

# 1 **Evaluation of Close-range Stereo Matching Algorithms Using Stereoscopic Measurements**

2

## 3 **Description**

4 This paper describes a new assessment protocol for close range stereo matching algorithms using  
5 a stereo display and presents evaluation results of three stereo processing pipelines used in current  
6 and future Mars rover operations.

## 7 **Abstract**

8 The performance of binocular stereo reconstruction is highly dependent on the quality of the  
9 stereo matching result. In order to evaluate the performance of different stereo matchers, several  
10 quality metrics have been developed based on quantifying error statistics with respect to a set of  
11 independent measurements usually referred to as ground truth data. However, such data are  
12 frequently not available, particularly in practical applications or planetary data processing. To  
13 address this, we propose a ground truth independent evaluation protocol based on manual  
14 measurements. A stereo visualization tool has been specifically developed to evaluate the quality  
15 of the computed correspondences. We compare the quality of disparity maps calculated from three  
16 stereo matching algorithms, developed based on a variation of GOTCHA, which has been used  
17 in planetary robotic rover image reconstruction at UCL-MSSL (Otto and Chau, 1989). From our  
18 evaluation tests with the images pairs from Mars Exploration Rover (MER) Pancam and the field  
19 data collected in PProViScout 2012, it has been found that all three processing pipelines used in  
20 our test (NASA-JPL, JR, UCL-MSSL) trade off matching accuracy and completeness differently.  
21 NASA-JPL's stereo pipeline produces the most accurate but less complete disparity map, whilst  
22 JR's pipeline performs best in terms of the reconstruction completeness.

## 23 **Keywords**

24 Stereo matching, Stereoscopic visualization, Rover image processing, 3D reconstruction, Stereo  
25 matching evaluation

## 1 **1. Introduction**

2 Stereo matching has long been a fundamental and challenging research topic in computer vision.  
3 A large number of fully automated stereo matching algorithms have been developed since the  
4 earliest approach made by Hannah (Hannah, 1974) and further variations of local algorithms,  
5 which rely on the computation of correlations of local patches, developed in the 1990s. Follow-  
6 on optimisation and statistical machine learning techniques including dynamic programming  
7 (Birchfield and Tomasi, 1998), Markov random field (Geman, 1984), graph cuts (Boykov, 2001),  
8 belief propagation (Sun et al., 2003), semi-global matching (Hirschmuller, 2008), and seed-  
9 growing algorithms (Lhuillier and Quan, 2002), have been shown to be able to produce high  
10 quality disparity maps, but it is getting difficult to evaluate various matching algorithms  
11 developed for different purposes.

12 To our best knowledge, the Middlebury test is the most influential work on recent stereo  
13 evaluation (Scharstein and Szeliski, 2002). In this test, the authors propose a new taxonomy of  
14 comprehensive stereo algorithms and a C++ test bed for the quantitative evaluation of dense two-  
15 frame stereo correspondence algorithms. The Middlebury test basically performs an evaluation  
16 based on the error metrics computed from sparse “ground truth” point pairs or by synthesizing a  
17 warped image from pre-computed dense disparity maps. Therefore, the reference data plays an  
18 important role in the evaluation process.

19 When the algorithms were not strong enough to process complicated scenes, the 3D geometry of  
20 reference data does not need to be complex, but it needs to be dense enough to evaluate a sparse  
21 set of point correspondences produced by test algorithms. For this reason, Scharstein et al.  
22 configured a test scene with a set of slanted 2D planes. Since a 2D homography of a planar object  
23 can be easily defined by 4 point correspondences, this approach can produce a virtually complete  
24 disparity map of two images from a few manual correspondences (Scharstein et al., 2001).  
25 However, as stereo algorithms evolve, a simple geometry is no longer able to differentiate  
26 advanced algorithms and people need more complex geometry at higher pixel resolution.

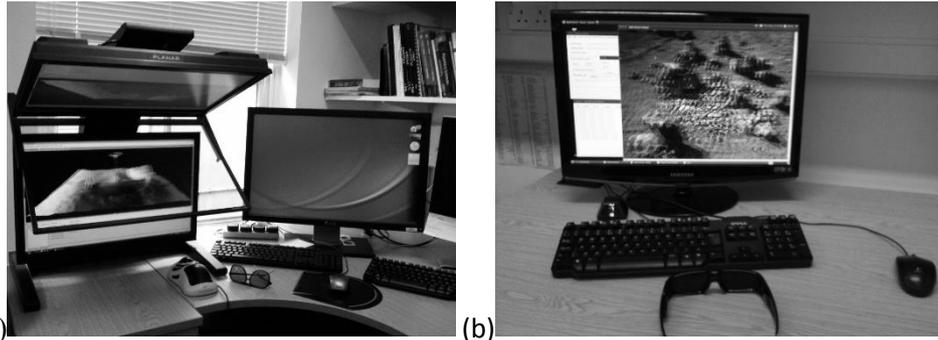
27 Synthetic images can be an option to improve the scene complexity (Morales and Klette, 2011)  
28 but they are generally insufficient to synthesize practical scenes affected by a range of noise and  
29 various lighting conditions. Alternatively, an active 3D sensor can be used to produce reference  
30 data. For example, a special structured light system was developed in the 2003 Middlebury test,  
31 where one or two projectors are used with a translating camera to create a dense reference  
32 disparity map for a stereo pair (Scharstein and Szeliski, 2003). This approach is particularly useful  
33 as we can have control over the spatial resolution of a disparity map with higher depth accuracy.  
34 However, a structured light is more suitable for capturing small objects in a controlled indoor  
35 environment. Geiger et. al. also pointed out this limitation, mentioning that higher ranking  
36 algorithms from the Middlebury reference data can go below average when it is tested against the  
37 images from outside the laboratory (Geiger et al., 2012).

38 Creating reference data for multiview stereo algorithms could be even more challenging. In  
39 addition to classic stereo matching, estimating external transforms between image pairs and  
40 locating the position of a camera in a previously reconstructed scene are other imperative features  
41 of a multiview stereo algorithm (e.g. visual odometry or SLAM). Therefore, the reference data  
42 should be registered with correct positional information. This normally requires combining  
43 multiple heterogeneous sensors and more complicated calibration steps.

44 For example, the Middlebury test images for multiview stereo algorithms were obtained using a  
45 robotic arm that can move on the surface of one-metre radius sphere with high precision (Seitz,  
46 2006). In addition, to improve the accuracy of a 3D model, the initial point cloud from multiple  
47 images was registered with a more refined laser scanning result using an ICP method. Jensen et.  
48 al. recently published a data set containing 80 scenes for large scale multiview stereo evaluation  
49 using a similar approach but with a structured light (Jensen et al., 2014). For outdoor scenes,  
50 Strecha et. al. proposed a method that can combine multiple Lidar scans with images based on  
51 physical markers placed on a test scene (Strecha et al., 2008). Later, Geiger et al. proposed more  
52 automated method which combines Lidar and two video cameras with accurate localisation

53 systems (e.g., GPS and IMU) to cover a wider area from a long-distance drive (39.2 km) (Geiger  
54 et al., 2012).

55 It is possible to produce a good quality of reference data for outdoor scene by registering active  
56 sensors to stereo cameras as mentioned above, and in fact it is widely used in the orbital sensor  
57 calibration process in many remote sensing applications. For example, the performance of the  
58 SIMBIO-SYS imaging suite employed in ESA BepiColombo mission was assessed during a  
59 pre-flight calibration process, where laser scans of a small target object are used to validate a  
60 stereo reconstruction result of the sensor (Simioni et al., 2014). Also, the high-resolution stereo  
61 camera (HRSC) on Mars Express was validated based on various outdoor scenes captured during  
62 on-ground and airborne test (Jaumann et al., 2007). However, this approach is not always  
63 available, especially, when performing planetary 3D reconstruction using robotic vision systems.  
64 Also, creating reference data using multiple sensors would be a very expensive process in terms  
65 of computation complexity and labour, even though a new set of test data is frequently required  
66 to evaluate advanced algorithms. To address this, we introduce a new accuracy evaluation method  
67 to assess stereo matching results when there is no prior knowledge about the depth of points within  
68 a scene. This “ground truth” independent evaluation criteria were inspired by the use of manual  
69 measurements in stereo photogrammetry, originally performed using film media and optic  
70 mechanical instrumentation but since the early 2000s using so-called softcopy stereo workstations  
71 based on stereoscopic displays. An early example of the use of these manual photogrammetric  
72 measurements using an analytical stereoplotter is discussed by Day and Muller, 1989. A recent  
73 paper also showed that the use of 3D stereoscopic display can improve human performance in  
74 locating objects and inferring depths of surfaces within a scene (Mcintire, 2014), so that this  
75 approach is not only more effective than the manual point selection used by the computer vision  
76 community in early days (Nakamura et al., 1996), but also closely related to the local cross-  
77 correlation process inspired by a biological vision system (Fleet et al. 1996).



78

(a)

(b)

79 Figure 1: Example of stereoscopic visualisation with a passive stereo display where images from  
80 upper and lower displays are reflected on a polarised beamsplitter in the middle (a), whereas an  
81 active stereo display uses a high refreshing LCD screen (120 HZ) with synchronised NVIDIA  
82 shutter glasses (b).

83

84 In this work, a Java-based stereo workstation has been developed based on work performed at  
85 JPL on being able to display stereo data on different stereo displays (Pariser and Deen, 2009). We  
86 trained a group of research participants to make repeat measurements of the three-dimensional  
87 position of fixed points in the same scenes using a stereo cursor on a stereo workstation display  
88 (Azari et al., 2009; Shin et al. 2011). A stereo display is afforded either using anaglyphic fusion  
89 of stereo-pairs on a colour display or by using different specialist stereo display devices [Fig. 1(a)  
90 and (b)] of increasing sophistication and cost. These tie-points are then used to compute error  
91 metrics of different stereo matching algorithms by comparing the computed disparity map with  
92 the corresponding manual measurements under three different manual selection scenarios. A 2D  
93 Gaussian function based scoring metrics have also been introduced for a quantitative evaluation.

94 The proposed evaluation method can be used to complement the Middlebury test when we need  
95 new test images from more complex scene at higher image resolution. More importantly, it can  
96 complement the missing evaluation work of stereo matching of rover imagery from planetary  
97 robotic missions, such as the NASA Mars Exploration Rover (MER) or Mars Science Laboratory

98 (MSL), where obviously we do not have either any “ground truth” 3D data nor any prior  
99 knowledge of the scene.

100 This evaluation method was proposed within the EU FP-7 Planetary Robotics Vision Ground  
101 Processing (PRoVisG: EU FP-7 PRoVisG project, <http://provisg.eu/>), and has been applied to  
102 evaluate the accuracy of disparity maps computed from stereo pairs in the PRoVisG Mars 3D  
103 challenge campaign (<http://cmp.felk.cvut.cz/mars/>) as well as additional stereo-pairs captured in  
104 the ExoMars Pancam test campaign at Clarach Bay in Aberystwyth (ExoMars test campaign:  
105 <https://www.youtube.com/watch?v=6gRo8QSXX5c>), using state-of-art planetary stereo  
106 technologies from NASA-JPL (USA), Joanneum Research Institute (Austria) and UCL-MSSL  
107 (UK).

108 We explain more details of the proposed evaluation protocol in the following section. Based on  
109 which, we present the evaluation results of a couple of disparity maps produced by JPL, JR, and  
110 UCL in Sec. 3, followed by our discussion in Sec. 4.

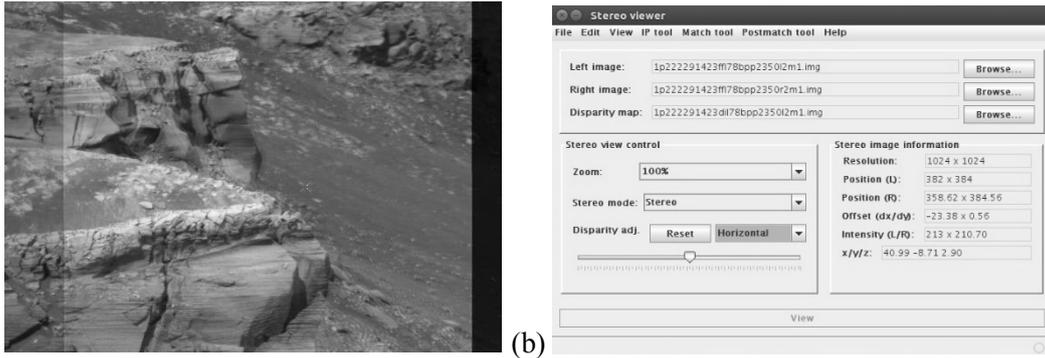
111

## 112 **2. Method**

### 113 **2.1 Stereo Workstation**

114 Most stereo matching algorithms used in the remote sensing community employ an automated  
115 workflow that has been built based on different mathematical definitions of image features (e.g.  
116 corners and edges) and/or matching (dis-)similarity of corresponding points on a stereo pair.  
117 However, this often neglects the impact of different detection errors from various imaging  
118 conditions such as image noise, viewing angle, resolution, and scale difference. In addition, there  
119 is normally no proper visual validation of the detected point pairs.

120



121

(a)

(b)

122 Figure 2: Example of a stereo anaglyph showing a stereo cursor: (a) the offset of a stereo cursor  
 123 is automatically set according to the supplied disparity map; (b) triangulated 3D position of a  
 124 corresponding pair is also displayed when there is calibration data based on the use of the  
 125 CAHVOR calibration model employed by NASA for MER and MSL cameras (Di and Li, 2004).

126

127 To address these issues, we developed a Stereo WorkStation (StereoWS) under the PProVisG  
 128 project. The proposed system is capable of visualizing tie-points on a stereo pair in a hardware-  
 129 independent manner, e.g. with a conventional colour display, it will automatically switch the  
 130 rendering mode to stereo anaglyphs [see Fig. 2(a)].

131 We also developed intuitive user interfaces to facilitate the tie-point validation and selection  
 132 process. For example, provided there is no pre-existing disparity map, users can make  
 133 measurements using a floating 3D cursor, or fix the cursor in the left image at a pre-defined point  
 134 and only allow the right image cursor to move in 3D (i.e. by changing the disparity of the stereo  
 135 cursor) in order to be able to place the 3D cursor onto a visually perceived surface. When there is  
 136 an initial disparity map available, however, the offset of the stereo cursor will be automatically  
 137 adjusted to speed up the tie-point selection process.

138 Information on each collected tie-point such as tie-point ID, coordinates, can also be displayed in  
 139 a separate window [see Fig. 2(b)], so that a user can easily edit the incorrect tie-point as well as  
 140 monitor progress. To assist a user to select a tie-point more efficiently, a range of basic image

141 processing tools are also included, and our in-house stereo matching algorithm, i.e. Adaptive  
142 Least Squares Correlation (ALSC) (Gruen, 1985) and Region growing (GOTCHA) (Otto and  
143 Chau, 1989) have been integrated into the software to produce a denser disparity map from the  
144 collected manual tie-points, if required.

145

## 146 **2.2 Selection of tie-points**

147 In this work, we define three types of tie-points and employ slightly different selection procedures  
148 to prepare a sub-pixel reference tie-points:

149 (a) **Feature based:** Irregularly distributed tie-points.

150 (b) **Regular grid:** Regularly distributed tie-points.

151 (c) **Discontinuities:** Tie-points around depth discontinuities.

152 Type (a) (i.e. feature-based) tie-points are collected to generate highly detectable reference tie-  
153 points from standard feature matching algorithms. Since many detectable image features are  
154 found around highly textured areas, we can easily select feature-based tie-points from visual  
155 identification. The selection procedure initially defines a number of “interesting” points from the  
156 left image using generic feature extraction algorithms, and then ask participants to identify the  
157 corresponding right point by adjusting the offset of a stereo cursor. Corresponding tie-points in  
158 the right image are, therefore, defined at integer resolution initially. However, an average is taken  
159 of a set of manual selections that result in sub-pixel selection. Alternatively, ALSC can be applied  
160 to the right tie-point to refine the pixel position.

161 Type (b) (i.e. regular grid) tie-points are proposed to collect regularly distributed reference tie-  
162 points across the whole image. This will improve the chance of getting reference tie-points from  
163 small depth discontinuity or from less-textured areas. Unlike the feature based selection, it will  
164 be a bit more challenging to pick a correct tie-point from visual identification. Therefore,  
165 participants are asked to collect tie-point from visual validation, i.e. an initial guess for a right tie-

166 point is given at the beginning. To provide good starting points to participants, a dense disparity  
167 map is generated using an in-house stereo processing pipeline and sampled at regular grid points.  
168 These initial tie-points are then visually inspected, e.g. moving the stereo cursor around the grid  
169 points and check if there is any abnormality, or adjusting the disparity offset of a stereo cursor at  
170 the point to check whether the estimation appears to be the best solution, and/or do both with 1.5  
171 or 2 times scaled-up images, which will increase the chance of getting correct correspondences  
172 (Chan et al., 2003). Finally, collect the resulting tie-points that pass the validation test.

173 Type (c) tie-points (i.e. discontinuities) aims to collect reference tie-points from the places that  
174 general automated matchers may fail (so-called pathological cases). These areas are normally  
175 resulted from occlusions, insufficient texture, and strong depth discontinuities, i.e. pixels whose  
176 neighbouring disparities differ by more than a threshold (refer to the Middlebury stereo evaluation  
177 (Scharstein et al., 2001)). Amongst these, we are particularly interested in matching performance  
178 around depth discontinuity, since some algorithms deliberately enforce the local smoothness  
179 around depth discontinuities in order to densify a disparity map. We manually select two pairs of  
180 tie-points around this area, i.e. one tie-point from background and another one from foreground  
181 and evaluate how correctly an algorithm can handle the scene occlusions (see Fig. 3 and Sec. 2.4).  
182 The scene occlusion is a well-known issue in classic stereo matching, therefore it might be  
183 interesting to see if it is possible to design an automated pipeline for populating type (c) tie-points  
184 (i.e. discontinuities) with conventional feature detectors. However, without knowing true  
185 foreground and background segmentation, we found this would be difficult to make it fully  
186 automated.

187 To select type (c) tie-points, an expert manually chooses a set of challenging tie-points around a  
188 typical problematic area, and participants are asked to validate them. The validation process is  
189 quite similar to the regular grid selection, except that this time no clues are given around tentative  
190 tie-points.

191

192 **2.3. Error metrics**

193 The next step is to estimate the error bounds according to the statistics recorded in the three types  
 194 of manual tie-point selection process. Suppose that  $T^k$  is a set of left tie-points from type (k)  
 195 dataset, i.e.  $T^k = \{\mathbf{t}_0^k, \dots, \mathbf{t}_M^k\}$ , where  $k \in \{a, b, c\}$  and  $M$  is the number of left tie-point defined in  
 196 type (k). Similarly, we can define a set of right tie-points corresponding to  $\mathbf{t}_i^k$  from manual  
 197 selections as  $S_i^k = \{\mathbf{s}_{0i}^k, \dots, \mathbf{s}_{Ni}^k\}$ , where  $N$  is the number of participants performing manual  
 198 measurement.

199 Although it is not always true that some of the measurements in  $S_i^k$  happen to be identical to  
 200 ground truth, it is highly likely that a true correspondence of  $\mathbf{t}_i^k$  can be found within a cluster of  
 201 selected points. Thus, our scoring method basically defines a local cluster of  $S_i^k$  based on the  
 202 mean  $\mathbf{m}_i^k$  and the standard deviation  $\sigma_i^k$  and evaluates final matching score.

203 When estimating the statistics from manual measurements, it should be considered that not  
 204 everyone is good at fusing a stereo pair and few people are not even capable of perceiving depth  
 205 difference from the stereo fusion. Therefore, the outliers need to be identified and removed before  
 206 evaluating statistics of the tie-point positions from a large group of manual selections.

207 To identify outliers, we define a simple error function using a pre-computed disparity map  $D$ . For  
 208 example, a selection error of a tie-point  $(\mathbf{t}_i^k, \mathbf{s}_{mi}^k)$ , can be defined as the pixel difference between  
 209 the manual measurement and computed disparity map for a point, i.e.

$$210 \quad e(\mathbf{t}_i^k, \mathbf{s}_{mi}^k; D) = d(\mathbf{t}_i^k, \mathbf{s}_{mi}^k) - d(\mathbf{t}_i^k, D(\mathbf{t}_i^k)), \quad (1)$$

211 where  $d(\mathbf{t}_i^k, \mathbf{s}_i^k) = \mathbf{s}_i^k - \mathbf{t}_i^k$  and  $D(\mathbf{t}_i^k) = \tilde{\mathbf{s}}_i^k$  is a corresponding point of  $\mathbf{t}_i^k$  defined by a pre-  
 212 computed disparity map  $D$ .

213 With this error metric (1), we can define an inlier set  $\hat{S}_i^k$  containing all reliable right tie-points,

$$214 \quad \hat{S}_i^k = \{\mathbf{s}_{mi}^k | \mathbf{s}_{mi}^k \in S_i^k, \mathbf{s}_{mi}^k \in C_m^k, \|e(\mathbf{t}_i^k, \mathbf{s}_{li}^k; D)\| < \delta \forall \mathbf{s}_{li}^k \in C_m^k\}, \quad (2)$$

215 where  $\delta$  is an error threshold which is normally set to around 10 pixels, and  $C_m^k$  is a set of right  
 216 tie-points collected by the  $m$ -th participant. Thus, an error bound of  $\mathbf{t}_i^k$  (denoted by  $\mathbf{b}_i^k$  in this  
 217 paper) can be defined as

$$218 \quad \mathbf{b}_i^k = \begin{bmatrix} \mathbf{m}_i^k \\ \boldsymbol{\sigma}_i^k \end{bmatrix} = \frac{1}{|\hat{S}_i^k|} \left[ \frac{\sum_i \mathbf{s}_{mi}^k}{\sqrt{\sum_i (\mathbf{s}_{mi}^k - \mathbf{m}_i^k)^2}} \right]. \quad (3)$$

219 As a general quality metric of a set of stereo measurements, we can also define a total  
 220 measurement error as

$$221 \quad e_{tot}(T^k, S^k: D) = \frac{1}{MN} \sum_i^M \sum_j^N \|d(D(\mathbf{t}_i^k), \mathbf{s}_{ji}^k)\|, \quad (4)$$

222 where  $S^k$  represents all measurements, i.e.  $S^k = \cup_i S_i^k$ . Similarly, we can also define a  
 223 measurement error of an inlier set and an outlier set, i.e.  $e_{in}(T^k, \hat{S}^k: D)$  and  $e_{out}(T^k, S^k -$   
 224  $\hat{S}^k: D)$ , respectively.

225

## 226 2.4 Assessment criteria

227 The proposed evaluation method basically assesses a disparity map in terms of matching score  
 228 (M) and rewarding score (R). A matching score is similar to the classic quality metric used in  
 229 stereo evaluation but the main difference is that our method evaluates it based on a set of error  
 230 bounds rather than ground truth. The proposed method also introduced a rewarding score. The  
 231 main purpose of this is to award more scores when an algorithm can cope well with challenging  
 232 matching problem defined in the discontinuous point selection.

233 In order to compute matching score, we define a 2D Gaussian function from an error bound. For  
 234 example, a scoring function for  $\tilde{\mathbf{s}}_i^k$  (i.e. the right pixel position of  $\mathbf{t}_i^k$  obtained from an input  
 235 disparity map for evaluation) is

236 
$$g(\tilde{\mathbf{s}}_i^k, \mathbf{b}_i^k) = \exp \left\{ -0.5 (\tilde{\mathbf{s}}_i^k - \mathbf{m}_i^k)^T \begin{bmatrix} \sigma_{xi}^2 & 0 \\ 0 & \beta \sigma_{xi}^2 \end{bmatrix}^{-1} (\tilde{\mathbf{s}}_i^k - \mathbf{m}_i^k) \right\}, \quad (5)$$

237 where  $\mathbf{b}_i^k$  is the error bound of  $\mathbf{t}_i^k$ ,  $\sigma_{xi}^2$  is the variance of the  $x$  values of the  $i$ -th tie-points in type  
238 (k) data set, and  $0 < \beta < 1$ .

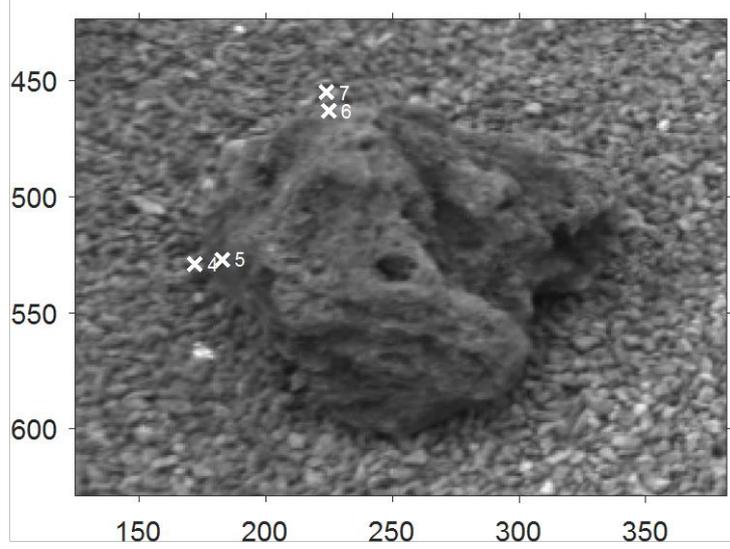
239 This means that we give a higher matching score when an input disparity is closer to the mean of  
240 inlier measurements. If a stereo selection is not confident (i.e.  $\sigma_x$  is high), then we penalise less  
241 even if a tie-point is further away from the mean. Another thing to note is that the covariance  
242 matrix in (5) is defined by a horizontal standard variance only, i.e.  $\sigma_{xi}$ . This is because  $\sigma_{yi}$  of  
243 manual measurements is nil as we rectify an input stereo pair for stereo measurement. However,  
244 to allow a little variation in  $y$  direction as some algorithms do refine vertical positions even if an  
245 input stereo pair is rectified, we have used  $\sigma_{yi} = 0.2\sigma_{xi}$  in our test. Please note that this weighting  
246 value was selected empirically based on our ALSC refinement results of the manual  
247 measurements.

248 A matching score of a set of right points from a disparity map is then defined as a weighted sum  
249 of (5), i.e.

250 
$$M(D, B) = \frac{1}{L} \sum_k \sum_i^{|T^k|} w_i g(\tilde{\mathbf{s}}_i^k, \mathbf{b}_i^k), \quad (6)$$

251 where  $L = |T^a| + |T^b| + |T^c|$ ,  $B^k$  is a set of all error bounds,  $D$  is a disparity map for evaluation  
252 which defines  $\tilde{\mathbf{s}}_i^k$ , and  $w_i = 1 - \frac{\sigma_{xi}}{2\max(\sigma_{x0}, \dots, \sigma_{xk})}$ , i.e. a higher weight is given to a more confident  
253 measurement.

254 The proposed rewarding score is defined for the tie-points at discontinuities (i.e. type (c)). As  
255 briefly explained earlier in Sec. 2.2. we have defined a pair of tie-points around object boundary.  
256 Supposing that  $P_i$  is the  $i$ -th pair of the discontinuous tie-points obtained around object boundary,  
257 we can define the  $i$ -th pair  $P_i = \{(\mathbf{t}_{2i}^c, \tilde{\mathbf{s}}_{2i}^c), (\mathbf{t}_{2i+1}^c, \tilde{\mathbf{s}}_{2i+1}^c)\}$  and an example of a pair can be found



258

259 Figure 3: Example of a pair of tie-points around object boundary, e.g.  $\mathbf{t}_5$  and  $\mathbf{t}_6$  are a pair of left  
 260 tie-points collected from background and foreground to evaluate rewarding score.

261

262 in Fig. 3. In this case, our rewarding function is defined as an averaged sum of sigmoid function  
 263 values, i.e.

$$264 \quad R(D, B, P) = \frac{1}{|P|} \sum_{i=0}^{|P|} \gamma(-|d(\mathbf{t}_{2i+1}^c, \mathbf{t}_{2i}^c) - d(\tilde{\mathbf{s}}_{2i+1}^c, \tilde{\mathbf{s}}_{2i}^c)|), \quad (7)$$

265 where  $\gamma(x)$  is a sigmoid function,  $\frac{2}{1+\exp(-x)}$ , and  $P$  is a set of all pairs of tie-points,  $P = \cup_i P_i$ .

266 Thus, (7) gives additional scores when a disparity map can give a similar estimation to the average  
 267 of manual measurements around a depth discontinuity.

268 Finally, a total score (TS) is defined as a weighted sum of the matching score and the rewarding  
 269 score, i.e.

$$270 \quad TS(D, B, P) = (1 - \alpha)M(D, B) + \alpha R(D, B, P), \quad (8)$$

271 where  $0 < \alpha < 1$ . The weighting coefficient in (8) can be set up differently depending on  
272 applications, e.g. a higher weight (e.g.  $0.5 < \alpha$ ) could be given to put the matching score ahead  
273 over the rewarding score of a disparity map.

### 274 **3. Experiment results**

275 The evaluation work described in this paper is based on the stereo matching results from UCL-  
276 MSSL, NASA-JPL, and the Joanneum Research Institute (JR hereafter) with respect to the  
277 datasets from the PRoVisG Mars 3D challenge and the ExoMars PanCam test campaigns. The  
278 PRoVisG Mars 3D challenge 2011, aimed at testing and improving the state of the art algorithms  
279 of visual odometry and 3D terrain reconstruction in planetary exploration.

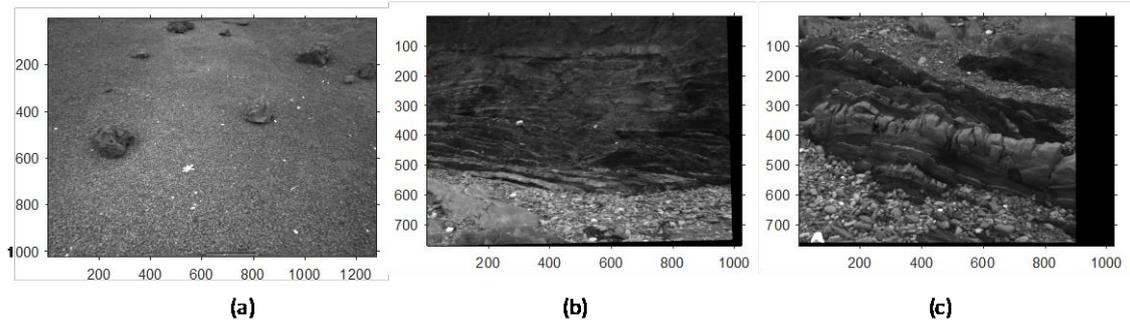
280 The task of the PRoVisG Mars 3D challenge was to reconstruct depth, camera trajectory and 3D  
281 maps of Mars landscapes observed by MER. The ExoMars PanCam test campaign also focused  
282 on the 3D processing results, as they are an essential component of mission planning and scientific  
283 data analysis for the ESA's ExoMars Rover mission, planned for launch in 2020.

284 We demonstrate the evaluation with 3 test sequences, taken from one of the PRoVisG Mars 3D  
285 challenge I datasets (sets C33) and the ExoMars PanCam test campaign (“65246” and “70000”).  
286 Examples of the images from each of these 3 test sequences are shown in Fig. 4. The evaluation  
287 work demonstrated in this paper was achieved through a workshop hosted at UCL-MSSL with 15  
288 participants including 9 students and 6 trainers.

289

#### 290 **3.1 Test datasets**

291 During this stereo matching evaluation workshop, the students were trained on how to use the  
292 StereoWS tool including the stereo display, manual measurements, and statistical analysis  
293 procedure. In this workshop, we have collected manual measurements, which were selected by  
294 different members of the workshop.



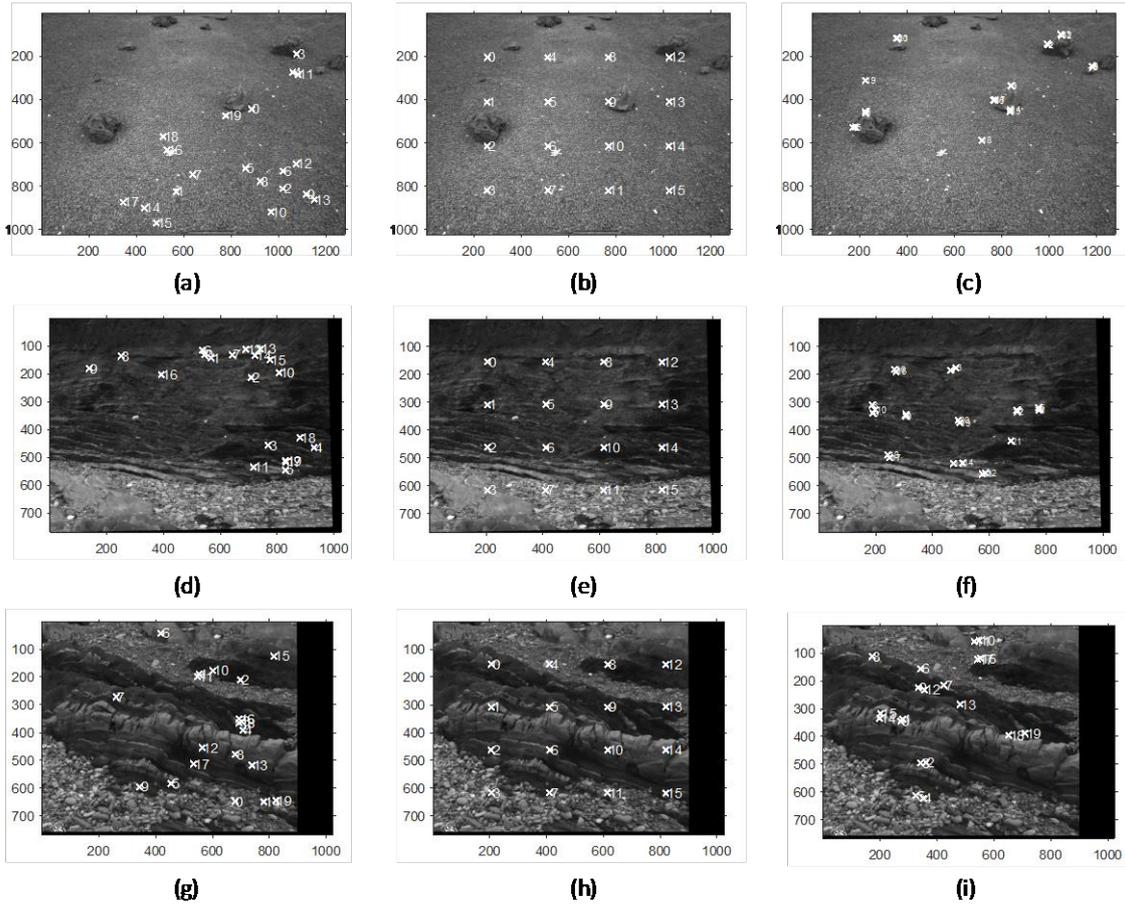
295

296 Figure 4: Test datasets from PProVisG Mars 3D Challenge and ExoMars PanCam Test Campaign,  
 297 showing left-eye images randomly picked from each test dataset; (a) C33 (b) 65246 (c) 70000.

298

299 During the manual measurement process, each participant was asked to collect 20 feature based  
 300 points, 16 regular grid points, and 10 discontinuity tie-points for each pair of test images shown  
 301 in Fig. 4. Figure 5 illustrates an example of left tie-points of some of the test images (i.e. C33,  
 302 65246, 7000) prepared for measurement.

303 For the feature based tie-points (see the first column of Fig. 5), participants only needed to identify  
 304 the corresponding right points using the stereo display. 20 left points are selected from the  
 305 extracted Scale Invariant Feature Transform (SIFT) key-points (Lowe, 2004) with the highest  
 306 matching similarity values. For the regular grid tie-points (see the second column of Fig. 5), we  
 307 collected 16 left points from the dense disparity map generated by our in-house GOTCHA  
 308 matcher. Participants were then asked to validate their matching correctness based on visual clues  
 309 by moving the stereo 3D cursor around the grid points to check if there were any abnormalities  
 310 and adjusting the disparity offset of the stereo cursor at certain points to seek for better solutions.  
 311 Results in this case that passed the validation were collected and averaged. For discontinuity tie-  
 312 points (see the last column of Fig. 5), an expert user from the workshop manually selected 10  
 313 pairs of left points around the object edge and other problematic areas. 9 pairs of discontinuity  
 314 tie-points are defined around an object boundary in C33, whilst the last two tie-points are selected



315

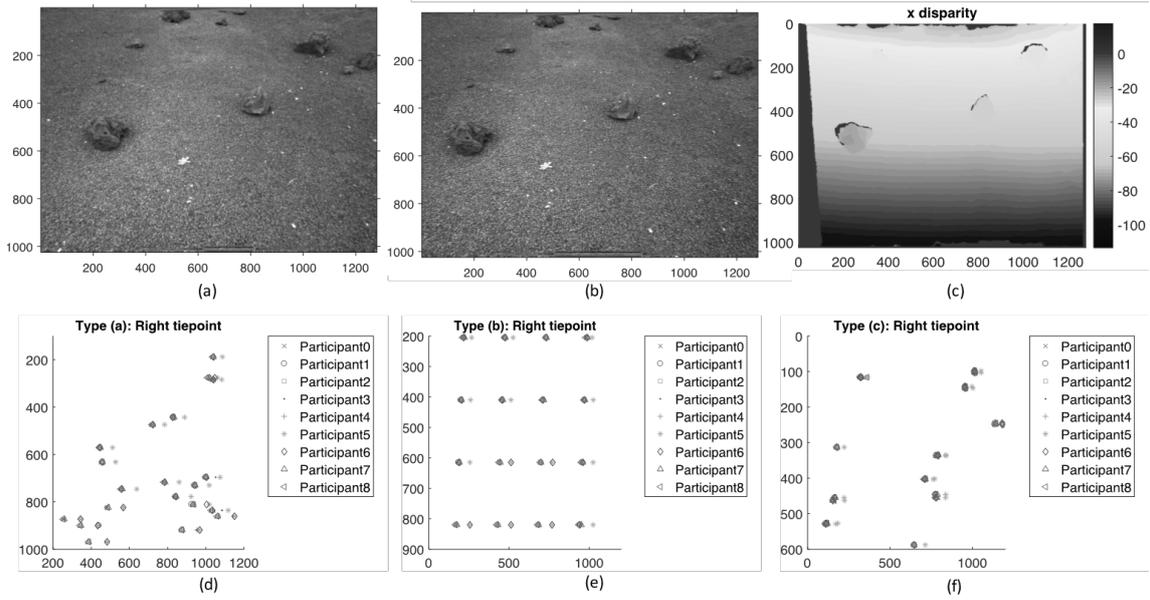
316 Figure 5: Example of left tie-points used in the stereo workshop: (a), (d), and (g) show 20 left tie-  
 317 points defined on the test images shown in Fig. 4(a), (b), and (c), respectively; (b), (e), and (h)  
 318 show 16 regular grid tie-points for the same test images; (c), (f), and (i) are for 20 tie-points  
 319 around discontinuities.

320

321 from a relatively smooth and less-textured area. [see Fig. 5(c)]. Other workshop participants then  
 322 defined the correspondences on the right image.

323

### 324 3.2 Evaluation of collected tie-points



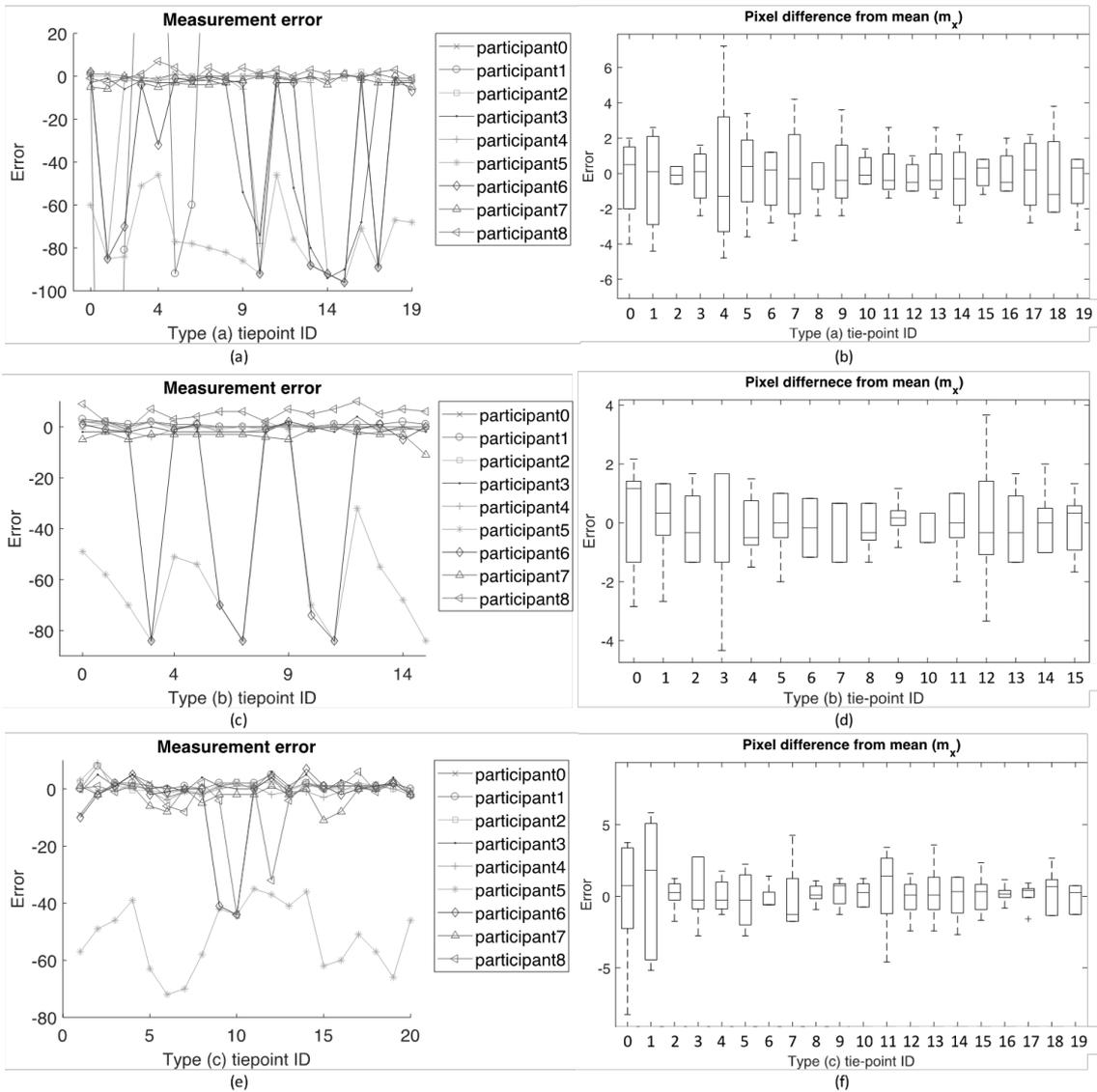
325

326 Figure 6: Example evaluation results of manual selection: (a) and (b) left and right input image  
 327 of C33; (c) a disparity map of (a) produced by UCL which was used to identify outliers in manual  
 328 measurements; (d), (e), and (f) show all measured right tie-points for type (a), (b), and (c),  
 329 respectively.

330

331 The manual selection results from the 9 workshop participants are presented in Fig. 6, where input  
 332 data are shown in the first row, whilst the positions of measured right tie-points are presented in  
 333 the second row.

334 It appears that some of the workshop participants can perform good visual identification and  
 335 visual validation with all three types of tie-points. On the other hand, a few workshop participants  
 336 were not good at fusing the stereo images. For example, participant 1, participant 3, participant 5,  
 337 participant 6 were not able to select good right points for the feature based tie-points [see Fig.  
 338 7(a)], and the performance of participant 5, participant 6, participant 8 was particularly worse  
 339 with discontinuity tie-points [see Fig. 7(e)]. Their average measurement error (i.e.  $e_{out}$ ) is 16.65  
 340 pixels which is significantly above the error bounds from a normal visual identification and  
 341 validation results. Their performance was improved when a pre-computed disparity map is given



342

343 Figure 7: Example of evaluation of manual measurements of C33: (a), (c), and (e) simple  
 344 measurement error from (1) of type (a)-(c) tie-points, respectively; (b), (d), and (f) show bar charts  
 345 of difference between inlier measurements and  $m_x$

346

347 although two participants still cannot visualise the tie-points in 3D, i.e. Participants 5 and 6 [see  
 348 Fig. 7(c)]. These outliers were then removed before calculating the error bounds.

349 Figure 7(a), (c), and (e) summarise the errors from the inlier means  $d(t_i^k, m_i^k)$  of all tie-points  
 350 from 9 participants. It is observed that tie-points from the indistinctive textures are generally

351 difficult to select, for example,  $t_1^a$ ,  $t_4^a$ ,  $t_5^a$ ,  $t_7^a$ , and  $t_9^a$  in the feature based tie-points have larger  
 352 measurement variation and more outliers [see Fig. 7(b)]. This reconfirms our understanding that  
 353 a stereo visualisation can help us detect correct tie-points better around the object boundary than  
 354 within plain/repetitive texture.

355 One interesting observation from the error graph is that the performance of participant 5, who  
 356 consistently produced a large measurement error regardless of the type of dataset, deteriorates  
 357 when a tie-point is closer to a camera (i.e. a larger  $x$  disparity). For example, the measurement  
 358 errors for  $t_3^b$ ,  $t_7^b$ ,  $t_{11}^b$ , and  $t_{15}^b$  (which is the bottom row of the grid in Fig. 5(b)) are getting worse  
 359 than the rest and we can see this pattern in Fig. 7(c).

360 The error metrics of measurements are evaluated and summarised in table 1. Without the removal  
 361 of outliers, the total measurement error increases significantly. The maximum of  $e_{tot}$  was  
 362 recorded with the feature based tie-points (20.83), whereas the minimum (8.39) was obtained  
 363 from the discontinuity tie-points. However, after removing obvious outliers (i.e.  $\delta > 10$  in (2)),  
 364 the measurement errors drop sharply to less than 2 pixels with small standard variation (see  $e_{in}$   
 365 and avg.  $\sigma_x$  in table 1). As mentioned earlier, we believe this happens because of the outliers  
 366 introduced by a few participants who fuse a stereo pair differently than the rest.

367 Table 1 Measurement errors of C33 (N.B. the Type (a) results of participant 2 was excluded due  
 368 to the incomplete of measurements.)

Type	$e_{tot}$	$e_{in}$	$e_{out}$	avg. $\sigma_x$
<b>a</b>	20.83	1.61	40.04	0.92
<b>b</b>	10.83	1.10	22.98	1.71
<b>c</b>	8.39	1.78	16.65	0.93
<b>avg.</b>	13.35	1.50	26.56	1.19

369

370 The bar charts of the inlier measurements for 3 datasets are shown in the second column of Fig.  
 371 7. Each bar chart summarises the differences between the inlier measurements and the mean of  
 372 the inlier measurements. Type (b) tie-point selection appears to be more difficult as participants

373 are often required to fuse the stereo cursor around textureless or smooth (i.e. small depth  
374 separation) areas. As a consequence, the inlier measurements of regular grid tie-points are  
375 generally inconsistent (i.e. avg.  $\sigma_x = 1.71$ ) compared to the others [see Fig. 7(d)]. On the other  
376 hand, strong depth discontinuity around an object boundary from type (c) tie-points improve the  
377 consistency of the measurements [see Fig. 7(f)]. We have found that the maximum standard  
378 deviation is 2.56 pixels, the minimum standard deviation is 0.37 pixels, and the average is 0.93  
379 pixels.

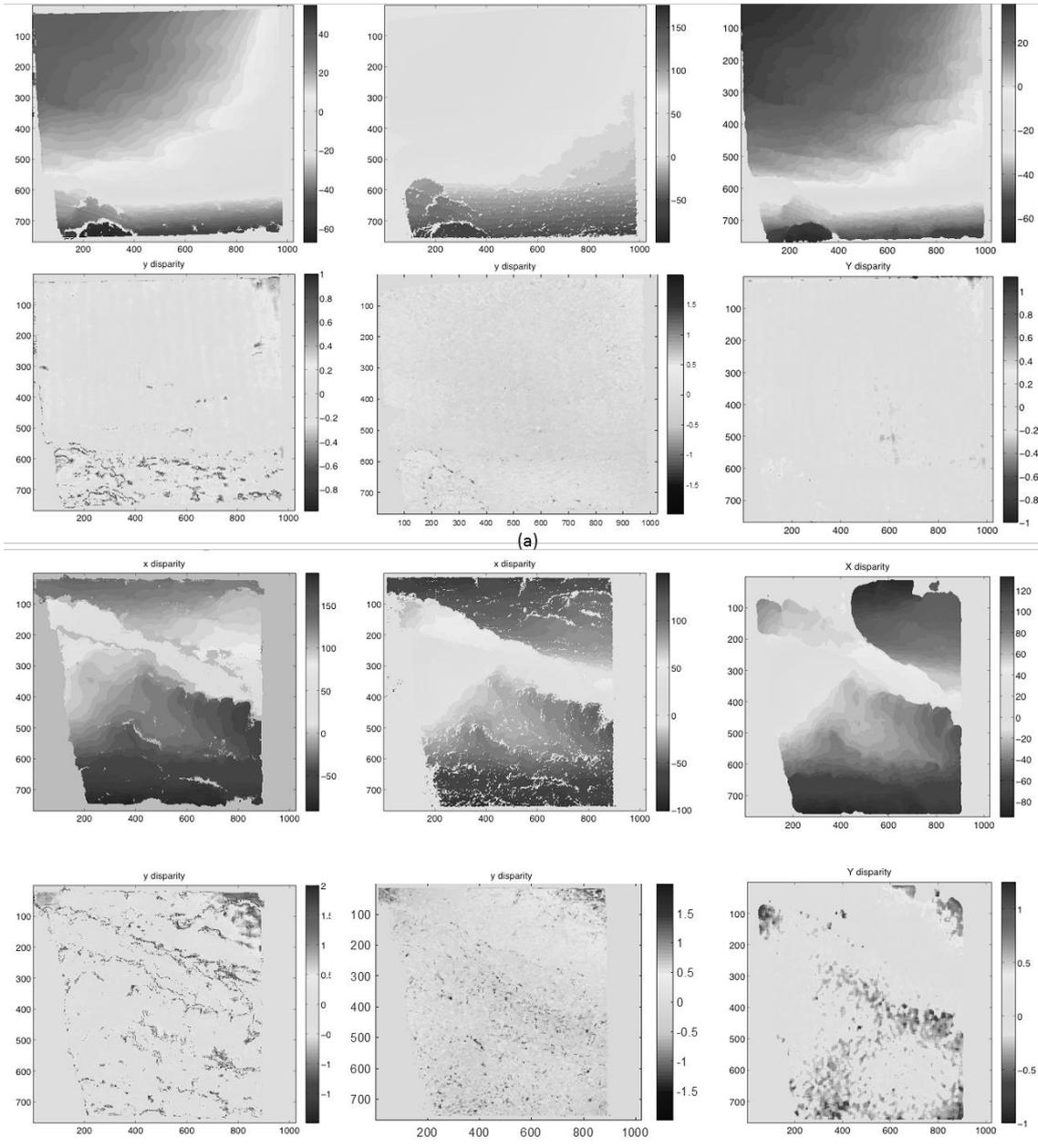
380 It is also interesting to see that SIFT keypoints performs the best for stereo fusion. Its average  
381 standard deviation is 0.92 which is marginally better than the second best but the left tie-points of  
382 type (a) were selected simply based on the texture information [see Fig. 7(b)]. We think that the  
383 distinctive gradient information around a keypoint can improve the performance of stereo  
384 measurements.

385

### 386 **3.3. Results of automated stereo matching**

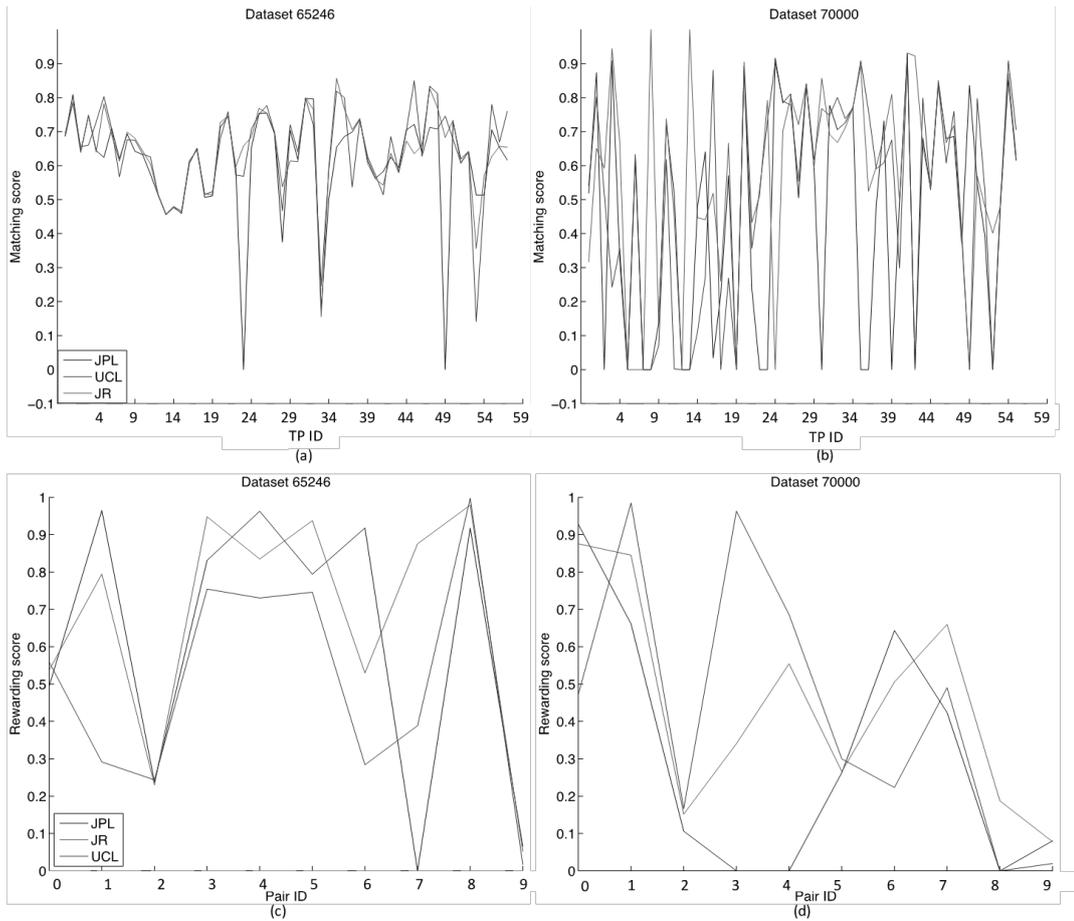
387 In our evaluation, we have collected two sets of processing results (i.e. a  $x$  and  $y$  disparity map)  
388 from UCL, JPL, and JR. Fig. 8(a) and (b) respectively represent these disparity maps of dataset  
389 65246 and 70000 from ExoMars PanCam Test Campaign, and each column of the figure  
390 represents the results from different organisations. To our best knowledge all three algorithms  
391 have been developed based on a variation of a correlation based stereo matching algorithm with  
392 an adaptive least square fitting technique (Deen and Lorre, 2005; Otto and Chau, 1989), but all  
393 results seem to be slightly different in terms of the completeness and the estimated values of a  
394 disparity map. All three results were able to produce a relatively denser disparity map with dataset  
395 65246. However, the results seem different with the other dataset, e.g. the JR result shown in the  
396 last column of Fig. 8(b) looks overly smoothed and its density is more incomplete than the other

397 two (but this does not mean it is sparse). Please also note that both  $y$  disparity maps from JPL  
 398 (see the second column of Fig. 8) contains a few spikes which are removed for visualisation.



399

400 Figure 8: Example of disparity maps: (a)  $x$  and  $y$  disparity maps of dataset 65246; (b) and dataset  
 401 70000. UCL, JPL, and JR results are shown in the first, the second and the last column.



402

403 Figure 9: (a) Individual matching scores of the processing results of two datasets; (b) Rewarding  
 404 scores from 10 tie-point pairs in two datasets.

405

406 Given the error bounds calculated from the manual measurements, the matching scores and  
 407 rewarding scores of each tie-point are evaluated and the results are shown in Fig. 9. Matching  
 408 scores of three algorithms are generally similar when they can define a tie-point, but when it fails  
 409 to define a tie-point no score was awarded, e.g. see JPL matching scores of ID 23 and 49 in Fig.  
 410 9(a). The rewarding score of UCL's disparity map is generally lower than the other two with the  
 411 dataset 65246 [see Fig. 9(c)]. However, it is improved with the other dataset having more depth  
 412 discontinuities.

413 The total scores were calculated using an equal weight of the matching scores and rewarding  
 414 scores, and the results are summarised in table 2, where the best scores for certain datasets are  
 415 labelled in bold font. We can observe that for dataset 65246 that JR's stereo matching pipeline  
 416 produced the best result for the overall area. To understand this result clearly, it is worth  
 417 mentioning that the total score (TS) shown in (8) has been designed to award more scores if a  
 418 disparity map defines all queried tie-points; in other words, no score is given if there is no  
 419 corresponding tie-point in a disparity map. Thus, this metric is generally favoured for a dense and  
 420 smooth disparity map, which we believe why JR's results perform best on both test datasets.

421 Table 2: Total score (TS) estimated from (8) with  $\alpha = 0.5$

Dataset	65246			70000		
	UCL	JPL	JR	UCL	JPL	JR
Matching score	63.96	61.26	64.16	50.45	45.15	57.01
MFR(%)	0.00	3.50	0.00	16.10	26.80	10.70
Rewarding score	50.11	61.87	67.15	43.07	31.05	44.64
MFR(%)	0.00	10.00	0.00	10.00	30.00	0.00
<b>TS</b>	55.65	61.63	<b>65.95</b>	46.02	36.69	<b>49.59</b>

422

423 To give more weight on the accuracy of an algorithm, we modified (8) not to penalise when they  
 424 failed to define a queried tie-point in a disparity map, and called this score, TS-B. The results of  
 425 TS-B of both datasets are also presented in table 3.

426 Table 3: Total score B (TS-B) which is similar to TS but removes the effect of missing tie-points

Dataset	65246			70000		
	UCL	JPL	JR	UCL	JPL	JR
Matching score	63.96	63.45	64.16	60.11	61.67	63.86
Rewarding score	50.11	68.75	67.15	47.85	44.35	44.64
<b>TS-B</b>	55.65	<b>66.63</b>	65.95	<b>52.75</b>	51.28	<b>52.33</b>

427

428 We also introduce a new term MFR representing the Matching Failure Rate. MFR can be used as  
429 an indicator for either the incompleteness of a disparity map or how conservative the algorithm  
430 is. As shown in table 2, JPL's results have higher MFR, but without counting on the match failure  
431 area (i.e. using TS-B) JPL's pipeline produced the best result on the dataset 65246. For dataset  
432 70000, JPL's pipeline gets the second best score whilst UCL's processing pipeline has produced  
433 the best accuracy.

434

#### 435 **4. Discussions and Conclusions**

436 In this paper, we introduced an accuracy evaluation method to assess the stereo matching results.  
437 The main motivation of this work is to provide a straightforward method which can be applied to  
438 the stereo matching evaluation work of planetary rover missions, where it is currently impossible  
439 to obtain ground truth data.

440 We have demonstrated the use of a generic portable stereo workstation including a stereo cursor  
441 from the open source StereoWS tool to produce visually correct tie-points of a stereo pair, i.e.  
442 manual tie-points, with the help of a softcopy stereo display. The manual tie-points from stereo  
443 measurements are not identical for all candidate tie-points, but our assumption is that the variation  
444 of multiple measurements can be used to estimate the confidence of a tie-point and this confidence  
445 values can quantitatively evaluate the quality of disparity maps from different algorithms. Based  
446 on this idea, we have defined useful evaluation metrics using the statistics of multiple  
447 measurements (such as means and variance). We also define three types of tie-points to test the  
448 performance at highly textured region, textureless region, and occluded region. The performance  
449 of textureless region is quite interesting for DTM construction from orbital imagery but this is left  
450 for the future work. Type (b) tie-points are related to the scene occlusion. At the moment, we  
451 populate these points manually but it is also possible to design a semi-automatic pipeline to collect

452 these points, e.g. detect one tie-point by conventional feature detector and find adjacent feature  
453 from background manually.

454 It is worth noting that in these experiments, the number of tie-points, particularly for the  
455 discontinuities, may not be sufficient in some cases. It would have been better to add more tie-  
456 points. However, we erred on the side of setting an experiment which could be accomplished with  
457 a group of ten “citizen scientists” within a limited time period (a week). Other comparison results,  
458 e.g. disparity density or 3D accuracy, could also be employed in future experiments to improve  
459 the final matching score.

460 During the evaluation work, we implemented an open source stereo workstation with an  
461 integrated stereo matching method that is used to produce the UCL results shown in the  
462 evaluation. We have published the Java code of the Stereo Workstation on SourceForge under a  
463 BSD license (available from SourceForge, <http://sourceforge.net/projects/stereows/>) to encourage  
464 other stereo researchers to use and modify our system for their own evaluation.

465 The experiments reported in this paper focused on planetary images. It would be straightforward  
466 to apply this method and our StereoWS to any future stereo research projects when any  
467 quantitative evaluation is required, wherever it is on Mars or the Earth or anywhere else for that  
468 matter. In the future, we hope our efforts could also benefit the stereo correspondence evaluation  
469 work and include more datasets, in particular the results from a wider variety of general stereo.  
470 Also, we expect that the same idea behind StereoWS could be applied to develop a more intuitive  
471 and immersive stereo measurement system using recent virtual reality technologies. In  
472 conjunction with the stereo measurement workshop held in 2011, we can provide the possibility  
473 of evaluation of these stereo matching results including more methods from our collaborators.

474 As future work, it is also interesting to investigate the performance of manual measurements from  
475 different lighting conditions (Kirk et. Al., 2016). We could measure the variation of human depth

476 perception under different illumination effects and reflect this on (5) to define more accurate  
477 metrics. However, this is currently beyond our research scope and left for the future work.

478

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