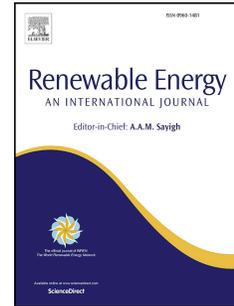


# Journal Pre-proof

Numerically efficient fatigue life prediction of offshore wind turbines using aerodynamic decoupling

Chao Chen, Philippe Duffour, Paul Fromme, Xugang Hua



PII: S0960-1481(21)00981-2

DOI: <https://doi.org/10.1016/j.renene.2021.06.115>

Reference: RENE 15640

To appear in: *Renewable Energy*

Received Date: 13 January 2021

Revised Date: 7 June 2021

Accepted Date: 8 June 2021

Please cite this article as: Chen C, Duffour P, Fromme P, Hua X, Numerically efficient fatigue life prediction of offshore wind turbines using aerodynamic decoupling, *Renewable Energy* (2021), doi: <https://doi.org/10.1016/j.renene.2021.06.115>.

This is a PDF file of an article that has undergone enhancements after acceptance, such as the addition of a cover page and metadata, and formatting for readability, but it is not yet the definitive version of record. This version will undergo additional copyediting, typesetting and review before it is published in its final form, but we are providing this version to give early visibility of the article. Please note that, during the production process, errors may be discovered which could affect the content, and all legal disclaimers that apply to the journal pertain.

© 2021 Published by Elsevier Ltd.

**Chao Chen:** Conceptualization, Methodology, Formal analysis, Software, Validation, Writing - Original Draft

**Philippe Duffour:** Conceptualization, Methodology, Writing - Review & Editing

**Paul Fromme:** Conceptualization, Methodology, Writing - Review & Editing

**Xugang Hua:** Methodology, Writing - Review & Editing, Funding acquisition

Journal Pre-proof

1 **Numerically efficient fatigue life prediction of offshore wind**  
2 **turbines using aerodynamic decoupling**

3

4 Chao Chen<sup>1</sup>, Philippe Duffour<sup>2</sup>, Paul Fromme<sup>3</sup>, and Xugang Hua<sup>1\*</sup>

5

6 <sup>1</sup>Key Laboratory for Wind and Bridge Engineering, Hunan University, Changsha,  
7 China

8 <sup>2</sup>Department of Civil, Environmental and Geomatic Engineering, University College  
9 London, United Kingdom

10 <sup>3</sup>Department of Mechanical Engineering, University College London, United King-  
11 dom

12

13

14

15

---

\*Corresponding author: cexghua@hnu.edu.cn

# 16 Numerically efficient fatigue life prediction of offshore wind 17 turbines using aerodynamic decoupling

18

19

## 20 Abstract

21

22 The fatigue life prediction for offshore wind turbine support structures is computa-  
23 tionally demanding, requiring the consideration of a large number of combinations of  
24 environmental conditions and load cases. In this study, a computationally efficient  
25 methodology combining aerodynamic decoupling and modal reduction techniques is  
26 developed for fatigue life prediction. Aerodynamic decoupling is implemented to sep-  
27 arate the support structure and rotor-nacelle assembly. The rotor dynamics were mod-  
28 elled using an aerodynamic damping matrix that accurately captures the aerodynamic  
29 damping coupling between the fore-aft and side-side motions. Soil-structure interac-  
30 tion is modelled using p-y curves, and wave loading calculated based on linear irregu-  
31 lar waves and Morison's equation at a European (North Sea) site. A modal reduction  
32 technique is applied to significantly reduce the required number of degrees of free-  
33 dom, allowing the efficient and accurate calculation of hotspot stresses and fatigue  
34 damage accumulation. The modal model was verified against a fully coupled model  
35 for a case-study, monopile supported offshore wind turbine in terms of response pre-  
36 diction and fatigue life evaluation. The modal model accurately predicts fatigue life  
37 (within 2%) for a range of parameters at a fraction of computational cost (0.5%) com-  
38 pared to the fully coupled model.

39

40 Key words: offshore wind turbines; fatigue life prediction; aerodynamic damping;  
41 modal analysis.

42

## 43 1 Introduction

44 As the size of Offshore Wind Turbines (OWTs) has been increasing in order to gener-  
45 ate electricity more efficiently, they have become more susceptible to large amplitude  
46 vibration and fatigue damage [1]. Therefore, an accurate prediction of fatigue life at  
47 the preliminary design stage is required. At present, there are many wind turbine

48 modelling software packages available, and most of them employ fully coupled mod-  
49 els in which different components of OWTs are coupled based on multibody dynam-  
50 ics. In the literature, many researchers used these fully coupled models to conduct fa-  
51 tigue damage calculation for OWTs [2]. For example, Koukoura et al. [3] studied the  
52 influence of wind-wave misalignment on fatigue in the OWT support structure. Their  
53 simulations were performed using HAWC2 [4], which is an aeroelastic software  
54 based on multibody formulation. Velarde et al. ([5][6]) also used HAWC2 to study  
55 the fatigue sensitivity and reliability of OWTs supported by gravity foundations and  
56 monopiles. Marino et al. [7] focused on the influence of alternative wave models  
57 when calculating wind turbine fatigue loads. The aero-servo-elastic software FAST  
58 [8] developed by NREL combined with an external hydrodynamic module was used  
59 by Hübner et al. [9] to obtain dynamic responses. They developed fatigue assessment  
60 methodologies for OWTs considering scattering environmental conditions. FAST  
61 modified to include Soil-Structure Interaction (SSI) matrices was used to conduct  
62 time domain simulations. Horn et al. [10] introduced a stochastic model to assess the  
63 fatigue reliability of an OWT. They used a fully coupled finite-element code  
64 USFOS/VpOne to establish the numerical model of a bottom-fixed monopile-  
65 mounted OWT.

66

67 A large number of environmental states and load cases needs to be considered when  
68 calculating the fatigue life of OWT support structures [11], requiring a significant  
69 computational effort. In a comprehensive fatigue analysis, the OWT structural re-  
70 sponse needs to be computed and analysed for each of the combinations of environ-  
71 mental parameters, leading to thousands of simulations [12]. In order to accelerate the  
72 fatigue prediction, many studies concentrated on the reduction of the number of load  
73 cases ([11][13][14][15]) or developing novel methods ([12][16]) to reduce the simula-  
74 tion requirements. Stieng and Muskulus [15] proposed a method of reducing the num-  
75 ber of required environmental states, based on importance sampling and a specially  
76 adapted two-stage filtering procedure, from which pseudo-optimal sets of load cases  
77 can be used to conduct the fatigue assessment of the monopile. Wilkie and Galasso  
78 [16] developed a computational framework to conduct the OWT fatigue reliability  
79 analysis, using Gaussian process regression to develop surrogate models of load-  
80 induced fatigue damage, which allows the reduction of the computational effort with  
81 high accuracy. Conducting the fatigue analysis of OWTs in the frequency domain

82 [17] significantly reduces the computational effort but is generally not as accurate as  
83 the time domain analysis. On the other hand, fully coupled models are usually more  
84 computationally intensive as the interaction between many components along with the  
85 environmental loading needs to be considered. In some cases, detailed Finite Element  
86 (FE) models of the support structures are required, but it is often not possible to im-  
87 plement those in current wind turbine modelling packages. As a result, a simplified  
88 decoupling approach is desirable for faster fatigue analysis. A common model simpli-  
89 fication is to lump the mass of the Rotor-Nacelle Assembly (RNA) at the top of the  
90 flexible tower and apply the aerodynamic resultant thrust together with a dashpot or  
91 an equivalent Rayleigh damping model to represent the aerodynamic damping [18].  
92 For instance, Dong et al. ([19][20]) imported aerodynamic loading from HAWC2 to  
93 USFOS to obtain the dynamic response of a jacket support structure in a 5 MW OWT  
94 and analysed the long-term fatigue accumulation. Rezaei et al. ([21][22]) studied the  
95 sensitivity of fatigue life of OWTs to damping and scour. They developed a detailed  
96 FE model in Abaqus including nonlinear soil springs, and aerodynamic loads calcu-  
97 lated by FAST. Muskulus [23] and Schafhirt and Muskulus [24] decoupled the wind  
98 turbine system by separating the aerodynamic thrust into a static mean force, a dy-  
99 namic turbulent force and a dynamic damping force. A simple expression for the  
100 thrust was obtained by fitting a thrust coefficient to fully coupled simulation results.

101

102 The definition of the aerodynamic damping in decoupled wind turbine models is usu-  
103 ally based on damping ratios. The determination of damping ratios can be based on  
104 theoretical predictions ([25][26][27]) or measurements ([28][29][30][31][32]). How-  
105 ever, using damping ratios separately in the Fore-Aft (FA) and Side-Side (SS) direc-  
106 tions to represent the aerodynamic damping in OWTs implicitly ignores the influence  
107 of damping coupling between the two directions. Tarp-Johansen et al. [33] found that  
108 the aerodynamic damping for the first lateral tower mode (in the SS direction) is dif-  
109 ferent for a normal tower configuration (the tower FA and SS motions both allowed)  
110 and a stiff downwind tower configuration (the tower FA motion not allowed). Studies  
111 by Chen et al. ([34][35]) emphasised the importance of the coupling between the FA  
112 and SS motions and developed a decoupled wind turbine model with an aerodynamic  
113 damping matrix to capture this coupling.

114

115 In summary, most studies in literature concentrated on reducing the number of load  
116 cases or developing more advanced statistical models to accelerate the fatigue analy-  
117 sis of OWTs. Among the relatively few studies using simplified decoupling models to  
118 conduct fatigue analyses, the inclusion of aerodynamic damping was usually imple-  
119 mented by using aerodynamic damping ratios, not considering the important aerody-  
120 namic damping coupling between the FA and SS motions. There is a need for compu-  
121 tationally efficient ways of calculating fatigue life of OWTs with more advanced  
122 decoupled models. This paper proposes a novel methodology, extending a previously  
123 developed model based on modal reduction and aerodynamic damping decoupling to  
124 include all relevant features such as soil-structure interaction and key dynamic cou-  
125 plings. It is organised as follows. Section 2 presents the reference monopile supported  
126 OWT which is used as a case study. The fully coupled model developed in Matlab  
127 used for reference predictions is described. Section 3 introduces the development of  
128 the decoupled full model with rigid blades and describes the modal reduction from the  
129 fully coupled model. Section 4 details the calculation of the stress time history given  
130 dynamic responses and the fatigue estimation method. Section 5 provides the fatigue  
131 life results and explores the effect of varying structural damping. Section 6 concludes  
132 the paper.

133

## 134 2 Fully coupled reference model

135 In the present study, a fully coupled aeroelastic model of a case study monopile-  
136 supported OWT was implemented in Matlab and used as a reference model against  
137 which reduced models are later compared. This structural model is a FE formulation  
138 including the blades, tower and monopile (Section 2.1) with soil springs as described  
139 in Section 2.2 representing SSI. The aerodynamic forces, presented in Section 2.3,  
140 were computed using unsteady Blade Element Momentum (BEM) theory. The hydro-  
141 dynamic force calculation is based on Morrison's equation, described in Section 2.4.  
142 The OWT model is based on the widely used 5MW reference monopile-supported  
143 offshore wind turbine published by NREL [36]. The basic properties of this OWT are  
144 listed in Table 1 and a schematic of it is shown in Fig. 1. The combination of the tow-  
145 er, transition piece, and monopile foundation is defined as the support structure of the  
146 OWT, which supports the RNA. The motivations for developing a bespoke model

147 were the ability to include SSI, as this is an important feature in monopile-supported  
 148 OWTs, and taking advantage of the improved accuracy of the FE formulation.

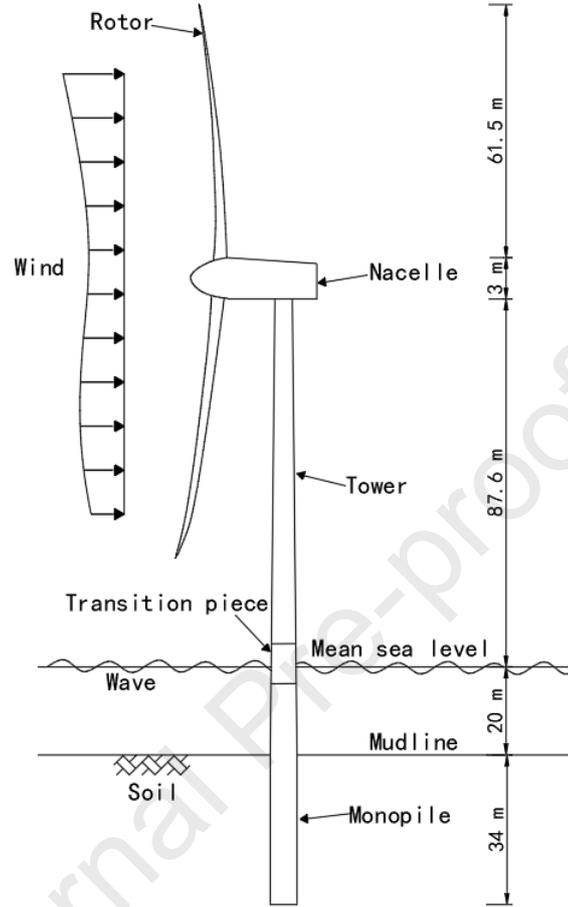


Fig. 1. Schematic of the NREL 5MW reference OWT.

149

150

151

## 152 2.1 Finite Element Model

153 In the FE model, the tower, blades and monopile were modelled using three-  
 154 dimensional Euler-Bernoulli beam elements. The numbers of beam elements for the  
 155 single blade, tower and monopile are 17, 11 and 26 respectively, bringing the total  
 156 number of beam elements is 88. For each node, there are six DOFs corresponding to  
 157 three translational motions and three rotational motions. A convergence study con-  
 158 firmed that the beam element number is sufficient. Given the material and geometrical  
 159 properties of the beam elements, the equations of motion of the OWT model can be  
 160 formulated by:

$$\begin{aligned} \mathbf{M}(t)\ddot{\mathbf{u}}(t) + (\mathbf{C}_{Struc}(t) + \mathbf{C}_{Soil}(t))\dot{\mathbf{u}}(t) + \mathbf{K}(t)\mathbf{u}(t) \\ = \mathbf{F}_{Wind}(t) + \mathbf{F}_{Wave}(t), \end{aligned} \quad (1)$$

161 where  $\mathbf{M}(t)$ ,  $\mathbf{K}(t)$  are the mass and stiffness matrices,  $\mathbf{C}_{Struct}(t)$  and  $\mathbf{C}_{Soil}(t)$  are  
 162 the viscous damping matrices representing structural damping and soil damping re-  
 163 spectively,  $\mathbf{u}(t)$  is the displacement vector,  $\mathbf{F}_{Wind}(t)$  and  $\mathbf{F}_{Wave}(t)$  are the wind  
 164 force and wave force vectors.  $\mathbf{M}(t)$  and  $\mathbf{K}(t)$  are time dependent matrices [37]  
 165 when the OWT is operating, as the rotation of the blades was taken into consideration  
 166 by introducing a time dependent transformation when assembling the global matrix  
 167 from the local elemental matrices. The structural damping and soil damping in this  
 168 study are both assumed to be proportional Rayleigh damping using the relationship  
 169  $\mathbf{C} = \alpha\mathbf{M} + \beta\mathbf{K}$ , where  $\alpha$  and  $\beta$  are Rayleigh coefficients. These were determined  
 170 such that the total damping ratios due to the structural damping in the support struc-  
 171 ture and the soil damping were 1.5% according to [38]. The structural damping of a  
 172 single blade was selected as 0.48%, following the default FAST setting. Note that the  
 173 structural and soil damping matrices are time dependent, as they are proportional to  
 174 the time-dependent mass and stiff matrices. The contribution of hydrodynamic damp-  
 175 ing and the aerodynamic damping of the tower are small compared to other damping  
 176 sources [38] and therefore were not included [33].

177

178 The nacelle was modelled using a lumped mass at the tower top, added to the mass  
 179 matrix. For simplicity, the gravitational centre of the nacelle was located at the tower  
 180 top, so that moments of inertia of the nacelle about all axes are zero. Time domain  
 181 analyses were conducted by implementing the numerical integration scheme HHT- $\alpha$   
 182 [39], which is a generalised version of the Newmark- $\beta$  method.

183

184 Table 1 Basic properties of the NREL 5MW reference OWT, based on [36].

Rotor Diameter, $R$	126 m
Hub Radius, $r_{hub}$	1.5 m
Hub Height from Mean Sea Level (MSL)	87.6 m
Water Depth (MSL?), $h$	20 m
Monopile Embedded Length	34 m
Tower Diameter, $D_{Tower}$	3.87-6.00 m
Tower Thickness, $t_{Tower}$	19-60 mm
Monopile Diameter, $D_{Pile}$	6 m
Monopile Thickness, $t_{Pile}$	60 mm
Lumped Mass at Top	$350 \times 10^3$ kg

Natural Frequency for the First Bending Mode of the Support Structure	0.24-0.25 Hz
Natural Frequency for the Second Mode of the Support Structure	1.74-1.75 Hz

## 185 2.2 Soil model

186 The soil profile used in this study is a layered combination of sandy soils typical for a  
 187 European offshore site for which the 5MW OWT model was developed. The soil pro-  
 188 file combines loose sand, medium sand, and dense sand from bottom to the pile head  
 189 with thicknesses of 14m, 14m, and 6m respectively, based on the data provided in  
 190 Appendix B in [40]. The soil properties are listed in Table 2.

191

192 Table 2 Mechanical properties of the soil profiles used in the model.

Soil type	Density $\gamma$ ( $1 \times 10^3$ kg/m <sup>3</sup> )	Poisson's ratio $\nu$	Friction angle $\varphi$	Shear modu- lus $G_s$ (MPa)	Shear wave velocity $V_s$ (m/s)	Elastic modulus $E_s$ (MPa)
Loose sand	1.75	0.30	33°	47	164	18
Medium sand	1.90	0.30	36°	109	240	42
Dense sand	2.07	0.30	38°	182	297	70

193

194 The SSI was modelled using p-y curves recommended in DNVGL-RP-C212 [41],  
 195 where  $p$  is the resistance (pressure) from the surrounding soil when the pile deflects  
 196 laterally by distance  $y$ . The p-y relationship for a vertical pile in cohesionless soil can  
 197 be established using the following equation:

$$p = Ap_u \tanh\left(\frac{k_m Z}{Ap_u} y\right), \quad (2)$$

198 where  $k_m$  is the initial modulus of subgrade reaction,  $A$  is a factor to account for  
 199 static or cyclic loading conditions,  $Z$  is the depth below the surface. This study  
 200 adopted the cyclic loading condition, as fatigue calculation corresponds to the cyclic  
 201 vibration of the monopile. The ultimate static lateral resistance,  $p_u$ , is defined as:

$$p_u = \min \left\{ \begin{array}{l} (C_1 Z + C_2 D_{Pile}) \gamma' Z, \\ C_3 D_{Pile} \gamma' Z, \end{array} \right. \quad (3)$$

202 where,  $C_1$ ,  $C_2$  and  $C_3$  depend on the friction angle of the soil,  $D_{Pile}$  is the diameter  
 203 of the monopile.

204

205 In the model, the soil was modelled by a series of horizontal soil springs characterised  
206 by Eq. (2) at different heights of the monopile foundation. The soil springs were lo-  
207 cated at the nodes of the monopile. The displacements of the nodes of the monopile  
208 were calculated given the average forces in the FA and SS directions. Then the soil  
209 springs were introduced by directly inserting the spring stiffness coefficients into the  
210 system stiffness matrix at relevant locates. In order to be consistent with the modal  
211 analysis, which will be introduced in Section 3.2, the soil springs were set to be linear  
212 such that the soil stiffness coefficients were kept constant during the time integration.

### 213 2.3 *Wind loading*

214 The wind loading calculation is based on classic unsteady Blade Element Momentum  
215 (BEM) theory ([42][43]) with corrections. The iteration loop in a steady BEM code is  
216 neglected in the unsteady BEM code since the iteration is replaced by a time evolu-  
217 tion, assuming that the time step chosen is sufficiently small. The corrections adopted  
218 in the unsteady BEM code include Prandtl and Glauert corrections [42]. To be con-  
219 sistent with the derivation leading to the aerodynamic damping matrix (described in  
220 Section 3), other corrections such as skew wake and dynamic wake corrections are not  
221 included in the unsteady BEM code.

222  
223 A non-uniform turbulent inflow wind field was used as the input to the unsteady BEM  
224 code to calculate the aerodynamic forces acting on the blade elements. A customised  
225 turbulent wind field generator was coded in Matlab, producing similar wind time se-  
226 ries compared to the wind field generator in FAST, TurbSim [44]. The Kaimal spec-  
227 trum was used to generate the turbulent wind field, and its relevant parameters (e.g.,  
228 coherence length parameters) were selected as recommended by IEC 61400-3 [45].  
229 The relationship between turbulence intensities and mean wind speeds at hub height  
230 was defined according to the Normal Turbulence Model (NTM). Medium turbulence  
231 intensity (Category B) was assumed.

232  
233 The inflow wind velocities, the velocity caused by rotor rotation and the velocities  
234 caused by blade vibration were used as input to the unsteady BEM code. The un-  
235 steady code calculated the instantaneous local aerodynamic forces for all blade ele-  
236 ments at every time step in the time integration. The aerodynamic force calculation

237 based on the customised wind field generator and the unsteady BEM code was suc-  
 238 cessfully verified against FAST (results not shown).

#### 239 2.4 Wave loading

240 Morison's equation was used for the wave loading calculation. The wave force ap-  
 241 plied to the monopile is a combination of a viscous drag force and an inertia force  
 242 which can be expressed by

$$F_{wave} = \frac{1}{2} \rho_w D_{pile} C_d |\dot{u}_w| \dot{u}_w + \frac{\pi}{4} \rho_w D_{pile}^2 C_m \ddot{u}_w, \quad (4)$$

243 where  $\dot{u}_w$  and  $\ddot{u}_w$  are the velocity and acceleration of water particles,  $C_d$  is the  
 244 drag coefficient,  $D_{pile}$  is the diameter of the monopile between the mean sea level  
 245 and the mudline,  $C_m$  is the inertia coefficient and  $\rho_w$  is the density of water.  $C_d$   
 246 and  $C_m$  were chosen as 1 and 2 respectively as the recommended values in [46]. The  
 247 velocities caused by monopile vibration were ignored in the wave loading calculation  
 248 as the monopile vibration velocities are much smaller than the wave particle veloci-  
 249 ties.

250  
 251 The wave profile is irregular and obtained by the superposition of wave components  
 252 following linear wave theory and JONSWAP spectrum [47]. For a particular frequen-  
 253 cy point  $f$ , the JONSWAP spectrum definition is given by

$$S_{JS} = S_{PM}(f) \cdot (1 - 0.287 \ln(\gamma)) \cdot \gamma^{\exp\left[-\frac{(f-f_p)^2}{2\sigma^2 f_p^2}\right]}, \quad (5)$$

254 where

$$S_{PM}(f) = 0.3125 H_s^2 T_p \left(\frac{f}{f_p}\right)^{-5} \exp\left[-1.25 \left(\frac{f}{f_p}\right)^{-4}\right]. \quad (6)$$

255  $f_p$  is the peak frequency defined as  $1/T_p$ ,  $H_s$  is the significant wave height,  $\gamma$  is  
 256 the peak-shape parameter, which is assumed to be equal to 3.3 for the North Sea con-  
 257 ditions according to [47],  $\sigma$  is the spectral width parameter.  $T_p$  is the wave peak pe-  
 258 riod. The wave elevation, velocity and acceleration time series can be obtained by  
 259 summing wave components corresponding to different wave frequencies. Combining  
 260 Morison's equation and the linear irregular waves defined above, the wave forces  
 261 were defined in the external wave force vector in Eq. (1).

262

### 263 3 Reduction to modal OWT model

#### 264 3.1 Decoupled model

265 The fully coupled model described in Section 2 can be decoupled by computing the  
 266 resultants of the aerodynamic wind-rotor interaction at the tower top. This decoupling  
 267 is briefly summarised here. It was described in more detail in [35] and [48] for on-  
 268 shore wind turbines, where wave loading and SSI were not considered. The decou-  
 269 pling process starts with the linearisation of the resultant aerodynamic forces from the  
 270 rotor into static forces and damping forces proportional to the tower top velocities, as-  
 271 suming rigid blades. These linearised aerodynamic forces are then applied on the  
 272 RNA mass lumped at the tower top and the dynamic responses of the finite element  
 273 model of the OWT support structure can be obtained, excluding the analysis of blade  
 274 vibration. This is schematically illustrated in Fig. 2. An aerodynamic damping matrix  
 275 is introduced when calculating the damping forces. This decoupling process results in  
 276 a decoupled model with rigid blades and simplifies the calculation of aerodynamic  
 277 forces applied to the rotor.

278

279 When the OWT is in operation, the tower, transition piece and monopile foundation  
 280 mainly vibrate in the FA direction ( $x$ ) and SS direction ( $y$ ). Here the vertical vibration  
 281 is neglected due to its insignificance in the decoupling process and its very small am-  
 282 plitude. The linear motions at the tower top are represented by  $\dot{x}$  and  $\dot{y}$ , and the an-  
 283 gular motions represented by  $\dot{\theta}_x$  and  $\dot{\theta}_y$ , around the  $x$  and  $y$  axes respectively,  
 284 which are defined in Fig. 2. The blades are assumed to be rigid and the blade vibration  
 285 is ignored, so parametric excitations due to rotor dynamics are not included. Combin-  
 286 ing the BEM theory and tower dynamics, the aerodynamic forces applied to a flexible  
 287 tower can be linearised to the sum of terms corresponding to the forces for an as-  
 288 sumed rigid tower, plus terms proportional to the tower top linear and angular veloci-  
 289 ties, which can be expressed as

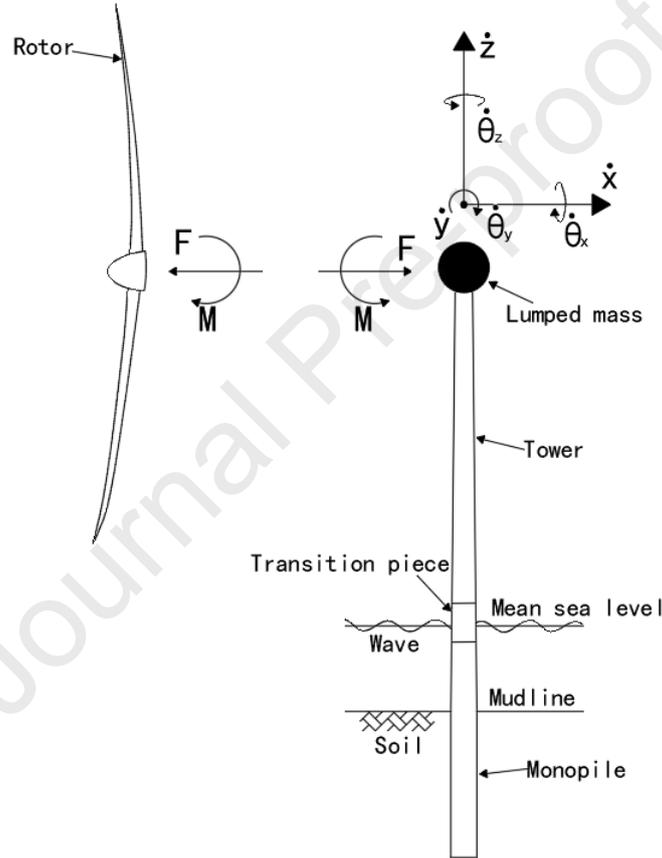
$$\mathbf{F}_{Top}^{Flex}(t) = \mathbf{F}_{Top}^{Rigid}(t) - \mathbf{C}_{Aero} \dot{\mathbf{u}}_{Top}(t). \quad (7)$$

290 The aerodynamic force resultants  $\mathbf{F}_{Top}^{Flex}(t)$  are calculated at the tower top as forces  
 291 and moments, as shown in Fig. 2.  $\mathbf{F}_{Top}^{Rigid}(t)$  does not depend on the tower vibration.  
 292  $\mathbf{C}_{Aero}$  is called the aerodynamic damping matrix, which captures the aerodynamic

293 damping caused by the wind-rotor interaction considering the coupling between the  
 294 tower top FA and SS motions. According to [48],  $\mathbf{C}_{Aero}$  is

$$\mathbf{C}_{Aero} = \begin{bmatrix} c_{xx} & c_{xy} & c_{x\theta_x} & c_{x\theta_y} \\ c_{yx} & c_{yy} & c_{y\theta_x} & c_{y\theta_y} \\ c_{\theta_x x} & c_{\theta_x y} & c_{\theta_x \theta_x} & c_{\theta_x \theta_y} \\ c_{\theta_y x} & c_{\theta_y y} & c_{\theta_y \theta_x} & c_{\theta_y \theta_y} \end{bmatrix}, \quad (8)$$

295 where the off-diagonal terms representing the damping coupling between the FA and  
 296 SS directions are not symmetric. The expression of  $\mathbf{F}_{Top}^{Flex}(t)$  is detailed in Appendix  
 297 A.



298

299 Fig. 2. Schematic illustrating the decoupling of the aerodynamic forces at tower top.

300

301 If the inflow wind field is turbulent and non-uniform,  $\mathbf{C}_{Aero}$  is a time-varying matrix.

302 To obtain a constant  $\mathbf{C}_{Aero}$  and thus simplify the aerodynamic decoupling,  $\mathbf{C}_{Aero}$

303 was calculated using an inflow wind field assumed to be uniform and constant at the

304 mean wind speed. It has been shown in a previous study [48] that the overall dynamic

305 responses from the model with the constant aerodynamic damping matrix agree well

306 with those from the model with the time-varying aerodynamic damping matrix. For a

307 particular set of mean wind speed, rotor rotation speed, and blade pitch angles, the  
 308 aerodynamic damping matrix can be calculated by following the derivations in [35]  
 309 and [48].  $\mathbf{F}_{Top}^{Rigid}(t)$  was calculated based on the non-uniform wind field and the un-  
 310 steady BEM code.

311

312 The decoupled model with rigid blades is formed as follows. The blade masses are  
 313 lumped together with the nacelle mass at the tower top, so the total number of beam  
 314 elements reduces to 37 due to the exclusion of the blade elements. The static compo-  
 315 nent of the condensed aerodynamic forces,  $\mathbf{F}_{Top}^{Rigid}(t)$ , can be directly applied at the  
 316 tower top as an external force independent of the tower top velocities. As a result, the  
 317 equations of motion for the decoupled model with rigid blades can be written as

$$\begin{aligned} \mathbf{M}'\ddot{\mathbf{u}}'(t) + (\mathbf{C}'_{Struc} + \mathbf{C}'_{Soil} + \mathbf{C}'_{Aero})\dot{\mathbf{u}}'(t) + \mathbf{K}'\mathbf{u}'(t) \\ = \mathbf{F}'_{Wind}^{Rigid}(t) + \mathbf{F}'_{Wave}(t), \end{aligned} \quad (9)$$

318 where  $\mathbf{M}'$ ,  $\mathbf{C}'_{Struc}$ ,  $\mathbf{C}'_{Soil}$ ,  $\mathbf{C}'_{Aero}$  and  $\mathbf{K}'$  are the reduced mass, structural damping,  
 319 soil damping, aerodynamic damping and stiffness matrices respectively.  $\mathbf{C}'_{Aero}$  con-  
 320 tains the terms in  $\mathbf{C}_{Aero}$  in Eq. (8) at appropriate locations.  $\mathbf{F}'_{Wind}^{Rigid}(t)$  is the external  
 321 aerodynamic force vector which includes  $\mathbf{F}_{Top}^{Flex}(t)$  at the nodes at the tower top.  
 322  $\mathbf{u}'(t)$  is the reduced displacement vector, where the prime sign represents the reduced  
 323 size of the matrices and vectors compared to those for the fully coupled model. The  
 324 model described by Eq. (9) effectively reduces the fully coupled OWT system by us-  
 325 ing finite elements to only model the support structure and capturing the wind-rotor-  
 326 tower interaction through the lumped mass at the top and the aerodynamic damping  
 327 matrix.

### 328 3.2 Modal model

329 A partial decoupling can be obtained from the equations of motion in Eq. (9) using the  
 330 normal (undamped) mode shapes. The undamped mode shape matrix  $\Psi$  can be com-  
 331 puted from the eigen analysis of the mass and stiffness matrices  $\mathbf{M}'$  and  $\mathbf{K}'$ . As the  
 332 damping matrix is not used to compute  $\Psi$ , the modes considered here are real. The  
 333 reduced displacement vector  $\mathbf{u}'(t)$  can then be written as the generalised coordinate  
 334 vector  $\alpha(t)$  multiplied by the normal (undamped) mode shape matrix:  $\mathbf{u}'(t) =$

335  $\Psi\alpha(t)$ . Multiplying the transpose of the modal shape matrix,  $\Psi^T$ , at both sides of Eq.  
 336 (9), we obtain

$$\begin{aligned} & \Psi^T \mathbf{M}' \Psi \ddot{\alpha}(t) + \Psi^T (\mathbf{C}'_{Struc} + \mathbf{C}'_{Soil} + \mathbf{C}'_{Aero}) \Psi \dot{\alpha}(t) \\ & \quad + \Psi^T \mathbf{K}' \Psi \alpha(t) \\ & = \Psi^T \mathbf{F}'_{Wind}{}^{Rigid}(t) + \Psi^T \mathbf{F}'_{Wave}(t). \end{aligned} \quad (10)$$

337 The equation above can be written in concise form:

$$\begin{aligned} & \bar{\mathbf{M}} \ddot{\alpha}(t) + (\bar{\mathbf{C}}_{Struc} + \bar{\mathbf{C}}_{Soil} + \bar{\mathbf{C}}_{Aero}) \dot{\alpha}(t) + \bar{\mathbf{K}} \alpha(t) \\ & = \bar{\mathbf{F}}_{Wind}{}^{Rigid} + \bar{\mathbf{F}}_{Wave}, \end{aligned} \quad (11)$$

338 where  $\bar{\mathbf{M}}$  and  $\bar{\mathbf{K}}$  are the modal mass and stiffness matrices,  $\bar{\mathbf{C}}_{Struc}$ ,  $\bar{\mathbf{C}}_{Soil}$  and  
 339  $\bar{\mathbf{C}}_{Aero}$  are the modal structural, soil and aerodynamic damping matrices,  $\bar{\mathbf{F}}_{Wind}{}^{Rigid}$  and  
 340  $\bar{\mathbf{F}}_{Wave}$  are the modal wind force and wave force vectors.  $\bar{\mathbf{M}}$  and  $\bar{\mathbf{K}}$  are diagonal ma-  
 341 trices due to orthogonality of the normal modes. As the structural damping and soil  
 342 damping are considered as Rayleigh damping,  $\bar{\mathbf{C}}_{Struc}$  and  $\bar{\mathbf{C}}_{Soil}$  are also diagonal.  
 343 However, as  $\mathbf{C}'_{Aero}$  is not of a Rayleigh damping type,  $\bar{\mathbf{C}}_{Aero}$  is neither symmetric  
 344 nor diagonal. Therefore,  $\bar{\mathbf{C}}_{Aero}$  causes coupling between different modes and differ-  
 345 ent vibration directions. It is possible to consider a particular number of modes by  
 346 truncating the matrices and vectors in Eq. (11). For example, if considering the first  
 347 two bending modes of the support structure, the system matrix size becomes 4×4 and  
 348 the decoupled model is reduced to a 4-DOF model. Theoretically, considering more  
 349 modes results in more accurate dynamic responses. However, it was found that the  
 350 dynamic responses of the OWT are dominated by the first two bending modes of the  
 351 support structure. For simplicity, only the results from the 4-DOF model are shown  
 352 and used later. The time history of the generalised modal coordinate  $\alpha(t)$  was ob-  
 353 tained by solving Eq. (11) using the HHT- $\alpha$  time integration method. The dynamic  
 354 responses of the whole tower and monopile were calculated using modal expansion  
 355 described by  $\mathbf{u}'(t) = \Psi\alpha(t)$ . If displacement-dependent p-y curves are implemented  
 356 to calculate the soil reactions at every time step, a time-dependent stiffness matrix in-  
 357 cluding soil stiffnesses is inevitably introduced, making the modal reduction infeasible.  
 358 Therefore, the inclusion of the soil springs in the modal model was realised using  
 359 constant soil spring stiffness corresponding to the slope of the p-y curve at the average  
 360 monopile lateral displacement.

361

362

## 363 4 Fatigue damage prediction

364 For a given mean wind speed, the dynamic responses of the whole support struc-  
 365 ture can be obtained from the modal model just described after time integration. Then,  
 366 for a specific hotspot, the stress time history is calculated from the dynamic as de-  
 367 scribed in the following sections.

368

369

### 370 4.1 Stress calculation

371 In the fully coupled model, the dynamic component of the normal stresses  $\sigma_{zz}$  at po-  
 372 sition  $(x, y)$  within a tower cross-section and at position  $z$  along the tower can be  
 373 directly obtained from the internal forces and the cross-section properties. The axial  
 374 stresses are made of a static component cause by the weight and a dynamic part  
 375 caused by the dynamic part of the FA and SS bending moments. In the reduced modal  
 376 model developed in Section 3.2, the displacement, velocity, and acceleration respons-  
 377 es along the wind turbine support structure can be directly obtained by superposition,  
 378 but further computation is necessary to obtain section stresses. Therefore, a method is  
 379 needed to estimate the stress time history at arbitrary locations using the displace-  
 380 ment, velocity and acceleration responses. Pelayo et al. [50] presented a method to ex-  
 381 tract the dynamic stress from the responses under dynamic loading and the modal pa-  
 382 rameters of a structure. This method was formulated for beams under uniaxial  
 383 bending [50], but the stresses in the FA and SS directions need to be considered sim-  
 384 ultaneously for OWTs. Therefore, this method was extended here to enable the calcu-  
 385 lation of stresses for bending in two directions.

386

387 Using the finite element method, the displacements  $u_x(z, t)$  and  $u_y(z, t)$  in FA and  
 388 SS directions at any arbitrary height  $z$  along an individual beam element can be ap-  
 389 proximated by

$$u_x(z, t) = \mathbf{N}^e(z)\mathbf{u}_x^e(t), \quad (12)$$

$$u_y(z, t) = \mathbf{N}^e(z)\mathbf{u}_y^e(t), \quad (13)$$

390 where  $\mathbf{N}^e(z)$  is the elemental shape function vector,  $\mathbf{u}_x^e(t)$  and  $\mathbf{u}_y^e(t)$  are the nod-  
 391 al displacement vectors in  $x$  and  $y$  directions for the beam element. For a given  
 392 cross-section-section and time, the Euler-Bernoulli bending strains are the product of  
 393 the local curvatures and the distance from the neutral axis in each direction. The

394 curvatures can be obtained from Eqs. (12) and (13) by differentiating the shape func-  
 395 tions twice with respect to  $z$ . The resultant longitudinal stress at time  $t$ , position  
 396  $(x, y)$  within the cross-section and  $z$  along the tower, is then the linear superposition  
 397 of the two strains multiplied by Young's Modulus  $E$ :

$$\sigma_{zz}(x, y, z, t) = -E(\mathbf{N}^{e''}(z)\mathbf{u}_x^e(t)x + \mathbf{N}^{e''}(z)\mathbf{u}_y^e(t)y). \quad (14)$$

398 The signs result from the conventions defined in Fig. 1.

#### 399 4.2 *Fatigue damage calculation*

400 The fatigue damage accumulation at the location of concern was calculated by rain-  
 401 flow counting the stress time series. The S-N curve was selected according to DNV  
 402 recommendations [49] and defined by

$$\log(N) = \log(\bar{a}) - m \log\left(\Delta\sigma \left(\frac{t_c}{t_{ref}}\right)^k\right), \quad (15)$$

403 where  $N$  refers to the number of cycles to failure,  $\Delta\sigma$  is the stress range,  $m$  is the  
 404 negative inverse slope of the S-N curve,  $\log(\bar{a})$  is the intercept of  $\log N$  axis,  $t_{ref}$   
 405 is the reference thickness,  $t_c$  is the thickness through which a crack will most likely  
 406 grow,  $k$  is the thickness exponent of fatigue strength. After using rainflow counting  
 407 to bin the stress amplitudes into multiple stress levels and counting the number of cy-  
 408 cles in every stress bin, respective damages for each stress bin were added using the  
 409 Palmgren-Miner (PM) sum rule to obtain the total damage index  $D$ :

$$D = \sum_{i=1}^{N_c} \frac{n_i}{N_i}, \quad (16)$$

410 where  $n_i$  is the number of cycles in  $i^{th}$  stress bin,  $N_i$  is the number of cycles to fa-  
 411 tigue failure for the nominal stress cycle amplitude  $i$ , and  $N_c$  is the total number of  
 412 bins. To better quantify the fatigue damage, the fatigue damage index is normalized  
 413 using a reference damage index  $D_{ref}$  which is the damage required in 10 minutes of  
 414 simulation time that would lead to a total damage of 1 (failure according to PM sum  
 415 rule) over 30 years. The normalized fatigue damage is denoted by  $D_{norm} = D/D_{ref}$ .

#### 416 4.3 *Environmental states*

417 Table 3 Environmental states, based on data from ([51][21]).

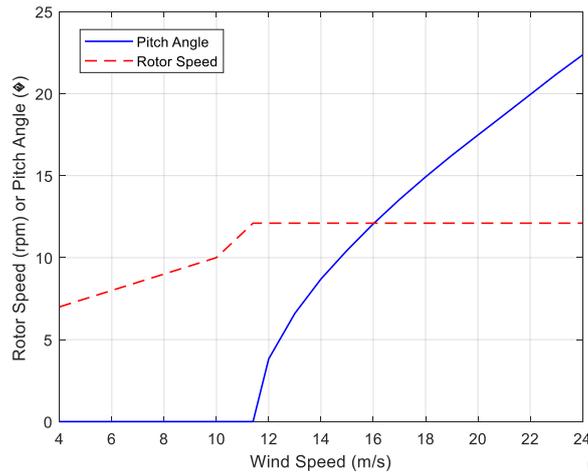
State	$V_w$ (m/s)	$T_z$ (s)	$H_s$ (m)	$P_{State}$ (%)	State	$V_w$ (m/s)	$T_z$ (s)	$H_s$ (m)	$P_{State}$ (%)
1	4	3	0.5	3.95	12	14	5	2.0	3.26

2	4	4	0.5	3.21	13	16	4	2.0	1.79
3	6	3	0.5	11.17	14	16	5	2.5	3.10
4	6	4	0.5	7.22	15	18	5	2.5	1.74
5	8	3	0.5	11.45	16	18	5	3.0	0.80
6	8	4	1.0	8.68	17	20	5	2.5	0.43
7	10	3	0.5	5.31	18	20	5	3.0	1.14
8	10	4	1.0	11.33	19	22	5	3.0	0.40
9	12	4	1.0	5.86	20	22	6	4.0	0.29
10	12	4	1.5	6.00	21	24	5	3.5	0.15
11	14	4	1.5	4.48	22	24	6	4.0	0.10

418

419 A set of environmental states according to ([51][21]) was adopted to determine the  
420 load combinations and calculate the accumulated fatigue damage. Every combination  
421 of wind speed  $V_w$ , significant wave height  $H_s$  and zero-crossing wave period  $T_z$   
422 corresponds to an occurrence probability  $P_{State}$ , as shown in Table 3. In line with the  
423 soil profile provided in Section 2.2, these environmental states are typical of a north-  
424 ern European offshore site. To obtain the JONSWAP spectrum, a relationship be-  
425 tween the zero-crossing wave period and the peak wave period  $T_p = 1.31T_z$  [52] was  
426 used. Wind speeds from 4 m/s to 24 m/s were grouped into 2 m/s bins. Wave heights  
427 and periods were grouped in 0.5 m and 1s bins, respectively. 22 environmental states  
428 were used to conduct the fatigue analysis. 91% of probability of occurrence is for the  
429 operational environmental states, with the remaining 9% corresponding to wind  
430 speeds below the cut-in speed and thus low contribution to fatigue damage. The wind  
431 and wave directionality in this study was simplified by assuming the wind and wave  
432 loads are in the same direction (see e.g. Koukoura et al. [3] for the influence of wind-  
433 wave misalignment). To represent the influence of the OWT control, the relationship  
434 between the mean wind speed, rotor rotation speed and blade pitch angles shown in  
435 Fig. 3 was adopted according to [36].

436



437

438 Fig. 3. Relationship between the rotor speed (dashed), pitch angle (solid) and inflow  
 439 wind speed, based on [36].

440

## 441 5 Results and discussion

### 442 5.1 Fatigue damage calculation for a single wind speed

443 This section illustrates the fatigue calculation procedure for the 17<sup>th</sup> environmental  
 444 state with a mean wind speed of 20 m/s and corresponding turbulence intensity ac-  
 445 cording to the NTM. Simulations were performed for all environmental states (Table  
 446 3), with fatigue damage calculation results for the 9<sup>th</sup> environmental state (mean wind  
 447 speed 12 m/s) shown in Appendix B.

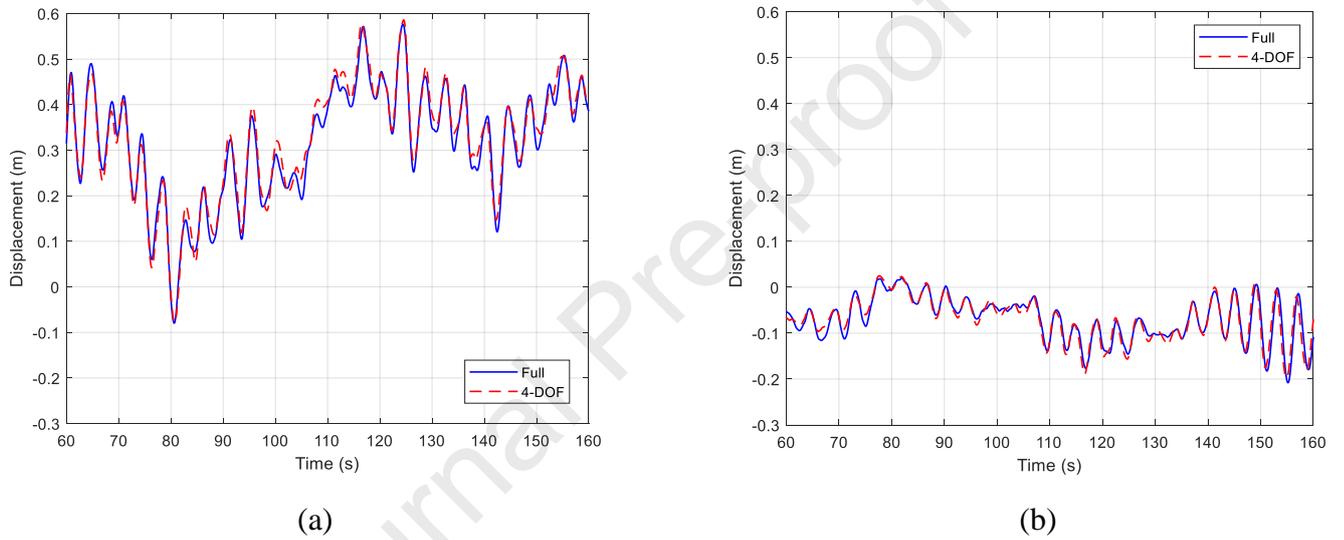
448

449 The inflow wind field and wave profile were generated with the specified parameters  
 450 and implemented as inputs to the fully coupled model. A 10-minute simulation with  
 451 time step selected of 0.05s was first conducted with the fully coupled model. Then the  
 452 fully coupled model was reduced to the 4-DOF model using the method described in  
 453 Section 3. The dynamic responses of the support structure were obtained from the two  
 454 models with the same time step. Fig. 4 compares the displacement responses at the  
 455 tower top in the FA and SS directions obtained from the fully coupled model and the  
 456 4-DOF model. The difference between the responses from these two models can be  
 457 explained by the fact that blade flexibility and structural damping are not considered  
 458 in the 4-DOF model. However, the tower top responses generated by the fully coupled  
 459 model and the 4-DOF model generally agree well in terms of dynamic amplitude and  
 460 phase. The Time Response Assurance Criterion (TRAC) [53] is used here to quantify

461 the degree of correlation between the two time histories. Considering two response  
 462 vectors  $\mathbf{u}_1(t)$  and  $\mathbf{u}_2(t)$ , the TRAC is defined as

$$TRAC = \frac{[\mathbf{u}_1(t)^T \mathbf{u}_2(t)]^2}{[\mathbf{u}_1(t)^T \mathbf{u}_1(t)][\mathbf{u}_2(t)^T \mathbf{u}_2(t)]}, \quad (17)$$

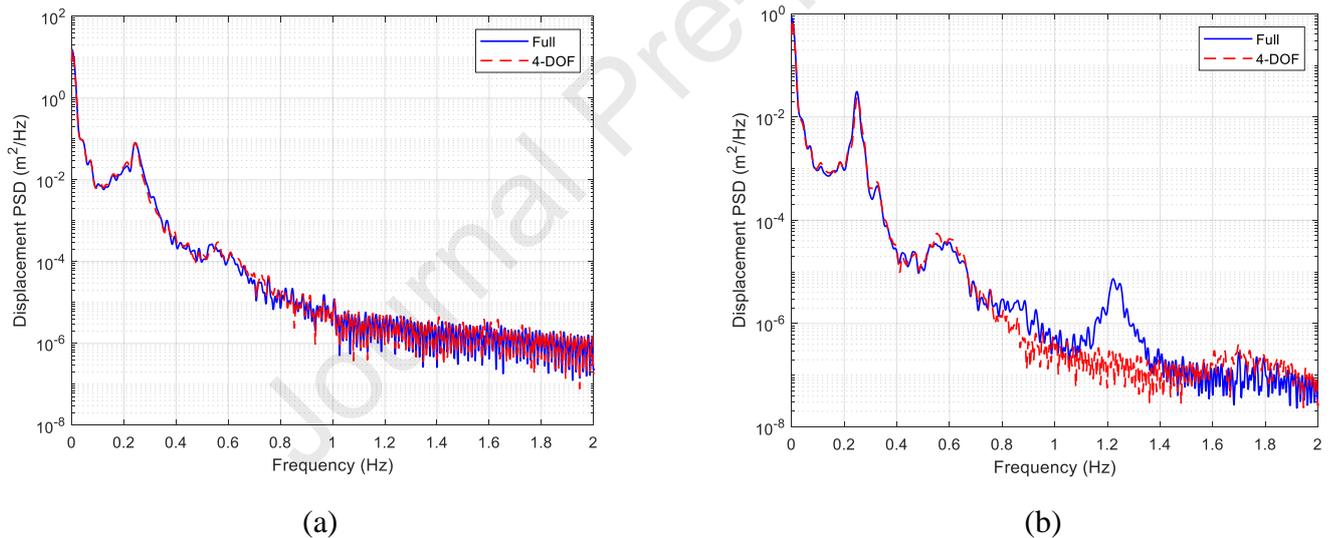
463 where  $\mathbf{u}_1(t)$  and  $\mathbf{u}_2(t)$  have the same duration and time step. A TRAC value close  
 464 to 1 indicates the two time histories are very similar. For the tower top displacement  
 465 responses from the fully coupled model and the 4-DOF model in Fig. 4, the calculated  
 466 TRAC values are 0.99 for the FA direction and 0.94 for the SS direction, indicating  
 467 that the responses from these two models are very close.



468 Fig. 4. Comparison of the FA (a) and SS (b) displacement responses at the tower top  
 469 between fully coupled model and the reduced 4-DOF model (17<sup>th</sup> environmental state,  
 470 wind speed 20 m/s).

471  
 472 The Power Spectral Density (PSD) curves calculated from the FA tower top responses  
 473 in Fig. 4(a) using the fully coupled model and the 4-DOF model are compared in Fig.  
 474 5(a). It can be seen that for the frequency range from 0 to 2 Hz these two curves agree  
 475 very well. The FA response is dominated by the first bending mode of the support  
 476 structure at approximately 0.25 Hz frequency. The influence of the 3P loading, which  
 477 has a frequency of about 0.6 Hz, is observable in the frequency domain. The 17<sup>th</sup> en-  
 478 vironmental state corresponds to the rated rotor rotation speed of 12.1 rpm and a 0.2  
 479 Hz rotation frequency. Fig. 5(b) compares the PSD curves of the SS tower top re-  
 480 sponses in Fig. 4(b). For frequencies lower than 0.8 Hz, the two PSD curves agree  
 481 well, confirming that the 4-DOF model successfully captures the OWT dynamic be-

482   behaviour in the SS direction in this frequency range. The peak at the 3P frequency is  
 483   clearer in this figure. However, the 4-DOF model does not capture the peak around  
 484   1.2 Hz which corresponds to the 6P loading [54] (the tracking of this peak at different  
 485   wind speeds confirmed this). This is due to the aerodynamic decoupling which simpli-  
 486   fies the wind-rotor interaction. Comparison between the two models was made for  
 487   other environmental states in the frequency domain, from which it is evident that the  
 488   4-DOF model cannot capture frequency components related to higher multiples of the  
 489   rotation frequency (6P, 12P, etc.) in the dynamic responses. Nevertheless, as the SS  
 490   response is dominated by the first bending mode, not capturing the peak at 6P does  
 491   not significantly influence the accuracy of the 4-DOF model in terms of dynamic re-  
 492   sponse generation. This can be observed from the good agreement of the predicted vi-  
 493   bration response in Fig. 4(b) and will be further demonstrated later for the fatigue  
 494   damage prediction.

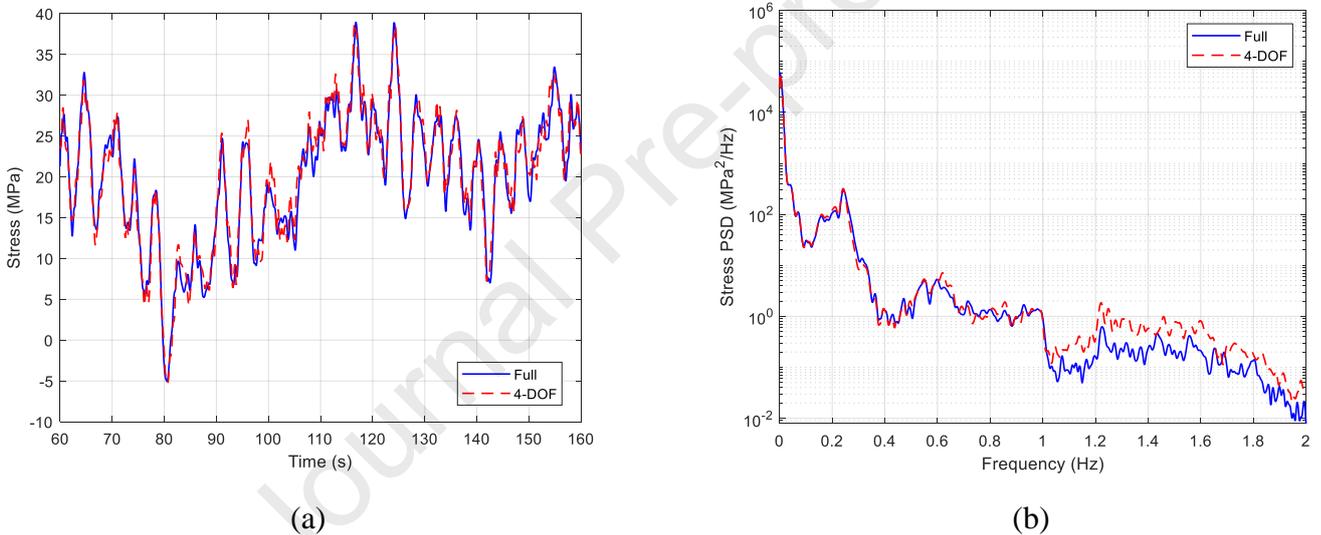


495   Fig. 5. Comparison of the PSD curves of tower top displacement responses in the FA  
 496   (a) and SS (b) directions obtained from the fully coupled model and the 4-DOF model  
 497   (time series shown in Fig. 4).

498

499   For the fatigue calculation, it is necessary to obtain the stress time history at the  
 500   hotspot. The location of the hotspot is selected at the position of the node at the mud-  
 501   line. Although the location where the moment reaches its maximum value can be be-  
 502   low the mudline [21], the location at the mudline was picked for the purpose of illus-  
 503   trating the methodology. For the fully coupled model, the stress time history was  
 504   obtained directly from the internal forces and beam section properties. For the 4-DOF

505 model, the calculation of the stress time histories was based on modal expansion ac-  
 506 cording to Eq. (14). At the selected section, the stress time history at the point where  
 507 the fatigue damage index reaches its maximum is used to compare the two models, as  
 508 shown in Fig. 6(a). Although there is some difference between the stress time histo-  
 509 ries, the fluctuations of the stresses are similar. The TRAC value for this stress time  
 510 history comparison is 0.99, indicating that stresses calculated by these two models  
 511 agree very well. In Fig. 6(b), the PSD curve of the maximum stress time history from  
 512 the fully coupled model agrees well with that from the 4-DOF model in the frequency  
 513 range from 0 to 1 Hz, showing that the 4-DOF model is able to capture similar dy-  
 514 namic behaviour in the dominant frequency range compared to the fully coupled  
 515 model.



516 Fig. 6. Comparison of the stress of the hotspot at the mudline from the fully coupled  
 517 model and the 4-DOF model in the time domain (a) and frequency domain (b).

518

519 The normalised fatigue damage indexes corresponding to the stress time histories  
 520 were obtained using the method described in Section 4.2. The normalised fatigue  
 521 damage index and the computation duration are listed in Table 4. The calculated nor-  
 522 malised damage indexes using the stress time histories from the two models are very  
 523 close with a percentage difference of 3.7%. More importantly, the computation dura-  
 524 tion of the 4-DOF model is significantly shorter than that of the fully coupled model,  
 525 demonstrating that the 4-DOF greatly outperforms the fully coupled model in terms of  
 526 calculation speed. The computation speed of 4-DOF model is also significantly faster

527 than that of OpenFAST [55], in spite of the latter modelling the blades and support  
 528 structure by modal superposition, thereby reducing the number of DOFs.

529

530 Table 4 Normalised fatigue damage indexes and computation durations for the fully  
 531 coupled model and the 4-DOF model (17<sup>th</sup> environmental state, wind speed 20 m/s).

	Normalised damage	Computation duration (s)
Fully coupled model	5.47	2348
4-DOF model	5.27	13

532

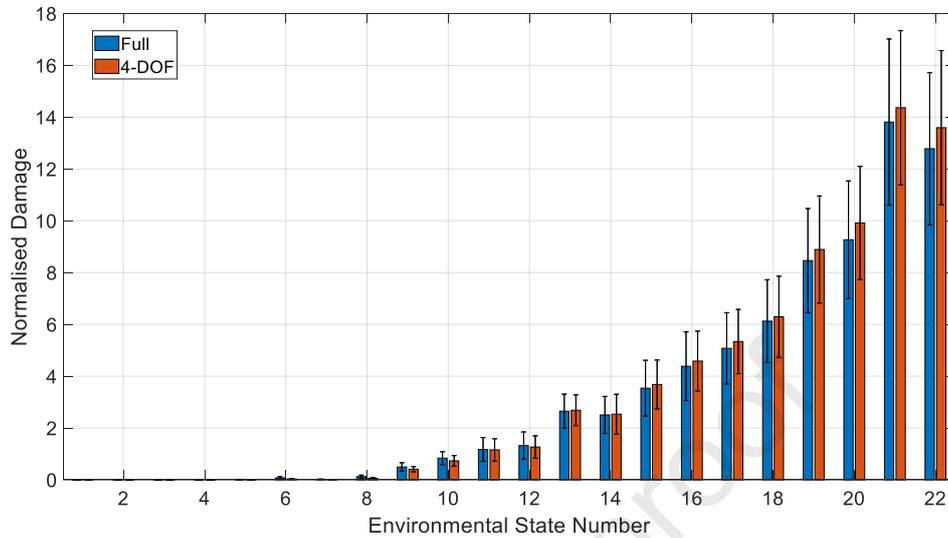
### 533 5.2 *Fatigue life prediction*

534 This section compares fatigue life prediction results calculated by the fully coupled  
 535 model and the 4-DOF model. The fatigue life prediction was based on the environ-  
 536 mental states in Table 3. For each of the 22 environmental states, to reduce the influ-  
 537 ence of randomness in turbulent wind and irregular waves, the normalised fatigue  
 538 damage index was calculated by averaging over simulations for 6 random seeds to  
 539 generate the inflow wind fields and the wave profiles. 10-minute simulations were  
 540 performed with the two models to obtain the stress time histories at the hotspot for  
 541 each random seed. The selection of the number and length of simulations is according  
 542 to IEC 61400-3 [45].

543

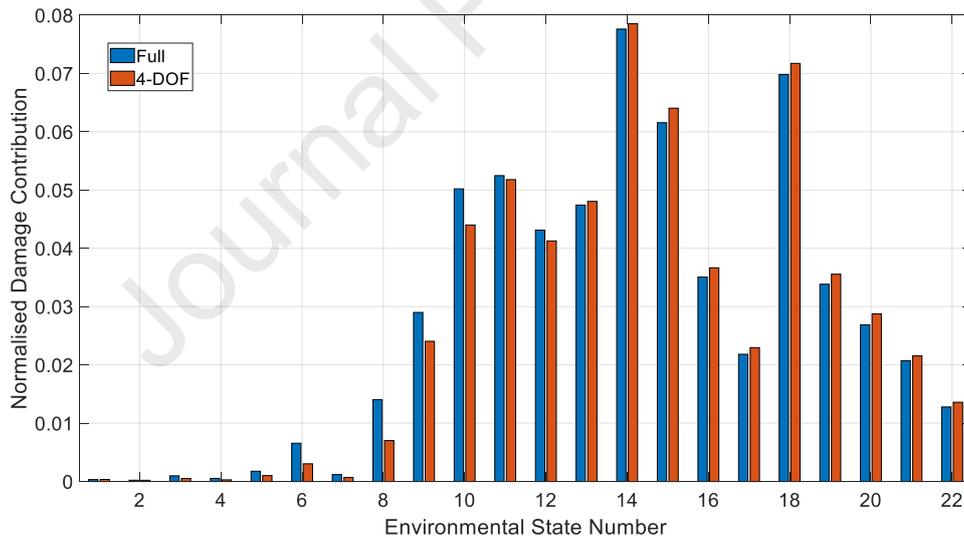
544 Fig. 7 compares the normalised damage indexes from the two models under different  
 545 environmental states. For low wind speeds, the normalised damage indexes are much  
 546 smaller than those with large wind speeds. Fig. 7 also shows the standard deviations  
 547 of the normalised damage indexes from the responses for the 6 random seeds from the  
 548 two models. It can be seen that for high environmental state numbers, the mean values  
 549 and standard deviations for the two models are generally close. The influence of the  
 550 random seed on the normalised fatigue damage index is relatively large for the higher  
 551 environmental states, as the standard deviations are large. For the 22<sup>rd</sup> environmental  
 552 state for instance, the mean value of the normalised fatigue damage index is around  
 553 12.5 with a standard deviation of around 3 (24%). Fig. 8 compares the normalised  
 554 damage contributions, which are the normalised damage indexes multiplied by the oc-  
 555 currence probabilities. Fatigue damage contributions are small for low wind speeds

556 corresponding to environmental states 1 to 7. Overall, the fatigue damage calculation  
 557 results by the two models are close.



558

559 Fig. 7. Comparison of the normalised damage indexes from the fully coupled model  
 560 and the 4-DOF model under different environmental states.



561

562 Fig. 8. Comparison of the normalised damage contributions from the fully coupled  
 563 model and the 4-DOF model under different environmental states.

564

565 The percentage difference between the normalised damage indexes calculated by the  
 566 two models can reach up to 40% for low environmental states (up to 8), correspond-  
 567 ing to wind speeds lower than 12 m/s, probably due to the low absolute values of the  
 568 damages. The percentage difference becomes much smaller (around 5%) for higher  
 569 environmental states (from 11 to 22) corresponding to wind speeds larger than 12 m/s

570 and these makes the most significant contribution to the fatigue life (as shown in Fig.  
571 8).

572

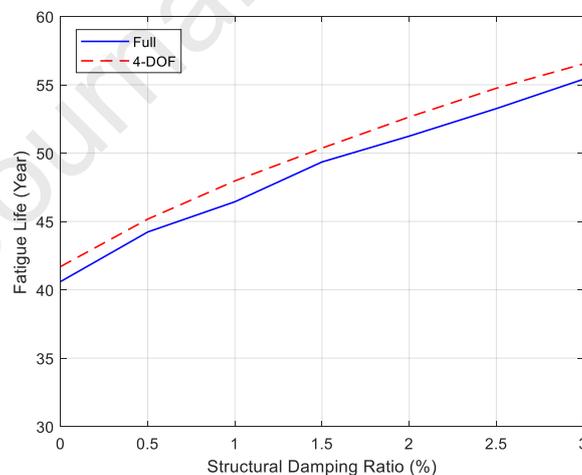
573 Subsequently, the fatigue life was obtained according to Palmgren-Miner sum rule by  
574 combing the calculated fatigue damage indexes in 10 minutes and the occurrence  
575 probabilities of the environmental states. Table 5 lists the fatigue life predicted by the  
576 fully coupled model and the 4-DOF model for the assumed structural damping of  
577 1.5%. These two models only result in 2% difference in terms of fatigue life predic-  
578 tion. The computation duration for the time integration of the fully coupled model is  
579 84 hours, but the 4-DOF model only requires 30 minutes to complete the calculation.

580

581 Table 5 Fatigue damage indexes and computation durations for the fully coupled  
582 model and the 4-DOF model (1.5% structural and soil damping).

	Fatigue life (year)	Computation duration
Fully coupled model	49.4	84 hours
4-DOF model	50.4	30 min

583



584

585 Fig. 9. Fatigue life prediction by the fully coupled model (blue, solid) and the 4-DOF  
586 model (red, dashed) for variation of the structural and soil damping.

587

588 A sensitivity analysis was conducted to study the influence of structural damping on  
589 the fatigue life prediction, to test how well this close match would hold for a wider  
590 range of input parameters. Damping ratios from 0 to 3% in 0.5% steps were assigned  
591 as the structural and soil damping of the OWT system, and the fatigue life was pre-

592 dicted using time series generated from the full and 4-DOF model for the same initial  
593 conditions ( $6 \times 10$ -minute simulations). As shown in Fig. 9, the predicted fatigue life  
594 increases as the structural damping increases. The fatigue life predicted by the 4-DOF  
595 model follows the same trend very closely and is consistently approximately 1-year  
596 larger than that from the fully coupled model, with a maximum difference of 1.5  
597 years. Given the uncertainty around standard fatigue life calculations, this consistently  
598 small difference is not significant and indicates that the reduced model can be used to  
599 carry out fatigue life assessments at a much-reduced computational cost.

### 600 *5.3 Discussion of modelling assumptions*

601 Combining the aerodynamic decoupling and modal reduction introduced in Sections  
602 3.1 and 3.2 simplifies the fully coupled model into a numerically efficient modal  
603 model. This process is underpinned by some assumptions, including rigid blades,  
604 lumped RNA mass at the tower top, and limited modes dominating the low-frequency  
605 vibration response in OWTs. More details of these assumptions can be found in refer-  
606 ences [35] and [48]. Among these assumptions, the rigid blade assumption is poten-  
607 tially the most problematic. However, it was demonstrated in [35] that assuming rigid  
608 blades does not significantly alter the aerodynamic damping contribution and only has  
609 a limited impact on the overall natural frequencies of the wind turbine system. The ef-  
610 fect of the number of modes required to carry out the fatigue analysis was investigated  
611 as discussed in Section 3.2 and it was found that the 4-DOF mode, considering the  
612 first two bending modes, provides the best compromise between computational speed  
613 and accuracy.

614

615 The methodology was developed around a specific case study that can easily be ex-  
616 tended or adapted to analyse other wind turbine systems such as fixed-bottom, three-  
617 bladed, horizontal axis OWTs of various sizes supported with different foundation  
618 types and considering wind, wave and tidal conditions.

619

## 620 **6 Conclusions**

621 This study proposes a computationally efficient fatigue life prediction methodology  
622 for offshore wind turbines based on a recently developed aerodynamic decoupling  
623 strategy and modal reduction. A fully coupled model can be reduced to a 4-DOF

624 model, thereby significantly decreasing the number of DOFs in the OWT system,  
625 while considering all relevant features such as soil-structure interaction and key dy-  
626 namic couplings. Combining modal expansion and a method to extract the stresses  
627 from nodal displacements, the stress time histories at the hotspot can be calculated ef-  
628 ficiently using the 4-DOF model. The fatigue life of a reference 5 MW model OWT  
629 was predicted considering typical northern European environmental states, using both  
630 a fully coupled model and the reduced model. Results show that the 4-DOF model ac-  
631 curately predicts fatigue damage and provides very close fatigue life prediction results  
632 compared to the fully coupled model. A structural damping sensitivity study was car-  
633 ried out and confirms that fatigue life predictions consistently matched within 2% for  
634 a range of parameters. The good accuracy of the reduced model can be attributed to  
635 the ability of the unconventional aerodynamic damping matrix, upon which it is  
636 based, to better capture the coupling between the FA and SS directions than conven-  
637 tional damping ratios.

638

639 In addition to accuracy, a significant advantage of the proposed fatigue life methodol-  
640 ogy is its numerical efficiency and rapid computational speed. Compared to the fully  
641 coupled model, aerodynamic decoupling and modal expansion significantly reduce  
642 the required DOFs to be considered in the time integration. As a result, the duration of  
643 the time integration for the modal model is around 0.5% of that for the fully coupled  
644 model. Therefore, the proposed fatigue life prediction methodology has the potential  
645 to be applied in the preliminary design practice to quickly estimate the fatigue life of  
646 OWTs. In practical fatigue life assessment of OWTs, the proposed methodology  
647 could be advantageous, as reducing the analysis time is demanding with many envi-  
648 ronmental states and load combinations to be considered. Employing the proposed  
649 methodology, a more comprehensive fatigue life prediction with increased numbers of  
650 load cases and parameter variation studies can be conducted. The proposed model  
651 could be used to predict the influence of variations, e.g., of scour, mean sea level, tid-  
652 al conditions, or changes to the turbine size and support structure. Some design pro-  
653 cedures require a large number of dynamic response calculations, such as Monte Car-  
654 lo-based fatigue reliability analysis or structural/control optimisation. Further research  
655 should consider the comparison and validation against experimental data for deployed  
656 offshore wind turbines and the extension to consider the flexibility and fatigue life  
657 prediction of wind turbine blades.

658

659 **7 Acknowledgement**

660 Financial support from the National Science Fund for Distinguished Young Schol-  
661 ars (No. 52025082) and the National Natural Science Foundation of China (No.  
662 51908209) are greatly appreciated. The financial support to the first author from Dr.  
663 Feipeng Liu of Northwest Engineering Corporation Limited through a research pro-  
664 ject (No. H202194370223) is also acknowledged.

665

666

667

Journal Pre-proof

668 **References**

- 669 [1] Oest J, Rene Sørensen, Lars LC, et al. Structural optimization with fatigue and  
670 ultimate limit constraints of jacket structures for large offshore wind turbines.  
671 *Struct Multidiscip Optim* 2017; 55: 779–793.
- 672 [2] Yuan Y, Tang J. On Advanced Control Methods toward Power Capture and  
673 Load Mitigation in Wind Turbines. *Engineering* 2017; 3: 494–503.
- 674 [3] Koukoura C, Brown C, Natarajan A, et al. Cross-wind fatigue analysis of a full  
675 scale offshore wind turbine in the case of wind–wave misalignment. *Eng Struct*  
676 2016; 120: 147–157.
- 677 [4] Torben J, Melchior A. *How 2 HAWC2, the user's manual*. Technical Report  
678 Risø-R-1597(ver. 3-1)(EN). Risø National Laboratory, Denmark, 2007.
- 679 [5] Velarde J, Kramhøft C, Sørensen JD. Global sensitivity analysis of offshore  
680 wind turbine foundation fatigue loads. *Renew Energy* 2019; 140: 177–189.
- 681 [6] Velarde J, Kramhøft C, Sørensen JD, et al. Fatigue reliability of large  
682 monopiles for offshore wind turbines. *Int J Fatigue* 2020; 134: 105487.
- 683 [7] Marino E, Giusti A, Manuel L. Offshore wind turbine fatigue loads: The  
684 influence of alternative wave modeling for different turbulent and mean winds.  
685 *Renew Energy* 2017; 102: 157–169.
- 686 [8] Jonkman JM, Buhl MLJ. *FAST user's guide*. Technical Report NREL/EL-500-  
687 38230. National Renewable Energy Laboratory: Golden, CO, USA, October  
688 2005.
- 689 [9] Hübler C, Gebhardt CG, Rolfes R. Methodologies for fatigue assessment of  
690 offshore wind turbines considering scattering environmental conditions and the  
691 uncertainty due to finite sampling. *Wind Energy* 2018; 21: 1092–1105.
- 692 [10] Horn JT, Leira BJ. Fatigue reliability assessment of offshore wind turbines  
693 with stochastic availability. *Reliab Eng Syst Saf* 2019; 191: 106550.
- 694 [11] Stieng LES, Muskulus M. Reducing the number of load cases for fatigue  
695 damage assessment of offshore wind turbine support structures using a simple  
696 severity-based sampling method. *Wind Energy Sci* 2018; 3: 805–818.
- 697 [12] Huchet Q, Mattrand C, Beaupaire P, et al. AK-DA: An efficient method for  
698 the fatigue assessment of wind turbine structures. *Wind Energy* 2019; 22: 638–  
699 652.
- 700 [13] Zwick D, Muskulus M. Simplified fatigue load assessment in offshore wind  
701 turbine structural analysis. *Wind Energy* 2016; 19: 265–278.

- 702 [14] Häfele J, Hübler C, Gebhardt CG, et al. A comprehensive fatigue load set  
703 reduction study for offshore wind turbines with jacket substructures. *Renew*  
704 *Energy* 2018; 118: 99–112.
- 705 [15] Stieng LES, Muskulus M. Load case reduction for offshore wind turbine  
706 support structure fatigue assessment by importance sampling with two-stage  
707 filtering. *Wind Energy* 2019; 22: 1472–1486.
- 708 [16] Wilkie D, Galasso C. Gaussian process regression for fatigue reliability  
709 analysis of offshore wind turbines. *Struct Saf* 2021; 88: 102020.
- 710 [17] Yeter B, Garbatov Y, Guedes Soares C. Evaluation of fatigue damage model  
711 predictions for fixed offshore wind turbine support structures. *Int J Fatigue*  
712 2016; 87: 71–80.
- 713 [18] Bisoi S, Haldar S. Dynamic analysis of offshore wind turbine in clay  
714 considering soil–monopile–tower interaction. *Soil Dyn Earthq Eng* 2014; 63:  
715 19–35.
- 716 [19] Dong W, Moan T, Gao Z. Fatigue reliability analysis of the jacket support  
717 structure for offshore wind turbine considering the effect of corrosion and  
718 inspection. *Reliab Eng Syst Saf* 2012; 106: 11–27.
- 719 [20] Dong W, Moan T, Gao Z. Long-term fatigue analysis of multi-planar tubular  
720 joints for jacket-type offshore wind turbine in time domain. *Eng Struct* 2011;  
721 33: 2002–2014.
- 722 [21] Rezaei R, Fromme P, Duffour P. Fatigue life sensitivity of monopile-supported  
723 offshore wind turbines to damping. *Renew Energy* 2018; 123: 450–459.
- 724 [22] Rezaei R, Duffour P, Fromme P. Scour influence on the fatigue life of  
725 operational monopile-supported offshore wind turbines. *Wind Energy* 2018; 1–  
726 14.
- 727 [23] Muskulus M. Simplified rotor load models and fatigue damage estimates for  
728 offshore wind turbines. *Philos Trans R Soc London A Math Phys Eng Sci* 2015;  
729 373: 20140347.
- 730 [24] Schafhirt S, Muskulus M. Decoupled simulations of offshore wind turbines  
731 with reduced rotor loads and aerodynamic damping. *Wind Energy Sci* 2018; 3:  
732 25.
- 733 [25] Salzmann DJC, Tempel J Van Der. Aerodynamic damping in the design of  
734 support structures for offshore wind turbines. In: *The European Offshore Wind*  
735 *Conference & Exhibition*. Copenhagen, Denmark, 2005.

- 736 [26] Valamanesh V, Myers AT. Aerodynamic damping and seismic response of  
737 horizontal axis wind turbine towers. *J Struct Eng* 2014; 140: 1–9.
- 738 [27] Liu X, Lu C, Li G, et al. Effects of aerodynamic damping on the tower load of  
739 offshore horizontal axis wind turbines. *Appl Energy* 2017; 204: 1101–1114.
- 740 [28] Hansen MH, Thomsen K, Fuglsang P, et al. Two methods for estimating  
741 aeroelastic damping of operational wind turbine modes from experiments.  
742 *Wind Energy* 2006; 9: 179–191.
- 743 [29] Ozbek M, Rixen DJ. Operational modal analysis of a 2.5 MW wind turbine  
744 using optical measurement techniques and strain gauges. *Wind Energy* 2013;  
745 17: 367–381.
- 746 [30] Koukoura C, Natarajan A, Vesth A. Identification of support structure damping  
747 of a full scale offshore wind turbine in normal operation. *Renew Energy* 2015;  
748 81: 882–895.
- 749 [31] Dai K, Wang Y, Huang Y, et al. Development of a modified stochastic  
750 subspace identification method for rapid structural assessment of in-service  
751 utility-scale wind turbine towers. *Wind Energy* 2017; 17: 657–669.
- 752 [32] Dong X, Lian J, Wang H, et al. Structural vibration monitoring and operational  
753 modal analysis of offshore wind turbine structure. *Ocean Eng* 2018; 150: 280–  
754 297.
- 755 [33] Tarp-Johansen NJ, Andersen L, Christensen ED, et al. Comparing sources of  
756 damping of cross-wind motion. In: *Proceeding of the Copenhagen Offshore*  
757 *Conference*. Stockholm, Sweden, 2009.
- 758 [34] Chen C, Duffour P, Fromme P. Novel aerodynamic damping identification  
759 method for operating wind turbines. *J Phys Conf Ser* 2019; 1222: 012008.
- 760 [35] Chen C, Duffour P, Fromme P. Modelling wind turbine tower-rotor interaction  
761 through an aerodynamic damping matrix. *J Sound Vib* 2020; 489: 115667.
- 762 [36] Jonkman JM, Butterfield S, Musial W, et al. *Definition of a 5-MW reference*  
763 *wind turbine for offshore system development*. Technical Report NREL/TP-  
764 500-38060. National Renewable Energy Laboratory: Golden, CO, USA, 2009.
- 765 [37] Staino A, Basu B. Dynamics and control of vibrations in wind turbines with  
766 variable rotor speed. *Eng Struct* 2013; 56: 58–67.
- 767 [38] Chen C, Duffour P. Modelling damping sources in monopile-supported  
768 offshore wind turbines. *Wind Energy* 2018; 21: 1121–1140.
- 769 [39] Gavin HP. *Numerical integration in structural dynamics*. Duke University,

- 770 <http://people.duke.edu/~hpgavin/cee541/NumericalIntegration.pdf> (2016).
- 771 [40] Subramanian N. *Steel structures - design and practice*. Oxford University  
772 Press, 2011.
- 773 [41] DNV GL. *DNVGL-RP-C212 Offshore soil mechanics and geotechnical*  
774 *engineering*. 2017.
- 775 [42] Hansen M. *Aerodynamics of wind turbines*. Second Edi. Routledge, 2008.
- 776 [43] Branlard E. Chapter 10 The Blade ElementMomentum (BEM) Method. In:  
777 *Wind Turbine Aerodynamics and Vorticity-Based Methods*. Epub ahead of print  
778 2017. DOI: 10.1007/978-3-319-55164-7.
- 779 [44] Jonkman BJ, Kilcher L. *TurbSim user's guide : version 1. 06.00*. Technical  
780 Report. National Renewable Energy Laboratory: Golden, CO, USA, 2012.
- 781 [45] International Electrotechnical Commission (IEC). *IEC 61400-3 Wind turbines -*  
782 *Part 3: Design requirements for offshore wind turbines*. 2009.
- 783 [46] Shirzadeh R, Devriendt C, Bidakhvidi MA, et al. Experimental and  
784 computational damping estimation of an offshore wind turbine on a monopile  
785 foundation. *J Wind Eng Ind Aerodyn* 2013; 120: 96–106.
- 786 [47] Hasselmann K, Barnett TP, Bouws E, et al. Measurements of wind-wave  
787 growth and swell decay during the Joint North Sea Wave Project (JONSWAP).  
788 *Erganzungsh zur Dtsch Hydrogr Zeitschrift R* 1973; A(8): 1–95.
- 789 [48] Chen C, Duffour P, Dai K, et al. Identification of aerodynamic damping matrix  
790 for operating wind turbines. *Mech Syst Signal Process* 2021; 154: 107568.
- 791 [49] DNV. RP-C203- Fatigue design of offshore steel structures. *Recomm Pract*  
792 *DNV-RPC203* 2014; 126.
- 793 [50] Pelayo F, Skafta A, Aenlle ML, et al. Modal Analysis Based Stress Estimation  
794 for Structural Elements Subjected to Operational Dynamic Loadings. *Exp Mech*  
795 2015; 55: 1791–1802.
- 796 [51] Tempel J Van Der. *Design of support structures for offshore wind turbines*.  
797 PhD Thesis. Delft University of Technology, 2006.
- 798 [52] Baniotopoulos C, Borri C, Stathopoulos T. *Environmental wind engineering*  
799 *and design of wind energy structures*. Springer Science & Business Media,  
800 2011.
- 801 [53] Avitabile P, Pingle P. Prediction of full field dynamic strain from limited sets  
802 of measured data. *Shock Vib* 2012; 19: 765–785.
- 803 [54] Sønnderby I, Hansen MH. Open-loop frequency response analysis of a wind

- 804 turbine using a high-order linear aeroelastic model. *Wind Energy* 2014; 17:  
805 1147–1167.
- 806 [55] National Renewable Energy Laboratory (NREL). OpenFAST Documentation -  
807 Release v2.3.0,  
808 <https://readthedocs.org/projects/openfast/downloads/pdf/master/> (2020).  
809

Journal Pre-proof

810 **Appendix A**

811 To consider a non-uniform inflow wind field, some modifications are needed to the  
 812 derivation process described in Section 3.3 of reference [35]. Keeping the initial as-  
 813 sumptions that the rotor is rigid and the RNA speed is small, the aerodynamic forces  
 814 applied to one blade element can be expressed by Eqs. (4) to (7) in [35]. However,  
 815 when summing up the elemental blade forces for one blade, the three blades must be  
 816 considered individually, as the total aerodynamic forces experienced by different  
 817 blades are different due to wind turbulence and different azimuthal positions. In this  
 818 way, the aerodynamic force resultants can still be linearised as forces applied to a rig-  
 819 id tower plus terms related to the tower top velocities. Using the notations introduced  
 820 in [35], the total force at the tower top in the  $x$  (FA) direction can be expressed as  
 821 the sum of thrusts applied to all blades:

$$\begin{aligned}
 F_x^{Flex}(t) &= \sum_{i=1}^{N_b} \int_0^R dT(V_{xRel}, V_{rRel}) \\
 &= \sum_{i=1}^{N_b} \int_0^R dT(V_0, V_r) - \dot{x} \sum_{i=1}^{N_b} \int_0^R \frac{\partial(dT)}{\partial V_0} - \dot{\theta}_y \sum_{i=1}^{N_b} \cos\gamma_i(t) \int_0^R r \frac{\partial(dT)}{\partial V_0} \\
 &\quad - \dot{y} \sum_{i=1}^{N_b} \cos\gamma_i(t) \int_0^R \frac{\partial(dT)}{\partial V_r} + \dot{\theta}_x \sum_{i=1}^{N_b} \int_0^R r \frac{\partial(dT)}{\partial V_r}.
 \end{aligned} \tag{A. 1}$$

822 The total force in the  $y$  (SS) direction is:

$$\begin{aligned}
 F_y^{Flex}(t) &= - \sum_{i=1}^{N_b} \cos\gamma_i(t) \int_0^R dS(V_{xRel}, V_{rRel}) \\
 &= - \sum_{i=1}^{N_b} \cos\gamma_i(t) \int_0^R dS(V_0, V_r) + \dot{x} \sum_{i=1}^{N_b} \cos\gamma_i(t) \int_0^R \frac{\partial(dS)}{\partial V_0} \\
 &\quad + \dot{\theta}_y \sum_{i=1}^{N_b} \cos^2\gamma_i(t) \int_0^R r \frac{\partial(dS)}{\partial V_0} + \dot{y} \sum_{i=1}^{N_b} \cos^2\gamma_i(t) \int_0^R \frac{\partial(dS)}{\partial V_r} \\
 &\quad - \dot{\theta}_x \sum_{i=1}^{N_b} \cos\gamma_i(t) \int_0^R r \frac{\partial(dS)}{\partial V_r}.
 \end{aligned} \tag{A. 2}$$

823 The total moment about the  $x$  axis is:

$$M_x^{Flex}(t) = \sum_{i=1}^{N_b} \int_0^R dM_x(V_{xRel}, V_{rRel}) \tag{A. 3}$$

$$\begin{aligned}
&= \sum_{i=1}^{N_b} \int_0^R r dS(V_0, V_r) - \dot{x} \sum_{i=1}^{N_b} \int_0^R r \frac{\partial(dS)}{\partial V_0} \\
&\quad - \dot{\theta}_y \sum_{i=1}^{N_b} \cos\gamma_i(t) \int_0^R r^2 \frac{\partial(dS)}{\partial V_0} \\
&\quad - \dot{y} \sum_{i=1}^{N_b} \cos\gamma_i(t) \int_0^R r \frac{\partial(dS)}{\partial V_r} + \dot{\theta}_x \sum_{i=1}^{N_b} \int_0^R r^2 \frac{\partial(dS)}{\partial V_r},
\end{aligned}$$

824 whereas the total moment about the  $y$  axis is:

$$\begin{aligned}
M_y^{Flex}(t) &= \sum_{i=1}^{N_b} \int_0^R dM_y(V_{xRel}, V_{rRel}) \\
&= \sum_{i=1}^{N_b} \cos\gamma_i(t) \int_0^R r dT(V_0, V_r) - \dot{x} \sum_{i=1}^{N_b} \cos\gamma_i(t) \int_0^R r \frac{\partial(dT)}{\partial V_0} \\
&\quad - \dot{\theta}_y \sum_{i=1}^{N_b} \cos^2\gamma_i(t) \int_0^R r^2 \frac{\partial(dT)}{\partial V_0} - \dot{y} \sum_{i=1}^{N_b} \cos^2\gamma_i(t) \int_0^R r \frac{\partial(dT)}{\partial V_r} \\
&\quad + \dot{\theta}_x \sum_{i=1}^{N_b} \cos\gamma_i(t) \int_0^R r^2 \frac{\partial(dT)}{\partial V_r}.
\end{aligned} \tag{A. 4}$$

825 The derivatives in Equations (A. 1) to (A. 4) can be found using expressions of partial  
826 derivatives in Appendix A in [35]. According to Equations (A. 1) to (A. 4), the result-  
827 ant aerodynamic forces from the rotor to the top of a flexible wind turbine tower,  
828  $\mathbf{F}_{Flex}^{Top}(t) = [F_x^{Flex}(t) F_y^{Flex}(t) M_x^{Flex}(t) M_y^{Flex}(t)]^T$ , can be rewritten in the following  
829 simplified form

$$\mathbf{F}_{Flex}^{Top}(t) = \begin{bmatrix} \sum_{i=1}^{N_b} \int_0^R dT(V_0, V_r) \\ - \sum_{i=1}^{N_b} \cos\gamma_i(t) \int_0^R dS(V_0, V_r) \\ \sum_{i=1}^{N_b} \int_0^R r dS(V_0, V_r) \\ \sum_{i=1}^{N_b} \cos\gamma_i(t) \int_0^R r dT(V_0, V_r) \end{bmatrix} - \mathbf{C}_{Aero} \begin{bmatrix} \dot{x} \\ \dot{y} \\ \dot{\theta}_x \\ \dot{\theta}_y \end{bmatrix} = \mathbf{F}_{Rigid}^{Top}(t) - \mathbf{C}_{Aero} \dot{\mathbf{u}}^{Top}(t), \tag{A. 5}$$

830 where

$$\mathbf{C}_{Aero} =$$

$$\begin{bmatrix}
\sum_{i=1}^{N_b} \int_0^R \frac{\partial(dT)}{\partial V_0} & \sum_{i=1}^{N_b} \cos \gamma_i(t) \int_0^R \frac{\partial(dT)}{\partial V_r} & -\sum_{i=1}^{N_b} \int_0^R r \frac{\partial(dT)}{\partial V_r} & \sum_{i=1}^{N_b} \cos \gamma_i(t) \int_0^R r \frac{\partial(dT)}{\partial V_0} \\
-\sum_{i=1}^{N_b} \cos \gamma_i(t) \int_0^R \frac{\partial(dS)}{\partial V_0} & -\sum_{i=1}^{N_b} \cos^2 \gamma_i(t) \int_0^R \frac{\partial(dS)}{\partial V_r} & \sum_{i=1}^{N_b} \cos \gamma_i(t) \int_0^R r \frac{\partial(dS)}{\partial V_r} & -\sum_{i=1}^{N_b} \cos^2 \gamma_i(t) \int_0^R r \frac{\partial(dS)}{\partial V_0} \\
\sum_{i=1}^{N_b} \int_0^R r \frac{\partial(dS)}{\partial V_0} & \sum_{i=1}^{N_b} \cos \gamma_i(t) \int_0^R r \frac{\partial(dS)}{\partial V_r} & -\sum_{i=1}^{N_b} \int_0^R r^2 \frac{\partial(dS)}{\partial V_r} & \sum_{i=1}^{N_b} \cos \gamma_i(t) \int_0^R r^2 \frac{\partial(dS)}{\partial V_0} \\
\sum_{i=1}^{N_b} \cos \gamma_i(t) \int_0^R r \frac{\partial(dT)}{\partial V_0} & \sum_{i=1}^{N_b} \cos^2 \gamma_i(t) \int_0^R r \frac{\partial(dT)}{\partial V_r} & -\sum_{i=1}^{N_b} \cos \gamma_i(t) \int_0^R r^2 \frac{\partial(dT)}{\partial V_r} & \sum_{i=1}^{N_b} \cos^2 \gamma_i(t) \int_0^R r^2 \frac{\partial(dT)}{\partial V_0}
\end{bmatrix} \quad (\text{A. 6})$$

831  $\mathbf{C}_{Aero}$  can be written more concisely:

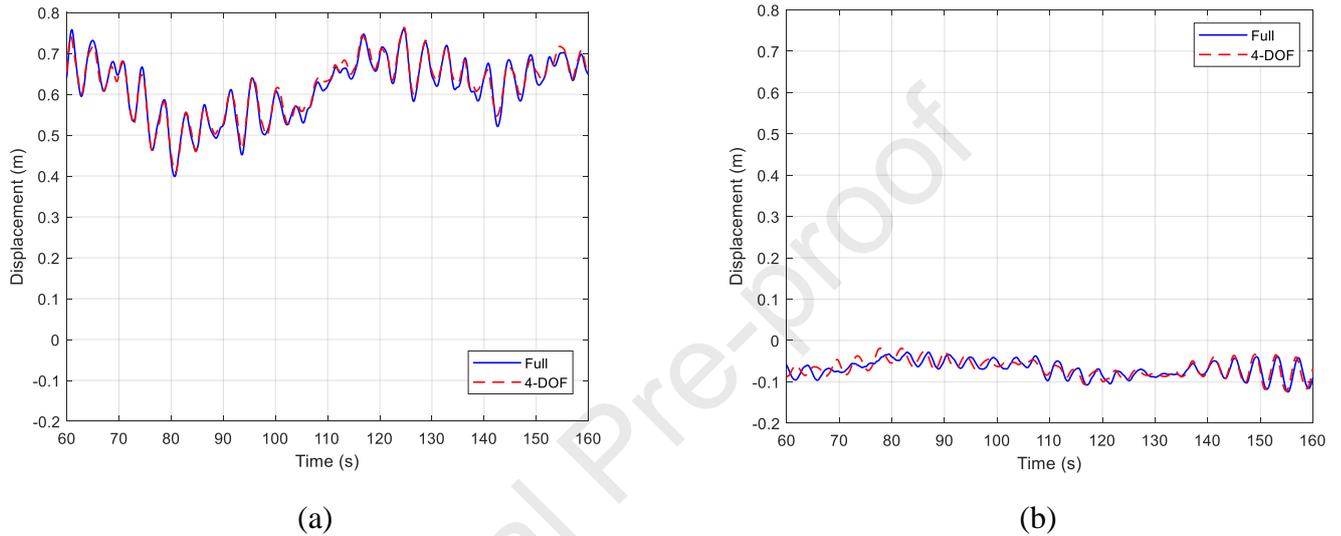
$$\mathbf{C}_{Aero} = \begin{bmatrix} c_{xx} & c_{xy} & c_{x\theta_x} & c_{x\theta_y} \\ c_{yx} & c_{yy} & c_{y\theta_x} & c_{y\theta_y} \\ c_{\theta_x x} & c_{\theta_x y} & c_{\theta_x \theta_x} & c_{\theta_x \theta_y} \\ c_{\theta_y x} & c_{\theta_y y} & c_{\theta_y \theta_x} & c_{\theta_y \theta_y} \end{bmatrix}. \quad (\text{A. 7})$$

832

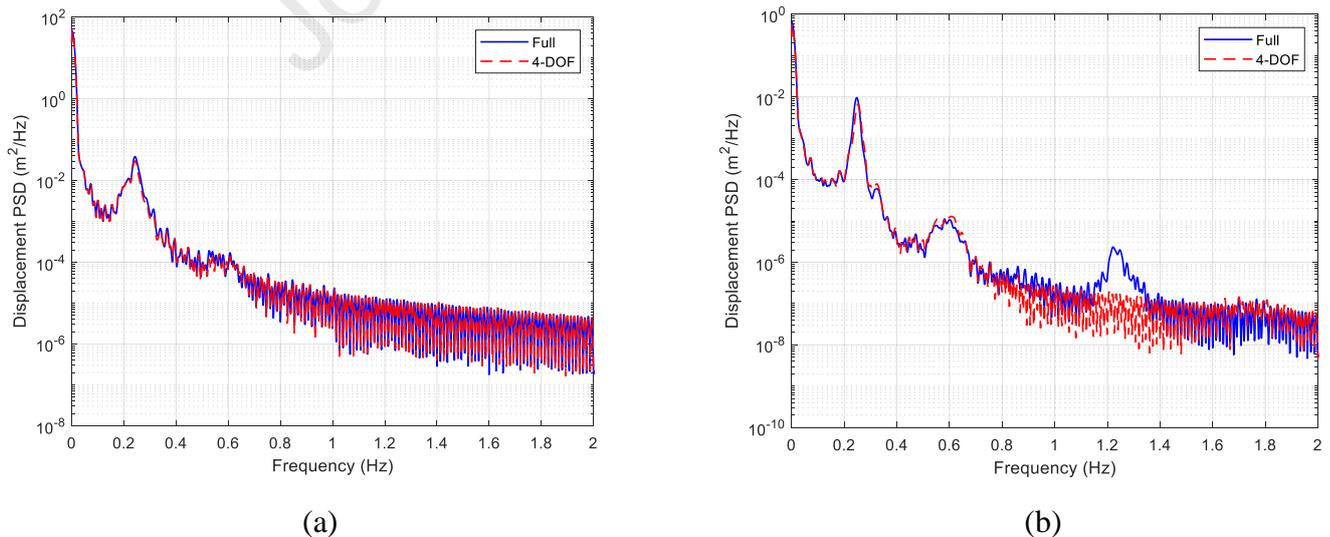
833

834 **Appendix B**

835 Simulations were conducted for all environmental states (Table 3), with Section 5.1  
 836 showing the fatigue calculation procedure for the 17<sup>th</sup> environmental state with a rela-  
 837 tively high mean wind speed of 20 m/s. The fatigue damage calculation results are  
 838 demonstrated here for the 9<sup>th</sup> environmental state, corresponding to a mean wind  
 839 speed of 12 m/s, near the rated wind speed (11.4 m/s) of the considered OWT.

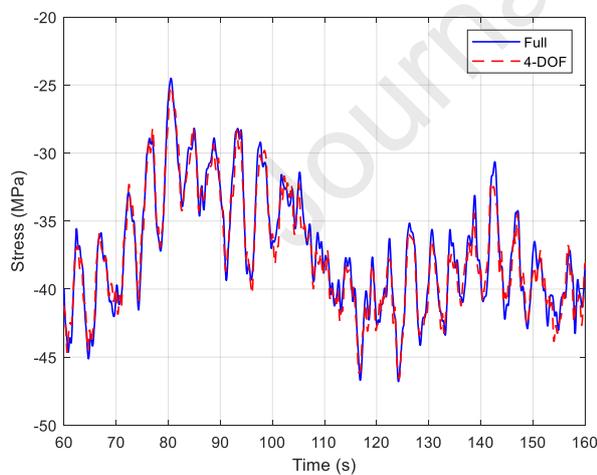


840 Fig. B1. Comparison of the FA (a) and SS (b) displacement responses at the tower top  
 841 between fully coupled model and the reduced 4-DOF model (9<sup>th</sup> environmental state,  
 842 wind speed 12 m/s).

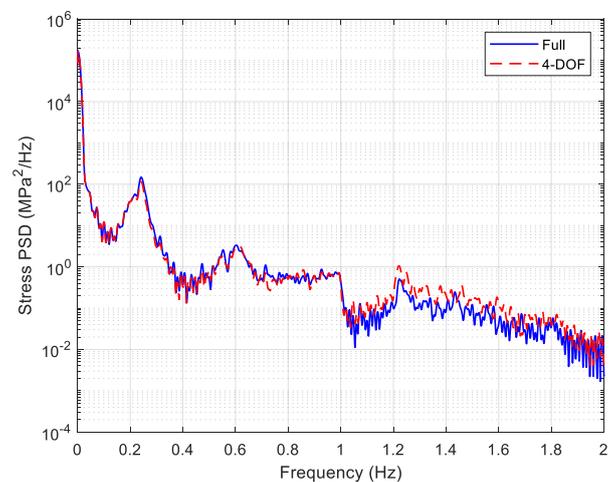


843 Fig. B2. Comparison of the PSD curves of tower top displacement responses in the  
 844 FA (a) and SS (b) directions obtained from the fully coupled model and the 4-DOF  
 845 model (time series shown in Fig. B1).

846 Fig. B1 compares the tower top displacement responses in the FA and SS directions  
 847 obtained from the fully coupled model and the 4-DOF model, with good agreement  
 848 and TRAC values of 0.99 for the FA direction and 0.96 for the SS direction. These are  
 849 comparable to the respective TRAC values of 0.99 (FA direction) and 0.94 (SS direc-  
 850 tion) obtained in Section 5.1 for a wind speed of 20 m/s (17<sup>th</sup> environmental state).  
 851 Fig. B2 shows the comparison of the tower top responses in the frequency domain. It  
 852 shows that the responses generated by the two models are overall very similar in both  
 853 the time and frequency domain. However, as observed in Section 5.1 (Fig. 5(b)), the  
 854 4-DOF model cannot capture the 6P peak at 1.2 Hz. The maximum stress time histo-  
 855 ries at the hotspot obtained from the fully coupled model and the 4-DOF model are  
 856 compared in Fig. B3(a), with a TRAC value of 0.99. In Fig. B3(b) the maximum  
 857 stress time histories obtained from these two models are compared in the frequency  
 858 domain, showing that the two models predict very similar stresses at the hotspot, es-  
 859 pecially up to a frequency of 1 Hz (similar to Fig. 6). The normalised fatigue damage  
 860 index and the computation duration are listed in Table B1, demonstrating that the 4-  
 861 DOF model is able to predict fatigue damage accurately and very quickly compared to  
 862 the fully coupled model.



(a)



(b)

863 Fig. B3. Comparison of the stress of the hotspot at the mudline from the fully coupled  
 864 model and the 4-DOF model in the time domain (a) and frequency domain (b).

865

866

867 Table B1 Normalised fatigue damage indexes and computation duration for the fully  
868 coupled model and the 4-DOF model (9<sup>th</sup> environmental state, wind speed 12 m/s).

	Normalised damage	Computation duration (s)
Fully coupled model	5.60	2350
4-DOF model	5.11	13

869

Journal Pre-proof

**Declaration of interests**

- The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.
- The authors declare the following financial interests/personal relationships which may be considered as potential competing interests:

Journal Pre-proof