

1 **Measurement and Simulation of Sooting Characteristics by an ATJ-SKA Biojet Fuel and**  
2 **Blends with Jet A-1 fuel in Laminar Diffusion Flames**

3 Bo Tian<sup>a,b</sup>, Anxiong Liu<sup>c,d</sup>, Cheng Tung Chong<sup>e\*</sup>, Luming Fan<sup>a</sup>, Shiyao Ni<sup>a</sup>, Andrew Hull<sup>f</sup>,  
4 Angelica Hull<sup>f</sup>, Stelios Rigopoulos<sup>d</sup>, Kai Luo<sup>c</sup>, Simone Hochgreb<sup>a</sup>

5 <sup>a</sup> Department of Engineering, University of Cambridge, Trumpington Street, CB2 1PZ Cambridge, UK

6 <sup>b</sup> College of Engineering and Technology, University of Derby, Markeaton Street, DE22 3AW Derby, UK

7 <sup>c</sup> Department of Mechanical Engineering, University College London, Torrington Place, London WC1E 7JE, UK

8 <sup>d</sup> Department of Mechanical Engineering, Imperial College London, South Kensington Campus, London SW7 2AZ, UK

9 <sup>e</sup> China-UK Low Carbon College, Shanghai Jiao Tong University, Lingang, Shanghai 201306, China

10 <sup>f</sup> Swedish Biofuels AB, Fjällvägen 3, 181 31 Lidingö, Sweden

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11 **Abstract**

12 We investigate the sooting propensity of an Alcohol-to-Jet-Synthetic Kerosene with Aromatics  
13 (ATJ-SKA) biojet fuel. The soot volume fraction and primary particle size in the pre-vaporised  
14 diffusion flames using ATJ-SKA biojet and blends with Jet A-1 at atmospheric conditions were  
15 measured experimentally and compared to numerical simulations. The measurements were  
16 conducted using extinction calibrated laser induced incandescence (LII). Within the 10%  
17 measurement uncertainty, the soot volume fractions measured using ATJ-SKA fuel do not show  
18 significant difference with measurements with Jet A-1. A comparison of the chemical  
19 composition of the fuels suggests that the Degree of Unsaturation (DoU) may not determine the  
20 sooting propensity of biojet fuels. The SEM analysis shows that diffusion flames using neat Jet  
21 A-1 produce finer soot particles and larger number density of compared to biojet and biojet  
22 surrogate. The soot model employs a semi-detailed chemical kinetic mechanism and a physical  
23 model which integrates the population balance equation governing the soot particle size  
24 distribution with the in-house reactive flow solver for multicomponent ideal gases. The model  
25 predicted the soot maximum soot volume fraction (SVF<sub>m</sub>) in the neat biojet case and the blended  
26 cases with Jet A-1 fuels within an error margin of 13% comparing with the measured values.  
27 However, the predicted a soot volume fraction distribution patterns differ with the measured  
28 ones and the possible reasons are discussed.

29 **Key words :** Biojet fuel; Soot; Laser induced incandescence (LII); Diffusion flame

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## 30 **1. Introduction**

31 The aviation industry is expected to grow over the next two decades in tandem with the growing  
32 population [1]. Passenger and cargo traffic for aviation industry is forecast to grow at the rate  
33 of 5% per annum until 2034 [2], while the International Air Transport Association (IATA) has  
34 projected an increase of air-travel passengers to 7.2 billion by 2035 [3]. The increase in travel  
35 will inevitably consume more aviation fuels and will in turn lead to an increase in pollutant  
36 emissions and greenhouse gases. The release of fine particles from the aircraft engine,  
37 commonly known as particulate matter (PM), has been a subject of scientific investigation  
38 owing to its impact on the upper atmosphere [4] and local air quality near airports [5]. Biomass-  
39 derived jet fuels, also known as biojet fuels, have gained much attention in recent years owing  
40 to sustainability and the potential of GHG reductions [6,7]. It is expected that the uptake of  
41 biojet fuel will continue to grow in the near future, in response to the decarbonization target set  
42 by IATA and the aviation community to reduce GHG by 50% (relative to 2005 level) by 2050  
43 for the aviation sector, where a substantial portion of GHG reduction is to be achieved via the  
44 adoption of biojet fuel [1]. The ultimate goal of reducing GHG and pollutant emissions has  
45 spurred the development of biojet fuel via different production pathways and feedstocks, hence  
46 detailed understanding of the fuel chemistry and pollutant formation mechanism becomes  
47 important.

48 Evaluation of the sooting propensity of alternative jet fuels in real jet engines has been  
49 performed by various research groups [8,9]. In a CFM56-7B engine test simulating the landing  
50 and take-off cycle, Lobo *et al.* [9] showed a reduction of 62% of PM emissions was achieved  
51 for the neat FT fuel compared to the Jet A-1 fuel. The reduction of PM emissions was attributed  
52 to the absence of aromatics content in FT fuel, as opposed to the 18.5 vol% of aromatics in the  
53 Jet A-1. Although lower aromatics content in synthetic fuel blend may result in lower soot,  
54 other problems such as insufficient swelling of engine seals was reported to occur [10,11].  
55 Hence, a minimum of 8.4 vol% aromatics content for synthetic jet fuel blend is specified under  
56 the ASTM D7566 standard [12]. Scripp *et al.* [13] tested two biojet fuels in a CFM56-5C4  
57 engine, i.e. catalytic hydrothermolysis jet (CHJ) fuel and alcohol-to-jet (ATJ) fuel. The neat  
58 ATJ fuel, which contains <1% of aromatics, showed a reduction of 70% in PM emissions,

59 whereas the CHJ fuel showed an increase in PM due to higher aromatic content (20.9 vol%)  
60 and lower fuel hydrogen content. The morphology of the biojet fuel soot exhaust from a J-85  
61 turbojet engine was examined at various thrust levels. The lower concentration of aromatics in  
62 biojet fuel blend resulted in a delayed particle inception at lower concentrations, thus allowing  
63 more dilution to occur in the fuel-rich soot region [14]. These engine tests have consistently  
64 shown that PM emissions are strongly correlated with the aromatics content, but detailed study  
65 of the combustion chemistry for biojet fuel is needed to elucidate the effect on soot formation  
66 without the complication of engine geometry and flow dynamics. Such information would be  
67 useful for soot model development and could serve as a validation target for fuel surrogate  
68 models.

69 The smoke point of a fuel, defined as the maximum flame height at which the fuel burns without  
70 smoking, is a standard specification in ASTM D7566 for measuring the sooting tendency of  
71 alternative jet fuel. In general, sooting tendency is inversely proportional to smoke point, where  
72 a low smoke point value indicates high sooting tendency and vice versa. Won *et al.* [15]  
73 reported that alternative jet fuels with low aromatic content exhibit considerably higher smoke  
74 point than conventional jet fuel, with FT-derived SPK showing the highest smoke point value  
75 of ~86 mm. The current ASTM D7566 specifies the minimum smoke point required for the  
76 final biojet/jet fuel blend is 25 mm or 18 mm with a maximum 3 vol% of naphthalenes, but no  
77 batch requirement on smoke point for synthetic jet fuel in neat form. The threshold sooting  
78 index (TSI), which is related to smoke point and molecular structure of fuel [16], is another  
79 method commonly employed to assess the sooting tendency of alternative jet fuel.  
80 Measurement of the smoke point of synthetic jet fuel derived from coal and gas blended with  
81 regular jet fuel at 50% vol. revealed that the soot concentration and TSI are strongly dependent  
82 on the aromatic content of the fuel [17]. Synthetic jet fuel with low aromatics content generally  
83 exhibits low sooting tendency compared to jet fuel. Although smoke point and TSI are useful  
84 indicators for assessing the sooting tendency in a practical combustor, information regarding  
85 the soot formation pathway and chemical oxidation is lacking. To examine the soot formation  
86 process at a fundamental level, a more advanced optical-based diagnostic method is needed to  
87 yield the spatial-temporal information of soot evolution in flame.

88 The group of Sung *et al.* [18] investigated the soot volume fraction of biojet fuel including FT-  
89 SPK, hydroprocessed esters and fatty acids from camelina (HEFA-Camelina), and alcohol-to-  
90 jet (ATJ) fuel in a non-premixed flame configuration at atmospheric conditions using laser-  
91 induced incandescence (LII). The results showed that the soot mass fraction for the less sooty  
92 alternative jet fuel is sensitive to fuel composition, strain rate and reactant concentration. Hong  
93 *et al.* [19] quantified the total soot volume of aviation bio-paraffin blended with 10-25 vol% of  
94 propylbenzene to study the soot formation in a co-flow laminar diffusion wick-fed flame using  
95 the light extinction method. It was reported that the soot concentration for bio-paraffin is only  
96 marginally different from those of straight-chain dodecane. An accurate quantification of the  
97 total soot produced in biojet fuel is useful and can serve as validation targets for fuel and flame  
98 model development, as well as enabling the prediction of soot emissions in combustor  
99 modelling.

100 In the present paper, the soot volume fractions of a practical biojet fuel, a synthetic paraffinic  
101 kerosene with aromatics derived from the alcohol-to-jet pathway, blends of biojet/jet fuel and  
102 surrogates of biojet fuel (39% n-dodecane, 52% iso-octane and 11% n-propylbenzene by  
103 volume) are quantified using the extinction-calibrated LII in an undiluted, pre-vaporised co-  
104 flow diffusion flame setup [20]. The technique has been shown to be a reliable method for soot  
105 quantification from a series of biofuels tests [21,22]. The spatial soot volume fraction (SVF)  
106 distribution within the flame structure of biojet flame is mapped and compared with the baseline  
107 jet fuel, followed by an investigation of the soot morphology using an electron microscope.

108 A numerical model is developed to simulate the 2D SVF distribution maps in the tested flames  
109 and compared with the measured data. A semi-detailed chemical kinetic mechanism for the  
110 pyrolysis and combustion of a large variety of practical fuels is employed for the calculation of  
111 gaseous phase reactions. The particle inception and size growth are modelled using a population  
112 balance method with integrated in-house reactive flow solver for multicomponent ideal gases.  
113 The model captured the key features of the SVF distribution, including distribution pattern and  
114 maximum SVF (with <10% error) in tested flames.

115 The present work of examining the complex fuel chemistry and formation of soot of biojet fuel  
116 at a fundamental flame level can contribute to the understanding of PM formation at engine

117 level.

## 118 2. Experiment

### 119 2.1 Fuel and surrogates

120 The biojet fuel tested in the present study is the Alcohol-to-Jet-Synthetic Kerosene with  
 121 Aromatics (ATJ-SKA) produced by Swedish Biofuels AB. Selected chemical and physical  
 122 properties are shown in Table 1. The fuel is composed mostly of iso- and n-alkanes, with low  
 123 values of cyclo-paraffinic hydrocarbons and polyaromatics. The aromatic species in the fuel  
 124 are mostly mono-aromatic. The di-aromatic content is almost negligible.

125 **Table 1.** Properties of the tested ATJ-SKA. The data in the table were provided by Swedish  
 126 Biofuels AB.

Test	Method	Unit	Value
Mono-aromatic content	ASTM D 6379	wt%	11.5
Di-aromatic Content	ASTM D 6379	wt%	0.2
Poly-aromatic Content	EN 12916	wt%	<0.1
Olefins	ASTM D 1319	vol%	1.5
Density @ 15 °C	ASTM D 4052	kg/m <sup>3</sup>	784
Distillation IBP	ASTM D 86	°C	160.4
Distillation FBP	ASTM D 86	°C	260.4
Residue	ASTM D 86	vol%	1.5
Loss	ASTM D 86	vol%	0.2
Flash point	IP 170	°C	46.0
Smoke point	ASTM D 1322	mm	27.2
Total oxygen	EN 13132	wt%	<0.2
Specific energy	ASTM D 3338	MJ/kg	43.56
Viscosity at -20 °C	ASTM D 445	mm <sup>2</sup> /s	3.891

127 The surrogates of the Jet A-1 and biojet for the modelling are listed in Table 2. The surrogate  
 128 for Jet A-1 is based on three criteria: (1) atomic composition and H/C ratio; (2) degree of  
 129 unsaturation (DoU); (3) fraction of cyclic alkane and aromatics. The DoU of a hydrocarbon  
 130 C<sub>n</sub>H<sub>m</sub> is defined as  $u=1+n-m/2$  [23]. The surrogate for the biojet is referred from Richter *et al.*'s  
 131 previous study on the fuel [24], which follows the detailed chemical analysis depicting a typical  
 132 component of the specific chemical family [25].

133 **Table 2.** Upper rows: Composition surrogate of Jet A-1; Bottom rows: biojet (Swedish Biofuels  
 134 AtJ-SKA) selected for soot formation simulation. The values of the Yield Soot Indices (YSI)  
 135 quoted were extracted from Ref. [23].

<b>Jet A-1 surrogate</b>					
<b>Formula</b>	<b>Name</b>	<b>wt%</b>	<b>Mol%</b>	<b>CAS</b>	<b>YSI</b>
nC <sub>16</sub> H <sub>34</sub>	n-hexadecane	50.25	37	544-76-3	11.7
C <sub>10</sub> H <sub>18</sub>	decahydronaphthalene	44.78	54	91-17-8	53.7
C <sub>7</sub> H <sub>8</sub>	toluene	4.97	9	108-88-3	172.5
<b>Biojet surrogate</b>					
nC <sub>12</sub> H <sub>26</sub>	n-dodecane	38.81	30	112-40-3	9.8
iC <sub>8</sub> H <sub>18</sub>	iso-octane	52.06	60	540-84-1	23.8
nC <sub>9</sub> H <sub>12</sub>	n-propyl benzene	9.13	10	95-63-6	260.6

136 The density of the two fuels are measured in the present study and shown in Table 3 along with  
 137 other relevant parameters. The density of Jet A-1 (0.793 g/cm<sup>3</sup>) and biojet (0.784 g/cm<sup>3</sup>) are  
 138 very similar, so that the volumetric blending ratio also corresponds to the mass blending ratio.  
 139 The heating values of the components in the biojet surrogate are obtained from the National  
 140 Institute of Standards and Technology (NIST) database [26–28], and the overall heat value of  
 141 the surrogate is estimated as a weighted mean value of each component as:

$$142 \quad Q = \sum_{i=1}^n Y_i Q_i \quad (1)$$

143 where  $Y_i$  and  $Q_i$  are mass fraction and heating value of each component. The calculated heating  
 144 value of the biojet surrogate is 47.02 MJ/kg. The DoU of the Jet A-1 (0.95) and ATJ-SKA biojet  
 145 (0.90) are also close. The DoU,  $u$ , of the surrogate is 0.40, and is estimated using Eq. (2)

$$146 \quad u = \sum_{i=1}^n X_i u_i \quad (2)$$

147 where  $X_i$  and  $u_i$  are mole fraction and degree of unsaturation of each of the N components. The  
 148 mean atomic composition, H/C ratio and DoU of the ATJ-SKA biojet are all remarkably similar  
 149 to that of Jet A-1 (within 5% difference for each variable), while the biojet surrogate (shown in  
 150 Table 2) has lower density and significantly smaller DoU.

151 **Table 3.** Properties of tested Jet A-1, biojet, and biojet surrogate. The densities were measured in

152 the present study using ASTM D 4052. Data of the Jet A-1 fuel are obtained from Refs. [29,30];  
 153 the formula and heating value of biojet were measured according to ASTM D3338. Heating values  
 154 of the components in the biojet surrogate were obtained from the NIST database [26–28].

	Jet A-1	Biojet (B100)	Biojet surrogate (S100)
<b>Density at 20 °C (g/cm<sup>3</sup>)</b>	0.793	0.784	0.723
<b>Heat value (MJ/kg)</b>	43.29	43.59	47.02
<b>Average formula (-)</b>	C <sub>11</sub> H <sub>22.1</sub>	C <sub>10.5</sub> H <sub>21.2</sub>	C <sub>9.3</sub> H <sub>19.8</sub>
<b>H/C ratio (-)</b>	2.009	2.019	2.130
<b>Degree of unsaturation (-)</b>	0.95	0.90	0.40
<b>Stoichiometric mixture fraction <math>Z_{st}</math> (-)</b>	0.0636	0.0635	0.0629
<b>Stoichiometric flame temperature (K)</b>	2593	2604	2754

155 The properties of the blended mixtures are shown in Table 4. Each mixed fuel is denoted by the  
 156 volumetric blending ratio BXX, or SXX where XX is the percentage of biofuel (B) or biojet  
 157 surrogate (S) in each mixture.

158 **Table 4.** Properties of the tested blending cases. Each fuel is denoted by the volumetric blending  
 159 ratio BXX, or SXX where XX is the percentage of biofuel (B) or biojet surrogate (S) in each  
 160 mixture.

	B10	B20	B50	B80	S10	S20	S50	S80
<b>Density at 20 °C (g/cm<sup>3</sup>)</b>	0.792	0.791	0.789	0.786	0.786	0.779	0.758	0.737
<b>Heat value (MJ/kg)</b>	43.32	43.35	43.44	43.53	43.63	43.98	45.07	46.22
<b>Average formula (-)</b>	C <sub>10.9</sub> H <sub>22.0</sub>	C <sub>10.9</sub> H <sub>21.9</sub>	C <sub>10.7</sub> H <sub>21.6</sub>	C <sub>10.6</sub> H <sub>21.4</sub>	C <sub>10.8</sub> H <sub>21.9</sub>	C <sub>10.6</sub> H <sub>21.6</sub>	C <sub>10.1</sub> H <sub>20.9</sub>	C <sub>9.6</sub> H <sub>20.2</sub>
<b>H/C ratio (-)</b>	2.018	2.009	2.019	2.019	2.028	2.038	2.069	2.104
<b>DoU (-)</b>	0.94	0.94	0.92	0.91	0.89	0.83	0.67	0.50
<b><math>Z_{st}</math> (-)</b>	0.0636	0.0636	0.0639	0.0635	0.0636	0.0635	0.0633	0.0631
<b>Flame <math>T</math> (K)</b>	2594	2595	2598	2602	2608	2623	2670	2720

## 161 2.2 Pre-vaporised diffusion flame setup

162 Undiluted pre-vaporised biojet fuel laminar diffusion flames are used in the present study. Soot  
 163 formation in a non-premixed laminar jet flame has been extensively studied [31] and had  
 164 provided a standard experiment platform for sooting propensity studies of hydrocarbon fuels.  
 165 However, in most of the previous studies, the tested fuel was diluted with N<sub>2</sub> [32–34], argon  
 166 [35], or mixed with methane [36] to lower the heat release and minimise the onset of gravity-  
 167 led instability of the flame. Yet the dilution effect itself may significantly affect the soot

168 formation and yield in these types of flames [37]. In this study, the stability issue is resolved by  
 169 using larger vapour delivery tubing and a precisely controlled evaporating system, so that  
 170 dilution carrier gas is not necessary, which simplifies the analysis. The burner and fuel delivery  
 171 system are shown in Fig. 1. The liquid was injected into the stainless-steel fuel tube by a  
 172 precisely controlled syringe pump (Infusion ONE Syringe Pump with  $\pm 0.5\%$  accuracy). A  
 173 precisely controlled, closed loop, preheating system was used to heat the tube well above the  
 174 boiling point of the fuels, that is, around  $400^\circ\text{C}$ , to make sure the fuels were fully vaporised  
 175 before entering the flame. The burner is a standard non-premixed burner as used in our previous  
 176 studies [31,38]. A co-flow of air at  $0.18\text{ m/s}$  is added to protect the flame from oscillation. The  
 177 operating conditions of the burner are listed in Table 5. The feeding mass rates for all cases are  
 178 kept at  $0.10\text{ g/min}$ , unless explicitly indicated.

179 The flame temperature for each case is estimated using the assumption of complete burning  
 180 at stoichiometric conditions:

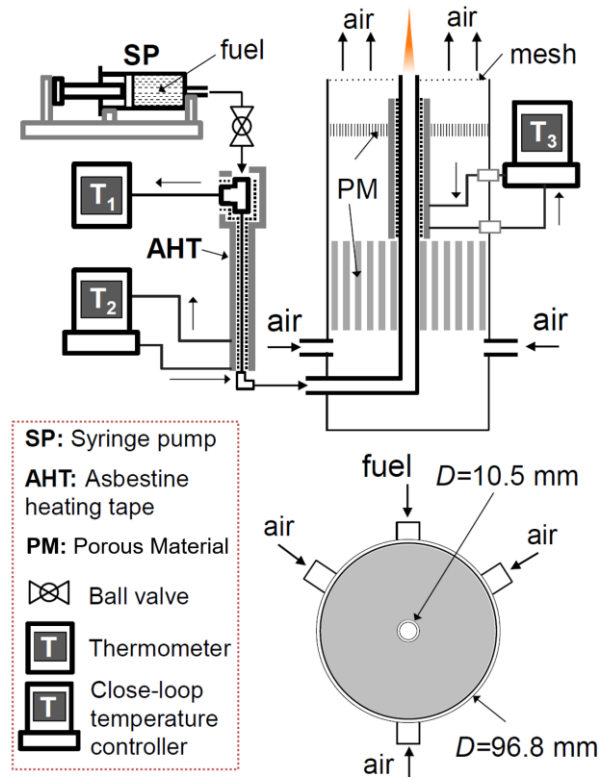
$$181 \quad T_f = Y_{fu,0} Z_{st} \frac{Q}{c_p} - (T_{ox,0} - T_{fu,0}) Z_{st} + T_{fu,0} \quad (3)$$

182 where  $Y_{fu,0}$  is the mass fraction of fuel in the fuel stream,  $Q$  the heating value from Table 3, and  
 183  $c_p$  is the specific heat of the mixture, and the value is  $1.216\text{ kJ/kg}\cdot\text{K}$ , which is taken as the  
 184 specific heat at constant pressure (1 atm) of air at  $1500\text{ K}$  [39]. The stoichiometric mixture  
 185 fraction is calculated using Eq. (4):

$$186 \quad Z_{st} = \frac{Y_{ox,0} / S}{Y_{fu,0} + Y_{ox,0} / S} \quad (4)$$

187 where  $Y_{ox,0}$  is the mass fraction of oxygen in the oxidizer stream,  $S$  is the oxygen to fuel ratio  
 188 by mass at stoichiometry, which are obtained via the chemical stoichiometric calculation based  
 189 on the average formula (listed in Table 4). Estimated temperature values are shown on Table 4.





**Fig. 1.** Cross section (upper) and the top view (bottom) of the co-flow pre-vaporised diffusion jet flame burner.

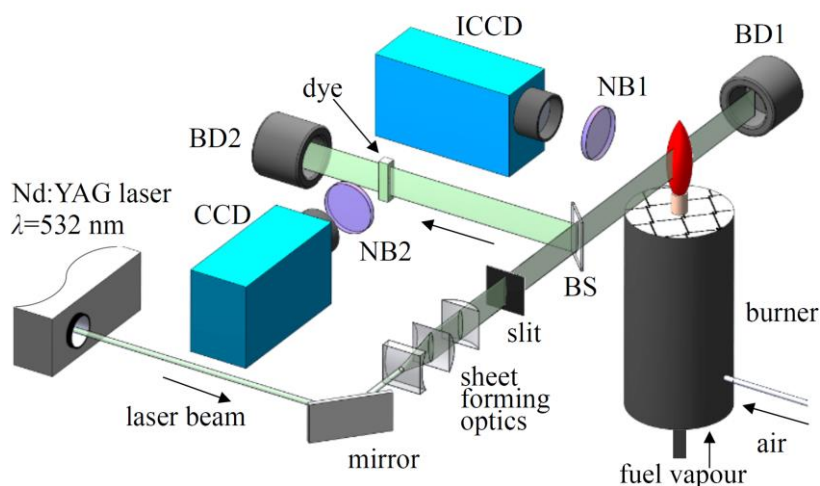
**Table 5.** Geometry and operating conditions of the burner systems

<b>Jet diameter (mm)</b>	10
<b>Fuel vaporisation</b>	Fuel injection, preheat and revalorised
<b>Fuel preheating temperature (°C)</b>	350-390
<b>Co-flow medium</b>	Air
<b>Co-flow velocity (cm/s)</b>	18
<b>Fuel flow rate (g/min)</b>	0.100

### 2.3 Extinction calibrated planar LII system

The extinction calibrated planar 2D LII system has been proven as a robust and non-intrusive method to quantitatively measure the soot volume fraction in flames. The set-up is shown in Fig. 2, which is similar to the system used in our previous studies [37,40,41]. The laser source is a 532 nm Nd:YAG laser (Litron nanoPIV) with pulse frequency within 10–25 Hz. The laser beam was carefully expanded and trimmed into a parallel top-hat laser sheet by a series of sheet forming and trimming optics (Thorlabs cylindrical lens with focal lengths of 75, – 25 and 100 mm, respectively, and an aperture). The cross section of the laser sheet is a rectangle of

202 approximate dimensions,  $31 \text{ mm} \times 0.5 \text{ mm}$ . The top-hat laser beam energy profile was  
 203 monitored using a cuvette filled with Rhodamine 6G dye, dissolved in ethanol solution. A small  
 204 portion, 1% in energy terms, of the laser sheet is reflected into the cuvette to induce fluorescence  
 205 and the luminosity is captured using a CCD camera (LaVision Imager Pro X 4M,  $1 \mu\text{s}$  gate  
 206 width,  $1024 \times 1024$  pixels) equipped with a Nikon AF Micro Nikkor 60 mm lens ( $f/5.6$ ) and a  
 207 narrow band filter (Thorlabs FB600 - 10, central wavelength =  $600 \pm 2 \text{ nm}$ , FWHM =  $10 \pm 2$   
 208 nm). As the intensity of the fluorescence is proportional to the local laser energy, the shape of  
 209 the fluorescence profile can be used to detect the uniformity of the energy distribution in the  
 210 top-hat laser sheet.



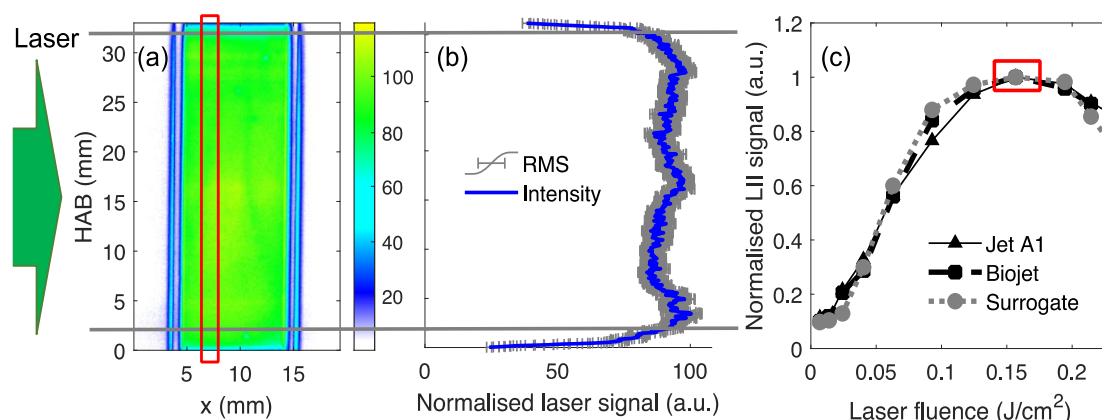
211

212 **Fig. 2.** Schematic of LII measurement setup. CCD Charge-Coupled Device Camera, BS  
 213 beam splitter, NB1  $400 \pm 20 \text{ nm}$  band filter, NB2  $600 \pm 5 \text{ nm}$  band filter, BD beam dump.

214 The fluorescence profile in the cuvette is shown in Fig. 3(a). The representative averaged laser  
 215 intensity profile over a continuous sequence of 500 shots is normalised (to 100%) as shown in  
 216 the centre figure, along with the local intensity fluctuation of the laser sheet, which remains  
 217 below 10%.

218 The dependence of the LII signal on the energy intensity per unit area (fluence) of the laser  
 219 sheet was also examined. The three unblended neat cases, real Jet A-1, ATJ-SKA biojet and  
 220 biojet surrogate, are tested. The mean LII intensity from HAB = 0 to 31 mm over 100 shots of  
 221 the three neat fuel flames are plotted against the mean laser energy fluence of the laser sheet in  
 222 Fig. 3(c). The LII signal rises with the laser fluence and reaches a plateau around  $0.15 \text{ J/cm}^2$ .

223 The peak level is selected to conduct the measurements, as at this point the LII signal is less  
 224 sensitive to the local laser energy fluctuations.



225

226 **Fig. 3.** (a) Rhodamine 6G fluorescence excited by laser sheet in a cuvette and (b) the  
 227 normalized laser intensity profile over the vertical region along vertical coordinate HAB, as  
 228 highlighted in the cuvette. The fluctuation of the laser intensity or spatial fluency is reflected  
 229 in the error bars, for values below 8% of the average; (c) Fluence dependence of the LII  
 230 signal for the neat Jet A-1, biojet and biojet surrogate as a function of the fluence of laser  
 231 sheet. The values of LII signal intensities are normalised by the maximum value of each  
 232 flame type. The peak level, highlighted by the red rectangle, is selected for the LII  
 233 measurement.

234 The LII images were quantitatively calibrated by the line-of-sight extinction method using a  
 235 638 nm wavelength continuous-wavelength diode laser source, with correction for signal-  
 236 trapping. The full details of the quantitative calibration and correction procedure can be found  
 237 in previous studies [20,40].

## 238 2.4 SEM/TEM analysis

239 The soot produced from the flames was collected by using the thermophoretic deposition  
 240 method described in Ref. [42]. A quartz plate was pre-cooled to 0°C and placed in the flame at  
 241 a fixed HAB of 15 mm for a duration of less than 1 second. As all test flames are highly  
 242 buoyancy controlled, a fixed sampling HAB ensures a constant residence time for the soot  
 243 inception and growth. The soot sampled from the flames was cooled and examined using the  
 244 LEO GEMINI 1530VP FEG-SEM system. The primary particle diameter was directly

245 measured from the SEM images, and the sizes of randomly selected 100 soot particles were  
246 fitted using a lognormal distribution [22].

### 247 **3. Soot modelling and numerical framework**

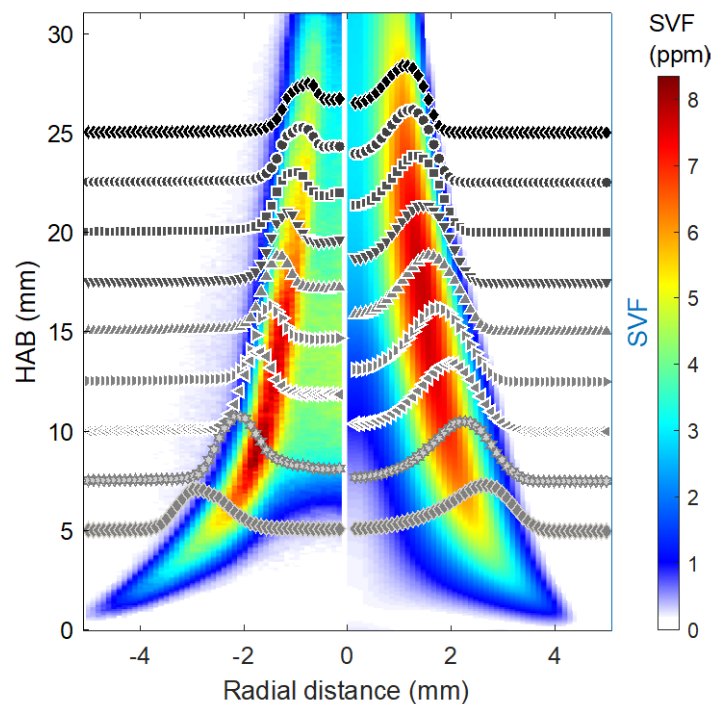
248 The model used for soot formation simulation employs a semi-detailed kinetic mechanism [43]  
249 for the pyrolysis and combustion of a large variety of practical fuels, including gasoline, jet  
250 fuels, diesel and biodiesel. Considering 249 chemical species and 8153 combined chemical  
251 reactions, this mechanism was developed based on hierarchical modularity and then validated  
252 using a number of experimental data sets on the laminar flame speeds of hydrocarbon and  
253 oxygenated fuels. The mechanism has been integrated in the CFD program BOFFIN, for the  
254 chemical reactions of the jet fuel and biojet surrogates, as well as the soot formation precursors.  
255 For example, long-chain alkanes, alkenes and aromatic hydrocarbons represent the composition  
256 of the practical fuels approximated in Table 2 (see Section 2.1). In addition, aromatic  
257 hydrocarbons, including naphthalene (A2), phenathrene (A3) and pyrene (A4), are set in the  
258 chemical kinetics to model the nucleation process in the soot formation.

259 The physical model integrates the population balance equation governing the soot particle size  
260 distribution with the in-house reactive flow solver for multicomponent ideal gases [44]. A  
261 feature of the simulation framework is a recently developed method for solving the population  
262 balance equation that combines accuracy in the prediction of the distribution with conservation  
263 of the soot volume fraction during the coagulation process. Besides detailed gas phase chemical  
264 kinetics, the model incorporates a complete set of PAH-based nucleation, condensation,  
265 HACA-based surface growth and oxidation kinetics as well as size-dependent coagulation and  
266 aggregation. Based on morphological considerations, the surface areas and geometrical  
267 properties of soot particles were estimated separately for primary particles and aggregates. The  
268 same empirical parameters in the soot model corresponding to the BBP chemical kinetics [45],  
269 obtained from a recent simulation of soot formation in an ethylene co-flow flame [46], were  
270 also used. The same soot model together with the chemical kinetics [43] in this study has been  
271 used to simulate soot formation in a co-flow flame with fuels of diesel and biodiesel surrogate  
272 [22]. The results showed that this soot model can effectively capture the reduction of soot  
273 formation on adding biodiesel fuels into diesel.

## 274 4. Results and discussion

### 275 4.1 Flame height and soot distribution

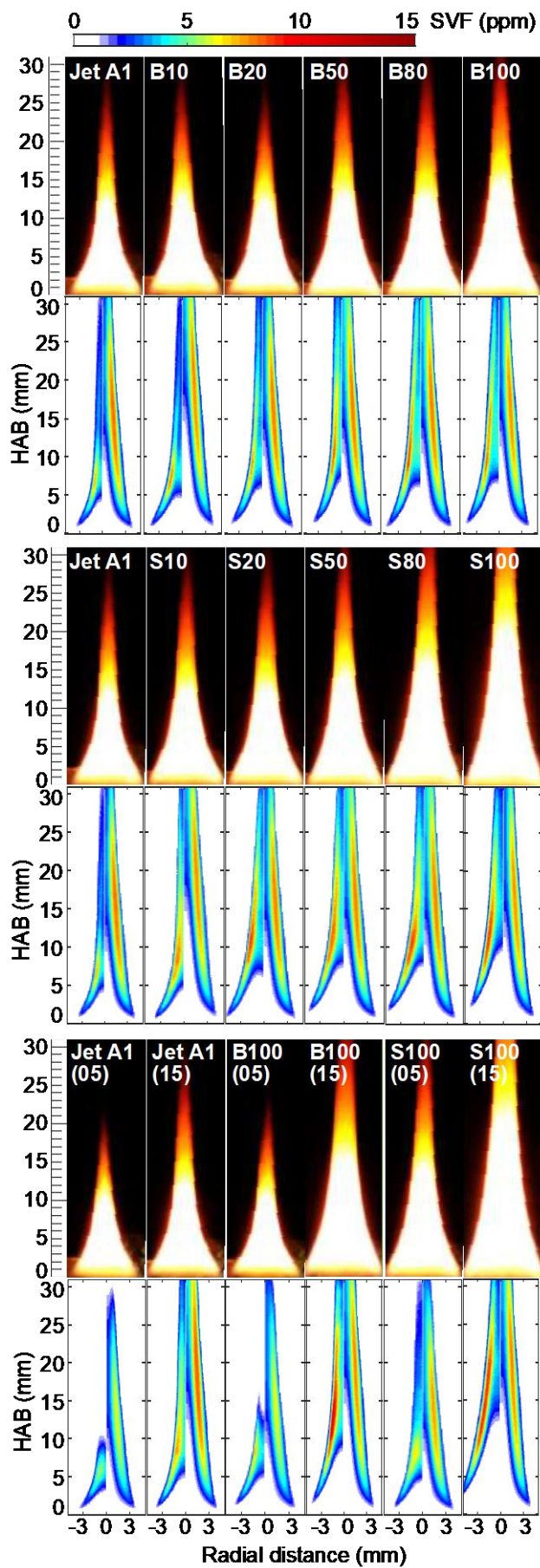
276 Figure 4 shows a typical comparison of soot volume fraction measurements with the simulation  
277 results, in this case for the B100 flame. The broken lines show profiles plotted in steps of  
278 2.5 mm HAB from 5 mm to 25 mm. Both measured and model results indicate a similar soot  
279 inception HAB (the height where SVF exceeds 0.05 ppm for the first time), immediately above  
280 the nozzle exit of the burner ( $< 2$  mm). The maximum soot volume fraction  $SVF_m$  appears in  
281 the reaction zone at the flame edge. The measured  $SVF_m$  in the B100 case is 8.3 ppm, while the  
282 modelled  $SVF_m$  in this particular case is 7.9 ppm, which is a good agreement in this particular  
283 case, and within the measurement uncertainty ( $\sim 10\%$ ) [31]. However, the measured location  
284 of  $SVF_m$  is around 12 mm at a radius of 2 mm, which is located at a lower position than the  
285 modelled value. Similarly, in the flame centre, the soot inception takes place at  $HAB = 7$  mm  
286 (where soot volume fraction exceeds 0.05 ppm for the first time along the stream line), which  
287 is also lower than modelled soot inception height by 3 mm. There are many possible reasons  
288 for the discrepancies, including the lack of a specific oxidation model for soot formed from  
289 these particular fuels, as well as inaccuracies in the diffusivity of the particles formed.



290

291 **Fig. 4.** Measured (left) and modelled (right) SVF in B100 flame from HAB = 0 to 31mm. Dotted  
292 lines show profiles plotted in steps of 2.5 mm HAB.

293 Figure 5 shows the natural luminous photos of flames and soot volume fraction (SVF)  
294 distribution in the tested Jet A-1 and biojet blending flames. The SVF data for the cases in Fig. 5  
295 are attached in the form of a readable TIFF figure in the Appendix. Each panel of two rows  
296 shows photos of each case in the top row, and on the second row of the pair, the measured SVF  
297 on the left half of each case, and the modelled results on the right half. On the bottom two rows,  
298 the flow rate of fuel is indicated in parentheses as in g/min (05) or (15).



300 **Fig. 5.** Each panel of a pair of rows shows photos of each case in the top row, followed by a  
 301 bottom row containing the measured SVF on the left half of each case, and the modelled  
 302 results on the right half. The fuel is denoted by the volumetric blending ratio BXX, or SXX  
 303 where XX is the percentage of biofuel (B) or biojet surrogate (S) in each mixture. On the  
 304 bottom two rows, the fuel flow rate is indicated in parentheses as in g/min (05) or (15).

305 Figure 5 shows that the visible luminous flame height of the cases in the top panel are similar.  
 306 According to the diffusion theory of jet flames [47–49], when the flame is dominated by high  
 307 buoyancy- and the initial flow velocity is ignored, the flame height  $H_f$  of a cylindrical diffusion  
 308 jet flame can be estimated as:

$$309 \quad H_f = \frac{22400\dot{m}}{4\pi D_0 MW \cdot \ln(1+S^{-1})} \left( \frac{T_0}{T_f} \right)^{0.67} \quad (5)$$

310 where  $\dot{m}$  is the fuel mass consumption rate in kg/s;  $D_0$  is the diffusion coefficient of the  
 311 mixture in  $\text{m}^2/\text{s}$  at the reference temperature  $T_0$ ;  $MW$  is the molecular weight of the fuel. Table  
 312 4 shows that the values  $T_f$  of Jet A-1 and biojet are similar; moreover, as the mean formula of  
 313 Jet A-1 and biojet are similar, the  $MW$  and  $S$  of fuels are also similar. Assuming a constant value  
 314 of  $D_0$  in tested flames of Jet A-1, biojet and their blending (first row of Fig. 5), the visible flame  
 315 heights should be very similar. The measured  $H_f$  of the flames in the first row is within the range  
 316  $28 \pm 3$  mm, which is about twice the predicted  $H_f$  using Eq. 5 ( $\sim 13$  mm). The large discrepancy  
 317 between the calculated and measured  $H_f$  could be caused by an insufficient soot oxidation  
 318 reaction time, and the absence of heat loss via radiation in the model, which results in  
 319 overestimations of the flame temperature, the reaction rate and hence the required residence  
 320 time is shorter and a smaller  $H_f$  is predicted [50].

321 A comparison across the measured SVF maps of Jet A-1, B10 to B100 cases (left panel in each  
 322 subfigure of the second row of Fig. 5) shows the SVF distribution patterns are very similar in  
 323 these cases. Along the flame edge, soot appears very close to the burner nozzle ( $HAB < 2$  mm)  
 324 and grows along the streamline until it reaches a maximum soot volume fraction ( $SVF_m$ ). At  
 325 the flame centre, the soot formation is delayed due to heat transfer from the flame edge to the  
 326 centre [51], thus the HAB where soot appears is higher than that at flame edge by 4-7 mm. In



327 all tested biojet/Jet A-1 flames (first row), the soot model roughly captures the typical  
328 distribution pattern of soot in the co-flow diffusion hydrocarbon jet flame: the maximum SVF  
329 appears along the streamline at the flame edge (the annular region of the cylindrical flame),  
330 rather than along the flame centreline. However, there are key discrepancies between the  
331 experimental and modelling data: (1) along the flame centre, the measured sooting points (the  
332 HAB where SVF exceeds 0.05 ppm for first time) are lower than the predicted ones; (2) at the  
333 annular region, the distribution of the soot is slightly broader than the measured patterns. As  
334 discussed in the context of Fig. 4, discrepancies may be caused by the inaccuracies in chemical  
335 model and species diffusivities. The current model includes many reactions, including light  
336 hydrocarbons, PAHs, several long-chain alkanes, alkenes and saturated and non-saturated  
337 methyl esters. Yet model validation relies on results for sooting from gaseous flames. The model  
338 requires as input fuel composition, ratio of carbon-hydrogen-oxygen, bond saturation and  
339 heating values. Soot modelling relies on empirical parameters calibrated according to the  
340 measured soot morphology (average primary particle size) in ethylene flames [44], rather than  
341 the present biojet or Jet A-1 fuel flames. Therefore, rates of formation of key species including  
342  $C_2H_2$ , OH, PAHs may not be accurate, thus directly affecting the predictions of the soot model.

343 Luminosity and SVF for flames of neat biojet surrogate (S100) and their blends with Jet A-1  
344 (S10, S20, S50, S80) are shown in the middle rows of Fig. 5, showing a slight increase in  $H_f$   
345 with blending ratio, as well as higher SVF values distributed over a higher distance. This is  
346 consistent with higher soot propensity in the biojet surrogate/Jet A-1 flame compared to pure  
347 Jet A-1. The estimated diffusion flame temperature of the biojet surrogate is the highest (~2754  
348 K) comparing the Jet A-1 (~2593 K) and biojet flames (~2604 K), which could lead to higher  
349 rates of soot formation, and thus visible luminosity. A direct measurement of the temperature  
350 in the tested heavy sooting flames was difficult as the soot particles easily deposit on the tip of  
351 the thermocouple. The comparison between the model and experimental results of the biojet  
352 surrogate + Jet A-1 flames (S10, S20, S50, S80, S100 cases, the second line in Fig. 5) shows  
353 similar disagreements with the measured values, as discussed above.

354 The third pair of rows in Fig. 5 shows the neat Jet A-1, biojet and surrogate flames for reduced  
355 and increased fuel flow rates of 0.05 g/min (jet A1 (05), B100(05), S100(05)) and 0.15 g/min

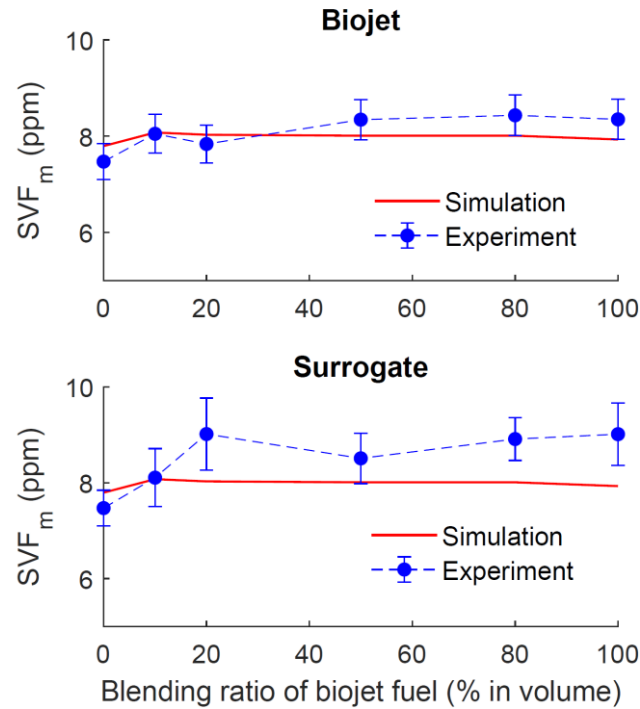
356 (jet A1(15), B100(15), S100(15)), respectively. Given the expected proportionality suggested  
357 in Eq. (5), it is not surprising that the luminous flame height of Jet A-1 (05) is lower than Jet A-  
358 1 (fuel consumption rate is 0.10 g/min) flame by 10 mm (70%). The measured SVF in Jet A-1  
359 (05) is also lower than Jet A-1(10) flame, as the residence time for soot particle growth is limited.  
360 The reduction of SVF in the Jet A-1 (05) flame compared to the Jet A-1 flame is captured by  
361 the model, but model predictions of the flame height are about twice the measured value. The  
362 Jet A-1(15) flame has neither a higher flame nor significantly larger SVF than Jet A-1(10) flame.  
363 This might be because the radiation loss in the heavy sooting flames is significant. When fuel  
364 consumption rate increases from 0.10 g/min to 0.15 g/min, the soot yielding increases and the  
365 heat loss via soot radiation become a dominant factor reducing the flame temperature and the  
366 flames were quenched. Some unburnt fuel vapour was emitted from the flame tip together with  
367 soot particles. The same trend was also observed in the B100(15) and S100(15) cases. A parallel  
368 comparison among the measured SVF maps of neat Jet A-1, biojet and biojet surrogate cases  
369 shows that high SVF region at flame edge extend further downstream for the B100 and S100  
370 flames compared with the Jet A-1 flame. This trend is even more pronounced for Jet A1 (15)  
371 compared with B100 (15) and S100 (15). This might be caused by a higher radiation loss in the  
372 B100 (15) and S100 (15) flames. The loss resulted in a lower flame temperature in the  
373 downstream of B100 (15) and S100 (15) flames and the oxidation of soot in are hence delayed.  
374 In general, as shown in Fig. 5, blending of biojet with the Jet A-1 does not fundamentally change  
375 the flame structure and soot distribution in the tested diffusion flames. The surrogate could  
376 reasonably represent the sooting propensity of the biojet fuel. As shown in Figs. 4 and 5, the  
377 model reasonably and quantitatively captures the distribution of  $SVF_m$  soot within the tested  
378 flames. However, differences in chemical composition and oxidation rates may not be perfectly  
379 captured, and similarly the absence of details on radiation losses may overestimate the  
380 temperatures, leading to differences in both soot formation and oxidation.

### 381 **4.3 Maximum and mean soot volume fraction**

382 The maximum soot volume fraction,  $SVF_m$  .in the tested cases are plotted in Fig. 6 against the  
383 volumetric blending ratio of biojet (upper) and biojet surrogate (bottom) with Jet A-1 fuel. The  
384 error bars in of the measured values are calculated based on the standard deviations of 20 LII

385 images for each case. The  $SVF_m$  in the biojet blending cases varies from 7.8 ppm (B20) to 8.4  
386 ppm (B80). Considering the uncertainty of the LII measurement of approximately 10%, the  
387 difference between the two values is insignificant. Thus, it is reasonable to conclude that the  
388 addition of the ATJ-SKA biojet does not change the soot yield of Jet A-1 fuel in terms of the  
389 maximum soot volume fraction. It is worthy to pointed out is that these SVF values shown in  
390 Figs 4, 5 and 6 also contains calibration uncertainties besides the random measurement  
391 uncertainty. Due to the nature of the optical measurement of soot, the calibration uncertainties  
392 could be as high as 40% [31]. The calibration process and uncertainty were analysed in detail  
393 in our previous study [31]. The interaction between light beam and soot particles is highly  
394 complex, as it depends on the wavelength of probing beam, maturity and chemical composition  
395 of soot (e.g. H/C ratio) [52], thus the calibration uncertainty is difficult to be quantified and  
396 hence was not shown in Fig. 6. However, the calibration affects the SVF measurement in a  
397 linear manner, thus it does not change the conclusion drawn in the present study, which are  
398 based on the relative comparison among the teste fuels.

399 The modelled  $SVF_m$  agrees with the measured data within the range of measurement uncertainty  
400 in all tested cases, which is impressive. The bottom part of Fig. 6 shows that the blended cases  
401 of biojet surrogate with the Jet A-1 produce higher  $SVF_m$  than the biojet/Jet A-1 blending cases  
402 by a small margin (<15%) in all corresponding cases. Our previous studies on petroleum and  
403 bio diesels show that the degree of unsaturation (DoU) of the fuels may play a key role in the  
404 sooting propensities of fuels [40].



**Fig. 6.** Maximum soot volume fraction against the blending ratio of biojet fuel (upper) and surrogate (bottom)

405

406

407

408 The DoU of the Jet A-1 and biojet shown in Table 3 (Section 2.1) 0.95 and 0.90, respectively,  
 409 whereas the DoU of the biojet surrogate is 0.40. So, it is very surprising to observe higher soot  
 410 values than the Jet A-1 and ATJ-SKA biojet, which is the opposite of the expected effect.

411 The Yield Soot Indices (YSI) is another indicator of the sooting propensity of jet fuels  
 412 [23,36,53]. The YSI of the surrogates for the Jet A-1 and biojet fuels are estimated as a mean  
 413 of the molar weighted values:

414

$$\text{YSI} = \sum_{i=1}^n X_i \text{YSI}_i \quad (6)$$

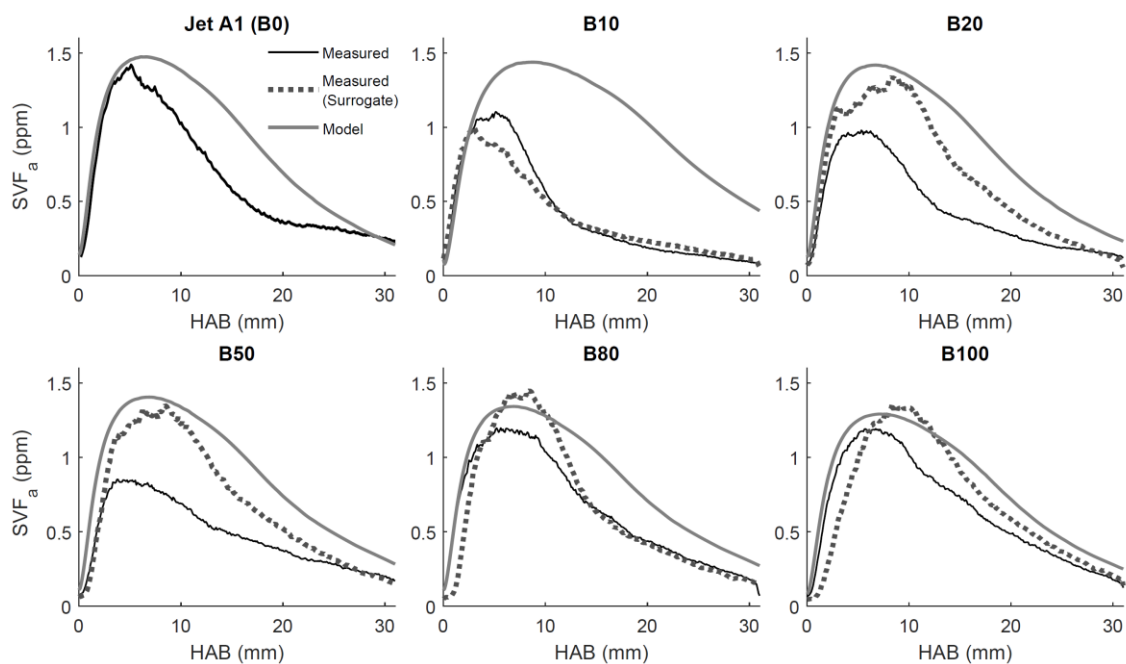
415 The YSI of each component of the surrogate for the Jet A-1 and biojet are obtained from [23]  
 416 (listed in the Table 2). Based on the YSI values in Table 2, the calculated YSI values for the  
 417 surrogate of biojet and Jet A-1 are 43.27 and 48.84 respectively. The YSI of the biojet surrogate  
 418 is lower than the Jet A-1 surrogate by 11%, whereas the biojet surrogate produces 15% higher  
 419  $\text{SVF}_m$  than biojet and Jet A-1. The modelled values of  $\text{SVF}_m$  in the neat jet A1 case (7.8 ppm)  
 420 is slightly lower than that in the neat biojet surrogate case (7.9 ppm) and indicates a comparison  
 421 opposite to that indicated by the YSI. One possible explanation for the higher soot yield of the

422 surrogate than Jet A-1 may be the presence of aromatic species. Previous studies show that the  
423 soot yielding of jet fuels are very sensitive to the presence of aromatic species in the fuels  
424 [30,54]. In the present study, the surrogate for the Jet A-1 contains 4.97% toluene  $C_7H_8$  in mass,  
425 which is less than the propylbenzene ( $C_9H_{12}$ ) mass fraction of 9.13% in the biojet surrogate, so  
426 it is reasonable that the Jet A-1 surrogate produce less soot than biojet surrogate. However, the  
427 YSI of decahydronaphthalene (53.7) is significantly higher than iso-octane (23.8), the  
428 calculated overall YSI of Jet A-1 (contains 44.78% decahydronaphthalene in mass) is hence  
429 slightly higher than biojet surrogate (contains 52.06% iso-octane in mass). Obviously, due to  
430 the high fraction of aromatics, the biojet surrogate overestimated the sooting tendency of the  
431 tested ATJ-SKA, but due to the presence of iso-octane (with very low YSI), the overestimation  
432 was not reflected by the value of YSI. The present study suggested that the fraction of aromatics,  
433 rather than YSI, may be a better indicator of a fuel's sooting characteristics.

434 A second measure of soot propensity may be given by the radially averaged soot volume  
435 fractions  $SVF_a$ , which is evaluated from the 2D soot distribution via Eq. (7).

$$436 \quad SVF_a = \frac{1}{\pi R^2} \int_0^R 2\pi r SVF(r) dr \quad (7)$$

437 The calculated results for  $SVF_a$  are plotted against HABs in Fig. 7. The biojet surrogate/Jet A-  
438 1 mixtures yield larger  $SVF_a$  than the biojet/Jet A-1 mixtures except the B10 case. However, at  
439 higher HABs (>20 mm), the values become closer. Around 31 mm, the  $SVF_a$  values for biojet  
440 surrogate/Jet A-1 mixtures and biojet/Jet A-1 mixtures are almost equal. The model predicts  
441 more soot in B0 to B50 cases, while in B80 and B100 cases, the peak  $SVF_a$  predicted by the  
442 model is lower than the biojet surrogate/Jet A-1 mixtures but higher than the biojet/Jet A-1  
443 mixtures.



444

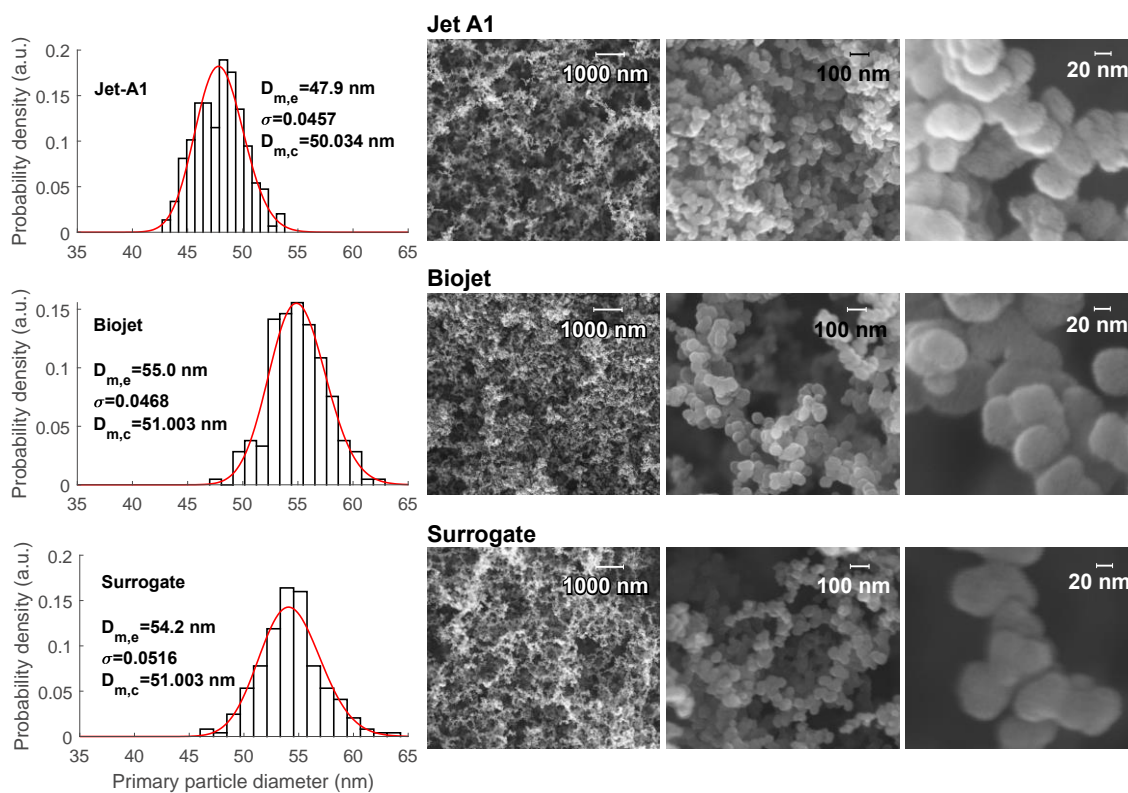
445

**Fig. 7.** Averaged  $SVF_a$  along HABs in tested cases

446 **4.4 Primary soot particle size and number density**

447 SEM images and corresponding particle size distributions for tested Jet A-1, biojet and biojet

448 surrogate pre-vaporised diffusion flames are shown in Fig. 8.



449

450 **Fig. 8.** SEM images and corresponding particle size distribution for tested Jet A-1, biojet (Swedish  
451 Biofuels ATJ) and biojet surrogate pre-vaporised diffusion flames.

452 The soot number density is estimated from the averaged soot volume fraction  $SVF_a$ , assuming  
453 particles of geometric mean agglomerate diameter  $D_m$  as determined from sampling and  
454 analysis of SEM images, via:

$$455 \quad N_p = \frac{6 \cdot SVF_a}{\pi D_m^3} \quad (8)$$

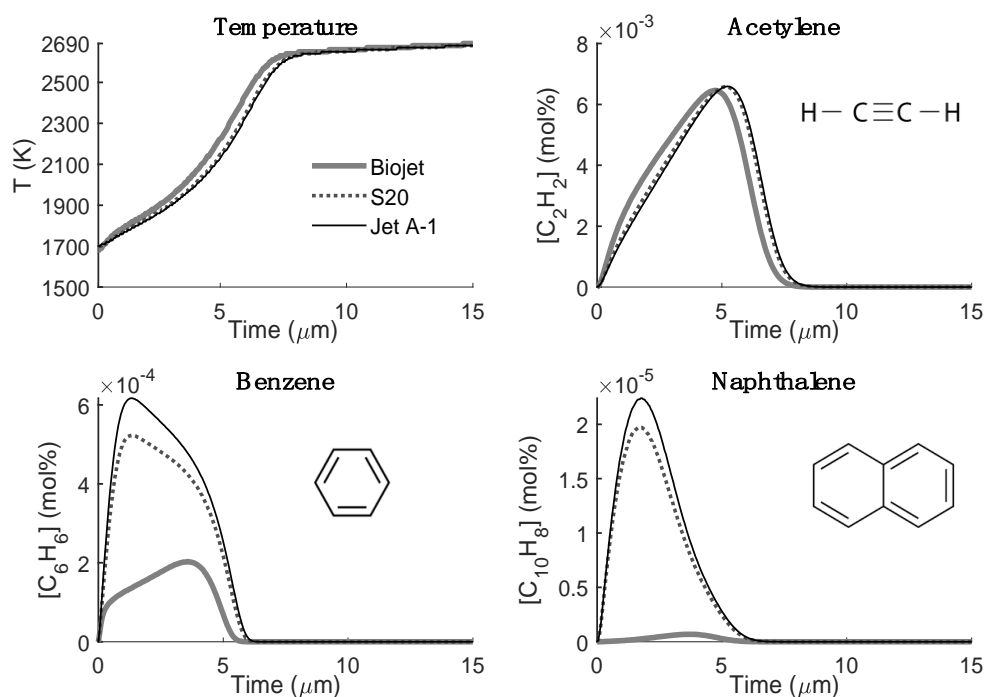
456 Estimates are only available at HAB = 15 mm, from which the data were sampled. The  
457 simulation results are shown in Table 6.

458 **Table 6.** Measured average soot volume fraction  $SVF_a$ , mean primary particle diameter  $D_m$   
459 and estimated particle number density  $N_p$  at HAB = 15 mm for neat Jet A-1 (B0), Biojet  
460 (B100) and biojet surrogate (S100) cases

	$SVF_a$ (ppm)	$D_m$ (nm)	$N_p$ ( $10^{13} \cdot m^{-3}$ )
Jet A-1	0.57	47.9	9.9
Biojet	0.72	55.0	8.3
Biojet surrogate	0.80	54.2	9.6

461 As shown in Table 6, although the  $SVF_a$  at HAB=15 mm in neat Jet A-1 flame is 20% and 28%  
462 lower than neat biojet and biojet surrogate flame, respectively, the mean values of  $N_p$  at HAB  
463 = 15 mm for Jet A-1 flame, the value of  $N_p$  in Jet A-1 flame is 19% and 3% higher than the neat  
464 biojet and biojet surrogate cases. The results indicate that tested ATJ-SKA biojet produces larger  
465 but less soot particles than the Jet A-1 fuel. The finding also implies the soot particle nucleation  
466 in the Jet A-1 flame is more frequent than the biojet and biojet surrogate, while the surface  
467 growth of soot particles is slower comparing the biojet and biojet surrogate flames. The  
468 measured primary particle size of the soot particles produced in the neat biojet flame and biojet  
469 surrogate flame are very similar and the difference in the mean diameter is within 2%. Both  
470 results agree well with the simulation data. The modelled soot particle size for distribution the  
471 neat Jet A-1, biojet and the biojet surrogate are noted as  $D_{m,c}$  and shown in Fig. 8, which agree  
472 well with the measured data. The model also successfully predicted that the Jet A-1 produced  
473 smaller particles than the other two fuels, but the difference is very narrow ( $< 1$  nm). This

474 indicates that the model may not be very sensitive in the prediction of the particle size produced  
 475 in the different fuels, and the mechanism for soot surface growth in the model, which dominates  
 476 the soot particle size, may need further adjustment.



477

478 **Fig. 9.** Temperature, mole fractions of acetylene  $C_2H_2$ , benzene  $C_6H_6$  and naphthalene  $C_{10}H_8$   
 479 produced in the combustion of the neat ATJ-SKA biojet, S20 biojet surrogate, and neat Jet A-1  
 480 surrogate.

481 To investigate the combustion performance of different chemical compositions and the effect  
 482 on soot formation, simulations of a perfect stirred reactor have been conducted in Reaction  
 483 Design's CHEMKIN-PRO commercial software with the semi-detailed mechanism. Three fuel  
 484 compositions have been studied in the stoichiometric air-fuel condition: pure jet fuel, biojet fuel  
 485 and the blend fuel with 20% biojet and 80% Jet A-1 (B20). The initial temperature is set at  
 486 1700 K for an easy ignition. The results of key species regarding soot formation are monitored,  
 487 including acetylene  $C_2H_2$  and PAHs. The temperature, mole fractions of acetylene, benzene  
 488  $C_6H_6$  and naphthalene  $C_{10}H_8$  are plotted against time in the Fig. 9. The temperature of the biojet  
 489 surrogate increases faster than Jet A-1 surrogate. Benzene and naphthalene are the key species  
 490 for soot inception, as they provide the first ring for the nascent soot particle nucleation [55,56].



491 The rate of formation of benzene and naphthalene in the ATJ-SKA biojet and S20 cases are  
492 lower than in the Jet A-1 flame. Indeed, the rate of formation of naphthalene in the ATJ-SKA  
493 biojet is negligible. This may explain the fact that the number density of soot in biojet flame is  
494 smaller than Jet A-1 flame. The yield of acetylene, the main species responsible for soot particle  
495 surface growth based on HACA mechanism, is very similar in the three cases, thus, the total  
496 soot yielding of the tested flames are in a same level.

## 497 **5. Conclusion**

498 The soot volume fraction and primary particle size in the pre-vaporised diffusion flames of an  
499 ATJ-SKA biojet fuel and its blends with Jet A-1 have been studied both experimentally and  
500 numerically. The visible flame height, spatial soot volume fraction distribution, and the  
501 maximum soot volume fraction  $SVF_m$  of neat ATJ-SKA biojet fuel and its blends with Jet A-1  
502 are close to those found for neat Jet A-1 fuel flames. The difference in  $SVF_m$  is within 8% and  
503 smaller than the measurement uncertainty. It is reasonable to conclude that the sooting  
504 propensity of the ATJ-SKA does not differ from standard Jet A-1 fuel. The flames using the  
505 biojet surrogate produce slightly more soot than the equivalent flames with biojet and Jet A-1.  
506 Both the values of  $SVF_m$  and  $SVF_{mean}$  produced in neat biojet surrogate fuel flames are higher  
507 than the values in neat biojet flames by 8.1% and 20%, respectively. Since the DoU of the biojet  
508 surrogate is lower than biojet, the results show that it is not the determinant factor for the sooting  
509 propensity of biojet fuels. This point should be taken into account in the design of jet fuel  
510 surrogates. The neat Jet A-1 produces finer soot particles and larger number density than ATJ-  
511 SKA biojet and the biojet surrogate. The result indicates the soot particle inception in the Jet A-  
512 1 flame is more frequent than the biojet and biojet surrogate, while the surface growth of soot  
513 particles is slower than the biojet and biojet surrogate flames. A simulation of the production of  
514 flame soot provides support for this conclusion. The soot model successfully predicted the soot  
515 distribution and  $SVF_m$  in the tested neat biojet case and the blended cases with Jet A-1 fuels.  
516 The differences between the measured and modelled  $SVF_m$  are within 10% of each other in all  
517 cases. In addition, the predicted soot primary particle size is within 10% of the measured values.  
518 However, the predicted  $SVF_a$  is significantly higher than the experimental data, showing the

519 model still needs further development.

## 520 **Acknowledgement**

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## 524 **List of supplementary material**

525 Soot Volume Fraction.tif

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