The three reactions
 151 occur in parallel with the RWGS reaction converting CO₂ to CO, which thereafter generates
 152 CH₄ through the CO methanation reaction. The rate equations that describe the methanation
 153 reaction are given below (Eqs 4-6):

$$r_{CO_2\text{ Meth.}} = \frac{\frac{k_{CO_2\text{ Meth.}}}{p_{H_2}^{3.5}} \left(p_{H_2}^4 p_{CO_2} - \frac{p_{CH_4} p_{H_2O}^2}{K_{eq,CO_2\text{ Meth.}}} \right)}{\left(1 + K_{CO} p_{CO} + K_{H_2} p_{H_2} + K_{CH_4} p_{CH_4} + \frac{K_{H_2O} p_{H_2O}}{p_{H_2}} \right)^2} \quad (4)$$

$$r_{RWGS} = \frac{\frac{k_{RWGS}}{p_{H_2}} \left(p_{H_2} p_{CO_2} - \frac{p_{CO} p_{H_2O}}{K_{eq,RWGS}} \right)}{\left(1 + K_{CO} p_{CO} + K_{H_2} p_{H_2} + K_{CH_4} p_{CH_4} + \frac{K_{H_2O} p_{H_2O}}{p_{H_2}} \right)^2} \quad (5)$$

$$r_{CO\text{ Meth.}} = \frac{\frac{k_{CO\text{ Meth.}}}{p_{H_2}^{2.5}} \left(p_{H_2}^3 p_{CO_2} - \frac{p_{CO} p_{H_2O}}{K_{eq,CO\text{ Meth.}}} \right)}{\left(1 + K_{CO} p_{CO} + K_{H_2} p_{H_2} + K_{CH_4} p_{CH_4} + \frac{K_{H_2O} p_{H_2O}}{p_{H_2}} \right)^2} \quad (6)$$

154 where $k_{CO_2\text{ Meth.}}$, k_{RWGS} , $k_{CO\text{ Meth.}}$ are the rate constants of reactions. K_{CO} , K_{H_2} , K_{CH_4} and, K_{H_2O}
 155 are the adsorption equilibrium constants and p_{CO_2} , p_{CO} , p_{H_2} , p_{CH_4} and p_{H_2O} are the partial
 156 pressure of species. By the constants Xu and Froment proposed in their model, the data
 157 according to kinetic and adsorption constants that were used for this CFD simulations were
 158 adjusted using parametric studies and can be found in a previous study [41]. There has been
 159 commodiously discussion in literature about the reaction intermediate of the methanation
 160 reaction with disagreement between different studies [54]. The three-step model used in this
 161 study is a Langmuir-Hinshelwood kinetic validated and used by many researchers [55–57]
 162 while it can address the CO₂ methanation and provide good agreement between experimental
 163 and simulated results [58].

164 2.2 Conservation equations

165 To design the reactor configurations mass balance equations were implicated for the
 166 transportation of species in the reactor. The Chemistry interface and the interface of Transport
 167 of Diluted Species with the feature of Reactive Pellet Bed are the physics that were employed

168 for this work using COMSOL Multiphysics. Eq. 7 describes the mass balance of species in the
 169 packed bed.

$$u_x \frac{\delta c_i}{\delta x} = D_{i,A} \frac{\delta^2 c_i}{\delta x^2} + D_{i,T} \frac{\delta^2 c_i}{\delta y^2} - J_i S_b \quad (7)$$

170 where, D_i and J_i are the coefficient of axial dispersion in the transverse or axial directions, and
 171 the fluid's molar flux in the powdered catalyst, respectively. The S_b is the catalyst's surface-
 172 active specific area in contact with the fluid reactants and is described as [59]:

$$S_b = \frac{3}{r_{pe}} (1 - \varepsilon) \quad (8)$$

173 where, ε is catalyst's bed void fraction and r_{pe} is the size of catalyst powder.

174 At the interface of pellet-fluid the film condition's assumption is made. The rate
 175 determined step can be the mass flux is related with mass balance and considered as boundary
 176 condition. The coefficient of external mass transfer is considered as the resistance and is
 177 described as:

$$J_i = h_i (c_i - c_{i,ps}) \quad (9)$$

$$h_i = \frac{Sh \cdot D_i}{2r_{pe}} \quad (10)$$

$$Sc = \frac{\mu}{\rho \cdot D_i} \quad (11)$$

$$Re = \frac{2r_p \cdot \rho \cdot u_x}{\mu} \quad (12)$$

$$Sh = 2 + 0.552 Re^{1/2} Sc^{1/3} \quad (13)$$

178 where, h_i and $c_{i,ps}$ are the coefficient of external mass transfer and species concentration at
 179 catalyst's surface. Sc , ρ and μ are the Schmidt number, the density, and the viscosity of the
 180 reacting fluids, respectively. Re is the Reynolds number and Sh is the Sherwood number
 181 [60,61].

182 The species mass balance equation in the unpacked area of coated wall reactor can be
 183 expressed as:

$$u_x \frac{\delta c_i}{\delta x} = D_i \left(\frac{\delta^2 c_i}{\delta x^2} + \frac{\delta^2 c_i}{\delta y^2} \right) \quad (14)$$

184 The reaction is occurring in the bed area where it is packed with catalyst in the form of
 185 powder. Across the spherical shell mass balance of the powdered particle and an extra 1D
 186 predefined dimension on the normalized radius ($r = r_{dim}/r_{pe}$) is expressed as:

$$4\pi N \left\{ r^2 r_{pe}^2 \varepsilon_{pe} \frac{\partial c_{pe,i}}{\partial t} + \nabla \cdot (-r^2 D_{i,eff} \nabla c_{pe,i}) = r^2 r_{pe}^2 R_{pe} \right\} \quad (15)$$

187 where, N is particles number, $D_{i,eff}$ is the effective diffusion coefficient of fluids in the pores
 188 of powdered particle, $c_{pe,i}$ is the concentration of components in the powdered catalyst and R_{pe}
 189 is the term of reaction rate.

190 Knudsen or bulk diffusion coefficients are considered to calculate the component species
 191 effective diffusivities in the pores of the powdered catalysts expressed as [60]:

$$D_{i,eff} = \frac{D_{i,AB} \Phi_p \sigma_c}{\tau} \quad (16)$$

192 where, $D_{i,AB}$ is the diffusivity of fluid components in bulk, Φ_p is the porosity of the powdered
 193 catalyst and σ_c and τ are the constriction factor and tortuosity, respectively.

194 The conservation equation of component species i transportation in the membrane is
 195 described as:

$$D_{i,m} \left(\frac{\delta^2 c_{i,m}}{\delta x^2} + \frac{\delta^2 c_{i,m}}{\delta y^2} \right) = 0 \quad (17)$$

196 where, $c_{i,m}$ and $D_{i,m}$ are the concentration and the species coefficient of diffusion, in the
 197 membrane.

198 The Particle Tracing Module is a tool offered by COMSOL to find the distribution of
 199 residence time by computing the direction of particles. The residence time distribution is
 200 determined by the following equation where is an alternative to the first order Newtonian
 201 formulation.

$$\frac{dq}{dt} = v \quad (18)$$

202 where, q is the pellet position (m) and v the velocity of the particle (m/s).

203 The boundary conditions used for investigated reactor configurations are given per
204 following:

205 Coated-wall reactor:

$$\text{at } x = 0; c_i = c_{i,in} \quad (19)$$

$$\text{at } x = x_i; \frac{\delta c_i}{\delta x} = 0 \quad (20)$$

$$\text{at } y = 0; c_i = 0 \quad (21)$$

$$\text{at } r = 1; c_{i,p} = c_{i,ps} \quad (22)$$

$$\text{at } r = 0; \frac{\delta c_{i,p}}{\delta r} = 0 \quad (23)$$

$$\text{at } y = h_1; c_{i,b} = K \times c_i \quad (24)$$

$$\text{at } y = h_2; c_{i,b} = K \times c_i \quad (25)$$

206 Membrane packed bed reactor:

$$\text{at } x = 0; c_i = c_{i,in} \quad (26)$$

$$\text{at } x = x_i; \frac{\delta c_i}{\delta x} = 0 \quad (27)$$

$$\text{at } y = 0; c_i = 0 \quad (28)$$

$$\text{at } r = 1; c_{i,p} = c_{i,ps} \quad (29)$$

$$\text{at } r = 0; \frac{\delta c_{i,p}}{\delta r} = 0 \quad (30)$$

$$\text{at } y = d_1, y = d_2; c_{i,m} = Hc_i \quad (31)$$

$$\text{at } y = 0, y = h_y; c_{i,m} = c_{i,g} \quad (32)$$

207 Membrane coated-wall reactor:

$$\text{at } x = 0; c_i = c_{i,in} \quad (33)$$

$$\text{at } x = x_i; \frac{\delta c_i}{\delta x} = 0 \quad (34)$$

$$\text{at } y = 0; c_i = 0 \quad (35)$$

$$\text{at } r = 1; c_{i,p} = c_{i,ps} \quad (36)$$

$$\text{at } r = 0; \frac{\delta c_{i,p}}{\delta r} = 0 \quad (37)$$

$$\text{at } y = h_1; c_{i,b} = K \times c_i \quad (38)$$

$$\text{at } y = h_2; c_{i,b} = K \times c_i \quad (39)$$

$$\text{at } y = d_1, y = d_2; c_{i,m} = Hc_i \quad (40)$$

$$\text{at } y = 0, y = h_y; c_{i,m} = c_{i,g} \quad (41)$$

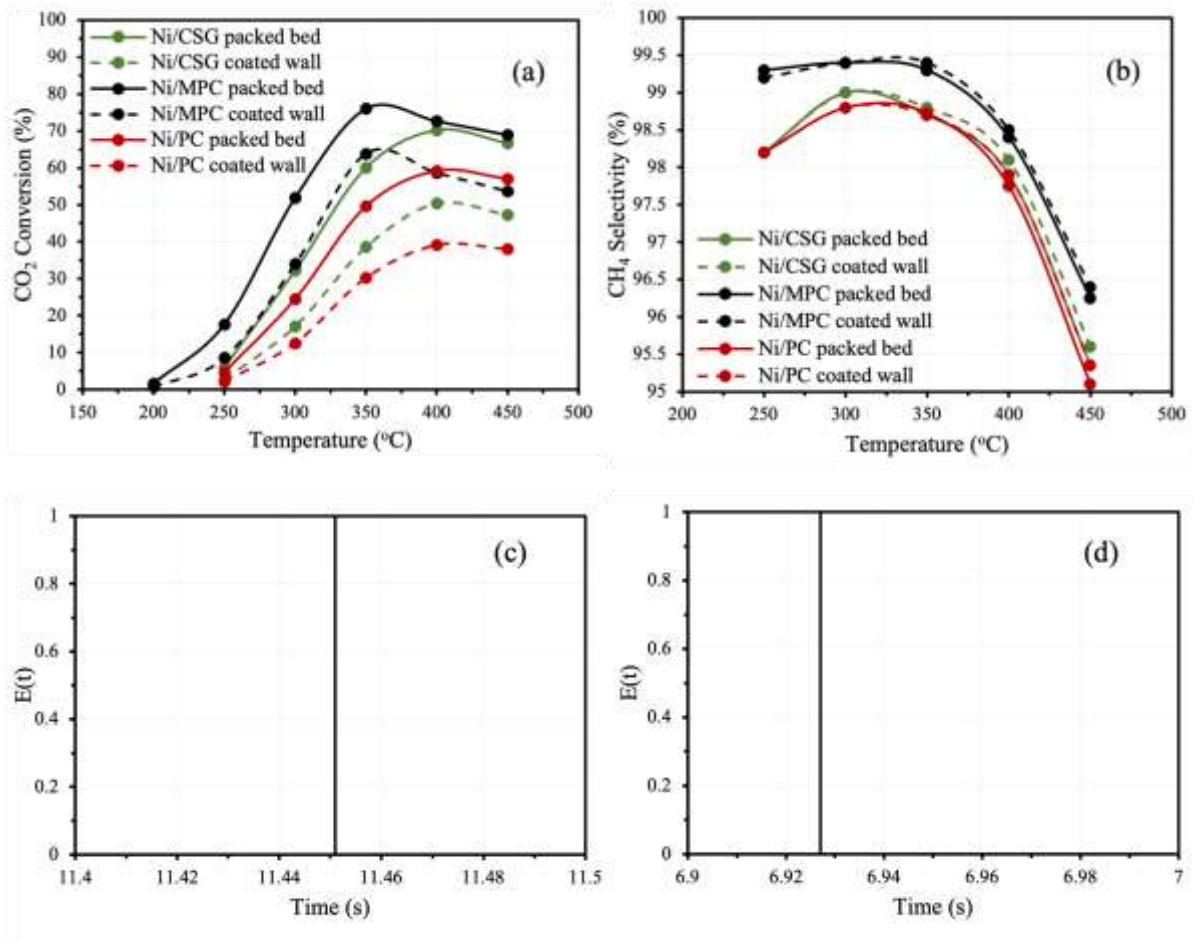
208 The software that was used for this work was the COMSOL Multiphysics in version 5.5
 209 to couple all the boundary conditions, mass balances and conservation equations. Coated wall
 210 reactor's geometry had a mesh with domain elements of 2700 and degrees of freedom of 81270.
 211 The membrane packed bed microreactor model geometry had a mesh with domain elements of
 212 2700 and degrees of freedom of 180600. The membrane coated wall microreactor model
 213 geometry had a mesh with domain elements of 2700 and degrees of freedom of 81270. The
 214 results for all the CFD models were found to be not influenced by the mesh as the solution was
 215 checked for higher degrees of freedom. The parameters used in this modelling study that were
 216 obtained from the experimental results are included in our previous published work [41].

217 **3. Results and Discussion**

218 **3.1 Coated wall and membrane reactor**

219 The results obtained from the CFD modelling studies are shown in this section. The
 220 validation of the model was examined in our previous study in packed bed reactor, where good
 221 agreement was observed from experimental and simulated results [41]. Coated wall and
 222 membrane reactors were investigated and compared to our previous work concerning the
 223 packed bed reactor. The reactors were operated at 1 atm and from 200 to 450 °C. The packed
 224 bed and coated wall reactor comparison is presented in Figure 2. It is observed from Figure
 225 2(a), that the conversion of CO₂ in the coated wall reactor has decreased comparing to the
 226 performance of packed bed, and that can be attributed to the flow distribution inside the reactor.

227 In coated wall reactor the inner diameter is decreased, whilst the gas fluid velocity within the
228 reactor has increased for the same inlet flow rate. The mass of the catalyst used in both
229 configurations was the same. Also, using the Particle Tracing Module offered by COMSOL,
230 an investigation of the residence time of each reactor has occurred as there is no pressure drop
231 or any mass and heat limitations to attribute the decrease of conversion in coated wall reactor.
232 Residence time of the coated wall reactor was found to be 6.927 sec, and the residence time of
233 the packed bed one was found to be around 11.451 sec, which is approximately 2 times than
234 that of the coated wall reactor (Figure 2(c) and (d)). E(t) function is a fraction of molecules
235 exiting the reactor that have spent a time t in the reactor. According to the residence time, we
236 can assume that not all of the reactant molecules are passing through the thin catalyst layer of
237 coated wall reactor, as the bed porosity is decreased. The selectivity was calculated considering
238 the concentrations of CH₄ and CO with the equation given as $C_{CH_4}/(C_{CH_4} + C_{CO})$. The CH₄
239 selectivity (Figure 2(b)), decreases as the temperature increases, while the results between both
240 reactors are similar. From this study it was obtained that the selectivity isn't influenced by the
241 configurations of the coating layer since the amount of the catalyst used in packed bed and
242 coated wall configurations is the same. The selectivity of a catalyst is mostly affected by the
243 reaction conditions and the nature of the catalyst [62].



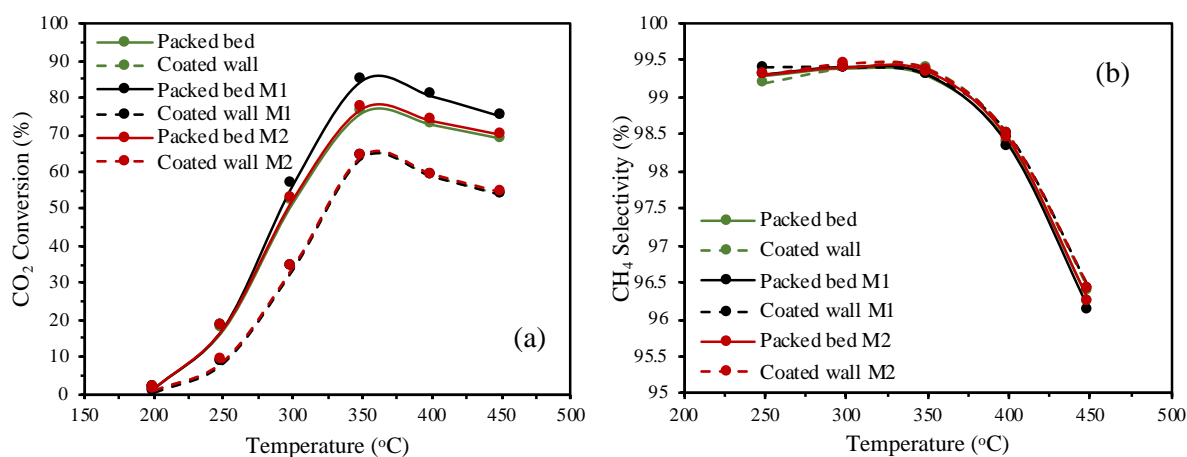
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245

246 **Figure 2.** (a) CO₂ Conversion and (b) CH₄ Selectivity as a function of reactor temperature for
 247 the packed bed and the coated wall reactor. Residence Time Distribution in (c) the packed bed
 248 and (d) the coated wall reactor. Reaction conditions: WHSV = 25,000 ml g_{cat}⁻¹ h⁻¹, bed porosity
 249 of packed bed 0.65 and bed porosity of coated wall 0.115.

250 The membrane modelling studies occurred for the best in performance catalyst, which is
 251 the Ni/MPC catalyst. M₁ and M₂ are the membrane configurations that were used in the CFD
 252 simulations. Membrane M₁ is selectively removing only H₂O and membrane M₂ is selectively
 253 separating CO₂, H₂ and H₂O from the gas mixture. By including the membranes in the reactor
 254 system, the methanation of CO₂ and the separation of various components is operating at the
 255 same time. The obtained results from both configuration studies can be found in Figure 3. It is
 256 observed from Figure 3(a), the conversion has slightly increased in packed bed reactor by using
 257 M₁ at higher temperatures. For the coated wall reactor, there is no significant difference
 258 between the initial study or with the addition of M₁. In both cases, almost 100% removal of
 259 H₂O is achieved. Removing the H₂O shifts the equilibrium of the reaction based on Le
 260 Chatelier's principle where is applied to restore the equilibrium and hence the CO₂ conversion

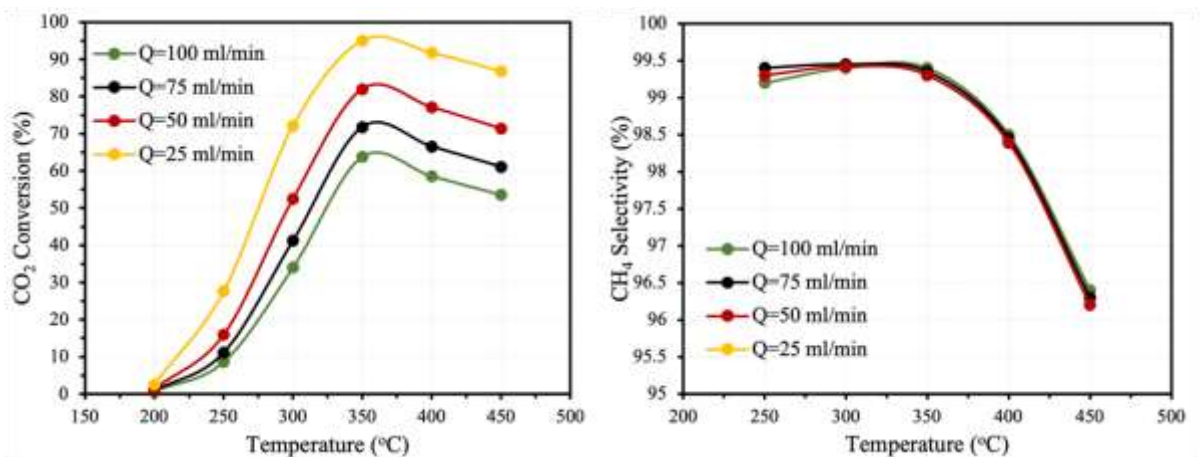
261 is increased. The scope of using the M_1 for the separation of H_2O only aims to increase the CO_2
 262 conversion. Catarina Faria et al. [63], used a traditional packed bed reactor and a H-SOD
 263 membrane reactor with the simulated results revealing that the H_2O permeable membrane
 264 improved the CO_2 conversion and herein the performance of the reactor. The water permeable
 265 membrane Ohya et al. [34], revealed that the conversion was increased by a maximum of 18%
 266 with the membrane. A second membrane, M_2 , was then investigated for the removal of CO_2 ,
 267 H_2 and H_2O . In packed bed reactor, it was observed from the figure that there is a slightly
 268 increase in the conversion, which it can be attributed to Le Chatelier's principle, while in coated
 269 wall reactor, no significant changes in the CO_2 conversion were observed. M_2 membrane not
 270 only removes H_2O , which is a product, but also the reactants. With the M_2 membrane, we aimed
 271 to create a single system where both reaction and separation of CH_4 from the other components
 272 can be achieved. CH_4 selectivity, as can be seen from Figure 3(b), remains constant in both
 273 reactors. The selectivity of the reaction is not influenced by the reactor configurations or the
 274 introduction of membranes in the system since the catalyst and the amount of the catalyst used
 275 for the computation studies was constant. Goswami et al. [64], compared three reactor
 276 configurations with the examined packed bed membrane, coated wall, and coated wall
 277 membrane reactors having a similar trend with our findings. The conversion in packed bed
 278 membrane reactor was obtained to be the optimum while the membrane coated wall reactor
 279 had better performance than the coated wall reactor.



280
 281 **Figure 3.** (a) CO_2 Conversion and (b) CH_4 Selectivity as a function of reactor temperature for
 282 the Ni/MPC catalyst in packed bed, coated wall, and membrane reactor configurations.
 283 Reaction conditions: $WHSV = 25,000 \text{ ml g}_{\text{cat}}^{-1} \text{ h}^{-1}$, bed porosity of packed bed 0.65 and bed
 284 porosity of coated wall 0.115.

3.2 Effect of flow rate in coated wall reactor

The conversion and selectivity were investigated how they're affected by the flow rate in this section in the coated wall reactor using the Ni/MPC catalyst. The initial inlet flow rate of the experimental and simulated studies was 100 ml/min. To enhance the methanation reaction in the coated wall reactor, a case study, was performed to examine the conversion of CO₂ at different inlet flow rates has occurred. 75, 50 and 25 ml/min flow rates were examined, and the results can be found in Figure 4. At lower inlet flow rates, the CO₂ conversion obtained higher values (Figure 4(a)). By decreasing the reactor's inlet flow rate, the fluid's velocity is also decreased and therefore the residence time of the fluid is affected. However, larger residence times led to increase of the conversion. The conversion and selectivity at 350 °C and 25 ml/min flow rate stand above 95 % and 99.3 %, respectively. Moreover, no significant differences in the selectivity of CH₄ are observed from Figure 4(b). Oh et al. [65], showed in a coated wall reactor, that the CH₄ conversion into olefins and higher hydrocarbons was affected by the flow rate having similar conversion trend as the one found in this study. At higher temperature and lower inlet flow rate, maximum conversion was achieved.



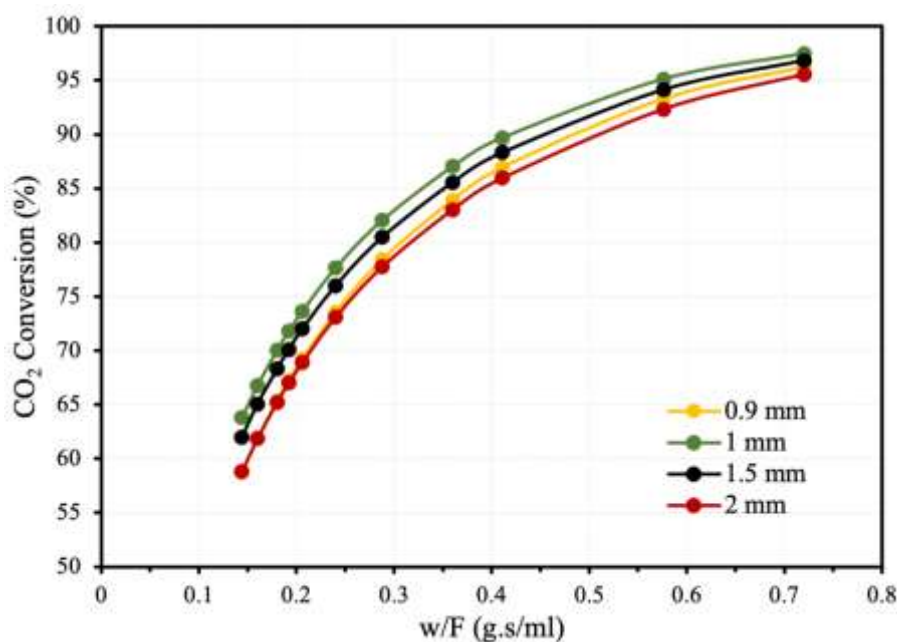
300

301 **Figure 4.** (a) CO₂ Conversion and (b) CH₄ Selectivity as a function of reactor temperature for
302 the Ni/MPC catalyst in coated wall reactor at different flow rates. Reaction conditions: Bed
303 porosity of coated wall 0.115.

3.3 Effect of bed thickness in coated wall reactor

305 In the initial study of coated wall, the bed thickness of each layer was 1 mm. The bed
306 thickness is important and contributes to the conversion of CO₂. The thickness is related with
307 the bed porosity, the reactor's inner diameter and herein fluid's flow rate and velocity. In this
308 section, a comprehensive case study was held combining all these parameters that are affected

309 by the thickness of the catalyst bed for the best performing catalyst (Ni/MPC), and the results
310 are presented in Figure 5. Four, different in thickness, coating layers were investigated, 0.9, 1,
311 1.5 and 2 mm for each layer, with bed porosities of 0.027, 0.115, 0.37 and 0.494, respectively,
312 at 350 °C and catalyst mass of 0.24 g. By reducing the flow rates, it is obtained an improvement
313 in the conversion due to fluid's larger residence time. Moreover, the less thicker the catalyst
314 layer, the higher the conversion. It's also observed that there is an optimum coating layer where
315 the conversion attains a maximum value. By decreasing the thickness of the catalyst bed
316 further, at 0.9 mm, a decrease in conversion was observed when compared to that of the coating
317 layer with 1 mm thickness. This can be attributed to the respective porosities, where in the first
318 case the porosity is very small obstructing the smooth transport of components in the coating
319 area. As can be observed, the coated wall reactor with 1 mm catalyst coating has the optimum
320 layer, with bed porosity of 0.115 and 20 ml/min flow rate reaching 97% conversion of CO₂.



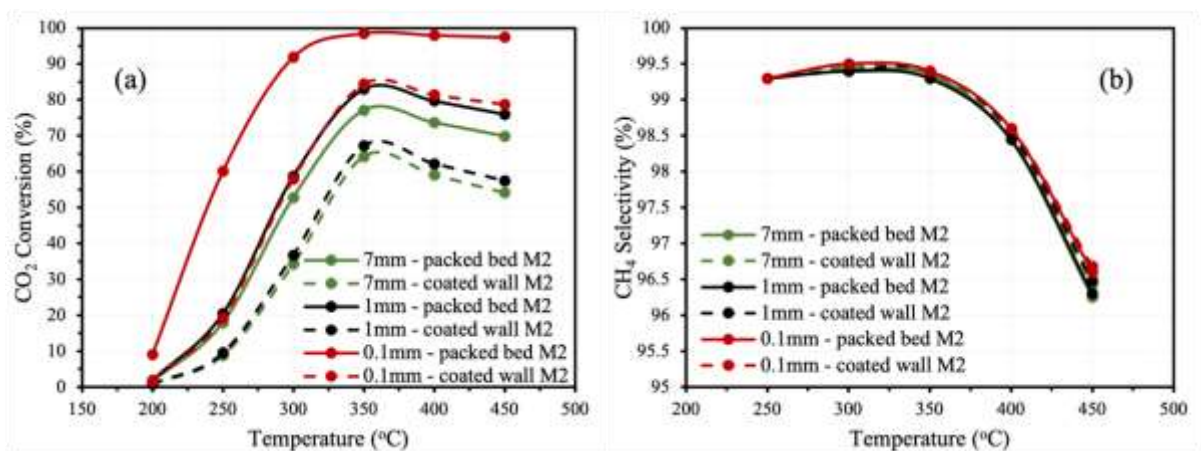
321

322 **Figure 5.** CO₂ Conversion as a function of the weight of catalyst/volumetric flow rate for the
323 Ni/MPC catalyst in coated wall reactor at 350 °C. Thickness of coating layers 0.9, 1, 1.5 and 2
324 mm each and bed porosities of 0.027, 0.115, 0.37 and 0.494, respectively, are presented.

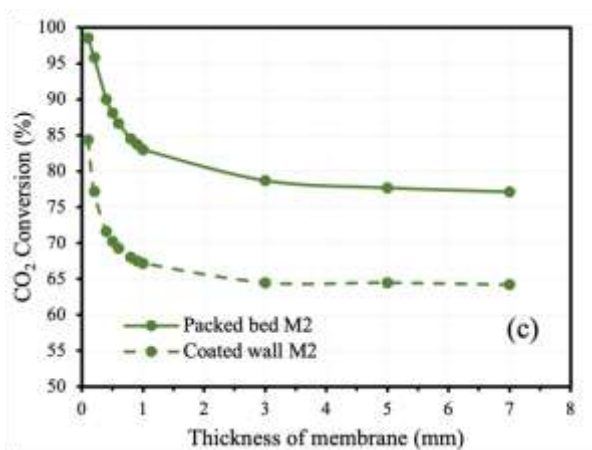
325 3.4 Effect of membrane thickness in packed bed and coated wall reactors

326 The effect of the thickness of the membrane on conversion of CO₂ and selectivity for CH₄
327 is discussed in this section. The initial membrane modeling study that occurred, investigated
328 two membranes, M₁ and M₂, where both had the same thickness of 7 mm. The thickness of the
329 membrane is related with its permeability and herein affects the removal efficiency of the

330 components. In this study, three membrane thickness values were investigated, 7, 1, and 0.1
 331 mm, for the best performing catalyst Ni/MPC, and with all the other parameters remaining
 332 constant. The M₁ membrane didn't show any difference in the results in both configurations
 333 (not shown). This might be attributed to the fact that at 7 mm membrane thickness 100 %
 334 removal of H₂O was already achieved, and that further reduction of membrane thickness didn't
 335 show any difference in the results. In contrast, at the initial study of the M₂ membrane, the CO₂,
 336 H₂ and H₂O removal was not 100 %. Figure 6 shows the conversion and selectivity of CO₂ and
 337 for CH₄, respectively, for the M₂ membrane. By decreasing the thickness of membrane, the
 338 mass transfer coefficient in membrane and flux of the separated components are increased,
 339 which led to better separation. In addition, Le' Chatelier's principle is implemented to restore
 340 the equilibrium and the conversion of CO₂ is increased (Figure 6(a)). As for the selectivity for
 341 CH₄, it can be observed from Figure 6(b) that no significant differences were obtained. Figure
 342 6 (c) shows the conversion of CO₂ for both M₂ membrane configurations as a function of
 343 membrane thickness. Decreasing the membrane thickness from 7 to 1 mm did not significantly
 344 change the conversion while the conversion increase was more obvious for membrane
 345 thickness between 0.1 – 1 mm. By decreasing the membrane thickness, the permeability of
 346 species is tended to increase with more species being removed from the reactor and higher
 347 conversions of CO₂ are obtained according to Le' Chatelier's principle. Packed bed M₂
 348 membrane reactor with 0.1 mm membrane thickness, bed porosity of 0.65 and 100 ml/min flow
 349 rate, had the best performance, with CO₂ conversion of over 98 % with CH₄ selectivity of 99.4
 350 %. The thickness of membranes should be kept minimal within manufacturing possibilities in
 351 order to achieve the maximum separation of components and reduce the manufacturing cost.



352



353

354 **Figure 6.** (a) CO₂ Conversion and (b) CH₄ Selectivity as a function of reactor temperature for
 355 the Ni/MPC catalyst in M₂ packed bed and M₂ coated wall membrane reactors at different
 356 membrane thickness. (c) CO₂ Conversion as a function of membrane thickness for the Ni/MPC
 357 catalyst in M₂ packed bed and M₂ coated wall at 350 °C. Reaction conditions: WHSV = 25,000
 358 ml g_{cat}⁻¹ h⁻¹, bed porosity of packed bed 0.65 and bed porosity of coated wall 0.115.

359 4. Conclusions

360 In this work, four different reactor configurations were investigated and compared based
 361 on their CO₂ methanation catalytic performance. The packed bed reactor, which was initially
 362 investigated in our previous study, displayed a higher CO₂ conversion than the coated wall
 363 reactor, as the residence time of packed bed was higher. Therefore, two different membranes,
 364 M₁ and M₂, which were able to separate solely H₂O (M₁) and CO₂, H₂ and H₂O (M₂), were
 365 included in the modelling. The packed bed membrane reactor showed that the separation of the
 366 reaction components tended to increase the CO₂ conversion, while the coated wall membrane
 367 reactor didn't show any significant difference in results. Additional case studies in the coated
 368 wall reactor of the flow rate effect on the CO₂ conversion showed that at lower flow rates,
 369 higher CO₂ conversion values are achieved. Moreover, the investigation of the bed thickness
 370 in the coated wall reactor revealed that the optimum layer of the catalyst coating was 1 mm
 371 with bed porosity of 0.115 and flow rate of 20 ml/min, where 97% CO₂ conversion was
 372 reached. As for the membrane thickness in both membrane reactor configurations, it was shown
 373 that there was no impact on CO₂ conversion for the M₁ membrane, while for the M₂ membrane,
 374 its reduction improved the CO₂ conversion. It was revealed that the packed bed M₂ membrane
 375 reactor with 0.1 mm membrane thickness, bed porosity of 0.65 and 100 ml/min flow rate had
 376 the best performance, reaching CO₂ conversion of over 98 % and CH₄ selectivity of 99.4 %.

377 The study of 3D CFD models regarding the CO₂ methanation reaction using all the same
378 simulation constants and parameters that were used in this study will be performed in a future
379 work as well as the examination of the veritableness of the performance of each reactor.
380 Moreover, the comparison between different kinetic rates for the CO₂ methanation reaction
381 will be performed to obtain substantial results. These fundamental findings may help develop
382 new or improve already existing reactor configurations to further enhance the methanation
383 reaction's performance.

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