

# Automatic segmentation of right ventricle in cardiac cine MR images using a saliency analysis

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(Dated: 13 October 2016)

## Purpose:

Accurate measurement of the right ventricle (RV) volume is important for the assessment of the ventricular function and a biomarker of the progression of any cardiovascular disease. However, the high RV variability makes difficult a proper delineation of the myocardium wall. This paper introduces a new automatic method for segmenting the RV volume from short axis cardiac magnetic resonance images by a salient analysis of temporal and spatial observations.

## Methods:

The RV volume estimation starts by localizing the heart as the region with the most coherent motion during the cardiac cycle. Afterwards, the ventricular chambers are identified at the basal level using the isodata algorithm, the right ventricle extracted and its centroid computed. A series of radial intensity profiles, traced from this centroid, is used to search a salient intensity pattern that models the inner-outer myocardium boundary. This process is iteratively applied towards the apex, using the segmentation of the previous slice as a regularizer. The consecutive 2D segmentations are added together to obtain the final RV endocardium volume that serves to estimate also the epicardium.

## Results:

Experiments performed with a public data set, provided by the RV Segmentation Challenge in Cardiac MRI, demonstrated this method is highly competitive with respect to the state of the art, obtaining a Dice score of 0.87, a Hausdorff distance of 7.26 mm while a whole volume was segmented in about 3 s.

## Conclusions:

The proposed method provides an useful delineation of the RV shape using only the spatial and temporal information of the cine MR images. This methodology may be used by the expert to achieve cardiac indicators of the right ventricle function.

Keywords: cardiac cine MR images, heart, profiles, shape and motion analysis

## I. INTRODUCTION

Cardiovascular disease (CD) remains the largest global cause of death, with 17.3 million fatalities per year worldwide<sup>1,2</sup>. This number is expected to rise up to 23.6 million by 2030 due to the influence of factors and habits associated with modern life such as smoking, physical inactivity, obesity, diabetes and stress. The elevated incidence and prevalence of this disease have triggered the alarms of most public health systems which, in consequence, have designed policies oriented to reducing the burden of this disease. Despite these endeavors, many of the CD sufferers will eventually undergo complex treatments aiming to preserve the maximum of cardiac function.

Due to its crucial role in the management of the acute phase of CD, the assessment of the cardiac function dynamics of the left ventricle (LV) has been thoroughly studied<sup>3-5</sup> whereas the role of the right ventricle (RV) has been considered as purely passive. The latter's role has been recently re-evaluated based on evidence

that suggests that any LV failure will overload the RV and, therefore, alters its dynamics<sup>6-11</sup>. Nowadays, the RV function constitutes an important biomarker of the progression of any cardiac disease as well as a sensitive prognosis indicator<sup>6</sup>.

Since subtle alterations of the right ventricle are practically undetectable in a conventional electrocardiogram, great attention has been paid to different imaging modalities<sup>12-16</sup>. Among these methods, anatomical structures are more clearly visualized with magnetic resonance (MR), during a complete cardiac cycle<sup>7,12,17</sup>, i.e., the cardiac chambers and their temporal motion patterns, from which different functional indexes can be computed and integrated to several clinic scenarios. However, quantification of the cardiac cycle requires accurate segmentation of the heart chambers. When performed manually, this process takes around 19 minutes per case<sup>18</sup> and presents high inter-observer variability<sup>19-21</sup>.

Semi-automatic and automatic approaches have been developed to obtain accurate and fast RV segmentations<sup>18,22</sup>. Unfortunately, the complex and highly variable anatomical nature of RV make these tasks very difficult. Additionally, the presence of blurry edges

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may mislead the segmentation algorithm, particularly at the apex level of the ventricle, where the reduced blood flow may result in a non identifiable cavity. In this last case observers are not able to accurately identify nor trace the RV contour. A robust algorithm which is able to overcome these challenges is still not available.

In this paper, a computational framework is proposed to segment the RV volume in short axis (SAX) cine cardiac MRI. The basis of the framework is a simple saliency analysis of the heart which, sequentially and hierarchically, refines the location of the RV. The process can be explained in the following three steps:

First, a **Coarse heart localization**, which locates the region with maximal motion that is known to include all the cardiac structures, reducing the examination area to a region of interest (ROI) that excludes neighboring organs which are not of interest for the present task.

Second, an **Endocardium segmentation**, by far the most complex and error-prone step, is further divided into four sub-tasks:

- **Basal ventricle separation**, done within the ROI by a simple threshold over the grayscale intensity calculated with the isodata algorithm<sup>23</sup> and *a priori* knowledge about the LV/RV spatial relationship.
- **Basal Endocardium delineation**, done by searching along the intensity profiles radiating outwards from the centroid of the RV, for the segments that correspond to the inner-outer myocardium boundary. The selected boundary is the profile segment which best matches a **shape prior**, in this case an upward opening parabola.
- **Basal endocardium refinement**, by which boundary point outliers are detected and removed and the contour is smoothed.
- **Propagation of the basal segmentation towards the apex**, computed by repeating the endocardium delineation process in the more apex-wise slices. Previous results, from more basal slices, are used to guide the search.

Third, an **Epicardium estimation**, by dilating the obtained endocardium volume. The method was validated using a cardiac MR data set of 48 subjects provided by the MICCAI 2012 RV Segmentation Challenge in Cardiac MRI (RVSC)<sup>22</sup>. In addition, the proposed strategy was qualitatively assessed on different database, the Sunnybrook Cardiac Data from a 2009 Left Ventricle Segmentation Challenge.<sup>24</sup>.

This paper describes an accurate and fast segmentation of the right ventricle. The method shows high correlations with clinical indexes calculated by manual delineation and demonstrates generalization at obtaining proper segmentations on a second public dataset (LV Segmentation Challenge). Unlike thresholding methods, this approach detects the ventricular wall using

exclusively a local intensity model of the ventricles, i.e., instead of taking a global threshold, the algorithm finds out the local patterns that characterize the ventricular wall and sets the particular inner-outer thresholds. An exhaustive radial wise search of this pattern is adapted for each region of the ventricle. As a result, this method does not require a training dataset and is competitive enough in terms of velocity and accuracy. Three main novelties of this method are

1. The exploitation of the temporal information drastically reduces the search of the right ventricular patterns.
2. The RV segmentation is based on a salient model of the ventricular intensity that determines the most probable locations of the inner-outer chamber boundary at a local level
3. the method is also globally regularized by the shape of the ventricle when propagating the first segmented region, the basal slice towards the apex, using always the precedent contour.

The paper is organized as follows: A background of the RV segmentation methods in cardiac MRI is briefly reviewed in Section II. In Section III, the proposed RV volume segmentation approach is described. The experiments and results are provided in Section IV. Finally, discussions and conclusions about the proposed method and associated results are presented in Section V and Section VI respectively.

## II. BACKGROUND

Previous attempts to solve the challenges associated to segmentation of the RV, can be divided into two groups. A first group is the set of methods that need prior information such as multi-atlas based strategies, statistical models and prior propagation. Multi-atlas methods<sup>25–28</sup> register a target case with an atlas database of annotated cardiac images and then somehow fuse annotations of the most similar cases. The registration uses intensity similarity measures and requires to ensure one-to-one correspondences between the target case and the atlas database. These strategies have reported good accuracy results (see Petitjean and Dacher for RV segmentation) as long as the registration ensures a deformation that preserves the topology of the heart structures. As these methods are fully dependent on the variability collected in the database, they may fail when the cardiac structures are very different from the pattern stored in the database. Finally, these methods are computationally very expensive. Statistical models<sup>29,30</sup>, similarly to atlas-based approaches, require priors as certain type of pre-defined structures or particular appearances that built up a model to be matched to the target. Statistical models have the advantage of providing a compact representation of the shapes within

183 a training set. However, as atlas-based methods, they<sup>234</sup>  
 184 need a large number of samples to capture the RV<sup>235</sup>  
 185 shape variability. On the other hand, prior propagation  
 186 methods<sup>31,32</sup> start by a manual segmentation that  
 187 is propagated to the rest of the cardiac structure.  
 188 Nevertheless, a proper RV segmentation may be affected  
 189 by the intrinsic expert variability and the inevitable error  
 190 propagation.

191 The second group includes models that need not  
 192 require prior information. They apply processing  
 193 techniques directly on the image. Among them, Wang,  
 194 Peng, and Chen obtained a coarse heart segmentation  
 195 applying an isodata algorithm after selecting the RV<sup>236</sup>  
 196 shape as the pixels with more motion, a descriptor that<sup>237</sup>  
 197 failed when the RV edges were fuzzy. Ringenberg *et al.*<sup>238</sup>  
 198 combined a window-constrained accumulator threshold<sup>239</sup>  
 199 method, difference of Gaussians, optimal threshold and<sup>240</sup>  
 200 morphological operators to segment the RV shape.<sup>241</sup>  
 201 Mahapatra and Buhmann segmented the RV shape by  
 202 extracting semantic information using a trained Random  
 203 Forest classifier. The principal problem with these,<sup>242</sup>  
 204 approaches is that they require a large number of<sup>243</sup>  
 205 parameters to be tuned and therefore a huge number of<sup>244</sup>  
 206 cases.<sup>245</sup>

207 The method herein proposed is part of this second<sup>246</sup>  
 208 category, i.e., without prior information, furthermore<sup>247</sup>  
 209 with the advantage of an appropriate estimation of the<sup>248</sup>  
 210 RV volume with only a few parameters and therefore a<sup>249</sup>  
 211 low computational cost.<sup>250</sup>

### 212 III. METHOD

213 The proposed approach segments the RV from SAX<sup>252</sup>  
 214 images using a cardiac cine MRI and quantifies the<sup>253</sup>  
 215 RV volume for the whole cycle. The method can<sup>254</sup>  
 216 be summarized in three steps: (1) A coarse heart<sup>255</sup>  
 217 localization by determining the region with more<sup>256</sup>  
 218 motion, reducing the RV search to a smaller region of  
 219 interest (ROI); (2) segmentation of the right ventricular  
 220 endocardium borders by performing a 2D hierarchical  
 221 delineation from basal to apex directions at each time of  
 222 the cardiac cycle; and (3) estimation of the epicardium  
 223 contour by dilating the obtained endocardium volume.

224 All images are pre-processed by remapping intensity  
 225 values of the slices into the full intensity range  $[0, 255]$ <sup>36</sup>.  
 226 These contrast improved images are smoothed with a  
 227 simple Marr-Hildreth operator<sup>37</sup>, i.e., the convolution of  
 228 the Laplacian of the Gaussian kernel and the original  
 229 image.

#### 230 A. Coarse Heart Localization

231 The structures surrounding the heart can be excluded<sup>258</sup>  
 232 from the segmentation process by limiting the ROI to<sup>259</sup>  
 233 that containing pixels with maximal motion during the<sup>260</sup>

whole cycle. This insures an area large enough to contain  
 all the cardiac structures.

The cardiac motion is estimated by computing  
 a saliency map that mimics the center-surround  
 principle<sup>38–41</sup> described for the human visual system, i.e.,  
 local features define a level of saliency by their differences  
 with their surroundings. To do so, an estimation of the  
 motion changes per slice  $\xi$  is achieved by computing the  
 temporal variations as follows. Given

$$C(\xi) = \{\hat{I}_{t=1}^{\xi}, \hat{I}_2^{\xi}, \hat{I}_3^{\xi}, \dots, \hat{I}_N^{\xi}\},$$

where  $C$  is the temporal sequence of the smoothed images  
 $\hat{I}$  of a slice location  $\xi$ . The slice  $\xi$  at the time  $t$  changes  
 with respect to rest of the cycle and  $\Delta_t^{\xi}$  stores these  
 differences, i.e., this is the set of differences between the  
 image  $\hat{I}_t^{\xi}$  at the time  $t$  and the image  $\hat{I}_k^{\xi}$  at any other  
 time  $k$

$$\Delta_t^{\xi} = \left\{ \delta_t^k = |\hat{I}_t^{\xi} - \hat{I}_k^{\xi}| : k = 1, 2, \dots, N \right\} \quad \forall t = 1, 2, \dots, N \quad (1)$$

Once these differences are calculated, a grid of patches  
 (each of  $5 \times 5$  pixels) is superimposed to each  $\delta_t^k$  and  
 the entropy  $H$  is calculated for every patch  $p$ . The  
 local motion estimation is obtained by the sum of local  
 entropies of the same patch along the temporal series of  
 differences  $\Delta_t^{\xi}$ . Higher entropies represent more motion  
 and therefore, higher saliency. The motion saliency map  
 ( $MSM$ ) is defined as

$$MSM(\xi)_{t,p} = \sum_{k=1}^N H(|\Delta_t^{\xi}(\delta_{t,p})|) \quad (2)$$

Finally, a binary 2D ROI enclosing the heart for the  
 slice  $\xi$  at each phase of the cardiac cycle is obtained  
 after applying a simple Otsu threshold<sup>42</sup> to the  $MSM(\xi)_t$   
 and filling the remaining holes in this binary image, as  
 illustrated in Fig. 1.



FIG. 1. Coarse heart localization. The left panel displays the  
 obtained motion saliency map (MSM), the center panel shows  
 the binarized MSM, and the right panel shows the final ROI  
 obtained after filling the binary image holes.

#### 237 B. Endocardium segmentation

The RV's wall shape depends strongly on the nature of  
 the cardiac pathology and on the patients' characteristics  
 resulting in a high variability in thickness and structure.

Consequently, the delineation of the outermost layer of the RV is usually difficult due to the wall's thickness and the superimposed epicardium fat<sup>43</sup>. Because of this, the proposed algorithm locates the innermost RV layer first and then uses it to guide the segmentation of the RV's outer layer.

The first part of this process consists in delineating the basal slice.

## 1. Basal ventricle separation

Overall, the RV at the basal level is well defined and can be solved as a straightforward segmentation task. At this position, the diastolic and systolic phases represent a large percentage of the whole volume and their segmentation can be used as a starting point for the delineation of the rest of the RV volume, which is independently performed for each phase of the cardiac cycle.

The estimation of the RV boundaries at the basal slice is carried out by a hierarchical approach:

Initially, the ventricular chambers are identified using the isodata algorithm<sup>23</sup> within the ROI (Fig. 2, left panel). The thresholded image suppresses the myocardium and preserves the cardiac cavities. An opening morphological operation reduces the noise of the resultant binary image. The structures of interest, the cardiac chambers, are then selected as the two largest structures that are close the ROI's center of gravity, as illustrated in mid panel of Fig. 2. The obtained coarse ventricular segmentation is displayed in right panel of Fig. 2

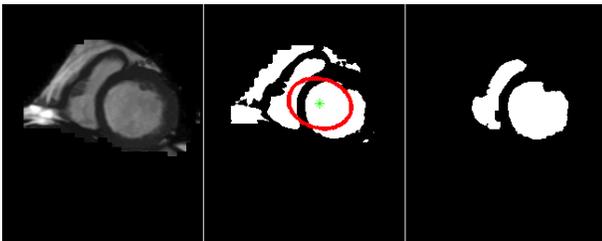


FIG. 2. Localization of the two cardiac chambers, left panel shows the MR image within the ROI. Mid panel illustrates the isodata segmentation and the center of gravity (in green). The two largest structures intersecting an ellipse concentric with the center of gravity are selected. Right panel displays the coarsely segmented ventricles.

## 2. Basal endocardium delineation

Even in the noisier conditions, a trained eye reconstructs a salient version of the myocardium tissue as a thick closed curve. In a polar space  $(r, \theta)$ , with the curve center as reference, this salience can be inferred

if similar intensity radial patterns are observed for neighboring angles. The core of the present work is supported on this observation and after a coarse version of the left and right ventricles is set, the RV boundary is estimated by searching similar patterns in the polar frame defined by the centroid of the initial estimated cardiac chamber.

The myocardium boundary is found out by analyzing the intensity profile along a ray traced from the coarse RV centroid, as illustrated in the top panel of Fig. 3. The lower panel of Fig. 3 shows the intensity profile of such ray. Observe how a first interval of this profile (from 0 to  $a$ ), with little intensity variation, is followed by a second segment (from  $a$  to  $b$ ) that resembles an upward opening parabola. This pattern is formed by the intensity drop produced when the ray crosses the inner endocardium and the subsequent rise when the ray reaches the outer epicardium (from  $(a, a')$  and  $(b, b')$  of the lower panel). These points are easily determined as the major changes of the derivative around the parabola minimum  $((f, f'))$ . As the range of intensities defined by each of these two ordinates ( $a'$  and  $b'$ ) is different, the analysis is performed using the inner parabola branch (from  $(a, a')$  to  $(f, f')$ ) since this boundary is always observed. Assuming the wall ventricle intensities are Gaussian distributed and the mean corresponds to the darkest intensity  $f'$ , it is then reasonable to suppose that the major concentration of dark intensities is within the interval defined by the first standard deviation of the Gaussian, about 68% of the probability mass. Such value corresponds to the intensities between  $f'$  and  $m'$ , being  $m'$  the 32% of the segment between the minimum  $f$  and the branch maximum  $a'$ , obviously corrected by  $f'$ . The resultant parabola, shown in blue at the lower panel of Fig. 3, is defined then by three control points ( $cp$ ): the vertex at the minimum intensity value  $(f, f')$  and the two branch points defined at  $(m, m')$  and  $(n, m')$ .

There are of course variations from this simple pattern, with the three most common variations illustrated in Fig. 4:

- The simplest pattern is displayed in the top panel of Fig. 4. In this case the three control points are easily determined in the single parabola present. This pattern is characteristic of cardiac images with low noise.
- Center panel in Fig. 4 shows a radial intensity profile with a unique decay (half parabola), usually observed when the epicardium border is blurred or noisy. In this case the criterion is relaxed and only half of the parabola, the one on the endocardium side, is matched with the intensity profile. The epicardium boundary is assumed to be symmetric on the missing (dashed) side.
- Other structures with a similar composition to the myocardium may appear, particularly in pathological conditions. These tissues may appear

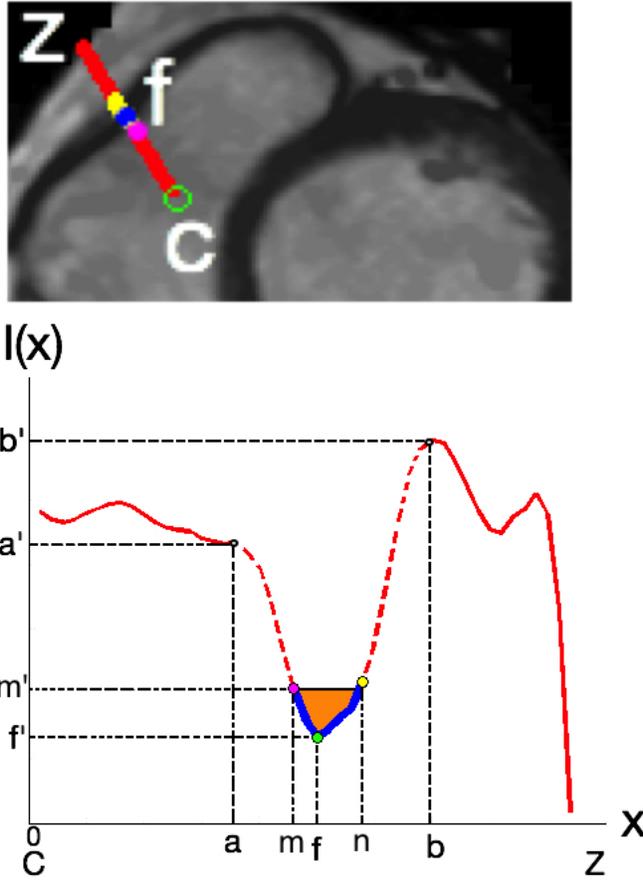


FIG. 3. The top panel illustrates outward radiating segment starting from the centroid  $C$  of the RV. The lower panel shows intensity profile values along that ray  $CZ$ . The parabola pattern in yellow is defined by three control points: The vertex in green, the inner myocardium boundary in magenta and the outer myocardium boundary in blue.

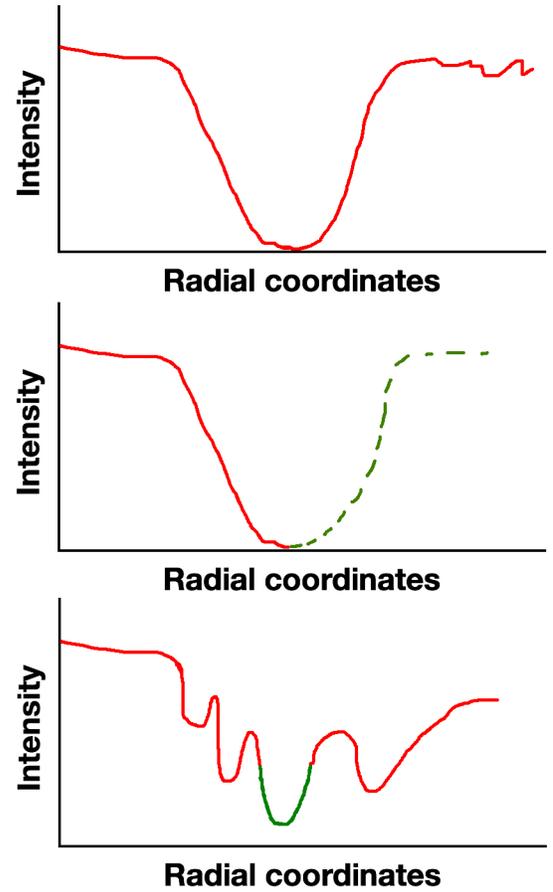


FIG. 4. Different configurations of the radial intensity pattern: A simple profile with a single parabola (top), a fuzzy epicardium border resulting in a half parabola (center) and a profile with multiple possible parabola patterns (bottom).

352 as multiple parabolas/minimal in the radial profile,<sup>370</sup>  
 353 as illustrated at the bottom panel of Fig. 4.<sup>371</sup>

354 Taking these possible configurations into account, the  
 355 most probable myocardium outline is found as follows.<sup>373</sup>

356 1. The intensity profile is extracted in all radial<sup>374</sup>  
 357 directions at  $1^\circ$  steps for every angle  $\theta \in$ <sup>375</sup>  
 358  $[0, 360]$ . The method only takes into account<sup>376</sup>  
 359 those parabolas whose vertex intensity values are<sup>377</sup>  
 360 below the dynamic range mean. The intensity<sup>378</sup>  
 361 values of the three control points  $I_c(cp_{\theta,k})$  of any<sup>379</sup>  
 362 found parabola  $k$  are systematically stored for every<sup>380</sup>  
 363 radial profile.<sup>381</sup>

364 2. If the radial profile matches the trivial cases shown<sup>382</sup>  
 365 in the top and center panels of Fig. 4, i.e., a unique<sup>383</sup>  
 366 full or partial parabola, the three control points are<sup>384</sup>  
 367 easily determined and their intensities stored.<sup>385</sup>

3. When multiple parabola candidates exist, as illustrated in the bottom panel of Fig. 4, the method chooses the one with the best match to the parabolas found in the neighboring radial profiles, minimizing the functional:

$$cp_\beta = \operatorname{argmin}_k \sum_{\theta \in \Theta} \sum_{k \in \Gamma} \|I_c(cp_\theta) - I_c(cp_{\beta,k})\|_2 \quad (3)$$

In Equation 3,  $cp_\beta$  is the set of searched control points,  $\Gamma$  is the number of local minima (parabola candidates) found for the radial profile at a particular angle  $\beta$  and  $\Theta$  is a neighborhood of the angle  $\beta$  composed of the three precedent and posterior profiles. If any of these profiles contains multiple minima, it is removed and replaced with the closest one with a single minimum.

This analysis may miss some segments of the endocardium boundary when rays are parallel to the myocardium wall, as illustrated in the left panel of Fig. 5. Provided that the RV shape is not rounded but rather

386 an elongated structure attached to the left ventricle, new<sup>422</sup>  
 387 rays are traced from two reference points  $n$  and  $m$  that<sup>423</sup>  
 388 correspond to the centers of two circumferences that best<sup>424</sup>  
 389 approximate the whole RV coarse shape, as illustrated<sup>425</sup>  
 390 in the right panel of Fig. 5. A complementary radial<sup>426</sup>  
 391 analysis consists then in tracing rays from the centers<sup>427</sup>  
 392  $n$  and  $m$ , **excluding** rays that intersected one another<sup>428</sup>  
 393 within the ROI, as shown in the right panel of the same<sup>429</sup>  
 394 figure. Observe that no rays are projected neither from<sup>430</sup>  
 395  $n$  nor  $m$  in the arcs delimited by points  $r$  and  $s$ .

396 The final estimation of the endocardium contour  
 397 corresponds to the border points found using three  
 398 different references,  $c$ ,  $n$  and  $m$ , resulting **in a more robust**  
 399 **estimation** over the boundary. These points, however,  
 400 may be useful when locating the contour of the next slices  
 401 in the basal-apex direction.

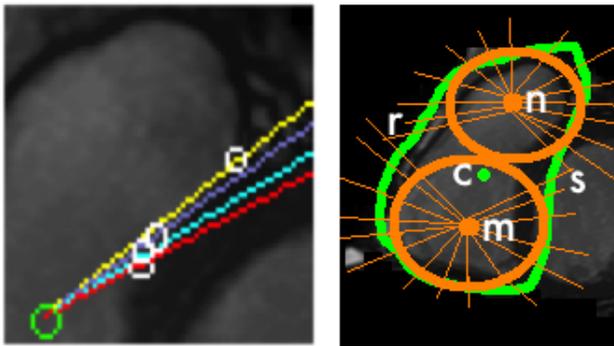


FIG. 5. Left panel zooms out a segment of the RV wall,<sup>435</sup>  
 with the consecutive rays traced from the usual  $c$  centroid.<sup>436</sup>  
 Note that a portion of this segment is completely missed by<sup>437</sup>  
 the radial analysis. Right panel shows the rays projected<sup>438</sup>  
 from two points  $n$  and  $m$ , corresponding to the centers of two<sup>439</sup>  
 circumferences that approximate the RV. The whole chamber<sup>440</sup>  
 is covered, but radii from them never intersect one another.<sup>441</sup>

### 3. Basal endocardium refinement

405 The unidimensional analysis thus far performed can  
 406 be misled by certain structures like the trabeculae or  
 407 papillary muscles, resulting in an unsmooth endocardium  
 408 contour, as illustrated in left panel of Fig. 6.  
 409 Furthermore, the radial analysis may result in more than  
 410 one connected segment or in scattered points. These  
 411 spurious points may be found and removed by mapping  
 412 the contour to a Normalized Radial Length (NRL) vector  
 413  $d_\theta$ , as described in Tahmasbi, Saki, and Shokouhi<sup>44</sup>. The  
 414 right panel of Fig. 6 displays the NRL vector of the RV  
 415 contour at the left panel. Note that the actual contour  
 416 approximately follows the blue dotted curve, except for  
 417 some red outliers (right panel of Fig. 6). These red  
 418 points are removed by applying a local regression to  
 419 the endocardium NRL contour points. Every point of  
 420 the endocardium boundary is further adjusted within  
 421 a small NRL neighborhood. In fact, a second order

polynomial regression<sup>45</sup> is applied within an interval  
 iteratively centered at each of the points of the NRL  
 vector  $d_\theta$ , while varying  $\theta$  from  $-180^\circ$  to  $180^\circ$ . The  
 points of the NRL vector minimize the distance to  
 the curve generated by all second order approximations  
 within an interval width that was herein set to a 10 %  
 of the total points. Finally, the NRL vector is mapped  
 back to Cartesian coordinates to obtain the endocardium  
 contour.

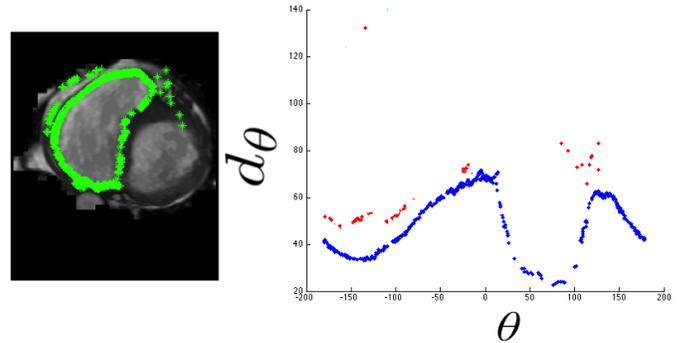


FIG. 6. The points of the endocardium contour are mapped  
 to a Normalized Radial Length (NRL) space  $(\theta, d_\theta)$ , where  
 inconsistencies are removed. The initial endocardium border  
 points are displayed in the left panel in green and the NRL is  
 shown in the right panel with  $d_\theta$  varying from  $-180^\circ$  to  $180^\circ$ .

### 4. Propagation of the basal segmentation towards the apex

The RV volume is the result of the sum of the  
 found areas from each slice multiplied by the inter-slice  
 distance. If one assumes that adjacent slice-to-slice  
 changes are smooth, it is reasonable to expect that a well  
 segmented basal slice should be used by the next slice as  
 a regularizer and that subsequent slices use the precedent  
 one. The overall algorithm is illustrated in Algorithm 1.

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**Algorithm 1** Pseudocode for propagation of the basal  
 segmentation towards the apex

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**Require:** the endocardium segmentation  $\zeta_\xi$  of the basal slice

- $\xi = 0$
- 1: **repeat**
- 2: **if**  $\zeta_\xi$  centroid  $\in$  RoI **then**
- 3:  $\zeta_{\xi+1} \leftarrow$  by applying the radial analysis of section III B 2  
 using  $\zeta_\xi$  centroid as the reference.
- 4: **else**
- 5:  $\zeta_{\xi+1} \leftarrow$  by applying the radial analysis of section III B 2  
 using the centroid of the left half of the RoI as the  
 reference.
- 6: **end if**
- 7:  $\zeta_{\xi+1}$  is refined as described in section III B 3
- 8:  $\zeta_\xi$  is superimposed to the slice  $\xi + 1$  and centered around  
 the  $\zeta_{\xi+1}$  centroid
- 9:  $\zeta_{\xi+1} \leftarrow$  is updated by finding the searched pattern which  
 is closer to the  $\zeta_\xi$  contour and is defined in section III B 2
- 10:  $\xi \leftarrow \xi + 1$
- 11: **until**  $\xi >$  number of slices

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### C. Epicardium estimation

Once the whole endocardium volume is estimated, the epicardium is also determined using the endocardium segmentation. To do this, the RV endocardium contour is dilated by a diamond-shaped structuring element of size  $\rho$ , being  $\rho$  the median of the Euclidean distance between the inner and outer myocardium boundary in the third clockwise quadrant, i.e., the free wall of the right ventricle seen from the centroid previously determined. Overall, most dilation operations have been performed using circular structuring elements<sup>34,46,47</sup>, while the present investigation used a diamond shaped. This diamond structuring element promoted the propagation of the information exclusively in the normal direction of the ventricular wall.

### D. Data

The performance of the proposed method was tested over a public Cardiac MRI dataset of 48 subjects, supplied by the organizers of the Right Ventricle Segmentation Challenge in MICCAI (RVSC) 2012<sup>22</sup>. The CMR data were acquired from 1.5T short-axis cine CMRI planes, in a plane resolution of 1.3 mm, a between-slice distance of 8.4 mm, a matrix size of 256 × 216 and 20 heart phases for each subject. This data set has been split by the RVSC into three groups: Training, Test 1 and Test 2. Training data consists of a set of 16 cardiac MRI, with equal number of male and female subjects, with an average age of 51 ± 12 years. Test 1 dataset was split into 3 women and 13 men cases, with an average age of 48 ± 18 years, while test 2 dataset was divided into 5 women and 11 men with an average age of 54 ± 22 years. The recorded subjects were diagnosed with several cardiac pathologies namely myocarditis, ischaemic cardiomyopathy, arrhythmogenic right ventricular dysplasia (ARVD), dilated cardiomyopathy, hypertrophic cardiomyopathy, aortic stenosis and cardiac tumour, as well as left ventricular ejection fraction assessment.

For each subject, endocardium and epicardium contours have been delineated by a single observer at the end of the diastole (ED) and the end of the systole (ES).

## IV. RESULTS

### A. Segmentation accuracy

Figure 7 shows the ROI obtained by the motion saliency map on subjects and slices randomly selected from the RVSC dataset.

In spite of the high variability of the test set, as illustrated in Fig. 7, the method successfully encloses

the cardiac chamber in these images encompassing heart slices at different levels and times of the cardiac cycle.

A qualitative evaluation of the endocardium segmentation may be observed in Fig. 8. The images present, superimposed, the segmentation and manual delineations for a single subject on different slices and at different moments of the cardiac cycle. Observe how the automatically generated endocardium segmentation is in strong accordance with the manual delineation and follows closely the ventricle boundary. Some parts of the contour at the apex level appear to be slightly displaced (shown in white arrows Fig. 8), particularly at the boundary with the left ventricle. This might be attributed to the high density of the pectinati and papillary muscles next to the left ventricle. A quantitative assessments are the Dice Score<sup>48</sup> (DSC) and the Hausdorff Distance<sup>49</sup> (HD) between the automatic and manual boundaries. The DSC measures the spatial overlap in a range that goes from 0 (no overlap) to 1 (maximum overlap). The HD provides the average distance between the boundaries of the two contours. The Hausdorff measure  $\Psi(A, B)$  computes the maximum distance between two sets of points as

$$\Psi(A, B) = \max_{a \in A} \min_{b \in B} \|a - b\|_2^2 \quad (4)$$

Table I lists the average and standard deviation of the DSC and HD metrics for the end of diastole (ED) and systole (ES) of the 48 subjects of the RVSC dataset. Although only Test 1 and Test 2 sets are usually used for evaluation, in this work this assessment was extended to the training set (previously described) since the presented method need not require training. Overall, results demonstrate a volume overlap average of about 87 % for the three different experimental groups, with relatively small variances (about 0.1). Overlapping is larger for the diastole, as expected, because of the considerably smaller proportion of papillary muscles and other structures with respect to the perimeter of the chamber wall in this phase of the cycle. That is, the contracted structures form a much more irregular boundary in the systole phase, making this part of the cycle more error-prone. In terms of the HD, which estimates the segmentation compactness or the influence of the local errors, results show a small distance between each point of the automatic contour with respect to the manual delineation, an average of 7.26 mm for a total of 48 cases. Likewise, the epicardium is also segmented and the estimated contours show a slightly better overlapping than the endocardium, probably because the inner structures that contaminate the estimation of the endocardium contour are not longer present. It is important to notice that this estimation allows the ventricular mass to be calculated, a clinical index that most methods never report.

Table II shows a summary of the quantitative reported performance for different methods at the ED and ES,

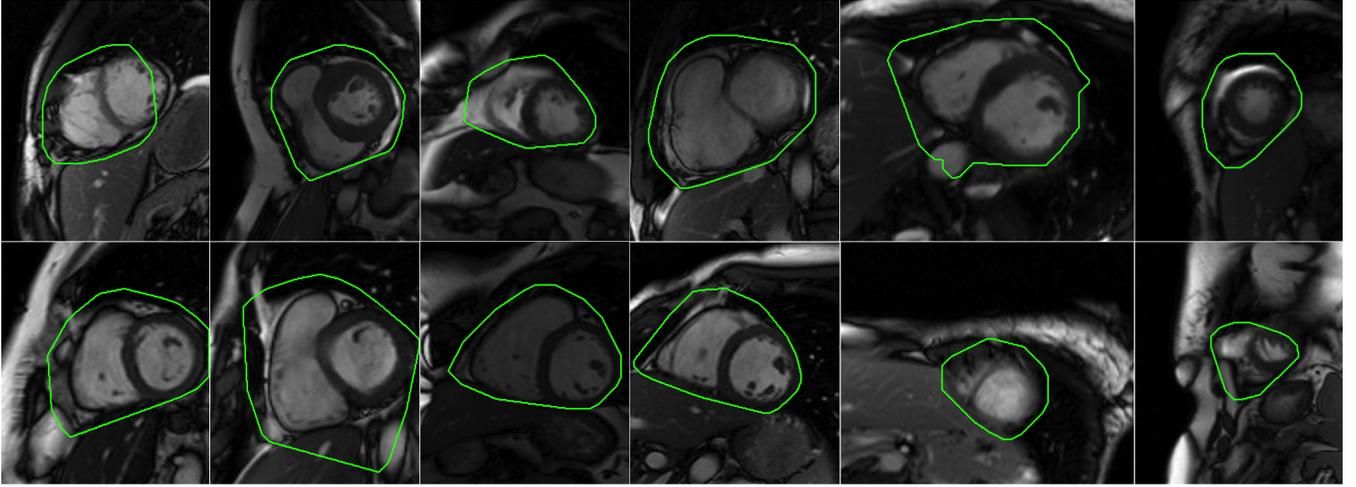


FIG. 7. Each panel corresponds to the coarse heart localization of a random level of the RV volume at a random state of the cardiac cycle of an only subject randomly selected from the RVSC dataset. In all tested images the method consistently locates an ROI containing the whole RV. Although on rare occasions a small portion of the LV is left outside of the ROI, as illustrated in the upper left panel, this does not affect the RV segmentation.

TABLE I. Mean ( $\pm$ standard deviation) of the Dice Score (DSC) and Hausdorff distance (HD, in  $mm$ ) for RV endocardium (Endo) and epicardium (Epi) at the end of the diastole (ED) and end of the systole (ES) using the RVSC dataset.

	Training		Test 1		Test 2		Summary		
	ED	ES	ED	ES	ED	ES	ED	ES	
Endo	DSC	0.87 (0.12)	0.84 (0.12)	0.87 (0.13)	0.83 (0.13)	0.88 (0.13)	0.84 (0.12)	0.87	0.84
	HD	6.21 (1.76)	8.65 (3.40)	6.30 (1.77)	8.66 (3.41)	6.22 (1.72)	8.59 (3.00)	6.24	8.63
Epi	DSC	0.89 (0.08)	0.86 (0.06)	0.89 (0.09)	0.87 (0.07)	0.90 (0.08)	0.87 (0.06)	0.89	0.87
	HD	5.59 (1.27)	8.63 (3.06)	5.66 (1.29)	8.64 (3.14)	5.52 (5.98)	8.50 (3.32)	5.59	8.59

549 assessed with the same dataset: test 1. One method did 569  
 550 not report the epicardium segmentation (N/A). Overall,  
 551 the presented method outperforms previous works but 570  
 552 the results presented by Ringenberg *et al.* at the ED. 571  
 553 In this work, Ringenberg *et al.* reported a DSC=0.88 572  
 554 for the endocardium and DSC=0.9 of the epicardium, 573  
 555 against a DSC of 0.87 for the endocardium and 0.89 for 574  
 556 the epicardium with our method. However, our approach 575  
 557 reports a smaller Hausdorff Distance (5.66 against 7.69) 576  
 558 and a smaller associated standard deviation. This 577  
 559 difference might indicate that the presented method is 578  
 560 less prone to be influenced by outliers. 579

## 561 B. Computation time

562 The proposed method has been observed to have a 582  
 563 very low computational cost, about 3 seconds in average  
 564 for the whole RV volume segmentation at a particular 583  
 565 time  $t$ , using a Matlab implementation without any 584  
 566 optimization. The whole approach was run in a computer 585  
 567 with a RAM of 16 GB and a 2.5 GHz intel core i5 586  
 568 processor. 587

## C. Clinical indexes

To assess the clinical utility of the proposed method, the robustness for computing clinical indexes was calculated. The RV volumes at ED and ES were computed as well as the ejection fraction and the ventricular mass. The RV volumes at the ED (EDV) and the ES (ESV) are obtained using the endocardium slice segmentations, which are then summed and multiplied by the inter-slice gap size. The most important indicator of the RV function, the ejection fraction (EF), is computed as:

$$580 \quad EF = \frac{EDV - ESV}{EDV} \times 100\% \quad (5)$$

581 The ventricular mass ( $V_M$ ) is defined as:

$$V_M = density * (EDV_{epi} - EDV_{endo}) \quad (6)$$

being  $EDV_{epi}$  and  $EDV_{endo}$  the volumes at the ED for epicardium and endocardium tissues, respectively, with a density of  $1.05 g/cm^3$  52.

Table III shows the correlation coefficients obtained for the linear regressions performed between the automatic

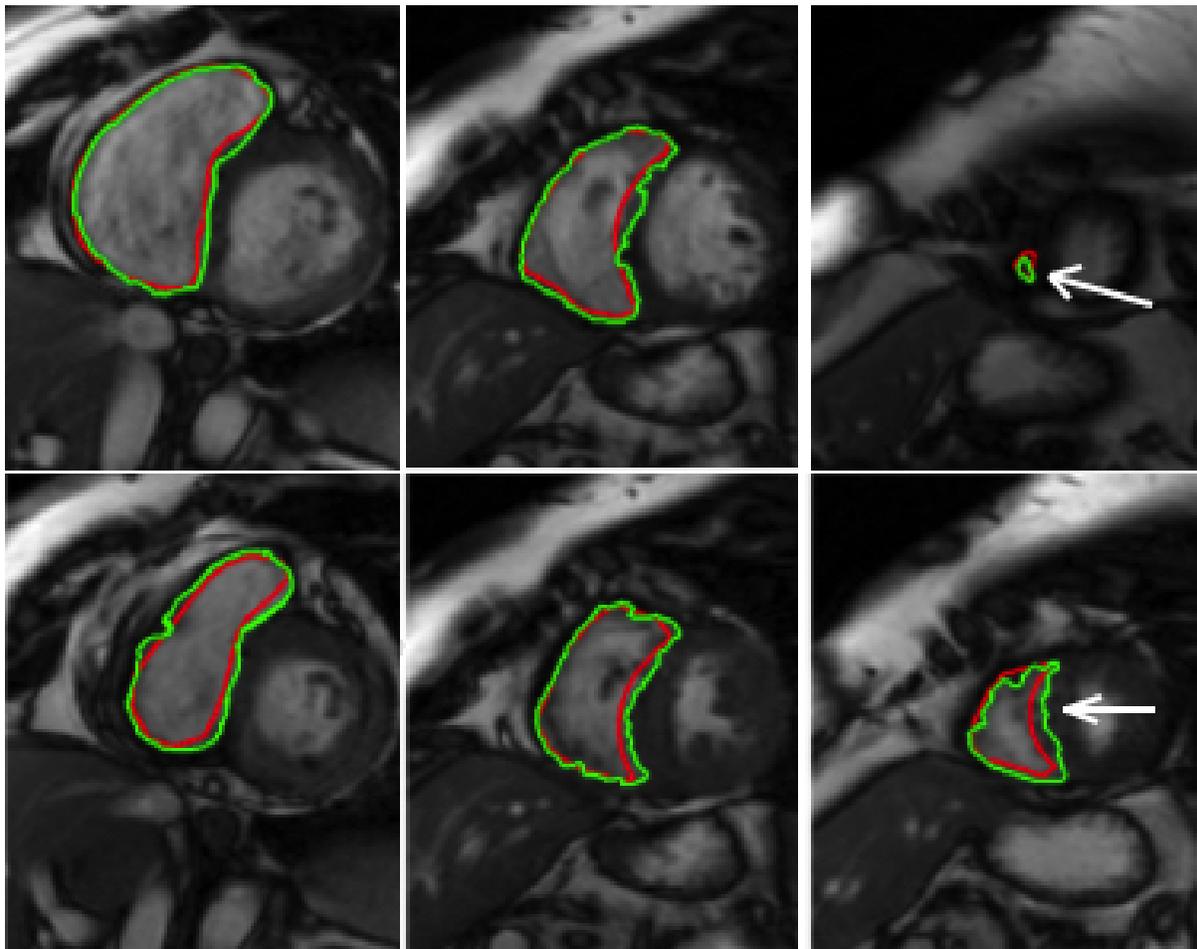


FIG. 8. Figure illustrates the endocardium automatic segmentation (green line) against the manual delineation (red line). Top row shows slices at the end of the diastole while bottom row displays the corresponding slice at the end of the systole. From left to right, panels show the basal, mid and apex levels of the heart segmentation.

TABLE II. Reported mean and standard deviation of several methods (including ours) for the Test 1 set. These results show the Dice Score and Hausdorff metrics (HD in *mm*) for RV endocardium and epicardium at the End of the Diastole (ED) and the End of the Systole (ES)

Method	End of the Diastole				End of the Systole			
	Endocardium		Epicardium		Endocardium		Epicardium	
	DSC	HD	DSC	HD	DSC	HD	DSC	HD
	Automatic							
<b>Our method</b>	0.87 (0.13)	5.66 (1.29)	0.89 (0.09)	6.30 (1.77)	0.83 (0.13)	8.64 (3.14)	0.87 (0.07)	8.66 (3.41)
Ou et al. <sup>50</sup>	0.66 (0.24)	17.66 (8.67)	0.67 (0.23)	17.44 (8.51)	0.53 (0.32)	20.44 (17.80)	0.60 (0.30)	21.91 (18.92)
Ringenberg et al. <sup>34</sup>	0.88 (0.11)	7.69 (6.03)	0.90 (0.08)	8.02 (5.96)	0.77 (0.18)	10.71 (7.69)	0.82 (0.13)	11.52 (7.70)
Wang et al. <sup>33</sup>	0.63 (0.32)	22.89 (25.01)	0.70 (0.34)	21.45 (25.14)	0.50 (0.34)	27.99 (24.97)	0.55 (0.36)	27.58 (24.82)
Zuluaga et al. <sup>26</sup>	0.83 (0.17)	9.77 (7.88)	0.86 (0.13)	10.23 (7.22)	0.72 (0.27)	11.41 (10.49)	0.77 (0.23)	11.81 (9.46)
Moolan et al. <sup>51</sup>	0.86 (0.10)	8.40 (4.21)	N/A	N/A	0.75 (0.18)	10.02 (5.78)	N/A	N/A
	Semi-automatic							
Bai et al. <sup>47</sup>	0.86 (0.11)	7.70 (3.74)	0.88 (0.08)	7.93 (3.72)	0.69 (0.25)	11.16 (5.53)	0.77 (0.17)	11.72 (5.44)
Grosgeorge et al. <sup>46</sup>	0.83 (0.15)	9.48 (5.41)	0.86 (0.10)	9.84 (5.49)	0.69 (0.23)	10.56 (5.54)	0.78 (0.15)	11.09 (5.34)
Punithakumar et al. <sup>31</sup>	N/A	N/A	N/A	N/A	0.77 (0.16)	9.64 (4.15)	0.82 (0.10)	9.99 (3.85)

588 and manual delineations, for each clinical index, namely<sup>591</sup>  
589 EDV, ESV, EF and  $V_M$  and for the whole RVSC dataset.<sup>592</sup>  
590 These coefficients evidence a strong correlation between<sup>593</sup>

the automatic and manual contours, with values always  
larger than a 90%. [Table IV](#) illustrates the comparison of  
these clinical indexes results obtained on the Test1 from

TABLE III. Clinical indexes results obtained on the RVSC dataset at the ED and the ES frames of the cardiac cycle by computing the correlation coefficient (ideal=1).

	EDV	ESV	EF	VM
Training	0.98	0.98	0.95	0.93
Test 1	0.98	0.97	0.93	0.92
Test 2	0.96	0.97	0.93	0.90

#### D. Application to other datasets

The method was also evaluated with another dataset to illustrate how the proposed strategy is robust to changes of each particular dataset, i.e., it is independent of the capture conditions; an important issue for most models that require a fine tuning phase for each particular acquisition protocol. The data collection provided by the Sunnybrook Health Sciences Center<sup>24</sup>, was made publicly available for the Cardiac MR Left Ventricular Segmentation Grand Challenge (MICCAI 2009). From the full set of 45 subjects, 30 were randomly selected for testing, including 24 diagnosed with various cardiac pathologies such as hypertension, cardiac failure or hypertrophic cardiomyopathy. Figure 9 shows the obtained ROIs and endocardium segmentations for different slices, levels and cases. The MSM achieved a correct enclosing the two cardiac chambers for all cases of this dataset. Also observe how, despite the huge shape variability, the strategy locates the right chamber and correctly delineates its boundary. Each image of this figure correspond to a random slice of a random volume of a random subject of this dataset. Observe how the endocardium (green line) contour is properly delineated by our method. Figure 10 illustrates a series 3D surface of the obtained segmentation of the RV endocardial volume during the cardiac cycle of a patient randomly selected.

TABLE IV. Reported clinical indexes results obtained on the Test 1 from RVSC dataset at the ED and the ES frames of the cardiac cycle by computing the correlation coefficient of several methods (including ours).

METHODS	EDV	ESV	EF	VM
Our method	0.98	0.97	0.93	0.92
Ringengberg et al. <sup>34</sup>	0.98	0.95	0.78	0.97
Zuluaga et al. <sup>26</sup>	0.96	0.97	-	-
Bai et al. <sup>47</sup>	0.99	0.98	0.92	0.91

## V. DISCUSSION

This paper has introduced a novel and automatic approach to segment the right ventricular chamber in SAX cine MRI. Unlike other RV segmentation methods,

this method uses the heart motion to estimate a salient ROI and focuses the exploration on this region. Under a 2D saliency analysis, the endocardium is segmented at every slice at any moment of the cardiac cycle by a local radial search over the intensity profile of a shape prior (parabola) within the salient ROI containing the ventricular structures. The RV basal level is the first slice to be segmented since at this level the right ventricle boundaries tend to be well defined. This first basal segmentation is propagated towards the more noisy slices in the apex direction, using the precedent contour as a reference for the slice segmentation, i.e., the radial search of the prior (parabola) is iteratively performed along the slices and the precedent contour serves as an initial condition of the search. Finally, the epicardium contour is estimated by dilating this endocardium volume.

Results have demonstrated that the present approach is competitive with respect to the techniques of the state of the art. The strategy outperformed the other methods in terms of the HD measure, an estimation of the contour compactness which is very sensitive to local errors. When the DSC measure is used, the proposed method's segmentation accuracy is slightly below ( $-0.02$ ) the results reported by Ringenberg *et al.*. However, in comparison with this approach and other state-of-the-art methods, the present strategy requires no parameter fine tuning, nor previous training or a minimal quantity of data. Other methods demand a strong adjustment of parameters<sup>34,46,51</sup>, or are atlas based and, in consequence, computationally expensive and data quantity/quality dependent<sup>26,28,50</sup>. Some authors<sup>31</sup> have used the propagation of a manual segmentation to the rest of the RV, but the dependency on the expert is inevitable and a considerable burden. Other authors<sup>33</sup> have detected the region with maximal motion and selected the RV by a simple threshold. Their reported results, however, are below most state-of-the-art methods. Finally, the computational cost is also a crucial factor of consideration: the present method achieves a complete volume segmentation in approximately 3s using non optimal implementation on an ordinary computer.

In the presented method the parameters requiring adjustments were kept to a minimum. The MSM, for instance, uses a classical patch size of  $5 \times 5$  and consistently detects the cardiac motion in different databases. However, other nearby structures that usually move with the cardiac structures, such as the lung or fragments of the diaphragmatic and pericardium fat, may be incorrectly included in the analysis. As shown in this article, the detection of the two main chambers focuses the analysis and the radial search of the prior, excluding most neighboring tissues.

The interval width for the polynomial regression was also adjusted: The larger the interval width the more points may be removed and the more rigid the obtained curve, whereas the smaller the values the noisier the final curve. A good compromise was found by defining moving intervals and selecting only a ten percent of the contour

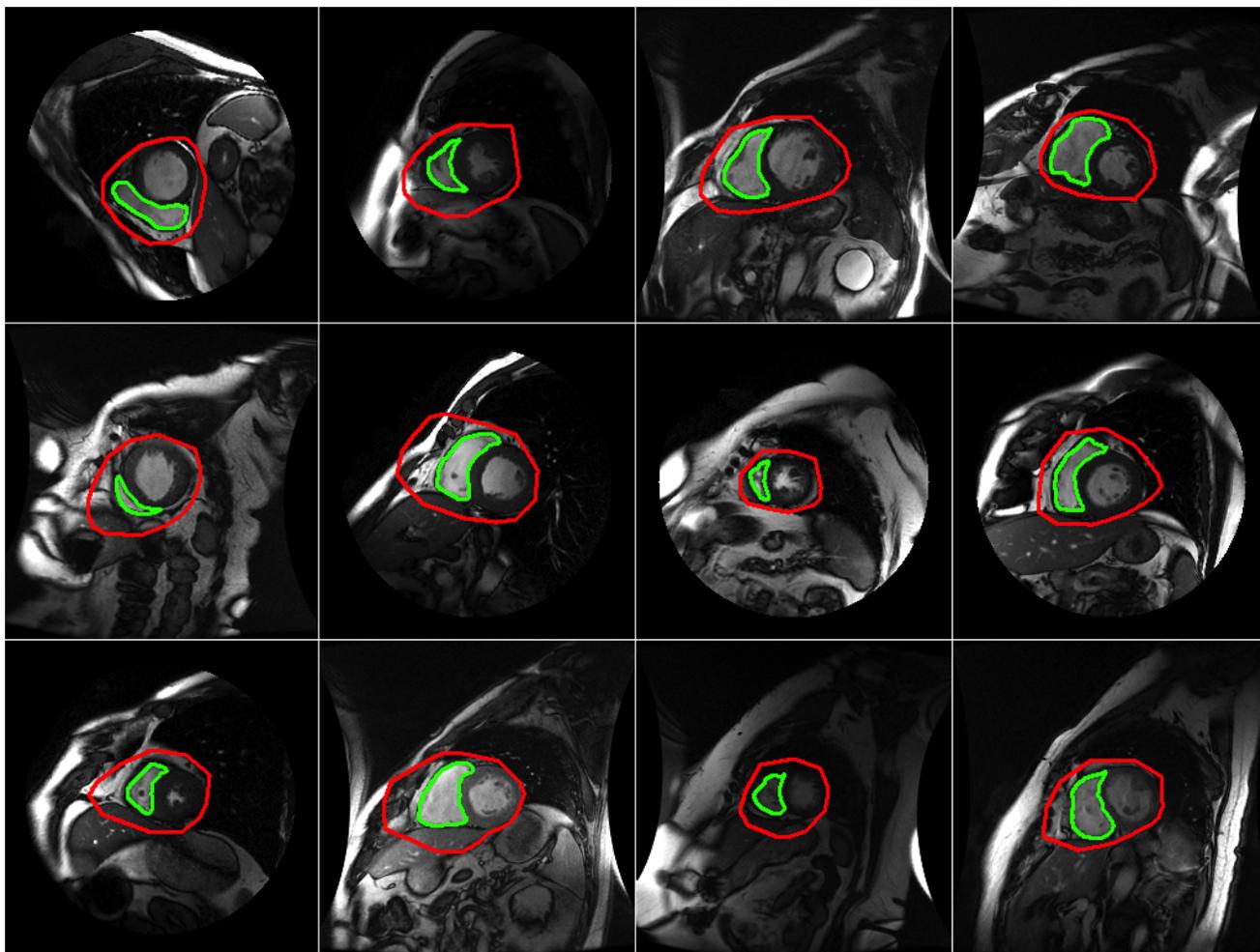


FIG. 9. RV endocardium segmentation for different slices at different phases of the cardiac cycle, where each slice corresponds to a random subject of the Sunnybrook dataset. The endocardium contour is displayed in green line, while the RoI in red line.

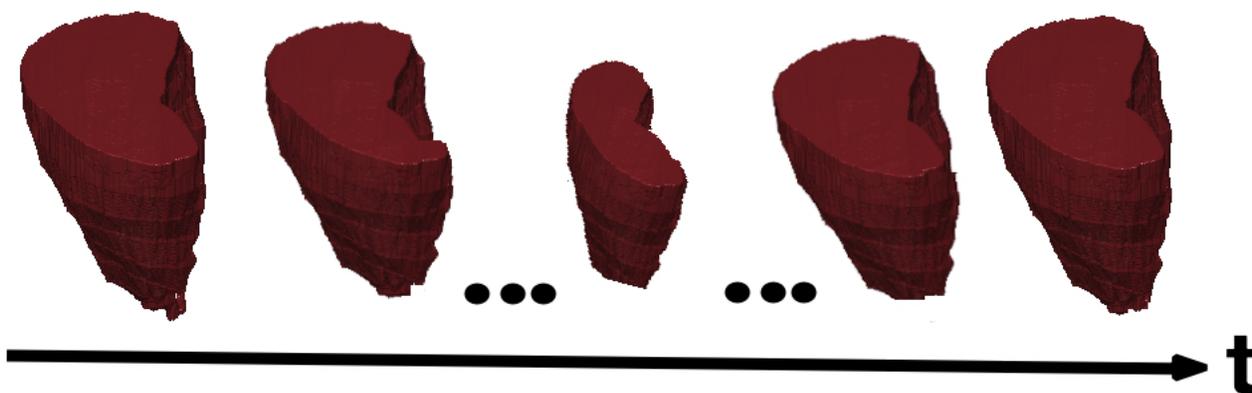


FIG. 10. A series 3D surface data of the obtained segmentation of the RV endocardial volume of a patient during a cardiac cycle.

686 points at each interval.

687 Some conditions that may result in a failure of other  
688 segmentation approaches are the similarity between the

689 myocardium and its surrounding tissue. This is overcome  
690 in the present method by the regularization using the  
691 segmentation of the precedent slice. The overlap errors

692 for the proposed method, calculated using the automatic<sup>741</sup>  
 693 and the manual delineations, was of about 1.12% for the<sup>742</sup>  
 694 ED and of 1.5% for the ES.<sup>743</sup>

695 Wrong estimations of the RV may appear when<sup>744</sup>  
 696 the wall trabeculation increases. This pattern has<sup>745</sup>  
 697 been described in pathologies like the right ventricular<sup>746</sup>  
 698 dilation, RV hypertrophy, idiopathic pulmonary<sup>747</sup>  
 699 hypertension, Fallot's tetralogy or the cardiac idiopathic<sup>748</sup>  
 700 dilation, which constitute the group of rare cardiac<sup>749</sup>  
 701 diseases<sup>750</sup>. These trabeculae are also salient and might<sup>751</sup>  
 702 be confused with myocardium. However, these cases<sup>752</sup>  
 703 could be managed by including a manual correction of<sup>753</sup>  
 704 the pattern in these very complicated and blurred areas.<sup>754</sup>

705  
 706 The presented method has successfully segmented the<sup>755</sup>  
 707 RV in SAX views under very different and challenging<sup>756</sup>  
 708 anatomic and pathological conditions. This approach<sup>757</sup>  
 709 may be easily extended to segment the left ventricle<sup>758</sup>  
 710 in CMRI. Future work includes a refinement in the<sup>759</sup>  
 711 estimation of the myocardium prior by an exhaustive<sup>760</sup>  
 712 analysis of the myocardium wall in larger populations<sup>761</sup>  
 713 that include different pathologies.<sup>762</sup>

## 714 VI. CONCLUSIONS

715 This paper has introduced a novel automatic<sup>763</sup>  
 716 segmentation strategy to delineate the right ventricle in<sup>764</sup>  
 717 short axis cine MRI for any phase of the cardiac cycle.<sup>765</sup>  
 718 The proposed strategy captures most of the cardiac<sup>766</sup>  
 719 variability without any dependency on the nature of the<sup>767</sup>  
 720 cardiac pathology. The presented approach achieved an<sup>768</sup>  
 721 average DSC=0.87 and HD=7.26 mm over 48 real cases,<sup>769</sup>  
 722 demonstrating that the obtained contours correlate with<sup>770</sup>  
 723 independent manual delineations. These results suggest<sup>771</sup>  
 724 this segmentation method may be suitable to support the<sup>772</sup>  
 725 expert in cine MRI and reduce the inter and intra expert<sup>773</sup>  
 726 variability.<sup>774</sup>

## 727 ACKNOWLEDGMENTS

728 This work was supported by Colciencias-Colombia,<sup>775</sup>  
 729 Grant No. 647 (2015 call for National PhD studies) and<sup>776</sup>  
 730 a UCL-Santander Research Catalyst Award.<sup>777</sup>

## 731 CONFLICT OF INTEREST DISCLOSURE

732 The authors have no relevant conflicts of interest to<sup>778</sup>  
 733 disclose.<sup>779</sup>

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