

Tests on Prototype Pretensioned Natural Stone Beams

Wendel Sebastian¹, Steve Webb²

¹ *Department of Civil, Environmental and Geomatic Engineering, University College London, Chadwick Building, Gower Street, London WC1E 6BT, UK*

² *WebbYates Engineers, 48-50 Scrutton Street, London EC2A 4HH*

ABSTRACT

Stone has over millennia been used for structures which naturally develop compression under gravity loads. This study focuses on segmental stone beams with artificially induced compression. Prototype specimens were fabricated using epoxy adhesive for longitudinal shear transfer between prestressed steel strands and pre-cut Valange limestone blocks with mortar inter-block joints. Each specimen was prestressed by a single strand, to enable focus on the fundamental mechanics. Each strand was tensioned against the stone, then released after the epoxy became structurally active, so this is a form of pretensioning which eliminates external anchors and elastic shortening losses, and which enables agile construction because it can be implemented either at the factory or on site. Specimen details were informed by pullout tests. One specimen type entailed concentrically pretensioned square-section stone blocks, the other eccentrically pretensioned rectangular-section blocks. One concentric-strand specimen was strain-gauged near both ends to enable identification of the transfer zone, while an eccentric-strand specimen was instrumented at midspan with strain and displacement gauges to quantify pretensioning-induced camber and strains. Vibration tests were conducted on both specimens, then an eccentric-strand specimen was tested to ultimate in three-point flexure while a concentric-strand specimen was subjected to fire. The results reveal good damping, a high and consistent elastic modulus for the stone based alternately on local and global data, beneficial delay of cracks at the joints due to the pretensioning and protection of the epoxy by the stone over an extended period in fire. The ultimate limit state under load entailed gradual spalling of stone in the peak compression zone followed by a dominant asymmetric crack. These results strongly hint at the viability of pretensioned stone beams for low-carbon floor applications.

KEYWORDS : stone, prestressing, pretensioning, transfer zone, damping, fire, pullout, epoxy.

¹ Corresponding Author, Email Address : W.Sebastian@ucl.ac.uk

34 **1. Introduction**

35 *1.1 Stone and prestressing*

36 Much of the world's historic architectural heritage is testament to the successful use of stone in
37 construction over millennia. The structural integrity of cathedrals, bridges and other heritage stone
38 artefacts stems from the compression-dominated mechanics of their component arches, vaults,
39 walls, columns and flying buttresses, in turn predicated on stone's high compressive strength.
40 Heyman [1] emphasised this point by stating that, barring flexure, instability and stress raisers, a
41 typical construction stone column can exceed a mile in height before self-weight causes crushing.

42 Its excellent durability is another feature which renders stone eminently suited to heritage structures
43 and, more recently, to cladding [2]. This durability is evidenced by the wealth of heritage structures
44 (Stonehenge (UK), the rock-cut architecture of Petra (Jordan), Luxor Temple (Egypt), etc) which
45 have endured centuries of weathering [3]. London's iconic buildings such as St Paul's and
46 Westminster cathedrals along with 18th century churches by Sir Christopher Wren were built of
47 Portland Stone, a form of limestone which has withstood well the acute demands of the city's
48 complex environment [4]. Alongside this evidence from long-standing structures, laboratory tests
49 are crucial to assessing durability, for example to show that the compressive strengths of some
50 limestones exhibit a low sensitivity to freeze-thaw action [5], and to elucidate the role of stone
51 micro-fabric in durability [6]. More widely, multiple studies [7-10] have focused on the short-
52 term, long-term and fire behaviours of construction stones. In testing for mechanical properties,
53 the anisotropy of the stone due to the bedding planes at the quarries must be considered [11].

54 Owing to the shift towards construction of low environmental impact, there is a resurgence of
55 interest in natural stone as a low-carbon material for modern architecture. Stone requires only
56 extraction at the quarry followed by transportation to and assembly at site, without the need for
57 high energy, greenhouse gas emitting chemical transformations or treatments between source and
58 application [11]. Hence, the embodied carbon (kgCO₂/tonne) of limestone is about 30% and 93%
59 less than those of reinforced concrete (RC) and steel, respectively [3]. Limestone outperforms RC
60 and steel on durability, although steel sections for a given application may be lighter. Moreover it
61 is estimated that, globally, at the current rate of extraction there is an 850 million year reserve of
62 stone, and that this rate of extraction is probably exceeded by the rate of new stone formation in
63 the earth's crust [12]. Also, there is a wide perception of stone as an elegant material which lends
64 an aura of quality to the internal environments of buildings. Polished stone surfaces are eye-

65 catching, which removes the need for other materials to provide finishes when it is used indoors.
66 Consequently, structural uses of stone including staircases, floor toppings and cladding have gained
67 traction recently [11, 13-22]. Expo '92 in Seville showcased the Pavilion of the Future, which still
68 exists and which comprises 17.4 m diameter stone arches on steel trusses and 28 m high stone
69 columns, offering a blueprint for 21st century architecture.

70 Wider applications are inhibited by a lack of specific guidance in contemporary structural design
71 codes. Where the application entails flexure of the stone structure, reinforcing or prestressing
72 overcomes the nominal zero tensile strength of the joints between stone blocks and indeed the low
73 tensile strength of the stone itself (though this often exceeds the tensile strength of concrete). As
74 a result, ad-hoc structural testing of reinforced or prestressed stone structures has been conducted
75 [14, 15, 17, 19, 20]. The form of prestressing used to date is post-tensioning, with steel plates
76 anchored against the end faces of the stone to transfer the compression into the stone structure.

77 The present study considers use of prestressed stone beams for floor applications. Fig. 1(a) shows
78 a recent trial construction, now dismantled and to be re-assembled in a different layout in future for
79 testing at the UCL structural engineering laboratory. As can be seen, the trial structure comprised
80 two 12 m long post-tensioned limestone beams, with limestone slabs spanning 1.5 m transversely
81 between the beams. Post-tensioning is reversible as the strands can be de-tensioned, enabling re-
82 use of the stone. This is a sustainability benefit of post-tensioning.

83 In Fig. 1(a), the exposed steel plates and protruding strands seen at the near-ends of the stone beams
84 can be problematic if space at the beam-wall joint is limited. In such cases it is useful to conceal
85 the mechanism of strand-stone force transfer within the stone, leaving the end faces of the stone
86 members clear of any external anchorage. This concealment is an integral feature of pretensioning.

87 In its application to concrete the strands are tensioned before casting, thus pretensioning. Once the
88 concrete has cured sufficiently, the strands are released and their forces are transferred into the bulk
89 of the concrete via a thin concrete zone around the strands. Fig. 1(b) shows the strand force profiles
90 along the beam at the start and end of pretensioning. After release there is a transfer zone along
91 which the strand's tensile force, and so the concrete's equilibrating compressive force, increases
92 nonlinearly from zero at the ends to a peak at short distances inwards. Use of pullout and other
93 tests to study the transfer zone mechanics is at the core of pretensioned concrete research [23-29].

94 Note that for pretensioning to take root, it is not sufficient for the bulk concrete to have cured. The
95 concrete immediately surrounding each strand must also have cured, since it is this concrete which

106 acts as a longitudinal shear connector (enabling force transfer) between the strand and the bulk
107 concrete. Without curing of this concrete near the strand, there is no pretensioning even if the bulk
108 concrete further away has cured. This idea is fundamental to the stone application. An internal
109 strand-to-stone longitudinal shear connector is needed if the transfer mechanism is to be concealed
110 within the stone. Epoxy adhesives show good potential for this role. The epoxy can be poured wet
111 to flow along the hole, thereby occupying the space between the strand and the stone. On curing,
112 the epoxy develops good adhesion to the stone and possesses good compression / shear stiffness
113 and strength which are crucial to interaction with each released strand. Since the strand is tensioned
114 before the epoxy becomes structurally active, this is an example of pretensioning. It is important
115 to understand the transfer mechanics and the wider effectiveness of this application of pretensioning
116 for the stone-adhesive-strand system. That fact has motivated the study reported in this paper.

107

108 *1.2 Comparisons between pretensioning of stone and of concrete*

109 In elucidating the mechanics of pretensioned stone beams (PSBs), some important differences from
110 the more well-established pretensioned concrete beams (PCBs) should be noted, as follows :

- 111 1) For PCBs, external anchors fixed to a casting bed are needed initially to keep the strands
112 stretched, as the wet concrete cannot perform that role, while for PSBs the stone is used initially
113 to equilibrate the stretched strands, thus eliminating external anchors and reducing tool costs.
- 114 2) Hence PCBs can originate only at a factory, while PSBs are an agile form of construction,
115 implementable either at a factory or in-situ. Thus for remote sites where long PCBs cannot be
116 transported, short stone blocks can be transported in packs, sequenced and pretensioned in-situ.
- 117 3) PCBs exhibit elastic shortening losses (Fig. 1(b)) because the concrete shortens during *release*
118 of the strands, but PSBs don't because the stone shortens during *tensioning* of the strands.
- 119 4) PCBs proceed directly to the pretensioned state, while PSBs are first post-tensioned (when the
120 stone initially equilibrates the stretched strands) en route to the final pretensioned state.
- 121 5) The strand-to-beam shear connection is a uni-material system (the concrete) for PCBs, but is a
122 bi-material (epoxy-stone) system with an interface between the two materials for PSBs.
- 123 6) The pretensioning process is accelerated by steam curing the parent concrete material for PCBs,
124 and by using a rapid hardening epoxy for the shear connecting material in PSBs.

125

126

127

128 *1.3 Aim and objectives of the present study*

129 Prestressing has multiple benefits including precambering of the stone beam (to reduce dead and
130 live load deflections), counteracting the stresses induced in the beam by externally applied loads
131 (which can improve load capacity) and stiffening the beam (which is good for vibration behaviour,
132 etc) by using precompression to inhibit cracks at the mortar joints between stone blocks.

133 Hence the overall aim of this study is to demonstrate the successful fabrication and load testing of
134 pretensioned stone beams comprising Valange limestone blocks with mortar joints, prestressing
135 steel strands and epoxy adhesive as the strand-to-stone transfer element.

136 The specific objectives are to :

- 137 1) Illustrate an effective method of feeding the epoxy into the stone around the strands.
- 138 2) Use pullout tests to confirm the epoxy adhesive as an effective strand-to-stone shear connector.
- 139 3) Illustrate the mechanics of the transfer zone in the pretensioned stone members.
- 140 4) Demonstrate that these members show good vibration characteristics.
- 141 5) Compare elastic modulus values for the stone based on local and global measurements
- 142 6) Demonstrate the failure modes and load-carrying capability of the pretensioned beams.
- 143 7) Gain initial insight into the fire performance of this pretensioned strand-epoxy-stone system.

144 Now the standard pullout test entails an initially unstressed strand of arbitrary embedment length,
145 while a pretensioned beam entails an already tensioned strand with a distinct transfer zone. Hence
146 the pullout test doesn't quite mimic a pretensioned beam, but it is a simple test which gives a good
147 preliminary idea of the internal anchorage potential which is so fundamental to pretensioning.

148 With this in mind, the following strand-epoxy-stone specimen tests were conducted in this study:

- 149 1) Pullout tests on specimens of different embedment lengths.
- 150 2) Pretensioning, vibration and fire tests on square-section stone specimens with a concentric strand.
- 151 3) Pretensioning, vibration and failure tests on rectangular-section stone beams with an eccentric strand.

152 One strand was used per specimen, to enable a focus on the fundamental science. The concentric
153 strand specimens were used to elucidate the transfer zone mechanics, while the eccentric strand
154 beams enabled effects such as precamber to be assessed. In what follows the materials, specimens
155 and tests are discussed, then conclusions are drawn and avenues for future research are suggested.

156 2. Materials

157 Valange is an oolitic limestone quarried in the commune of Massangis, located in North central
158 France. It is off-white in colour, with veins and including fossil fragments, Fig. 2(a), (b). The
159 supplier quoted properties for Valange include a compressive strength of 73 N/mm^2 and modulus
160 of rupture of 7.5 N/mm^2 [30]. Samples weighed in the study reported in the present paper gave
161 a density of 2400 kg/m^3 . No elastic modulus was given by the supplier, but a value of 28.9
162 kN/mm^2 was deduced from the present study as described in Section 6.0 of this paper.

163 The adhesive used was a thixotropic two-part epoxy. The manufacturer (Parex) gives a pot life
164 of 25 mins at 20°C , compressive strength of 70 N/mm^2 at 7 days, tensile, flexural and slant shear
165 strengths of 26 N/mm^2 , 58 N/mm^2 and 55 N/mm^2 respectively, and a 3.6 kN/mm^2 elastic modulus
166 [31]. Parex walling mortar was used to make 4 mm thick mortar joints between consecutive
167 stone blocks in the specimens. The manufacturer's data for this mortar include a pot life of 45
168 mins, compressive strength of 35 N/mm^2 at 7 days and a 7 N/mm^2 flexural strength [31].

169 The prestressing steel was a seven-wire smooth surface strand of 15.7 mm diameter, 1860
170 N/mm^2 tensile strength, 150 mm^2 section area and a maximum force of 321 kN peak value.

171 In making one of the rectangular-section beams, a cartridge was used to inject the adhesive via
172 a side hole drilled into the mortar joint between the two middle stone blocks. This side hole ran
173 perpendicular to and intersected the main 20 mm diameter hole drilled longitudinally into the
174 stone blocks for feeding the prestressing steel strand through. Hence the adhesive travelled a
175 short distance (65 mm) along this side hole, then turned through 90° and flowed in both directions
176 along the main hole to fill the gap between the strand and the stone wall of the main hole. Some
177 adhesive would also have seeped into the pores of the stone through the wall of this main hole,
178 which would have provided the adhesive with some keying action into the stone.

179 Fig. 2(c) shows a short length of Valange stone which fractured off a beam specimen during a
180 failure test. Note the middle strip of a different colour, which is the hardened adhesive that
181 originally encircled the lower half of the steel strand and which (namely the adhesive) is still
182 embedded in the stone. The inclined grooves in the adhesive are from the wires of the strand,
183 which shows how closely the adhesive fitted around the strand. Overall the image shows that
184 the adhesive flowed into and cured well in the main hole, in the process developing good bond
185 with the stone. These are all testament to the success of the cartridge injection of the adhesive.

186

187 **3.0 Pullout tests**

188 *3.1 Setup and procedure*

189 The pullout tests were conducted using individual Valange stone blocks of 150 mm x 150 mm
190 square cross section. Four different embedment lengths were tested, namely 200 mm, 400 mm,
191 600 mm and 800 mm, henceforth named the P200, P400, P600 and P800 specimens respectively.

192 Fig. 3(a) shows the generic details at the pulling end. An open box fabricated from welded steel
193 plates was used to equilibrate the force from the jack which pulled on the strand, by transmitting
194 this force to the front face of the Valange stone block. To allow passage of the prestressing
195 strand, a hole was drilled through the front face plate of the box (against which the jack reacted)
196 and a horseshoe shape was cut out of the back face plate (which reacted against the stone) of this
197 steel box. A pancake load cell placed between the jack and the front face plate of the box was
198 used to measure the force from the jack. In addition, two L-shaped steel plates were bolted to
199 each other, effectively clamped, around the strand to form a T within the free space of the steel
200 box. Strand-stone slip at the pulling end of the block was measured by two displacement
201 transducers which at their back ends were fixed to the sides of the Valange block via magnetic
202 bases and bonded steel plates, and which at their front ends touched the outstanding arms of the
203 L-shaped plates. The pulling end slip was taken as the mean of the two transducer readings.

204 Fig. 3(b) shows the actual test setup for specimen P600. The hydraulic jack was activated by
205 manual pumping of oil from a nearby reservoir. During the test, the jack load was gradually
206 increased by steady pumping, while the load cell and transducer readings were recorded at 1 Hz
207 continuously into an electronic data acquisition system until failure occurred.

208

209 *3.2 Results and discussion*

210 In all cases the bond between the strand and adhesive failed, while the adhesive-stone bond
211 appears to have remained intact. For specimens P200 and P400 there were audible cracking
212 sounds as failure by significant strand-adhesive slip was approached. The left image of Fig. 4(a)
213 shows specimen P400 after failure, note the clear length of pulled out strand without adhesive.
214 For specimens P600 and P800 loud bangs were heard at ultimate. In addition splitting cracks
215 appeared along P600, see the right image of Fig. 4(a) which also shows a small truncated cone
216 of Valange stone pulled off at the front end of the block.

217 Fig. 4(b) shows the pullout force vs slip plots for all specimens. The plots show a high initial
218 stiffness followed by nonlinear behaviour and a ductile plateau for specimen P200, with a near
219 ductile plateau for specimen P400. Specimens P600 and P800 show sharp drops in load after
220 the peak, although P600 stabilised at high slip, showing a semblance of a ductility plateau.

221 Fig. 4(c) shows how the mean bond stress, defined as the quotient of the pullout force and the
222 bonded surface area of the bar along the entire embedment length, varied with slip for each
223 pullout specimen. It is evident that the peak mean bond stress is quite similar for all four
224 specimens, falling within a narrow range from 4.6 N/mm² for P400 to 5.5 N/mm² for P200.
225 Indeed, the entire pre-peak curves for P400, P600 and P800 closely resemble each other, with
226 that for P200 in good proximity to the others. Such consistency hints at good quality control on
227 both the materials and workmanship used to fabricate the pullout specimens.

228 Fig. 4(d) shows the pullout load capacity plotted as a function of embedment length. A linear
229 relationship is evident, with a mean gradient of 245 kN/m length of strand. Now pullout capacity
230 tends to level off beyond a threshold embedment length. Fig. 4(d) shows that this threshold was
231 not reached in the tests, suggesting that even more pullout capacity than the 196 kN achieved at
232 800 mm embedment length might've been possible at longer embedments. Further tests are
233 needed to establish this threshold embedment length, beyond which the mean shear bond stress
234 vs slip curves will drop relative to those shown in Fig. 4(c).

235 These pullout test results provided encouragement for taking the next step, namely to fabricate
236 Valange stone beams with a pretensioning level per strand of about 200 kN, which is about 70%
237 of the strand's characteristic maximum force.

238

239 **4.0 Transfer specimen**

240 *4.1 - Specimen setup and instrumentation*

241 Two concentrically pretensioned specimens were used to understand the transfer zone mechanics
242 of the strand-epoxy-Valange stone system. Fig. 5(a), (b) show the details of these specimens.
243 As can be seen, each specimen was of 150 mm x 150 mm square cross section, with a single
244 concentric prestressing strand, and 3.5 m long. This length was informed by the rough guide
245 which emerged from the pullout tests described above.

246 Each specimen was fabricated using five 700 mm long pre-cut Valange stone blocks. Mortar
247 joints, each 4 mm thick and comprising the mortar described previously, was used between stone
248 blocks. The mortar was left for a week to cure before the prestressing operation took place.

249 Fig. 5(a), (b) show that at multiple sections near both ends of one specimen, longitudinally
250 oriented strain gauges were placed at the centres of all four faces. This enabled the mean strain
251 at each such section to be evaluated, which in turn enabled plotting of the mean strain profile
252 along the block both at the strand stressing and strand release stages. The strain gauged section
253 labelled S1 in Fig. 5(a) will be focused on shortly in this paper. Meanwhile note that the use of
254 a single concentric strand was a move to try and ensure as near as possible uniform stress on
255 each section. Hence this specimen and instrumentation setup were ideally suited to
256 understanding the transfer zone mechanics for this pretensioned system.

257

258 *4.2 - Pretensioning operation*

259 Fig. 5(c), (d) show the pretensioning setup. Fig. 5(c) in particular also shows the strain gauges
260 already installed at the black taped locations. The 7-wire strand had already been fed through
261 the 20 mm diameter hole pre-drilled through the blocks. At the near-end in Fig. 5(c), it is evident
262 that the strand has been locked into place by a barrel-and-wedge system which in turn reacts
263 against two thick steel plates with large diameter studs between them. The outer plate directly
264 equilibrated the load coming through the barrel, while the inner plate distributed the load in
265 bearing to the end face of the stone specimen via a thin rubber pad. Fig. 5(d) shows the pulling
266 end, which was similar except for the presence of the jack and the load cell.

267 The pretensioning operation progressed at the jacking end in four key stages, as follows :

- 268 1) Zero all strain gauges, then set the data logger to record strains and loads at 1 Hz continuously.
- 269 2) Tension the strand by loading the jack using a manual pump connected to an oil reservoir.
- 270 3) On reaching 200 kN jack load, drive the wedges firmly into the barrel to grip the strand.
- 271 4) The jack is unloaded to release (and hence de-tension the exposed length of) the strand.

272 Fig. 6(a) shows the strain vs jack force plots for section S1 identified in Fig. 5(a). Three key
273 conclusions from this plot are as follows :

- 274 1) After an initial nonlinear bedding-in regime at low loads, the behaviour was linear.

275 2) Three faces developed similar strains, the fourth face developed only 14% less strain than the
276 others. This justifies an assumption of uniform mean strain at the section.

277 3) The unloading lines were linear and parallel for all four strains.

278

279 The dashed lines of Fig. 6(a) show how the mean of the four strains at S1 varied during both
280 loading and release stages. Later in this paper this plot, which represents local elastic behaviour
281 of the Valange stone, will be used to estimate an elastic modulus value for the material.

282 After release, the epoxy adhesive was then pumped into the longitudinal hole in the stone around
283 the strand, left to cure for ten days and finally the strand was completely de-stressed by slightly
284 and gradually pulling on the strand with the jack so that the barrel-and-wedge system could be
285 dismantled. At that stage all of the force was transferred from the strand to the stone via the
286 cured adhesive connection along this hole occupied by the strand in the stone. Data logging
287 continued for some time after initial transfer.

288 Fig. 6(b) shows the final mean strain profile (using the absolute values of the strains) recorded
289 along the specimen. Two key points from this plot are as follows:

290 1) There is some asymmetry about the specimen's mid-length and the reason for the slightly
291 higher strain near mid-length is not clear, but these deviations from the ideal are modest and
292 the plot overall shows a strong semblance to a uniform specimen's strain profile at transfer.

293 2) The left and right sides show transfer lengths of 600 mm and 800 mm respectively. For
294 comparison with concrete, it may be noted for example that transfer lengths of 582 mm and
295 463 mm were obtained for 12.7 mm diameter, seven-wire strands pretensioned to 184 kN jack
296 load in concretes of compressive strengths 23 N/mm² and 36 N/mm² respectively [29].

297 These results confirm that pretensioning based on use of an epoxy adhesive as the longitudinal
298 shear connector between the strand and the stone was successful. The transfer lengths are
299 reasonable for a realistic level of strand pretensioning force (namely 70% of the characteristic
300 ultimate force that the strand can carry), and the final release strain profile suggests that both the
301 epoxy adhesive shear connector and the stone may be regarded as homogenous.

302

303 *4.3 Vibration tests*

304 The strain gauged pretensioned specimen was supported near its ends and excited by thumping
305 it with a mallet at midspan. A short length of timber was used at midspan to soften the blow and

306 avoid breaking off pieces of the stone. Data logging of the strain gauges at 1.2 kHz started just
 307 before thumping and continued for 30 s after thumping, to capture the impulse response.

308 Fig. 7(a) shows the strain vs time plot for a gauge near midspan. A Fast Fourier Transform of
 309 the data is shown in Fig. 7(b), revealing a clear fundamental natural frequency of 19.9 Hz, which
 310 is used later in this paper as a global basis for estimating the elastic modulus of the stone.

311 The positive amplitude points in Fig. 7(a) were plotted against their corresponding times. The
 312 result is Fig. 7(c). Note also the best-fit exponential curve drawn through the points. The
 313 logarithmic decrement, δ , which reflects the rate of decay of the oscillations, is defined as [32] :

314

$$315 \quad \delta = (1/N) \ln(X_0/X_N) \quad (1),$$

316

317 where X_0 and X_N are amplitudes of motion separated by N cycles. Now using the equation of
 318 the exponential approximation as given on Fig. 7(c), if the times of occurrence of the amplitudes
 319 are t_0 and t_N respectively, then the following apply, namely :

320

$$321 \quad X_0 = 34.244 e^{-4.695t_0} \quad \text{and} \quad X_N = 34.244 e^{-4.695t_N} \quad (2)$$

322

323 Combining Eqns (1) and (2) leads to the following, namely :

324

$$325 \quad \delta = 4.695(t_N - t_0) / N \quad (3),$$

326

327 Now between the start and end of the plot as presented in Fig. 7(c), $N = 8$ and the time interval
 328 $(t_N - t_0)$ is 0.409167 s. These numbers lead to a δ value of 0.24013. Then, the following equation
 329 relates the specimen's damping constant, ζ , to the logarithmic decrement, namely [32] :

330

$$331 \quad \zeta = \delta / [4\pi^2 + \delta^2]^{1/2} \quad (4)$$

332

333 Using $\delta = 0.24013$ in this equation gives a damping constant of 3.8%. Fig. 7(c) also shows the
 334 amplitude decay and associated best-fit exponential plots based on the strain vibration data for
 335 the instrumented eccentric-strand specimen discussed later in this paper. Processing of these

336 latter plots as above gives a damping constant of 3.5%, showing good consistency with the above
337 value.

338

339 *4.4 Fire testing*

340 Fig. 8(a) shows the specimen being subjected to a preliminary fire test outdoors. This was done
341 after the above pretensioning operation and vibration test had been conducted. As can be seen,
342 the specimen was supported near its ends at height, with the middle block subjected to fire from
343 a drum directly below it. The fire was fuelled with wood thrown in via the top of the drum and
344 air fed from an airline through a pipe at the base of the drum. The test lasted almost 2.5 hours.

345 No explosive failure of the prestressed specimen was observed throughout the test. At about 85
346 minutes into the test longitudinal cracking was observed on the top face of the middle block, see
347 Fig. 8(b). Soon after these cracks were first seen, an extra thin flame was observed to pour out
348 of the top crack. This suggests that the crack had extended from the surface to the central hole,
349 in the process creating a path for burning of the epoxy from within that central hole to emerge
350 at the top surface. It may be that the similar crack on the bottom face of the stone had also
351 extended to the hole at the core, thereby providing a direct, uninhibited path for the heat of the
352 flame to have accessed and burnt the epoxy. In order to better understand this occurrence, future
353 work may consider the fire-induced thermal stresses in the stone that lead to such cracking.

354 After the test was over, an approximately 2 mm thick layer was found to have peeled off the
355 bottom face of the middle Valange block which was directly above the fire, Fig. 8(c). Observe
356 also the longitudinal crack on that face, which might've channelled the heat of the flame directly
357 up to the epoxy. Finally, the portions of stone which were directly above and near the fire were
358 broken up with a big hammer to reveal samples of stone, e.g. Fig. 8(d), containing the epoxy
359 adhesive around the strands at the core of the cross section. It is seen that the lower part of the
360 right hand sample (which was nearer the fire) experienced burning of the adhesive, and also that
361 a short length over the upper part of that sample shows the adhesive changing colour from its
362 original white to a yellow-orange, indicating that this short length of adhesive too was near
363 burning. The sample of Valange on the left of the photo shows adhesive exhibiting a healthy
364 white resin colour, hence this portion of adhesive remained intact throughout the fire.

365 Fig. 8(e) shows the temperature variations recorded from the middle Valange block (which was
366 directly above the fire), using high temperature-resistant thermocouples placed at two locations

367 of the block as shown on the diagram drawn within the plot. It is seen that one thermocouple
368 was placed just under the surface of a vertical face of the block, while the other thermocouple
369 was located about 5 mm above the core longitudinal hole in that block. Henceforth these near-
370 surface and near-core thermocouples will be referred to as NS and NC respectively. In future,
371 the NC thermocouple could be placed just *below* the core, in the direct path of heat coming
372 upwards from the fire through the stone, while the NS thermocouple could be placed just above
373 the bottom face where higher temperatures would very likely be experienced. The following
374 points emerge from Fig. 8(e) :

- 375 1) The NS temperature started rising rapidly after only 2 minutes, while NC started rising at a
376 much lower rate and only after 10 minutes when NS had already exceeded 210°C.
- 377 2) The NS temperature then rose nonlinearly up to a peak of 700°C after about 1.75 hours, while
378 the NC temperature rose almost linearly up to a peak of 480°C after circa 2.25 hours.
- 379 3) The NC temperature continued to rise even for another 20 minutes after the NS temperature
380 dropped towards the end of the test, because there was still heat flow from the surface through
381 the material to the core.
- 382 4) After almost 2 hours the NS temperature started to fall owing to exhaustion of the wood fuel,
383 but the internal (NC) temperature continued to rise. After 2.25 hours when the test was
384 concluded, the NS temperature had dropped to about 100°C. At this stage water was thrown
385 over the specimen, inducing a thermal shock which exacerbated the above cracking and
386 peeling.
- 387 5) The sudden and large drop in NS temperature about 40 minutes into the test was resolved by
388 feeding more wood fuel to resurrect the fire.

389 That the inside of the stone, including the adhesive at its core, lagged so much behind the outside
390 in temperature means that the Valange stone served as a good insulator. Further tests should be
391 conducted to establish minimum surface-to-adhesive distances needed to protect the adhesive,
392 as a function of the surface temperature in fire.

393

394 **5.0 BEAM SPECIMENS**

395 *5.1 – Beam specimen setup and instrumentation*

396 Two eccentrically pretensioned beam specimens were fabricated and tested. One of the beams was
397 strain gauged as shown in Fig. 9. Key features of the beams and instrumentation are as follows :

- 398 1) Each beam was of 150 wide x 300 mm deep section, and 4220 mm long, made by sequencing six
399 Valange blocks each of 700 mm length with 4 mm thick mortar inter-block joints.
- 400 2) The single strand was at 50 mm eccentricity below the centroid of the section. In theory this
401 created a pretensioning stress distribution entailing zero stress at the top of the section and
402 maximum compressive stress at the base. The target pretensioning strand force was 200 kN.
- 403 3) Three blocks were strain gauged (see below), each at its mid-length.
- 404 4) On one of the blocks adjoining midspan, longitudinal strain gauges were placed at three different
405 levels, namely on the soffit (SG1), at mid-depth (SG2, SG3) on both vertical faces and near the
406 top (SG5, SG6) also on both vertical faces. The net strain at each of the two highest levels was
407 taken as the mean of the readings from the two gauges at that level.
- 408 5) Gauge SG6 was placed on the soffit of the block on the other side of midspan, to enable checks
409 on symmetry of load response by comparison with readings from gauge SG1.
- 410 6) One end block was strain gauged (SG7, SG8) at mid-depth on both vertical faces, to provide
411 results for comparison with the gauges (SG2, SG3) placed at the same level on the block near
412 midspan during the pretensioning operation.

413 The beams were first pretensioned using the same operation previously described for the square
414 section, concentric-strand specimens, with one minor exception. While for the concentric-strand
415 specimens only one pulling cycle was used to anchor the strand force against the end stone block,
416 for the eccentric-strand specimens two pulling cycles were used. This is discussed further below.

417 In what follows, results are presented for the pretensioning operation on the strain-gauged beam,
418 after which the failure mode and load under three-point bending are discussed for the beam which
419 wasn't strain gauged, and finally the behaviour of the strain-gauged beam up to advanced stages
420 of nonlinearity also under three-point bending is discussed.

421

422 5.2 Pretensioning operation

423 As for the square section, concentrically prestressed specimens, the pulling jack force and strain
424 gauge readings were recorded at 1 Hz during the prestressing operation. The upward deflection at
425 midspan due to the eccentricity of the pretensioning force was also recorded. Fig. 10(a) shows how
426 this upward movement at midspan varied with jack force. There is pronounced nonlinearity up to
427 about 100 kN force, possibly due to friction within the system, then linear behaviour up to the peak
428 force of 180 kN. At this point the wedges were driven back into the barrel at the jacking end so as
429 to grip the strand at that end, following which the jack was unloaded. The plot shows that during

430 this unloading phase the deflection dropped nonlinearly as a function of jack force (due to draw-in
431 of the strand within the barrel-wedge system), losing about 30% of the peak deflection when the
432 jack was fully unloaded. In an attempt to increase the residual upward midspan deflection further,
433 the jack was reloaded, this time up to 200 kN. Fig. 10(a) shows that, during this final pull, the
434 deflection remained unchanged until the vertical reloading line intersected the original loading
435 characteristic, at which point the deflection started to increase again because the wedges were
436 loosened from the barrel, removing their grip on the strand. This second load-deflection curve is
437 seen to have been palpably steeper than its predecessor. Then the wedges were again driven in and
438 the jack was unloaded a second time, again producing a nonlinear unloading characteristic.
439 Although the second peak jack load exceeded the first by about 10%, the second (and final) residual
440 deflection exceeded the first by only 5%.

441 Fig. 10(b) shows that the variations with jack force of the mean strains at the three gauged levels
442 near midspan broadly follow that of the midspan deflection. Also, Fig. 10(b) confirms that this
443 phase of the below-centre eccentric prestressing operation did achieve the desired outcome of peak
444 compressive strain on the section at the base of the beam, modest compressive strain at mid-depth
445 and low compressive strain near the top. No cracking / crushing of the mortar joints was observed.

446 Now once the second pulling operation was complete, the adhesive was injected into the beam
447 around the strand and left to cure over 10 days. At the end of the curing period, the barrel-wedge
448 system at the pulling end was gradually loosened to enable transfer. Fig. 10(c) shows the variation
449 over time of all recorded strains, from not long before the wedges were released up to 30 minutes
450 later, well after the wedges were released and equilibrium was attained at the transfer stage. The
451 wedges were released circa 5 minutes (300 s) into the plot. It is seen that wedge release affected
452 none of the gauge readings from the midspan zone, but led to distinct changes in the SG7, SG8
453 gauge readings from near the ends because these latter gauges were in the transfer zone. The plot
454 shows that there was subsequently only marginal creep of the SG7 / SG8 readings, to values which
455 stabilised by the end of the plot. Overall, there was roughly a $50 \mu\epsilon$ change in strain at 350 mm
456 from one end of the beam at transfer. This modest change, along with the almost zero strain change
457 at midspan, points to a very effective epoxy adhesive shear connection between the strand and stone.

458

459 5.3 *Failure mode in three-point bending*

460 Of the two eccentrically pretensioned specimens the one which was not instrumented, except for the
461 presence of the load cell, was loaded to failure in three-point bending. Fig. 11(a) shows the test

462 setup. Cracking of the mortar joint between blocks at midspan was first observed at about 40% of
463 the failure load. This delay of the cracking (relative to zero cracking load for no prestressing) is
464 clearly beneficial to serviceability behaviour in practice. Fig. 11(b) shows that the mode of failure,
465 which occurred at 52 kN, was asymmetric about midspan. It was defined by a single dominant crack
466 which progressed from the midspan loading location at an inclination through the nearest Valange
467 block, until this crack reached the level of the strand, at which point it propagated almost
468 horizontally to the near end of the beam. In effect, the strand-adhesive system served as a defect
469 which triggered the horizontal crack. Fig. 11(b) also shows spalling of a large chunk of Valange
470 stone in the flexural compression zone under the midspan load. These features suggest a combined
471 flexural-shear failure of the beam. Also, that the crack propagated undisturbed across blocks is
472 testament to the high degree of continuity provided between blocks by the strand and the mortar
473 joints. This form of failure crack has previously been reported for reinforced concrete block
474 masonry beams [33]. Future studies may consider whether the formation of this crack might be
475 delayed using internally anchored vertical bars within the stone blocks.

476 As Fig. 11(c) shows, at midspan, towards failure pronounced separation (cracking) was observed at
477 the left mortar - stone block interface near the base of the beam. Higher up this mortar joint the
478 mortar-stone interface remained broadly intact and no crushing of the mortar was observed. In Fig.
479 11(c), the vertical strand was part of the loading setup at midspan, right next to the mortar joint of
480 interest, hence its appearance and the oblique angle of the image.

481 The instrumented beam was similarly loaded in three-point bending. For this test from the unloaded
482 state up to an advanced stage of loading into the nonlinear regime, Fig. 12 shows the variations with
483 time of the total strains recorded from gauges SG4 and SG5 in Fig. 9, which were on opposite
484 vertical faces near the top of one stone block adjacent to midspan. It is seen that at the start of the
485 test there was the residual compressive strain of about $45 \mu\epsilon$ from the prestressing operation. As
486 the load applied to the beam increased, the compressive strains increased nonlinearly with time. A
487 disparity between the strains on Fig. 12 is evident, with SG4 having been about 20% less than SG5
488 towards the end of the recording period. Now Fig. 10(c) shows that the strains at these two locations
489 were almost identical during the pretensioning operation, when the force in the strand was
490 symmetric with respect to the width of the specimen. This suggests that the stone material was
491 homogenous across the width of the gauged block. Hence, the across-width asymmetry evident
492 from Fig. 12 may have been due to uneven loading across the width of the beam rather than to
493 material asymmetry across the same.

494 Fig. 12 shows that SG5 recorded compressive strains up to 1100 $\mu\epsilon$. If the stone was within its
495 linear regime of behaviour at that strain value, and assuming the mean elastic modulus of 28.9
496 kN/mm^2 deduced in the next section, this strain corresponds to a longitudinal stress of about 32
497 N/mm^2 , which approaches half the stated 73 N/mm^2 compressive strength of the Valange stone.

498

499 **6.0 Estimates of elastic modulus of Valange stone**

500 As stated earlier, prestressing improves serviceability performance by precambering and by
501 enhancing section stiffness through crack reduction or elimination. Thus, quantification of the
502 stone's elastic modulus is important. In what follows, some of the test data presented above are
503 used to estimate this modulus. Crucially, these estimates are based alternately on local and global
504 aspects of structural action. Both the square section concentric-strand and rectangular section
505 eccentric-strand specimens are used, to illustrate the consistency of the results across specimens.

506 *6.1 Global estimates*

507 Two elements of data were used to estimate global elastic modulus values for the Valange stone.
508 One was based on the midspan deflection of the rectangular section specimen due to the eccentric
509 pretensioning force. The other relied on the natural frequency of the concentric-strand specimen.

510 During the jacking operation on the strand, the below-centroid eccentricity of the pretensioning
511 force induced a negative section moment that in turn precambered the rectangular section specimen.
512 Recall that the associated upward deflection was measured during the test and is plotted against the
513 jacking force in Fig. 10(a). Since the measurements started when the jacking operation began, self-
514 weight deflections are excluded. For the purposes of the present calculation it is the linear zone,
515 and hence upper part of the first pull operation on the plot of Fig. 10(a), which is of interest. Assume
516 that throughout the beam, i.e. globally, E and I are the elastic modulus of the Valange stone and the
517 second moment of area of the uncracked stone section respectively, with L being the span of the
518 beam, P is the pretensioning (jacking) force and e is the eccentricity of this force with respect to the
519 section centroid. For a midspan deflection of Δ_{mid} , and recalling that $M = Pe$, beam theory gives :

520

$$521 \quad \Delta_{\text{mid}} = ML^2 / (8EI) = PeL^2 / (8EI) \quad (5),$$

522

523 Which may be re-written as follows :

524

525

$$E = (P/\Delta_{mid})(eL^2/[8I]) \quad (6)$$

526

527 In the present approach (P/Δ_{mid}) is taken as the gradient of the line joining points of ordinates
528 110 kN and 170 kN on the first rising characteristic of Fig. 10(a), while $e = 50$ mm, $L = 4220$
529 mm, and $I = 150 \times 300^3 / 12 = 3375 \times 10^5$ mm⁴. Quantifying that linear gradient from the plot,
530 then inserting this gradient and the values of the other symbols into Equation (6) leads to an E
531 value of 28.8 kN/mm². This calculation assumes that the mortar joints made for full continuity
532 between the Valange stone blocks, which is justified by the plots of Fig. 10(b) indicating
533 compression through the entire depth of the stone section and the stiffness of the mortar joints.

534 The second global estimate of E uses the natural frequency of the square-section specimen
535 consistent with the plot of Fig. 7(b). The following expression applies to the first natural
536 frequency (pertinent to the half sine wave mode shape) of a beam of uniform mass per unit length:

537

538

$$f = (\pi/2) [EI/(qL^4)]^{0.5} \quad (7),$$

539

540 where f is natural frequency, E , I and L have their previous meanings, while q refers to the mass
541 per unit length. This may be re-written to give :

542

543

$$E = (4f^2/\pi^2)(qL^4/I) \quad (8)$$

544

545 Now Fig. 7(b) gives $f = 19.9$ Hz, while $I = 0.15^4/12 = .0000421875$ m⁴, $q = 2400 \times 0.15^2 = 54$
546 kg/m, and in this case the supports were moved short distances in from the ends to ensure the
547 vibrating member didn't fall of either support, giving $L = 3.45$ m. These numbers into Equation
548 (8) lead to $E = 29.1$ kN/mm².

549

550 6.2 Local estimates

551 The locally-based estimates of E are predicated on the section strains recorded from the
552 instrumented concentric-strand and eccentric-strand specimens during their pretensioning
553 operations. First, recall Fig. 6(a), which shows for the concentric-strand specimen how the mean of

554 four strain gauge readings (one per face) at one section developed with jack force. Again the
555 gradient of the linear, and hence upper part of the plot applies. If on this linear portion a strand force
556 increment P induces a mean strain increment ε , then assuming a constant section area A the
557 following applies:

558

$$559 \quad P = AE\varepsilon \quad (9),$$

560

561 which, on re-writing, gives:

562

$$563 \quad E = (P/\varepsilon) / A \quad (10)$$

564 (P/ε) is taken as the gradient of the line joining points of ordinates 40 kN and 180 kN on the rising
565 portion of Fig. 6(a). Along with $A = 150^2 = 22500 \text{ mm}^4$, an E value of 28.4 kN/mm^2 is obtained.

566 Finally, recall that Fig. 10(b) shows strain variations with jacking force for three levels within the
567 stone section for the eccentric-strand specimen during the jacking stage of pretensioning. The strain
568 at the base of the beam (SG1) was the largest of the three and so is used here as it very likely
569 incorporated the least error. At the risk of repetition, the linear upper zone of the SG1 plot is
570 relevant. Now assuming the section of be of depth d , this strain gauge SG1 was at distance $d/2$
571 vertically from the section's centroid. So using beam theory and the symbols with their meanings
572 as above, the following equations for the stress σ_b and strain ε_b at the base of the beam apply:

573

$$574 \quad \sigma_b = E \varepsilon_b = P[1/A + ed/2I] \quad (11),$$

575

576 which, on re-writing, gives the following equation for E as a function of the other parameters:

577

$$578 \quad E = (P/\varepsilon_b) [1/A + ed/2I] \quad (12)$$

579

580 Now (P/ε_b) is taken as the gradient of the line joining the points with ordinates 40 kN and 140 kN
581 on the first rising characteristic for SG1 on Fig. 10(b), while $A = 150 \times 300 = 45000 \text{ mm}^2$ and $d =$
582 300 mm , with e and I assuming their values (in mm and mm^4 units respectively) as stated earlier for
583 this rectangular section beam. The result is an E value of 29.4 kN/mm^2 .

584

585 6.3 Discussion of results

586 Table 1 summarises the E values obtained by the four different calculations listed above. As shown,
587 a mean E value of 28.9 kN/mm² and a CoV of only 1.3% are the results. These results emerged
588 from local and global data, from both the concentric-strand and eccentric-strand specimens, and
589 from both vibration and quasi-static test data. In future these tests may be backed up by axial tests
590 on instrumented cylindrical Valange stone specimens. The consistency of these results hint at the
591 validity of assumptions such as undisturbed continuity provided by the mortar joints between
592 Valange stone blocks, which in turn points to the high effectiveness of the pretensioning operation
593 in fully compressing these mortar joints made of material of good stiffness.

594 This elastic modulus value of 28.9 kN/mm² for Valange limestone from France sits between the
595 values of 13.9 kN/mm² found for Sanliurfa limestone from Turkey [5] and 62.3 kN/mm² found
596 for Piobbico-Cesana limestone from Italy [7]. It also sits within the narrower range between values
597 of 27.1 kN/mm² and 38.3 kN/mm² found for two different types of sandstones [7]. More widely,
598 the elastic modulus can vary significantly for different versions of nominally the same form of stone,
599 e.g. values of 10.48 kN/mm² and 57.1 kN/mm² have been given for different marbles in separate
600 studies [7, 19]. For the Valange limestone, axial tests on strain gauged cylinders will be useful for
601 gathering statistically significant data on the full-range constitutive behaviour in compression, from
602 which properties such as elastic modulus may be further quantified with confidence.

603

604 7.0 Conclusions and Further Work

605 In this study, four Valange stone beams with mortar joints have been successfully pretensioned
606 using steel strands internally anchored within the stone by a two-part epoxy adhesive. Further
607 work should be done to establish whether the specific outcomes of this study as presented below
608 are more widely applicable.

- 609 1) The use of cartridges to inject the adhesive from small side holes in the mortar joints between
610 Valange blocks enabled good flow of this adhesive along distances up to 2 m around the
611 prestressing strands. Samples of stone from failed specimens revealed excellent cured
612 adhesive which had bonded well to the stone and had packed tightly around the strands' wires.
- 613 2) Pullout specimens failed by strand-adhesive slip which was ductile for the shorter (200 & 400
614 mm long) specimens, with a peak pullout load of 196 kN for the longest (800 mm) specimen.
615 These values gave confidence in use of the adhesive for pretensioning the stone beams.

616 3) Strains recorded in this study from the stone during concentric-strand pretensioning revealed
617 transfer lengths of 600 mm and 800 mm. This should be compared with transfer lengths of
618 almost 600 mm and 500 mm obtained in previous studies, for strands of 20% less diameter
619 used to pretension concretes of 23 and 36 N/mm² compressive strengths.

620 4) Vibration tests revealed 3.5% and 3.8% damping for both concentrically and eccentrically
621 pretensioned specimens respectively. This level of damping is useful for floors in buildings.

622 5) A mean elastic modulus of 28.9 kN/mm² was estimated for the Valange stone along the spans
623 of the specimens. This modulus value was highly consistent between estimates based on local
624 (strain) and global (deflection) test data, for both the concentric-strand and eccentric-strand
625 specimens, and from both the quasi-static pretensioning operation and the vibration tests.

626 6) Fire testing was conducted on a 150 mm x 150 mm square section concentric-strand
627 specimen. The near-surface temperature rose nonlinearly to 700°C after 1.75 hours while the
628 temperature near the centre rose slowly and linearly after a delayed start (relative to the near-
629 surface) to 480 °C after 2.25 hours. Peeling of the stone and longitudinal cracks on the
630 surfaces were observed. The stone did not fail explosively. Burning of the adhesive seems
631 to have started well after an hour and stopped at short distances away from the fire. Larger
632 stone sections may insulate the epoxy even better, towards meeting fire safety regulations.

633 7) For the specific eccentric-strand specimen tested in this study, three-point bending led to
634 failure by spalling of compression stone at midspan and by formation of a dominant
635 asymmetric crack which propagated through the stone from midspan, first at an inclination
636 and then horizontally on reaching the level of the strand in the stone blocks. Cracking at the
637 midspan mortar joint was delayed to about 40% of the peak load, a clear benefit of the
638 pretensioning. Repeat tests are needed to establish whether this failure mode occurs
639 consistently.

640 8) The use of concentric-strand, square section specimens to identify transfer zones and
641 eccentric-strand, rectangular section specimens to elucidate the combined effects of
642 pretensioning and external loads, including the effects of the mortar joints between blocks, is
643 recommended for study of pretensioned beams comprising blocks of other types of stone.

644

645 Future work may extend to multi-strand specimens covering longer spans. Within such studies,
646 it would be useful to investigate whether strategies such as internally anchored vertical bars may
647 be successful at inhibiting flexure-shear failure under different load types. Development of
648 design principles from such work would provide the basis for safe, wide application of this
649 promising form of low-carbon floor construction.

650 8. References

- 651 [1] Heyman J. The Stone Skeleton. *Int. J. Solids Structures*, 1966, Vol. 2, 249-279.
- 652 [2] Hamoush S, et al. Development of sustainable engineered stone cladding for toughness,
653 durability, and energy conservation. *Construction and Building Materials*, 2011, 25, 4006-4016.
- 654 [3] Khatib J. *Sustainability of Construction Materials*, 2016, 742 pp, Woodhead Publishing, 2nd
655 Edition, ISBN 978-0-08-100995-6.
- 656 [4] Lott G. Sourcing stone for the conservation and repair of historical buildings in Britain.
657 *Quarterly Journal of Engineering Geology and Hydrogeology*, 2013, 46, 405-420.
- 658 [5] Turgut P, Yesilnacar MI, Bulut H. Physico-thermal and mechanical properties of Sanliurfa
659 limestone, Turkey. *Bulletin of Engineering Geology and the Environment*, 2008, 67, 485-490.
- 660 [6] Török Á, Příkryl R. Current methods and future trends in testing, durability analyses and
661 provenance studies of natural stones used in historic monuments. *Engineering Geology*, 2010,
662 115, 139-142.
- 663 [7] Sorace S. Long-term tensile and bending strength of natural stones. *Materials and Structures*,
664 August / September 1996, Vol. 29, 426-435.
- 665 [8] Yates T, et al. Changes in engineering properties of natural stone. *Proc. ICE, Construction*
666 *Materials*, 2012, 165(3), 127-133.
- 667 [9] Karaca Z, Onargan T. A new approach to stone deformation : stone deformability index. *Proc.*
668 *ICE, Construction Materials*, 2012, 165(3), 189-195.
- 669 [10] Ozguven A, Ozcelik Y. Investigation of some property changes of natural building stones
670 exposed to fire and high heat. *Construction and Building Materials*, 2013, 38, 813-821.
- 671 [11] Boote S, Lynes A. Stone as a structural material. Part 1: Mechanical properties. *The Structural*
672 *Engineer*, March 2020, 20-25.
- 673 [12] Stone Federation Great Britain. *Natural stone, the oldest sustainable material*. 2011,
674 Publication Number SUS01/11.
- 675 [13] Blanchard I. The use of natural stone for internal flooring. *Proc. ICE, Construction Materials*,
676 2012, 165(3), 177-187.

- 677 [14] Metalssi OO, et al. Experimental study on reinforced stone beams. *Engineering Structures*,
678 2013, 54, 1-8.
- 679 [15] Pedreschi R. A feasibility study of post-tensioned stone for cladding. *Construction and*
680 *Building Materials*, 2013, 43, 225-232.
- 681 [16] Camposinhos RS. Undercut anchorage in dimension stone slab cladding. *Proc. ICE*,
682 *Construction Materials*, 2013, 166(3), 158-174.
- 683 [17] Ye Y, Guo ZX, Chai ZL. Flexural behaviour of stone slabs reinforced with prestressed NSM
684 CFRP bars. *ASCE J. Comp. Constr.*, 18(4), 2014, 04014004 / 1-12.
- 685 [18] Contrafatto L, Cosenza R. Behaviour of post-installed adhesive anchors in natural stone.
686 *Construction and Building Materials*, 2014, 68, 355-369.
- 687 [19] Xie J, Wu X, Xu F. Experimental study on the flexural behaviour of stone beams strengthened
688 with a combination of angle steels and PET belts. *Materials and Structures*, August / September
689 2016, Vol. 49, 1013-1024.
- 690 [20] Ye Y, et al. Strengthening stone beams with prefabricated polymer-reinforced stone plates.
691 *Proc. ICE, Structures and Buildings*, 2020, doi: 10.1680/jstbu.19.00165
- 692 [21] Boote S. Stone as a structural material. Part 2: Traditional and reinforced stone stairs. *The*
693 *Structural Engineer*, June 2020, 18-23.
- 694 [22] Boote S, Lynes A. Stone as a structural material. Part 3: Post-tensioned stone structures. *The*
695 *Structural Engineer*, August 2020, 22-28.
- 696 [23] Marti-Vargas JR, et al. Bond of 13 mm prestressing steel strands in pretensioned concrete
697 members. *Engineering Structures*, 2012, 41, 403-412.
- 698 [24] Marti-Vargas JR, et al. Slip distribution model along the anchorage length of prestressing
699 strands. *Engineering Structures*, 2014, 59, 674-685.
- 700 [25] Bai F, Davison JS. Composite beam theory for pretensioned concrete structures with solutions
701 to transfer length and immediate prestress losses. *Engineering Structures*, 2016, 126, 739-758.
- 702 [26] Brearley LM, Johnston DW. Pull-out bond tests of epoxy-coated prestressing strand. *ASCE J.*
703 *Struct. Eng.*, 1990, 116(8), 2236-2252.

704 [27] Laco J, Borzovic V. Experimental investigation of prestressing strand on bond behavior of
705 concrete members. ACI Struct. J., 2017, 114(1), 15-24.

706 [28] Shin HO, et al. Bond behaviour of pretensioned strand embedded in ultra-high-performance
707 fiber-reinforced concrete. Int. J. Conc. Str. Mat., 2018, 12.

708 [29] Mohandoss P, et al. Transmission length of pretensioned concrete systems – comparison of
709 codes and test data. Mag. Conc. Res., 2019, 71(17), 881-893.

710 [30] <https://www.polycor.com/stone/limestone/valanges/>

711 [31] https://www.parex.co.uk/Technical_Mortars/Grouts/Epoxy_Resin_Based

712 [32] Little JA, Mann BP. Optimizing logarithmic decrement damping estimation through
713 uncertainty propagation, Journal of Sound and Vibrations, 2019, 457, 368-376.

714 [33] Sarhat S, Sherwood EG. Shear Strength of GFRP-Reinforced Concrete Masonry Beams. In
715 ASTM International Selected Technical Papers: Masonry 2018, STP 1612, Ed. Krogstad NV
716 & McGinley M. 131-157.

717

718

719

720

721

722

723

724

725

726

727

728

729
730
731
732
733
734
735
736
737
738

Global or Local?	Figure	E (kN/mm²)	Notes
Local	Fig. 6(b)	28.4	Average axial strain in concentric-strand specimen at jacking stage
Global	Fig. 7(b)	29.1	Free vibration of pre-tensioned concentric-strand specimen
Global	Fig. 10(a)	28.8	Midspan upward deflection of eccentric-strand specimen due to jacking
Local	Fig. 10(b)	29.4	Net strain at soffit of eccentric-strand specimen due to jacking
Mean E value = 28.9 kN/mm² : CoV = 1.3%			

739
740
741
742
743
744
745
746

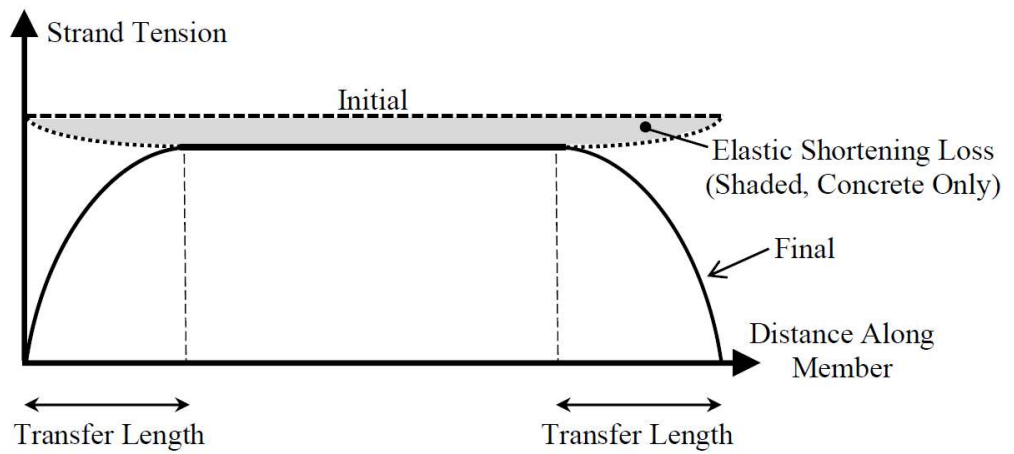
Table 1 – E value of Valange Stone Estimated From Test Results

747

748



(a) 12 m Long Post-tensioned Limestone Floor Beams



(b) Strand Force Profiles Along Member During Pretensioning

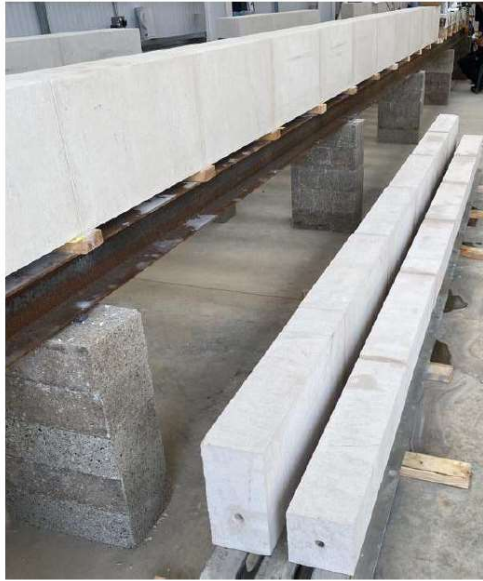
749

750

Fig. 1 – Prestressing Options

751

752



(a) Valange limestone blocks assembled into specimens



(b) Cut surface revealing C-shaped fossil fragment

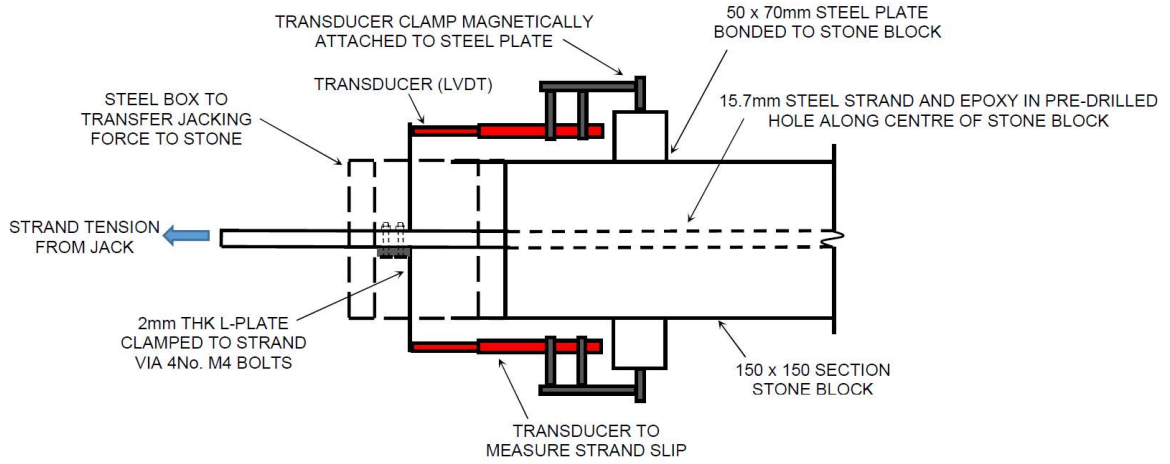


(c) Post-test sample from beam showing cured epoxy that enclosed half of strand section

754

755

756



(a) Plan View at Jacking End



(b) Test Setup for Specimen P600

757

758

759

760

761

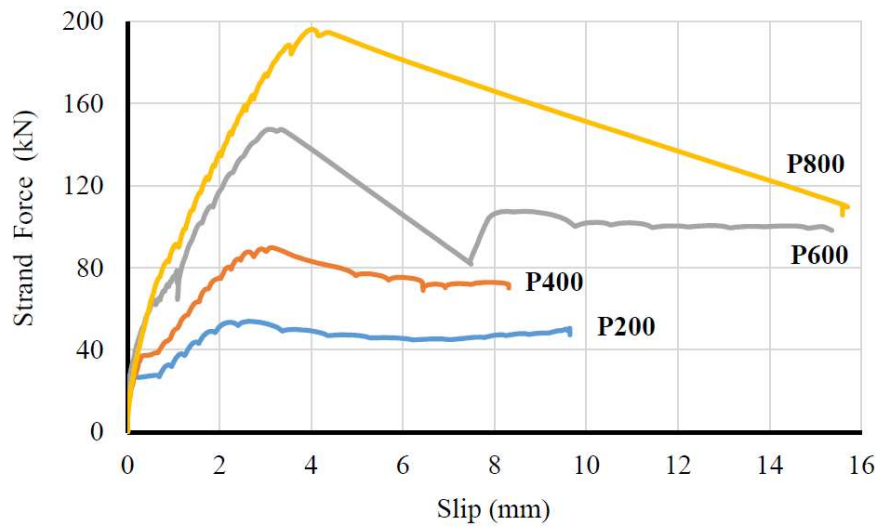
762

763

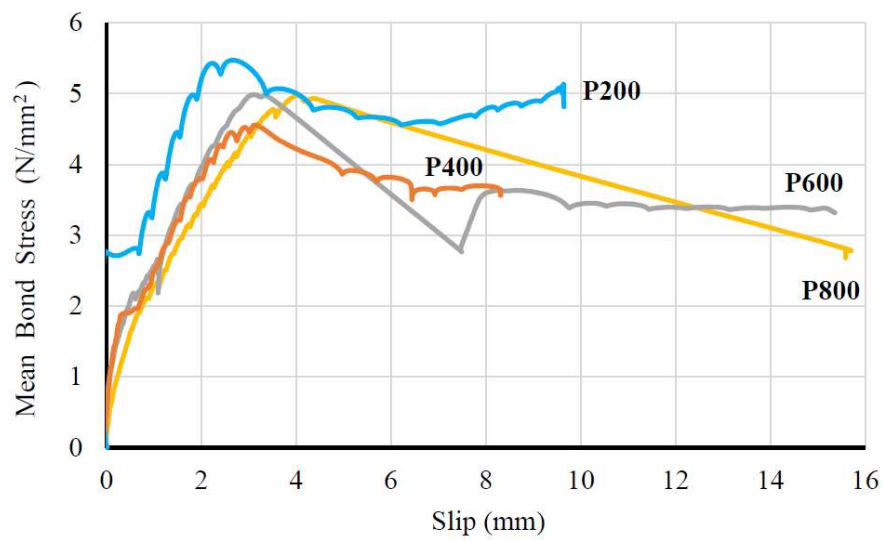
Fig. 3 – Pullout Test Setup



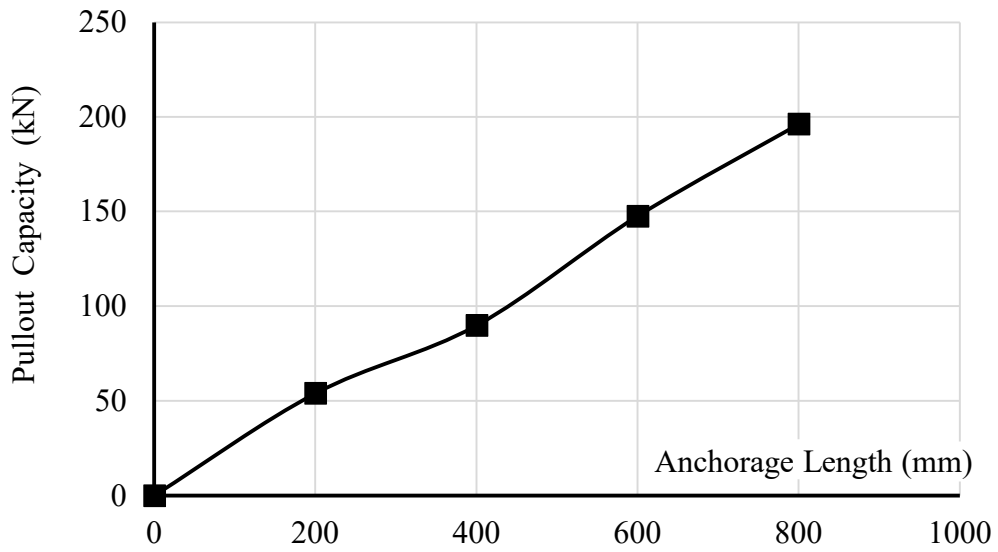
(a) Failure of Specimens P400 (Left) and P600



(b) Strand Force vs Slip Characteristics



(c) Variation of Mean Shear Bond Stress with Slip



(a) Variation of Pullout Failure Load with Embedment Length

Fig. 4 – Pullout Test Results

765

766

767

768

769

770

771

772

773

774

775

776

777

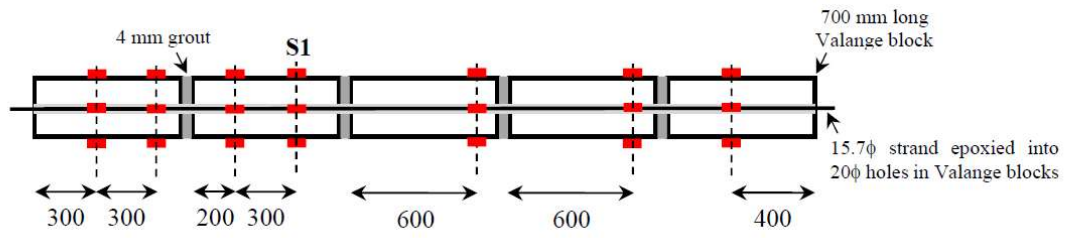
778

779

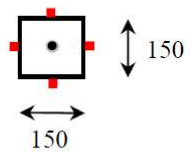
780

781

782



(a) Plan



(b) Section

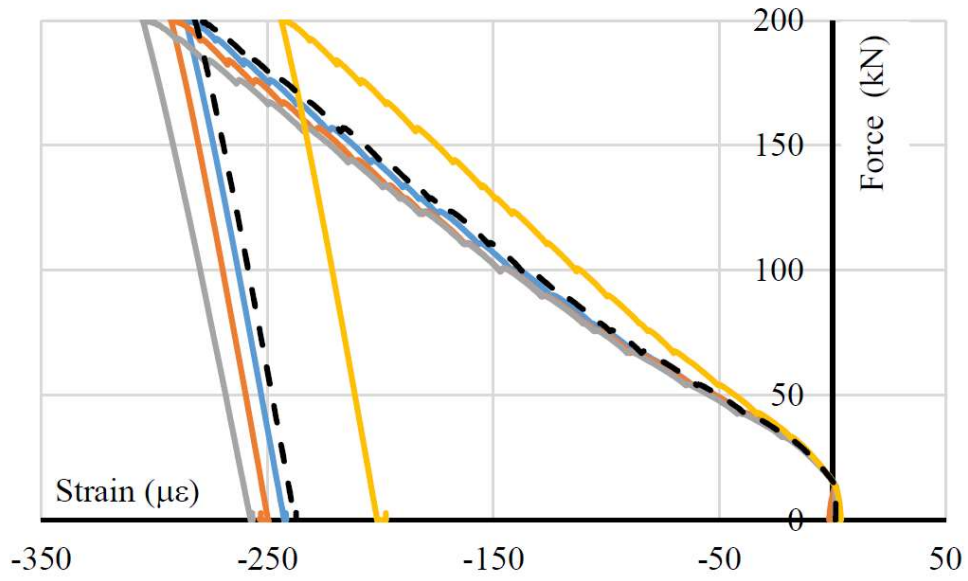


(c) Tensioning stage at anchored end

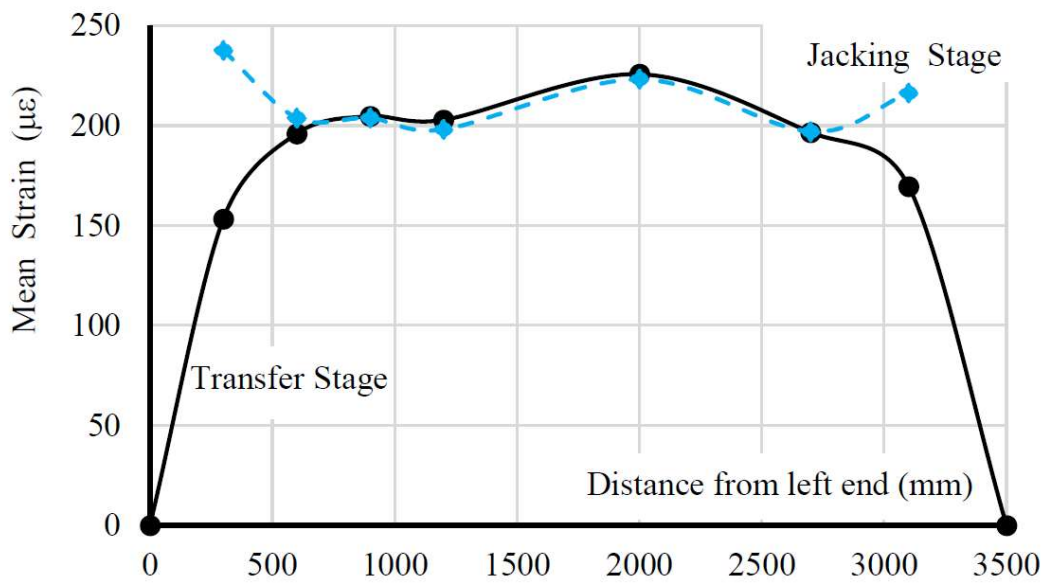


(d) Tensioning stage at jacking end

Fig. 5 – Prestressing setup for concentric-strand specimen



(a) Individual and mean strains at section S1 (Fig. 5(a)) during tensioning stage



(b) Section mean compressive strains (absolute values) along specimen after release

Fig. 6 – Strain response during pretensioning of concentric-strand specimen

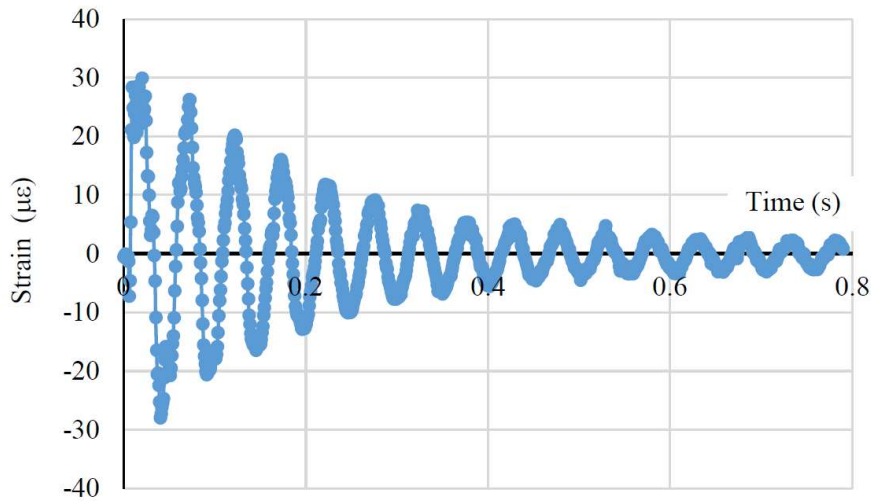
784

785

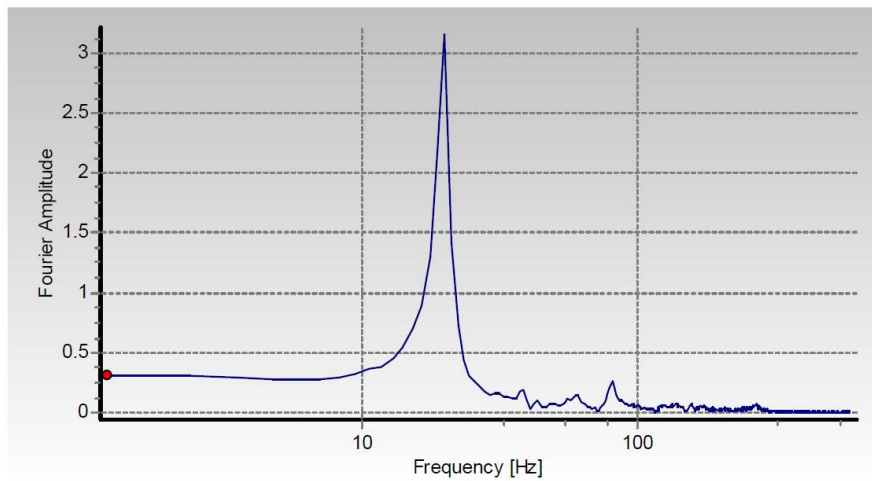
786

787

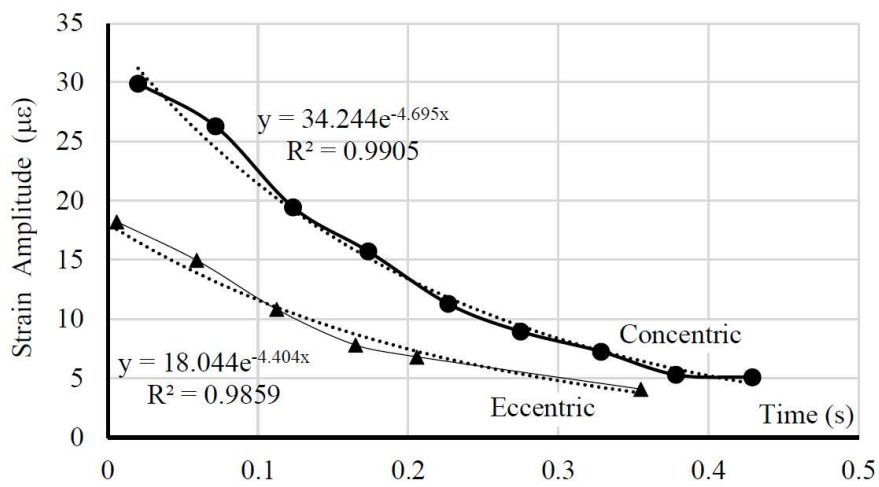
788



(a) Free vibration strain-time plot for concentric-strand specimen



(b) Fast Fourier Transform for concentric-strand specimen

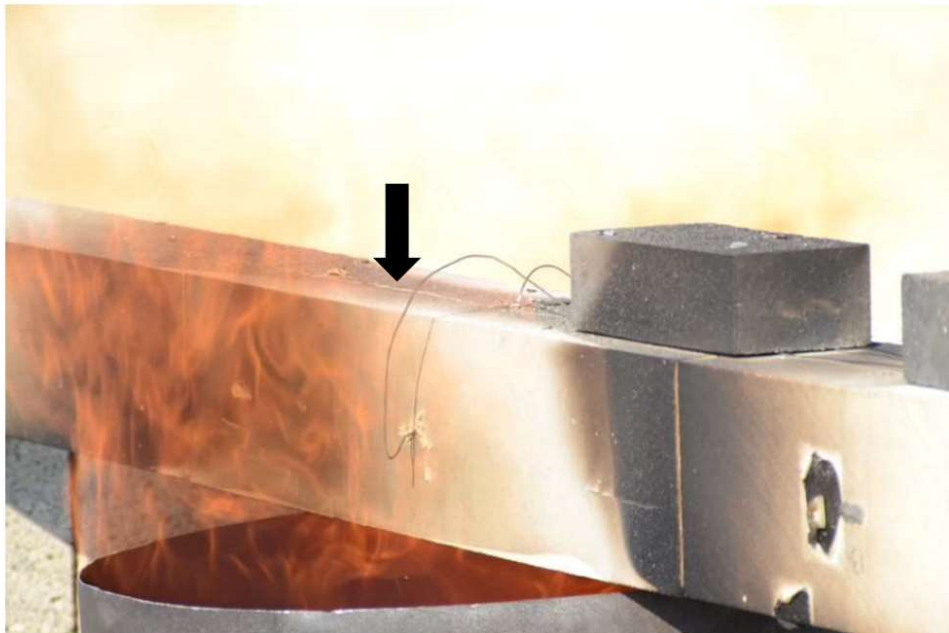


(c) Vibration decay for eccentric-strand and concentric-strand specimens

Fig. 7 – Vibration Test Results



(a) Fire Test in Progress



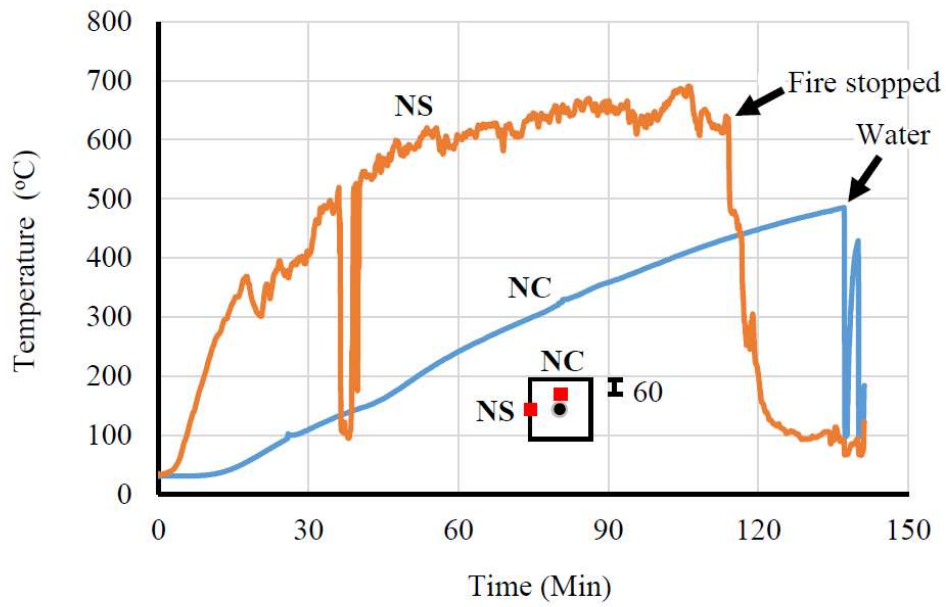
(b) Longitudinal crack on top face during fire



(c) Bottom Face Post Fire : Stone Peeling



(d) Adhesive Intact (left), Burnt or Degraded (right)



(e) Measured Temperature Variations Over Time

Fig. 8 – Fire Test Results

791

792

793

794

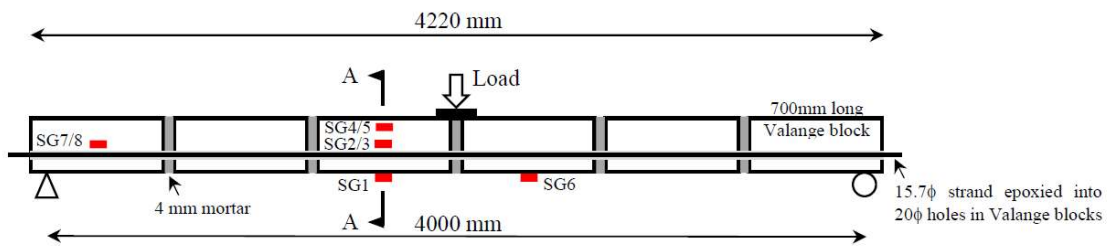
795

796

797

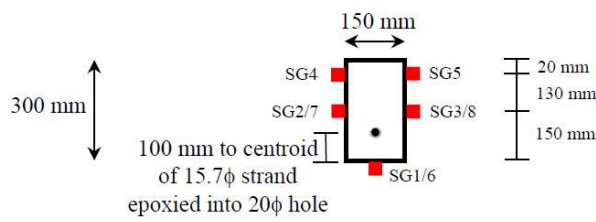
798

799



(a) Elevation

SGn – Strain Gauge n



(b) Section A-A

Fig. 9 – Load and Instrumentation Setup for One Pre-tensioned Valange Stone Beam

800

801

802

803

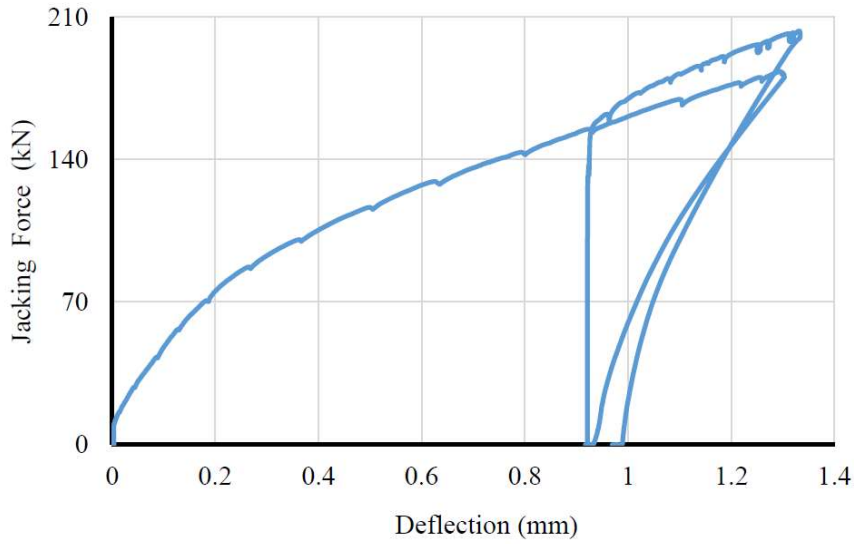
804

805

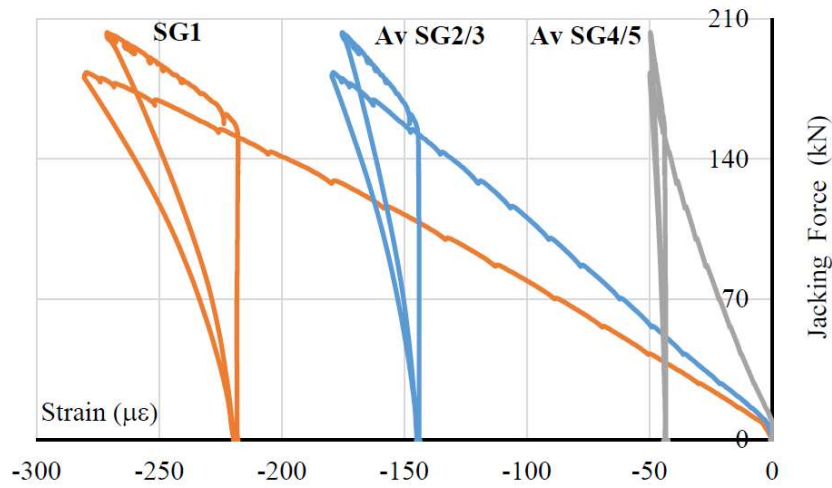
806

807

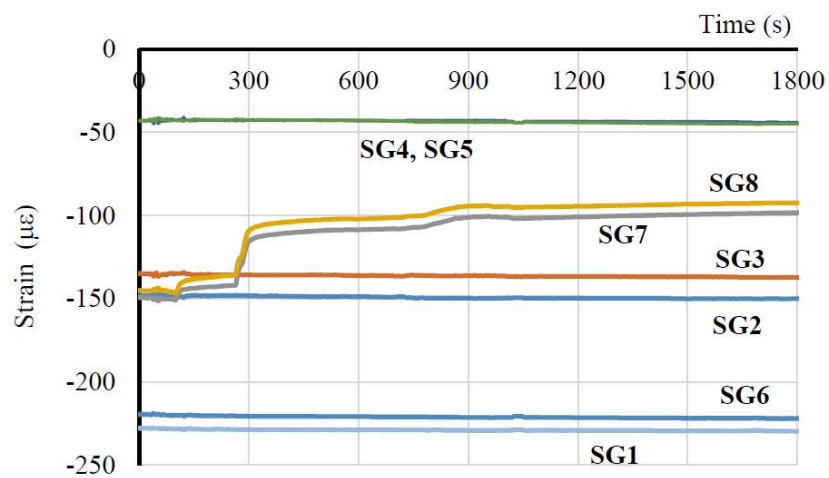
808



(a) Variation with jacking force of midspan upward deflection



(b) Variations with jacking force of near-midspan strains at three levels



(c) Effect of release on strains

Fig. 10 – Prestressing of Eccentric-Strand Specimen



(a) Test setup



(b) Asymmetric failure crack trajectory



(c) Separation (crack) at mortar-stone interface at midspan

Fig. 11 – Failure of pretensioned eccentric-strand specimen in three-point bending

810

811

812

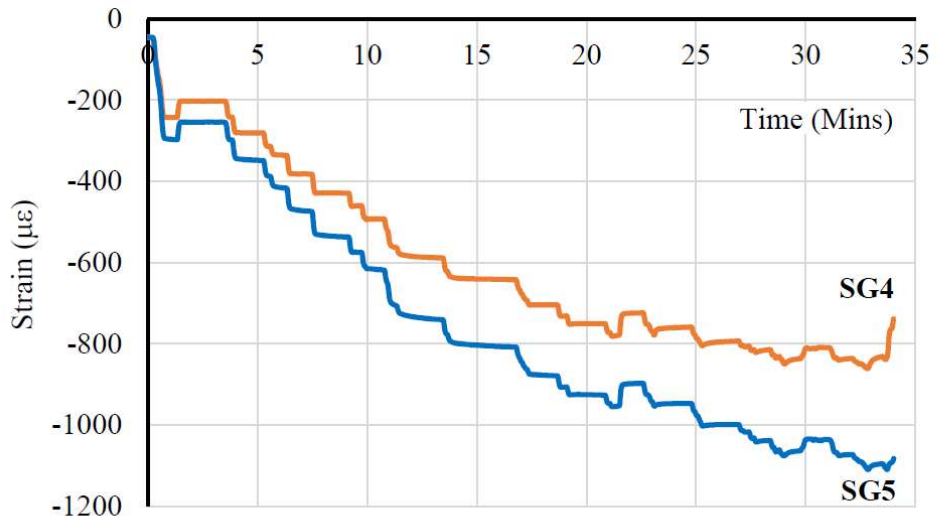
813

814

815

816

817



NB – See Fig. 9 for locations of strain gauges SG4, SG5

Fig. 12 – Eccentric-strand specimen : near-midspan top level strain variations with time

818