

1 **GUIDED WAVE SCATTERING AT A DELAMINATION IN A QUASI-ISOTROPIC**
2 **COMPOSITE LAMINATE: EXPERIMENT AND SIMULATION**

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8 **ABSTRACT**

9 Carbon fibre composite laminates are increasingly being used for aerospace structures due to
10 their low weight and improved mechanical performance. Impact damage can cause
11 delaminations below the visible surface of the structure due to limited interlaminar strength.
12 Guided ultrasonic waves can detect and characterize delaminations in composite laminates.
13 The scattering of the A_0 Lamb wave mode at an artificial delamination, located at an
14 asymmetric depth in a quasi-isotropic laminate, was investigated. Full field non-contact laser
15 measurements were used to visualise wave trapping and scattered waves. A three-dimensional
16 finite element model was developed and validated against the experiments. The influence of
17 delamination shape and depth on guided wave scattering were studied. Small variations in
18 delamination shape significantly affected the interference pattern on top of the delamination,
19 but had limited effect on the scattered wave outside the delamination. Delamination depth was
20 found to strongly influence the angular direction and amplitude of scattered waves.
21 Implications for structural health monitoring were discussed.

22 **Keywords:** Composite laminate, Delamination, Scattering, Guided waves, CFRP, Lamb
23 waves

24 **INTRODUCTION**

25 Fibre reinforced composite laminates are being increasingly used in a range of applications to
26 reduce the weight of structures whilst improving their mechanical performance. However,
27 composite laminates have limited interlaminar strength and are prone to low velocity impact
28 damage [1]. Multilayer defects, consisting of delaminations (separation of the ply layers), fiber
29 breakage and matrix cracking, occur throughout the thickness of the laminate, below the visible
30 surface. The extent relates to the impact velocity and energy, the bending stiffness mismatch

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31 between adjacent ply layers due to different fibre orientations [2], as well as the thickness of
32 the laminate [3, 4]. In thick laminates, impact damage has been demonstrated to propagate as
33 a cone away from the impact location creating a ‘pine tree’ pattern [5]. In thin laminates,
34 matrix cracking typically starts in the lowest ply layer due to bending stresses, and intra-ply
35 cracks and interface delaminations propagate from the lowest surface up towards the impacted
36 surface, resulting in a reverse pine-tree pattern [6]. A ‘butterfly’ pattern of (approximately)
37 circular and ellipse shaped delaminations of varying size is often observed in the in-plane
38 direction [7, 8, 9]. Whilst impact damage is complex and consists of multiple and interacting
39 failure modes, delamination is considered the most dominant and critical failure mechanism in
40 composites [10], and thus constitutes the focus of the present study. A relatively small impact
41 load can cause extensive delamination damage below the laminate surface, resulting in barely
42 visible impact damage (BVID) that is difficult to detect [11]. Subsequent application of
43 external loads may induce fracture growth, leading to degradation of material properties (e.g.,
44 compressive strength reduction), and eventually catastrophic failure. Therefore, rapid and
45 reliable non-destructive evaluation (NDE) techniques are required to locate and characterise
46 delamination damage in multi-layered structures [12]. Radiographic [13, 14] and ultrasonic
47 methods [15] are commonly used for composite components.

48 Guided ultrasonic waves can be exploited for rapid screening of large areas due to their long
49 range propagation at low excitation frequencies, providing a promising in-situ structural health
50 monitoring (SHM) solution for composites [16]. Generally, it is desirable to generate a single
51 guided wave mode in a structure, below the cut-off frequency of the higher order wave modes.
52 The fundamental symmetric S_0 mode has been used in several studies due to its low dispersion
53 and high propagation velocity (first arrival) [17]. However, S_0 mode reflection is highly
54 dependent on the through thickness location of the delamination, as no scattered wave is
55 observed for disbonds at interfaces with zero shear stress [18]. On the other hand, the A_0 mode
56 is sensitive to defects at any depth. It is more highly attenuated than the S_0 mode, resulting in
57 shorter propagation distances. However, the A_0 mode has a slower phase velocity and shorter
58 wavelength, and so has better resolution for small defects. The A_0 mode wave propagation
59 shows less directional dependency compared to the S_0 mode for anisotropic composite
60 structures [18].

61 Whilst numerical and experimental studies have demonstrated that guided waves can be used
62 to detect delaminations, scattering at a delamination remains a complex problem. The
63 anisotropy of a multi-layered plate influences the direction of scattered waves [19], [20]. Mode

64 conversion and scattering occur when guided waves interact with a delamination. These effects
65 can be used to detect and characterise damage [21]. Waves propagate in each of the sub-
66 laminates above and below the delamination, typically with different velocities depending on
67 the ply layup [22]. Numerous studies have reported that the amplitude of guided waves
68 increased significantly over the delamination area, which could be exploited for damage
69 detection [23, 24]. This effect is particularly pronounced for the A_0 mode, as the bending
70 stiffness of thinner laminates is lower. The increase in amplitude is also caused by multiple
71 reflections within the sub-laminates constructively interfering and generating standing waves,
72 ‘trapping’ energy around the delamination area [25]. This increase in amplitude can be
73 exploited for damage localization, and the difference in arrival times between multiple
74 reflections can be used to estimate delamination size [26].

75 Wave trapping has been observed in both numerical simulations and laser doppler vibrometer
76 measurements [27]. Several image processing techniques have been developed to take
77 advantage of this behaviour and to highlight delaminations. Sohn et al. [25] proposed a standing
78 wave filter in order to emphasise standing waves surrounding a delamination, whereas Testoni
79 et al. [28] used a warped curvelet transform to remove the incident wave to isolate the reflected
80 waves from the delamination. Kudela et al. [29] developed a selective weighted root mean
81 square algorithm to generate clear damage maps for delaminations in cross ply panels with
82 uniform thickness. The wave trapping phenomena has been used to distinguish between
83 different sized delaminations at several depths for multilayer damage [30].

84 Scattered amplitudes and scattering directivity patterns depend on the ratio of delamination
85 size to wavelength and the through thickness location of the defect [31]. Both back-scattered
86 and forward scattered amplitudes can be observed, the amplitude of the latter being dependent
87 on the phase difference between waves propagating in each of the sub-laminates [32]. When a
88 delamination is located at an asymmetric depth, a high trapped amplitude can be observed on
89 top of the thinner sub-laminate [23]. Delaminations located towards the mid-plane experience
90 less wave trapping but have a higher scattered wave amplitude [33]. The scattering directivity
91 pattern has been shown to be influenced by the fibre orientation of the outer plies of the
92 laminate, due to fibre steering effects [22]. Scattering patterns depend on the layup sequence,
93 even for laminates with the same number of ply layers [34]. Mei et al. found that the number
94 of delaminations at the same location with different depths has an influence on the scattering
95 pattern and the amplitude of trapped waves [35]. Mode velocity, wavelength, and deflection
96 angle at a square delamination were found to vary with delamination depth [36].

97 Limited experimental studies have focused on guided wave scattering at a circular
98 delamination. Murat et al. performed a systematic study on the influence of interlaminar
99 damage depth and size through 3D Finite Element (FE) simulations with a zero volume square
100 delamination, compared with experimental results for BVID [20]. Ng and Veidt [31] used 3D
101 FE simulations to investigate the A_0 mode scattering at circular delaminations of various depths
102 and sizes. The numerical model was verified experimentally for an artificial delamination
103 created by an insert embedded at the laminate midplane. Pudipeddi et al. [37] performed a
104 numerical investigation of mode conversion and scattering in a quasi-isotropic laminate
105 containing circular delaminations of various depths and sizes. The discrete model was validated
106 experimentally for the case of an undamaged laminate.

107 This contribution aims to improve the understanding of A_0 mode scattering at a circular
108 delamination in a quasi-isotropic carbon fiber reinforced composite (CFRC) laminate. Full
109 field, non-contact laser measurements were performed on a composite panel containing an
110 artificial delamination located at an asymmetric depth, building on preliminary results [38]. A
111 3D FE model containing a zero-volume ellipse shaped delamination was developed to provide
112 comparison to the experimental results and the convergence of the FE model was discussed.
113 Two delamination shapes were modelled and compared with the experimental measurements.
114 A systematic study was performed to investigate the influence of delamination depth on
115 scattering.

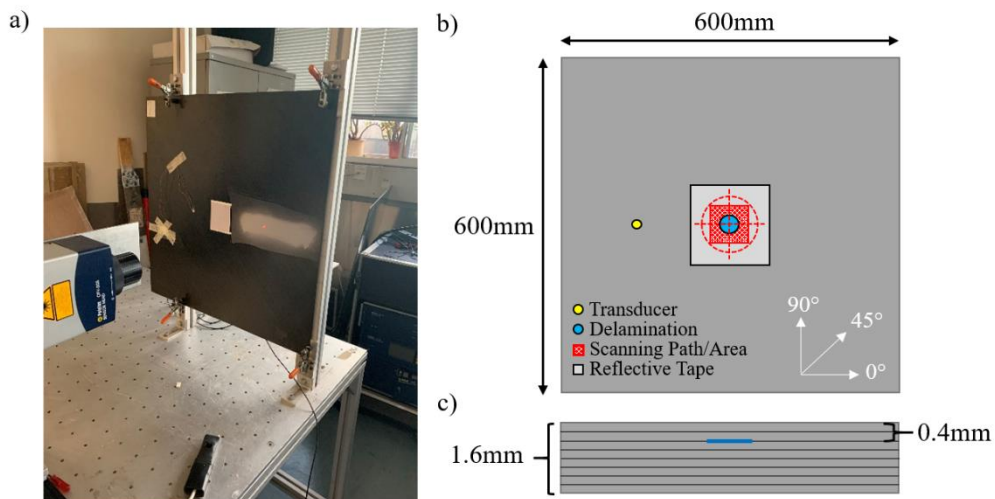
116 **EXPERIMENTAL MEASUREMENTS**

117 Experiments were carried out on an 8-ply quasi-isotropic graphite/epoxy laminate with layup
118 $[-45/45/90/0]_s$ and dimensions 600mm x 600mm x 1.6mm [39]. The panel was manufactured
119 using unidirectional pre-preg plies and manual lay-up. The material properties of a single ply
120 layer are given in Table 1. An artificial insert delamination was manufactured at the centre of
121 the panel by inserting a circular polytetrafluoroethylene (PTFE) film, 15mm in diameter and
122 0.02mm thickness. The film was placed between the second and third plies during the layup
123 process to give a delamination depth of 0.4mm. The resulting CFRC laminate was then cured
124 in an autoclave. The cure cycle consisted of raising the temperature from 30°C to 175°C at 2.5
125 °C/min and was held at 175°C for 120 minutes at 3.5 atm. The position of the delamination
126 was verified through an ultrasonic C-scan (Olympus OmniScan SX, 5 MHz phased array
127 probe). An oval shaped crown was identified indicating detached plies, giving an actual flaw
128 size of approximately 20 mm x 16 mm [40].

129 **Table 1:** Engineering constants for a single ply layer of the 8 ply CFRP composite plate, based on [30].

E_1 [GPa]	E_2 [GPa]	E_3 [GPa]	G_{12} [GPa]	G_{13} [GPa]	G_{23} [GPa]	ν_{12}	ν_{13}	ν_{23}	ρ [kg/m ³]
175	6.90	6.90	4.18	4.18	2.35	0.25	0.25	0.46	1520

130 A piezoelectric transducer (lead zirconate titanate (PZT) disk, PI Ceramic PIC-255, diameter
 131 10 mm, thickness 0.25 mm) was bonded by cyanoacrylate glue to the surface of the composite
 132 plate 100 mm from the centre of the delamination location and was used to generate the A_0
 133 guided wave mode. The excitation signal was a 5-cycle sine wave modulated by a Hanning
 134 window and was generated at 50kHz center frequency using a programmable function
 135 generator (Agilent 33220A). The excitation signal was amplified to 25V_{pp} (Krohn-Hite 7602M
 136 wideband amplifier) and applied to the transducer. A laser vibrometer (Polytec sensor head
 137 OFV-505, OFV-5000 vibrometer controller) attached to a scanning rig was used to measure
 138 the velocity of the out-of-plane displacement of the plate surface. The laser head was moved
 139 parallel to the sample both horizontally and vertically. Retroreflective tape was applied to the
 140 plate to improve the laser beam reflection and thus signal-to-noise ratio. The time signals were
 141 filtered using a band-pass filter with cut-off frequencies 25kHz above and below the centre
 142 frequency of excitation. The signals were then recorded and averaged 20 times using a digital
 143 storage oscilloscope before being saved to a PC to be further analysed in MATLAB R2019b.



144

145 **Figure 1:** a) Experimental setup with laser head and composite plate specimen; b) schematic of quasi-isotropic
 146 composite laminate (top view) with transducer and damage locations marked. Red square indicates scanning area.
 147 Dotted lines indicate scanning paths across delamination; c) through thickness position of the delamination.

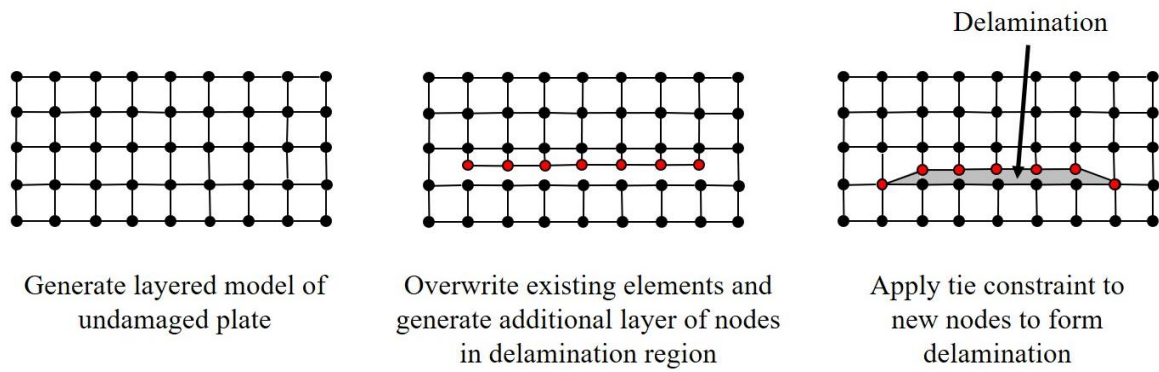
148 Three different scans were performed on the sample, as shown schematically in Fig. 1. A square
149 area 40 mm x 40 mm centred on the delamination was scanned in 1 mm steps. A linear scan
150 70 mm in length was performed horizontally, and vertically, in 1 mm steps with each line
151 crossing through the central point of the delamination. A circular scan centred on the
152 delamination with radius 30 mm was performed in steps of 2°. To estimate the attenuation
153 within the sample, additional line scans on an undamaged region of the plate were performed.
154 The scans were performed along a 130mm line in 1mm steps along the 0° fibre direction. The
155 first measurement point was at 10mm distance from the transducer. The reduction in amplitude
156 along this line of points was used to estimate material damping.

157

158 **FINITE ELEMENT MODEL**

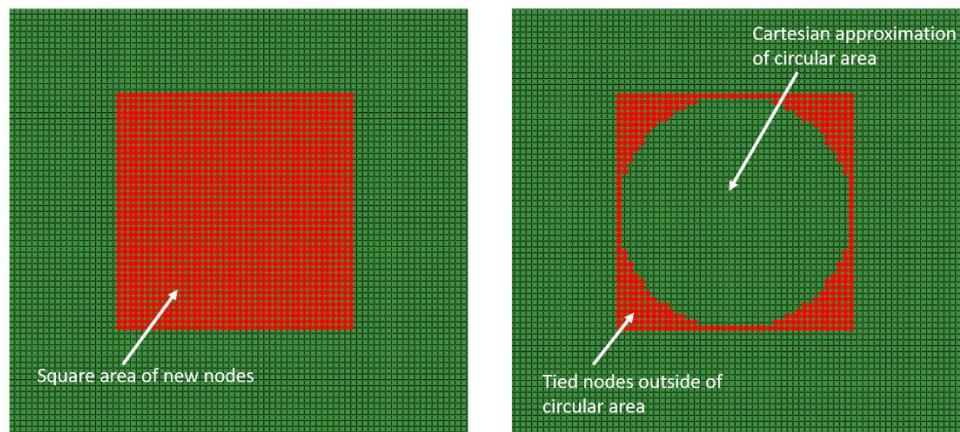
159 A full 3D layered FE model of a quasi-isotropic laminate with dimensions 600mm x 600mm x
160 1.6mm was developed. A model input file specifying the model geometry and parameters was
161 generated in MATLAB and imported into ABAQUS/Explicit 2018 to perform the analysis.
162 Eight node solid brick elements with reduced integration and hourglass control (C3D8R) were
163 selected for the model. Each ply layer was modelled as a unidirectional layer of elements, with
164 a single element through the thickness (0.2mm). The homogenous material properties given in
165 Table 1 were assigned to each layer individually and the orientation of each layer was defined
166 to produce the stacking sequence of the specimen $([-45/45/0/90]_s)$. A regular Cartesian mesh
167 was used, as it has been shown to reduce numerical dispersion when modelling wave
168 propagation [41].

169 A zero-volume delamination was incorporated into the model by overwriting existing elements
170 at the delamination location, as shown schematically in Fig. 2. New nodes and elements,
171 connected to one side of the plate, were defined over a square area with the approximate
172 dimensions of the delamination. A node to node tie constraint was applied to form a circular
173 shape (interpolated onto a Cartesian grid) as shown in Fig. 3. This procedure was also used to
174 discretize an ellipse shaped delamination by defining a rectangular area of new nodes with
175 dimensions of the major and minor axis of the ellipse. This approach provides an identical
176 geometry to the more standard approach of two distinct regions with tie constraints [42], while
177 allowing for straightforward automated generation of circular or ellipse shaped delaminations
178 using the MATLAB code. For the present study, a 20mm x 20mm circular delamination was
179 initially modelled and used as the standard case throughout.



180

181 **Figure 2:** Schematic of procedure to model zero volume delamination. Through thickness view of mesh
 182 surrounding delamination region at different steps. Red nodes represent new nodes generated in the delamination
 183 area. Volume of delamination is exaggerated.



184

185 **Figure 3:** Close up top view of delamination region in ABAQUS: a) new nodes created in delamination region;
 186 b) tied nodes to form circular delamination area.

187 An out-of-plane force was applied to a single node located 100mm from the delamination
 188 centre to simulate generation of the A_0 mode. The excitation signal was a 5-cycle sine wave
 189 modulated by Hanning window with a centre frequency of 50kHz. Stiffness proportional
 190 damping was included into the model. The (Rayleigh) damping coefficient was set to $\beta = 30\text{ns}$.
 191 A 60mm x 60mm grid of monitoring points centred on the delamination was defined in 1mm
 192 steps. History output requests for the out-of-plane displacements were recorded at each
 193 measurement point. A 40mm x 40mm grid, bilinear interpolation onto a 30mm circle, and
 194 horizontal and vertical lines can be selected from this data during analysis for comparison to
 195 the experiments. A baseline model containing no damage was also created and the complex
 196 magnitude (amplitude and phase) of the incident wave at the center frequency (50 kHz) was
 197 calculated using Fast Fourier Transform (FFT). The magnitude of the scattered wave was
 198 isolated by subtracting the FFT baseline magnitude from the FFT magnitude of the signals for

199 the simulations containing the delamination. Using the complex difference in the frequency
200 domain retains both phase and amplitude information, removes the incident wave, and isolates
201 the scattered component [43].

202 **FE MODEL VALIDATION**

203 **MODEL CONVERGENCE**

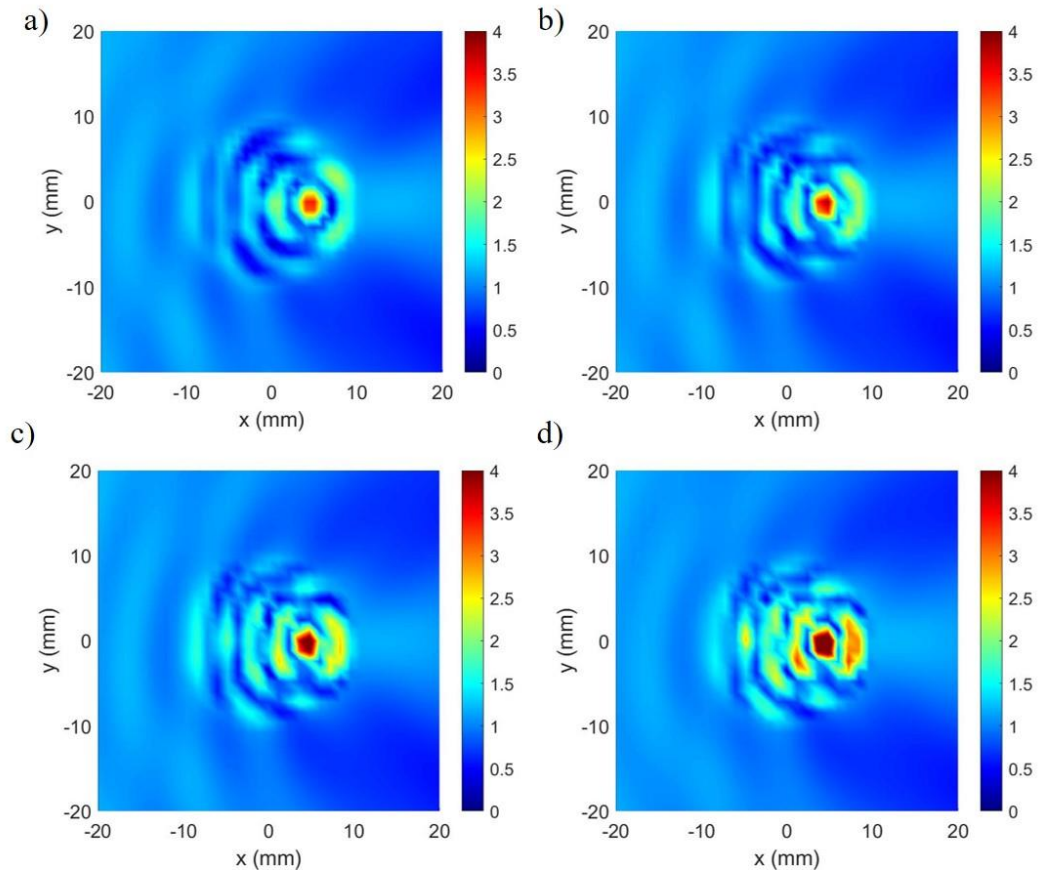
204 The element size was varied to determine the model convergence. An element size of 0.5mm
205 x 0.5mm x 0.2mm was chosen initially. The thickness of the elements was kept constant at
206 0.2mm (one element per ply through the thickness), whilst the in-plane dimensions were varied
207 to 0.4mm, 0.3mm, and 0.2mm respectively. The parameters for the convergence simulations
208 are given in Table 2. The delamination was placed at 2 different depths: between the second
209 and third plies (depth 0.4mm) to match the experimental specimen, and between the fourth and
210 fifth plies (midplane of the plate, depth 0.8mm). A baseline simulation was run for each element
211 size. The simulation time was 0.3ms for all element sizes. Additionally, monitoring points at
212 each node along a 60mm horizontal line passing through the centre of the delamination were
213 implemented.

214 The magnitude of the FFT at the centre frequency of the signal was extracted for each
215 measurement point. Signals were time gated to remove any edge reflections. The magnitude
216 was then normalised relative to the baseline magnitude of the FFT at the centre of the defect
217 location ($x = 0, y = 0$). Figure 4 shows the full field of a 40mm x 40mm area centred on the
218 delamination at depth 0.4mm for each element size. The incident wave propagates from left to
219 right. Similar interference patterns were observed for each element size, but the amplitude of
220 the guided wave field on top of the delamination showed some variation.

221 **Table 2:** Model parameters for convergence simulations.

Element size	Time increment (ns)	No. of elements (million)	Running time (hours)
0.5mm	50	12	4.5
0.4mm	25	18	9
0.3mm	25	32	15
0.2mm	20	32*	20

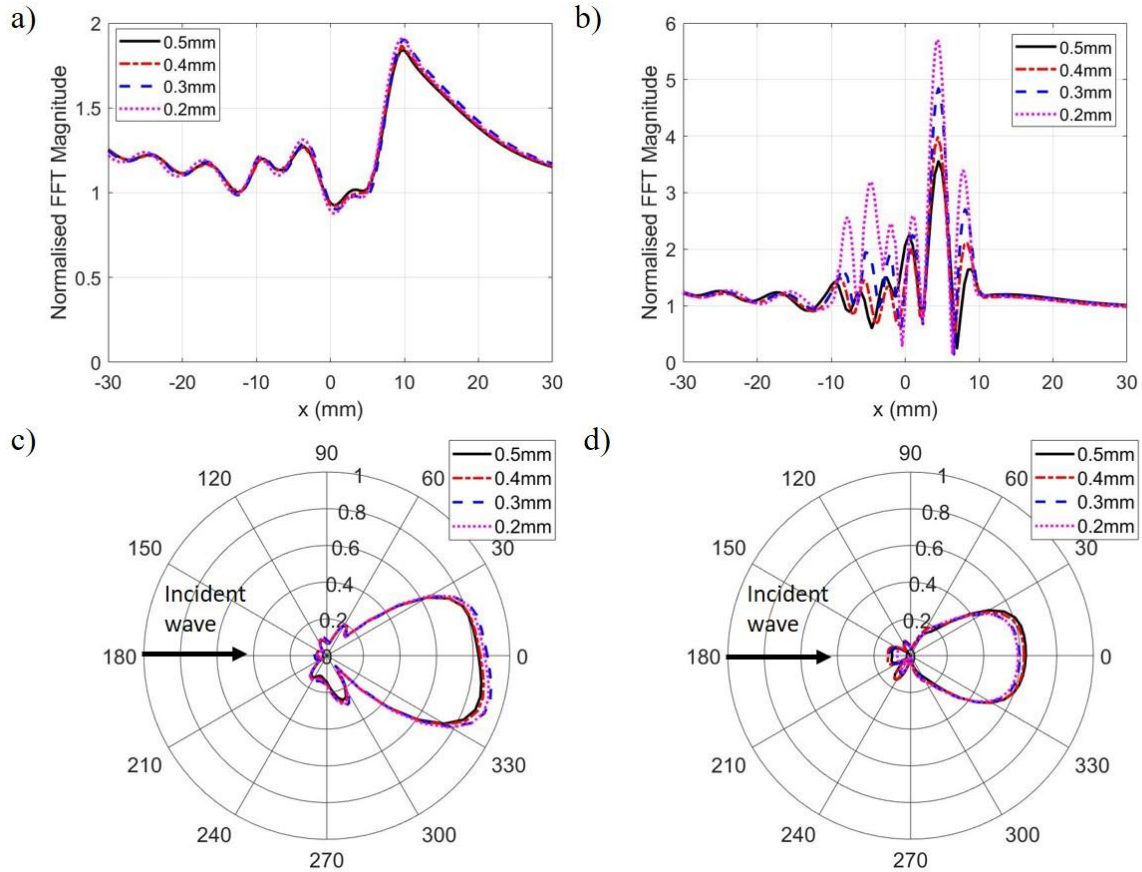
222 *0.2mm element size required plate size to be reduced to 400mm x 400mm x 1.6mm due to memory constraints.



223

224 **Figure 4:** Magnitude of FFT at 50kHz for a 40mm x 40mm grid of measurement points centred on a 20mm x
 225 20mm circular delamination; depth 0.4mm. In-plane element size: a) 0.5mm, b) 0.4mm, c) 0.3mm, d) 0.2mm.

226 The FFT magnitude at 50kHz along a horizontal line ($y = 0$) of measurement points for each
 227 element size is shown in Fig. 5. For a delamination located at the midplane of the plate (Fig.
 228 5a, 0.8mm depth) the magnitude of the scattered wave is in good agreement to within 5% in
 229 front of, and inside, the delamination region for all element sizes. At delamination depth of
 230 0.4mm (Fig. 5b) the magnitudes of the wavefield outside the delamination area are in
 231 agreement to within 6% for all element sizes. However, for the delamination region ($x = -$
 232 10mm to +10mm), whilst the overall scattering pattern and alignment of the peaks is similar
 233 between element sizes, the amplitudes of the individual peaks vary in magnitude by up to 45%
 234 as the element size is reduced, indicating that the model has not converged in this region. This
 235 is likely due to the waves propagating in the thin upper sub-laminate having a shorter
 236 wavelength ($\lambda = 7\text{mm}$) than those propagating through the full plate thickness ($\lambda = 16\text{mm}$), and
 237 so a smaller element size would be required to achieve full convergence on top of the
 238 delamination.



239

240 **Figure 5:** Normalised FFT magnitude (50 kHz) for different element sizes along a 60mm horizontal line of
 241 monitoring points for delamination depths a) 0.8mm, b) 0.4mm. Magnitude of baseline subtracted scattered wave
 242 for different element sizes for delamination depths c) 0.8mm, d) 0.4mm.

243 In addition to the interference pattern on top of the delamination, the scattered wave
 244 propagating in the undamaged region outside of the delamination area must be considered.
 245 Baseline subtraction was performed for a 30mm circle of measurement points in 2° increments.
 246 The 30mm radius is approximately twice the wavelength of the A_0 mode for the full plate
 247 thickness, sufficiently far from the defect to avoid the influence of near field scattering effects.
 248 Figure 5c/d show the angular magnitude of the scattered wave at delamination depths 0.8mm
 249 and 0.4mm respectively. At both delamination depths there is a large lobe around the 0°
 250 direction ($\pm 30^\circ$), indicating significant forward scattered amplitude. The amplitude is highest
 251 in the 0° direction and reduces towards the 30° direction, consistent with results in literature
 252 [20, 31, 37] The magnitudes are in agreement to within 5% for all element sizes at each depth,
 253 indicating that the model has converged in the undamaged region outside of the delamination.

254 Despite significant variation in peak magnitude, the qualitative features of the scattering on top
 255 (e.g., location of the peaks) of the delamination at 0.5mm element size reasonably match that

256 of the smaller element sizes. In addition to the in-plane dimensions of the elements, the number
257 of elements through the thickness per ply layer and the element type can also affect the
258 numerical accuracy and hence the model convergence. It should be noted that employing a
259 different element type, or two elements per ply layer, was found to affect the interference
260 pattern on top of the delamination, but had limited effect on the scattered wave in the
261 undamaged region of the laminate. In the context of SHM of composite structures, modelling
262 the precise scattering behaviour on top of the delamination is of less interest as usually the aim
263 of guided wave testing is to detect and quantify the scattered wave at some distance from the
264 damage, so that damage can be localized. As the 0.5mm element size has been demonstrated
265 to accurately model scattered wave propagation in the surrounding laminate whilst maintaining
266 reasonable computation time, an element size of 0.5mm was selected for the further simulations
267 presented in this study.

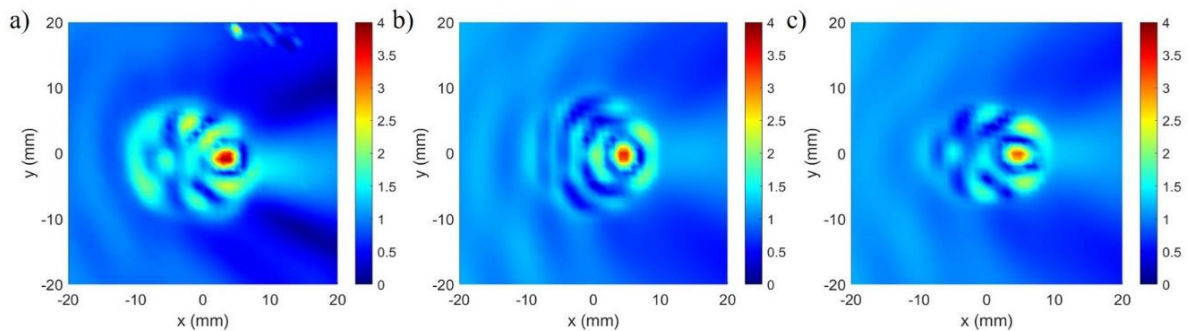
268 **INFLUENCE OF DELAMINATION SHAPE**

269 The ultrasonic C-scan results in [40] indicated that the artificial delamination has a slightly
270 oval shape with a best estimate of 20mm length in the x-direction and 16mm width in the y-
271 direction. The magnitude of the FFT at 50kHz over a 40mm x 40mm grid, horizontal line, and
272 30mm circle for an oval 20mm x 16mm shape and a circular 20mm x 20mm case were
273 compared with the experimental measurements. Figure 6a shows the experimental FFT
274 magnitude over a 40mm x 40mm grid of measurement points. The incident wave propagates
275 from left to right. The magnitude significantly increases in a circular region with the
276 approximate area of the delamination. The high magnitude over this region indicates that
277 energy trapping is occurring within the delamination, which has been reported previously [20,
278 23, 25, 27]. The regions of high and low amplitude suggest that there are multiple reflections
279 of guided wave modes within the delamination. A strong forward scattered wave can be
280 observed at the right of the delamination, with two ‘shadow’ regions of low magnitude either
281 side indicating destructive interference leading to lower wave amplitude. The small spots of
282 high amplitude at the top of Fig. 6a are due to experimental noise.

283 An increase in FFT magnitude within the delamination region can be observed in both the
284 20mm x 16mm and 20mm x 20mm models (Fig 6b/c respectively). The delamination shape
285 affects the shape of the high magnitude region. This could potentially be used to estimate
286 delamination size from noncontact laser measurements. The predicted increase in magnitude
287 relative to the surrounding regions is slightly lower for the numerical results than observed in

288 the experiment. The forward scattered component can be observed in each of the simulations,
 289 but the drop in amplitude in the shadow regions either side of the forward lobe is lower than
 290 for the measurements. The scattering pattern on top of the 20mm x 16mm delamination
 291 matches the measured pattern more closely than the 20mm x 20mm circular defect, indicating
 292 that the delamination width affects the interference pattern on top of the defect. Whilst the
 293 scattering pattern on top of the delamination is sensitive to relatively small changes in
 294 delamination shape (mm), there is limited sensitivity to smaller geometric imperfections (e.g.,
 295 sub-laminates not being perfectly flat, ply wrinkling). This is due to the wavelength of the A_0
 296 mode being relatively large in comparison to these imperfections.

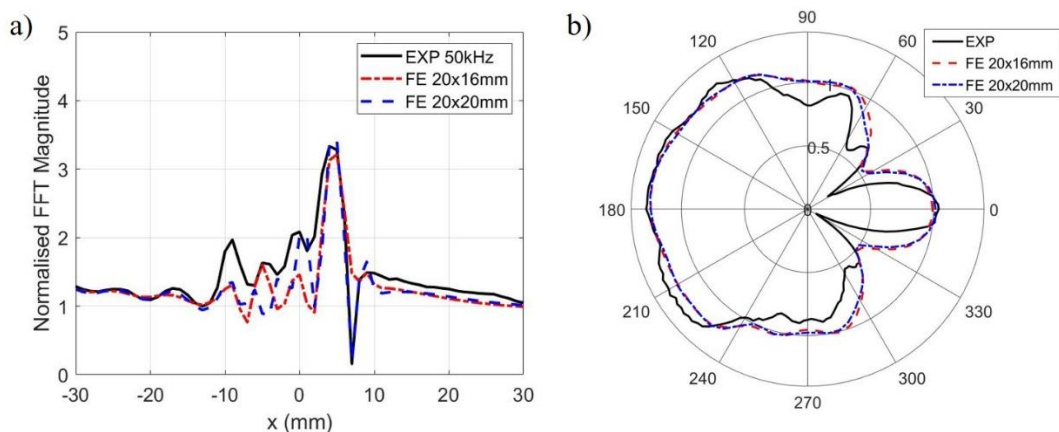
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298

299 **Figure 6:** Normalised magnitude of FFT at 50kHz over a 40mm x 40mm grid of measurement points for a)
 300 experimental measurements; b) FEA 20mm x 16mm delamination; c) FEA 20mm x 20mm delamination.

301



302

303 **Figure 7:** Measured and simulated magnitude of FFT at 50kHz for a) 60mm line of measurement points in 1mm
 304 steps, passing through the centre of the delamination; b) Circle of measurement points with radius 30mm (2°
 305 steps) centred on the delamination.

306 The measured FFT magnitude along a horizontal line of measurement points is denoted by the
307 blue line in Fig. 7a. The magnitude decreases along the propagation direction until a sharp
308 increase in magnitude is observed at the front edge of the delamination ($x = -10$ mm), consistent
309 with the full field scan in Fig. 6a. The decrease in magnitude with propagation distance is
310 expected due to wave spreading and attenuation. The variation in magnitude in front of the
311 delamination occurs due to constructive and destructive interference with the backscattered
312 wave. On top of the delamination, there are several amplitude peaks, with the highest peak at
313 +4mm and a trough at +7mm. The forward scattered amplitude beyond 10mm is larger than
314 that of the incident wave.

315 The wave amplitude for the FE simulation of the circular 20mm x 20mm delamination is
316 denoted by the blue line in Fig. 7a. The incident wave, the peak at +4mm and trough at +7mm
317 show good agreement with the measured values, to within 3%. However, the overall magnitude
318 on top of the delamination and the forward scattered wave is lower than in the experiment. The
319 incident wave for the 20mm x 16mm delamination model (red line Fig. 7a) has reasonable
320 agreement within 9% of the measured values. The location of the major peak is in good
321 agreement, however the trough at the edge of the delamination is not visible. Again, the
322 magnitude on top of the delamination, and of the forward scattered wave, are lower than the
323 measurements. In contrast to the 20mm x 20mm delamination, the location of the peaks within
324 the delamination region of the 20mm x 16mm model match the experiment reasonably well.
325 These results suggest that the interference pattern on top of the delamination is strongly
326 influenced by the size and shape of the delamination, but that the forward and backward
327 scattered waves are less sensitive to the exact defect shape.

328 The angular FFT amplitude of the scattered wave outside the damage area for the experiment
329 (black), 20mm x 20mm delamination model (blue), and 20mm x 16mm delamination model
330 (red) around a circle of measurement points with radius 30mm is shown in Fig. 7b. The
331 measurements show a strong lobe in the 0° direction, consistent with the forward scattered
332 wave observed in full field measurements in Fig. 6a. A steep drop in amplitude is observed at
333 30° and 330° , which corresponds to the location of the regions of destructive interference in
334 the measured full wave field. The forward scattered amplitude is generally lower than the
335 amplitude in the backscattered direction. The scattering pattern is reasonably symmetric.

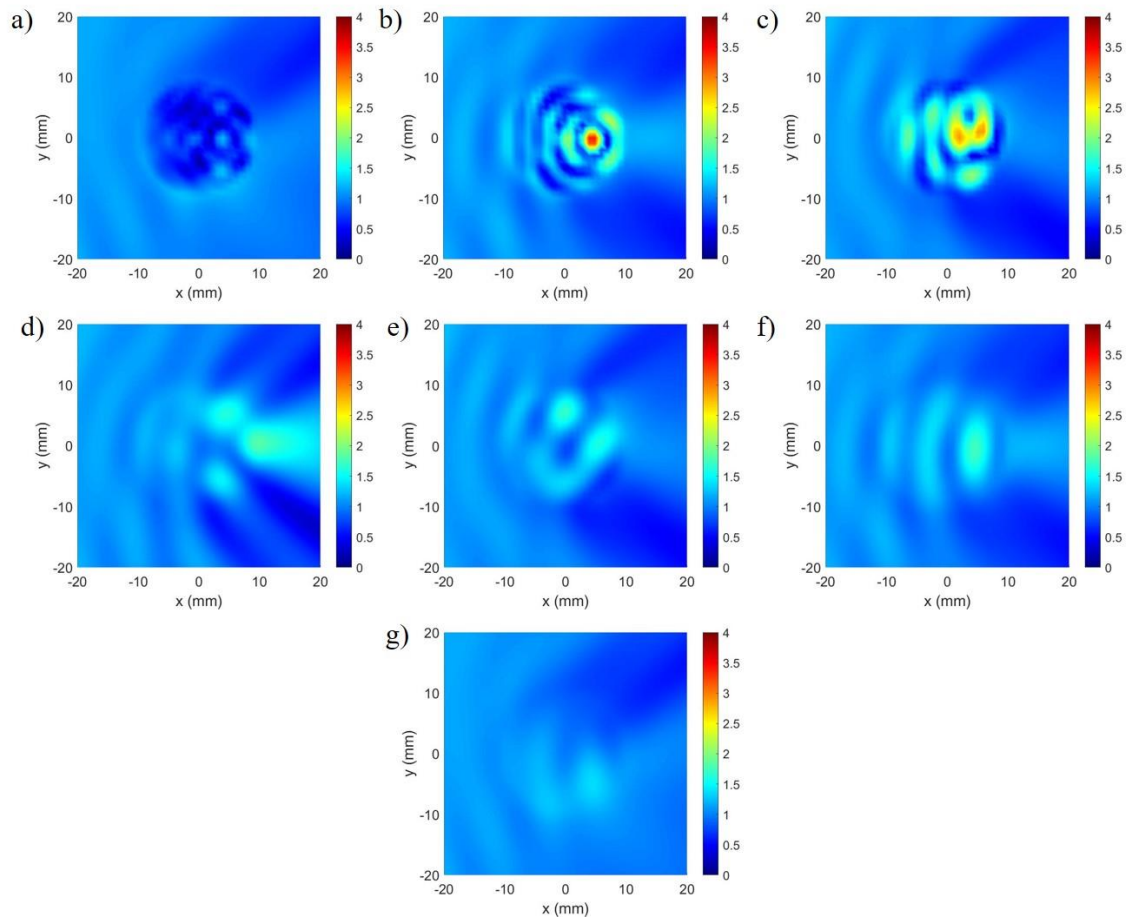
336 The scattering patterns for the modelled delamination shapes agree with each other to within
337 3%, which suggests that delamination shape does not significantly influence the scattering

338 pattern outside of the delamination. The magnitude of the scattered wave in the 0° and 180°
339 directions agrees with the measurements to within 3% for the 20mm x 20mm delamination,
340 and 5% for the 20mm x 16mm delamination. The forward scattered lobe is observed in the
341 models, but the overall shape differs from the measurements. Two regions of lower amplitude
342 are observed at 35° and 325° for both delamination sizes. However, the reduction in amplitude
343 is not as strong as observed in the experiments, consistent with the full field results in Fig. 6.
344 Overall, the FE results show good agreement with the experimental measurements, although
345 certain features, such as the forward scattered lobe, were less distinct. It has been demonstrated
346 that the interference pattern on top of the defect is strongly influenced by delamination shape
347 and size, whereas the scattered wave around the delamination is similar for the considered
348 cases.

349 **INFLUENCE OF DELAMINATION DEPTH**

350 The depth of a 20mm x 20mm circular delamination was systematically varied in 0.2mm
351 increments (between each ply layer) and the scattering of the A_0 mode was simulated. The full
352 field amplitudes over a 40mm x 40mm grid are shown for each delamination depth in Fig 8.

353 For a delamination at depth 0.2mm (Fig. 8a) a low amplitude region is observed over the
354 delamination location, in contrast to most reports in literature [17]. A thin sub-laminate has a
355 lower bending stress, so the amplitude of trapped waves on top of the delamination was
356 expected to be high at 0.2mm delamination depth. At delamination depth 0.4mm (Fig. 8b), the
357 amplitude of the scattering pattern on top of the delamination is higher, as observed previously
358 and in line with literature. When the delamination is located at 0.6mm depth (Fig. 8c) some
359 wave trapping on top of the delamination can be observed, although the scattering pattern is
360 not as symmetrical as observed at 0.4mm depth. The forward scattered component can be
361 observed between the 0° and $+45^\circ$ directions. The ply layup of the top sub-laminate at 0.6mm
362 depth is asymmetric ($-45^\circ/+45^\circ/90^\circ$) which could contribute to the steering of the forward
363 scattered wave. At the midplane of the plate (0.8mm depth, Fig. 8d) almost no wave trapping
364 on top of the delamination, but the highest 0° forward scattered component, are observed. A
365 scattered component either side of the 0° wave can be observed (approximately $\pm 45^\circ$
366 directions), although the amplitudes of the additional components are much lower. At the
367 remaining delamination depths (Fig. 8e/f/g) only very limited wave trapping on top of the
368 delamination is observed. This is likely due to the monitoring points being located on the
369 opposite side of the plate to the thinner sub-laminate, where the higher amplitude reflections

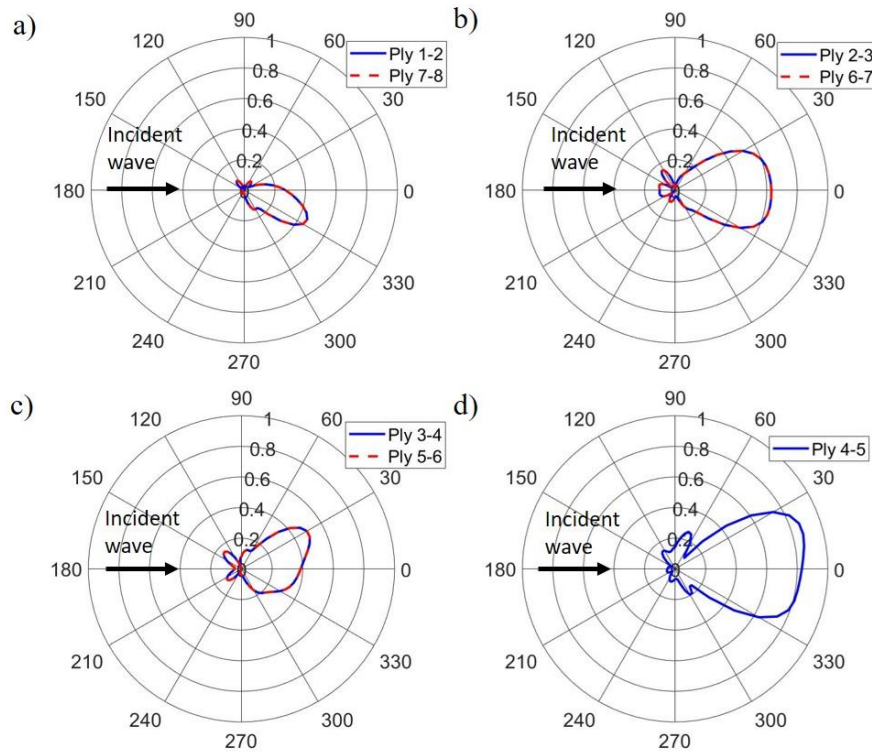


370

371 **Figure 8:** Normalised scattered wave amplitude (FFT at 50 kHz) for 20mm x 20mm circular delamination at
 372 range of delamination depths: a) 0.2mm; b) 0.4mm; c) 0.6mm; d) 0.8mm; e) 1.0 mm; f) 1.2mm; g) 1.4mm.

373 are observed. The amplitude outside of the delamination region at these depths indicate that
 374 the scattering outside of the delamination is similar at symmetric delamination depths.

375 In order to determine the influence of delamination depth on the scattering outside of the
 376 delamination, a baseline subtraction analysis was performed to determine the magnitude of the
 377 scattered wave on a 30mm circle centred on the delamination. Figure 9 compares the scattered
 378 wave for delaminations located at symmetric depths. Each pair of symmetric delamination
 379 depths has an identical scattered wave pattern outside the delamination area. Fig. 9a shows a
 380 narrow lobe (approximately 0.4 of the amplitude of incident wave) directed towards the 330°
 381 direction for delamination depths 0.2mm and 1.4mm, likely due to energy focusing along the
 382 fibres of the outer -45° direction plies. At delamination depths 0.4mm and 1.2mm (Fig. 9b) a
 383 symmetric lobe in the 0° direction is observed, with a higher amplitude than the 0.2mm and
 384 0.6mm cases, which could be due to the symmetric layup of the top sub-laminate (+/-45°
 385 direction). Increasing the delamination depth to 0.6mm or 1.0mm generates a lobe with the
 386 highest amplitude in the 30° direction. The highest amplitude of the scattered wave occurs for



387

388 **Figure 9:** Scattered wave around a 30mm circle of measurement points, obtained via baseline subtraction.
 389 Symmetric delamination depths plotted together: a) ply 1-2 (0.2mm) and ply 7-8 (1.4mm) b) ply 2-3 (0.4mm) and
 390 ply 6-7 (1.2mm) c) ply 3-4 (0.6mm) and ply 5-6 (1.0mm) d) ply 4-5 (0.8mm – midplane).

391 a delamination at the midplane of the plate (Fig. 9d). Constructive interference due to the
 392 symmetric sub-laminae could contribute to the higher amplitude.

393 The results presented in Fig. 9 indicate that the delamination depth and ply lay-up of the sub-
 394 lamina influence the direction of scattered waves outside of the delamination. The scattered
 395 wave can therefore be used to determine two possible through thickness locations of the
 396 delamination. At all delamination depths the backscattered amplitude is small, which suggests
 397 that a pulse-echo detection approach for SHM of the composite plate would have limited
 398 sensitivity. For a pitch-catch approach, the forward scattered wave shows a counterintuitive
 399 increase in amplitude behind the delamination rather than the often expected decreased
 400 amplitude behind the damage. The pitch-catch approach could be more reliable for detecting
 401 delaminations, but care must be taken, as the direction of the forward scattered lobe may differ
 402 from the incident propagation direction.

403 This investigation has focused on guided wave interaction with simple circular and ellipse
 404 shaped delaminations. Whilst these damage shapes can occur as part of multilayer damage,
 405 wave scattering around real BVID will likely differ from that of the idealised shapes presented

406 here. The procedure for incorporating damage into the FE model presented in this work could
407 potentially be extended to incorporate more complex damage if separate damage data is
408 available, for example X-ray CT data [7]. Some studies have focused on detection and sizing
409 of the major (largest) delamination at real BVID [44] and wave trapping has been demonstrated
410 to be sensitive to multi-layered delaminations [30]. This indicates that the methodology
411 presented in this work could be applied to more realistic damage types.

412 **CONCLUSIONS**

413 Guided wave propagation and scattering at an ellipse shaped delamination in a quasi-isotropic
414 composite laminate has been investigated through experiments and FE simulation. The
415 artificial delamination was located asymmetrically through the full thickness of the plate. Full
416 field non-contact laser measurements verified the wave trapping phenomena with increased
417 amplitude on top of the delamination, and visualised the forward scattered wave and shadow
418 regions behind the defect. A full 3D layered FE model containing a zero-volume delamination
419 was developed and showed good agreement with the experimental results. The convergence of
420 the model was investigated by varying element size and good convergence was observed in the
421 undamaged laminate outside of the delamination region. Inside the delamination significant
422 amplitude variation was observed between element sizes, however the qualitative location of
423 the peaks showed good agreement. The influence of delamination shape and depth were
424 investigated numerically. Small changes in delamination shape were found to have a significant
425 effect on the interference pattern on top of the delamination, but limited effect on the scattered
426 wave directivity some distance from the defect. The region of high amplitude on top of the
427 delamination could be used to estimate delamination size and shape. Delamination depth
428 significantly influenced both the interference pattern on top of the delamination, and the
429 scattering pattern outside of the delamination, due to the different ply layups of the sub-
430 laminate. Generally, both wave trapping and forward scattered components were observed for
431 delaminations located between the outer plies of the laminate. The largest forward scattered
432 amplitude occurred at the mid-plane delamination, likely due to the symmetrical layup of the
433 sub-laminates. The incident wave was removed, and the scattered wave was isolated by
434 performing a complex difference baseline subtraction to obtain the angular energy distribution.
435 At all delamination depths negligible backscattered amplitude was observed, indicating that
436 delaminations may be difficult to detect using a pulse-echo SHM approach. The strong forward
437 scattered amplitude indicates that a pitch-catch approach could be more appropriate, although
438 care must be taken as the forward scattered component is not always directed along the incident

439 wave propagation direction. The delamination shapes investigated in this study are idealised
440 compared to real BVID, however the methodology presented could be extended to incorporate
441 more complex damage types.

442 **DATA AVAILABILITY**

443 The raw and processed data required to reproduce these findings cannot be shared at this time
444 as the data also forms part of an ongoing study.

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