

Figure 2a shows the THz amplitude and phase measured at the Rx2 as a function of time for the OIL system i.e. without any feedback to the QCL current source (hollow squares) and the OIPLL system (solid squares). The Rx2 delay line was scanned to measure the amplitude and phase of the QCL emission. We can see that over 10 minutes, the THz amplitude and phase of the OIPLL system was $\sim 225 \text{ mV} \pm 10 \text{ mV}$ and -0.06π respectively, and it remained stable throughout the measurement period. However, for the OIL system, the amplitude ($\sim 225 \text{ mV} \pm 100 \text{ mV}$) and phase ($\sim 0.1\pi$) drifted significantly after the 5th minute. The amplitude drifts by more than 50%, whereas the phase underwent $\sim 0.4\pi$ shift. This drift could be due to the thermal, electrical or mechanical noises in the system. Adding the PLL enhanced the amplitude and phase stability of the OIPLL system.

When in the OIPLL state, the locked QCL frequency is determined by the injected THz reference frequency and the phase of the locked QCL (relative to the reference phase) can now be controlled independently by adjusting the offset of the PLL. Inset in Figure 2a shows the measured THz amplitude and phase values as a function of the offset voltage. With the THz amplitude remaining constant, the QCL phase undergoes a 0.3π phase shift when the offset voltage is changed between -0.3 V to 0.3 V . Beyond the 0.3 V , the PLL filter amplifier saturated.

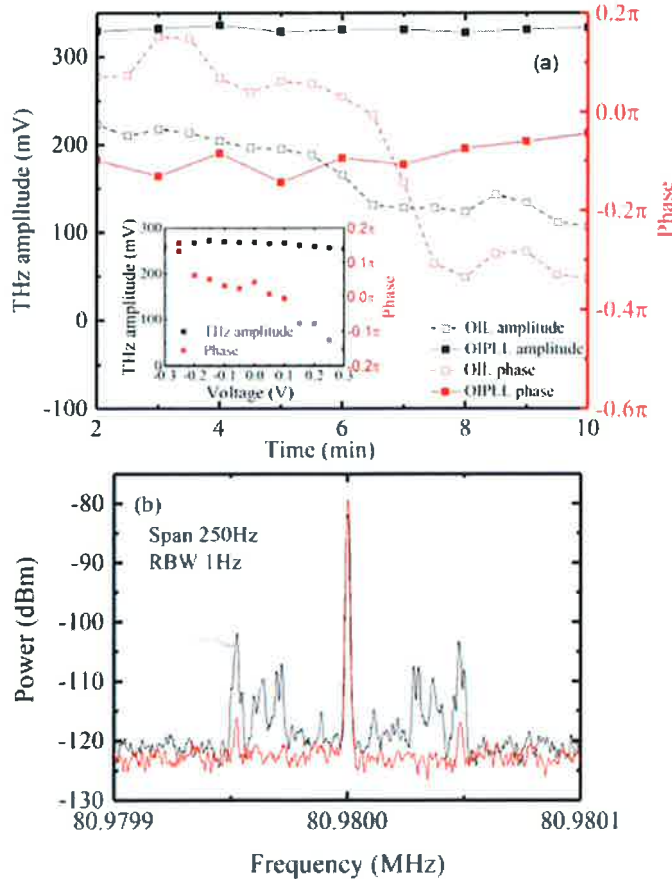


Figure 2: (a) The THz amplitude and phase at Rx2 measured as a function of time for the OIL (hollow squares) and OIPLL (solid squares) system. Inset shows the THz signal amplitude (black symbols and line) and phase (red symbols and line) plotted as a function of the DC voltage offset. (b) Measured linewidth spectra for the OIL (black) and OIPLL (red) states.

The linewidth of the locked QCL was measured for the OIL and OIPLL states by heterodyning the locked QCL frequency and frequency-shifted version of the THz reference frequency

in the Rx2. A fibre-coupled acousto-optic modulator was used to frequency shift one of the DSDBR lasers by 80.98 MHz on the Rx2 beam path. The transimpedance amplifier gain and bandwidth was adjusted to be 10^4 and 80 MHz, respectively. Figure 2b shows the measured linewidth spectrum for the OIL and OIPLL states at a 250 Hz span and a RBW of 1 Hz. The 3 dB linewidth is $<1 \text{ Hz}$ for both states suggesting that the spectrum analyser limits the measured linewidth of the locked QCL. The presence of sideband peaks on the OIL spectrum at $80.98 \text{ MHz} \pm 50 \text{ Hz}$ is due to the electrical and mechanical disturbances, which are compensated by the use of PLL resulting a cleaner spectrum for the OIPLL.

III. SUMMARY

We report the absolute frequency and phase control of a THz QCL locked to a microwave optical synthesizer by an OIPLL. The THz amplitude and phase was stabilized using the OIPLL system. The stabilized phase of the locked QCL was controlled using a PLL. The instrument-limited linewidth of the locked QCL was measured to be $<1 \text{ Hz}$. All the components used in the work, IR comb, QCL, PLL and photomixers could be monolithically-integrated onto a single photonic chip making a compact and portable high-precision THz system.

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