

Online Supporting Information for:

EMMLi: A maximum likelihood approach to the analysis of modularity

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Table S1: Identification of landmarks from the data set presented in (Goswami and Polly 2010). Numbers indicate the module designations in the present analysis for different model structures. N/F is the Neurocranial/Facial 2-module hypothesis (e.g., Drake and Klingenberg 2010), C6 is the Cheverud 6-module hypothesis from (Cheverud 1995). G6 is the Goswami 6-module hypothesis from (Goswami 2006a). C/G8 is an eight-module model merging the Cheverud and Goswami models. TO is the tissue origin model as described in (Goswami 2006a). CMM and GMM are “monotreme” model hypotheses that are modifications of each six-module hypotheses (Cheverud and Goswami, respectively) with some strong modules (either 1,2, and 6 or just 1 and 6) and some unintegrated traits (Unint.), similar to the monotreme pattern described in (Goswami 2006a).

| | Landmark | N/F | C6 | G6 | C/G 8 | TO | CMM | GMM |
|----|---|-----|----|----|----------|--------------|-----|-----|
| 1 | Premaxilla anterior midline suture | 1 | 1 | 1 | 1 | Neural Crest | 1 | 1 |
| 2 | Premaxilla - Maxilla lateral suture - left | 1 | 1 | 1 | 1 | Neural Crest | 1 | 1 |
| 3 | Premaxilla - Maxilla lateral suture - right | 1 | 1 | 1 | 1 | Neural Crest | 1 | 1 |
| 4 | Premaxilla - Maxilla ventral suture | 1 | 1 | 1 | 8 | Neural Crest | 1 | 1 |
| 5 | Canine - lateral extreme - left | 1 | 1 | 1 | 8 | Neural Crest | 1 | 1 |
| 6 | Canine - mesial extreme - left | 1 | 1 | 1 | 8 | Neural Crest | 1 | 1 |
| 7 | Canine - lateral extreme - right | 1 | 1 | 1 | 8 | Neural Crest | 1 | 1 |
| 8 | Canine - mesial extreme - right | 1 | 1 | 1 | 8 | Neural Crest | 1 | 1 |
| 9 | Palatine - Maxilla - ventral suture | 1 | 1 | 2 | 2 | Neural Crest | 1 | 2 |
| 10 | Maxilla - Palatine lateral suture - left | 1 | 1 | 2 | 2 | Neural Crest | 1 | 2 |

| | | | | | | | | |
|----|---|---|---|---|---|--------------|--------|--------|
| 11 | Maxilla - Palatine lateral suture - right | 1 | 1 | 2 | 2 | Neural Crest | 1 | 2 |
| 12 | Anterior P1 - left | 1 | 1 | 2 | 2 | Neural Crest | 1 | 2 |
| 13 | Anterior P1 - right | 1 | 1 | 2 | 2 | Neural Crest | 1 | 2 |
| 14 | Nasals - anterior midline extreme | 1 | 2 | 1 | 1 | Neural Crest | 2 | 1 |
| 15 | Nasals - Frontal midline suture | 1 | 3 | 3 | 3 | Mixed | Unint. | Unint. |
| 16 | Nasal - Premaxilla suture - left | 1 | 2 | 1 | 1 | Neural Crest | 2 | 1 |
| 17 | Nasal - Premaxilla suture- right | 1 | 2 | 1 | 1 | Neural Crest | 2 | 1 |
| 18 | Jugal - Maxilla (Orbit crest) suture - left | 1 | 3 | 3 | 3 | Mixed | Unint. | Unint. |
| 19 | Jugal - Maxilla (Orbit crest) suture - right | 1 | 3 | 3 | 3 | Mixed | Unint. | Unint. |
| 20 | Lacrimal - Frontal - Maxilla suture - left | 1 | 3 | 3 | 3 | Mixed | Unint. | Unint. |
| 21 | Ethmoid - Lacrimal - Frontal suture - left | 1 | 3 | 3 | 3 | Mixed | Unint. | Unint. |
| 22 | Lacrimal - Frontal - Maxilla suture - right | 1 | 3 | 3 | 3 | Mixed | Unint. | Unint. |
| 23 | Ethmoid - Lacrimal - Frontal suture - right | 1 | 3 | 3 | 3 | Mixed | Unint. | Unint. |
| 24 | Maxilla - Jugal posterior interior suture - left | 1 | 4 | 3 | 4 | Mixed | Unint. | Unint. |
| 25 | Maxilla - Jugal posterior interior suture - right | 1 | 4 | 3 | 4 | Mixed | Unint. | Unint. |
| 26 | Sphenoid - Jugal - Frontal interior suture - left | 1 | 4 | 3 | 3 | Mixed | Unint. | Unint. |
| 27 | Sphenoid - Jugal - Frontal interior suture - right | 1 | 4 | 3 | 3 | Mixed | Unint. | Unint. |
| 28 | Jugal - Maxilla (base of zygomatic arch) suture - left | 1 | 4 | 2 | 4 | Mixed | Unint. | 2 |
| 29 | Jugal - Maxilla (base of zygomatic arch) suture - right | 1 | 4 | 2 | 4 | Mixed | Unint. | 2 |
| 30 | Jugal - Frontal (postorbital bar) suture - left | 1 | 3 | 3 | 3 | Mixed | Unint. | Unint. |
| 31 | Jugal - Frontal (postorbital bar) suture - right | 1 | 3 | 3 | 3 | Mixed | Unint. | Unint. |
| 32 | Jugal - Squamosal dorsal suture - left | 1 | 4 | 4 | 4 | Mixed | Unint. | Unint. |

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|----|---|---|---|---|---|------------|--------|--------|
| 33 | Jugal - Squamosal dorsal suture - right | 1 | 4 | 4 | 4 | Mixed | Unint. | Unint. |
| 34 | Jugal - Squamosal ventral suture - left | 1 | 4 | 4 | 4 | Mixed | Unint. | Unint. |
| 35 | Jugal - Squamosal ventral suture - right | 1 | 4 | 4 | 4 | Mixed | Unint. | Unint. |
| 36 | Parietal - Frontal suture | 2 | 5 | 5 | 5 | Mixed | Unint. | Unint. |
| 37 | Parietal - Squamosal - Frontal suture - left | 2 | 5 | 5 | 5 | Mixed | Unint. | Unint. |
| 38 | Parietal - Squamosal - Frontal suture - right | 2 | 5 | 5 | 5 | Mixed | Unint. | Unint. |
| 39 | Parietal - Squamosal - Occipital suture - left | 2 | 5 | 4 | 5 | Mixed | Unint. | Unint. |
| 40 | Parietal - Squamosal - Occipital suture - right | 2 | 5 | 4 | 5 | Mixed | Unint. | Unint. |
| 41 | Jugal - Frontal - Alisphenoid suture - left | 2 | 4 | 5 | 5 | Mixed | Unint. | Unint. |
| 42 | Jugal - Frontal - Alisphenoid suture - right | 2 | 4 | 5 | 5 | Mixed | Unint. | Unint. |
| 43 | Frontal - Sphenoid - Squamosal suture - left | 2 | 4 | 5 | 5 | Mixed | Unint. | Unint. |
| 44 | Frontal - Sphenoid - Squamosal suture - right | 2 | 4 | 5 | 5 | Mixed | Unint. | Unint. |
| 45 | Pterygoid tip lateral - left | 2 | 6 | 4 | 7 | Mixed | 6 | Unint. |
| 46 | Pterygoid tip lateral - right | 2 | 6 | 4 | 7 | Mixed | 6 | Unint. |
| 47 | Pterygoid tip medial - left | 2 | 6 | 4 | 7 | Mixed | 6 | Unint. |
| 48 | Pterygoid tip medial - right | 2 | 6 | 4 | 7 | Mixed | 6 | Unint. |
| 49 | Presphenoid - Palatine - Alisphenoid suture - left | 2 | 6 | 4 | 7 | Mixed | 6 | Unint. |
| 50 | Presphenoid - Palatine - Alisphenoid suture - right | 2 | 6 | 4 | 7 | Mixed | 6 | Unint. |
| 51 | Basisphenoid - Presphenoid - Alisphenoid suture - left | 2 | 6 | 4 | 7 | Mixed | 6 | Unint. |
| 52 | Basisphenoid - Presphenoid - Alisphenoid suture - right | 2 | 6 | 4 | 7 | Mixed | 6 | Unint. |
| 53 | Basioccipital-Basisphenoid-Bulla suture - left | 2 | 6 | 6 | 6 | Mesodermal | 6 | 6 |
| 54 | Basioccipital-Basisphenoid-Bulla suture - right | 2 | 6 | 6 | 6 | Mesodermal | 6 | 6 |

| | | | | | | | | |
|----|---|---|---|---|---|------------|--------|--------|
| 55 | Bulla anterior medial extreme - left | 2 | 6 | 6 | 6 | Mesodermal | 6 | 6 |
| 56 | Bulla anterior medial extreme - right | 2 | 6 | 6 | 6 | Mesodermal | 6 | 6 |
| 57 | Bulla posterior lateral extreme - left | 2 | 6 | 6 | 6 | Mesodermal | 6 | 6 |
| 58 | Bulla posterior lateral extreme - right | 2 | 6 | 6 | 6 | Mesodermal | 6 | 6 |
| 59 | Parietals - Occipital suture | 2 | 5 | 4 | 5 | Mixed | Unint. | Unint. |
| 60 | Occipital condyle - extreme - left | 2 | 6 | 6 | 6 | Mesodermal | 6 | 6 |
| 61 | Occipital condyle - extreme - right | 2 | 6 | 6 | 6 | Mesodermal | 6 | 6 |

Table S2: Results for the Adult Male data set (n=25) using congruence coefficients. Model parameters, raw log-likelihood fits for each tested model, AIC_c and ΔAIC_c scores are provided. Model log-likelihoods and the model posterior probability are also shown. Sample size used to calculate AIC_c was 1830. See methods for details. Model ID's correspond to the numbering in Table 1. The optimal model in the set of evaluated models is highlighted in bold italics.

| Model ID | K | LogL | AIC_c | ΔAIC_c | Model LogL | Model Post. Prob. |
|-----------------|-----------|----------------|---------------------------|----------------------------------|-------------------|--------------------------|
| 1 | 2 | 2175.77 | -4347.53 | 335.29 | 1.56E-73 | 1.56E-73 |
| 2 | 3 | 2221.21 | -4436.40 | 246.42 | 3.10E-54 | 3.10E-54 |
| 3 | 4 | 2228.99 | -4449.96 | 232.85 | 2.73E-51 | 2.73E-51 |
| 4 | 3 | 2245.09 | -4484.17 | 198.64 | 7.33E-44 | 7.33E-44 |
| 5 | 8 | 2310.25 | -4604.43 | 78.39 | 9.50E-18 | 9.50E-18 |
| 6 | 17 | 2298.53 | -4562.72 | 120.10 | 8.34E-27 | 8.34E-27 |
| 7 | 22 | 2363.69 | -4682.82 | 0.00 | 1.00 | 1.000 |
| 8 | 3 | 2211.58 | -4417.14 | 265.68 | 2.04E-58 | 2.04E-58 |
| 9 | 8 | 2256.30 | -4496.53 | 186.29 | 3.53E-41 | 3.53E-41 |
| 10 | 17 | 2258.68 | -4483.01 | 199.80 | 4.10E-44 | 4.10E-44 |
| 11 | 22 | 2303.40 | -4562.25 | 120.57 | 6.58E-27 | 6.58E-27 |
| 12 | 3 | 2217.10 | -4428.18 | 254.63 | 5.09E-56 | 5.09E-56 |
| 13 | 10 | 2247.77 | -4475.41 | 207.40 | 9.18E-46 | 9.18E-46 |
| 14 | 30 | 2304.49 | -4547.94 | 134.87 | 5.16E-30 | 5.16E-30 |
| 15 | 37 | 2335.16 | -4594.75 | 88.07 | 7.52E-20 | 7.52E-20 |
| 16 | 3 | 2176.94 | -4347.86 | 334.95 | 1.84E-73 | 1.84E-73 |
| 17 | 5 | 2257.53 | -4505.03 | 177.79 | 2.48E-39 | 2.48E-39 |
| 18 | 5 | 2186.56 | -4363.08 | 319.74 | 3.72E-70 | 3.72E-70 |
| 19 | 7 | 2267.15 | -4520.24 | 162.58 | 4.97E-36 | 4.97E-36 |
| 20 | 3 | 2260.27 | -4514.53 | 168.29 | 2.86E-37 | 2.86E-37 |
| 21 | 4 | 2260.68 | -4513.34 | 169.47 | 1.58E-37 | 1.58E-37 |
| 22 | 5 | 2294.69 | -4579.34 | 103.48 | 3.39E-23 | 3.39E-23 |
| 23 | 6 | 2295.10 | -4578.15 | 104.67 | 1.87E-23 | 1.87E-23 |
| 24 | 6 | 2267.15 | -4522.26 | 160.56 | 1.37E-35 | 1.37E-35 |
| 25 | 8 | 2301.57 | -4587.06 | 95.76 | 1.61E-21 | 1.61E-21 |
| 26 | 3 | 2241.96 | -4477.91 | 204.90 | 3.20E-45 | 3.20E-45 |
| 27 | 4 | 2243.42 | -4478.81 | 204.01 | 5.02E-45 | 5.02E-45 |

| | | | | | | |
|----|---|---------|----------|--------|----------|----------|
| 28 | 5 | 2251.07 | -4492.10 | 190.72 | 3.86E-42 | 3.86E-42 |
| 29 | 6 | 2252.52 | -4492.99 | 189.82 | 6.03E-42 | 6.03E-42 |
| 30 | 6 | 2251.53 | -4491.01 | 191.81 | 2.24E-42 | 2.24E-42 |
| 31 | 8 | 2260.63 | -4505.18 | 177.63 | 2.68E-39 | 2.68E-39 |

Table S3: Results for the Adult Female data set (n=24) using congruence coefficients. Model parameters, raw log-likelihood fits for each tested model, AIC_c and ΔAIC_c scores are provided. Model log-likelihoods and the model posterior probability are also shown. Sample size used to calculate AIC_c was 1830. See methods for details. Model ID's correspond to the numbering in Table 1. The optimal model in the set of evaluated models is highlighted in bold italics.

| Model ID | K | LogL | AIC_c | ΔAIC_c | Model LogL | Model Post. Prob. |
|-----------------|-----------|----------------|------------------------|-------------------------|-------------------|--------------------------|
| 1 | 2 | 2078.86 | -4153.72 | 916.21 | 1.11E-199 | 1.11E-199 |
| 2 | 3 | 2134.49 | -4262.97 | 806.96 | 5.89E-176 | 5.89E-176 |
| 3 | 4 | 2147.54 | -4287.06 | 782.88 | 1.00E-170 | 1.00E-170 |
| 4 | 3 | 2219.34 | -4432.67 | 637.26 | 4.17E-139 | 4.17E-139 |
| 5 | 8 | 2380.83 | -4745.58 | 324.35 | 3.69E-71 | 3.69E-71 |
| 6 | 17 | 2395.76 | -4757.18 | 312.75 | 1.22E-68 | 1.22E-68 |
| 7 | 22 | 2557.25 | -5069.93 | 0.00 | 1.00 | 1.000 |
| 8 | 3 | 2153.94 | -4301.87 | 768.06 | 1.65E-167 | 1.65E-167 |
| 9 | 8 | 2226.56 | -4437.03 | 632.90 | 3.69E-138 | 3.69E-138 |
| 10 | 17 | 2257.63 | -4480.93 | 589.01 | 1.26E-128 | 1.26E-128 |
| 11 | 22 | 2330.25 | -4615.93 | 454.00 | 2.60E-99 | 2.60E-99 |
| 12 | 3 | 2172.35 | -4338.69 | 731.24 | 1.63E-159 | 1.63E-159 |
| 13 | 10 | 2246.04 | -4471.95 | 597.98 | 1.41E-130 | 1.41E-130 |
| 14 | 30 | 2417.44 | -4773.85 | 296.09 | 5.07E-65 | 5.07E-65 |
| 15 | 37 | 2491.12 | -4906.68 | 163.26 | 3.54E-36 | 3.54E-36 |
| 16 | 3 | 2079.47 | -4152.93 | 917.00 | 7.50E-200 | 7.50E-200 |

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|----|---|---------|----------|--------|-----------|-----------|
| 17 | 5 | 2214.56 | -4419.08 | 650.85 | 4.67E-142 | 4.67E-142 |
| 18 | 5 | 2109.73 | -4209.43 | 860.51 | 1.39E-187 | 1.39E-187 |
| 19 | 7 | 2244.82 | -4475.57 | 594.36 | 8.62E-130 | 8.62E-130 |
| 20 | 3 | 2262.47 | -4518.93 | 551.01 | 2.24E-120 | 2.24E-120 |
| 21 | 4 | 2265.54 | -4523.05 | 546.88 | 1.76E-119 | 1.76E-119 |
| 22 | 5 | 2324.39 | -4638.75 | 431.18 | 2.34E-94 | 2.34E-94 |
| 23 | 6 | 2327.46 | -4642.87 | 427.06 | 1.84E-93 | 1.84E-93 |
| 24 | 6 | 2286.11 | -4560.17 | 509.76 | 2.03E-111 | 2.03E-111 |
| 25 | 8 | 2348.03 | -4679.99 | 389.95 | 2.11E-85 | 2.11E-85 |
| 26 | 3 | 2181.12 | -4356.23 | 713.70 | 1.05E-155 | 1.05E-155 |
| 27 | 4 | 2181.12 | -4354.23 | 715.71 | 3.85E-156 | 3.85E-156 |
| 28 | 5 | 2204.15 | -4398.27 | 671.66 | 1.42E-146 | 1.42E-146 |
| 29 | 6 | 2204.15 | -4396.26 | 673.67 | 5.17E-147 | 5.17E-147 |
| 30 | 6 | 2195.90 | -4379.76 | 690.18 | 1.35E-150 | 1.35E-150 |
| 31 | 8 | 2218.93 | -4421.78 | 648.15 | 1.80E-141 | 1.80E-141 |

Table S4: Results for the Juvenile (M1 erupted) data set (n=42) using congruence coefficients. Model parameters, raw log-likelihood fits for each tested model, AIC_c and ΔAIC_c scores are provided. Model log-likelihoods and the model posterior probability are also shown. Sample size used to calculate AIC_c was 1830. See methods for details. Model ID's correspond to the numbering in Table 1. The optimal model in the set of evaluated models is highlighted in bold italics.

| Model ID | K | LogL | AIC_c | ΔAIC_c | Model LogL | Model Post. Prob. |
|-----------------|-----------|----------------|------------------------|-------------------------|-------------------|--------------------------|
| 1 | 2 | 2370.87 | -4737.74 | 578.45 | 2.47E-126 | 2.47E-126 |
| 2 | 3 | 2401.99 | -4797.96 | 518.23 | 2.94E-113 | 2.94E-113 |
| 3 | 4 | 2401.99 | -4795.95 | 520.24 | 1.08E-113 | 1.08E-113 |
| 4 | 3 | 2497.10 | -4988.19 | 328.00 | 5.97E-72 | 5.97E-72 |
| 5 | 8 | 2620.86 | -5225.63 | 90.56 | 2.17E-20 | 2.17E-20 |
| 6 | 17 | 2556.62 | -5078.90 | 237.28 | 2.98E-52 | 2.98E-52 |
| 7 | 22 | 2680.37 | -5316.19 | 0.00 | 1.00 | 1.000 |
| 8 | 3 | 2426.61 | -4847.21 | 468.98 | 1.46E-102 | 1.46E-102 |
| 9 | 8 | 2491.29 | -4966.49 | 349.69 | 1.16E-76 | 1.16E-76 |
| 10 | 17 | 2486.80 | -4939.26 | 376.93 | 1.41E-82 | 1.41E-82 |
| 11 | 22 | 2551.47 | -5058.38 | 257.81 | 1.04E-56 | 1.04E-56 |
| 12 | 3 | 2427.43 | -4848.84 | 467.35 | 3.29E-102 | 3.29E-102 |
| 13 | 10 | 2521.49 | -5022.85 | 293.33 | 2.01E-64 | 2.01E-64 |
| 14 | 30 | 2575.48 | -5089.93 | 226.26 | 7.40E-50 | 7.40E-50 |
| 15 | 37 | 2669.54 | -5263.52 | 52.67 | 3.65E-12 | 3.65E-12 |
| 16 | 3 | 2373.02 | -4740.03 | 576.15 | 7.76E-126 | 7.76E-126 |
| 17 | 5 | 2498.93 | -4987.83 | 328.36 | 4.98E-72 | 4.98E-72 |
| 18 | 5 | 2377.82 | -4745.60 | 570.58 | 1.26E-124 | 1.26E-124 |
| 19 | 7 | 2503.72 | -4993.39 | 322.80 | 8.03E-71 | 8.03E-71 |
| 20 | 3 | 2570.70 | -5135.39 | 180.80 | 5.49E-40 | 5.49E-40 |
| 21 | 4 | 2582.24 | -5156.45 | 159.74 | 2.06E-35 | 2.06E-35 |
| 22 | 5 | 2618.04 | -5226.05 | 90.14 | 2.67E-20 | 2.67E-20 |
| 23 | 6 | 2629.57 | -5247.10 | 69.08 | 9.97E-16 | 9.97E-16 |
| 24 | 6 | 2584.75 | -5157.46 | 158.73 | 3.41E-35 | 3.41E-35 |
| 25 | 8 | 2632.09 | -5248.11 | 68.08 | 1.65E-15 | 1.65E-15 |
| 26 | 3 | 2446.94 | -4887.87 | 428.32 | 9.80E-94 | 9.80E-94 |
| 27 | 4 | 2451.77 | -4895.51 | 420.68 | 4.48E-92 | 4.48E-92 |

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|----|---|---------|----------|--------|----------|----------|
| 28 | 5 | 2465.94 | -4921.85 | 394.34 | 2.35E-86 | 2.35E-86 |
| 29 | 6 | 2470.77 | -4929.49 | 386.70 | 1.07E-84 | 1.07E-84 |
| 30 | 6 | 2461.70 | -4911.35 | 404.84 | 1.23E-88 | 1.23E-88 |
| 31 | 8 | 2480.70 | -4945.32 | 370.86 | 2.94E-81 | 2.94E-81 |

Table S5: Results for the Infant (deciduous dentition only) data set (n=42) using congruence coefficients. Model parameters, raw log-likelihood fits for each tested model, AIC_c and ΔAIC_c scores are provided. Model log-likelihoods and the model posterior probability are also shown. Sample size used to calculate AIC_c was 1830. See methods for details. Model ID's correspond to the numbering in Table 1. The optimal model in the set of evaluated models is highlighted in bold italics.

| Model ID | K | LogL | AIC_c | ΔAIC_c | Model LogL | Model Post. Prob. |
|-----------------|-----------|----------------|---------------------------|----------------------------------|-------------------|--------------------------|
| 1 | 2 | 2015.51 | -4027.02 | 923.56 | 2.83E-201 | 2.83E-201 |
| 2 | 3 | 2038.25 | -4070.49 | 880.09 | 7.78E-192 | 7.78E-192 |
| 3 | 4 | 2053.90 | -4099.78 | 850.79 | 1.79E-185 | 1.79E-185 |
| 4 | 3 | 2120.12 | -4234.23 | 716.35 | 2.80E-156 | 2.80E-156 |
| 5 | 8 | 2327.91 | -4639.75 | 310.83 | 3.19E-68 | 3.19E-68 |
| 6 | 17 | 2289.78 | -4545.22 | 405.36 | 9.48E-89 | 9.48E-89 |
| 7 | 22 | 2497.57 | -4950.58 | 0.00 | 1.00 | 1.000 |
| 8 | 3 | 2048.56 | -4091.11 | 859.47 | 2.34E-187 | 2.34E-187 |
| 9 | 8 | 2147.33 | -4278.58 | 672.00 | 1.19E-146 | 1.19E-146 |
| 10 | 17 | 2183.26 | -4332.19 | 618.39 | 5.23E-135 | 5.23E-135 |
| 11 | 22 | 2282.03 | -4519.50 | 431.07 | 2.47E-94 | 2.47E-94 |
| 12 | 3 | 2046.33 | -4086.64 | 863.94 | 2.50E-188 | 2.50E-188 |
| 13 | 10 | 2186.52 | -4352.92 | 597.66 | 1.66E-130 | 1.66E-130 |
| 14 | 30 | 2315.57 | -4570.11 | 380.47 | 2.41E-83 | 2.41E-83 |
| 15 | 37 | 2455.77 | -4835.96 | 114.61 | 1.29E-25 | 1.29E-25 |
| 16 | 3 | 2016.76 | -4027.51 | 923.07 | 3.62E-201 | 3.62E-201 |
| 17 | 5 | 2202.45 | -4394.86 | 555.72 | 2.13E-121 | 2.13E-121 |
| 18 | 5 | 2049.95 | -4089.86 | 860.72 | 1.25E-187 | 1.25E-187 |
| 19 | 7 | 2235.63 | -4457.20 | 493.38 | 7.33E-108 | 7.33E-108 |
| 20 | 3 | 2218.66 | -4431.30 | 519.28 | 1.74E-113 | 1.74E-113 |
| 21 | 4 | 2237.35 | -4466.69 | 483.89 | 8.39E-106 | 8.39E-106 |
| 22 | 5 | 2324.18 | -4638.32 | 312.26 | 1.56E-68 | 1.56E-68 |
| 23 | 6 | 2342.87 | -4673.70 | 276.88 | 7.53E-61 | 7.53E-61 |
| 24 | 6 | 2282.04 | -4552.03 | 398.55 | 2.86E-87 | 2.86E-87 |
| 25 | 8 | 2387.56 | -4759.04 | 191.54 | 2.56E-42 | 2.56E-42 |
| 26 | 3 | 2116.35 | -4226.70 | 723.88 | 6.47E-158 | 6.47E-158 |
| 27 | 4 | 2160.11 | -4312.20 | 638.38 | 2.39E-139 | 2.39E-139 |

| | | | | | | |
|----|---|---------|----------|--------|-----------|-----------|
| 28 | 5 | 2141.88 | -4273.73 | 676.85 | 1.06E-147 | 1.06E-147 |
| 29 | 6 | 2185.64 | -4359.23 | 591.35 | 3.90E-129 | 3.90E-129 |
| 30 | 6 | 2179.53 | -4347.02 | 603.56 | 8.68E-132 | 8.68E-132 |
| 31 | 8 | 2205.06 | -4394.04 | 556.54 | 1.41E-121 | 1.41E-121 |

Table S6: Results for the Juvenile (M1 erupted) data set (n=42) using congruence coefficients for individual x-, y-, and z-coordinates. Model parameters, raw log-likelihood fits for each tested model, AIC_c and ΔAIC_c scores are provided. Model log-likelihoods and the model posterior probability are also shown. Sample size used to calculate AIC_c was 16653. See methods for details. Model ID's correspond to the numbering in Table 1. The optimal model in the set of evaluated models is highlighted in bold italics.

| Model ID | K | LogL | AIC_c | ΔAIC_c | Model LogL | Model Post. Prob. |
|-----------------|-----------|-------------|---------------------------|----------------------------------|-------------------|--------------------------|
| 1 | 2 | 20945.27 | -41886.54 | 941.41 | 3.75E-205 | 3.75E-205 |
| 2 | 3 | 20984.40 | -41962.79 | 865.17 | 1.35E-188 | 1.35E-188 |
| 3 | 4 | 20988.41 | -41968.81 | 859.15 | 2.75E-187 | 2.75E-187 |
| 4 | 3 | 21151.61 | -42297.23 | 530.73 | 5.67E-116 | 5.67E-116 |
| 5 | 8 | 21282.48 | -42548.96 | 279.00 | 2.61E-61 | 2.61E-61 |
| 6 | 17 | 21305.14 | -42576.24 | 251.71 | 2.19E-55 | 2.19E-55 |
| 7 | 22 | 21436.01 | -42827.96 | 0.00 | 1.00 | 1.000 |
| 8 | 3 | 21034.66 | -42063.31 | 764.65 | 9.10E-167 | 9.10E-167 |
| 9 | 8 | 21095.65 | -42175.30 | 652.66 | 1.89E-142 | 1.89E-142 |
| 10 | 17 | 21118.13 | -42202.23 | 625.73 | 1.33E-136 | 1.33E-136 |
| 11 | 22 | 21179.13 | -42314.20 | 513.76 | 2.75E-112 | 2.75E-112 |
| 12 | 3 | 21084.55 | -42163.10 | 664.86 | 4.24E-145 | 4.24E-145 |
| 13 | 10 | 21158.55 | -42297.09 | 530.86 | 5.30E-116 | 5.30E-116 |
| 14 | 30 | 21312.40 | -42564.68 | 263.28 | 6.76E-58 | 6.76E-58 |
| 15 | 37 | 21386.40 | -42698.63 | 129.33 | 8.26E-29 | 8.26E-29 |
| 16 | 3 | 20945.27 | -41884.54 | 943.41 | 1.38E-205 | 1.38E-205 |
| 17 | 5 | 21096.60 | -42183.21 | 644.75 | 9.87E-141 | 9.87E-141 |
| 18 | 5 | 20968.11 | -41926.22 | 901.73 | 1.55E-196 | 1.55E-196 |
| 19 | 7 | 21119.45 | -42224.89 | 603.07 | 1.11E-131 | 1.11E-131 |
| 20 | 3 | 21133.24 | -42260.48 | 567.47 | 5.96E-124 | 5.96E-124 |
| 21 | 4 | 21133.24 | -42258.48 | 569.47 | 2.19E-124 | 2.19E-124 |
| 22 | 5 | 21229.87 | -42449.74 | 378.21 | 7.44E-83 | 7.44E-83 |
| 23 | 6 | 21229.87 | -42447.74 | 380.22 | 2.74E-83 | 2.74E-83 |
| 24 | 6 | 21156.37 | -42300.73 | 527.23 | 3.27E-115 | 3.27E-115 |
| 25 | 8 | 21253.00 | -42489.99 | 337.97 | 4.08E-74 | 4.08E-74 |
| 26 | 3 | 21030.26 | -42054.51 | 773.44 | 1.12E-168 | 1.12E-168 |
| 27 | 4 | 21042.91 | -42077.82 | 750.14 | 1.29E-163 | 1.29E-163 |

| | | | | | | |
|----|---|----------|-----------|--------|-----------|-----------|
| 28 | 5 | 21035.66 | -42061.31 | 766.65 | 3.34E-167 | 3.34E-167 |
| 29 | 6 | 21048.31 | -42084.61 | 743.34 | 3.84E-162 | 3.84E-162 |
| 30 | 6 | 21058.04 | -42104.08 | 723.88 | 6.48E-158 | 6.48E-158 |
| 31 | 8 | 21063.44 | -42110.87 | 717.09 | 1.93E-156 | 1.93E-156 |

Table S7: Results for the red fox, *Vulpes vulpes*, adult data set (n=22) using congruence coefficients for 55 landmarks, detailed in (Goswami 2006b). Model parameters, raw log-likelihood fits for each tested model, AIC_c and ΔAIC_c scores are provided. Model log-likelihoods and the model posterior probability are also shown. Sample size used to calculate AIC_c was 1485. See methods for details. Model ID's correspond to the numbering in Table 1. The 8-module model was not included, due to fewer landmarks in the fox dataset rendering some modules too small to analyze meaningfully. The optimal model in the set of evaluated models is highlighted in bold italics.

| Model ID | K | LogL | AIC_c | ΔAIC_c | Model LogL | Model Post. Prob. |
|-----------|-----------|-----------------|-----------------|----------------|------------|-------------------|
| 1 | 2 | 462.6197 | -921.231 | 1861.943 | 0 | 0 |
| 2 | 3 | 462.6197 | -919.223 | 1863.951 | 0 | 0 |
| 3 | 4 | 494.106 | -980.185 | 1802.99 | 0 | 0 |
| 4 | 3 | 534.5225 | -1063.03 | 1720.146 | 0 | 0 |
| 5 | 8 | 746.222 | -1476.35 | 1306.828 | 1.68E-284 | 1.68E-284 |
| 6 | 17 | 1043.7 | -2052.98 | 730.1918 | 2.76E-159 | 2.76E-159 |
| 7 | 22 | 1255.4 | -2466.11 | 317.0679 | 1.41E-69 | 1.41E-69 |
| 8 | 3 | 551.5688 | -1097.12 | 1686.053 | 0 | 0 |
| 9 | 8 | 970.3137 | -1924.53 | 858.6449 | 3.53E-187 | 3.53E-187 |
| 10 | 17 | 995.1886 | -1955.96 | 827.2147 | 2.36E-180 | 2.36E-180 |
| 11 | 22 | 1413.933 | -2783.17 | 0 | 1 | 1 |
| 16 | 3 | 463.084 | -920.152 | 1863.023 | 0 | 0 |
| 17 | 5 | 847.2522 | -1684.46 | 1098.711 | 2.62E-239 | 2.62E-239 |
| 18 | 5 | 561.2773 | -1112.51 | 1670.661 | 0 | 0 |
| 19 | 7 | 945.4455 | -1876.82 | 906.3596 | 1.54E-197 | 1.54E-197 |
| 20 | 3 | 594.9729 | -1183.93 | 1599.245 | 0 | 0 |
| 21 | 4 | 767.7127 | -1527.4 | 1255.776 | 2.05E-273 | 2.05E-273 |
| 22 | 5 | 704.1936 | -1398.35 | 1384.828 | 1.94E-301 | 1.94E-301 |
| 23 | 6 | 876.9334 | -1741.81 | 1041.365 | 7.42E-227 | 7.42E-227 |
| 24 | 6 | 822.5601 | -1633.06 | 1150.111 | 1.81E-250 | 1.81E-250 |
| 25 | 8 | 931.7808 | -1847.46 | 935.7106 | 6.50E-204 | 6.50E-204 |
| 26 | 3 | 754.149 | -1502.28 | 1280.893 | 7.20E-279 | 7.20E-279 |
| 27 | 4 | 841.7608 | -1675.49 | 1107.68 | 2.95E-241 | 2.95E-241 |
| 28 | 5 | 952.0534 | -1894.07 | 889.1084 | 8.56E-194 | 8.56E-194 |
| 29 | 6 | 1039.665 | -2067.27 | 715.9011 | 3.50E-156 | 3.50E-156 |

| | | | | | | |
|----|---|----------|----------|----------|-----------|-----------|
| 30 | 6 | 922.2105 | -1832.36 | 950.8106 | 3.42E-207 | 3.42E-207 |
| 31 | 8 | 1120.115 | -2224.13 | 559.0424 | 4.03E-122 | 4.03E-122 |

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