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2 Mechanical behaviour of a compacted well-graded granular material
3 with and without cement

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15 **Abstract:**

16 Cement additions improve the performance of granular soils. However, most literature
17 examples of cement additions are in poorly graded sands, either to mimic the behaviour of
18 sandstones or to accentuate the mechanical differences between cemented and uncemented
19 soils. In this article, the behaviour of a well graded granular soil, used for base and sub-base of
20 roads, was studied by doing triaxial tests on cemented and uncemented samples. Samples were
21 compacted to achieve a dense fabric and tested at stresses commonly used in practice. Sieving
22 was used to understand if breakage is important and to determine the grain size distributions of
23 the samples after compaction and shearing. The results show that the addition of small
24 percentages of cement greatly increase stiffness and dilation. Thereby, generating larger
25 strengths; this is particularly important at low confining stresses in roads and parking areas,
26 where this material is commonly used. At large strains, the results show that different Critical
27 State Lines exist for both the uncemented and cemented soils. Each line has a different slope,
28 which is believed to be the result of the evolution of the grain size distribution of the cemented
29 soil. The normalised data indicate that a unique state boundary surface can be determined for
30 all three tested soils.

31 **Key words:**

32 Cemented soil, compacted soil, triaxial test, critical state, base and sub base, granular soil.

33

34 **1 Introduction:**

35 It is well known that soil properties can be enhanced by the addition of a cementitious material
36 i.e. Portland cement. Many researchers have shown the benefits in terms of bearing capacity,
37 shear strength and stability, reducing settlements and lateral deformation and to resist seismic
38 loads (Delfosse-Ribay et. al 2004, Tang et al. 2007, Shafabakhsh & Rezaeian 2010, Wand & Leung
39 2008a, Wand & Leung 2008b and Lohani et al. (2004). These cement percentages must be chosen
40 based on the desired property enhancement, such that the composite soil can perform according
41 to a set of specifications. Other researchers use this technique to mimic the behaviour of
42 sandstones in order to study the effects of structure (Alvarado et al. 2012a), as the poorly graded
43 soil exacerbates the effect of bonding, given the high void ratios produced.

44 The behaviour of natural and artificially cemented soils has been interpreted by many
45 researchers using the Critical State soil mechanics framework (Huang and Airey 1993, Coop
46 and Atinkson 1993, Cuccovilo and Coop 1997a and Haeri et al. 2006). Normalisation of the
47 data is based on the Critical State Line (CSL), as high-pressure equipment is often required to
48 determine the NCL of cemented soils, particularly if these are of a granular nature.

49 To understand the effects of cementation, the responses of the cemented and uncemented soils
50 are compared. Research in uncemented granular material has highlighted the importance of
51 breakage, where the onset of breakage in the NCL is a function of the mineralogy of the grains
52 [12]. Breakage is important as it also marks the location of the CSL, and many researchers have
53 shown that by changing the grain size distribution, the CSL will also change (Thevanayagam et
54 al. 2002, Carrera et al. 2011 and Xiao et al. 2016]. In structured sands, only a few researchers
55 considered the changes in particle size distribution (PSD) and its effect on altering the location
56 of the CSLs and NCLs, when compared to the uncemented samples (Cuccovilo and Coop
57 1997a and Marri et al. 2012). Certain results have shown that due to cementation, the resultant

58 CSL would have a reduced gradient (Cuccovilo and Coop 1997a), whilst others have shown
59 that the cementation increases the gradient of CSL (Schnaid et al. 2001). In the aforementioned
60 research, it is not clear if the alterations of the CSL gradient are due to particle breakage, bond
61 degradation or a combination of both. Different critical state lines for the same samples with
62 different cement contents are also reported by Cruz et al. (2011). The DEM results have shown
63 that alterations in the CSL are due to the breakage of the bonds and the generation of a different
64 grain size distribution, as some of the particles are still cemented together (Yu et al. 2014 and
65 Yu et al. 2015). The alteration of the CSL due to breakage was also investigated by Ghafghazi
66 et al. (2014), where they claimed that breakage causes a downward parallel shift in the CSL,
67 and according to Bandini and Coop (2011), large amounts of breakage are needed for
68 significant changes to occur.

69 In the majority of the research encountered so far, the samples were prepared using poorly
70 graded granular materials (sands of aeolian origin) or with lower densities; this was done in
71 order to accentuate the breakage or the improvement caused by the binding agent added. In a
72 couple of articles (Rios et al. 2014 and Consoli et al. 2014) well graded residual soils are
73 reinforced with cement, however some of them have fines and there is no attempt to measure
74 or determine the breakage.

75 When well graded soils are used the research tends to concentrate on the mechanical properties
76 of the material at small strains i.e. stiffness and strength up to peak, using multiple-step loading
77 triaxial tests (Kongsukprasert and Tatsuoka 2007 and Taheri et al. 2012). These tests have the
78 advantage of allowing the use of a single sample to cover a large range of stresses, however it
79 is unclear what the effect of damage to the cement bonds and particle breakage is from the
80 previous loading steps. Hence, the effect of the addition of cement on manmade materials used
81 for engineering purposes is not very well understood.

82 The purpose of this paper is then to study the effect of small levels of cementation on a very
83 dense fabric, created by compaction of a well graded granular material, under monotonic
84 loading, on commonly used soils. The improvement of the mechanical properties and examines
85 the effects of cementation within the Critical State framework is also explored.

86 **2 Material tested:**

87 The soil used in this research was a crushed limestone with 88% CaCO_3 , collected from a depot
88 in South London and is currently used commercially for the bases of roads in Southern
89 England. The soil was wet sieved and each particle size range was stored in separate bags. The
90 main properties of this material are summarised in Table 1, with the particle size distribution
91 (PSD) shown in Figure 1, together with the range defined by the UK Highways Agency (2016)
92 for a base and sub-base type.

93 The idealised grading curve proposed by Fuller and Thompson (1907) is based on the idea that
94 when larger particles are in contact with each other, larger voids are generated and occupied
95 by intermediate particles; this procedure is then followed to the smallest size available. The
96 idealised curve generates dense fabrics and was then used to correct the initial grading curve
97 of the soil, given that the particles are not spherical, it is argued that it then does not generate
98 the densest possible fabric. Given the sizes of the particles available, the PSD named “Adjusted
99 grading” (Figure 1) was used for all the tests. This curve follows the Fuller curve for the largest
100 sizes, and below the size 3.35mm it was translated downwards as not enough material was
101 available. For the same reason, sizes below 0.425 were chosen to make sure that all samples
102 would have the same grain size distribution and the grading within the Type 1, as defined by
103 the UK Highways Agency (2016) for a base and sub-base. As the triaxial equipment used is
104 capable to test samples up to 100mm diameter and 200mm high, the grain size distribution was
105 truncated at 20mm.

106 Cemented samples were created by adding Portland cement classified as CEM1, in accordance
107 to the British Standards (BS EN 197-1:2011). Given the high strength of the compacted
108 samples, only small percentages of cement (1 and 2%) were used to generate modest changes
109 in strength that could be tested in a triaxial equipment.

110 **3 Apparatus and sample preparation:**

111 A computer-controlled triaxial apparatus, with a local strain measurement system capable of
112 measuring 10^{-6} strain, similar to Cuccovillo and Coop (1997b), was used for the conventional
113 triaxial tests (Figure 2). The system uses RDP electronics LVDTs (model D6/05000) attached
114 to a modulator/demodulator (model S7DC) that allow the full configuration of the output
115 electric signal. At the beginning of the shearing, the local instruments are reset to zero to take
116 advantage of the 16-bit auto scale of the data logger. The volumetric strain was measured using
117 the volume gauge and the local instrumentation.

118 The desired amount of each fraction of soil was thoroughly mixed in a tray, with different
119 moisture contents, before being compacted in 5 layers, using 27 blows of a 5kg hammer falling
120 from a height of 450mm (BS 1377-4, 1990). A compaction curve for the uncemented soil was
121 determined in order to define the optimum moisture content. Given that the cemented and
122 uncemented samples were tested, a decision was made to compact all samples with a moisture
123 content of around 10%, providing enough water for cement hydration at the cost of a lower dry
124 density. Table 2 contains the properties of every sample tested.

125 After compaction, the uncemented samples were transported to the pedestal of the triaxial
126 equipment for testing. Suction maintained that the sample was intact before the confining
127 pressure was applied and the percolation procedure started.

128 The cemented samples were prepared with two different percentages of cement (45g for 1%
129 and 90g for 2% cement); where an equivalent mass was removed from the smallest grading of
130 the samples' PSD. The sample preparation followed a similar procedure to the one described
131 above, except that the cement and dry soil were thoroughly mixed together before adding the
132 same water amount, mixing was then continued until homogeneity was achieved. After
133 compaction the sample and mould were put inside of a plastic bag and allowed to cure for 24
134 hours. The sample was then placed inside of a tank with water at 22°C and allowed to cure,
135 submerged, for another 4 days. At day 5 the sample was removed from the tank, mounted on
136 the triaxial pedestal and prepared for testing. This procedure was followed to guarantee that
137 the cement could hydrate fully.

138 A volume in excess of 2000cc of water was percolated through the sample to remove air
139 bubbles. The pressure applied was around 18kPa, caused by the difference in height between a
140 water container located approximately 2m above the sample and the outlet from the pedestal.
141 The water coming from the sample was clear and the authors believe that no cement particles
142 were removed from the sample during percolation. The sample was then saturated, maintaining
143 an effective stress of 15 kPa. A B-parameter test was performed at different back pressures,
144 from 100 to 350 kPa on the first sample. Whilst it increased slightly up to 250kPa, the increases
145 at 300 and 350kPa were negligible (values measured were of the order of 0.86 to 0.92). It is
146 important to mention that the volume gauge only changed slightly during the increase in
147 pressures, being fairly constant once the required pressures were maintained. This indicated
148 that the sample was saturated and the B-parameters would not reach the required value.
149 Therefore, a minimum back pressure of 250kPa was used in all drained tests and monitored by
150 another transducer at the top of the sample.

151 In the consolidation stage the effective stress was raised to the value used in the test. This
152 procedure would take around 2 to 3 days before shearing; however, the cemented samples were
153 all sheared in a drained way at the end of day 7. Therefore, the consolidation stage was extended
154 even if the volume change was negligible.

155 During drained shearing a constant confining pressure was maintained throughout the test. The
156 sample was sheared at a constant rate of strain of 0.016mm/min, this was determined based on
157 the capacity of the data acquisition system to interpret strains of 10^{-6} . Well after peak strength,
158 the speed was doubled until the test was terminated. Tests were terminated either by achieving
159 a constant strength and a constant volume, or by reaching an axial strain of 30%.

160 The moisture content was determined by using left over soil from the tray, and the initial void
161 ratio of each sample was calculated in five different ways: an average of the initial dimensions,
162 the volume of voids and solids, the dry unit weight and the final water content. Outliers were
163 removed and an average of the values deemed acceptable was used. Although the samples were
164 carefully prepared, a variation in the initial void ratio was unavoidable (Table 2).

165

166 **4 Breakage:**

167 The idea of having a balance between particle breakage and particle rearrangement at critical
168 state has been reported by many authors [(Chandler 1985, Daouadji et al. 2001, Coop et al. 2004,
169 Salim and Indraratna 2004, Muir Wood and Maeda 2008 and Rubin and Einav 2011). The literature
170 review has also shown that the level of breakage in dense granular materials, at lower pressures,
171 is rarely investigated. It is often disregarded and assumed not to affect critical state, particularly
172 when a large number of contacts is expected. Therefore, samples were sieved to evaluate

173 breakage after shearing, whilst extra samples were prepared to determine if compaction caused
174 particle breakage (Figure 3).

175 The results showed that after compaction small amounts of breakage can be seen in all sizes.
176 Breakage was also seen after shearing, where the largest changes in PSD were seen in sizes
177 ranging from 1 to 7mm, where the increase in passing percentage is in the order of 8%. The
178 smaller sizes have also increased, perhaps indicating the shearing of the asperities at the small
179 confining stresses used.

180 An attempt to determine the PSD for the cemented samples was carried out by breaking the
181 cement bonds before sieving, samples were put on individual sealed bags and the bonding
182 destroyed by hand. Larger pieces that were kept intact were removed by hand, and only the soil
183 that seemed not to have bonds was used. The results showed that the PSD curve of sample M-
184 2%-200 is slightly above the original curve for sizes above 3mm and below the original curve
185 for sizes below 3mm; whilst the M-2%-20 is below the original size tested (Figure 3). This
186 demonstrates the effect of the confining stress on the destruction of the bonds and the difficulty
187 to destroy by hand, the bonds on the smallest sizes, even after a monotonic shearing has taken
188 place.

189 **5 Triaxial tests (stress-strain behaviour)**

190 The triaxial test results are shown on Figure 4, where the stress-strain and the volumetric curves
191 of 15 tests are plotted. As expected, all samples showed a strain-softening behaviour towards
192 a constant strength after peak stress. The volumetric behaviour is similar; after a large dilation
193 that reduces with the confining stress, it is possible to visualise a steady state, where no change
194 in volume and strength is seen with the increase in shear strain. Large volumetric strains are
195 also seen particularly at low stresses, where there are sharp changes in the volumetric

196 behaviour, possibly indicating the occurrence of localisation. However, all samples have failed
197 in barrelling and only in a few samples signs of localisation were noticed. A couple of tests
198 were terminated earlier, due to small punctures on the membrane given the large strains. The
199 axial strain, ϵ_a , was measured by two local displacement transducers up to a certain point
200 (usually peak stress) switching to the external transducer afterwards.

201 The effect of the addition of cement in the strength is clear, as the peak values increase with
202 the addition of cement for all confining stresses tested. Simultaneously, there is also an increase
203 in the brittleness index (the ratio between the peak shear strength and the shear strength at large
204 strains) of the samples. Figure 5 shows the brittleness index calculated for all of the samples.
205 The samples with 2% cement have a much larger brittleness index when compared to the other
206 samples. It is also clear that the values of brittleness index calculated for the 1% cement
207 samples have little deviation from the 0% samples; i.e., the addition of 1% cement causes small
208 changes to this parameter.

209 The results also show that increasing the cement content reduces the level of strain required to
210 reach the peak stress. This is true for every confining stress tested, confirming that there is an
211 increase in stiffness with the addition of cement. Figure 6 shows a direct comparison between
212 the cemented and uncemented samples for certain confining stresses, to better show the effect
213 of cementation in the peak shear strength and the volumetric behaviour, where higher cement
214 content generates larger dilative volumetric strains. For the uncemented soil, the area
215 correspondent to the maximum rate of dilation directly corresponds to the peak strength, whilst
216 the cemented samples experience peak slightly before the maximum rate of dilation. The
217 change seen is not large, but enough to demonstrate that small additions of cement can generate
218 a structure that affect the strength of even very dense fabrics, as shown in Figure 7.

219 Figure 8 shows the tangent stiffness curves (slope of the stress-strain curves) with arrows
220 indicating the points where a change in shearing rate was performed to accelerate the tests. The
221 gross yield points, regarded as the onset of bonding degradation and the locus where significant
222 plastic deformations start to occur, are also indicated in the curves with the use of a black
223 square. These were determined using the method proposed by Malandraki and Toll (1996) and
224 Alvarado et al. (2012b) and are marked by the start of the change in direction of the stiffness
225 curve. It is clear that the addition of cement increases the tangent stiffness; the tangent stiffness
226 of the uncemented samples start at values lower than 1GPa, whilst the samples with 1% cement
227 start at values lower than 2 to 3GPa, and the samples with 2% show values lower than 7 or
228 8GPa. It can also be seen that increasing the strain reduces the tangent stiffness and that the
229 rate of reduction in stiffness is related to the percentage of cement (i.e. lower cement
230 percentages lower reductions and higher cement percentages higher reductions). Comparing
231 tests in each group, it is also seen that increasing the confining pressure also results in higher
232 stiffnesses, despite the fact that in certain samples this is not very clear and it is likely to be the
233 effect of the scales used in the graph.

234 **5.1 Stress-Dilatancy:**

235 A stress-dilatancy analysis was performed and Figure 9 contains the plots of all 15 uncemented
236 and cemented samples, shown with the respective cement percentage. On each graph, the peak
237 strength, the gross yield and last test point are represented by different symbols. The
238 uncemented samples show an increase in the ratio q/p' with dilation, up to a peak, reached at
239 the same time as the highest dilation rate. From that point onwards, dilation rate reduces
240 together with the q/p' ratio. As the volume stops changing, a unique value of $M= 1.76$ can be
241 determined, corresponding to a friction angle at critical state $\phi'_{cs}=43^\circ$.

242 The effect of the cement percentage can be seen by the initial change in the shape of the curve.
243 At the start of shearing, as dilation develops, the samples quickly reach higher ratios of q/p' ,
244 indicating that the cementation is now active and allowing a stiffer response from the sample.
245 This difference is proportional to the cement percentage; i.e., the higher cement percentage, the
246 higher the ratio q/p' . The effects of cementation are also visible in the location of the peak
247 stress, as it occurs before the maximum rate of dilation; this is similar to what was observed
248 previously in Figure 7 and described by Leroueil and Vaughan (1990). However, the difference
249 between the ratio q/p' , measured at the peak stress and at the maximum rate of dilation is very
250 small, indicating that the peak is largely governed by dilation rather than by cement content.
251 The samples with 1% cement do not show this as clearly as the samples with 2% cement.
252 Another expected behaviour is the reduction in dilation rate with the confining stress, seen in
253 all cement and uncemented samples, similar to the behaviour of cemented sands, demonstrated
254 by Coop and Wilson (2003), Consoli et al. (2012) and Alvarado et al. (2012b).

255 The same authors have pointed out that after the maximum dilation rate the samples seem to
256 follow a linear frictional trend, however, as the stress ratio reduces, the dilation rate seems to
257 reduce much quicker, i.e. volumetric strains change at a larger rate, and the path moves inwards
258 and away from the frictional trend. The authors attribute this behaviour to the occurrence of
259 localisation and the rapid reduction of volumetric strains. In the case of the samples tested here,
260 a similar behaviour was observed after peak, however, as the shearing continues this trend is
261 reversed and the samples seem to converge to a unique value of M : $M=2.00$ for 1% cement and
262 $M=2.05$ for 2 % cement. As can be seen in Figures 9b and 9c, if the linear trend line is followed,
263 a higher value of M is determined for the same percentages of cement, whilst in the case of
264 Coop and Wilson (2003), a lower value would be defined.

265 The work done by Muhlhaus and Vardoulakis (1987) and Finno et al (1997), show that the
266 thickness of the shear band is proportional to the particle size distribution. Authors mention
267 values of 16 and 10 to 25 times d_{50} respectively. Given that the triaxial sample has a finite
268 volume this implies that the volumetric strains measured in a triaxial sample are a function of
269 the grain size distribution. Therefore, variations in the grain size distribution during shear, will
270 cause large changes in the dilation ratio. The samples tested are lightly cemented and the grain
271 size distribution curve obtained after shearing, shows that the final grading has larger
272 intermediate particles than the original grading. This indicates that there is an evolution of the
273 particle size distribution during the shearing process. The DEM work done by Wang and Leung
274 [4-5], clearly shows that despite the shearing, there are still clusters of particles that remain
275 intact within the sample. The authors, therefore, believe that as bonds degrade due to shearing
276 there is a constant change in the particle size distribution. The consequence are seen as different
277 volumetric strain rates that bring the dilation path inwards. As shearing continues, a more stable
278 grading is achieved and a different value of M is reached at critical state.

279 **6 Critical state:**

280 The points correspondent to the peak strength and the end of tests were plotted in Figure 10,
281 together with the results obtained from the Indirect Tensile tests (ITS) (BS EN 13286-42:2003),
282 as well as Unconfined Compressive tests (UCS) (BS EN 13286-41:2003), on samples of the same
283 size, prepared using the same methodology. These samples are not shown on Table 2 but fall
284 within the same average values. These results served to plot the peak envelopes, as the
285 cemented samples have a small tensile strength and it must be considered when defining the
286 peak envelopes of the cemented soils. The failure envelopes plotted suggest values of M that
287 are very similar to the values determined in the dilation plots above. Figure 10b shows the
288 small stress area with more detail. It is also important to point out that the peak envelope for

289 the uncemented soil is curved and seems to join the CSL at p' of around 1100 kPa. The
290 properties of the strength envelopes are shown on Table 3, where the peak friction angle for
291 the uncemented soil was calculated assuming no cohesion.

292 Been et al. (1991) have shown that within the normal range of engineering stresses, sands show
293 a steady state line at small stresses that is much shallower than at high stresses. Therefore, the
294 paths followed by the tested samples were plotted on the specific volume, $\ln p'$ space on
295 Figure 11, with the final point of each test indicated by a symbol. Although the arrows indicate
296 the direction the tests were following when they were terminated, Figure 4 shows that the
297 magnitude of this movement was very small for most of the tests. The results show that there
298 is no unique CSL for the cemented and uncemented soils. Instead, the results point clearly to
299 the location of three distinct CSLs, one for each type of soil tested. The results also show that
300 the addition of cement increases the slope of the CSL when compared to the uncemented soil.
301 The larger dilative behaviour seen in the cemented samples is responsible for the steeper curve
302 gradient shown by the cemented samples. A summary of the parameters obtained for the steady
303 state lines in Figure 11 is shown in Table 3.

304 The steady state lines determined for the cemented soils seem to reach a common point at
305 stresses of around $p'=1000\text{kPa}$. This is compatible with the results shown by the grain size
306 distribution curves, where the PSD of cemented samples sheared at large stresses is very similar
307 to the PSD of the uncemented or original grain size distribution. As the percentages of cement
308 content used in this research were very small, the effect on the strength of the samples is likely
309 to be felt only at small stresses. At larger confining stresses, the resultant frictional strength
310 mobilised is much larger than the contribution of the cement. At that point the changes in the
311 critical state lines caused by the cementation are very small.

312 **6.1 Normalised behaviour:**

313 Given that the stresses used to consolidate the samples were very low and it was not possible
314 to determine a Normal Compression Line (NCL), each set of tests was normalised with respect
315 to M and the equivalent pressure on the CSL, by using Equation 1 (λ is the slope of the CSL,
316 Γ is the specific volume at $p'=1\text{kPa}$ and v is the specific volume, on the CSL and p'_{cs} is the
317 mean effective stress on the CSL):

$$318 \quad p'_{cs} = \exp\left(\frac{\Gamma-v}{\lambda}\right) \quad \text{Eq.1}$$

319 The normalised stress paths show that it is possible to determine a state boundary surface for
320 the peak states for each set of test up to the critical state line (broken line on Figure 12). The
321 normalised gross yield points determined from the stiffness curves for each set of tests was also
322 plotted in Figure 11. The gross yield envelopes are fully enclosed within the respective SBSs
323 indicating that the cement percentages generated a very weak bonding. At low stresses, the
324 yield surface seems to coincide with the SBS, however, as the stresses increase the yield surface
325 moves inside and away from the SBS. The effect of the cement percentage is seen in the
326 proximity between the gross yielding surface and the SBS, as the larger cement content keeps
327 the yield surface closer to the SBS.

328 In Figure 13 all the state boundaries and yield surfaces were plotted together. The results show
329 that these are very similar, and a unique SBS could be used to represent the effect of the
330 cemented and uncemented tests, when normalised by the CSL and the value of M. The gross
331 yield surface of the uncemented and the 1% cement are coincident, however, a unique surface
332 cannot be assumed as the 2% cement results have shown a significantly higher gross yield
333 surface.

334 **7 Conclusions**

335 This work presents the findings of a study conducted in cemented and uncemented samples of a well
336 graded compacted granular material, used for base and sub-base construction in the UK. The following
337 conclusions can be drawn from this work:

- 338 • The mechanical properties of a well graded compacted granular material traditionally used in
339 construction, can be further improved with the addition of small percentages of cement.
- 340 • The addition of cement also increases the dilative tendency of these soils, providing better
341 results particularly when small confining stresses are used as is the case of base and sub-base
342 for road construction.
- 343 • The results show that it is possible to determine a unique Critical state line for the uncemented
344 material and that the addition of cement will increase the slope of this line within the range of
345 stresses commonly observed in engineering practice.
- 346 • When the data is normalised by the equivalent pressure on the CSL and the value of M , it is
347 possible to determine a unique state boundary surface for the cemented and uncemented soils
348 used in this research. The gross yield surface, however, is not unique and will depend on the
349 cement percentage.

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458

Table 1- The index properties of research material from dry sieving

Description	Crushed Limestone
Max Density- Vibrating Hammer (g/cm ³)	2.24
Max void ratio	0.83
Min Density (gr/cm ³)	1.51
Min void ratio	0.23
Particle Density (gr/cm ³)	2.76
Max Dry Density-Automatic Heavy Compaction (gr/cm ³)	2.24
Optimum water Content (Modified Proctor)	6%
Type of soil	GW
D ₁₀ (mm)	0.2
D ₃₀ (mm)	1.5
D ₅₀ (mm)	3
D ₆₀ (mm)	4
Uniformity Coefficient $C_u = \frac{D_{60}}{D_{10}}$	20
Curvature Coefficient- $C_c = \frac{D_{30}^2}{D_{10} \times D_{60}}$	2.8

462 Table 2- Properties of the samples tested: the name indicates the cement percentage and the
 463 confining stress used during shearing

Test Name	W ₀ (%)	e ₀ *	e _{con} **	γ _{Dry} (g/cm ³)	q _{max} (kPa)
M-0%-020	9.61	0.379	0.378	1.952	301
M-0%-050	8.63	0.376	0.370	1.961	482
M-0%-100	9.66	0.417	0.405	1.938	804
M-0%-200	10.03	0.404	0.388	1.978	1177
M-0%-400	9.71	0.400	0.374	1.973	2067
M-1%-050	9.59	0.397	0.392	1.958	941
M-1%-100	8.44	0.367	0.357	1.974	1219
M-1%-200	8.72	0.392	0.364	1.968	1910
M-1%-300	9.83	0.410	0.381	1.943	2247
M-1%-400	9.03	0.393	0.350	1.965	2755
M-2%-020	9.21	0.380	0.380	1.961	809
M-2%-050	8.74	0.388	0.383	1.960	1359
M-2%-100	8.61	0.371	0.361	1.972	1656
M-2%-200	9.04	0.396	0.380	1.951	2157
M-2%-300	8.67	0.388	0.360	1.973	2718

464 *: e₀ – initial void ratio, **: e_{con} is the void ratio after consolidation, before shearing.

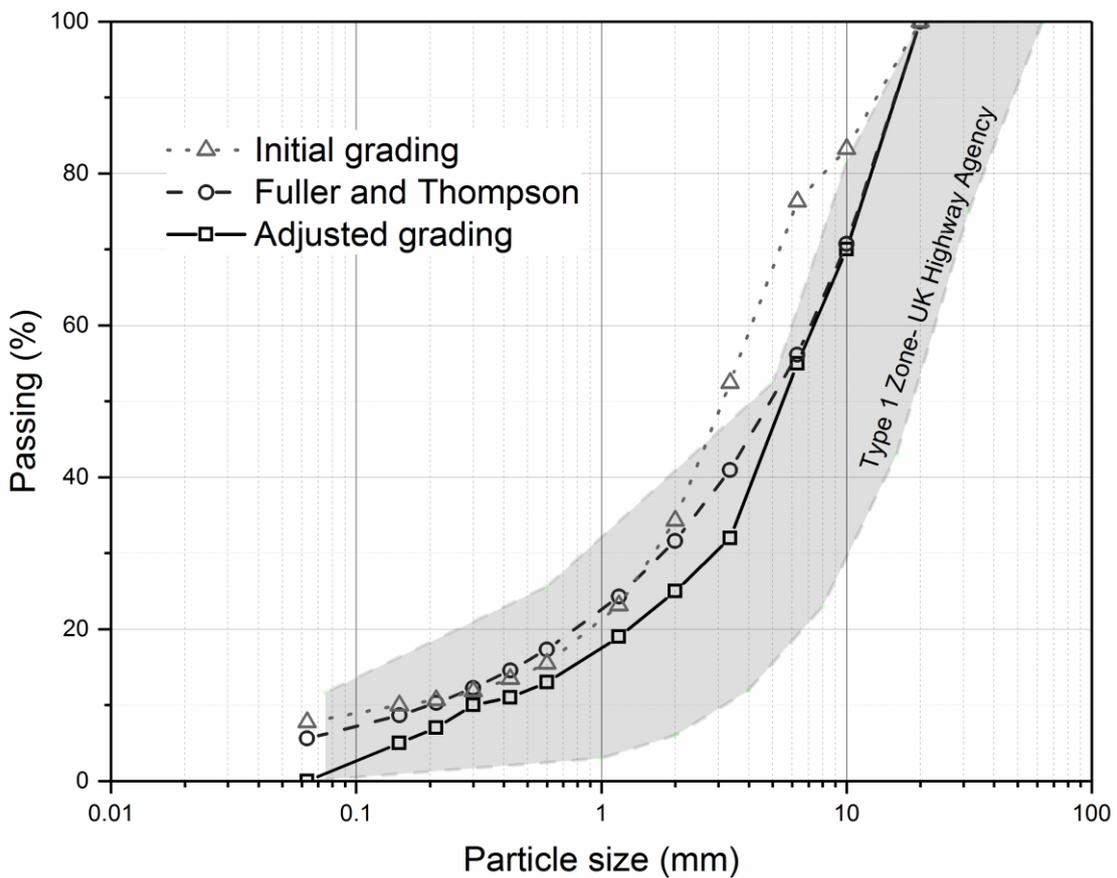
465

Table 3- Specification of peak and critical state line

Type of crushed limestone	Critical state				Peak		
	λ	Γ	M	ϕ'_{cs} (°)	q/p'	q Intercept	ϕ'_p (°)
Uncemented	0.053	1.747	1.77	43.1	1.81	0	46.6°
1% cement	0.101	2.054	2.00	48.6	1.90	265	45.9°
2% cement	0.122	2.218	2.05	49.8	2.03	299	46.7°

467

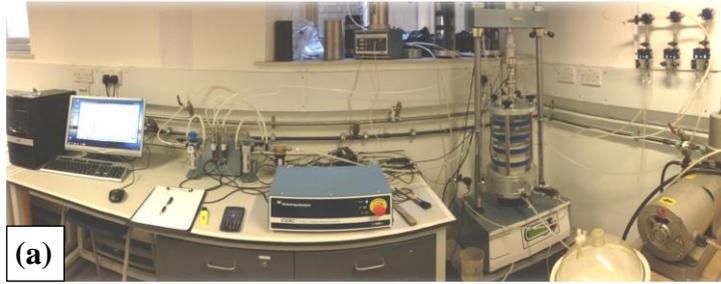
468 Figures:



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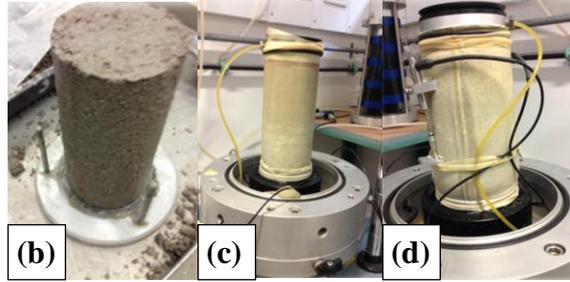
470 **Fig. 1** Particle size distributions: Initial grading; Fuller and Thompson (1907) and the Adjusted
 471 grading. The grey band defines the range of type 1 (UK Highway Agency 2016)

472



(a)

473



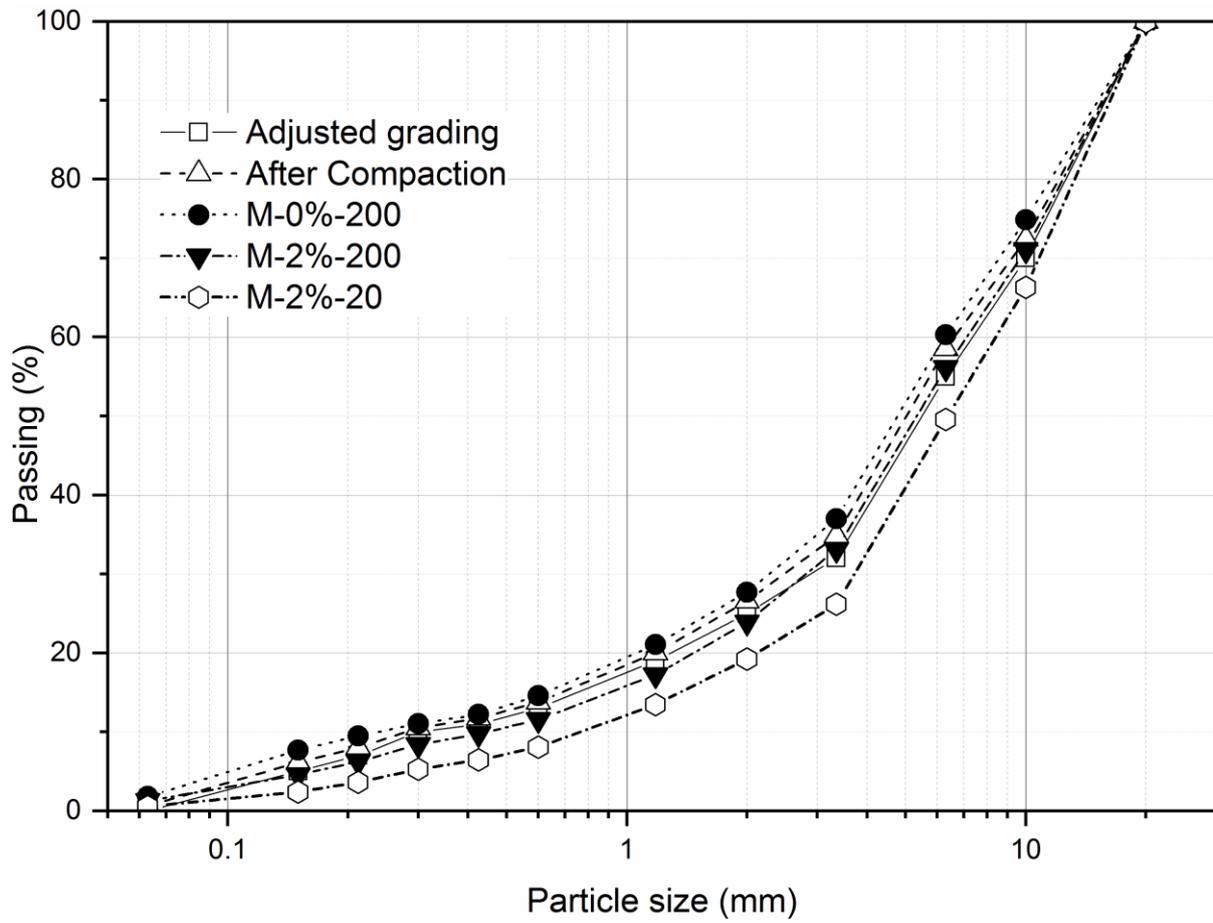
(b)

(c)

(d)

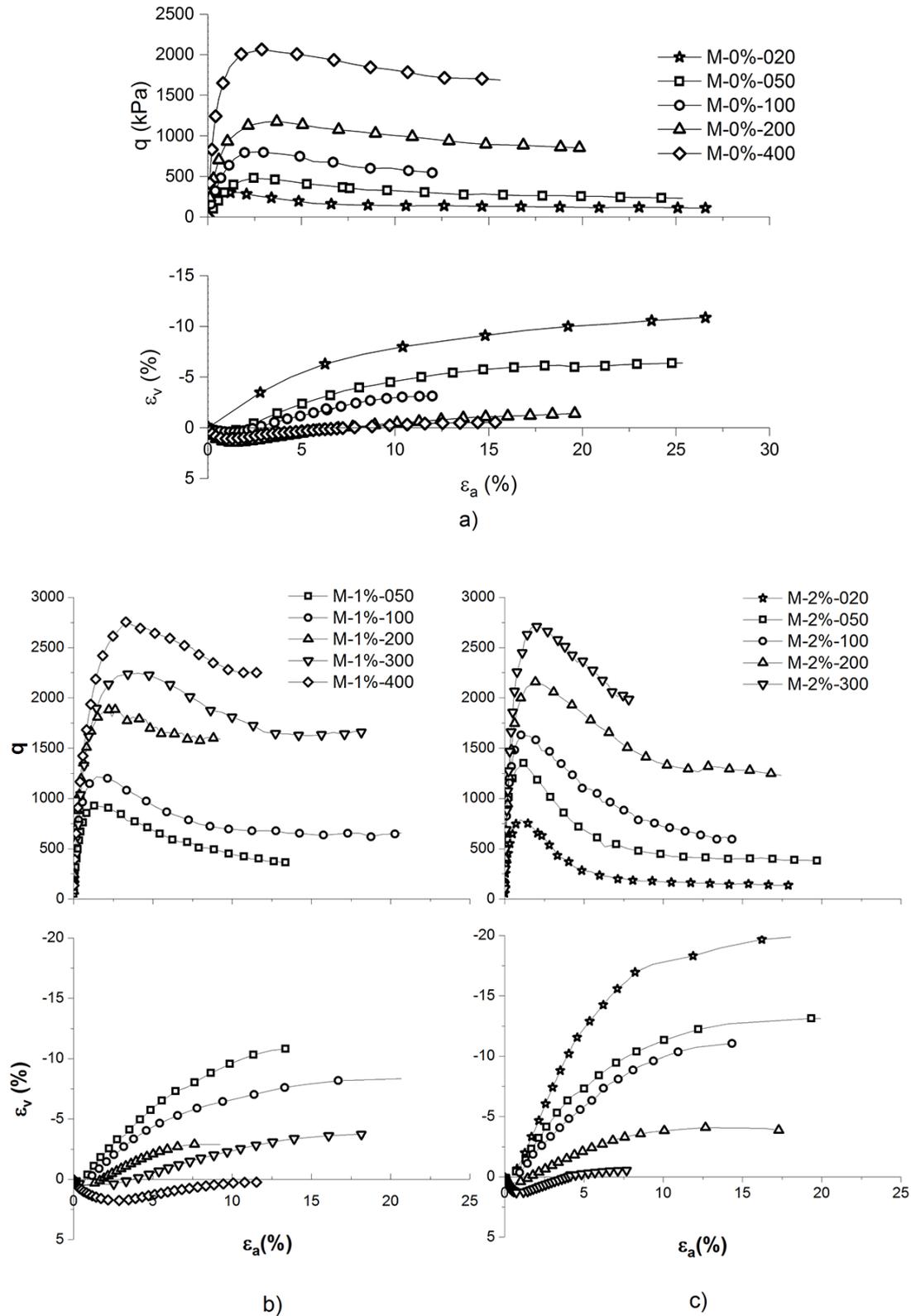
474 **Fig 2** Picture of the equipment and samples: a) triaxial equipment in the lab; b) compacted
475 sample in the pedestal and sample with local instrumentation before closing the triaxial
476 chamber.

477



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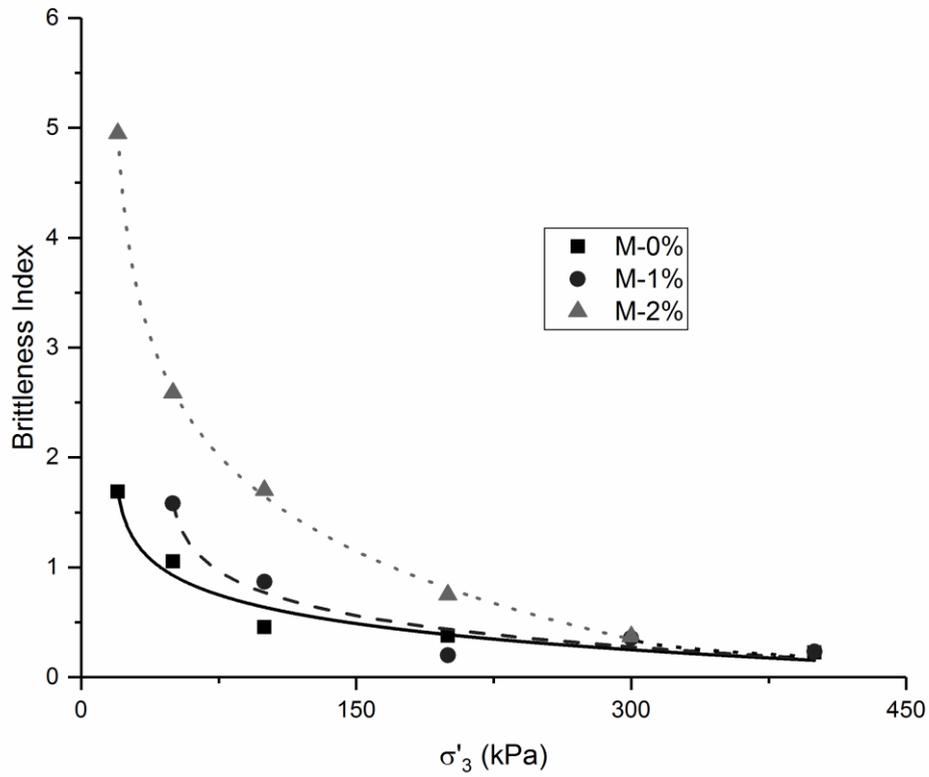
479 **Fig 3** Particle size distributions of the samples: original and after the compaction and
480 monotonic shearing.



481

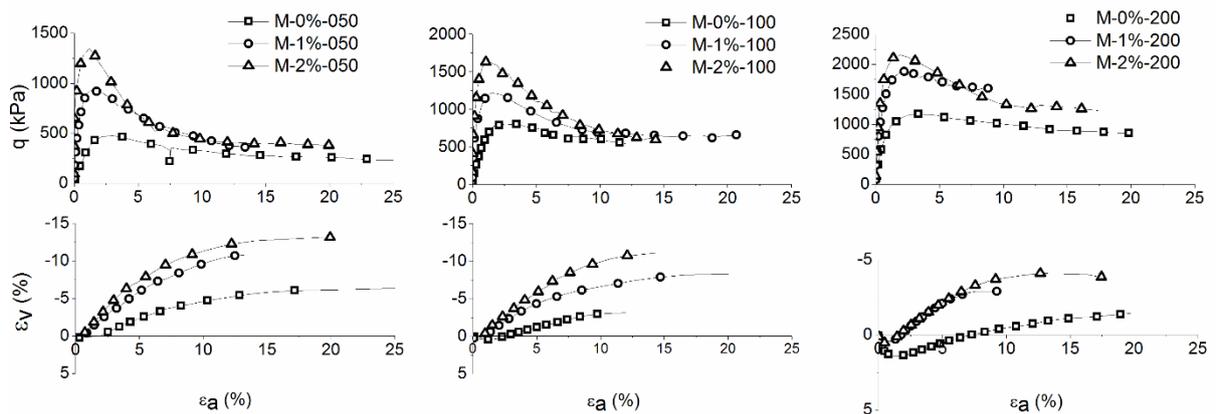
482 **Fig 4** Stress-strain and volumetric response of the soils tested with: a) 0%, b) 1% and c) 2%

483 cement content



484

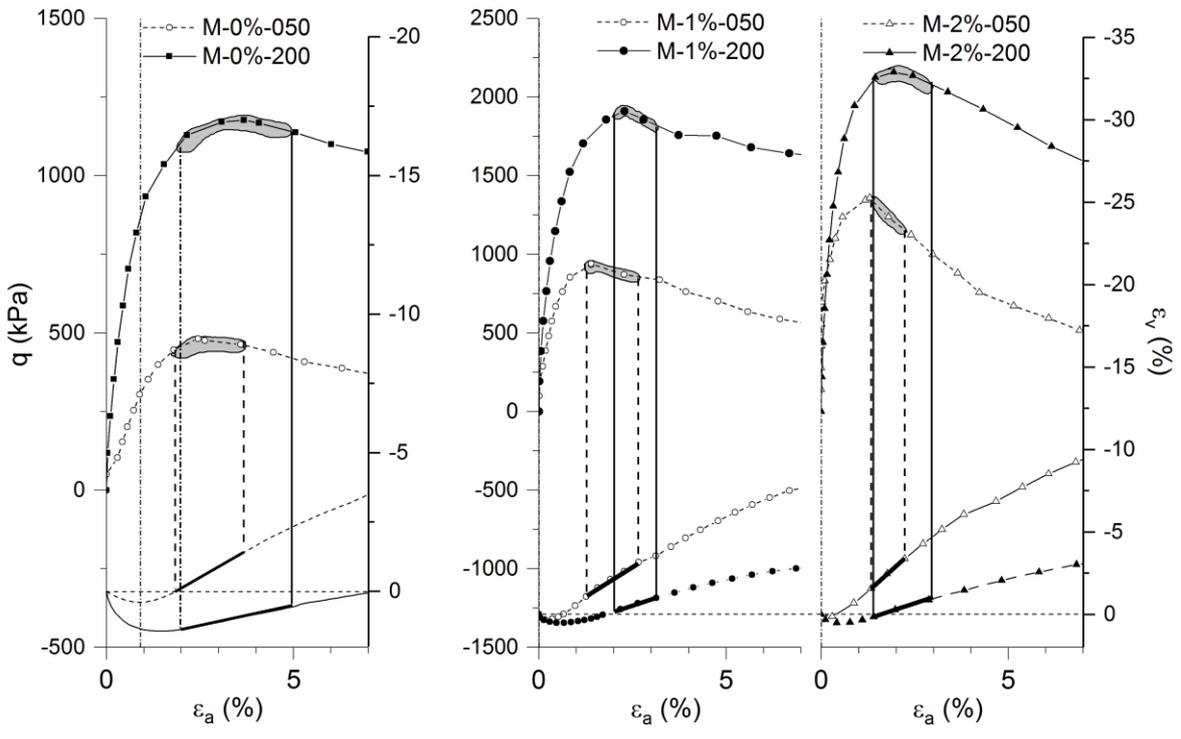
485 **Fig 5** The relationship between brittleness index and confining pressure.



486

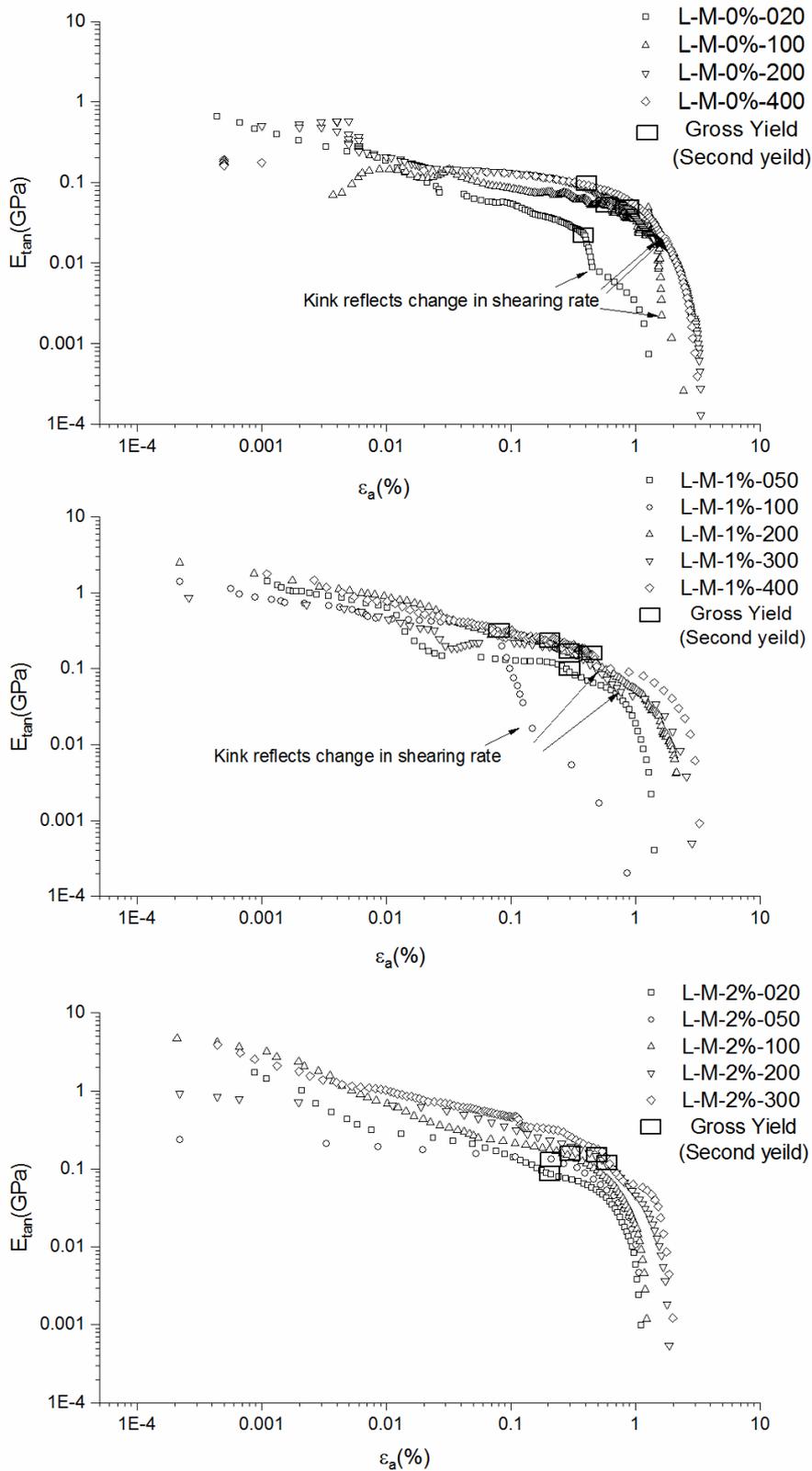
487 **Fig 6** Comparison of the stress-strain and volumetric responses of the samples with 0%, 1%

488 and 2% cement, under different confining pressures.



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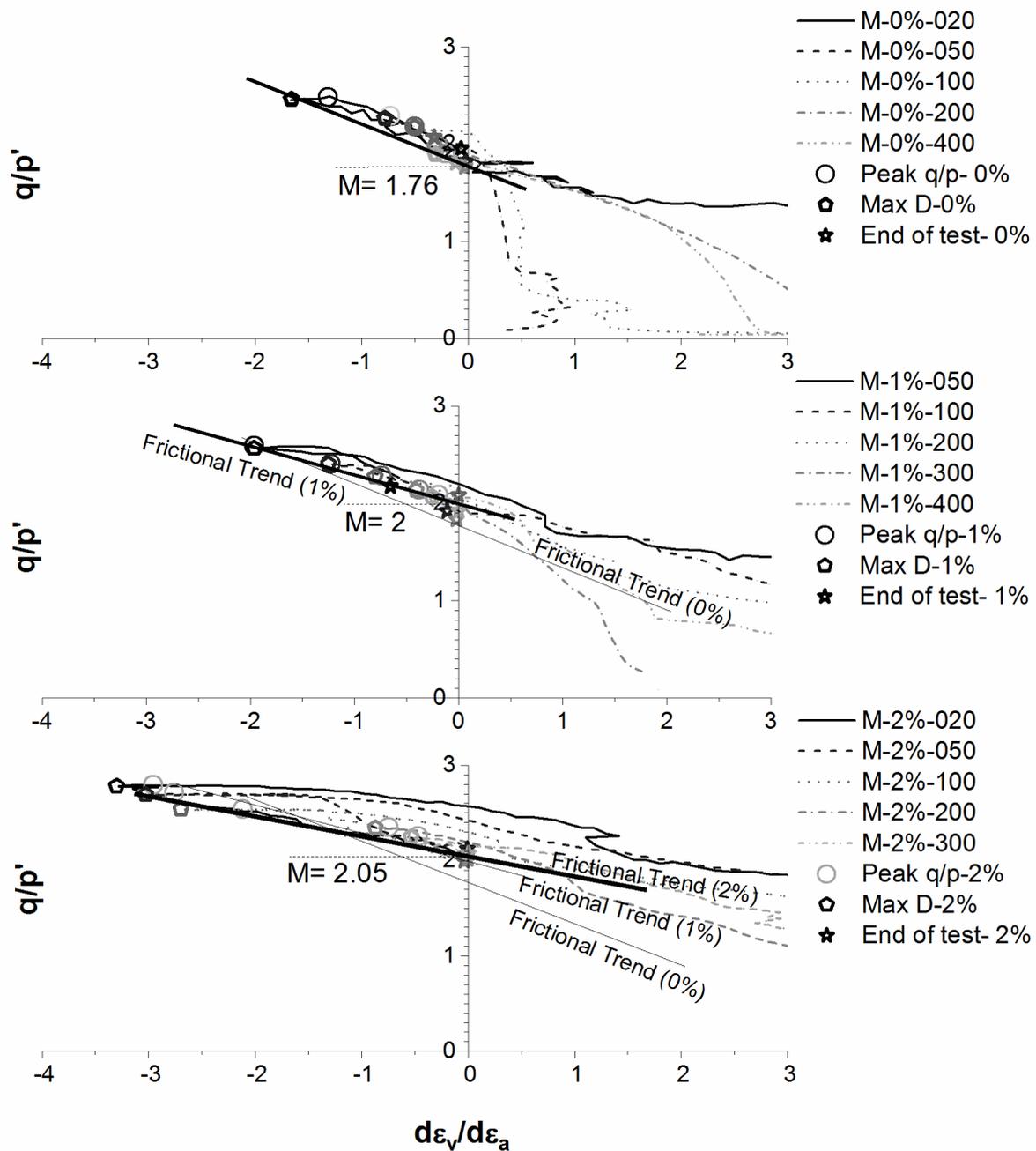
490 **Fig 7** Relationship between peak stress and maximum rate of dilation for 50 and 200kPa
 491 confining stress: 0% cement on the left; 1% in the middle and 2% on the right.



492

493 **Fig 8** Tangent stiffness against axial strain in log scale, together with the gross yield points for:

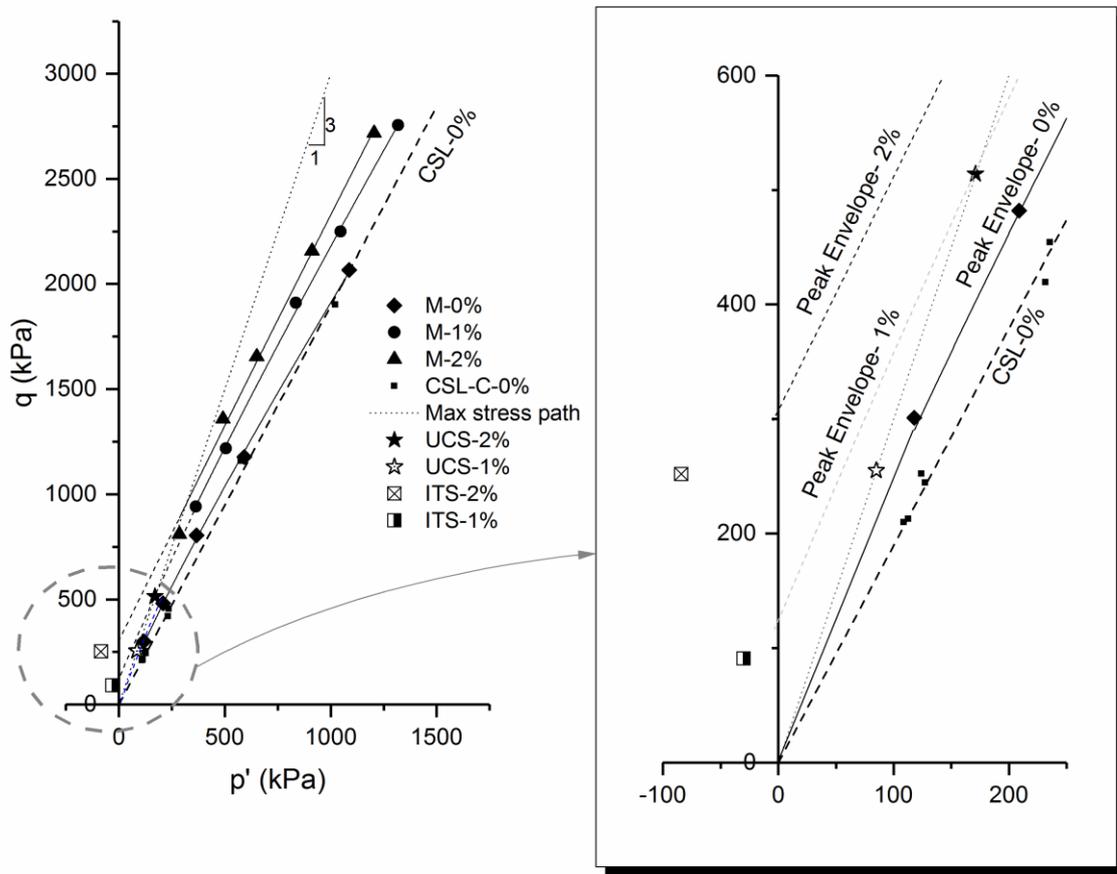
494 a) 0%, b) 1% and c) 2% cement



496

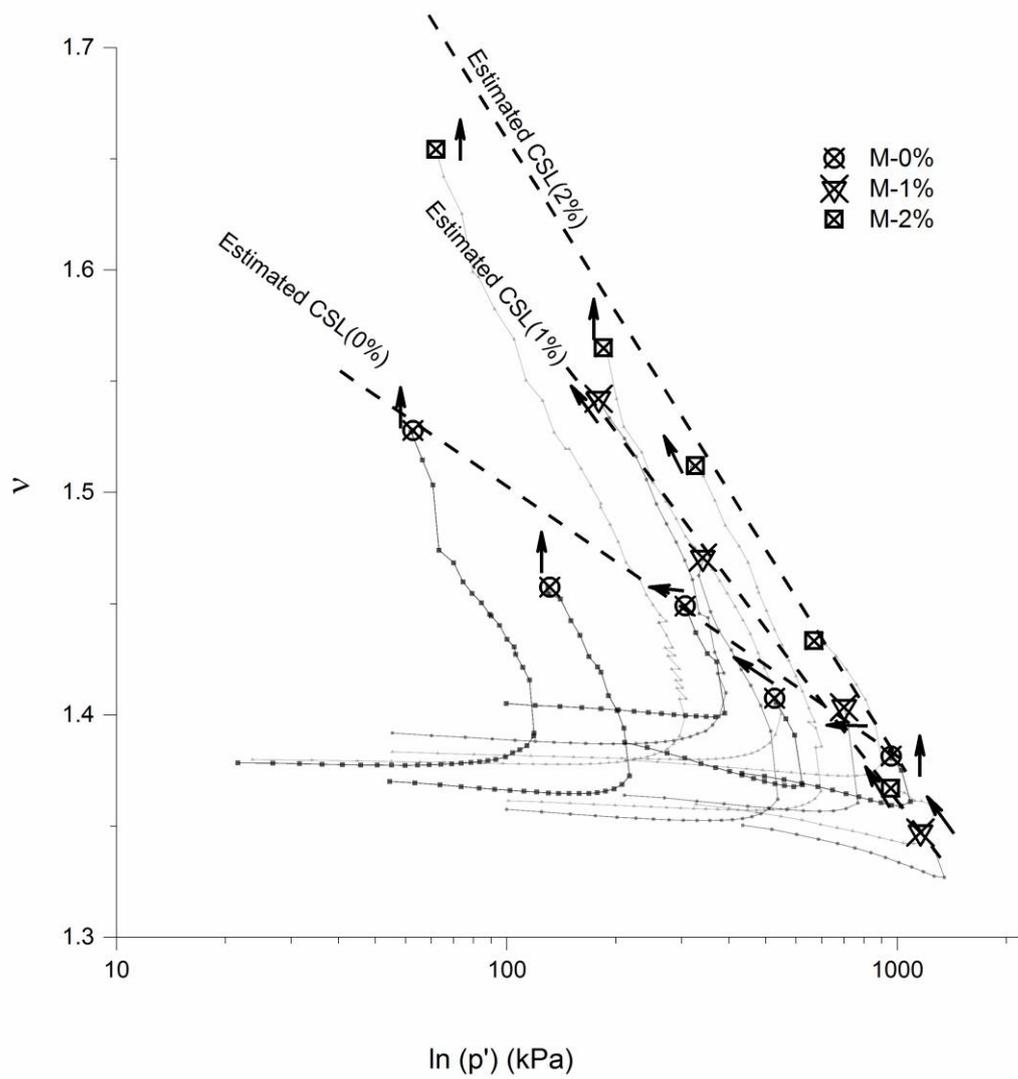
497 **Fig 9** Stress-dilatancy analysis: a) 0%, b) 1% and c) and 2% cement content

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499

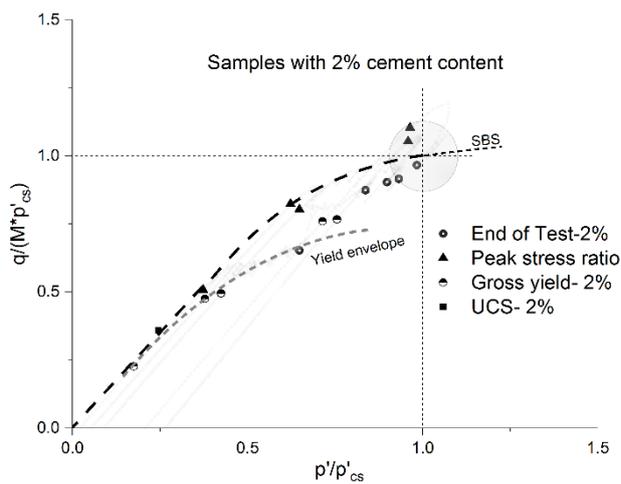
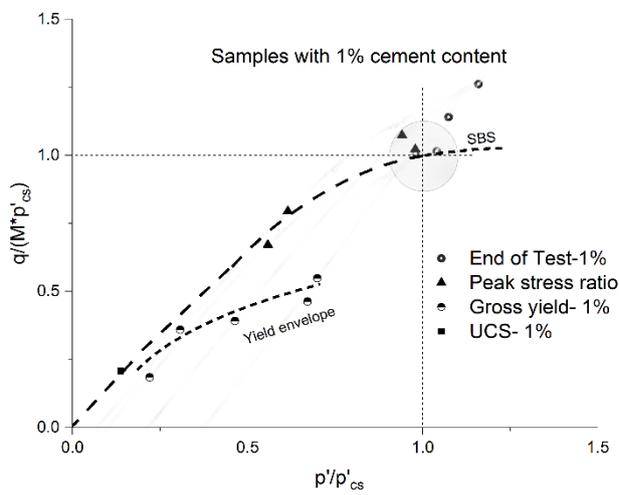
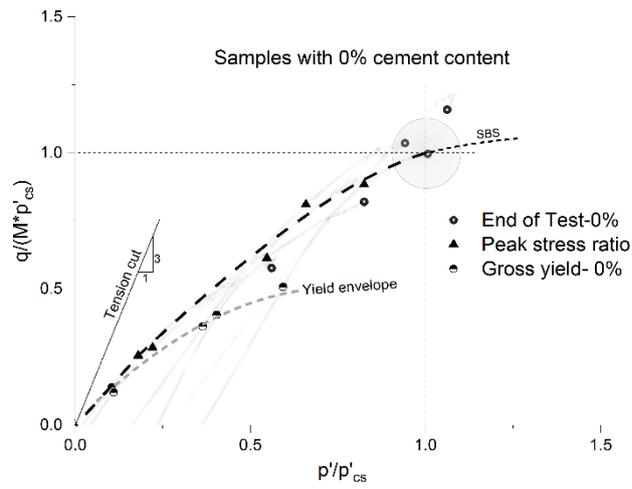
500 **Fig 10** Peak envelop on q versus p' diagram; the inset shows the small stresses region



501

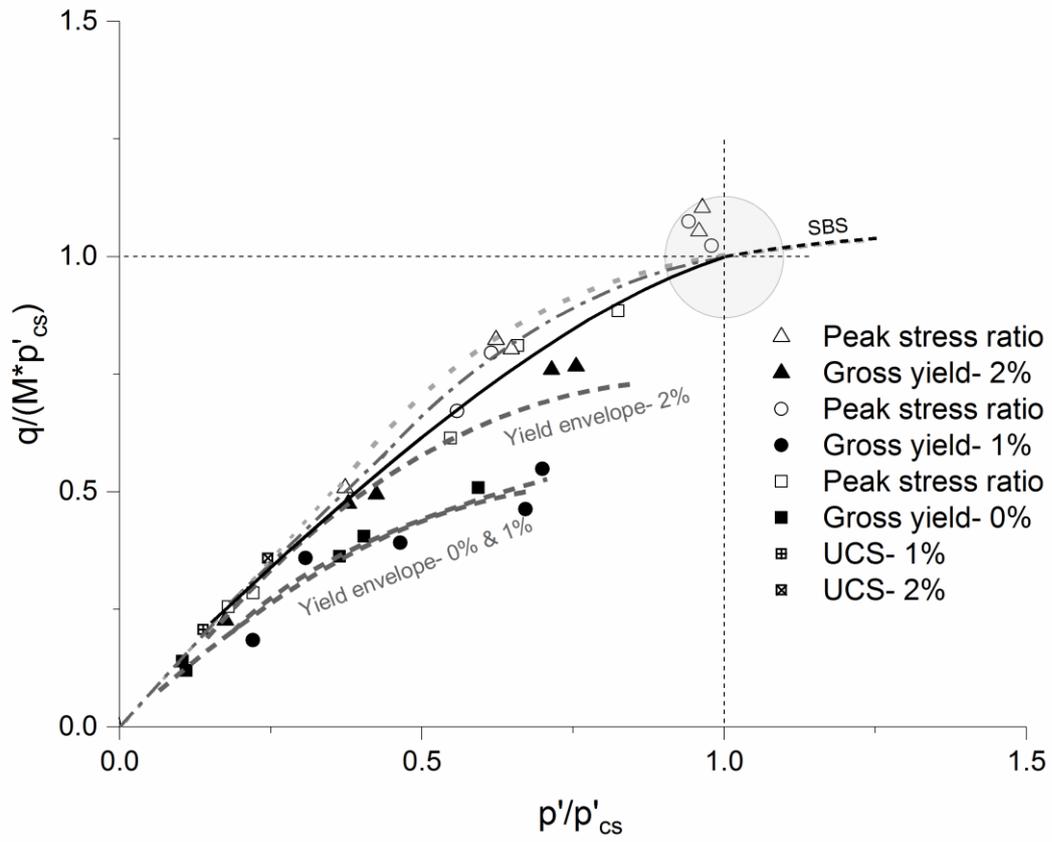
502 **Fig 11** Location of critical state lines for samples with 0%, 1% and 2% cement content on the
 503 specific volume, v , versus the logarithm of the mean effective stress, $\ln(p')$.

504



505

506 **Fig 12** Normalised yield and strength envelopes: a) 0%, b) 1% and c) 2% cement



508

509 **Fig 13** Comparison of the normalized data for the uncemented and cemented soils

510