Future climates: Markov blankets and active inference in the biosphere

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 We formalise the Gaia hypothesis about the Earth climate system using advances in theoretical biology based on the minimization of variational free energy. This amounts to the claim that nonequilibrium steady-state dynamics—that underwrite our climate—depend on the Earth system possessing a Markov blanket. Our formalization rests on how the metabolic rates of the biosphere (understood as Markov blanket's internal states) change with respect to solar radiation at the Earth's surface (i.e., external states), through the changes in greenhouse and albedo effects (i.e., active states) and ocean-driven global temperature changes (i.e., sensory states). Describing the interaction between the metabolic rates and solar radiation as climatic states—in ^a Markov blanket—amounts to describing the dynamics of the internal states as actively inferring external states. This underwrites climatic nonequilibrium steady-state through free energy minimisation and thus a form of planetary autopoiesis.

Key words: Autopoiesis, active inference, free energy minimization, Earth's climate system, Gaia hypothesis

1- Introduction

 The standard models of the Sun's evolution show an increase in its radiation and brightness over time [1,2]. Yet, 26 there is empirical and model evidence that, despite exposure to increasing radiation, the temperature of Earth's climate has remained bounded at habitable levels ≈0–40°C since the Archean (4 billion years before present) [3,4]. In contrast, Earth's climate dynamics would not be possible for its planetary Lifeless neighbours—such as Mars and Venus—whose dynamics are non-habitable [5].

30 It has been noted since the inception of physiology that biological systems maintain their organization and bounded internal conditions in the face of external fluctuations [6]. In contrast, the entropy of inert (and closed) systems is unbounded and increases indefinitely. This asymmetry between external and internal conditions is thus broadly recognized as an important characteristic of biological systems [7,8]. Schrödinger asked about such internal conditions, '*how can the events in space and time which take place within the spatial boundary of a living organism be accounted for by physics and chemistry?*' [9], p.2.

35 Recent advances in theoretical biology suggest that biological systems can resist dissipation and external fluctuations through predictive behaviour [10–12]. That is, biological systems preserve their organization and bounded internal conditions by anticipation or active inference, or at least behave as if they had these predictive faculties. The underlying 38 observation is that the time evolution of all systems, whether they are biological or not, depends on the past. However, the time evolution of living systems, looks as if it depends not only on the past and present, but also on the future [10–12]. The reason 40 for this is that living systems act on the basis of a predictive model of their ambiance: they appear to model their ambiance to preserve their organization and bounded internal conditions [10–12]. Such predictive behaviour is named anticipation [10,13– 42 16], allostasis [11,17,18] and recently, active inference [12,19-21]. Active inference is a corollary of the free energy principle 43 that describes the self-organisation of systems that can be distinguished from their external milieu, in virtue of possessing a Markov blanket [12,21].

 Since the asymmetry between the Earth's internal and external conditions implies some sort of action to maintain the 46 bounded temperatures at habitable levels, we therefore offer the following hypothesis: can the Earth's climate system be

 interpreted as an anticipatory system that minimizes variational free energy? [22]. This hypothesis provides an interesting connection with the Gaia hypothesis which argues for Earth's planetary bounded internal conditions *by* and *for* the biosphere [23–25]. Here, we formalise the Gaia hypothesis by providing key organizational relationships among the atmosphere, hydrosphere, lithosphere, and biosphere that allow a mathematical formulation of a Markov blanket for the Earth's climate system. This should be considered as a precondition for interpreting and proving (elsewhere) that the temperature of the Earth's climate—bounded within habitable ranges—has arisen due to an anticipatory or active (Bayesian) inference. In the 53 following section, we briefly review the relationship between Markov blankets, free-energy minimization, and active inference. We then propose, based on empirical evidence and prior model-based theoretical work, the existence of a Markov blanket for the Earth's climate system. Finally, we point out some implications of this formal treatment for studying the Earth's climate dynamics.

2- Free energy, Markov blankets and active inference

 Although the principle of free energy minimization arose in neuroscience, it turned out to be sufficiently generic to ascribe cognitive processes to all living systems [12]. Thus, the minimization of free energy (a.k.a., a generalised prediction error) can be regarded as a dynamical formalization of the embodied cognition implicit in autopoiesis or biological self- production [12,26–30]. One of the conditions for the existence of an autopoietic system is a boundary [31], which resonates with Schrodinger's question above. A Markov blanket defines the boundary between a system of interest and its environment in a statistical sense. More specifically, it provides a statistical partitioning of a system into states internal and states external to the system. In this context, a Markov blanket is a set of variables through which things internal and external to a system interact.

 Important examples of Markov blankets arise in multiple fields. One of the most commonly encountered is the present – which is the Markov blanket separating the past from the future and underwrites the notion of a Markov process. Markov processes (Gagniuc 2017) are stochastic (random) processes whose dynamics may be characterized without reference to their distant past. In other words, if we know the present state of a system, knowing about the past tells us nothing new about the likely future. On one reading of Newtonian physics, the positions and momenta of particles can be seen as the Markov blankets through which particles interact with one another (Friston 2019). In the life sciences, Markov blankets have been associated with the physical boundaries surrounding cells (Friston 2013, Kirchhoff, Parr et al. 2018, Palacios, Razi et al. 2020) (i.e., their membrane) through which all influence between the intracellular and extracellular spaces are mediated. At larger spatial scales, they have been drawn around plant physio-anatomy (Calvo and Friston 1917) and neural networks (Hipolito, Ramstead et al. 2020) such that the superficial and deep pyramidal cells of the cerebral cortex play the role of a Markov blanket, through mediating interactions between different cortical columns. This concept has been extended to an arbitrary number of spatial scales (Ramstead, Badcock et al. 2018), with muscles and sensory receptors acting as an organism's 80 Markov blanket, and specific organisms acting as blankets to separate groups of organisms. The thing all of these examples have in common is that they separate the world into two sets of states, which interact only via their Markov blanket (Clark 2017).

84 Pearl [32] introduced the term 'Markov blanket' to describe the set of variables that mediate relationships to and from 85 a variable of interest. More precisely, for a given variable X and its known blanket states b , no more information about X is gained when knowing the state of variables outside b . This does not imply that knowing the blanket states allows one to fully 87 predict the evolution of the target variable. This is because there may be some intrinsic properties in the system that renders X stochastic. Markov blankets segregate 'directed graphs' known as Bayesian networks such that one side of the blanket is conditionally independent of the other, given the blanket. This conditional independence clearly has important existential implications.

92 The Markov blankets that one considers in active inference, comprise sensory and active states, that feature specific coupling or causality relationships with internal and external states [12,21] (see Figure 1). Here, the term "states" stands for any variable of the system. A stipulative condition for the existence of a Markov blanket is that internal states must be conditionally

- 95 independent of external states, given blanket states and vice-versa. This formalizes the idea that there are no direct 96 interactions between internal and external states, only via the blanket states. In other words, internal and external states can 97 only influence one another via sensory and active states and the internal states only 'see' the external states through the 'veil'
- 98 of the Markov blanket [12,21]. Specifically, active states mediate the influence of internal states on external states, and sensory
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- 99 states mediate the reciprocal influences. In other words, internal states cannot influence sensory states, while external states 100 cannot influence active states [12,21] (Figure 1). The conditional independence between internal and external states—provided
- 101 by blanket states—enables interactions between the inside and outside of the system, but only via the blanket. It is worth noting
- 102 that the terms 'active' and 'sensory' derive from applications of this formalism to biology. However, the same mathematical
- 103 relations exist in Hamiltonian dynamics, where these may be replaced with the labels 'position' and 'momentum'.

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 Figure 1. Markov blankets and active inference. Panel A and B illustrates the partition of states into internal states and hidden or external states that are separated by a Markov blanket—comprising sensory and active states in the brain and in a cell, respectively. For the assignation of states in the brain see reference [33,34]. B) The internal states can be associated with the intracellular states of a cell, while sensory states become the surface states of the cell membrane overlying active states (e.g., the actin-like MreB filaments [REF] that mediate 109 cell mobility). The intracellular state dynamics of a cell correspond to perception, while action mediates coupling from internal states to 110 external states. Importantly, once such a Markov blanket is established for a system of interest, along with the necessary condition of non-111 equilibrium steady state (NESS), one can formally show that the internal states predict external states and thereby autoregulate the system, via a minimization of variational free energy [33,34]. This in turn implies that the expected entropy of sensory states remains bounded, thereby ensuring resistance to dissipation by external fluctuations. Note that *^s* here is assumed to be given by a static function of *x*. This contrasts with the dynamical formulation presented in some papers. The underlying reason for this is that most software implementations use *^g* to specify a likelihood of sensations given external states, under an adiabatic approximation to the underlying dynamics.

116 Active inference is, thus, an account of autopoiesis in dynamic terms, provided that such systems are (i) at non-117 equilibrium steady state (NESS) and (ii) that can be statistically segregated from their environment as in Figure 1. The first 118 NESS condition simply means that a system persists over a nontrivial time-scale and does not dissipate. This implies the 119 existence of a NESS density to which the system self-organises that can be thought of as a probabilistic description of the 120 system's pullback attractor [35,36]. The second (statistical segregation) condition implies the presence of a Markov blanket 121 [20,32]. The NESS dynamics of the system—and the presence of the conditional independencies implied by a Markov 122 blanket—means that the average internal state effectively parameterise a probability distribution over the external states 123 [12,20,33,34]. In other words, for any given blanket state, the average internal state represents the causes (i.e., hidden, or 124 external) of sensory impressions. It is fairly straightforward to show that the dynamics of the (average) internal state constitute a 125 gradient flow on a variational free energy functional of this parameterised density. The minimization of free energy (and implicit 126 minimisation of sensory entropy) enables biological systems to maintain their sensory states within physiological bounds, and 127 undertake predictive behaviour about the causes of their sensation necessary to sustain their existence [12,21,37].

129 **In this context, minimisation of free energy means resisting entropic fluctuation and maintenance of a bounded set of** 130 physiological states. As free energy is a functional of a probabilistic model (the parameterised density over external states 131 above), this means a system must instantiate an implicit model of its ambient space. Minimising free energy fits such a model 132 to sensory states, thereby ensuring good predictive behaviour. In Bayesian statistics, the evidence for such a model is known 133 as the 'model' evidence or marginal likelihood: namely, the probability of observing some data, given a model of how those data 134 were generated. Variational free energy upper bounds the negative log model evidence, which is a ubiquitous quantity in 135 statistical physics, Bayesian statistics and machine learning [38]. In machine learning, the variational free energy is commonly 136 called the evidence lower bound, or ELBO [39]. In engineering, it is the cost function associated with Kalman filters. In 137 information theory, minimising free energy corresponds to maximising efficiency or minimum description length approaches. In 138 predictive coding, the evidence is taken as the (precision weighted) prediction error. Crucially, in the free energy framework 139 these are all the same thing: the probability distribution encoded by the internal states that quantifies the dynamics of the 140 external states and evolves towards the variational free energy minimum [40]—an upper bound on surprise or negative log 141 evidence (i.e., the negative log probability of finding the system in a particular state) [12]. 142

143 The surprise is a function of the states of the Markov blanket itself [40]. Free energy is a function of probabilistic 144 beliefs, encoded by internal states about external states (i.e., expectations about the probable causes of sensory interaction), 145 oiven any blanket state¹. When these beliefs are equal to the posterior probability over external states, free energy becomes 146 equivalent to surprise. Otherwise, it is always greater than (i.e., constitutes an upper bound on) surprise [40]. Vicarious 147 interaction through a Markov blanket lends an interpretation to the dynamics of such systems, as if internal states were inferring 148 external states based upon the blanket states. This implies that the kind of organization of Markov blankets we consider results 149 in processes that work to seek out evidence (active inference), namely self-evidencing dynamics underlying the autopoietic— 150 thus autonomous—organization of life.

 151 In brief, this means we can characterize living systems as minimising variational free energy, and therefore surprise, 152 where the minimisation of variational free energy entails the optimisation of beliefs about things beyond the Markov blanket 153 (i.e., external states). Thus, external fluctuations can therefore (or must therefore) be modelled to maintain a bounded set of 154 physiological states. This formalism has been applied to a range of problems in biology [12,28,41,42] including thermodynamic 155 physical systems [33,34]. On the basis of the ensuing Bayesian process of active inference, we turn next to defining and 156 evidence-based Markov blanket for the Earth's climate system.

157 **3. Markov blankets and the Earth's climate system**

 Several authors suggest that autopoiesis happens at the planetary scale [43–52]. The implication of this view is that minimization of variational free energy must also occur at the planetary level. The challenge for this perspective is to identify the Markov blanket of a climate system (here, the Earth) such that we can think about how internal states of the system may appear to infer and act upon external states. Delineating this blanket is essential in finding the generative model that determines climate dynamics. To do so, we need to define variables (i.e., states) internal and external to the Earth's climate 163 system—those states that constitute or are intrinsic to the system and those that are not. In so doing, we regard empirical and 164 model-evidence based interactions between the Earth's climate components and identify a set of variables that satisfy the conditional independencies allowed by the Markov blankets that underwrite active inference (Figure 2):

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¹ Technically, this means that surprise is a *function* of blanket states, while variational free energy is a *functional* of a probability distribution about external states, given a blanket state.

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169 **Figure 2 – Earth's climate and Markov blankets.** This figure illustrates the conditional dependencies between four key variables in the 170 Earth's climate system. These conditional dependencies imply a Markov blanket comprising active (*a*) and sensory (*s*) states (in analogy 171 with perception-action loops in cognitive science) that mediate the interactions between internal (μ) and external (χ) states. The internal 172 states are the metabolic rate changes of atmospheric greenhouses and aerosols turnover (see section 3.2 for the full explanation). These 173 influence active states (changes in greenhouse and albedo effects) (see section 3.3) and vicariously the external states (solar radiation 174 changes at the Earth's surface) (see section 3.1). The external states cause changes in the sensory states (ocean-driven global temperature 175 changes) (see section 3.4), which leads to changes in the internal states. External (and sensory) states exhibit dynamics prescribed by 176 stochastic differential equations (or a static stochastic mapping) with Gaussian white noise uncorrelated in time (*ω*). Internal and active 177 states perform a gradient descent on variational free energy (*F*), defined in relation to a (characteristic) NESS density for the external and 178 sensory states. As a consequence, the internal states appear to model and act upon the external and sensory states. 179

180 Figure 2 illustrates the conditional dependencies between variables forming the Earth's climate system and Markov blanket, 181 highlighting that the metabolic rates of the biosphere (internal states) only influences solar radiation at the Earth's surface 182 (external states) via changes in greenhouses and albedo effects (active states), while reciprocal interactions are mediated by 183 the ocean-driven global temperature changes (sensory states). We turn next to defining each of these variables that constitute 184 this climatic partition of states.

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187 **3.1 External states (***x***): Solar radiation changes at the Earth's surface**

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189 The space weather² and external environment of the Earth system, such as the electromagnetic solar radiation and 190 galactic cosmic shortwave radiation and energetic electron precipitation, are the source of energy, but also of external forcing 191 and perturbation, respectively [53]. In many mainstream climate models (radiative energy balance models, EMICs and GCMs) 192 cosmic rays are not a source of forcing fluctuation in the climate system. Indeed, those who normally study the impact of 193 cosmic rays on Earth are not climatologists, but astrophysicists and planetary scientists. In line with the interdisciplinary 194 perspective offered here, we mention these possibilities – which could be incorporated into the external states of a Markov 195 blanket for the Earth's climate system. However, the key construct of the Markov blanket does not depend upon this, and the 196 external states stand in for anything outside of the system of interest that causes changes to the blanket states.

² "Space weather refers to dynamic conditions on the Sun and in the space environment of the Earth, which are often driven by solar eruptions and their subsequent interplanetary disturbances" [56].

 According to the standard model of stellar evolution, the incoming solar radiation during the Archean to the Proterozoic eon (3.8 billion to 542 million years ago) was 20–30% lower than at present [1,54]. The faint young Sun was only 76%-83% as intense as its current value [55]. Also, the Sun often displays extreme and severe coronal mass ejections, solar flares, and storms, making the Earth's space weather difficult to predict [56]. Sunspots and low solar activity (solar Maunder minimum) correspond with historically documented cold periods on Earth—and is often related to little ice ages, in the form of frost fairs [57]. Diverse reconstructions of past climate records, in cosmogenic isotope archives, have revealed associations between the Earth's climatic response to solar radiation changes and cosmic ray variations [58].

 Despite changing space weather, such as solar radiation fluctuation, the Earth is close to being in *radiative equilibrium*. The incoming energy (mainly of the Sun) is balanced by an equal flow of heat that the Earth radiates back to outer 207 space. Under the condition of the Earth's so-called energy flux balance [59], Earth's temperature is bounded at habitable levels [4]. How the energy flows into—and away from—the Earth is key to understanding climate dynamics [60]. This also indicates 209 that although the solar radiation at the Earth's surface is necessary, it is not the only factor affecting global temperatures on Earth. There are different constraints and processes that account for the Earth's energy flux balance. These depend on the time scale. At very short times scales, among other phenomena, the incoming Sun radiation leads to evaporation of seawater and sea surface temperature changes [61]. At millennial times scales (the last 3 million years) changes of solar radiation at the Earth's surface due to variations in the Earth's orbit *triggered* climatic changes such as glacial-interglacial oscillations (variations in ice volume and ice sheet extent) [62], the so-called Milankovic effect of orbital (astronomical) forcing. At long time scales (from 2 to 4 billion years), different constraints on the Earth system offset the weak forcing and radiation of the faint voung Sun. Thus, the solar radiation exerts different forcing at different time-scales. Our proposal is that changes in solar 217 radiation at the Earth's surface account for the external states of the Earth's Markov blanket (x) (Fig. 2).

 For the Earth's Markov blanket proposed here, volcanoes—a source of carbon and abiogenic aerosols—may not be external to the Earth's climate system. This follows from the next argument: the structure of inner and outer layers of the continental plates appears to have been dominated by water-dependent continental drift changes [63]. The hydrological cycle, which allows continental drift and geomorphological changes, is life-dependent [64]. Together with the shift from the reductive to oxidative atmosphere—from the advent of photosynthesis and the shifting balance between seafloor and terrestrial 224 weathering REFMills et al in the middle Archean to the proterozoic period —resulted in the strength of the hydrological cycle, continental drift, continent growth, plate spreading, volcanic activity [65–68]. Tectonic and volcanic activity and their products, therefore, are ultimately internal to the Earth system functioning, and thus to its Markov blanket.

228 Under free energy minimization, the forcing by the external sates may affect Earth's climate only through its Markov 229 blanket's sensory states $(x \to s)$ (ocean-driven global temperature changes) (Fig. 2). At first glance, one might think this to be 230 only partially true, because the solar irradiance impacts on the Earth's upper atmosphere. However, the insolation on the upper atmosphere is quite different to the insolation reaching the Earth's surface after passing through the atmosphere, most of which is metabolically derived (see next sections). Hence, changes of atmospheric states triggered by the solar irradiance and cosmic 233 ray particle ionization—such as large-scale electric current dynamic changes in the troposphere [69], or enhanced cloud formation [70]—are ultimately determined by the internal states through active states. In short, the changes in solar radiation at the Earth's surface may be selected by the internal states through active inference.

3.2 Internal states (): metabolic rate changes

238 Internal states must be conditionally independent of external states provided blanket states and vice-versa. This 239 formalises the idea that there are no direct interactions between internal and external states, only via the blanket states. Here 240 we propose that the metabolic rate changes fulfil this condition, and thus are the Earth's Markov blanket internal states (μ) . We base this proposition on the following arguments.

243 The metabolic rate reactions directly depend on habitable bounded temperatures and only indirectly on the incoming 244 solar radiation (external states). This means that the external states of Earth's Markov blanket can only affect the metabolic rate 245 changes through bounded sensory states $(x \rightarrow s \rightarrow u)$ (Fig 2). One may argue that this is not true, because the photosynthesis depends on solar radiation. However, at low temperatures, between 0-10°C or above 20°C the enzymes that carry out 247 photosynthesis do not catalyse at the optimum photosynthetic rate, which is obtained between 10 and 20 $^{\circ}$ C [71,72]. Indeed, all 248 the metabolic rate reactions on the Earth system depend directly on the physiological temperatures between ≈0–40°C [74] at 249 which the Earth has remained since the Archean [3].

250 The metabolic rate changes affect the incoming solar radiation (external states) only through its active states ($\mu \rightarrow$ $a \rightarrow x$) (Fig 2), which are fundamentally linked to the rate of net primary productivity (NPP). While the biosphere captures no more than 1% of solar radiation, and thus can be considered insignificant on the Earth's energy flux balance, from the Archean to the present the atmospheric and lithospheric chemical elements have been continuously metabolically transformed, produced [25,75–79], mobilized [80], localized [81], and integrated into biogeochemical cycles by a relatively stable microbial 255 set of core enzymes involved in major redox reactions and electron transfer of Earth's chemistry, despite enormous genetic diversity [82]. Indeed, through Earth's ontogeny global NPP had contributed three times more energy to the geochemical cycles 257 than Earth's internal heat [65]. While the contribution of the marine ecosystems (mostly microbial) is longer over geological time scales, the continental ecosystems per unit area contributes much more and faster due to availability of key nutrients and solar 259 energy. However, due to the extension of the ocean and the accelerated rates of continental weathering in the continents both have equivalent contribution to the global NPP. Thus, the metabolic rate changes have resulted, among other things, in changes in greenhouse and albedo effects (active states) (Fig. 2), and hence in the Earth's energy flux balance and habitable 262 temperatures.

263 More specifically, the biogeochemical carbon cycle, upon which most of the current climate change depends (IPCC 2013), involves carbon dioxide (CO₂) and methane (CH₄) in the troposphere due respectively to metabolic enhancement of rock weathering [83,84] and methanogenesis rates [85]. On Earth 99.9% of CH₄ is due to methanogenesis [86]. The biogeochemical 266 carbon cycle also is linked to the O₂ levels (availability of free energy) and the formation of ozone (O₃) in the stratosphere which intercepts, absorbs and converts more than 97% of the sun's mutagenic ultraviolet radiation into heat [67]. The biogeochemical sulphur cycle involves the production and release into the troposphere of biogenic cloud-forming aerosols, such as dimethyl 269 sulphide (DMS). On average, the aerosols of ocean microorganisms boost the number of cloud droplets by about 60% annually [87]. DMS is produced not just on the sea [88], but also on continents [89,90]. The microbes suspended in the atmosphere also induce cloud formation [91,92]. A biogenic aerosol-climate linkage has been postulated, through the albedo effect of clouds affecting the incoming solar radiation, hence the Earth's energy flux balance and temperature [93]. Model-based evidence shows this is highly plausible [94–96]. What is crucial is that the existence of glaciers and ice sheets, which translates effectively into changes in albedo effects (active states), depends on the accumulation of snow and therefore on a great part of 275 global cloud cover derived from metabolism.

276 Metabolism is a self-organizing phenomenon [97–101] involving not just the biosphere, but the atmosphere, hydrosphere, and geosphere [103–106]. Nevertheless, the internal states proposed here focuses on carbon cycling, biogenic 278 aerosols and (oxygenic) photosynthesis, whereas the metabolic network of the biosphere is much more complicated [82] and 279 rates may be limited by other components such as nitrogen availability (also biologically constrained). A more extensive 280 overview of the different ways in which metabolic interactions within the biosphere intertwined with the dynamics of the Earth's geochemistry [82] should be considered in the future for a more detailed account of internal states. Here, we simply acknowledge that the system cannot respond with infinite capacity to appropriate temperature ranges when it also depends on biological cycling of essential nutrients. In this regard the dynamics of internal states' response may be critical.

 Different explanations have associated biological evolution at the "species" level with the metabolic responses [Ref $286 - 1.2$. These proposals suggested that the persistence of the biosphere increased its likelihood of acquiring further persistence-287 enhancing traits and that species that destabilize their environment are short-lived and result in extinctions until a stable state is found. While it is reasonable to say that metabolic rate changes plays out on the diversity, richness, abundance, and connectivity (trophic and symbiotic relations) of eukaryotic systems and prokaryotic microorganisms in the ocean, continents, deep subsurface and atmosphere [45,108–110], "speciation" requires the arising of new lineages, which may take ecological and geological timescales. At least, so far, there is no experimental evidence of speciation under controlled conditions even at the level of operational taxonomic units in microorganisms. Thus, although the biospheric diversity encodes the metabolic capacity, it is more congenial that the dynamics of the internal states' responses are associated with metabolic rate changes based on a relatively stable phylogenetic redundancy of a set of a key core enzymes (e.g. Rubisco) [82] [107] scattered in a single rhizome network of the biosphere [102]. Enzymes are fast acting and demand low energy of activation [Ref], which 296 continuously and directly ensures the changes in greenhouse and albedo effects that constitute the active states (Fig. 2), and thus instantiate the internal states (μ) beneath the Earth's Markov blanket.

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3.3 Active states (*a***): changes in greenhouse and albedo effects**

 From the Archean to the Proterozoic eons (from 4 to 2.5 billion years ago), solar radiation alone was too weak [1,2], to maintain liquid water and ice-free conditions on Earth [54] (see section 3.1). Indeed, if all other global parameters are held constant, and if the Archean-Proterozoic Earth's greenhouse gas concentration in the atmosphere were the same as now (405 ppm/0.0405% and 722ppb/0.007% and of the air of CO₂ and CH₄ respectively), the Earth's mean temperature would have been below the freezing point of seawater (−18 °C) [55,111]. Earth would have been in continual deep freeze, with glaciers reaching 306 the Equator, at until one billion years ago, when the solar radiation had increased enough to melt the ice [55,111]. In this case, the internal states of the Earth's system, which rely on liquid water and physiological temperatures, would have been very limited or perhaps non-existent. And yet, there is ample geologic, paleontological and model-based evidence regarding this 309 geological period showing the existence of extensive bodies of liquid water at the surface and continuous habitable Earth's temperatures (≈0–40°C) [3,54,55,112,113]. This puzzle is called the faint young Sun paradox.

 Earth's climate responses compensated for the young Sun's lower radiation at the Archean Earth's surface through the warming produced by higher greenhouse gas concentrations and reduced albedo [3,54,55,112–114]. The so-called greenhouse effect, on which greenhouses gases trap heat emitted from the surface's reflection. Precisely, the CH₄, which has 315 stronger radiative forcing than $CO₂$ and is almost entirely metabolically produced (see section 3.2), could have provided 10–12 \degree °C of surface warming [115] with levels ranging 10² to 10⁴ times higher than modern amounts [3]. A high amount of atmospheric nitrogen (increasing atmospheric pressure), dependent on the biogeochemical nitrogen cycle, would have given 4.5°C extra warming [116]. Thus, the increment of greenhouse gas fluxes and abundance was *necessary* to offset a fainter Sun [3,112], if 319 the habitable conditions of the Earth's system were to be maintained.

320 The solar radiation has steadily increased by twenty to thirty percent from the Mesoarchean, to the Proterozoic, to the present [1,2]. That is, the faint young Sun became a bright mature Sun. Yet, the Earth's liquid water did not evaporate as with 322 Venus or dissipate as with Mars [5]. Increasing solar forcing through time is roughly cancelled by decreasing greenhouse and 323 increasing albedo effects by atmospheric clouds and lithospheric ice-snow cover, which reflect the Sun's radiation back into space [117,118]. Evidence shows that over that period, the CH₄ and CO₂ greenhouse gases declined to their preindustrial 325 values, ~722ppb/0.007% and ~200 ppm/0.02% respectively [114]. This was an active process. Oxidative metabolic enhanced silicate weathering dampened the CO₂ concentration 1000 times faster [83,119] compared to inorganic anoxic carbonate– 327 silicate weathering [120]. The oxidative atmosphere derived from the evolution of photosynthesis shifted the metabolic rates towards oxidation and thus faster reduction of greenhouse gases [68,121]. The Proterozoic CH₄ has been damped by reverse 329 methanogenesis, causing an anti-greenhouse effect by forming a thick hydrocarbon organic haze given the changes of CH₄/CO₂ ratios higher than ~0.1 [115,122]. Moreover, since the late Archean, climate moderation by the carbon cycle (mainly CO2/CH4) is consistent with the increase of snow-ice cover, and thus occasional glaciations [3,123]. Glaciers, ice-sheets, and 332 snow cover depend on the cloud formation. Model-based evidence shows that the net effect of cloud cover is cooling [94–96]. Glaciers, ice-sheets and snow cover account for more than 70% of the Earth's albedo effect [60]. These results indicate that the 334 albedo effect is necessary to counterbalance the steadily increase of incoming solar radiation.

335 These rather basic observations allow us to assert that changes in greenhouse and albedo effects instantiate the active states of the Earth's Markov blanket. Both effects, the greenhouse and albedo, are conditionally dependent on the metabolic rate changes that result in modelling, inference and selection, through this blanket, of the incoming solar radiation at 338 the Earth's surface (external states) ($\mu \to a \to x$) (Fig. 2). Importantly, by acting upon the external states, the active states of the Earth's Markov blanket also bind (i.e., upper bound) the entropy of its sensory states, so that it does not increase 340 indefinitely, i.e., dissipate $(a \rightarrow x \rightarrow s)$ (Fig. 2)³.

3.4 Sensory states (*s***): ocean-driven global temperature changes**

 The ocean is a driving force affecting the Earth's mean temperature and thus the climate system's temporal evolution 345 [60,124,125]. Changes in Earth's mean temperature depend sensitively on the thermal inertia of the ocean's capacity to absorb heat (ocean heat uptake) [126,127]. The ability to absorb heat from the ocean is influenced by the physical-chemical properties of the water (high specific heat capacity), and also by the dynamics of the ocean itself and its interaction with the atmosphere. That is, the ocean does not change its temperature "rapidly" as the atmosphere does, and the oceans' heat uptake reduces the 349 effective climate sensitivity⁴ and weakens its warming response [124–126,128,129]. As a consequence, the ocean drives the global temperatures by distributing heat around the planet, responding very slow to thermal fluctuation and absorbing ¹⁰⁰⁰ 351 times more heat than the atmosphere without changing its temperature. It thus accumulates about 93% of the Earth's thermal energy [130]. The excess energy that the ocean stores can lead to the ocean's thermal expansion, e.g., melting of ice sheets and thus to sea-level rise, which on the latest glacial-interglacial oscillation represents changes in sea level over 100 m [131].

355 These empirical and model-based observations let us consider the ocean-driven global temperature changes as accounting for the sensory states (s) of the Earth's Markov blanket (Fig. 2), and, therefore, bidirectional interactions of the sensory states with external and active states. Incoming solar radiation (external states) mainly causes evaporation of ocean- surface water via sea-surface heat and surface temperature changes [61]. This affects water-vapor concentration in the troposphere, air-temperature distribution, winds, cloud formation and intermittent precipitation on continents and the absorption of greenhouse gases⁵ [132]. All these evince the influence of external on sensory and of sensory states on active states. Conversely, the effect of active states on sensory states is most likely the freshwater nutrient-rich fluxes from continents and ice-sheets to the oceans that create density gradients of salinity [133]. It is through the thermal and density gradients of seawater that sensory states affect (external states) incoming solar radiation changes at the Earth's surface. Both gradients ultimately determine ocean convection, turnover, and general circulation accounting for the slowdown in surface warming and the cooling of the ocean with the relevant effects on the glacial cycles [REF]. The overall ocean dynamics results in moving heat from Earth's equator to the poles, distributing energy throughout the Earth's climate components, and thus on the ocean-driven global temperature changes [124–126,128,129].

 These arguments speak to the dynamics of Markov blankets, in which external states cannot directly affect changes 370 in active states (greenhouse and albedo effects), but only as mediated through the sensory states. Similarly, the changes in solar radiation at the Earth's surface affect the metabolic rate changes (internal states) only through the sensory states (ocean-372 driven global temperature changes) $(x \to s \to \mu)$ [132,134]. That is, the ocean dynamics becomes the sensory states for the dynamics of whole biosphere (marine and continental) (see section 3.2). At first glance, one might question this, because the oceans cannot mediate the interactions between solar radiation and the continental ecosystems. However, the metabolic rate changes, not just in marine, but in continental ecosystems are driven by the Earth's mean temperature [79,135,136], which in turn is buffered, hence driven by the oceans' heat uptake and dynamics. At the same time, the only way that the internal states affect the ocean is through the chemical modification of the atmosphere and lithosphere, which results in changes of 378 greenhouse and albedo effects (active states) (see previous sections). This interaction between internal and external states as climatic states—in a Markov blanket—in turn will look present as the instantiation of active inference at a planetary scale.

³ Technically speaking, the entropy of the sensory state is effectively bounded from above and below. This follows, because the active maintenance of an Earth-like nonequilibrium steady-state precludes both high and low entropy NESS densities, e.g., solar, and lunar climates, respectively.

Climate sensitivity refers to how much, in the near and the long-term, the Earth's climate will warm (or cool) after a perturbation like an increase in $CO₂$ concentrations or solar radiation.

The ocean is the most important sink of atmospheric CO₂ [132].

4. Discussion: Active inference at the planetary-scale

 Within the free energy framework, the consideration of planetary autopoiesis as active inference rests upon the existence of a Markov blanket for the Earth's climate system. That is, in the relation and coupling of internal and external states through the Markov blanket. If we take the perspective that the metabolic rates change (the internal states of the Earth's Markov blanket) is performing active inference about the changes in incoming solar radiation (external states), we can frame 387 their dynamics in terms of approximate Bayesian inference, which is equivalent to the minimization of variational free energy. This treats the metabolic rate changes as if they parametrize an implicit (variational) probability density over solar radiation changes at the Earth's surface and optimize this to maximize model evidence of changes in external states to preserve habitable conditions.

 As the metabolic rate changes influence changes in greenhouse and albedo effects, the indirect or mediated 392 influence of solar-radiation variation at the Earth's surface is mathematically equivalent to Bayesian inference. This is because 393 we could, in principle, use the average solar radiation changes at the Earth's surface to draw inferences about the variables affecting the metabolic rate changes. This perspective implies a NESS density associated with the blanket and its external 395 states, i.e., the density that the system tends toward when it is perturbed. In analogy with biological-like behaviours at the planetary-scale proposed by the Gaia hypothesis, this may be thought of as the range of values within which Earth's homeorhetic dynamics can anticipate (and accommodate) any deviations. Dynamic anticipation of this sort implies that changes in greenhouse and albedo effects also optimize the same quantity through changing ocean-driven global temperatures (directly and via external states).

400 An alternative interpretation of the NESS density is as a generative model. This implies that the metabolic rate changes implicitly may model solar radiation changes at the Earth's surface and select them via changes in greenhouse and albedo effects. This process of selection through modelling the environment means that to find the dynamics of the metabolic 403 rate changes—and their influence over changes in greenhouse and albedo effects—we need only to specify the NESS for solar 404 radiation variation at the Earth's surface and ocean-driven global temperatures. The dynamics of active and internal states will emerge from minimizing free energy. That is to say, a sort of planetary selection of permissible perturbations from solar radiation changes at the Earth's surface results in the continuous operating of the Earth's system habitability. What is selected 407 will depend on the active inference at planetary-scale, in relation to the model it generates through the integrated dynamics of 408 the biosphere, atmosphere, lithosphere, and hydrosphere.

 This perspective of such a mathematical formalism may be useful in the modelling of the Earth's climate system as a 411 systemic unity in three ways. The first is in inferring parameters of the implicit NESS density (or generative model) that underwrites the Earth's climate dynamics. The second is that alternative models (with alternative NESS densities) may be proposed to formulate alternative hypotheses about the Earth's climate system. A common mathematical framework enables 414 model comparison (i.e., hypothesis testing) to adjudicate between these hypotheses. Thirdly, this may be useful in predictive modelling, that is, in establishing how different interventions may impact the long-term evolution of Earth's climate. A pragmatic consideration here is that if one can write down the NESS density over external (solar) and sensory (oceanic) states—that is characteristic of the Earth—one can simulate the metabolic (i.e., internal states), greenhouse and albedo effects (i.e., active 418 states) using a gradient flow on variational free energy. The key point here is that the requisite gradients are analytically and numerically tractable; enabling the climactic simulations, much along the lines of how active inference is used to model 420 experimental subjects in cognitive science (neuroscience and ethology).

 While this paper sets out a possible conditional dependency structure between environmental variables, consistent with a Markov blanket, this should be viewed as a hypothesis. This is subject to evidence that could support or refute this. For 424 example, if it were demonstrated that solar radiation at the Earth's surface and metabolic rates in the biosphere are not (approximately) conditionally independent of one another, once greenhouse, albedo, and ocean temperatures are taken into account, this would offer strong evidence against our hypothesis.

 The relatively abstract treatment here – based upon conditional dependencies – means we have not specified a functional form for the equations of motion linking the dynamics of each climate component. This highlights the work yet to be 430 done to move from a theoretical framing of climate dynamics to a useful model that can be used to test empirical hypotheses. The next two phases of this research will be as follows. First, we need to specify the functional form of the external state dynamics, as a function of the active states, and the form of the sensory states as a function of the internal and active states. This sets up an implicit generative model from the perspective of the active and internal states and means we can test the face 434 validity of this formulation through numerical simulation. In addition, we hope to demonstrate construct validity in relation to 435 established climate models. The second phase will be to fit these numerical simulations implemented with standard software routines (e.g. **spm_ADEM.m⁶**) to climate data. In doing so, we hope to develop a tool that lets us evaluate the evidence afforded by alternative hypotheses about the causes of these data. Under active inference, these hypotheses are typically framed in terms of the parameters of prior beliefs implicit in a generative model (Schwartenbeck and Friston 2016). In other 439 words, we can think of internal states as evolving as if they held beliefs about the external states, and can test hypotheses about what these beliefs might be. The utility of this framing is that our interest is in how biotic and abiotic elements of the climate interact, so it is helpful to be able to pose hypotheses about the one in relation to the other. However, the perspective that the internal states of the Earth's Markov blanket perform inferences about—and act on—the incoming energy radiation through the ocean (sensory) and the greenhouse-albedo effects (active) states may tell us something profound about the character and nature of the Earth.

5. Conclusion

 This paper outlines key organizational relationships among the Earth's systemic components—comprising the atmosphere, hydrosphere, lithosphere, and biosphere—that allows one to posit the existence of a Markov blanket for the Earth's climate system. The motivation for this proposal follows the hypothesis that the nonequilibrium steady-state dynamics that underwrite our climate history depends on planetary active inference, which rest upon the existence of a Markov blanket that enshrouds the Earth's internal states. This requires an appeal to the mathematics of living (cognitive) systems, such as minimization of variational free energy, where the formalism of interaction with an external environment has been most comprehensively developed. The Earth system's Markov blanket proposed above conforms to some basic model-based and empirical observations about how the metabolic rate (framed as the internal states) interacts with changes in the solar radiation at the Earth's surface (external states) through ocean-driven global temperatures (sensory states) and through the atmospheric-lithospheric greenhouse-albedo effects (active states). Crucially, a Markov blanket equips the Earth's climate system with a Bayesian process that will allow us to see whether the average internal states appear to engage in active inference—to actively maintain a nonequilibrium steady-state. That is to say, establishing a Markov blanket for the Earth's climate system may allow us to treat its dynamics as performing active inference, in the fashion of biological anticipation (Rosen 1985), and as a form of planetary autopoiesis.

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Part of the freely available as Matlab code in the SPM12 academic software: <http://www.fil.ion.ucl.ac.uk/spm/>

