

1 **An overview of modelling craniosynostosis using finite element**
2 **method**

3
4 Oyvind Malde¹, Joseph Libby², Mehran Moazen¹

5 ¹UCL Mechanical Engineering, University College London, London WC1E 7JE, UK

6 ²School of Engineering and Computer Science, University of Hull, Hull, HU6 7RX, UK,
7

8 Corresponding author:

9 Mehran Moazen, BSc, PhD, CEng

10 Email: m.moazen@ucl.ac.uk; mehran_moazen@yahoo.com
11

12
13
14 **Abstract:**

15 Craniosynostosis is a medical condition caused by the early fusion of the cranial joint. Finite
16 element method is a computational technique that can answer a variety of “what if” questions
17 in relation to the biomechanics of this condition. The aim of the paper was to review the current
18 literature that has used finite element method to investigate the biomechanics of any aspect
19 of craniosynostosis being its development or its reconstruction. This review highlighted that a
20 relatively small number of studies (n=10) have used finite element method to investigate the
21 biomechanics of craniosynostosis. Current studies set a good foundation for future studies to
22 take advantage of this method and optimize reconstruction of various forms of
23 craniosynostosis.
24

25
26
27 **Keywords:** biomechanics, skull growth, finite element, model validation
28
29
30
31
32
33
34
35
36
37
38
39
40

41

1- Introduction

42 During the early years of life, human brain volume increases rapidly and the cranium
43 undergoes rapid morphological changes in both size and shape (Dekaban, 1977; Scheuer and
44 Black 2004; Abbott et al., 2010). The neurocranium in particular is required to expand to
45 provide protection for the brain (Morriss-Kay and Wilkie, 2005; Richtsmeier and Flaherty,
46 2013). This is accommodated by the cranial joints i.e. sutures (Opperman, 2000; Herring,
47 2008). Premature closure of the sutures, or craniosynostosis, is a medical condition that
48 occurs in about 1 in 2,000 births with several reports of increase in its occurrence (van der
49 Meulen et al., 2009; Johnson and Wilkie, 2011; Cornelissen et al., 2016; Al-Rekabi et al.,
50 2017). The majority of cases (70%) are non-syndromic i.e. single suture synostosis, with the
51 remaining instances being syndromic (e.g. Crouzon and Apert), in which more than one suture
52 fuses and where additional features are present such as midfacial hypoplasia (Morriss-Kay
53 and Wilkie, 2005; Wilkie et al., 2017).

54 Current treatments of this condition in the majority of cases involve invasive surgery where a
55 multidisciplinary working group of plastic and reconstructive surgeons, neurosurgeons,
56 anaesthetist, maxillofacial surgeons and orthodontists correct this craniofacial deformity. This
57 group is also supported by a larger team of experts in psychology, speech and language
58 therapy and genetics (Mathijssen, 2015). The underlying aim of the surgery is to release the
59 pressure on the growing brain and provide the required space for it to grow while the overlying
60 complex of bones and sutures form a protective shell. At the same time there are a large
61 number of patient-specific factors that need to be considered during the course of
62 craniosynostosis treatment such as age and intracranial pressure. There are a number of
63 reconstruction techniques for different forms of craniosynostosis. These techniques have
64 generally evolved over years in each craniofacial centre due to their experience, while
65 ensuring the best surgical outcome for the child (e.g. McCarthy et al., 1995; Clayman et al.,
66 2007; Thomas et al., 2015). Nonetheless, when comparing different centres' techniques for
67 treatment of a single form of craniosynostosis there could be huge variations between them
68 (e.g. Hopper et al., 2002; Taylor and Maugans, 2011; Simpson et al., 2017). For example, in
69 the case of sagittal synostosis which is the most common form of craniosynostosis (Wilkie et
70 al., 2017), there are a number of different techniques used. These range from newer
71 techniques such as: minimally invasive endoscopic strip craniotomy with helmeting or spring-
72 mediated cranioplasty, to other invasive calvarial reconstruction techniques such as Pi and
73 modified Pi techniques, H technique or total cranial vault remodelling (e.g. Jimenez and
74 Barone, 2013; Gerety et al., 2015; Simpson et al., 2017).

75

76 Calvarial reconstruction in craniosynostosis can be optimized using various computational
77 tools. Finite element method (FEM) is a well-established tool that has been widely used to
78 design, develop and optimize various mechanical structures such as aeroplanes and bridges
79 (e.g. Fagan, 1992). In brief, FEM works by dividing the geometry of the problem under
80 investigation into a finite number of sub-regions, called elements. The elements are connected
81 together at their corners and sometimes along their mid-sides points, called nodes. For
82 mechanical stress analysis, a variation in displacement (e.g. linear or quadratic) is then
83 assumed through each element, and equations describing the behaviour of each element are
84 derived in terms of the (initially unknown) nodal displacements. These element equations are
85 then combined to generate a set of system equations that describe the behaviour of the whole
86 problem. After modifying the equations to account for the boundary conditions applied to the
87 problem, these system equations are solved. The output is a list of all the nodal displacements.
88 The element strains can then be calculated from the displacements, and the stresses from the
89 strains. This method can be then performed iteratively to optimize a particular design to
90 achieve a certain displacement or level of strain and stress considering the loading applied to
91 the system and its requirements.

92

93 The FEM was introduced to the field of orthopaedic trauma in 1950s (Huiskes and Chao, 1983)
94 and is nowadays widely used in design and development of various implantable devices.
95 Perhaps the earliest finite element analysis of the craniofacial system date back to 1970s (see
96 e.g. Hardy and Marcal, 1973; Tanne et al., 1988; Lestrel, 1989). For example, Hardy and
97 Marcal, (1973) developed a simplified model of skull and concluded that skull is well designed
98 for resistance to anterior loads. There are a large number of studies that have used FEM in a
99 wide range of application on the craniofacial system. Many studies have used FEM for
100 example in the field of craniofacial injury and trauma with a number of studies focusing on
101 adult as well and infant related trauma (e.g. Horgan and Gilchrist, 2003; Roth et al., 2010;
102 Wang et al., 2016; Dixit and Liu, 2017; Ghajari et al., 2017). At the same time in the past 20
103 years, evolutionary biologists and functional morphologists have widely used this technique to
104 understand the form and function of craniofacial systems in an evolutionary context (e.g.
105 Rayfield, 2007; Moazen et al., 2009; Wang et al., 2010; O'Higgins et al., 2011; Prado et al.,
106 2016). More recently this technique has been used to understand the biomechanics of
107 craniofacial development and its associated congenital diseases such as cleft lip palate and
108 craniosynostosis (e.g. Remmler et al., 1998; Pan et al., 2007; Khonsari et al., 2013; Jin et al.,
109 2014; Lee et al., 2017; Marghoub et al., 2018).

110

111 The aim of this study was to review the current literature that have used finite element method
112 to investigate the biomechanics of craniosynostosis in its development or its reconstruction.
113 This review was organized to review these studies with respect to the steps involved in
114 development of such models and to briefly describe their results. Recommendations for future
115 research and areas which require further scientific investigation are also discussed.

116

117 **2- Materials and Methods**

118 A detail survey of literature was carried out to identify the studies that used FEM to investigate
119 the biomechanics of craniosynostosis. A number of databases: Web of Science, SCOPUS,
120 PubMed and Google Scholar were searched with the following keywords: craniosynostosis
121 AND finite AND element. We identified 10 published articles that met the inclusion criteria of
122 this review. The overall aims of these studies and type of synostosis are summarized in Table
123 1.

124

125 Four key steps were highlighted in the identified studies (as per any finite element study):
126 representation of the skull, sutures and craniotomies; representation of the material properties
127 of bones and sutures; representation of the loads; and simulation predictions. Figure 1 shows
128 how one of these studies transformed computed tomography data of a patient with sagittal
129 synostosis to model a reconstruction technique for treatment of this condition using finite
130 element method (Wolanski et al., 2013). The following sections review these steps in the
131 identified studies. These details are also summarized in Table 1 and 2.

132

133 **2-1 Representation of the skull, sutures and craniotomies**

134 Computer aided design tools have been used to simplify the morphology of the human head
135 to geometries such as spherical, spheroidal or ellipsoidal shells. A study by Weickenmeier et
136 al., (2017) used such an approach to model several types of craniosynostosis i.e. predicting
137 the pre-operative calvarial morphology. On the other hand, computed tomography (CT) and
138 magnetic resonance imaging (MRI) have also been used to develop a more detailed
139 representation of the skull (e.g. Nagasao et al., 2010; Wolanski et al., 2013; Li et al., 2017;
140 Borghi et al., 2018). The images are generally reconstructed using an image processing
141 software. Some studies have only modelled craniofacial bones and craniotomies (e.g. Larysz
142 et al., 2012; You et al., 2010; Wolanski et al., 2013; Zhang et al., 2016; Li et al., 2017) while
143 others have also included the cranial sutures (e.g. Nagasao et al., 2011).

144

145 **2-2 Representation of the material properties of bones and sutures**

146 Bone and sutures have been generally modelled as linear, elastic materials with most of the
147 studies using a constant value across the skull (You et al., 2010; Larysz et al., 2012; Wolanski
148 et al., 2013; Zhang et al., 2016). Nonetheless, a wide range of elastic modulus (E) have been
149 used to model the calvarial bones. For example, studies of Larysz et al., (2012) and Wolanski
150 et al., (2013) used an elastic modulus of 380 MPa for bones in children aged 3-5 months and
151 1 year of age. Zhang et al., (2016) used an elastic modulus of 1300 MPa for infants aged 3-6
152 months and 6500 MPa for infants older than 6 months (see Table 1 and 2). For suture material
153 properties, however, only one value of 3.8 MPa was reported by Nagasao et al., (2010 and
154 2011). Borghi et al., (2018) recently used a value of 16 MPa to model coronal and lambdoid
155 sutures in a patient-specific model of sagittal synostosis spring assisted reconstruction.
156

157 **2-3 Representation of the loads**

158 Most of the studies considered the foramen magnum as a stationary point on the human skull
159 during the growth (e.g. Nagasao et al., 2010 and 2011). This anatomical point has, therefore,
160 been used as the main area of constraint for most of the FE studies. Most of the studies
161 modelled immediate post-operative reconstruction and only loaded their models with a
162 constant intracranial pressure (You et al., 2010; Jiang et al., 2010; Larysz et al., 2012;
163 Nagasao et al., 2010 and 2011; Wolanski et al., 2013; Zhang et al., 2016; Li et al., 2017). The
164 only study that modelled the calvarial growth during the development is the work of
165 Weickenmeier et al., (2017).
166

167 **2-4 Simulation predictions and accuracy**

168 Generally, two parameters have been extracted from the results of the finite element models:
169 (1) deformation of the skull, which has also been used to calculate the cephalic index (the
170 maximum width to maximum length ratio multiplied by 100); (2) mechanical strain and stress
171 within the calvarial bone.
172

173 The accuracy of finite element models depends on the choice of input parameters as well as
174 the number of computations used to derive the solution. The number of computations is related
175 to the number and type of elements in the model i.e. mesh convergence. Most of the studies
176 have used the input parameters related to material properties of their models based on
177 previous experimental studies (You et al., 2010; Nagasao et al., 2010 and 2011; Zhang et al.,
178 2016; Weickenmeier et al., 2017; Li et al., 2017). However, they generally have not reported
179 details of mesh convergence.
180

181 **3- Results**

182 The cases studied and their key outcomes are summarized in Table 3. In brief, studies of
183 Nagasao et al., (2010 and 2011) mainly focused on the deformation of the orbits either
184 preoperatively investigating the effect of different types of craniosynostosis or postoperatively
185 investigating the effect of forehead remodelling. Studies of You et al., (2010), Jiang et al.,
186 (2010), Larysz et al., (2012) and Wolanski et al., (2013) and Li et al., (2017) compared different
187 methods of reconstruction for sagittal and metopic synostosis. Authors virtually reconstructed
188 the skull based on different craniotomies and commented on the skull shape immediately post-
189 operatively and the pattern of stress and strain distribution in different reconstructions (see
190 example from Wolanski et al., 2013 in Figure 1). Zhang et al., (2016), used finite element
191 method to quantify the spring force in spring assisted cranioplasty for sagittal synostosis. They
192 measure spring forces in the range of 5-8 N. A study by Weickenmeier et al., (2017) predicted
193 calvarial growth for different types of craniosynostosis.

194 Overall, there was a lack of detailed validation of the FE results. For example, Weickenmeier
195 et al., (2017) compared their modelling findings quantitatively with clinical data only in terms
196 of the cephalic index for different types of craniosynostosis. Similarly, study of Nagasao et al.,
197 (2011) compared their FE prediction of orbital distance in three different groups (normal skull,

198 metopic synostosis and metopic synostosis following forehead reconstruction) with their
199 clinical data. Perhaps, the most detail validation study to date is the study of Borghi et al.,
200 (2018), who developed a patient-specific model of sagittal synostosis and compared the skull
201 shape based on their FE predictions versus post-operative 3D head scan of the same patient's
202 head.

203 **4- Discussion**

204 The current biomechanical literature relating to craniosynostosis was reviewed. Several
205 studies were found that directly developed finite element models of craniosynostosis (n=10).
206 Whilst these studies all highlighted the potential of finite element method to advance treatment
207 of craniosynostosis, it is clear that there is more work to be done. Here two key areas that can
208 be improved are discussed: (1) addressing the modelling assumptions and (2) validating the
209 finite element results.

210 Firstly, there is a clear lack of detail description of the methodologies used in these studies.
211 The technical details and how the models have been developed can be significantly improved.
212 Here perhaps, four areas can be highlighted: (1) loading – most of the studies have applied a
213 constant pressure to load the calvaria with exception of study of Weickenmeier et al., (2017).
214 This approach allows for a comparison of different reconstructions at a single time point during
215 the development. It does not, however, explain how the growing brain interacts with different
216 calvarial reconstructions during the development. In this respect, intracranial volume or brain
217 soft tissue can be modelled and expanded based on the changes in the intracranial volume to
218 take into account the loading arising from the growing brain (Jin et al., 2014; Libby et al., 2017;
219 Marghoub et al., 2018); (2) modelling the sutures – it is well established that the sutures can
220 release the local mechanical strain (e.g. Moss, 1954; Jaslow and Biewner, 1995; Moazen et
221 al., 2013). It is important to include the sutures to develop more realistic models of the
222 craniofacial system (Jin et al., 2013; Weickenmeier et al., 2017; Libby et al., 2017; Marghoub
223 et al., 2018). Sutures can be segmented during the reconstruction of the model of the skull via
224 image processing and incorporated into the finite element simulation; (3) modelling dura mater
225 and other soft tissues – including other soft tissues such as dura mater and muscles will
226 evidently lead to more realistic finite element models of the skull growth. You et al., (2010)
227 included dura mater in their model but it is not clear to us how this tissue was modelled. In this
228 respect, head models developed to simulate head injuries include various soft tissues (e.g.
229 Roth et al., 2010). These models can provide insights for developing more representative
230 models of craniosynostosis (see review by Dixit and Liu, 2017). It must be noted that while
231 increasing the complexity of FE models is possible, further studies are required to investigate
232 how much complexity is needed to develop a validated model of craniosynostosis, whereby,
233 the outcome of different reconstructions can be reliably predicted; (4) material properties – our
234 understanding of changes in mechanical properties of calvarial bones and other related
235 tissues such as dura mater during the development is still limited. Few studies have quantified
236 such changes during the development (e.g. McPherson and Kriewall, 1980; Margulies and
237 Thibault, 2000; Henderson et al., 2005; Coats and Margulies, 2006; Wang et al., 2014;
238 Moazen et al., 2015). Clearly, soft tissues involved in the calvarial development are visco-
239 elastic materials and their properties changes during the development. Most of the current
240 studies have used linear elastic material models. It is encouraging that recent study of Borghi
241 et al. (2018) took into account the viscoelasticity effect of bone and sutures. In this respect,
242 the models can improve including time-dependent changes during the growth. This perhaps
243 also requires further experimental studies.

244 Second, detailed validation of the finite element models is a key step to build confidence in
245 the results of such models. To our understanding, most of the reviewed studies in this paper

246 lack a detailed validation of their simulation. The authors are clearly conscious of the
247 importance of validation in such models. For example, the study by Nagasao et al., (2010),
248 compared their FE results with clinical data in terms of orbital changes in different
249 craniosynostosis groups that they modelled. Similarly, Weickenmeier et al., (2017) compared
250 cephalic indices of their predicated 2D and 3D craniosynostotic skull shapes and compared
251 their results with clinical measurements. While such simple measurements are reassuring, if
252 the CT data of the whole skull is available a full 3D comparison between the FE and *in vivo*
253 data can be carried out (Libby et al., 2017) and provide a more comprehensive analysis of the
254 size and shape differences. In the case of craniosynostosis and predicting the outcome of
255 different surgical techniques, FE results need to be compared against the follow up CT data
256 of the same child. A caveat to this is that there might be ethical or resource issues in obtaining
257 such CT data. In this respect, (1) 3D surface scanners can provide invaluable information (e.g.
258 Dai et al., 2017; Borghi et al., 2018); (2) *in vitro* experimental studies can also be an alternative
259 way to validate the FE models in a simpler condition (e.g. Szwedowski et al., 2011; Toro-
260 Ibacache et al., 2016; Libby et al., 2017).

261 The present study focused on the finite element models of craniosynostosis, however, there
262 are a number of studies that have used computer aided design and three dimensional printing
263 to visualize different reconstructions of craniosynostosis for pre-operative planning of this
264 condition (e.g. Imai et al., 1999; Mommaerts et al., 2001; Meehan et al., 2003; Iyer et al.,
265 2018). These studies are clearly advancing the treatment of craniosynostosis and models
266 generated from these studies can be used to develop finite element simulations of the skull
267 growth to predict the outcomes of different reconstructions on a virtual platform.

268 In summary, a few studies to date have used finite element method to optimize the
269 reconstruction of craniosynostosis skulls. The reviewed studies clearly show the potentials of
270 this technique, however, there are several limitations that need to be addressed in relation to
271 their input parameters and validations. Nonetheless, they provide a strong foundation for
272 future studies.

273
274
275
276
277
278
279
280
281
282
283
284
285
286
287
288
289
290
291
292
293
294
295
296
297
298
299
300
301
302
303
304
305

306
307
308
309
310
311
312
313

314
315
316
317
318
319
320
321
322

References:

1. Abbott A, Netherway DJ, Niemann DB, Clark B, Yamamoto M, et al: CT-Determined Intracranial Volume for a Normal Population. *J Craniofac Surg* 11: 211-23 (2000).
2. Al-Rekabi Z, Cunningham ML, Sniadecki NJ: Cell mechanics of craniosynostosis. *ACS Biomater Sci Eng* 3: 2733–43 (2017).
3. Borghi A, Rodriguez-Florez N, Rodgers W, James G, Hayward R, et al: Spring assisted cranioplasty: A patient specific computational model. *Med Eng Phys.* 53:58-65 (2018).
4. Clayman MA, Murad GJ, Steele MH, Seagle MB, Pincus DW: History of craniosynostosis surgery and the evolution of minimally invasive endoscopic techniques: the University of Florida experience. *Ann Plast Surg* 58(3): 285-7 (2007).
5. Coats B, Margulies SS: Material properties of human infant skull and suture at high rates. *J Neurotrauma* 23:1222-32 (2006).
6. Cornelissen M, Ottelander Bd, Rizopoulos D, van der Hulst R, Mink van der Molen A, et al: Increase of prevalence of craniosynostosis. *J Craniomaxillofac Surg* 44(9): 1273-9 (2016).
7. Dai H, Pear N, Smith W, Duncan C: A 3D Morphable model of craniofacial shape and texture variation. *Proc IEEE Int Conf Comp Vis 2017-Oct*, 8237597: 3104-12 (2017).
8. Dekaban AS: Tables of cranial and orbital measurements, cranial volume, and derived indexes in males and females from 7 days to 20 years of age. *Ann Neurol* 2: 485-91 (1977).
9. Dixit P, Liu GR: A review on recent development of finite element models for head injury simulations. *Arch Computat Methods Eng* 24:979-1031 (2017).
10. Fagan MJ: *Finite element analysis: theory and practice.* Longmans (1992).
11. Gerety PA, Basta MN, Fischer JP, Taylor JA: Operative management of nonsyndromic aagittal synostosis: a head-to-head meta-analysis of outcomes comparing 3 techniques. *J Craniofac Surg* 26(4): 1251-7 (2015).
12. Ghajari M, Hellyer PJ, Sharp DJ: Computational modelling of traumatic brain injury predicts the location of chronic traumatic encephalopathy pathology. *Brain* 140:333-43 (2017).
13. Hardy CH, Marcal PV: Elastic analysis of a skull. *J Appl Mech* 40(4): 838-42 (1973).
14. Henderson JH, Chang LY, Song HM, Longaker MT, Carter DR: Age-dependent properties and quasistatic strain in the rat sagittal suture. *J Biomech* 38:2294–301. (2005).
15. Herring SW: Mechanical influences on suture development and patency. *Front Oral Biol* 12: 41-56 (2008).

- 323 16. Hopper RA, Grant GA, Ellenbogen RG: Controversies in the management of
324 craniosynostosis. *Sem Neur* 13: 81-95 (2002).
- 325 17. Horgan TJ, Gilchrist MD: The creation of three-dimensional finite element models for
326 simulating head impact biomechanics. *Int J Crash* 8: 353-66 (2003).
327
- 328 18. Huiskes R, Chao EY: A survey of finite element analysis in orthopedic biomechanics:
329 the first decade. *J Biomech* 16(6): 385-409 (1983).
330
- 331 19. Imai K, Tsujiguchi K, Toda C, Enoki E, Sung KC, Sakamoto H, Kitano S, Hatoko M,
332 Tajima S: Reduction of operating time and blood transfusion for craniosynostosis by
333 simulated surgery using three-dimensional solid models. *Neurologia medico-*
334 *chirurgica*, 39(6): 423-6 (1999).
335
- 336 20. Iyer RR, Wu A, Macmillan A, Musavi L, Cho R, Lopez J, Jallo GI, Dorafshar AH, Ahn
337 ES: Use of computer-assisted design and manufacturing to localize dural venous
338 sinuses during reconstructive surgery for craniosynostosis. *Childs Nerv Syst.*
339 34:137-42 (2018).
- 340 21. Jaslow CR, Biewner AA: Strain patterns in the horncores, cranial bones and sutures
341 of goats (*Capra hircus*) during impact loading. *J. Zool. Lond.* 235:193-210 (1995).
342
- 343 22. Jiang X, You J, Wang N, Shen Z, Li J: Skull mechanics study of PI procedure plan for
344 craniosynostosis correction based on finite element method. *4th International*
345 *Conference on Bioinformatics and Biomedical Engineering*, Chengdu, 2010, pp. 1-4.
346
- 347 23. Jimenez DF, Barone CM: Early treatment of coronal synostosis with endoscopy-
348 assisted craniectomy and postoperative cranial orthosis therapy: 16-year experience.
349 *J Neurosurg Pediatr* 12(3): 207-19 (2013).
- 350 24. Jin J, Shahbazi S, Lloyd J, Fels S, de Ribaupierre S, et al: Hybrid simulation of brain-
351 skull growth. *Simulation* 90(1): 3-10 (2014).
352
- 353 25. Johnson D, Wilkie AOM: Craniosynostosis. *Eur J Hum Genet* 19: 369-76 (2011).
354
- 355 26. Khonsari RH, Olivier J, Vigneaux P, Sanchez S, Tafforeau P, Ahlberg PE, Di Rocco
356 F, Bresch D, Corre P, Ohazama A, Sharpe PT, Calvez V: A mathematical model for
357 mechanotransduction at the early steps of suture formation. *Proc R Soc B* 280:
358 20122670 (2013).
- 359 27. Larysz D, Wolanski W, Kawlewska E, Manderka M, Gzik M: Biomechanical aspects of
360 preoperative planning of skull correction in children with craniosynostosis. *Acta of*
361 *Bioengineering and Biomechanics* 14(2): 19–26 (2012).
362
- 363 28. Lee C, Richtsmeier JT, Kraft RH: A computational analysis of bone formation in the
364 cranial vault using a coupled reaction-diffusion-strain model. *J Mech Behav Biomed*
365 *Mater.* 29:529-43 (2017).
366
- 367 29. Lestrel PE: Some approaches toward the mathematical modeling of the craniofacial
368 complex. *J Craniofac Gene Dev Bio.* 9(1): 77-91 (1989).
369
- 370 30. Li X, Zhu W, He J, Di F, Wang L, et al: Application of computer assisted three-
371 dimensional simulation operation and biomechanics analysis in the treatment of
372 sagittal craniosynostosis. *J Clin Neurosci.* 44: 323-29 (2017).
373

374 31. Libby J, Marghoub A, Johnson D, Khonsari R, Fagan MJ, Moazen M: Modelling
375 human skull growth: a validated computational model. J Roy Soc Int. 14:20170202
376 (2017).

377 32. Marghoub A, Libby J, Babbs C, Pauws E, Fagan MJ, Moazen M: Predicting calvarial
378 growth in normal and craniosynostosis mice using a computational approach. J
379 Anatomy, 232:440-48 (2018).
380

381 33. Margulies SS, Thibault KL. Infant skull and suture properties: measurements and
382 implications for mechanisms of pediatric brain injury. J Biomech Eng 122(4):364-71
383 (2000).
384

385 34. Mathijssen IMJ: Guideline for care of patients with the diagnoses of craniosynostosis:
386 working group on craniosynostosis. J Craniofac Surg 26(6): 1735-1807 (2015).
387

388 35. McCarthy JG, Glasberg SB, Cutting CB, Epstein FJ, Grayson BH, et al: Twenty-year
389 experience with early surgery for craniosynostosis: I. Isolated craniofacial synostosis-
390 results and unsolved problems. Plast Reconstr Surg 96(2): 272-83 (1995).

391 36. McPherson GK, Kriewall TJ. Fetal head molding: an investigation utilizing a finite
392 element model of the fetal parietal bone. J Biomech. 13:17-26 (1980).
393

394 37. Meehan M, Teschner M, Girod S: Three-dimensional simulation and prediction of
395 craniofacial surgery. Orthodon & Craniofa 6(1): 102-7 (2003).
396

397 38. Moazen M, Costantini D, Bruner E: A sensitivity analysis to the role of fronto-parietal
398 suture in *Lacerta bilineata*: a preliminary finite element approach. Anat Rec, 296: 198-
399 209 (2013).
400

401 39. Moazen M, Curtis N, O'Higgins P, Evans SE, Fagan MJ: Biomechanical assessment
402 of evolutionary changes in the lepidosaurian skull. Proc Nat Acad Sci USA, 106: 8273-
403 8277 (2009).
404

405 40. Moazen M, Peskett E, Babbs C, Pauws E, Fagan MJ: Mechanical properties of
406 calvarial bones in a mouse model for craniosynostosis. PLoS ONE. 12;10:e0125757
407 (2015).
408

409 41. Mommaerts M, Jans G, Wander Stoten J, Staels PF, Van der Perre G, et al: On the
410 assets of CAD planning for craniosynostosis surgery. J Craniofac Surg 12(6): 547-
411 554 (2001).
412

413 42. Morriss-Kay GM, Wilkie AOM: Growth of the normal skull vault and its alteration in
414 craniosynostosis: insights from human genetics and experimental studies. J Anat 207:
415 637-53 (2005).
416

417 43. Moss ML: Growth of the calvaria in the rat, the determination of osseous morphology.
418 Am. J Morphol. 94: 333-361 (1954).
419

420 44. Nagasao T, Miyamoto J, Uchikawa Y, Tamaki T, Yamada A, et al: A biomechanical
421 study on the effect of premature fusion of the frontosphenoidal suture on orbit
422 asymmetry in unilateral coronal synostosis. Cleft Palate Craniofac J 47(1): 82-91
423 (2010).
424

- 425 45. Nagasao T, Miyamoto J, Jiang H, Kaneko T, Tamaki T: Biomechanical analysis of the
426 effect of intracranial pressure on the orbital distances in trigonocephaly. *Cleft Palate*
427 *Craniofac J* 48(2): 190–196 (2011).
428
- 429 46. O'Higgins P, Cobb SN, Fitton LC, Gröning F, Phillips R, et al: Combining geometric
430 morphometrics and functional simulation: An emerging toolkit for virtual functional
431 analyses. *J Anat* 218(1): 3-15 (2011).
432
- 433 47. Opperman LA: Cranial sutures as intramembranous bone growth sites. *Dev Dyn* 219:
434 472-85 (2000).
435
- 436 48. Pan X, Qian Y, Yu J, Wang D, Tang Y, Shen G: Biomechanical effects of rapid
437 palatal expansion on the craniofacial skeleton with cleft palate: a three-dimensional
438 finite element analysis. *Cleft Palate Craniofac J*. 44(2):149-54 (2007).
439
- 440 49. Prado FB, Freire AR, Cláudia Rossi A, Ledogar JA, Smith AL, Dechow PC, Strait
441 DS, Voigt T, Ross CF: Review of in vivo bone strain studies and finite element
442 models of the zygomatic complex in humans and nonhuman primates: implications
443 for clinical research and practice. *Anat Rec* 299(12):1753-78 (2016).
444
- 445 50. Rayfield EJ: Finite element analysis and understanding the biomechanics and
446 evolution of living and fossil organisms. *Ann Rev Ear Plan Sci* 35: 541-76 (2007).
447
- 448 51. Remmler D, Olson L, Ekstrom R, Duke D, M;atamoros A, et al: Pre-surgical CT/FEA
449 for craniofacial distraction: I. Methodology, development, and validation of the cranial
450 finite element model. *Med Eng Phys* 20(8): 607–619 (1998).
451
- 452 52. Richtsmeier JT, Flaherty K: Hand in glove: brain and skull in development and
453 dysmorphogenesis. *Acta Neuropathol* 125: 469-89 (2013).
454
- 455 53. Roth S, Raul J-S, Willinger R: Finite element modelling of paediatric head impact:
456 Global validation against experimental data. *Comput Methods Programs Biomed*, 99:
457 25-33 (2010).
458
- 459 54. Szwedowski TD, Fialkov J, Whyne CM: Sensitivity analysis of a validated subject-
460 specific finite element model of the human craniofacial skeleton. *Proc Inst Mech Eng*
461 *H* 225(1):58-67 (2011).
462
- 463 55. Scheuer L, Black S: *The juvenile skeleton*. Elsevier Academic Press (2004).
464
- 465 56. Simpson A, Wong AL, Bezuhy M: Surgical Correction of Nonsyndromic Sagittal
466 Craniosynostosis Concepts and Controversies. *Ann Plast Surg* 78: 103–10 (2017).
467
- 468 57. Tanne K, Miyasaka J, Yamagata Y, Sachdeva R., Tsutsumi S, et al: Three-
469 dimensional model of the human craniofacial skeleton: method and preliminary results
470 using finite element analysis. *J Biomed Eng* 10: 246–52 (1988).
471
- 472 58. Taylor JA, Maugans TA: Comparison of spring-mediated cranioplasty to minimally
473 invasive strip craniectomy and barrel staving for early treatment of sagittal
474 craniosynostosis. *J Craniofac Surg* 22:1225-9 (2011).
475

- 476 59. Thomas GP, Johnson D, Byren JC, Jayamohan J, Magdum SA, et al: Long-term
477 morphological outcomes in nonsyndromic sagittal craniosynostosis: a comparison of
478 2 techniques. *J Craniofac Surg* 26(1): 19-25 (2015).
479
- 480 60. Toro-Ibacache V, Fitton LC, Fagan MJ, O'Higgins P: Validity and sensitivity of a
481 human cranial finite element model: implications for comparative studies of biting
482 performance. *J Anat.* 228: 70-84 (2016).
483
- 484 61. van der Meulen J, van der Hulst R, van Adrichem L, Arnaud E, Chin-Shong D, et al:
485 The increase of metopic synostosis: a pan-European observation. *J Craniofac Surg*
486 20: 283-86 (2009).
487
- 488 62. Wang JW, Huang J, Li Z, Wang J, Li ZD, et al: Research progress on biomechanics
489 of craniocerebral injury in children. *J Forens Med* 32 (6): 448-51 (2016).
490
- 491 63. Wang J, Zou D, Li Z, Huang P, Li D, Shao Y, et al. Mechanical properties of cranial
492 bones and sutures in 1–2-year-old infants. *Med Sci Monit* 20:1808-13 (2014).
493
- 494 64. Wang Q, Wright BW, Smith A, Chalk J, Byron CD: Mechanical impact of incisor
495 loading on the primate midfacial skeleton and its relevance to human evolution. *Anat*
496 *Rec* 293:607-17(2010).
497
- 498 65. Weickenmeier J, Fischer C, Carter D, Kuhl E, Goriety A: Dimensional, Geometrical,
499 and Physical Constraints in Skull Growth. *Phys Rev Lett* 118(24): 1–5 (2017).
500
- 501 66. Wilkie AOM, Johnson D, Wall SA: Clinical genetics of craniosynostosis. *Curr Opin*
502 *Pediatr.* 29(6):622-8 (2017).
503
- 504 67. Wolański W, Larysz D, Gzik M, Kawlewska E: Modeling and biomechanical analysis
505 of craniosynostosis correction with the use of finite element method. *Int J for Numer*
506 *Method Biomed Eng* 29(9): 916-25 (2013).
507
- 508 68. You J, Jiang X, Hu M, Wang N, Shen Z, et al: The bone slot effect study of PI
509 procedure for craniosynostosis correction plan based on finite element method. *3rd*
510 *International Conference on Biomedical Engineering and Informatics, Yantai, 2010,*
511 *pp. 605-608. (2010).*
- 512 69. Zhang G, Tan H, Qian X, Zhang J, Li K, et al: A Systematic Approach to Predicting
513 Spring Force for Sagittal Craniosynostosis Surgery. *J Craniofac Surg* 27(3): 636-43
514 (2016).

515

Table 1: A summary of previous studies objectives, details of patient population considered.

Authors	Aims and objectives	Type of synostosis/Groups	Patient(s)/Specimens	Source of geometry
Nagasao et al. (2010)	To compare the difference in orbital deformation in patients with unicoronal synostosis between those whom only show unicoronal synostosis and those whom also show sphenoidal fusion.	<ul style="list-style-type: none"> • Unicoronal • Unicoronal and lambdoid 	<ul style="list-style-type: none"> • 4.2±1.4 m/o (8 unicoronal) • 4.6±2.2 m/o (7 unicoronal and lambdoid) [Untreated, normal expansion]	i. CT
You et al. (2010) & Jiang et al., (2010)	To analyze the relationship between different craniotomies, and the overall skull rigidity in PI- shape reconstruction.	<ul style="list-style-type: none"> • Not specified 	<ul style="list-style-type: none"> • Not specified [Untreated, virtual surgery]	i. CT
Nagasao et al. (2011)	To investigate how normal, pre-operative metopic and post – operative metopic craniosynostosis orbital morphology are affected by the loading from intracranial pressure.	<ul style="list-style-type: none"> • Metopic [untreated] • Metopic [treated] • Healthy skull (HS) 	<ul style="list-style-type: none"> • 8.2±4.5 months (10 MS patients) • 8.6±4.3 months (10 HS patients) [Untreated and treated, normal expansion]	i. CT
Larysz et al. (2012)	To propose a method of pre-operative planning for craniosynostosis based on 3D modelling and biomechanical analysis using finite element method.	<ul style="list-style-type: none"> • Sagittal • Metopic 	<ul style="list-style-type: none"> • 1 y/o, male • 3 m/o, male [Untreated, virtual surgery]	i. CT ii. MRI
Wolanski et al. (2012)	To highlight the potentials of finite element method for pre-operative planning and post-operative evaluation of patients with craniosynostosis	<ul style="list-style-type: none"> • Sagittal • Metopic 	<ul style="list-style-type: none"> • 5 m/o, male (2 scenarios) • 3 m/o, male (2 scenarios) [Untreated, virtual surgery]	i. CT
Zhang et al. (2016)	To present and validate a system which accurately can predict the optimal spring force for sagittal craniosynostosis reconstruction.	<ul style="list-style-type: none"> • Sagittal [Spring assisted surgery]	<ul style="list-style-type: none"> • 3-6 m/o, unknown sex (15 patients) • >6 m/o, unknown sex (8 patients) [Virtual surgery]	i. CT ii. Laser

Table 1 continued.

Authors	Purpose	Type of synostosis/Groups	Patient(s)	Source of geometry
Weickenmeier et al. (2017)	To predict typical skull morphologies in most common forms of craniosynostosis	<ul style="list-style-type: none"> • Unicoronal [untreated] • Bicoronal [untreated] • Lambdoid [untreated] • Metopic [untreated] • Sagittal [untreated] • Healthy skull [untreated] 	<ul style="list-style-type: none"> • 2D study: Cross-sectional area of newborn scaled to healthy CI value of 78 (First 4 scenarios above) • 3D study: Approximated as ellipsoid with CI of 78 (All 6 scenarios above) 	<ul style="list-style-type: none"> i. MRI (2D) ii. CAD (3D)
Li et al. (2017)	To quantify the positive outcome of using computer assisted pre-operative planning such as biomechanical analysis and 3D printing	<ul style="list-style-type: none"> • Sagittal [Calvarial vault remodeling] 	<ul style="list-style-type: none"> • 8-13 m/o, 7x male & 3x female (10 patients - Traditional treatment) • 8-13 m/o, 4x male & 4x female (8 patients - Computer assisted pre-op planning) 	<ul style="list-style-type: none"> i. CT ii. MRI iii. Cephalograms
Borghi et al. (2018)	To develop a patient specific computational model of sprint assisted cranioplasty to predict the individual overall head shape	<ul style="list-style-type: none"> • Sagittal 	<ul style="list-style-type: none"> • Pre-operative CT data at 4.4 m/o 1x male and post-operative 3D surface data at 5.5 m/o of the same patient 	CT

Table 2: A summary of the material properties and boundary conditions considered in the previous studies.

Authors	Material properties	Constraints	Loading
Nagasao et al. (2010)	<ul style="list-style-type: none"> Cortical bone: E= 134000 MPa, v=0.3 Cancellous bone: E= 7700 MPa, v=0.3 Cranial sutures: E= 3.78 MPa, v=0.45 <p>[Remained constant]</p>	<ul style="list-style-type: none"> Foramen magnum – fixed in all DOF 	<ul style="list-style-type: none"> Intracranial pressure of 15 mm Hg was applied normal to all element of inner surface of skull.
You et al. (2010) & Jiang et al., (2010)	<ul style="list-style-type: none"> Bone: E=2500 MPa, v=0.22, density=2.15 kg/cm³ Dura matter: E=34.5MPa, v=0.45, density=1.14 kg/cm³ <p>[Remained constant]</p>	<ul style="list-style-type: none"> Posterior distal edge of parietal bone – fixed in all DOF 	<ul style="list-style-type: none"> Intracranial pressure of 2kPa (15mm Hg) was applied normal to all element of inner surface of skull.
Nagasao et al. (2011)	<ul style="list-style-type: none"> Cortical bone: E=134000 MPa, v=0.3 Cancellous bone: E=7700 MPa, v=0.3 Cranial suture: E=3.78 MPa, v=0.45 <p>[Remained constant]</p>	<ul style="list-style-type: none"> Foramen magnum – fixed in all DOF 	<ul style="list-style-type: none"> Intracranial pressure of 15 mm Hg was applied normal to all element of inner surface of skull.
Larysz et al. (2012)	<ul style="list-style-type: none"> Bone: E=380 MPa (based on radiological density in Hounsfield Units) <p>[Remained constant]</p>	<ul style="list-style-type: none"> Not specified. 	<ul style="list-style-type: none"> Not clear to us.
Wolanski et al. (2012)	<ul style="list-style-type: none"> Bone: E=380MPa, v=0.22 <p>[Remained constant]</p>	<ul style="list-style-type: none"> Fixed – base of skull 	<ul style="list-style-type: none"> Intracranial pressure of 2.66 kPa (19.95 mm Hg) was applied normal to all element of inner surface of skull. Applied deformation based on re-modelling of skull
Zhang et al. (2016)	<ul style="list-style-type: none"> Bone: E=1300 MPa, v=0.28 - (Group A) Bone: E=6500 MPa, v=0.22 - (Group B) <p>[Remained constant]</p>	<ul style="list-style-type: none"> Opposite edge of spring fixed 	<ul style="list-style-type: none"> Point loading force at spring contact region (Initial value of 6.9 N)
Weickenmeier et al. (2017)	<ul style="list-style-type: none"> Not specified. 	<p>2D: Fixed at the center and kinematic constraint on sutures</p> <p>3D: Center fixed and corresponding suture region depending on scenario</p>	<p>2D: Unidirectional homogeneous expansion</p> <p>3D: Orthotropic in-plane growth: Length. Width and Bidirectional loading</p> <p>(Simulates 12 months growth, 30% increase in circumference)</p>

Table 2 continued.

<i>Authors</i>	<i>Material properties</i>	<i>Constraints</i>	<i>Loading</i>
Li et al. (2017)	<ul style="list-style-type: none"> • Bone – details are not specified. • Fixation device - details are not specified 	<ul style="list-style-type: none"> • Not specified. 	<ul style="list-style-type: none"> • Not specified.
Borghi et al. (2018)	<ul style="list-style-type: none"> • Bone: E=421 MPa, $\nu=0.22$ • Sutures: E=16 MPa, $\nu=0.49$ <p>The viscoelasticity of both bone and sutures were modelled through Prony shear and bulk relaxation relationship.</p>	<ul style="list-style-type: none"> • Model was constrain at the distal end of three quarter of the skull (in the transverse plane) to avoid free expansion of the head base in this plane. 	<ul style="list-style-type: none"> • Spring expansion was simulated.

Table 3: A summary of results of current finite element analysis of craniosynostosis. NA abbreviate “not applicable”.

Authors	Presented data	Validation	Outcome
Nagasao et al. (2010)	<ul style="list-style-type: none"> Orbital deformation around the eye socket 	Quantitative analysis of clinical data	<ul style="list-style-type: none"> Results showed that only frontoparietal synostosis caused more deformation around the orbit compare to combined frontoparietal and frontosphenoidal synostosis. Degree of fusion presented by frontosphenoidal synostosis should be evaluated in detail
You et al. (2010) & Jiang et al., (2010)	<ul style="list-style-type: none"> FE Stress & displacement on different craniotomies for Pi-shaped operation 	NA	<ul style="list-style-type: none"> Results indicated that cranial bone rigidity is a key factor with profound influence on post-op. outcomes and lower bone rigidity leads to better results (Schemes 4-5). No validation of the research was provided to support these results/claims
Nagasao et al. (2011)	<ul style="list-style-type: none"> Orbital deformation around eye socket for normal skulls, untreated and treated metopic synostosis skulls 	Quantitative analysis of clinical data	<ul style="list-style-type: none"> Results showed expansion of interorbital distances due to intracranial pressure is constrained structurally in metopic synostosis. The remodeling of the frontals during metopic synostosis treatment allows the expansion of the frontals. This then increases the interorbital distance and improve the facial morphology.
Larysz et al. (2012)	<ul style="list-style-type: none"> FE stress and deformation on critical sections of skull following endoscopic surgical cuts 	NA	<ul style="list-style-type: none"> Pattern of skull deformation following patient-specific metopic and sagittal synostosis calvarial reconstruction were presented. Authors also presented bone thickness and the loading levels required to cut the calvarial bones.
Wolanski et al. (2012)	<ul style="list-style-type: none"> FE stress and displacement of cranium following virtual surgery 	Qualitative analysis of clinical data	<ul style="list-style-type: none"> Results showed that in metopic reconstruction remodelling of the forehead by one incision along the metopic and two incisions along the coronal sutures showed higher maximum displacement comparing to the same craniotomies with additional two incisions in the middle of each half of the frontal bones. Results showed that in sagittal reconstruction inverted modified pi procedure with half-incisions in the middle of the parietal bone showed lower maximum displacement comparing to the same craniotomy with full incision in the parietal bone. Note skulls were loaded with intracranial pressure.
Zhang et al. (2016)	<ul style="list-style-type: none"> Optimal spring force based on pre-operative patient-specific properties 	Quantitative analysis of clinical data	<ul style="list-style-type: none"> Development of a computer platform capable of predicting optimal spring force in Spring-assisted surgery (SAS) for sagittal synostosis. In vivo and clinical data results indicated that bone thickness and spring force play a crucial role in surgical outcome.
Weickenmeier et al. (2017)	<ul style="list-style-type: none"> CI values for various simulated craniosynostosis models in 2D and 3D 	Quantitative analysis of clinical data	<ul style="list-style-type: none"> Typical craniosynostotic skull shapes were predicted using simplified 2D and 3D elliptical models. The cephalic index predictions based on the 2D model showed 0.5% to 12% difference with clinical data across sagittal, lambdoid, metopic, uni/bi coronal synostosis. The 3D model showed 0.5% to 3.5% difference between the predicted and clinical cephalic indexes.

Table 3: continued.

Authors	Presented data	Validation	Outcome
Li et al. (2017)	<ul style="list-style-type: none"> Surgical data such as time, blood loss, cost and CI values were measured and compared 	Qualitative analysis of clinical data	<ul style="list-style-type: none"> Presented stress and strain analysis of a single case for sagittal synostosis reconstruction. Quantitative data i.e. operative duration, blood loss, hospital cost pre & post-operative cephalic indexes were also presented comparing a preoperative planning cohort versus a non-pre-operative planning cohort.
Borghi et al. (2018)	<ul style="list-style-type: none"> Spring opening over time and predicted calvarial shape following surgery. 	Quantitative comparison versus 3D surface data obtained from a handheld scanner.	<ul style="list-style-type: none"> A validated patient-specific model of spring assisted sagittal synostosis was developed. Highlighted the potentials of finite element method to predict the skull shape of craniosynostotic patients following surgery.

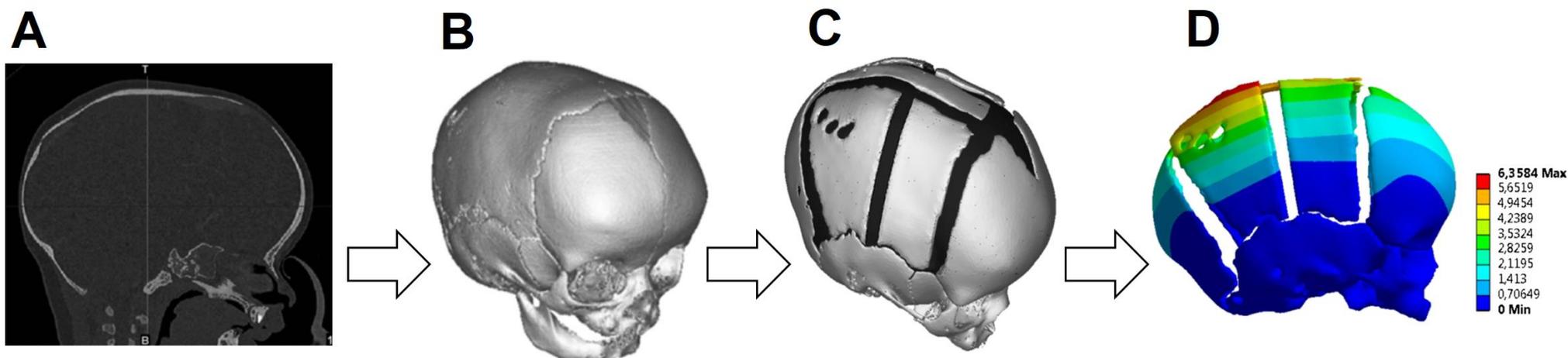


Figure 1: A summary of model development from (A) computed tomography to (B) 3D reconstructed model of the skull pre-operatively to (C) then 3D virtual reconstruction post-operatively and then to (D) finite element predictions, here due to constant pressure applied to the inner surface of the skull (modified with permission from Wolanski et al., 2013).