

Discovery of X-ray polarization angle rotation in active galaxy Mrk 421

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Abstract

The magnetic field conditions in astrophysical relativistic jets can be probed by multiwavelength polarimetry, which has been recently extended to X-rays. For example, one can track how the magnetic field changes in the flow of the radiating particles by observing rotations of the electric vector position angle Ψ . Here we report the discovery of a $\Psi_{\mathbf{x}}$ rotation in the X-ray band in the blazar Mrk 421 at an average flux state. Across the 5 days of Imaging X-ray Polarimetry Explorer (IXPE) observations of 4-6 and 7-9 June 2022, $\Psi_{\mathbf{x}}$ rotated in total by $\geq 360^\circ$. Over the two respective date ranges, we find constant, within uncertainties, rotation rates (80 ± 9 and $91 \pm 8^\circ/\text{day}$) and polarization degrees ($\Pi_{\mathbf{x}} = 10\% \pm 1\%$). Simulations of a random walk of the polarization vector indicate that it is unlikely that such rotation(s) are produced by a stochastic process. The X-ray emitting site does not completely overlap the radio/infrared/optical emission sites, as no similar rotation of Ψ was observed in quasi-simultaneous data at longer wavelengths. We propose that the observed rotation was caused by a helical magnetic structure in the jet, illuminated in the X-rays by a localized shock propagating along this helix. The optically emitting region likely lies in a sheath surrounding an inner spine where the X-ray radiation is released.

1 Introduction

Despite decades of effort, the physical processes shaping the dynamics and emission of relativistic jets are in large part still unclear (e.g. [1]). However, in the last decade, several important clues have been obtained thanks to new facilities that allow the possibility of following in detail the time-variable emission properties of jets, especially at high photon energies. A similar leap is now expected from the newly-opened window of X-ray polarimetry, which provides us with an unprecedented view of the physical sites of particle acceleration and emission.

Blazars, whose relativistic jets point close to the Earth, provide excellent laboratories to investigate the physics of jets and test current theoretical

ideas (e.g. [2]). Among blazars, the so-called high-peaked BL Lac objects (HBLs), whose synchrotron and Compton components peak in the X-ray and very-high-energy γ -ray band, respectively, are the ideal sources to investigate acceleration and cooling processes acting on ultra-relativistic electrons (with Lorentz factors $\gamma \gtrsim 10^6$). From the theoretical point of view, the main mechanisms advocated for the energization of particles in relativistic jets are diffusive shock acceleration (DSA; e.g., [3]), magnetic reconnection (e.g., [4]), possibly triggered by instabilities (e.g., [5]) or specific anti-parallel magnetic field structures [6], or reconnection plus stochastic acceleration in relativistic turbulence in a highly magnetized plasma (e.g., [7]).

Polarimetry is a powerful tool that can break the degeneracies involved in the modeling of the spectral energy distribution (SED) and gain insight into the magnetic field and emission region geometry [8]. Recent theoretical efforts have allowed us to identify polarimetric signatures expected under different scenarios of blazar emission regions that can be contrasted with observational evidence. Polarimetric measurements are very sensitive to the geometrical structure of the magnetic field permeating the flow and to its global properties (e.g., chaotic vs. globally ordered). In particular, the evidence for systematic and large variations of the polarization angle, potentially associated with powerful γ -ray flares (e.g., [9, 10]), has been interpreted in terms of a helically twisted jet (e.g., [11]), an emission region moving along helical field lines that propagate down the jet (e.g., [12–14]), or light-travel delays when a shock forms in a jet with a predominantly helical/toroidal field [15, 16]. Such a structure for the global field is supported by (spatially resolved) polarimetric studies of parsec-scale jets in the radio band [17, 18]. Interaction between a moving and a stationary shock can also produce large rotations [e.g., 19]. An alternative explanation is that the polarization behavior is stochastic, related to turbulence in the flow [20, 21], possibly combined with a standing shock [22, 23]. In this framework, the observed polarimetric parameters do not carry any direct information on the structure of the magnetic field in the jet, since they are mainly related to the turbulent nature of the flow. Turbulence can play an important role even if an average ordered magnetic field is present. In this case, while the polarization angle can display rotations related to the effect of the ordered field, the overall level of polarization can be decreased by the depolarizing effect of turbulence (e.g., [24, 25]).

Mrk 421 is a nearby (redshift $z = 0.0308$) HBL that has been intensively studied at many wavelengths (e.g., [26]). It is among the first blazars detected at both GeV (by EGRET onboard the *Compton* Gamma Ray Observatory; [27]) and TeV energies (by the Whipple Observatory; [28]). It is bright and well-monitored in the X-ray band (e.g., [29, 30]), where the synchrotron SED peaks at a high flux level, making it a prime target for linear polarization observations by IXPE.

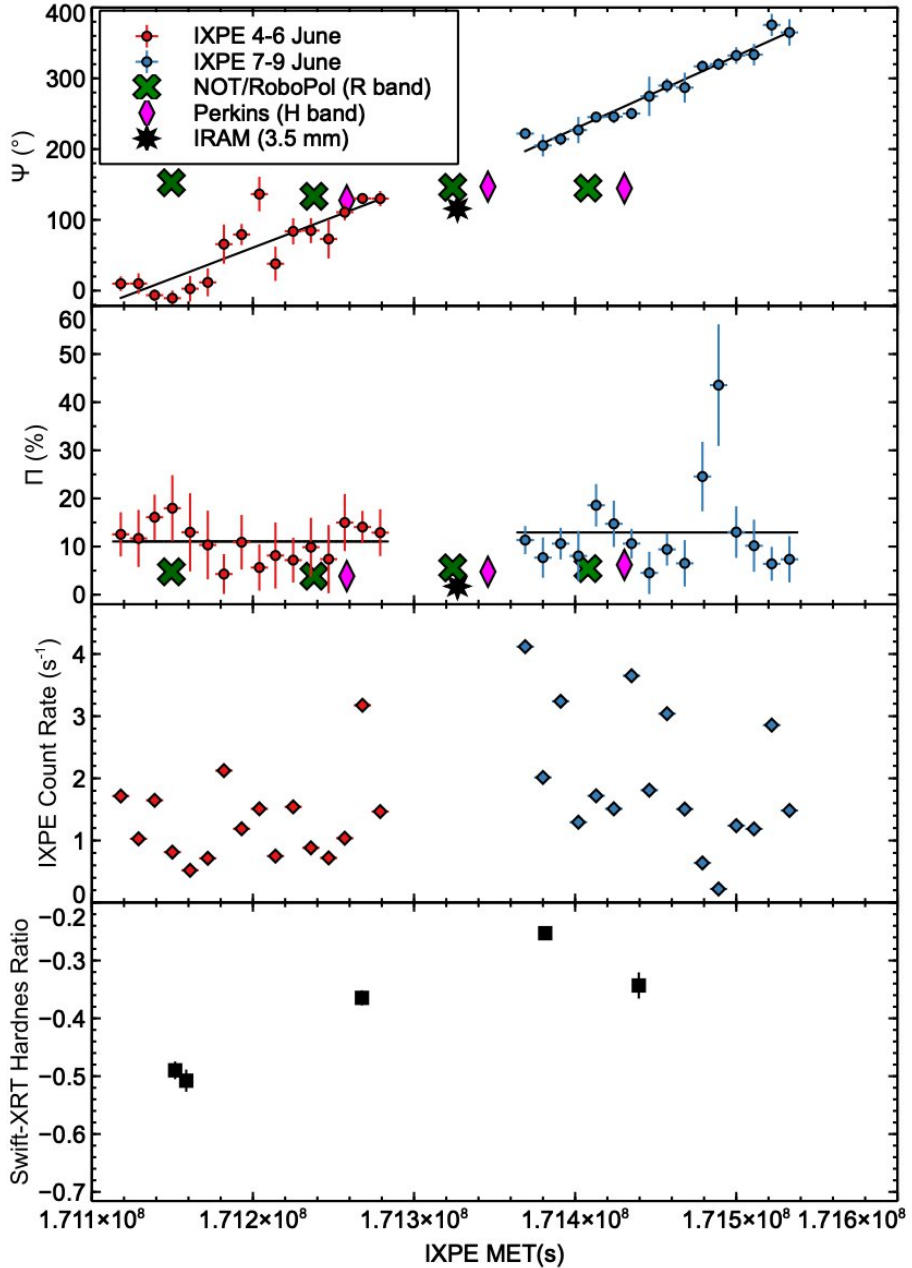


Fig. 1 From top to bottom: time evolution of the X-ray polarization angle, degree, IXPE photon count rate in time bins of ~ 3 hours within the IXPE pointings of 4 June (red diamonds) and 7 June (blue diamonds) 2022, and hardness ratio in the X-ray band (black squares) measured with Swift-XRT. As a comparison, we display the polarization properties from simultaneous radio (IRAM: black stars), infrared (Perkins: magenta diamonds), and optical observations (NOT/RoboPol: green crosses).

2 Results

In the first year of IXPE operation, we observed the blazar Mrk 421 three times (on 4 May, 4 June, and 7 June 2022) to search for multi-epoch variability of the X-ray polarization properties. In this case, a single IXPE pointing extends over ~ 2 days, which permits a search for intra-day variations of the polarization properties as well [25]. The IXPE observations were complemented with radio-millimetre [Very Long Baseline Array (VLBA), Institut de Radioastronomie Millimétrique (IRAM) and the SubMillimeter Array (SMA)], infrared (KANATA, Perkins Telescope), and optical polarization measurements [KANATA, Nordic Optical Telescope, Observatorio de Sierra Nevada (OSN), and Skinakas Observatory], as detailed in Table 1 and displayed in Figures 1 and 5. We captured the source in an average activity state relative to its flux history (see **Methods**), discounting occasional major, multi-band outbursts [31].

In May 2022, Mrk 421 was significantly X-ray polarized (with a polarization degree $\Pi_x \sim 15\%$ at a position angle $\Psi_x \sim 35^\circ$) and did not exhibit any substantial variability of the X-ray polarization properties within the IXPE pointing [32]. This is consistent with the X-ray polarization of Mrk 501, the other prototypical HBL observed by IXPE [33]. In both cases, the X-ray polarization degree was larger than at radio, infrared, and optical wavelengths. This suggested that the X-rays are produced by rapidly cooling, high-energy electrons accelerated at a shock, while the emission at longer wavelengths is emitted in a larger, downstream region containing a more disordered magnetic field and lower-energy electrons at increased distances from the shock.

In contrast, during two subsequent IXPE observations in June 2022, the X-ray polarization was undetected in the time-averaged IXPE data (see **Methods** section). In these observations, the X-ray flux was twice as high as in May 2022 ($\sim 1.5 \times 10^{-10}$ and $\sim 3.02 \times 10^{-10}$ erg s⁻¹ cm⁻² in the 2-8 keV IXPE band on 4-6 June and 7-9 June, respectively). A similar increase in flux (by a factor of ~ 1.2 ; see Table 1 and Fig. 5) was also measured in the radio (IRAM), infrared (Perkins), and optical (NOT) data between 4-5 May and 6-7 June 2022.

When measured over shorter time intervals of the IXPE observations of June 2022 (Fig. 1), the X-ray polarization angle varied significantly in a manner consistent with a smooth rotation, as often observed for blazars in the optical band [e.g., 34–38]. For example, on 4–6 June the X-ray polarization angle Ψ_x varied from $9^\circ \pm 1^\circ$ at the beginning of the IXPE pointing to $130^\circ \pm 11^\circ$ at the end of the observation, while on June 7–9 Ψ_x changed from $222^\circ \pm 7^\circ$ to $360^\circ \pm 20^\circ$ (considering time bins of ~ 3 hours, as in Fig. 1). We adopt a simple model where the polarization angle rotates at a constant rate, while the polarization degree remains constant, to test the hypothesis that a polarization angle rotation caused canceling of the polarization degree in

the time-averaged data. Using a maximum-likelihood method, a fit of binned Stokes parameter time-series, and a fit in the Q-U plane (see Methods section), three independent analyses by subsets of the authors support this hypothesis. The data of 4-6 June are consistent with a rotation rate $\dot{\Psi}_X$ of $80 \pm 9^\circ/\text{day}$ at constant $\Pi = 10\% \pm 1\%$, while for the data of 7-9 June the parameters are $\dot{\Psi}_X = 91 \pm 8^\circ/\text{day}$ and $\Pi_X = 10\% \pm 1\%$. Our analysis suggests that both Π_X and $\dot{\Psi}_X$ probably varied somewhat with time about the above average values.

While the X-ray polarization angle was rotating, the millimetre-wave, infrared, and optical polarization angles did not vary substantially (Fig. 1). In the VLBA images of the radio core of 5 June (see Methods), some fanning out of the polarization vectors on the southeast side of the the core is apparent, which indicates an azimuthal component to the magnetic field, as one would expect if that component were helical. In the optical, the scatter of Ψ_O during the June IXPE observations is $\sim 20^\circ$, with no significant trend. Given the gaps in the optical observations, and considering the intrinsic 180° ambiguity, it is possible that a poorly sampled rapid rotation occurred. However, no straightforward scenario makes all the radio/infrared/optical data points consistent with the time series of the X-ray polarization angle. Therefore, we conclude that polarization angle rotation at the longer wavelengths was either absent or proceeded at a different rate compared to the X-ray band. Simultaneously with the polarization angle rotation, the X-ray spectrum changed significantly (see Fig. 1, bottom panel, and Methods section). Swift X-ray Telescope (XRT) data taken over the same time frame as the IXPE pointing show that the flux in the 2.0-10.0 keV band increased by a factor of ~ 3 , while in the 0.3-2.0 band the increase in flux was by a factor of ~ 1.2 . The maximum flux was recorded by the Swift-XRT in correspondence with the beginning of the second IXPE pointing. Then, by the end of the IXPE observation, the source brightness relaxed back to the same level as in the beginning. The spectral shape also changed in a harder-when-brighter fashion, with the brightest point corresponding to the flattest (hardest) spectrum. In contrast, in May 2022 the X-ray flux during the IXPE pointing changed in a similar fashion, but with no change in X-ray spectral shape or polarization angle [32]. At $\sim \text{GeV}$ γ -ray energies, Mrk 421 was in a quiescent state during the IXPE pointing: the Fermi Large Area Telescope (LAT) [39] observed minor activity in the 6-month period around the IXPE observations, never reaching more than twice the average catalog flux (see fig. 3).

3 Discussion

Virtually all of the processes shaping the dynamics of particles in blazar jets predict specific characteristics of variability of the optical-to-X-ray polarization properties [40], which we can compare against our observations of

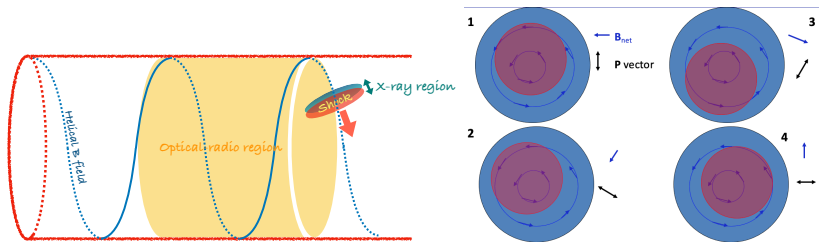


Fig. 2 Sketches of the scenario proposed to explain the X-ray polarization angle rotation in Mrk 421. Left: an off axis emission feature, e.g., a magnetosonic shock, propagates along helical magnetic field lines down the jet. Right: the appearance of the emission feature, magnetic field, and polarization vector at 4 azimuthal positions along its spiral path as viewed by a distant observer aligned with the jet. The red circle represents the emission feature, while the blue-shaded region is the ambient jet.

Mrk 421. Our basic finding conforms to the scenario of an energy-stratified jet, as discussed above for Mrk 421 in May 2022 and for Mrk 501. We find that the roughly constant value of Π_X , while the polarization angle was rotating, is higher than Π_O , Π_{IR} , and Π_R , and similar to the level observed at non-rotating epochs. In addition, simultaneous radio, infrared, and optical polarization measurements do not show evidence of a similar polarization angle rotation. Due to the limited sampling and intrinsic 180° ambiguity, we cannot exclude the possibility that the optical polarization angle was rotating at some level. However, we consider a rotation of the optical polarization angle at the same rate as the X-ray polarization angle unlikely. Indeed, typical optical polarization rotation rates of blazars vary between a few and a few tens of degrees per day [41], in contrast to the $\sim 85^\circ/\text{day}$ that we estimated in the X-ray. The optical rotation rates may be higher during bright outbursts associated with the passage of knots through the radio core [19, 42]. No such outburst was recorded for Mrk 421 at the time of the IXPE pointings. Moreover, no solution of the 180° ambiguity can completely reconcile the radio/optical/infrared polarization angle time series with the X-ray curve. Therefore, as the polarization angle was likely not rotating (or rotating in a different way) at longer wavelengths, we suggest that the radio/infrared/optical emission sites are, at most, only partially co-spatial with the X-ray emission region.

In an energy-stratified jet, the X-rays are emitted closer to the site of acceleration of the particles, while the lower-energy particles emitting at radio to optical wavelengths span a larger region downstream owing to their longer radiative cooling times (e.g., [33]). Acceleration of electrons by a shock can explain the high X-ray polarization, since the shock front partially aligns a previously disordered magnetic field (e.g., [43, 44]). The harder-when-brighter spectral behavior that Mrk 421 displayed while the X-ray polarization angle was rotating is also expected within the shock scenario [45].

The energy stratification of the particles in the jet can be either linear, in the downstream direction, or radial, in the case of a structured jet [46–48],

including an inner fast spine surrounded by a slower sheath. Such a spine-sheath jet explains, for example, the limb-brightening morphology that has been reported in very long-baseline interferometry (VLBI) radio maps of HBLs, including Mrk 421 [49, 50]. In the first case, the turbulent component of the magnetic field could become increasingly dominant over the ordered component with distance from the shock [51]. In the second case, turbulence may prevail in the sheath. In both these frameworks, the particle-energy stratification would lead to lower polarization of the optical, infrared, and radio emission. Detailed modeling of the variability of flux and polarization induced by turbulence predicts erratic variability, as seen in the past at optical wavelengths in Mrk 421 [51], which may by chance result in an apparent rotation of the polarization angle [22]. However, such apparent rotations are highly unlikely to explain, for example, the systematic rotations of the optical polarization angle in BL Lac and PKS 1510–089 [34, 35]. This has led to the proposal that these events occurred upstream of the most turbulent region of the jet. In a larger study of a number of optical-band rotation events in a sample of blazars, it was found that a random walk of the polarization vector cannot reproduce the majority of the observed properties of the population [9, 52].

We have investigated whether the rotation of the polarization vector in Mrk 421 could be produced through random walks of the polarization angle by comparing the observations against simulated polarization light curves, following [52, 53] (see Methods). We consider two scenarios: either the rotations in the observations of 4–6 June and 7–9 June are independent events, or they are part of a single long rotation that spanned seven days, of which we observed two segments separated by a one-day gap. In either scenario, we find, under the most favorable conditions, that only about 2% of the simulated curves of $\dot{\Psi}_X$ and Π_X vs. time are consistent with the observations. For the second scenario, if the rotation were actually longer than 7 days, the fraction of simulation trials that reproduce the observed properties would decrease. This suggests that it is unlikely that the observed behavior can be attributed to random variations of the polarization angle, and instead points to a coherent, deterministic process responsible for the observed rotation(s).

Magnetic reconnection episodes, which can result from the development of a large-scale kink instability [54] or current sheet [55], may also cause rapid polarization angle swings. These could be associated with γ -ray flares [56] or quasi-periodic oscillations of the source flux [57, 58]. In our case, we did not witness any such oscillations or γ -ray flare while the polarization angle was rotating. Moreover, in contrast to our observations of Mrk 421, simulations of magnetic reconnection often display, on average, a similar level of polarization degree in the X-ray and in the optical [25]. In some cases, the X-ray polarization degree can also be much lower than the optical because of time averaging of the polarization vector, which is the opposite of what is observed [25].

A specific model for deterministic polarization angle rotation involves an off-axis emission feature, such as a magnetosonic shock, propagating toward the observer and down a helical magnetic field [11, 13, 14, 16]. The observed rotation rate is determined by the time required for the feature to execute an orbit around the jet axis, modulated by light-travel delays and possibly other relativistic effects [59]. We display sketches of this scenario in Fig. 2, both in the reference frame of the host galaxy (left panel) and as seen by an observer whose line of sight is along the jet axis (right panel).

As a quantitative example of such a model, we find that we can reproduce the observed rotation rate $\dot{\Psi}_X \sim 85^\circ/\text{day}$ over 5 days if (1) the center of the emission feature is displaced by $2 - 4 \times 10^{16}$ cm from the jet axis (for an angle to the line of sight ranging from 4° to 0°), and (2) moves at a velocity of $0.99875c$ (Lorentz factor of 20), with a component parallel to the jet axis of $0.9975c$ and a transverse, rotational component of $0.05c$. During the rotation, the feature moves through a distance between 0.8 and 1.7 pc (depending on the line-of-sight angle) parallel to the line of sight in the observer's frame.

If the jet is structured, the helical field component may be limited to the spine. Moreover, the spine can also contribute somewhat to the emission at longer wavelengths. This would lead to different polarization behaviour in X-ray than at longer wavelengths, and, at the same time, can explain a possible rotation of the optical polarization angle and the similarities in the variability of the X-ray to millimetre fluxes on longer time-scales (i.e., between May and June 2022).

The discovery of X-ray polarization angle rotation in HBLs, made possible by the new capability of IXPE, opens up the possibility of fully investigating analogies and differences between polarization angle rotations at different frequencies and for different classes of blazars. For example, [60] discuss a version of the model in which the polarization angle rotations occur immediately downstream of a shock, where the compressed magnetic field is dominated by an ordered (helical) magnetic field superposed on a turbulent component. As the shock is the site of acceleration of the particles that radiate at the frequency of the peak of the synchrotron SED, the highest polarization and main rotation events should be observed near that frequency. This argument has been invoked to explain why optical polarization angle rotations preferably occur in low-synchrotron-peak (LSP) blazars [61], and naturally predicts a more frequent occurrence of X-ray polarization angle rotations in the case of HBLs. In the same speculative framework, as optical polarization angle rotations are often correlated with $\sim\text{GeV}$ γ -ray flares [37], X-ray polarization angle rotations should be accompanied by $\sim\text{TeV}$ activity, which is, in the case of HBLs, the analog of $\sim\text{GeV}$ activity for LSPs.

In conclusion, this first study of X-ray polarization angle rotation in HBLs in a multi-wavelength framework shows how the availability of the X-ray polarization diagnostic enriches our ability to probe the magnetic field geometry and particle acceleration in different regions of relativistic jets, and thereby represents a new, fundamental step towards a comprehensive view of relativistic astrophysical jets.

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Competing interest. The authors declare that they have no competing interests.

Data availability. The data that support the findings of this study are freely available in the HEASARC IXPE Data Archive (<https://heasarc.gsfc.nasa.gov/docs/ixpe/archive/>). The multiwavelength data are available on request from the individual observatories.

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Methods

IXPE and multi-wavelength data

IXPE data

The log of all of our observations of Mrk 421 in May–June 2022, including radio/millimetre, optical, infrared, and X-ray polarization measurements, along with Swift monitoring in the X-ray band, is listed in Table 1 and 2. Here we report the analysis of the second and third IXPE observations of

Mrk 421 that were performed from 11:20 UTC on 4 June 2022 to 11:00 UTC on 6 June (hereafter Obs. 2), and from 09:00 UTC on 7 June to 11:10 UTC on 9 June (hereafter Obs. 3). The livetimes for these pointings are ~ 96 ks and ~ 86 ks, respectively.

The raw IXPE data were processed using a standard pipeline¹ that estimates the photo-electron emission direction, correcting for charging effects, detector temperature, Gas Electron Multiplier (GEM) gain non-uniformity, and instrumental spurious modulation [62]. The level-2 event files (one for each of the three detector units (DU) on-board IXPE) from the pipeline contain all the information typical of an imaging X-ray astronomy mission (e.g., photon arrival time, detector coordinates, and energy), with the addition of the polarization information in the form of event-by-event Stokes parameters. Before proceeding with the scientific analysis, when necessary, we adjusted the data for small time-dependent changes to the gain correction obtained from data taken with the on-board calibration sources close to the actual time of observation [63].

We performed the scientific analysis of the IXPE data using the *ixpeobssim* software [64, 65]. At the angular resolution of IXPE ($\sim 30''$), blazars like Mrk 421 are point-like sources. Using the *xpselect* tool, we selected the source events using a circular $60''$ radius region, while we used an annulus centered on the source (with inner and outer radii of $2.5'$ and $5.0'$) to estimate the background. Within the *ixpeobssim* suite, the method of [66] for estimating the polarization of a set of events is implemented in the PCUBE algorithm. We created the Stokes-parameter spectra of the source, using the PHA1, PHAQ, PHAU algorithms. The PHA1, PHAQ, and PHAU algorithms map the I , Q , and U Stokes parameters of the photons into OGIP-compliant PHA spectral files (3 Stokes-parameter spectra per 3 detector units). We prepared the spectra for the spectro-polarimetric fit by binning the I spectrum, requiring a minimum of 30 counts in each energy bin, as needed for the χ^2 statistics in the fits. Finally, we binned the Q and U spectra by grouping the channels by a constant factor of 10. To search for variability of the flux and polarization properties within the time span of the IXPE pointings, we created light curves with different time binning, using the LC algorithm in *ixpeobssim*. We applied the time binning of these light-curves to time-slice each of the event files and computed a PCUBE in each time interval. We thereby created light curves of the polarization properties as a function of time, including normalized Stokes parameters ($q(t), u(t)$), polarization degree ($\Pi(t)$), and polarization angle ($\Psi(t)$).

We applied to the $\Psi(t)$ light-curves a standard procedure [36] to solve the 180° ambiguity of Ψ . By assuming that temporal variations of Ψ are

¹<https://heasarc.gsfc.nasa.gov/docs/ixpe/analysis/IXPE-SOC-DOC-009-UserGuide-Software.pdf>

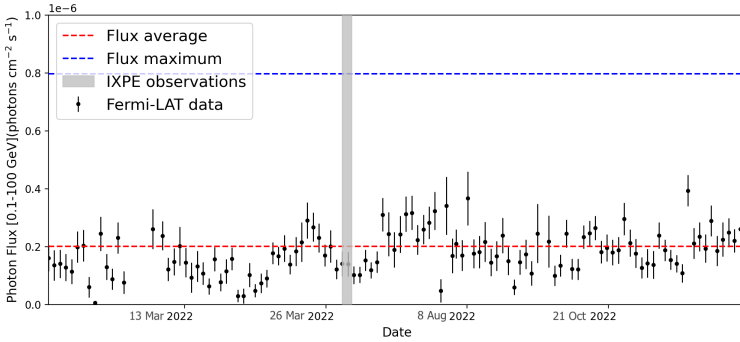


Fig. 3 Fermi-LAT light curve of Mrk 421, integrated over the 0.1 – 100 GeV energy range. The gray band illustrates the time range of the two IXPE observations of Mrk 421 discussed in this work. The red dashed line indicates the average photon flux of Mrk 421 over the LAT mission duration, while the blue solid line marks the highest photon flux recorded by the LAT, which corresponds to the Mrk 421 flare of 2012. The plots include only points for which the test statistic for source detection is above 9.

gradual, we minimized the variation $\Delta_n \Psi$ between consecutive points Ψ_n and Ψ_{n+1} as follows. For two consecutive data points $\Delta_n \Psi$ was defined as $|\Psi_{n+1} - \Psi_n| - \sqrt{\sigma^2(\Psi_{n+1}) + \sigma^2(\Psi_n)}$, where $\sigma(\Psi_{n+1})$ and $\sigma(\Psi_n)$ are the errors for the consecutive angles considered. If $\Delta_n \Psi$ was larger than 90° , we shifted Ψ_{n+1} by multiples of $\pm 180^\circ$ as needed to minimize $\Delta_n \Psi$. Otherwise, when $\Delta_n \leq 90^\circ$, we left Ψ_{n+1} unshifted. This procedure serves only for clarity of displaying the data, and is not critical for our estimation of the rotation rate, which was performed using unbinned event data or Stokes-parameter time series (see below).

γ -ray data

We studied the γ -ray activity of Mrk 421, analyzing data collected with the *Fermi*-LAT in the energy range 0.1-100 GeV. We made use of the 3-day cadence light curve (within the years 2021 and 2022), which was extracted from the LAT Light Curve Repository (LCR), as displayed in Figure 3. We refer to [67] for the detailed description of the unbinned maximum-likelihood data analysis. For this work, we adopted the light curve that was obtained using the option of leaving the spectral slope free to vary in the fit.

X-ray flux and continuum spectrum

We monitored the X-ray (0.3-10.0 keV) flux and spectral variations of Mrk 421 both near the time of, and simultaneously with, the IXPE pointings of May-June 2022 using the Neil Gehrels Swift X-Ray Telescope (XRT) (Table 2). The Swift-XRT observations each had an exposure time of ~ 1 ks and were performed in Windowed Timing (WT) mode. The data were processed using the XRT Data Analysis Software (XRTDAS, v. 3.6.1). In the analysis, we

used the latest calibration files available in the *Swift*-XRT CALDB (version 20210915). The X-ray source spectrum was extracted from the cleaned event file using a circular region with a radius of $47''$. The background was extracted using a circular region with the same radius from a blank sky WT observation available in the *Swift* archive. As a final step, we binned the 0.3-10 keV data to achieve at least 25 counts in each energy bin.

For our spectral analysis, we used the Xspec program [68]. In all our fits we included Galactic absorption along the line of sight ($N_{\text{H}} = 1.34 \times 10^{20} \text{ cm}^{-2}$; [69]) using the TBABS model, with Fe abundances set according to [70]. For all the datasets, we found that a log-parabolic model, where the photon index varies as a log-parabola in energy (i.e., $N(E) = K(E/E_{\text{p}})^{(\alpha - \beta \log(E/E_{\text{p}}))}$ [71]), fits the spectra better than a simple power law (with $\Delta\chi^2$ in the range between -23 and -233, for one additional degree of freedom). In the log-parabolic model, the pivot energy E_{p} is a scaling factor, α is the spectral slope at the pivot energy, β corresponds to the spectral curvature, and K is a normalization constant. In our fits, we set the pivot E_{p} to 5.0 keV [32, 72], so that α approximates the photon index in the 3.0-7.0 keV range. In this way, we extracted the X-ray spectral evolution of Mrk 421 in May/June 2022 (Fig. 4), including soft (S band: 0.3-2.0 keV) and hard (H band: 2.0-10.0 keV) X-ray fluxes, hardness ratio (H-S/H+S), and α and β parameters.

Within the IXPE pointing of May 2022, the X-ray flux rose by a factor of ~ 2 with no significant change in spectral shape [32]. Conversely, during the two IXPE pointings of June 2022, the flux increased from $\sim 7.5 \times 10^{-10} \text{ erg s}^{-1} \text{ cm}^{-2}$ at the beginning of Obs. 2 to the brightest point of $\sim 1.4 \times 10^{-9} \text{ erg s}^{-1} \text{ cm}^{-2}$ at the beginning of Obs. 3, and then decreased back to the previous level. The maximum variation of the soft flux was by a factor of ~ 1.2 , while the hard flux varied by a factor of ~ 3 . This is in agreement with the IXPE measurement in the 2.0-8.0 keV band, where the flux of Obs. 3 was \sim twice as high as during Obs. 2 (see Table 1). Therefore, the spectrum became harder and flatter (i.e., α decreased while the hardness ratio increased), with the flattest spectral shape coinciding with the brightest point.

Optical & infrared data

All the optical, infrared, and radio/millimetre polarization measurements of Mrk 421 in the time frame as the IXPE pointings are displayed in Fig. 5. Polarization observations in the optical were performed simultaneously with the IXPE pointings using the Hiroshima Optical and Near-InfraRed camera (HONIR) at the KANATA telescope, RoboPol at the Skinakas observatory 1.3-m telescope [73], the Alhambra Faint Object Spectrograph and Camera (ALFOSC) mounted at the 2.5m Nordic Optical Telescope (NOT), and the T90 telescope at the Sierra Nevada Observatory (SNO) during May/June 2022 in the R-band ($\lambda=6500\text{\AA}/E=1.9 \text{ eV}$, $FWHM=1300 \text{\AA}/0.4 \text{ eV}$). The

HONIR observations were performed in three optical bands². The Stokes parameters are estimated by rotating the half-wave plate to four positions angles and combining the exposures. The instrument and data analysis are described in detail in [74, 75]. RoboPol is a novel 4-channel opto-polarimeter with no moving parts and with the ability to measure the normalized Stokes q and u parameters with a single exposure simultaneously. A detailed description of the semi-automated analysis and data reduction pipeline can be found in [38, 76]. The NOT data were reduced using the pipeline developed at the Tuorla Observatory, which follows standard photometric procedures [77, 78]. We performed the SNO observations with polarized R_c filters, and calibrated the data using polarized and unpolarized standard stars. For the RoboPol, HONIR, and NOT observations in the R-band, we corrected for the host-galaxy depolarization by subtracting the (presumed unpolarized) host-galaxy flux density estimated for the individual apertures used in each observation [79]: $\Pi_{\text{intr}} = \Pi_{\text{obs}} \times I / (I - I_{\text{host}})$, where Π_{intr} and Π_{obs} are the intrinsic and observed polarization degree, respectively, I is the total flux density in mJy, and I_{host} is the host-galaxy flux density in mJy for the aperture of the observation [77].

The IR observations were performed in H-band with the 1.8m Boston University Perkins telescope (Flagstaff, AZ) using the IR camera MIMIR in May/June 2022, supplemented by H-band HONIR observations in May 2022. The MIMIR instrument and data reduction procedures are described in detail in [80]. The Perkins H-band observations were corrected for the host-galaxy contribution following the prescription above. To find the contribution of the host galaxy for the aperture necessary for the correction, we performed a photometric decomposition of the galaxy light using the IMFIT package [81]. The model for the image decomposition consisted of a Sersic profile for the host galaxy plus a point source for the blazar, determined by fitting a Moffat function [82] to several isolated stars in the image to create an average point-source function. We determined the parameters of the host galaxy as $n = 1.18 \pm 0.35$ for the Sersic index, an ellipticity of $e = 0.238 \pm 0.03$, an effective radius of $r_e = 2.1'' \pm 0.14''$, and a surface brightness of $\mu_e = 16.59 \pm 0.17$. For the average aperture diameter of $5.2''$ used for the polarization observations, we estimated the contribution of the host-galaxy to be 12.41 ± 0.06 mag. Any additional infrared observations have not been corrected for the host-galaxy contribution, and hence should be considered as lower limits to the intrinsic polarization degree. All the optical/infrared observations are listed in Table 1.

Radio/millimetre data

Images of Mrk 421 at 7 mm wavelength with a resolution of ~ 0.2 milliarcseconds (mas), corresponding to 0.12 pc, were produced with data from Very Long Baseline Array (VLBA) observations at epochs 30 April, 5 June, and 24 June 2022. The observations were from the Blazars Entering

²<http://hasc.hiroshima-u.ac.jp/instruments/honir/filters-e.html>

the Astrophysical Multi-Messenger Era (BEAM-ME) program (see website www.bu.edu/blazars/BEAM-ME.html). The data acquisition and analysis are described in [83]. Figure 6 presents the images, in which total intensity is indicated by contours, polarized intensity by colour coding, and polarization direction by yellow line segments. (Note that the 30 April image has lower dynamic range than the others, hence the jet is not as apparent.) The images reveal a change in the polarization direction of the “core” (feature of peak intensity) between 30 April and the June epochs. The 5 June image exhibits some fanning out of the polarization vectors on the southeast side of the core, indicating an azimuthal component to the magnetic field, as one would expect if that component were helical. However, at the location of the 7 mm core, this component is weak relative to a more randomly oriented magnetic field component.

Polarization at the shorter wavelengths of 3.5 mm (86.24 GHz) and 1.3 mm (230 GHz) was measured with the 30 m Telescope of the Institut de Radioastronomie Millimétrique (IRAM), located at the Pico Veleta Observatory (Sierra Nevada, Granada, Spain), on several nights in May/June 2022, as listed in Table 1. The observations were obtained within the Polarimetric Monitoring of AGN at Millimetre Wavelengths (POLAMI) program [84, 85] following the reduction and calibration pipeline described in detail in [84].

No significant polarization at 1.3 mm from Mrk 421 was detected by IRAM either in May or June 2022, with an upper limit (at a confidence level of 95%) of $< 6\%$ and $< 4\%$, respectively. The early May 3.5 mm observations are consistent within uncertainties with an average $\Pi_R = 3.4 \pm 0.7\%$ at an average $\psi_R = 54.5 \pm 6^\circ$. The 30 May 2022 observation shows an increase in the polarization degree to $\Pi_R = 7.9 \pm 0.9$, with a polarization angle almost perpendicular to the early May observations ($\psi = 128 \pm 2.4^\circ$). The subsequent observation shows a similar Π_R to the early May observations ($1.76 \pm 0.6\%$) at a roughly consistent angle of $\psi = 116 \pm 9^\circ$. We obtained additional observations at 1.3 mm (225.538 GHz) using the Submillimeter Array (SMA) [86] within the SMAPOL (SMA Monitoring of AGNs with POLarization) program. SMAPOL follows the polarization evolution of 40 γ -ray bright blazars, including Mrk 421, on a bi-weekly cadence, as well as other sources in a target-of-opportunity (ToO) mode, including objects observed by IXPE. The Mrk 421 observations reported here were conducted on 4 June and 16 June 2022. The SMA observations employed two orthogonally polarized receivers, tuned to the same frequency range in full polarization mode, and used the SWARM correlator [87]. These receivers are inherently linearly polarized, but are converted to circular polarization by using the quarter-wave plates of the SMA polarimeter [88]. The lower sideband (LSB) and upper sideband (USB) covered 209-221 and 229-241 GHz, respectively. Each sideband was divided into six sub-bands with bandwidths of 2 GHz and a fixed channel width of 140

kHz. The SMA data were calibrated with the MIR software package³. Instrumental polarization leakage was calibrated independently for USB and LSB using the MIRIAD task `gpcal` [89] and removed from the data. The polarized intensity, position angle, and percentage were derived from the Stokes I, Q, and U visibilities. Between 4 and 16 June 2022, Mrk 421 decreased slightly in total flux, with values of 0.20 ± 0.02 Jy and 0.14 ± 0.02 Jy on 4 and 16 June, respectively. The linear polarization remained stable within the uncertainties between the two epochs, with a linear polarization degree of $2.3 \pm 0.2\%$ and $2.3 \pm 0.3\%$ and a polarization angle of $129.6 \pm 2.6^\circ$ and $132.6 \pm 3.9^\circ$ on 4 and 16 June, respectively. MWC 349 A was used for the total flux calibration, and the calibrator 3C 286, which has a high linear polarization degree and stable polarization angle, was observed in both sessions as a cross-check of the polarization calibration.

X-ray Polarization Analysis

Time-averaged IXPE data

The analysis of the first IXPE observation of Mrk 421, which discovered an X-ray polarization $\Pi_X = 15\% \pm 2\%$ at a polarization angle $\Psi_X = 35^\circ \pm 4^\circ$, is reported in [32]. Conversely, the X-ray polarization of Mrk 421 was undetected in the IXPE data of Obs. 2 and 3 when time-averaged over the entire length of the observations. Using the procedure of [66] within `ixpeobssim`, we found for the 2.0–8.0 keV band data a nominal minimum detectable polarization (equivalent to a 99% confidence upper limit) of 5% and 4% for Obs. 2 and 3, respectively. Fig. 7 displays the two-dimensional confidence contours for the X-ray polarization degree and angle obtained with the same method, to visually illustrate the lack of constraints on the X-ray polarization angle in these time-averaged data. A spectropolarimetric fit [90] of the data gives similar upper bounds for the polarization properties, assuming that the polarization degree and angle are constant with energy (using the `polconst` model in `Xspec`). A log-parabolic model best fits the I spectra, where we used the same fixed pivot energy as for the Swift-XRT data, $E_p = 5.0$ keV (see above). The IXPE data follow the same harder-when-brighter trend as for the Swift-XRT data: $\alpha = 3.17 \pm 0.06$, $\beta = 0.7 \pm 0.1$ and $\alpha = 2.81 \pm 0.03$, $\beta = 0.61 \pm 0.03$, for Obs. 2 and 3, respectively.

In the following, we investigate the cause of the change in the polarization properties of Mrk 421. The non-detection of the X-ray polarization of Mrk 421 in time-averaged IXPE Obs. 2 and 3 data can be due to time variability of the polarization angle within the observation (see, e.g., [25]). A rotation of the polarization angle, as often observed for blazars in the optical band, can in principle cancel the polarization degree in time-averaged data. In the following, we test this hypothesis using a simple model where the polarization angle rotates at a constant rate while the polarization degree remains constant.

³<https://lweb.cfa.harvard.edu/cqi/mircook.html>

This assumption is sufficient to our aim, which is to assess the reality of the polarization angle rotation. Consideration of more complex models for the time variability is beyond the scope of this paper. In order to make this assessment, we employ three methods: (1) a maximum-likelihood, unbinned event-based method, as in [91], (2) a fit of the binned light-curves of the Stokes parameters using χ^2 statistics, and (3) a fit of a rotation pattern in the Q-U plane using χ^2 statistics. A by-product of this analysis is an estimation of the rotation rate, for which all three methods return consistent results.

Searching for the optimal rotation rate via a likelihood analysis

For a detailed treatment of the optimal estimation of the (normalized) Stokes parameters q and u in the case of unbinned polarimetric data via a likelihood analysis, we refer the reader to [91]. An unbinned likelihood analysis is appropriate for fitting X-ray event data because of the Poisson nature of the counting statistics. This method has the advantage of being independent of any subjective choice of the binning of the data in energy or time.

Here, we expand the likelihood analysis method to the case of a rotating polarization angle. The log-likelihood formula for the polarization parameters of a set of (Poisson distributed) events depends on the Stokes parameters as

$$S(q, u) = -2 \sum_i \ln(1 + q\mu_i \cos 2\Psi_i + u\mu_i \sin 2\Psi_i), \quad (1)$$

where the sum is over each event i , μ_i is the modulation factor for event i (at energy E_i), Ψ_i is the event's instrumental phase angle, and it is assumed that q and u do not depend on the source flux. In addition, we are not fitting for the parameters of the spectral model.

Since the time-averaged polarization is small and the apparent rotation is smooth, we can approximate the time behavior with a simple model that has a varying polarization vector of constant degree, rotating at constant rate $\dot{\Psi}$. We also assume that there is no steady non-rotating component of the polarization (i.e., $q_0 = u_0 = 0$). For this model, the likelihood can be written as

$$S(\dot{\Psi}, q, u) = -2 \sum_i \ln\{1 + q\mu_i \cos[2\dot{\Psi}(t_i - t_0)] + u\mu_i \sin[2\dot{\Psi}(t_i - t_0)]\}, \quad (2)$$

where t_0 is a reference time, such as the midpoint of the observation period, and t_i is the time of event i . For any given rotation rate $\dot{\Psi}$, one can determine the optimal Stokes parameters \hat{q}_r and \hat{u}_r by marginalizing over q and u and substituting \hat{q}_r and \hat{u}_r back into Eq. 2 to yield $S'(\dot{\Psi})$. The best-fit value of $\dot{\Psi}$, $\hat{\dot{\Psi}}$, is given by the minimum of $S'(\dot{\Psi})$ and, for Gaussian-distributed errors, uncertainties can be determined using $\Delta S'(\dot{\Psi}) = S'(\dot{\Psi}) - S'(\hat{\dot{\Psi}})$, since $\Delta S'(\dot{\Psi})$ is distributed as χ^2 with one degree of freedom, being a function of only one

interesting parameter. Furthermore, we can compute the significance that $\hat{\Psi}$ is non-zero using

$$\Delta S'(0) = S'(0) - S'(\hat{\Psi}) = S(0, \hat{q}_0, \hat{u}_0) - S(\hat{\Psi}; \hat{q}_r, \hat{u}_r). \quad (3)$$

Again, by marginalizing over q and u in order to test against the hypothesis that $\Psi = 0$, $\Delta S'(0)$ is distributed as χ^2 with one degree of freedom.

We searched for the minima of $\Delta S(\hat{\Psi})$ over a grid of values of $\hat{\Psi}$, which we set to be $-1000^\circ/\text{day}$ to $+1000^\circ/\text{day}$ using the IXPE event files of the three observations of Mrk 421. Upon determining the best-fit value of $\hat{\Psi}$, we estimated the uncertainty of the best-fit parameters at a confidence level of 90 % using $\Delta S'(\hat{\Psi})$. The results of this analysis are displayed in Fig. 8. As expected, for Obs. 1, the estimated rotation rate is consistent with null rotation ($\hat{\Psi} = -6 \pm 9^\circ/\text{day}$), while the estimated polarization degree ($\Pi_x = 15 \pm 2\%$) is consistent with our previous work [32]. Conversely, for Obs. 2 and 3 we find absolute minima of $\Delta S'(\hat{\Psi})$ at $\hat{\Psi} = 80 \pm 9^\circ/\text{day}$ and $\hat{\Psi} = 91 \pm 8^\circ/\text{day}$, respectively, and that $\hat{\Psi} = 0$ is ruled out at better than 7σ for both observations. The estimated polarization degrees for these two data sets were both $\Pi_x = 10 \pm 1\%$, which suggests that while the polarization angle was rotating, the polarization degree may have remained similar to that measured when not rotating. The estimated rotation rates for Obs. 2 and 3 are consistent within the uncertainties, which suggests that we may have sampled two segments of one continuous rotation event spanning three days. Combining Obs. 2 and 3, we found a rotation rate of $R = 77.0 \pm 2.4^\circ/\text{day}$ and $\Pi_x = 10.1 \pm 0.8\%$, indicating that the third observation was approximately in phase with the second after a day passed.

Modeling the time-binned Stokes parameters

As a second test of the hypothesis of polarization angle rotation canceling the polarization degree in the time-averaged data, we modeled the time series of the normalized Stokes parameters. As in [32], in order to investigate the polarization variability on different time scales, we used the temporal variations of the normalized Stokes parameters $q(t)$ and $u(t)$ with various time bin sizes in the range from ~ 8 ks (corresponding to $N_{\text{bins}}=20$ bins) to ~ 60 ks ($N_{\text{bins}}=3$). We fit all the time series with (1) a constant model and (2) a model where the polarization angle rotates at a constant rate $\dot{\Psi}$ while the polarization degree Π remains constant, such that the Stokes parameters vary as trigonometric functions: $q(t) = \Pi \cos(2(\dot{\Psi}t + \phi))$ and $u(t) = \Pi \sin(2(\dot{\Psi}t + \phi))$ (where ϕ is a phase angle). As a test of the goodness of the fits, we computed, for all the cases tested, the probability for the null hypothesis (P_{null}) to obtain by chance a χ^2 value at least as large as that measured if the data are drawn according to the model.

Figure 9 displays, for both IXPE observations and for all the tested time binning schemes, the P_{null} values obtained for the constant model (black symbols) and the constant rotation model (red symbols). A constant model is statistically unacceptable ($P_{\text{null}} < 1\%$) for any time binning. A model including a linear time variation of the polarization angle always provides a better fit (i.e., an increase of P_{null} , up to $\sim 99\%$ in several cases) than a constant model. Figure 10 shows all the fit realizations, for the case N_{bins} in the range between 3 and 20. In the fitting exercise of Figure 9, we keep the parameters $\dot{\Psi}$ and Π fixed to those determined from the likelihood analysis. Hence, ϕ is the only free parameter. Moreover, we note that the independent fits of $q(t)$ and $u(t)$ return best-fit values of ϕ consistent within each other (within a typical uncertainty of $\sim 8^\circ$). This is an *a posteriori* indication that our fits are physical. To further assess the phenomenology of the polarization variability, we allow, in turn, the rotation rate $\dot{\Psi}$ and the polarization degree Π to be free in our fits. We find that $\dot{\Psi}$ is unconstrained in these fits. Conversely, the best fit corresponds to values of Π that are marginally inconsistent between the fit of $q(t)$ (e.g., $\Pi = 11\% \pm 2\%$ for the case $N_{\text{bins}}=16$) and that of $u(t)$ (e.g., $\Pi = 5\% \pm 2\%$). This suggests that Π and/or $\dot{\Psi}$ are somewhat variable with time about the average values, rather than constant. The detailed modeling of these variability features is beyond the scope of our hypothesis testing, and may be assessed in future works in the context of physically motivated models.

Fitting a rotation model in the Q - U plane

As a third and final test, we modeled the time behaviour of the data in the Q - U plane, with $N_{\text{bins}} = 24$. We display the time evolution of the data in Figure 11. In this framework, as a first, straightforward test for variability, we calculated the χ^2 statistic for the mean Q/U Stokes parameters in each time bin under the null hypothesis that they are all consistent with the time-integrated mean Stokes parameters (\bar{Q} and \bar{U}). Since the Stokes parameters from each time bin (denoted as Q_i and U_i , respectively, for time bin i) are normally distributed and independent, the quantity

$$\chi^2 = \sum_i \frac{(Q_i - \bar{Q})^2 + (U_i - \bar{U})^2}{\sigma_i^2} \quad (4)$$

under this null hypothesis follows a χ^2 distribution with $2N_{\text{bins}} - 2 = 46$ degrees of freedom. We can therefore compare the observed value of χ^2 with the expected values. For Obs. 1, we find $\chi^2 = 55$, the probability of which arising from the null hypothesis of constant Stokes parameters is $P_{\text{null}} \sim 0.17$, suggesting that these data are consistent with the constant polarization model. Conversely, for Obs. 2 and 3, we determine χ^2 values of 78 and 121, respectively. The probability of acquiring χ^2 exceeding this value by chance under the null hypothesis of constant polarization is $P_{\text{null}} < 2 \times 10^{-3}$. This implies

that, in these cases, the null hypothesis can be rejected with high confidence. Using this same statistical framework, we are able to determine the best-fit rotation rate $\dot{\Psi}_x$ for the model by assuming that both $\dot{\Psi}_x$ and the polarization degree are constant (see above for the mathematical form of this model). When applying these calculations to the data of Obs. 1, we find no evidence of time-dependent rotation of Ψ_x : the best-fit constant rotation rate is -4 ± 7 °/day). For Obs. 2 and 3, the best-fit rotation rates are $\dot{\Psi}_x = 78 \pm 8$ °/day and 83 ± 6 °/day respectively. These values are consistent with the findings of the previously described methods using the same model, indicating that all three methods result in a consistent rate of rotation. The corresponding χ^2 value for each of these fits is 53 for 45 *d.o.f.*, with a corresponding value of $P_{\text{null}} \sim 0.18$. We can therefore conclude that a constant rotation model provides a good fit to the data. Attempts to fit these data to a more complex elliptical rotation model (i.e., where the polarization degree varies with time) do not result in a statistically significant improvement in the overall value of χ^2 given the reduced degrees of freedom.

Comparison with a stochastic model

In order to verify further our explanation of the cause of the X-ray polarization angle rotation in Mrk 421, we tested the hypothesis that the rotation occurred by chance as a result of a stochastic variation of Ψ_x . We considered two possibilities for the involvement of random processes. First, the variations in Ψ_x during the two IXPE observations of June corresponded to two independent rotations. Second, the two IXPE observations were part of one continuous rotation, of which we sampled only two segments. To determine the probability of the rotation(s) occurring by chance due to the random variations of Ψ_x , we simulated the time dependence of the polarization degree and angle that occur via random walks, and compared them to the IXPE results. As described in detail in [52, 53], the simulations are based on two parameters: the number of maximally polarized (i.e., each with uniform magnetic field) cells, N_{cell} , and the number of cells that change per day, N_{var} . The cells each have the same intensity, hence the total intensity $I_{\text{total}} = N_{\text{cell}}I$. The initial Stokes parameters Q and U for each cell were drawn from Gaussian distributions. At every simulation time step, one cell was selected randomly, and its Q , U values were drawn anew, then the averages of Q , U , Π , and Ψ over all cells were calculated anew. The number of simulated time steps depends on the observation duration and (N_{var}); e.g., for $N_{\text{var}} = 100$ we simulated 100 data points per day. For each of the aforementioned possibilities, we performed a grid search in the N_{cell} , N_{var} parameter space to identify episodes of rotation of Ψ .

For the first case, we set the total length of the simulated polarization light curves to the length of each of the IXPE observations. We created 10,000 simulated light curves, binned to match one of the data binning schemes, and recorded the average Π of the light curve and the longest continuous variation

of Ψ that could be interpreted as a rotation. We considered a trial successful if the average Π and standard deviation of the simulated time dependence was within 10% of the observed values, and if the variation in Ψ was equal to or larger than that observed. Figures 12 and 13 show the results for the parameter search of each event. The binning of the data can have a significant effect on the number of successful trials. For that reason, we repeated the analysis for different numbers of bins from 3 to 18. For IXPE Obs. 2 (first rotation) we found the p significance values to range from 0.0049 to 0.14 (13 bins), with a median of 0.057. For the following rotation (IXPE Obs. 3), we found $p = 0.0013$ to 0.21 (17 bins), with a median of 0.032. The probability of two independent events occurring by pure chance in a row is then $p = 0.029$.

For the second possibility, we set the length of the simulated light curves equal to the total duration of the observations from the beginning of IXPE Obs. 2 to the end of Obs. 3. To test the case of an individual rotation, the polarization-angle curve of Obs. 3 was shifted by $\pm 180^\circ$ as needed to align the two segments. In this case, we explored from 3 to 26 bins and additionally required that the rotation rate of the second segment lie within 10% of that of the first segment. We repeated the above procedure and estimated the number of successful trials (Fig. 14). We find $p = 0.0006$ to 0.022 (23 bins) with a median of 0.0053. All of the above results indicate that it is unlikely that the observed rotation(s) were caused by a purely stochastic process. Rather, the event has a high probability of being related to non-stochastic physical processes in the jet.

Activity state of Mrk 421

In Fig. 15 we display the long term light curves of Mrk 421 in optical brightness (top panel) from the Steward observatory monitoring program [92] and ATLAS [93–95], as well as the X-ray flux (bottom panel) from the Swift XRT. The optical observations cover a time range from 2006 to 2022 and we highlight as vertical grey lines the time of the IXPE pointings.

The Swift-XRT observations are in the 0.3–10 keV band. The minimum and maximum value of the X-ray flux were 0.5×10^{-10} and 55×10^{-10} erg s⁻¹ cm⁻², respectively, with a median value of 8.5×10^{-10} . As a comparison, the flux measured by Swift at the time of the IXPE pointings (see Table 2) ranged between 7.5×10^{-10} and 14.1×10^{-10} erg s⁻¹ cm⁻². Thus, we conclude that Mrk 421 was at an average level of X-ray activity at the time of the IXPE observations.

We display the optical brightness in the top panel of Fig. 15. The Steward observatory observations are in the R-band, while for ATLAS we show both c-band and o-band observations. While the Steward and ATLAS observations are not directly comparable without applying conversion factors between optical bands, it is evident from the overlap of the two surveys (2016–2018) that any difference is rather small compared to the overall brightness variations of Mrk 421. The ATLAS observations in 2022 are ~ 0.5 mag lower than the

average of the Steward observations (2011-2016) and ~ 1 -1.5mag lower than the flares seen in the Steward data. Therefore, we can also conclude that the optical brightness of Mrk 421 at the time of the IXPE observations was at an average state.

Table 1 Log of polarization measurements of Mrk 421 used in this work.

Telescope	Band (eV)	Dates (YYYY-MM-DD)	Radio Flux Density ($10^{-25}\text{erg s}^{-1}\text{ cm}^{-2}\text{ Hz}^{-1}$)	Radio Polarization $\Pi_{\text{R}}(\%)$ $\Psi_{\text{R}}(^{\circ})$	
SMA	9.5×10^{-4}	2022-06-04	28 ± 2	2.3 ± 0.2	130 ± 2
SMA	9.5×10^{-4}	2022-06-16	38 ± 2	2.3 ± 0.2	133 ± 4
IRAM	3.5×10^{-4}	2022-05-04	28 ± 1	3.0 ± 0.7	237 ± 7
IRAM	3.5×10^{-4}	2022-05-05	38 ± 2	3.8 ± 0.7	232 ± 4
IRAM	3.5×10^{-4}	2022-05-31	32 ± 2	7.9 ± 0.8	128 ± 2
IRAM	3.5×10^{-4}	2022-05-06	36 ± 1	1.8 ± 0.6	116 ± 9
VLBA	1.7×10^{-4}	2022-04-30	34.6 ± 0.1	1.6 ± 0.3	100 ± 10
VLBA	1.7×10^{-4}	2022-06-05	27.6 ± 0.1	2.6 ± 0.3	147 ± 10
VLBA	1.7×10^{-4}	2022-06-24	25.6 ± 0.1	2.2 ± 0.3	132 ± 10
Telescope	Band (eV)	Dates (YYYY-MM-DD)	Infrared flux density ($10^{-25}\text{erg s}^{-1}\text{ cm}^{-2}\text{ Hz}^{-1}$)	Infrared Polarization $\Pi_{\text{IR}}(\%)$ $\Psi_{\text{IR}}(^{\circ})$	
Perkins	H:0.9	2022-05-04	3.92 ± 0.05	1.3 ± 0.5	220 ± 11
Perkins	H:0.9	2022-05-05	1.77 ± 0.03	2.9 ± 0.8	212 ± 8
Perkins	H:0.9	2022-05-09	4.19 ± 0.05	3.1 ± 0.8	181 ± 7
Perkins	H:0.9	2022-05-14	3.55 ± 0.04	1.7 ± 1.0	175 ± 17
Perkins	H:0.9	2022-06-06	4.87 ± 0.05	3.9 ± 0.5	128 ± 3
Perkins	H:0.9	2022-06-07	4.52 ± 0.05	4.8 ± 0.9	147 ± 5
Perkins	H:0.9	2022-06-08	4.14 ± 0.06	6.2 ± 1.3	145 ± 6
Kanata ¹	H:0.9	2022-05-04	–	3.1 ± 0.2	197 ± 2
Kanata ¹	H:0.9	2022-05-05	–	3.4 ± 0.3	187 ± 4
Telescope	Band (eV)	Dates (YYYY-MM-DD)	Optical flux density ($10^{-25}\text{erg s}^{-1}\text{ cm}^{-2}\text{ Hz}^{-1}$)	Optical Polarization $\Pi_{\text{O}}(\%)$ $\Psi_{\text{O}}(^{\circ})$	
Skinakas	R:1.9	2022-05-13	1.60 ± 0.04	2.7 ± 0.2	192 ± 2
Skinakas	R:1.9	2022-05-13	1.64 ± 0.04	3.2 ± 0.2	195 ± 2
Skinakas	R:1.9	2022-05-13	1.61 ± 0.04	2.7 ± 0.2	193 ± 2
Skinakas	R:1.9	2022-05-14	1.48 ± 0.04	3.7 ± 0.2	179 ± 2
Skinakas	R:1.9	2022-05-16	1.41 ± 0.04	3.5 ± 0.3	176 ± 2
Skinakas	R:1.9	2022-05-18	1.41 ± 0.04	2.7 ± 0.4	179 ± 5
Skinakas	R:1.9	2022-05-22	1.53 ± 0.04	3.3 ± 0.2	118 ± 2
Skinakas	R:1.9	2022-05-30	2.02 ± 0.04	5.6 ± 0.2	149 ± 1
Skinakas	R:1.9	2022-05-31	1.98 ± 0.04	5.4 ± 0.2	150 ± 1
Skinakas	R:1.9	2022-06-01	2.05 ± 0.04	5.3 ± 0.2	142 ± 1
Skinakas	R:1.9	2022-06-02	1.93 ± 0.04	5.1 ± 0.2	152 ± 1
Skinakas	R:1.9	2022-06-07	2.12 ± 0.04	5.4 ± 0.3	145 ± 1
Skinakas	R:1.9	2022-06-17	2.05 ± 0.04	4.7 ± 0.3	152 ± 2
NOT	R:1.9	2022-05-04	1.89 ± 0.04	2.9 ± 0.1	202 ± 1
NOT	R:1.9	2022-06-04	2.02 ± 0.04	4.8 ± 0.1	153 ± 1
NOT	R:1.9	2022-06-05	2.25 ± 0.04	3.9 ± 0.1	133 ± 1
NOT	R:1.9	2022-06-06	2.27 ± 0.07	5.6 ± 0.2	146 ± 1
SNO	R:1.9	2022-01-16	2.34 ± 0.01	3.8 ± 0.4	136 ± 3
SNO	R:1.9	2022-04-19	1.95 ± 0.01	4.6 ± 0.7	264 ± 3
SNO	R:1.9	2022-06-16	2.40 ± 0.50	9.5 ± 1.1	137 ± 4
Kanata ¹	R:1.9	2022-05-04	2.50 ± 0.40	3.1 ± 0.2	200 ± 1
Kanata ¹	R:1.9	2022-05-05	2.20 ± 0.02	3.4 ± 0.3	201 ± 1
Telescope	Energy range (keV)	Dates (YYYY-MM-DD)	X-ray flux ($10^{-11}\text{erg s}^{-1}\text{ cm}^{-2}$)	X-ray Polarization ² $\Pi_{\text{X}}(\%)$ $\Psi_{\text{X}}(^{\circ})$	
IXPE	2.0-8.0	2022-05-04	8.67 ± 0.03	15 ± 2	35 ± 4
IXPE	2.0-8.0	2022-06-04	15.69 ± 0.09	NOT DETECTED	NOT DETECTED
IXPE	2.0-8.0	2022-06-07	30.2 ± 0.2	NOT DETECTED	NOT DETECTED

¹Not corrected for dilution of polarization by unpolarized starlight from the host galaxy.²X-ray polarization degrees are for the time-averaged IXPE data.

Table 2 Log of Swift observations of Mrk 421 in May/June 2022.

Swift-Obs ID	Dates (YYYY-MM-DD)	0.3-10.0 keV flux (10^{-11} erg s $^{-1}$ cm $^{-2}$)
31540031	2022-05-01	46 ± 1
31540032	2022-05-03	38 ± 1
31540033	2022-05-05	44 ± 1
31540034	2022-05-07	64 ± 1
96557003	2022-05-02	46 ± 1
96557004	2022-05-03	42 ± 1
96557005	2022-05-04	39 ± 1
96557006	2022-05-05	48 ± 1
96557008	2022-05-08	84 ± 1
31540051	2022-06-01	93 ± 1
31540052	2022-06-02	90 ± 1
96557009	2022-06-03	88 ± 1
31540053	2022-06-04	75 ± 1
31540054	2022-06-04	79 ± 1
31540055	2022-06-05	69 ± 1
96557010	2022-06-06	116 ± 1
89326001	2022-06-07	141 ± 1
96557011	2022-06-08	104 ± 2
96557012	2022-06-12	73 ± 2
31540056	2022-06-16	52 ± 1
31540057	2022-06-17	69 ± 1
31540059	2022-06-19	110 ± 1
31540060	2022-06-20	74 ± 1
31540061	2022-06-21	59 ± 1
31540062	2022-06-22	61 ± 1
31540063	2022-06-23	62 ± 1
31540064	2022-06-24	56 ± 1

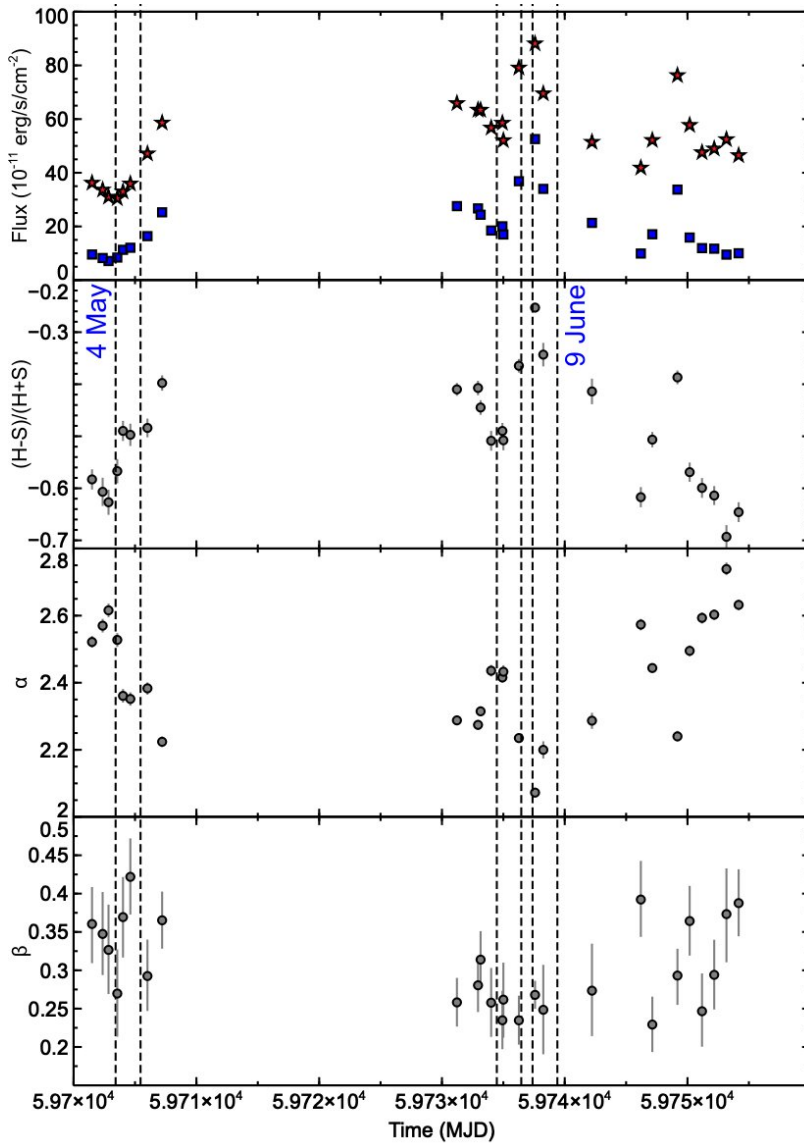


Fig. 4 Swift-XRT light curves of Mrk 421 in May-June 2022. From top to bottom: soft (S band: 0.3-2.0 keV, red stars) and hard (H band: 2.0-10.0 keV, blue squares) fluxes, hardness ratio, α and β parameters for a best-fit log-parabolic model. The dashed vertical lines indicate the beginning and the end of each IXPE observation.

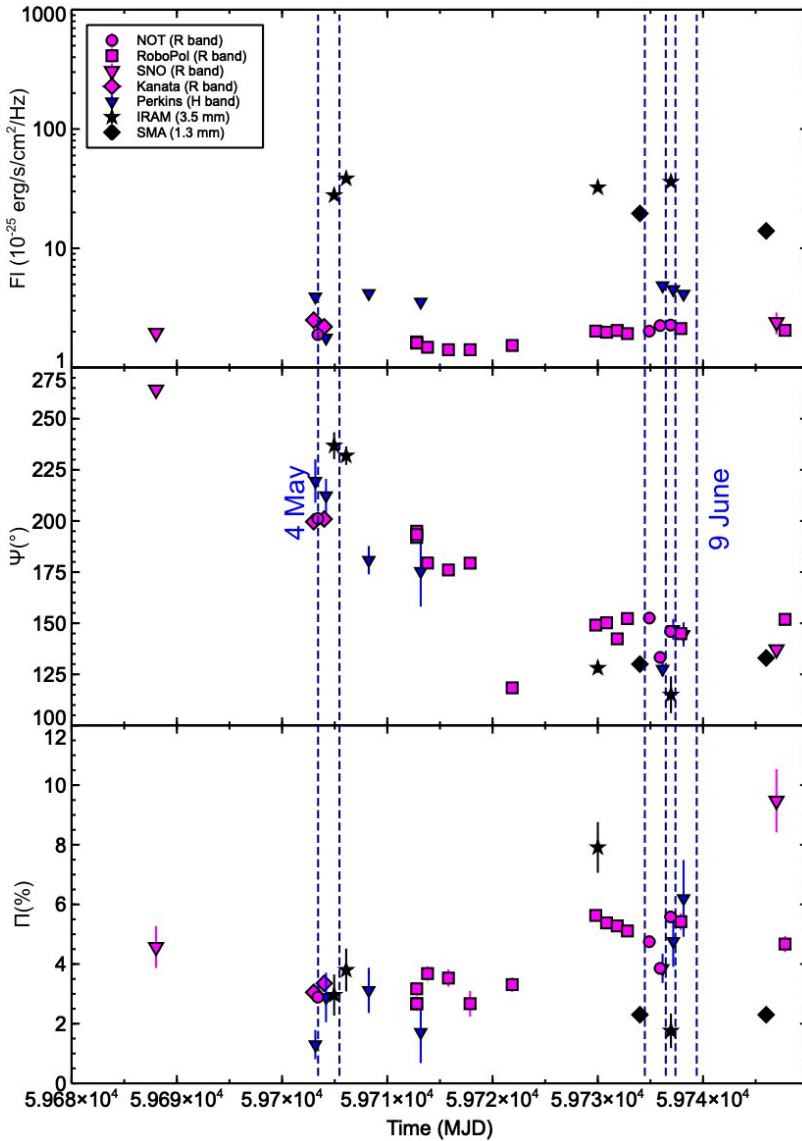


Fig. 5 Time evolution of the flux (top panel), polarization angle (middle panel), and polarization degree (bottom panel) of Mrk 421 at radio/millimetre (IRAM: black stars, SMA: black diamonds), infrared (Perkins: blue triangles), and optical (NOT: magenta circles, RoboPol: magenta squares, SNO: magenta triangles, Kanata: magenta diamonds) wavelengths. The dashed vertical lines mark the beginning and the end of each of the three IXPE observations.

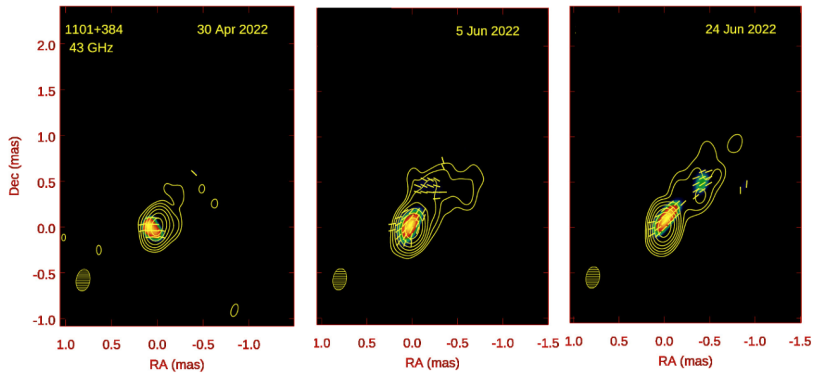


Fig. 6 VLBA images of Mrk 421 at 7 mm at three epochs near the times of the IXPE observations. Contours represent total intensity, in factors of 2 starting at 2% (left image) or 1% (middle and right images) of the peak intensity of (left to right) 0.35, 0.28, and 0.26 Jy per beam. Colour coding indicates relative linearly polarized intensity, with maxima of (left to right) 5.7, 7.2, and 5.7 mJy per beam. The yellow line segments correspond to the position angle of polarization. The cross-hatched ellipse in the lower left of each panel gives the FWHM of the elliptical restoring beam, which corresponds to the direction-dependent angular resolution. Marked positions are relative to the locations of the maximum intensity.

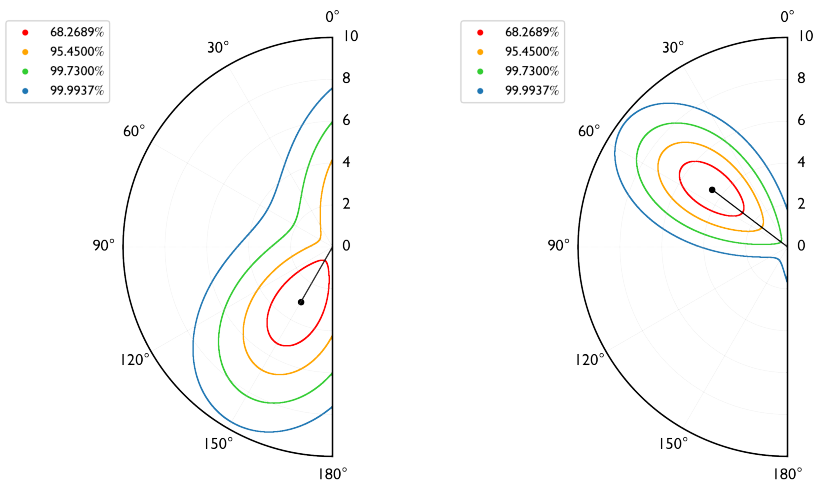


Fig. 7 Polar plot of the Π_x - ψ_x plane. Confidence contours of X-ray polarization derived within ixpeobssim for IXPE are shown for Obs. 2 (left panel) and 3 (right panel) of Mrk 421. The polarization degree is displayed in percentage units. For each case, the contours at 68.26%, 95.45%, 99.73%, and 99.994% confidence level (considering two degrees of freedom) are displayed, colour-coded in red, yellow, green, blue.

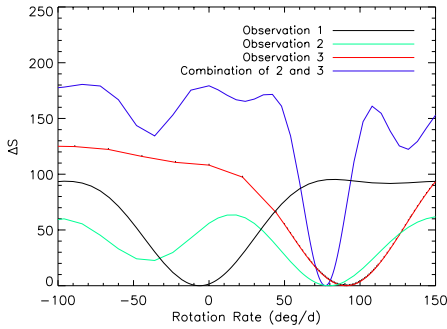


Fig. 8 Log-likelihood difference as a function of the polarization angle rotation rate according to the maximum likelihood analysis method (see section 3 and [91]). For each observation set, the difference is relative to the minimum at the best fit value of the rotation rate, $\dot{\Psi}$. Results of the search for Obs. 1, 2, 3, and for Obs. 2 and 3 combined are colour-coded in black, green, red and blue, respectively. In Obs. 2, for example, $\dot{\Psi} = 0$ can be ruled out at the 7σ level because $\Delta S > 50$ with respect to the best fit.

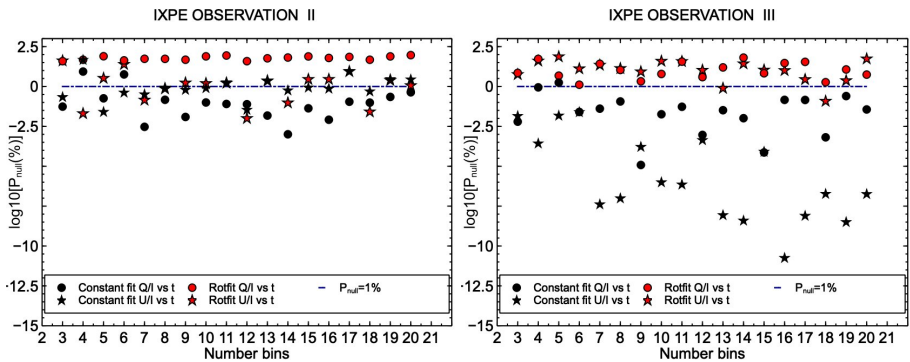


Fig. 9 Results of fitting the Stokes parameters vs. time ($q(t)$: circles $u(t)$: stars), with a constant model (black symbols) or with a model including a constant rotation of the polarization angle (red symbols), for Obs. 2 (left panel) and 3 (right panel). The null hypothesis probability for all the fits is displayed as a function of the number of time bins involved.

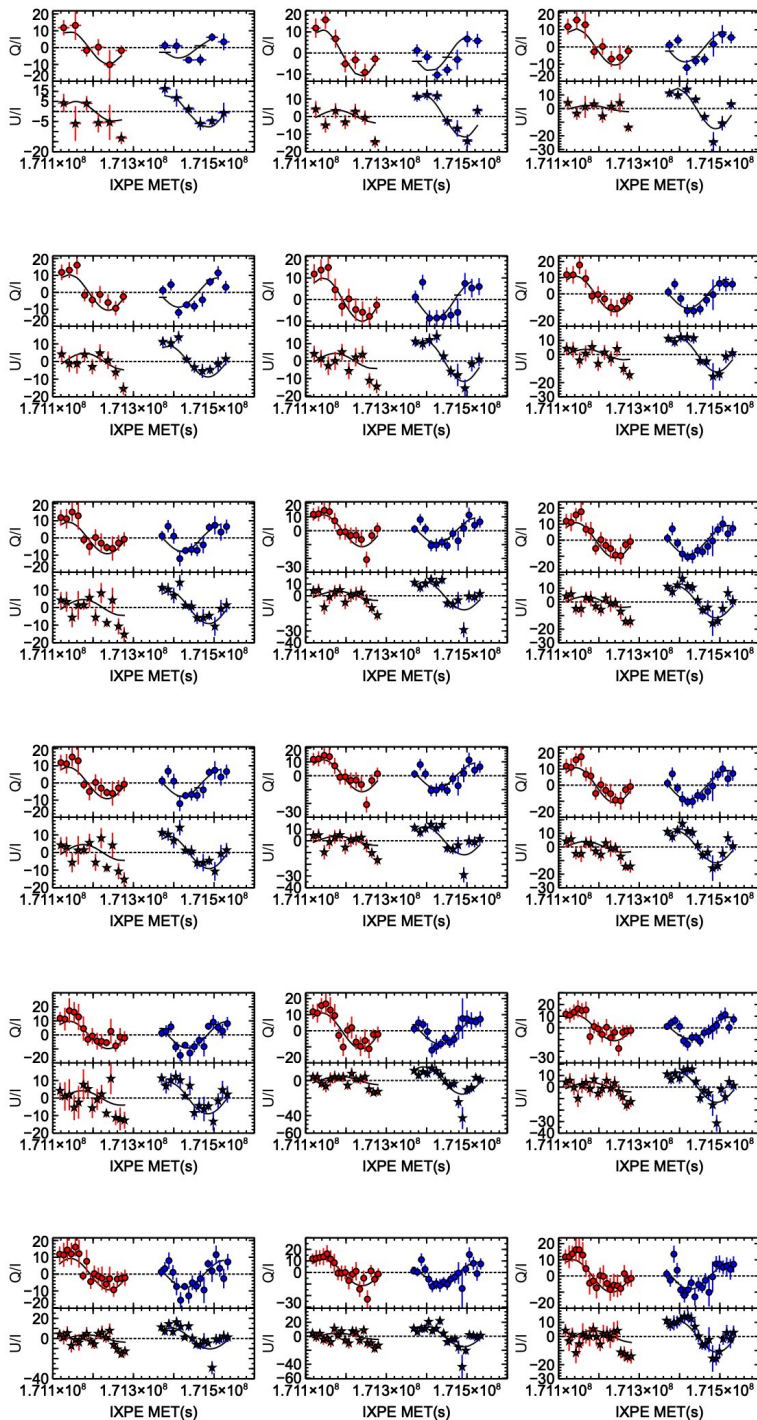


Fig. 10 Stokes parameters vs. time ($q(t)$: circles, top panel, $u(t)$: stars, middle panel) for Obs. 2 (red symbols) and 3 (blue symbols) for a number of time bins between 3 (i.e. ~ 17 hours) and 20 (i.e. \sim one hour). The black solid line represents a fit with a model of a constant rotation of the polarization angle. The dotted horizontal line indicates null Stokes parameters.

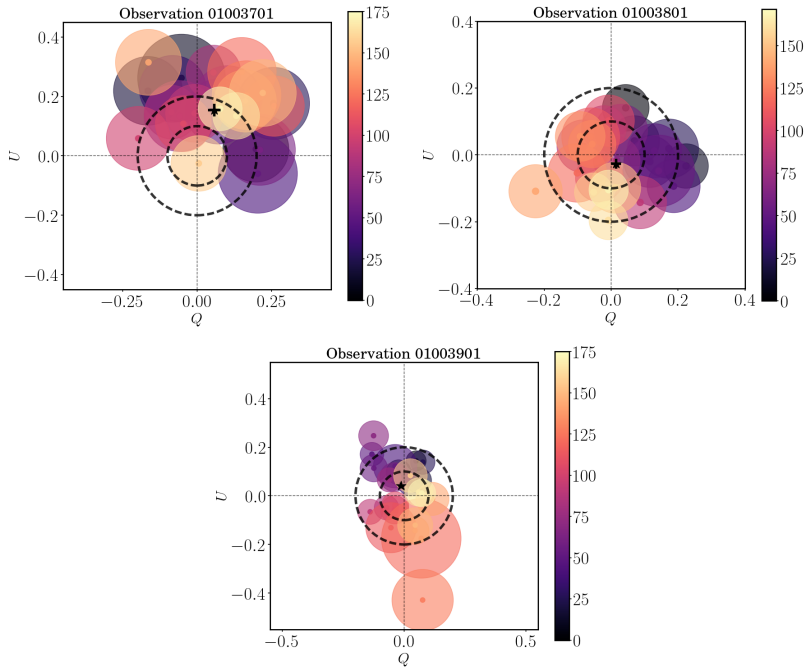


Fig. 11 Variation in the Stokes parameters as a function of time through all three observations of Mrk 421 taken with IXPE. The black cross denotes the time-integrated average values of Q and U along with its $1 - \sigma$ uncertainty region. The coloured circles denote the measured mean values of Q and U in each time bin and their $1 - \sigma$ uncertainty radii. The inner and outer dashed circles represent constant polarization degrees of $\Pi = 10\%$ and $\Pi = 20\%$, respectively, to help guide the eye. The colours of the data points correspond to the elapsed time relative to the beginning of the observation (in ks).

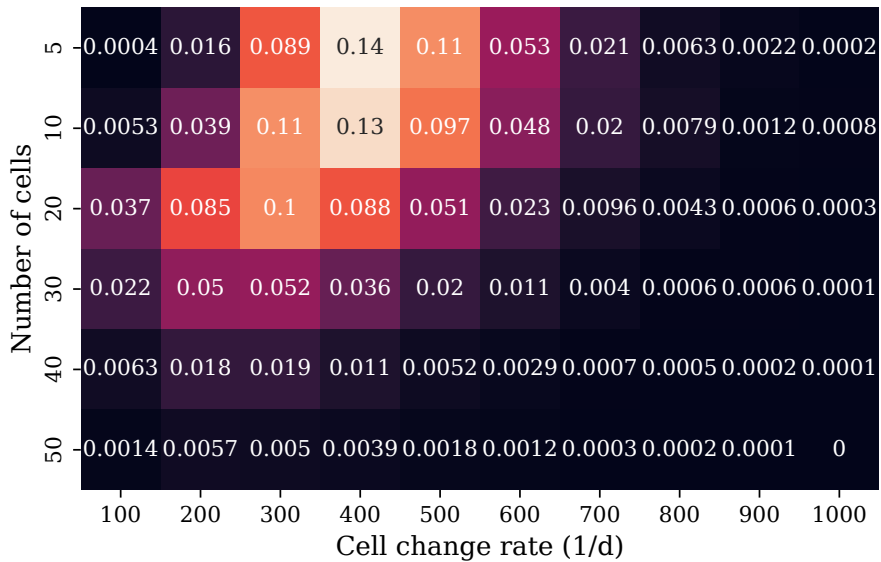


Fig. 12 Random-walk parameter search for the second IXPE observation. The numbers in the squares indicate the fraction of successful trials.

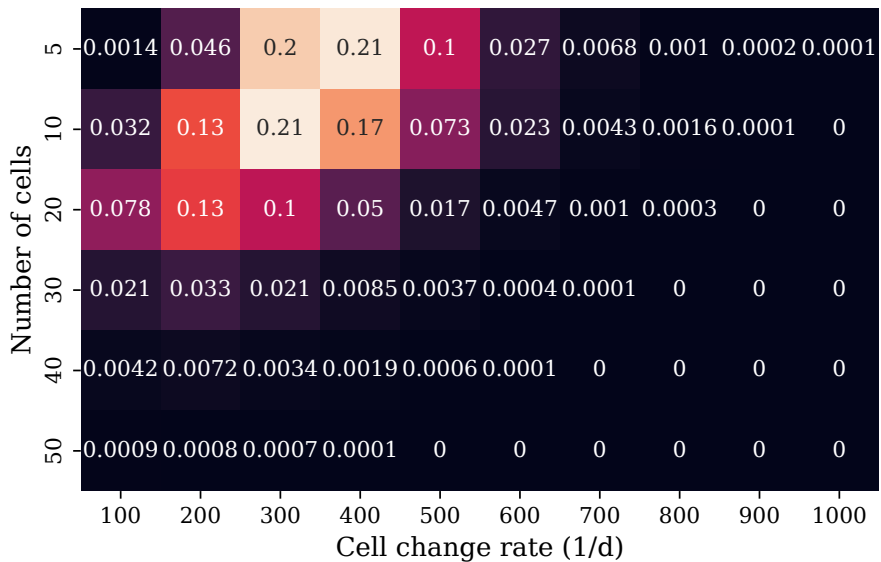


Fig. 13 Random-walk parameter search for the third IXPE observation. The numbers in the squares indicate the fraction of successful trials.

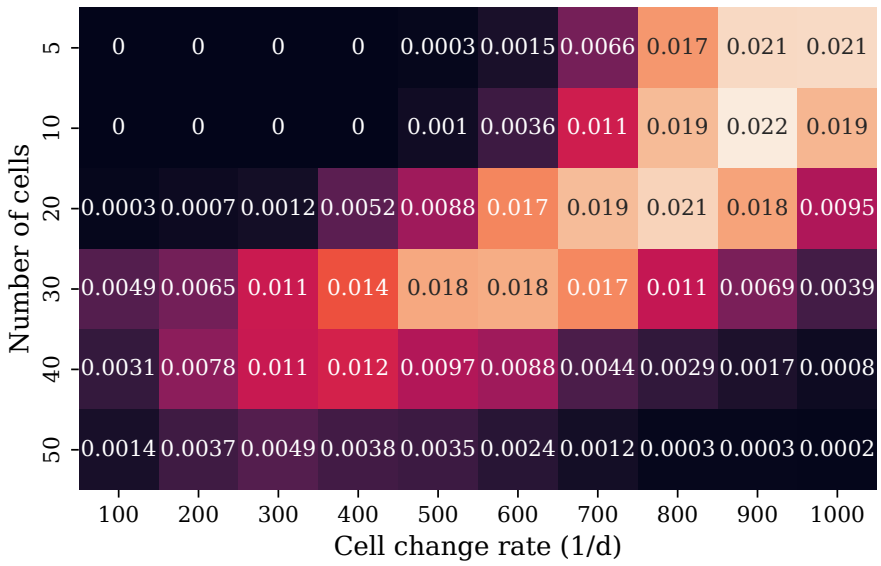


Fig. 14 Random-walk parameter search assuming the second and third IXPE observations are part of the same rotation. The numbers in the squares indicate the fraction of successful trials.

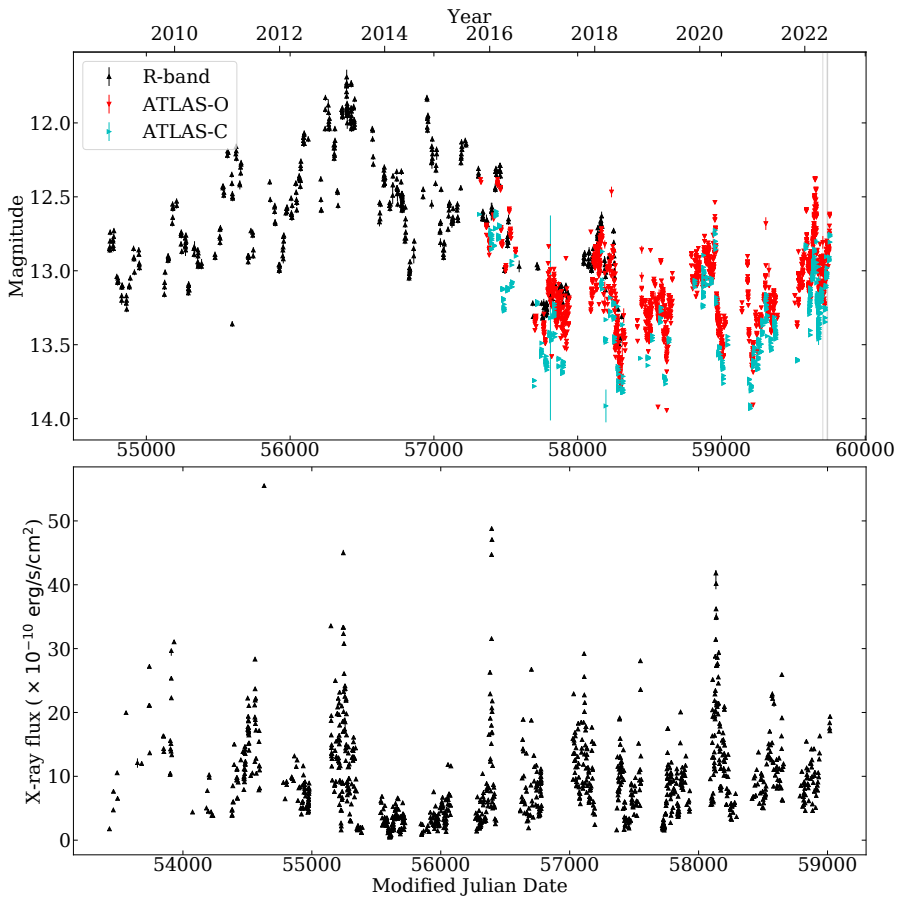


Fig. 15 Archival optical brightness (black triangles: R-band, Steward observatory, red and cyan triangles: c-band and o-band, ATLAS observatory), and X-ray flux (lower panel, black triangles) light curves for Mrk 421. The grey shaded areas represent the duration of the IXPE pointings.