

Diffusional microfluidics for protein analysis

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Abstract

Wastewater-based epidemiology (WBE) is an emerging tool to monitor public health and the outbreak of infective diseases. It requires real-time information by measuring chemicals or biomarkers in wastewater generated by people at community-level for WBE analysis. Protein-based biomarkers provides valuable insights into community public health. However, due to the complexity of wastewater, the bottleneck of protein analysis in WBE lies in the lack of high-sensitive, cost-efficient and high-throughput analytical techniques. Diffusional microfluidics, which involves co-flowing streams of analytes and buffer under laminar flow conditions, allows the detection and analysis of biomolecules in their native state via the study of their diffusive behaviour in flow. In this review, recently developed analytical techniques, microfluidic diffusional sizing, free-flow electrophoresis, and hydrodynamic focusing microfluidic mixer, that are based on diffusional microfluidics are reviewed. Their applications in protein analysis including protein sizing, protein-protein interaction, protein separation and protein identification are highlighted.

Keywords: Diffusional microfluidics; Microfluidics; Protein analysis; Protein biomarker detection; Wastewater-based epidemiology

1. Introduction

Wastewater-based epidemiology (WBE) was firstly outlined as an analytical tool to investigate the illicit and misused drugs in local community by quantitatively or qualitatively analysing chemicals from wastewater [1]. Wastewater is also an ideal medium for pathogenic microorganisms such as viruses, bacteria, parasites, parasitic worms and protozoa [2-3]. Thus, by analysing pathogens and/or their biomarkers in wastewater at community-level, WBE is also developed to understand the health of local communities and serve as an early warning system for outbreaks of infective diseases [4-4]. For example, WBE has recently been used to monitor the COVID-19 outbreak; the RNA of SARS-CoV-2 was quantified in sewage to track the disease infection in local community [6-7]. Among the pathogens and biomarkers in wastewater, proteins have attracted increasing attention as 1) proteins are particularly useful biomarkers to track pathogenic microorganisms in wastewater as they are often the effectors of diseases [4], 2) proteomics in WBE can provide valuable new insights into community public health.

39 However, due to the complexity of wastewater, the bottleneck of protein analysis for WBE lies in the
40 lack of high-sensitive, cost-efficient and high-throughput analytical techniques [3].

41

42 Microfluidics, which processes small amounts of fluids with channel dimensions of tens to hundreds of
43 micrometres, provides a platform to develop analytical techniques that can potentially overcome these
44 challenges [7]. For its applications in analysis, microfluidics offers a number of useful capabilities,
45 including consuming small quantities of samples, rapid measurements on the order of tens of seconds,
46 solution analysis in a confined environment, portable analytical device for potential on-site
47 measurements, and high modularity to integrate other functionalities [8], which are all desirable features
48 for protein analysis in WBE [9-11]. Based on the flow type, microfluidics can be classified as droplet-
49 based microfluidics and continuous-flow microfluidics [8]. Droplet-based microfluidics contains a
50 dispersed phase and a continuous phase to generate highly monodispersed microdroplets, which can be
51 employed as miniaturised containers for potential high-throughput analysis [12]. For the applications
52 of droplet-based microfluidics in WBE, we refer readers to ref. [13] for a detailed discussion on
53 quantification of pathogen biomarkers, single-cell analysis, and living cell biosensing using droplet-
54 based microfluidics. Continuous-flow microfluidics rely on a steady flow through the microchannels
55 for fluid process which enables uninterrupted analysis of samples within a device [8]. Diffusional
56 microfluidics is a subject of continuous-flow microfluidics which achieves fluid mixing or separation
57 only through diffusion within a microfluidic device [14].

58

59 In this review, we aim to highlight recent advances in diffusional microfluidics and its application in
60 protein analysis. The basis of diffusional microfluidics including its working conditions will be firstly
61 introduced to provide the scientific background. Then, the classic device designs to fulfil diffusional
62 microfluidics will be presented to briefly demonstrate the working principles of diffusional
63 microfluidics. Follow by that, recently developed analytical techniques based on diffusional
64 microfluidics and their application in protein analysis will be highlighted. At the end of this review,
65 challenges and perspective of future application of diffusional microfluidics in WBE will be discussed
66 after the conclusion.

67

68 **2. The basis of diffusional microfluidics**

69 In our day-to-day experience with fluids, random eddies continuously disturb fluid elements in bulk
70 solution, which dramatically increase the rate of fluid mixing [8]. In microchannels of microfluidic
71 device, however, fluid behaviour is dramatically different. Fluid flow at the microscale is normally in
72 laminar which means each plane of fluid flows smoothly in parallel with each other [8,14-16]. The
73 naturally arised laminar flow in the microchannels is resulted from the low inertial forces of fluid
74 comparing to the viscous forces which can be characterised by Reynolds number (Re) [14-17]. Re is a

75 dimensionless parameter that defines fluid as being turbulent or laminar. It is calculated by the ratio of
76 inertial to viscous forces.

77

78

$$Re = \frac{\rho v L}{\mu}$$

79 , where ρ is the density of fluid; v is the flow rate; L is the characteristic length, for microfluidic device
80 it is given by the hydraulic diameter of the channel (typically span from 10 to 2000 μm) and μ is the
81 dynamic viscosity of fluid. Laminar conditions occur when Re is smaller than 2300 [14-15,17]. For
82 common microfluidic devices, the value of Re is typically smaller than 1 which ensures laminar flow
83 within microfluidic devices [17-19]. With this prerequisite, fluid mixing within microfluidic device can
84 only occur by diffusion as turbulent mixing is completely suppressed, which results in significantly
85 longer mixing time than that in bulk solution. It also means that the concentration gradient of flow
86 ingredients, created by purely diffusion within the laminar flow, would last much longer than in bulk
87 solutions. In other words, temporal separation of flow ingredients can be achieved without the need of
88 a solid boundary.

89 In addition, fluid properties in microfluidic device are greatly affected by the competition between
90 convection and diffusion which can be characterised by Péclet number (Pe) [14,18-19]. Pe is a
91 dimensionless parameter that can be calculated by the ratio of advective transport rate to diffusive
92 transport rate.

93

94

$$Pe = \frac{Lv}{D}$$

95

96 , where L is the characteristic length; v is the linear flow velocity and D is the diffusion coefficient.
97 When Pe is very large ($Pe > 10^7$), diffusion within a microfluidic device can be neglected because the
98 advective transport of fluid is extraordinarily faster than diffusion [19]. At the other extreme, a small
99 Pe ($Pe < 1$) indicates that the diffusion processes of fluid are dominant within the length scale of
100 microfluidic device [19]. Fluid mixing, thus, happens only in a certain area through diffusion. In
101 contrast, at an intermediate Pe value, the advective transport of fluid is faster than diffusive transport.
102 Therefore, a rich amount of fluid mixing states can be observed along the downstream within the
103 microchannels of a microfluidic device [18-19]. It also means that the diffusion process of ingredients
104 within the fluid flow is location dependent. In other words, spatial separation of flow ingredients
105 without a solid boundary is possible in a microfluidic device. Diffusional microfluidics works at an
106 intermediate Pe value.

107

108 The possibility to achieve both temporal and spatial separation of ingredients in a diffusional
109 microfluidic device enables the application of diffusional microfluidics in analytical sensing by
110 extracting the physical information of analytes from their diffusive behaviour.

111

112 **3. Classic design of diffusional microfluidic devices**

113 One basic design to achieve diffusional microfluidics is the so-called T-sensor [20]. As shown in Fig.
114 1A, T-sensor has two inlets and one outlet, involving two fluid streams that enter the T-sensor separately
115 and merge to flow adjacently through a microchannel (because of low Re at the microscale). Fluids,
116 solutes, and suspended particles, thus, only mix through diffusion in the laminar flow, where small
117 ingredients diffuse longer average distance per time than larger ingredients [20]. When it is operated at
118 intermediate Pe , it forms an interdiffusion zone (sector) within the middle of the microchannel (Fig.
119 1A). The key parameters that control the interdiffusion zone are the ingredient diffusivity, channel
120 length, width and flow rate [20]. The interdiffusion zone can be determined and measured by labelling
121 with a fluorescent marker which gives information on analyte concentration, diffusivity, etc. T-sensor
122 based diffusional microfluidic devices, thus, have been widely employed for chemical sensing [21-22].

123

124 Another basic design of diffusional microfluidics is the H-filter (Fig.1B). H-filter [23] is essentially
125 similar to the T-sensor but has two outlets. Fluids, solutes and suspended particles within the combined
126 stream diffuse differently, depended on their diffusion coefficient, flow rate, and dimensions of the
127 microchannels (channel width, length and height). Basically, in the combined stream, small ingredients
128 diffuse faster than the larger ones and will traverse the middle section of the channel onto the other side,
129 while larger ingredients remain in the same side as they flow in (Fig. 1B). Therefore, ingredients
130 separation can be achieved in the H-filter. While many other separation methods require a physical
131 boundary, mechanical agitation, and/or external fields (electrical or gravitational) [23], it is not
132 necessary for H-filter as it relies on purely diffusion which facilitates further biological analysis in their
133 native state. In addition, H-filter enables the potential for direct analysis of complex samples without
134 the need of prior purification which is a desirable feature for WBE.

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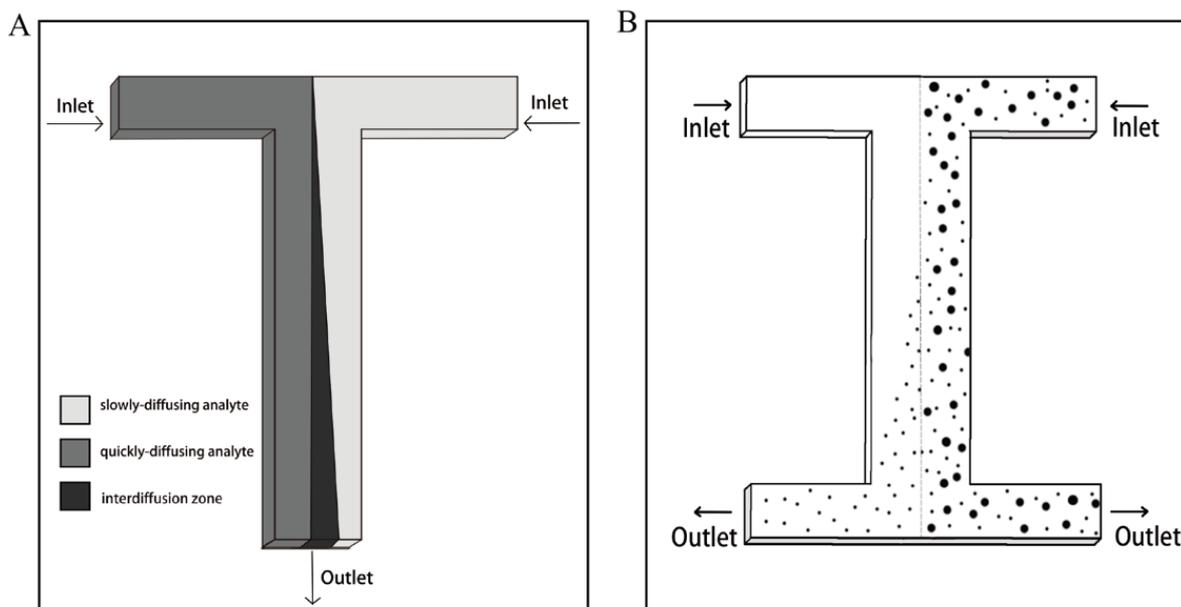


Fig. 1 (A) The schematic of T-sensor. Fluids are in laminar flow within the microchannels and mix only through diffusion. Small ingredients diffuse quicker than larger ingredients. (B) The schematic of H-filter. In the sample mixture, small ingredients diffuse faster than the larger ones and will traverse the middle section of the channel onto the other side, while larger ingredients remain in the same side as they flow in. Ingredients with different sizes can be separated using the H-filter.

4. Diffusional microfluidics-based protein analytical techniques

4.1 Microfluidic diffusional sizing (MDS)

Recently, a sizing technique based on diffusional microfluidics, named microfluidic diffusional sizing (MDS) [24], has been developed for protein analysis in terms of protein sizing [25-28], protein-protein interaction [25-31], protein separation [30] and protein identification [32-33]. In this technique, MDS devices are designed based on either the T-sensor or H-filter. The diffusion coefficient D of protein can be extracted from the mixing rate of proteins in the laminar flow by observing the time-evolution of the interdiffusion zone. The interdiffusion zone can be observed under a fluorescence microscope when proteins are either pre-labelled or post-labelled with a fluorescent dye. For protein that has large number of tryptophan and tyrosine, the interdiffusion zone can even be observed without any dye labelling because of its intrinsic fluorescence [34]. After obtaining the diffusion coefficient D , the average hydrodynamic radius (R_h) of the proteins can be calculated accordingly based on the Stokes-Einstein equation.

$$D = \frac{k_B T}{6\pi\eta R_h}$$

, where k_B is the Boltzmann constant, T is temperature (K), η is the solution viscosity, D is the diffusion coefficient and R_h is the hydrodynamic radius.

162 MDS allows the measurement of average R_h without a bias towards large protein which is one of the
163 major limitations of dynamic light scattering (DLS). Moreover, the measurements are performed in
164 solution without interference from a solid boundary (as measurements using gel electrophoresis) which
165 allows analysis of protein under their native states. In addition, by analysing the changes of protein R_h
166 with or without the presence of interacting partners, protein interactions can be studied, and related
167 binding affinity can be calculated.

168

169 Arosio *et al.* [25] designed a MDS device based on the T-sensor for protein analysis using dye-labelled
170 proteins (Fig. 2A). In this design, the stream with dye-labelled proteins is sandwiched by two flanking
171 buffer flows. And the proteins can laterally diffuse into the buffer streams under the laminar flow. The
172 diffusion can be observed under fluorescent microscope as the proteins are pre-labelled with fluorescent
173 dye. By measuring the width of the interdiffusion zone at certain locations of the microchannel
174 (detection points) under fluorescence microscope, the diffusivity of proteins can be calculated (Fig. 2A
175 detection region) and, consequently, the related R_h can be calculated based on the Stokes-Einstein
176 equation. To ensure the protein stream precisely located in the centre of the channel, a multistage nozzle
177 that is ten times wider than the diffusion channel is introduced. Besides, a high channel aspect ratio
178 (1:12) has been considered to ensure an intermediate Pe number so that all protein particles explore the
179 whole channel height within the MDS device. The MDS device has been validated by measuring the
180 average sizes of proteins, peptides and even fluorescence labelled nanoparticles with the size range
181 from 1 to 100 nm. The R_h measured by the MDS device are consistent with that measured by
182 conventional techniques such as DLS. Compared with DLS, this MDS requires a significantly smaller
183 amount of sample. The authors used the same MDS device to further detect protein-protein interactions
184 [25]. The interactions between dye-labelled α -synuclein, a protein whose aggregation is related to the
185 Parkinson's disease, and nanobody (NbSyn87), a single domain antibody fragment, have been
186 conformed based on the increased R_h when the α -synuclein is titrated with NbSyn87 nanobody [25].
187 The authors further demonstrate the power of the MDS device for analysing mixtures of proteins via
188 the deconvolution of experimental signals into the contributions that are from the individual protein
189 (Fig. 2A (e)) [25]. Basically, the distribution of the diffusion coefficients ($\rho(D_i)$) of the species in
190 solution is reflected from the shape of the concentration profile ($c(x)$) as a linear superposition. The
191 distribution of $\rho(D_i)$ as a function of diffusion coefficients can be obtained via inverting the linear
192 superposition relationship using a regularisation algorithm. A regularization coefficient (α), which is
193 determined by calibration with known standards, is introduced to ensure stability in the presence of
194 experimental noise. Global analysis of several diffusion profiles, thus, enables the deconvolution of
195 experimental signal into a linear combination of simulated standard profiles, thereby leading to the
196 evaluation of the size distribution of proteins in the mixture. The acquisition of a large number of

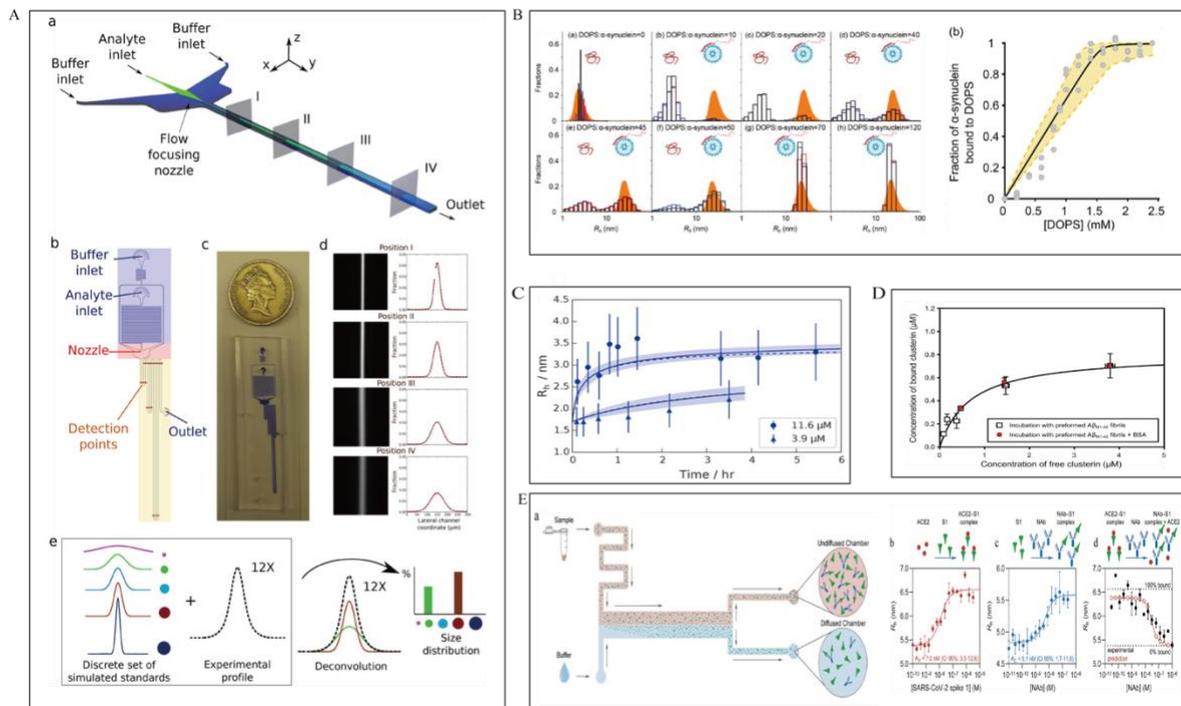
197 diffusion profiles is a key factor to assure the robustness of the method and allow clear resolution of
198 individual size peaks of proteins in a mixture.

199

200 Using the same MDS device, Gang *et al.* [26] investigated the interaction between dye-labelled α -
201 synuclein and negatively charged lipid vesicles which is not detectable using DLS. The R_h of α -
202 synuclein is measured when the lipid vesicles are titrated (Fig. 2B). Thus, the dissociation constant and
203 binding stoichiometry between α -synuclein and the vesicles can be characterized. Wright *et al.* [27]
204 studied the self-assembly behaviour of chaperones (Hsp70) by monitoring the R_h change of dye-labelled
205 SBD641(subdomain of HsP70) as a function of SBD641 concentration and time (Fig. 2C). Scheidt *et*
206 *al.* [28] explored the function of chaperones towards the aggregation of dye-labelled amyloid- β (M1-
207 42) peptide by following the size variation of amyloid- β (M1-42) fibrils with the presence of chaperone
208 (either brichos domain or clusterin). The results show that clusterin chaperone can inhibit the elongation
209 of amyloid- β fibrils (Fig. 2D). Scheidt *et al.* [28] also studied the interactions between the fibrils of α -
210 synuclein and the small heat-shock protein α B-crystallin with the MDS device. By measuring the
211 diffusion coefficient of bound and unbound chaperones, the thermodynamics and kinetics of binding
212 can be studied within minutes.

213

214 Fiedler *et al.* [30] reported another MDS device, designed based on the H-filter, to study the
215 neutralisation of SARS-CoV-2 (Fig. 2E), through the quantification of the interactions between the
216 SARS-CoV-2 spike protein (S1) and the angiotensin-converting enzyme 2 (ACE2, which is virus
217 receptor on the cell), as well as interactions between S1 and an antibody (NAbs). As shown in Fig. 2E,
218 sample containing either mixture of dye-labelled ACE2 and S1, mixture of NAbs and dye-labelled S1,
219 or mixture of dye-labelled ACE2, S1 and NAbs is loaded into the MDS device together with a flanking
220 flow of buffer. Only the unbound proteins diffuse into the buffer stream as they are smaller than the
221 protein complex. Consequently, the unbound proteins and protein complex are separated into two
222 observation regions at the end of the diffusion chamber. The average R_h of the proteins in the sample is
223 then determined by the ratio of fluorescence between the two observation regions, leading to the
224 quantification of dissociation constants between either S1 and ACE2 or NAbs and S1. These results can
225 be used to indicate the level of SARS-CoV-2 inhibition in human serum.

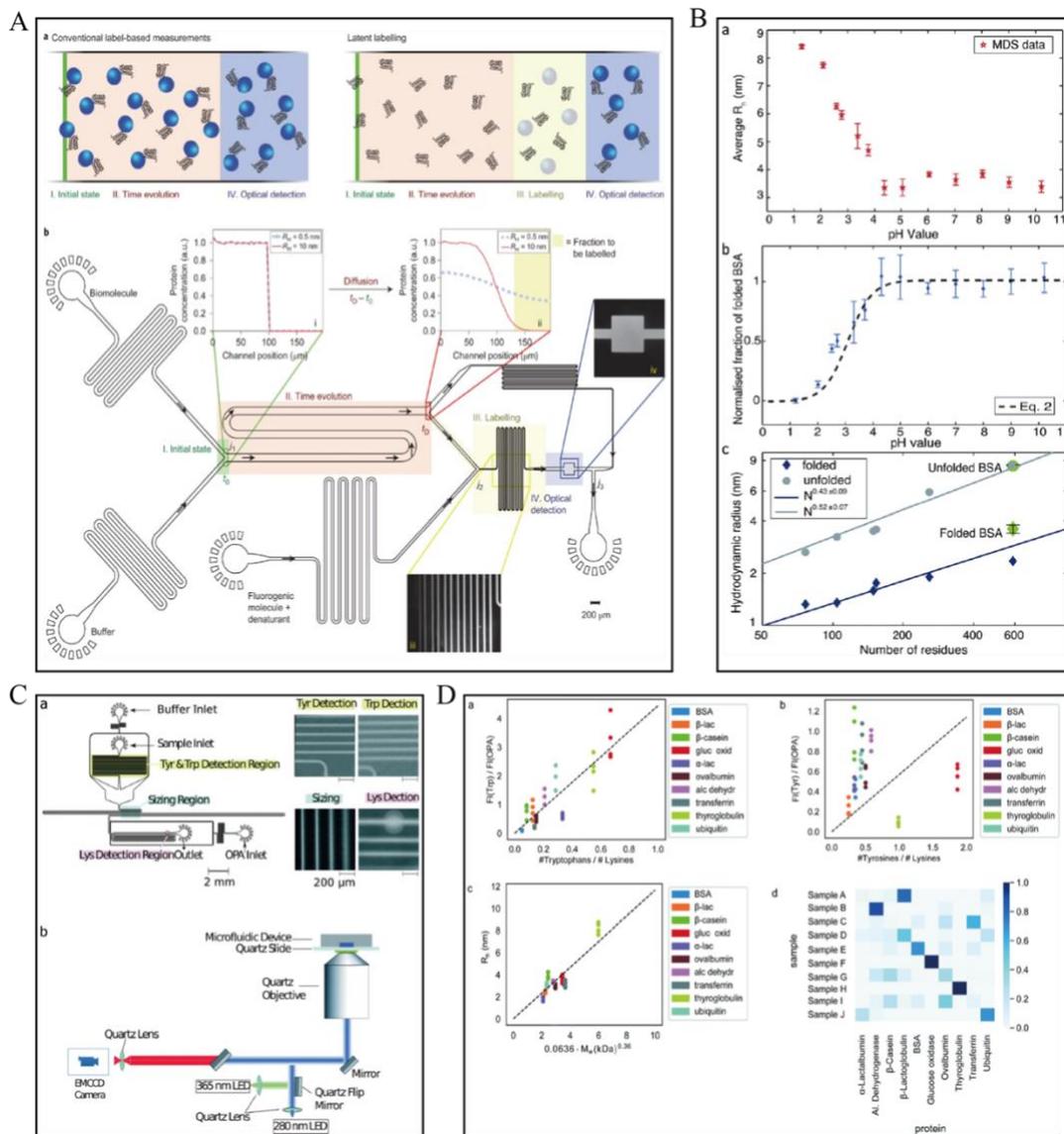


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227 **Fig. 2** (A) (a)-(c), The design of microfluidic diffusional sizing device. (d), Fluorescent images of colloid analytes at different
 228 positions along the microchannel and the comparison between measured and simulated diffusion profiles. (e), Global analysis
 229 of different diffusion profiles both in time and space to deconvolute the experimental signal into a linear combination of
 230 simulated standard profiles [Reprinted with permission from Ref. [25]]. (B) (a), Distribution profiles and R_h of α -synuclein
 231 measured by MDS (bars) and DLS (filled curves) in the absence and presence of vesicles. (b), Characterisation of the binding
 232 between α -synuclein and vesicles with MDS [Reprinted with permission from Ref. [26]]. (C) The R_h of SBD641 at different
 233 concentrations measured by MDS [Reprinted with permission from Ref. [27]]. (D) Binding curve of clusterin to amyloid- β
 234 (M1-42) fibrils measured by MDS [Reprinted with permission from Ref. [28]]. (E) (a), The neutralisation of SARS-CoV-2 is
 235 investigated using H-filter type MDS device. The R_h of analytes is calculated from the ratio of fluorescence intensities in the
 236 diffused chamber and the undiffused chamber. (b-d), The study of equilibrium binding of ACE2-S1, S1-NAb and NAb-S1
 237 ACE2 complex within the MDS, respectively [Reprinted with permission from Ref. [30]].

238 Fluorophore labelling are prone to affect the conformational structure of proteins, resulting in false
 239 biochemical properties of protein. Yates *et al.* [31] thus developed a MDS device for protein analysis
 240 under their native state using a latent protein labelling strategy (Fig. 3A). As shown in Fig. 3A, the
 241 protein and buffer stream with equal volumetric flow rates meet at the beginning of a diffusional channel
 242 (labelled t_0 , Fig. 3A). At this point, the protein and buffer stream span half the width of the diffusional
 243 channel, separately. Subsequently, protein diffuse laterally into the buffer stream along with the flow
 244 direction in the diffusional channel. At the end of the diffusional channel (t_D), a third of the total stream
 245 is diverted into a latent labelling region where the diffused proteins are quantitatively labelled with a
 246 dye molecule of o-phthalaldehyde (OPA). Measuring the fluorescence intensity in the observation
 247 region defines the total concentration of protein diverted for labelling at position t_D , which in turn
 248 reveals the protein distribution at position t_D , allowing determination of R_h of protein by comparison
 249 with values simulated for particles of known R_h values. With this technique, R_h of biomolecules and
 250 heterogenous mixtures can be determined at attomole level. The high sensitivity of the MDS technique
 251 is desirable feature for the application of WBE. Moreover, the interaction between monomeric α -
 252 synuclein and a nanobody (NbSyn2) is studied under their native states based on the variation of R_h

253 values [31]. Using the same MDS device, Zhang *et al.* [35] investigated the stability of bovine serum
 254 albumin (BSA) under different pH conditions (Fig. 3B). Based on the measured average R_h and
 255 calculated linear interpolation, the fraction of folded BSA can be calculated. This method provides a
 256 new approach for studying the structural stability of proteins and other substances under native state of
 257 protein [35].
 258
 259



260 **Fig. 3** (A) Latent labelling microfluidic diffusional sizing device {Reprinted with permission from Ref. [31]}. (B) (a), Average
 261 R_h of BSA measured with the latent labelling microfluidic diffusional sizing device under various pH conditions. (b),
 262 Normalized fraction of folded BSA derived from the measured R_h . (c), Fitted the measured folded and unfolded BSA to the
 263 literature value of average R_h versus the number of residues in a polypeptide chain {Reprinted with permission from Ref. [35]}.
 264 (C) The platform used for obtaining multidimensional signatures for proteins. (a), The MDS microfluidic device used for
 265 extracting a multidimensional characteristic signature of each analyte; (b), Schematic of the UV-LED fluorescence microscope
 266 {Reprinted with permission from Ref. [33]}. (D) Protein identification using the MDS device. (a)-(c), The ratio of the measured
 267 physical parameters. (d), The measured signals for each of the ten samples (A–J) were converted to estimates of their sequence-
 268 composition using the relationships outlined in panels (a)-(c) and the latter estimates were used to evaluate the probabilities of
 269 each of the ten samples being any one of the ten proteins in data set by using Gaussian mixture models {Reprinted with
 270 permission from Ref. [33]}.

271 To further avoid protein labelling with fluorophore, a label-free approach for MDS analysis of protein
272 is developed through direct detection of the intrinsic fluorescence of proteins [33,36]. The intrinsic
273 fluorescence of proteins is resulted from aromatic amino acids, such as tyrosine (Tyr) and tryptophan
274 (Trp). Zhang *et al.* [33] reported that the interdiffusion zone with proteins in a MDS device can be
275 directly observed using a home-built UV-LED microscope without any dye-labelling (Fig. 3C) [33].
276 The R_h of proteins can thus be obtained under their native state in solution. Moreover, by applying
277 emission filters, the fluorescent intensity of Tyr and Trp of a protein can be quantified separately. These
278 multidimensional physical properties of intrinsic fluorescence intensity and hydrodynamic radius show
279 unique fingerprints for protein identification (Fig. 3D).

280

281 4.2 Free-flow electrophoresis (FFE)

282 Apart from the diffusivity and R_h , protein surface charges are also important information for protein
283 analysis [37]. FFE is developed based on diffusional microfluidics to measure protein surface charges
284 by integrating an electric field into diffusional microfluidic devices. Unlike capillary electrophoresis
285 (CE) [38], the electric field is applied perpendicularly to the direction of the flow in FFE devices,
286 molecules travel perpendicular to the electric field [39-40]. The diffusion coefficient of protein can be
287 measured, in theory, using FFE based on the method described above. In addition, electrophoresis
288 measurements in FFE devices enable the calculation of electrophoretic mobility of a protein which can
289 be determined from the electrophoretic velocity and the effective electric field across the electrophoresis
290 channel without the need for reference molecules as mobility standards [41-45]. Consequently, the
291 relative effective charge of a protein can be derived with the measured diffusion coefficient using the
292 equation as below:

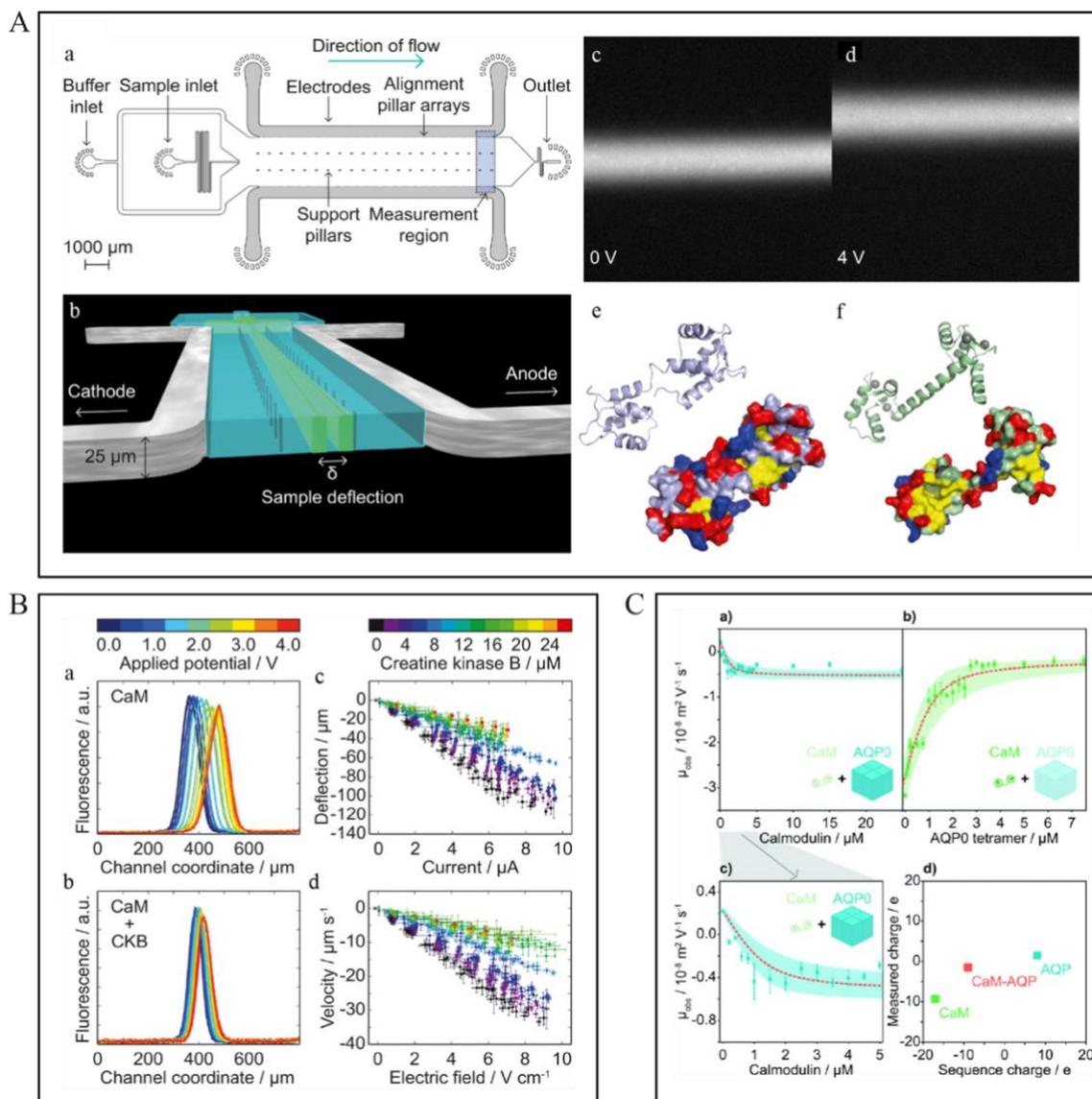
$$293 \quad \mu = \frac{v}{E_{eff}} = \frac{qD}{k_B T}$$

294 , where μ is electrophoretic mobility, v is electrophoretic drift velocity, E_{eff} is the electric field strength,
295 q is the effective charge, D is diffusion coefficient, k_B is the Boltzmann constant, T is temperature.
296 Comparing with conventional gel electrophoresis, FFE requires significantly smaller amounts of
297 samples. Moreover, proteins are studied at their native states without the interference of a solid
298 boundary or polymer matrix. Also, joule heat is negligible in a microfluidic device as it can be dissipated
299 efficiently due to the large surface to volume ratios [40-41]. The continuous nature of FFE provides a
300 possibility for high-throughput analysis of proteins [40].

301 Herling *et al.* [41] designed a FFE device in which the metal electrodes are in direct contact with fluid
302 flow within microfluidic channels. As shown in Fig. 4A, micro-pillar arrays are insert in the FFE device
303 to define the position of the electrodes within the channel, ensuring a homogeneous electric field within

304 the microchannel. The electric field is applied perpendicularly to the direction of the flow in FFE
305 devices. The flow of analytes occupies the centre of the microchannel and is flanked by streams of
306 buffer. The deflection (δ) upon the application of an electric potential is measured at the end of the
307 microchannel using fluorescence microscopy (Fig. 4A). The electrophoretic velocity, v , is calculated
308 based on the δ divided by the analyte residence time between the electrodes, which is known from the
309 flow rate through the device and the channel dimensions. E_{eff} across the device is equivalent to V_{eff}/w
310 (w is the width of the channel). Using Ohm's law, the V_{eff} across the solution was determined from the
311 buffer conductance and the measured current. The electrophoretic mobility (μ), thus, is given by the
312 slope of the plots of v against E_{eff} [41-45]. Therefore, the effective charge of protein can be determined
313 by the obtained electrophoretic mobility (μ) and a given diffusion coefficient (D) of analyte. Using this
314 FFE device, the effective charge of a charge-ladder family of mutant of calcium binding protein
315 calbindin D_{9k} was measured in solution under native conditions [42]. The same authors further [43]
316 investigated the interactions between calmodulin and creatine kinase using the FFE device. The change
317 of electrophoretic mobility of fluorescence labelled calmodulin upon titration of unlabelled creatine
318 kinase was monitored, which proved the formation of the complex of calmodulin and creatine kinase
319 (Fig. 4B).

320 Moreover, the combination of FFE and MDS can facilitate the charge analysis of unknown protein or
321 protein complex as their diffusion coefficient (D) in solution can be measured by MDS. Zhang *et al.*
322 [45] utilised the same FFE device to characterise the binding equilibrium between aquaporin (AQP0)
323 and calmodulin (CaM) by measuring the changes of electrophoretic mobility of AQP0 as function of
324 CaM concentration under intrinsic protein fluorescence (Fig. 4C). The diffusion coefficient of CaM
325 under different concentration of AQP0 was obtained using a MDS device as described in section 4.1.
326 Therefore, the effective charge of AQP0, CaM and AQP0-CaM complex was determined based on the
327 measured electrophoretic mobility and diffusion coefficient.



328

329 **Fig. 4** (A) (a)-(b), The scheme of FFE device. Integrated metal electrodes are shown in gray. Analytes deflect perpendicularly
 330 to the flow with applied electric field. The deflection of analytes is detected at the measurement region (measurement region)
 331 under fluorescence microscope. (c)-(f), Example of calmodulin 3D structure and its deflection at 0 V and 4 V {Reprinted with
 332 permission from Ref. [43]}. (B) Electrophoresis experiment that carried by FFE. (a)-(b), samples (CaM, CaM with CKB)
 333 deflection with applied voltage. (c)-(d), the sample deflection against current and sample deflection velocity against the electric
 334 field {Reprinted with permission from Ref. [43]}. (C) Investigation of the interactions between membrane protein (AQP0)
 335 and calmodulin using FFE by measuring electrophoretic mobility and charge. (a), The changes of electrophoretic mobility of
 336 AQP0 as a function of CaM. (b), The changes of electrophoretic mobility of CaM as a function of AQP0 concentration. (c),
 337 Expanded view of the data from a. (d), The measured and sequence charges for CaM, AQP0 and CaM-AQP0 {Reprinted with
 338 permission from Ref. [45]}.

339

340 4.3 Hydrodynamic focusing microfluidic mixer

341 As mixing at microscale is only contributed by diffusion, T-sensor and H-filter allow both temporal and
 342 spatial separation of proteins, which enables measurable fluid behaviour of proteins within a
 343 microfluidic device. However, it also means that the mixing efficiency within T-sensor and H-filter is
 344 low which limits their applications in areas where rapid mixing is required such as study of enzyme
 345 kinetics [46] and protein folding [47-48]. Hydrodynamic focusing microfluidic mixer is, thus,

346 developed based on T-sensors and H-filters to specifically increase the mixing efficiency for protein
347 analysis. It is typically achieved by introducing a middle inlet with analytes in a T-sensor or H-filter to
348 reduce diffusion path and increase the contact surface between fluids [49]. As shown in Fig. 5A and
349 Fig. 5B, the middle stream with analytes can be squeezed to a very small width (as narrow as 50 nm).
350 Reactants from the flanking flows, thus, can diffuse rapidly into the middle flow, leading to rapid
351 mixing. The width of the focusing flow is determined by α .

352

353

$$\alpha = \frac{P_s}{P_i}$$

354

355 , where P_s is the side flow pressure, and P_i is the middle inlet pressure. By adjusting the flow rate of
356 the middle inlet and the pressure of the flanking flows, the time for solvent mixing within the middle
357 flow can easily obtained below $10 \mu\text{s}$ [49]. The times scale is critical for studying rapid reaction kinetics
358 which cannot be achieved in a controllable manner by conventional mixing techniques [47-48].

359

360 Pollack *et al.* [47] fabricated an x-ray compatible hydrodynamic focusing microfluidic mixer device
361 with rapid mixing channel (Fig. 5C). With this design, the folding steps of the denatured state
362 cytochrome *c* has been studied by time-resolved x-ray scattering. Cytochrome *c* in pH 2 buffer is
363 introduced into the middle inlet and buffer at pH 7 is injected into the side channels, forming a thin
364 section with cytochrome *c*. Solvent molecules from the buffer and the protein flows mix rapidly within
365 the thin section and the pH of the protein flow, thus, increase to above 3 within $200 \mu\text{s}$. Comparing to
366 mixing technologies used in previous small-angle x-ray scattering (SAXS) studies, the resolution of
367 mixing time within the hydrodynamic focusing microfluidic mixer device has been increased by almost
368 2 orders of magnitude, allowing observation of protein folding process triggered by quick pH change.
369 Kratky plot (Fig. 5D) show that the state of denatured cytochrome *c*, at $150 - 500 \mu\text{s}$ after mixing with
370 buffer solution with high pH, both compact denatured and native states of cytochrome *c* are observed,
371 revealing that cytochrome *c* is one of the fastest folding protein.

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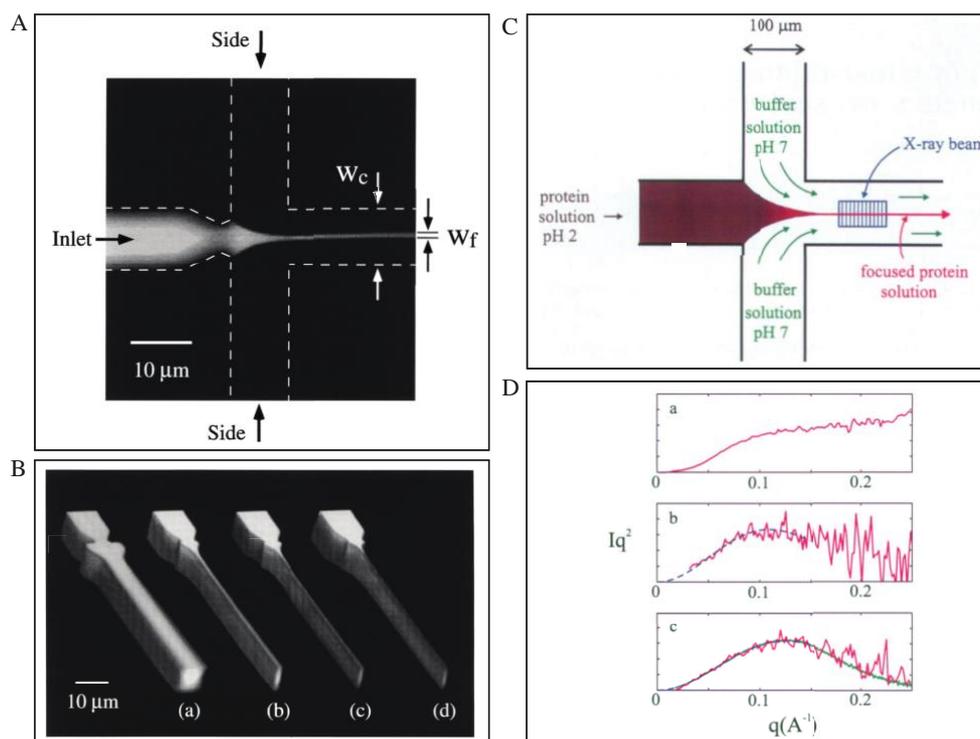


Fig. 5 (A) Hydrodynamic focusing: flow from the inlet channel was labelled by fluorescence dye while non-fluorescence labelled buffer flow from the side channel {Reprinted with permission from Ref. [49]}. (B) Hydrodynamic focusing with $P_i = 5$ *psi* and different values of α with (a) 0.5, (b) 1.0, (c) 1.1, and (d) 1.2 {Reprinted with permission from Ref. [49]}. (C) A schematic of the x-ray compatible hydrodynamic focusing microfluidic mixer {Reprinted with permission from Ref. [47]}. (D) Time-resolved Kratky plots of the data from three different positions in the device. (a) before mixing, (b) after 150 - 500 μ s mixing, and (c) after 10 ms mixing time {Reprinted with permission from Ref. [47]}.

5 Conclusion and Perspectives

Diffusional microfluidics, which involve co-flowing streams of analytes and buffer under laminar flow conditions, provides a platform to develop analytical techniques for detection and analysis of analytes such as protein, virus and bacteria. In this review, we have discussed the basis and the working principles of diffusional microfluidics. Three emerging analytical techniques that are based on diffusional microfluidics: microfluidic diffusional sizing (MDS), free-flow electrophoresis (FFE) and hydrodynamic focusing microfluidic mixer are highlighted. In addition, their application in protein analysis is discussed with selected examples which covers protein sizing, protein-protein interaction, protein separation and protein identification. Compared with traditional analytical techniques for protein analysis, such as dynamic light scattering and gel electrophoresis, diffusional microfluidic methods require significantly less samples yet provide higher sensitivity.

Wastewater-based epidemiology (WBE) has been consolidated as an effective tool to monitor public health and the outbreak of infective disease by measuring chemicals, biomarkers and/or pathogenic microorganisms in wastewater generated by people at community-level. To provide real-time information for WBE analysis, it requires analytical techniques that are high-sensitive, cost-efficient and high-throughput to analyse chemicals, biomarkers or pathogens. Thus, MDS, FFE and hydrodynamic focusing microfluidic mixer are promising analytical techniques for WBE. However,

398 since the three techniques currently mainly focus on protein analysis, one of the important future
399 directions for their application in WBE is to first extend their applications to direct detection and
400 analysis of pathogenic microorganisms and/or other biomarkers such as nucleic acids. In addition, due
401 to the complexity of wastewater in composition, another future direction of MDS, FFE and
402 hydrodynamic focusing microfluidic mixer should focus on development of multifunctional devices
403 that integrate sample purification, detection, analysis and data read-out modules to meet the requirement
404 of analysing the complex wastewater samples.

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407 **Declaration of competing interest**

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The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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417 **References**

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