Equimolar Mixtures of Aqueous Linear and Branched SDBS Surfactant Simulated on Single Walled Carbon Nanotubes

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ABSTRACT

In our previous simulation study [J. Phys. Chem. C, 2011, 115, 17286], branched sodium dodecyl benzenesulfonate (SDBS) surfactants showed self-assembled structures on single-walled carbon nanotubes (SWNTs) that were strongly dependent on tube diameter. Those results suggested that branched SDBS, as opposed to their linear counterparts, could specifically stabilize SWNTs of narrow diameter. Experimental data, however, show that SDBS stabilizes aqueous SWNTs of many diameters. This discrepancy between simulated and experimental results could be explained by the fact that experimental SDBS samples are isomeric mixtures. We report here molecular dynamics (MD) simulation results for equimolar mixtures of aqueous linear and branched SDBS on (6,6) and (20,20) SWNTs at ambient conditions. Our results suggest that there is no strong effect due to nanotube diameter on the morphology of mixed SDBS surfactant aggregates, although the adsorbed aggregate structure strongly depends on surfactant coverage. In-plane radial distribution functions suggest that linear and branched molecules distribute evenly onto the surfaces of (6,6) SWNTs, while some evidence of segregation, in which branched SDBS predominantly pack near other branched molecules, was obtained on (20,20) SWNTs at high surface coverage. These results suggest that the lack of specificity in stabilizing aqueous dispersions of carbon nanotubes using SDBS surfactants is probably due to the presence of multiple isomeric molecules in commercial
surfactant samples. Perhaps more importantly, these simulations suggest that using mixtures of surfactants could affect the structure of the adsorbed aggregates, and the stability of aqueous dispersion of carbon nanotubes.

**Keywords:** Molecular dynamics, Carbon nanotubes, Sodium dodecyl benzenesulfonate

**INTRODUCTION**

Surfactants are extensively used in stabilizing dispersions of single-walled carbon nanotubes (SWNTs). As it is the case with polymers and lipids, surfactants physically adsorb on the SWNTs surface without altering their electronic properties. This adsorption is in general due to hydrophobic forces between the surfactant tails and the SWNT surfaces, yielding self-assembled structures in which the surfactant tails adsorb on the nanotube walls and the hydrophilic heads are exposed to water.

A wide variety of surfactants have been investigated for stabilizing aqueous dispersions of SWNTs, and it is now well-known that the surfactant aggregates self-assembled on SWNTs depend on surfactant type, molecular architecture, concentration, the presence of salts, nanotube diameter, temperature, pH, etc. For example, flavin mononucleotide (FMN) surfactants were shown to provide selectivity in stabilizing (8,6) SWNTs in water, due to the helical self-assembly of the flavin moiety on the SWNTs surface. Sodium dodecyl benzenesulfonate (SDBS) and sodium deoxycholate (DOC) were found to be effective dispersants for HiPCO nanotubes. Sodium dodecyl sulfate (SDS) was found not as good a stabilizer as sodium cholate (SC) or SDBS for (9,4) SWNTs at 40°C. Gemini surfactants with aromatic spacers were found able to disperse SWNTs at higher surfactant/SWNT weight ratios than SDS, SDBS, or cetyltrimethylammonium bromide (CTAB). Two co-surfactants (DOC and SDS) were used to successfully suspend and isolate individual SWNTs with diameter up to 1.7 nm.
Understanding why some surfactants behave better than others would allow us to design novel compounds to stabilize carbon nanotubes of desired diameter, and perhaps chirality. Computer simulations, coupled with experiments, could prove useful in this objective because they can yield a detailed atomic-level picture of the aggregates formed on nanotubes. Using molecular dynamics (MD) simulations, Tummala and Striolo found disordered aggregates of SDS on SWNTs.\textsuperscript{27} Xu et al.\textsuperscript{28} computed the potential of mean force (PMF) between SWNTs covered by SDS; the results showed that the structure of adsorbed aggregates affects the PMF, with higher surfactant densities yielding more repulsive pair potentials. Lin and Blankschtein reported the structure of SC on SWNTs and calculated the SWNT-SWNT PMF.\textsuperscript{29} Suttipong et al. reported that the morphology of anionic dodecyl sulfate surfactants is affected by the counter-ions (Cs\textsuperscript{+} instead of Na\textsuperscript{+}), with Cs\textsuperscript{+} ions yielding a more compact coverage of (6,6) SWNTs.\textsuperscript{30} Lin et al. examined how self-assembled SC, SDS, and CTAB aggregates pre-formed on a SWNT influence the adsorption of aryl diazonium salt.\textsuperscript{31} They found that less rigid surfactant structures facilitate the formation of ionic bonds between the nanotube and the aryl group. Shih et al. developed coarse-grained (CG) MD simulations, combined with colloidal theories, to predict the amount of SC surfactant adsorbed as a function of bulk surfactant concentration.\textsuperscript{32} At high SC concentration small-diameter SWNTs can adsorb higher SC amounts than large-diameter ones, while the opposite occurs at low SC concentrations.

We previously studied the effect of SDBS molecular structure on the morphology of adsorbed self-assembled aggregates.\textsuperscript{33} Isomerically pure linear and branched SDBS were considered in our calculations. While the simulations were analysed by quantifying the structure of the self-assembled aggregates on SWNTs of different diameter [i.e., (6,6), (12,12) and (20,20) SWNTs were compared] and at different surface coverage, combining our results with insights from PMF calculations,\textsuperscript{21} we concluded that the branched molecules could be used to selectively stabilize aqueous dispersions of narrow, i.e., (6,6), SWNTs. This appears to be at odds with experimental observations. In fact, experiments show that SDBS can stabilize carbon nanotubes of a wide range of diameters.\textsuperscript{7, 19, 24, 34-36} The present investigation stems from the observation that commercial
SDBS samples typically contain isomeric mixtures: we are interested in quantifying the structure of self-assembled aggregates formed on (6,6) and (20,20) SWNTs by equimolar mixtures of linear and branched SDBS molecules, to understand whether the lack of specificity observed experimentally in the stabilization of SWNTs using SDBS surfactants could be due to the isomeric composition of the typical commercial samples. Linear-rich and branched-rich SDBS surfactant mixtures were not simulated, as it is expected that such systems would show features more similar to isomerically pure SDBS surfactants (linear and branched, respectively). We also did not consider SDBS surfactants in which the benzene ring is tethered to carbon atoms other than the first or the middle of the alkane chain, as it is expected that these surfactants would yield results intermediate between those obtained for the surfactants considered here and in our prior work.

The remainder of the manuscript is organized as follows: first, we summarize the simulation protocol; we then present the results in terms of the morphology of the surfactant aggregates and the packing of linear and branched surfactant molecules on the SWNT surfaces, and discuss the results against those presented previously for isomerically pure SDBS surfactants; finally, we summarise our conclusions.

**COMPUTATIONAL DETAILS**

Molecular dynamics (MD) simulations of aqueous mixtures containing SDBS surfactants self-assembled on (6,6) and (20,20) SWNTs were performed using the GROMACS 4.6.1 software package. Each simulated system was composed of one SWNT, a 50:50 mixture of linear and branched dodecyl benzenesulfonate surfactants, a sufficient number of Na\(^{+}\) ions to obtain an electrically neutral system, and water molecules. In the top panel of Fig. 1 we provide the schematic chemical structures for linear and branched SDBS surfactants. One SDBS consists of the dodecane backbone, one benzene ring, and one sulfonate head. In the branched molecule, the benzene-
sulfonate group is attached to the 5th carbon atom in the tail. Each portion of the surfactant (i.e., CH2 (CH for branched) and CH3 tail segments, centre of mass of benzene rings, centre of mass of the sulfonate group in the head groups, and Na+ ions) was used in quantifying the density profiles away from the SWNT surface. The vectors represented in the bottom panel of Fig. 1, one to identify the surfactant tail \( \vec{v}_{\text{tail}} \) and the other to identify the benzene-sulfonate segment \( \vec{v}_{\text{bs}} \), were used to compute the probability distribution of the orientation angle between each SDBS molecule and the SWNT axis. \( \vec{v}_{\text{tail}} \) was defined as the vector originating from the terminal CH3 group to the primary CH2 (linear SDBS) or CH3 (branched SDBS) group. \( \vec{v}_{\text{bs}} \) was defined as the vector originating from the carbon atom within the benzene ring [which is linked to CH2 (linear SDBS) or CH (branched SDBS) group of the tail] to the sulphur atom of the head.

We considered (6,6) and (20,20) SWNTs of 7.44 nm in length. Periodic boundary conditions were applied in three dimensions. Because of periodic boundary conditions, the SWNTs were infinitely long. The SWNTs diameters were of 0.81376 and 2.71252 nm for (6,6) and (20,20) SWNTs, respectively. The following SDBS surface coverages were examined: 1.0 SDBS molecules/nm² (\( \equiv 1.0 \text{ nm}^2/\text{headgroup} \)) and 2.8 SDBS molecules/nm² (\( \equiv 0.4 \text{ nm}^2/\text{headgroup} \)), which we refer to as ‘low’ and ‘high’ surface coverage, respectively. The compositions of the simulation systems studied in this work are listed in Table 1. The number of water molecules was sufficient to obtain a molecular density comparable to that of liquid water at ambient conditions far from the SWNTs (~33 water molecules per nm³).

The carbon atoms in SWNTs were treated as rigid uncharged Lennard-Jones (LJ) sites, based on the model proposed by Cheng and Steele.38 SDBS surfactants were assumed to completely dissociate into dodecyl benzene-sulfonate ions and Na+ ions. The SDBS hydrophobic tails (dodecyl groups) were modelled as chains of united-atom LJ spheres.39-41 The benzene-sulfonate groups were described within the all-atom formalism using the DREIDING force field.42 Water molecules were
modelled using the SPC/E formalism.\textsuperscript{43} The force fields were the same as those implemented in our prior work\textsuperscript{33} to provide sound comparison.

In all simulated systems, one SWNT was maintained at the centre of the simulation box of size 10×10×7.44 nm\textsuperscript{3}, and kept rigid throughout the simulation. The empty space outside of the SWNT was filled with the solvent molecules (mixed linear and branched molecules, Na\textsuperscript{+} ions, and water). The number of Na\textsuperscript{+} ions was always equal to the number of surfactants. Water was placed in the simulation system by using the genbox algorithm available in GROMACS. As the nanotube is hollow, the software inserted water molecules within it. These were removed, as we are interested in the behaviour of surfactants outside of the SWNTs. The equations of motion were integrated with the leaf-frog algorithm using a time step of 2 fs.\textsuperscript{44} All simulations were conducted under the NVT ensemble using the Nose-Hoover thermostat with a relaxation time of 0.1 ps.\textsuperscript{44} The long-range electrostatic interactions were calculated with the particle mesh Ewald method with a precision of 10\textsuperscript{-4}.\textsuperscript{45} All interactions were treated with cutoff set at 9 Å. The conjugate gradient algorithm was utilized to minimize the energy of the initial configurations for \textasciitilde2 ps. To ensure that the results were not affected by the initial configurations, we randomized them by performing short (X ns) MD runs at T = 600 K. The systems were then abruptly brought to T = 300 K, at which T equilibration was followed by production. Most systems were simulated for 250 ns, and one system, comprising of the (6,6) SWNT with surfactants at high surface coverage, was simulated for 300 ns. All systems were considered equilibrated when the results did not change over 50 ns of simulation time. Only the results collected during the last 20 ns of each simulation are reported in what follows.
Fig. 1 Top panel: schematic chemical structures of linear and branched SDBS surfactants; Bottom panel: vectors defined by surfactant tail $\mathbf{v}_{tail}$ and benzene-sulfonate segment $\mathbf{v}_{bs}$. Colour code: cyan for CH$_n$ groups in surfactant tail; purple and white for carbon and hydrogen atoms in benzene rings, respectively; red for oxygen atoms; yellow for sulphur atoms; blue for Na$^+$ ions; and grey for carbon atoms in SWNTs.

Table 1 Composition of simulated systems and population analysis results for equimolar mixtures of linear and branched SDBS surfactants adsorbed on SWNTs.

<table>
<thead>
<tr>
<th>SWNT</th>
<th>No. of C atoms in SWNT</th>
<th>No. of water molecules</th>
<th>No. of SDBS molecules simulated</th>
<th>Nominal surface coverage (nm$^2$/headgroup)</th>
<th>No. of adsorbed [non-adsorbed] SDBS molecules</th>
<th>Effective surface coverage (nm$^2$/headgroup)</th>
</tr>
</thead>
<tbody>
<tr>
<td>(6,6)</td>
<td>520</td>
<td>24105</td>
<td>10</td>
<td>0.95</td>
<td>10 [0]</td>
<td>0.95</td>
</tr>
<tr>
<td>(20,20)</td>
<td>2400</td>
<td>21465</td>
<td>32</td>
<td>0.99</td>
<td>30 [2]</td>
<td>1.07</td>
</tr>
<tr>
<td>(6,6)</td>
<td>520</td>
<td>23441</td>
<td>27</td>
<td>0.35</td>
<td>22 [5]</td>
<td>0.43</td>
</tr>
<tr>
<td>(20,20)</td>
<td>2400</td>
<td>19313</td>
<td>89</td>
<td>0.36</td>
<td>48 [41]</td>
<td>0.79</td>
</tr>
</tbody>
</table>
RESULTS AND DISCUSSION

Aggregate morphology – Inspection of simulation snapshots

Representative simulation snapshots of an equimolar mixture of linear and branched SDBS surfactants adsorbed on (6,6) and (20,20) SWNTs at low and high surface coverages are shown in Fig. 2 and 3, respectively. At low coverage, SDBS molecules lie flat on the SWNT surface. The surfactant tails and most benzene rings are close to the nanotube surfaces, while most of the head groups are slightly protruded into water. Some head groups can be found near the substrates. On the (6,6) SWNT the linear SDBS molecules tend to align along the nanotube axis (see Fig. 2a). Similar to what reported in the case of SDS,27 isomerically pure linear SDBS,33 CTAB,46 and single-tailed lipids3 self-assembled on narrow SWNTs, this preferential orientation rises from the maximization of the contacts between the alkane chain and the SWNT surface, while minimizing the bending of the alkyl tails.47 The branched SDBS molecules are found to assemble randomly on the nanotube surface on both (6,6) and (20,20) SWNTs at low coverage. On the (20,20) SWNT, shown in Fig. 2b, linear and branched SDBS surfactants wrap around the tube. Some linear molecules preferentially lie near each other, maximizing favourable tail-tail contacts. Our simulations show evidence of a few surfactants forming a small aggregate in water, even though unoccupied SWNT surface is available for adsorption. As noted previously,29 MD atomistic simulations are not long enough to describe the equilibrium amount of surfactants adsorbed on a SWNT. The effective surface coverage observed in our simulations is reported in Table 1 for all systems considered.

Upon increasing the surface coverage, the results in Fig. 3 show that equimolar SDBS mixtures not only pack more densely, but also remain highly disordered on both SWNTs. The results shown in Fig. 3a demonstrate that at the conditions chosen linear and branched molecules cover most of the (6,6) SWNT surface. Due to the reduction in nanotube surface area available per each surfactant molecule, most benzene rings and head groups are protruded toward the water phase. Similar behaviour is observed on the (20,20) SWNT (Fig. 3b), suggesting that the aggregate structure is due
mostly to the surface density rather than to the SWNT diameter. Within the simulated system containing the (20,20) SWNT we observe one surfactant micelle adsorbed on the aggregate, and two small micelles dispersed in water, suggesting that perhaps the amount of surfactants simulated exceeds the maximum amount that could be adsorbed on this SWNT. It is possible that the amount of surfactant simulated was larger than that which can be adsorbed on the (20,20) SWNT at the thermodynamic conditions considered, although it is also possible that the initial configurations led to the desorption of some of the surfactants from the nanotubes. As mentioned above, atomistic simulations are at present not able, because of computing power limitations, to assess the equilibrium amount of surfactant adsorbed. Coarse-grained approaches such as those proposed by Lin et al. will allow this type of calculations. Because a few surfactants desorbed in some of the systems simulated, the effective surface coverage differed from the nominal one in some cases. Both effective and nominal surface coverage are reported in Table 1. At high surface coverage, the simulation snapshots suggest that there is no preferential orientation of the linear molecules with respect to the nanotube axis, but instead the linear molecules tend to adopt random orientations.

In all cases considered in Fig. 2 and 3, it is clear that many counterions accumulate near the head groups. This is due to the strong electrostatic interactions between the oppositely charged groups on the sulfonate heads and on the Na\(^+\) counterions. On the (20,20) SWNT at high surface coverage we observe a high concentration of Na\(^+\) ions sandwiched between the head groups belonging to the surfactants in the micelle and those adsorbed on the SWNT (see Fig. 3b). Several reports document similar counterion-condensation phenomena.\(^{27, 29, 30, 33, 48}\)
Fig. 2 Front (left panels) and side (right panels) views of representative simulation snapshots for mixed linear and branched SDBS self-assembled on (a) (6,6) and (b) (20,20) SWNTs at low surface coverage. In the top panels of (a) and (b) we highlight the linear SDBS molecules (the branched isomer is transparent); in the bottom panels we highlight the branched SDBS molecules (the linear isomer is transparent). Water molecules are not shown for clarity. The colour code is the same as that used in Fig. 1.
Effective surface coverage

To quantify the effective surfactant coverage on the SWNTs we computed the time-averaged number of surfactant molecules adsorbed. One surfactant molecule was considered adsorbed if its centre of mass was found within a cutoff distance of 12 Å and 14 Å at low and high surface coverage.

**Fig. 3** Same as Fig. 2 but for high surface coverage.
coverage, respectively, from the nanotube surface. The number of non-adsorbed SDBS molecules was calculated as the difference between the latter number and the total number of SDBS molecules in the simulation box. Results regarding the population analysis are shown in Table 1. At low surface coverage all surfactants (linear and branched) remain adsorbed on the (6,6) SWNT, yielding the effective surface coverage of 0.95 nm² per SDBS head group. In the case of (20,20) SWNTs some SDBS molecules form one small aggregate in the bulk, yielding a higher effective surface coverage than that obtained on the narrow SWNT. As the number of surfactants in the simulated system increases, the number of non-adsorbed surfactants also increases, with the trend more pronounced on the (20,20) than on the (6,6) SWNT. On the (6,6) SWNT both at low and at high surface coverages, the numbers of linear and branched molecules adsorbed onto the tubes are equivalent, maintaining an equimolar surfactant mixture. This is not the case for the (20,20) SWNT, on which the adsorbed surfactants are enriched in linear molecules at both conditions considered. While these results suggest that perhaps different surfactant isomers have different propensity for adsorbing on the SWNTs, this cannot be guaranteed by the present simulations, because of the already mentioned limitations in the real time accessible with the available computing power. This however does not compromise the conclusions from the present study.

**Aggregates morphology – Radial density profiles**

We quantify the structural observations by calculating density distributions of surfactant tail, benzene ring, sulfonate head, and Na⁺ ion along the radial distance from the nanotube surface. These results are reported in Fig. 4. In the left and right panels we show results obtained at low and high surface coverages, respectively. At low surface coverage, our results suggest no strong effect of SWNT diameter on the adsorbed aggregate. Only the intensity of the peaks depends on the nanotube diameter. We observe a strong peak in the density profiles of the tail groups at 4.0 Å, indicating the formation of one surfactant layer near the SWNT surfaces (Fig. 4a). It should be
noted that this aggregate structure on the (6,6) SWNT is different than that proposed by Matarredona et al.,\textsuperscript{49} who suggested the formation of a cylindrical micelle of SDBS molecules with SWNTs at the centre. Our results are instead consistent with a disordered surfactant aggregate on the SWNT surface, which has been discussed for many simulated surfactant-SWNT systems reported in the literature.\textsuperscript{48} The surfactant aggregate is expected to resemble that proposed by Matarredona et al.\textsuperscript{49} only when the surfactants surface density is extremely high.\textsuperscript{28}

The density profiles obtained at low surfactant density show that most benzene rings are positioned close to the substrates, yielding a peak at 4.0 Å and a shoulder at 6.0 Å (Fig. 4b). Although some head groups are located near the SWNTs, as illustrated by two small peaks at 4.0 Å and 5.5 Å (Fig. 4c), one broad peak located at 7.5 - 10 Å from the nanotube surfaces indicates that the head groups are in large part projected towards water. On the two SWNTs, the results obtained for the counterion density profiles show that the Na\textsuperscript{+} ions strongly correlate to the head groups (Fig. 4d).

When the surface coverage increases, the peak at 4.0 Å in the tail density profiles for (6,6) and (20,20) SWNTs become stronger, suggesting that the surfactant monolayer becomes more compact via the packing of linear and branched molecules on the nanotube surfaces (Fig. 4e). The benzene rings are mainly away from the (6,6) SWNT, as demonstrated by a strong density peak at 6.5 Å (Fig. 4f), although some benzene rings remain positioned near the nanotube surface. We find that the majority of head groups on the (6,6) SWNT are projected into water, manifesting a broad peak at ~9.0 Å (Fig. 4g), while a few remain in contact with the (20,20) SWNT surface, as suggested by the density peaks at 4.0 Å and 5.5 Å. On the (20,20) SWNT, a small peak at 14 Å in the head group density profiles is due to the formation of the micellar aggregate adsorbed on the aggregate (the snapshot discussed in Fig. 3b). This density peak is consistent with a few surfactants desorbing from the SWNT and the formation of the micelles observed in the snapshot of Fig. 3. As mentioned above, coarse-grained approaches are needed to clarify why desorption occurs. The counterion density profiles show that the Na\textsuperscript{+} ions pack close to the head groups, yielding a strong peak at
~10.0 Å (Fig. 4h). On (20,20) SWNTs, some Na⁺ ions are located near the substrate, where they are attracted by the presence of sulfonate heads. In summary, based on our results at low and high surface coverages, the structure of linear and branched SDBS aggregates formed on the SWNTs does not depend strongly on the nanotube diameter.

It is worth noting that the position of the head groups is expected to play an important role in the stabilization of aqueous SWNT dispersions.\textsuperscript{27-29} Prior simulations have indeed suggested that the electrostatic repulsion between like-charged head groups, as well as the steric repulsion between such groups experienced at relatively close nanotube-nanotube separations, are necessary for stabilizing aqueous SWNT dispersions.
Fig. 4 Atomic density profiles of (a, e) surfactant tails, (b, f) benzene rings, (c, g) head groups, and (d, h) Na⁺ ions of SDBS molecules adsorbed on (6,6) and (20,20) SWNTs (r is measured radially from the nanotube surface). On the left and right panels we report the results obtained at low and high surface coverages, respectively. The black-solid and red-dashed lines represent the results obtained on (6,6) and (20,20) SWNTs, respectively. System compositions and effective coverages are reported in Table 1.
Surfactant packing arrangement on the SWNTs surfaces

To quantify whether linear and branched surfactants segregate from each other on the SWNT surfaces we computed in-plane radial distribution functions (RDFs) between the sulphur atoms in the head groups. Only the adsorbed surfactants were considered for these calculations. We projected the position of each atom of the surfactants adsorbed on the SWNT onto a plane parallel to the nanotube axis by unwrapping a circular arc of length \( r\theta \) onto a segment of length \( x \). \( r \) is the distance between the atom and the centre of the nanotube. \( \theta \) is the angle between the reference vector (y direction) and the vector connecting the atom to the centre of the nanotube. The distance between the reference point and the projected plane of each atom is equal to the corresponding \( r \). The atom z-coordinate in cylindrical and unwrapped coordinates is the same. The procedure is illustrated in Fig. 5. We used the unwrapped coordinates to calculate in-plane RDFs.\(^5\)0 The in-plane RDFs between linear-branched, linear-linear, and branched-branched SDBS molecules self-assembled on (6,6) and (20,20) SWNTs are shown in Fig. 6. On the (6,6) SWNT, at low and high surface coverage (Fig. 6a and b, respectively) the results are indicative of random packing, suggesting that linear and branched SDBS surfactants do not segregate on this substrate but instead they mix on the nanotube surface. On the (20,20) SWNT at low surface coverage (Fig. 6c) we instead observe a relatively strong peak at 6.5 Å in the RDF between linear surfactants, suggesting that the linear isomers prefer to segregate with other linear surfactants. Some evidence of preferential segregation among branched surfactants is observed at high surface coverage (Fig. 6d), but in general the results are consistent with a good degree of mixing of the two surfactant types on both SWNTs.
**Fig. 5** Left panel: SDBS surfactants adsorbed on a (6,6) SWNT. Middle panel: projection of the adsorbed surfactants on a plane. Right panel: algorithm implemented to project the atoms A and B in adsorbed surfactant on a plane. Linear and branched SDBS are shown in green and purple, respectively. Water molecules are not shown for clarity.

**Fig. 6** In-plane sulphur-sulphur radial distribution functions (RDFs) for SDBS molecules adsorbed on [(a) and (b)] (6,6) and [(c) and (d)] (20,20) SWNTs. In the left and right panels, the results are obtained at low and high surface coverage, respectively. The black-solid, blue-dashed, and red-dotted lines represent results for linear–branched, linear-linear, and branched-branched SDBS molecules, respectively.
Discussion

In this section we analyse the preferential orientation of linear and branched SDBS molecules adsorbed on SWNT surfaces, and compare the results to those obtained for isomerically pure surfactants presented in our prior report. We consider the orientation vectors shown in Fig. 1, bottom panel, with respect to the SWNT axis. An angle of 0° or 180° indicates that the correspondent vector is parallel to the nanotube axis, 90° indicates that the vector is perpendicular to the nanotube axis. The results are shown in Fig. 7 and 8, obtained on (6,6) and (20,20) SWNTs, respectively, in the form of probability distributions. On the (6,6) SWNT at low surface coverage, the surfactant tails of equimolar mixtures of linear and branched SDBS surfactants tend to be parallel to the SWNT axis, as indicated by the largest peaks in the angle distribution profiles at 0° and 180° (Fig. 7a). At these conditions the benzene-sulfonate segments are preferentially perpendicular to the SWNT axis, yielding one broad peak centred at ~90° (Fig. 7b). As the surface coverage increases the surfactant tails in equimolar SDBS mixtures are neither parallel nor perpendicular to the nanotube axis (Fig. 7c), while a significant amount of benzene-sulfonate groups remain perpendicular to the tube axis (Fig. 7d). Comparing the probability distributions just discussed against those obtained for pure linear and branched SDBS molecules, our results suggest that the surfactants from an equimolar mixture of linear and branched surfactants behave preferentially like pure branched SDBS surfactants, which orient their benzene-sulfonate groups for the most part perpendicularly to the nanotube axis. This is probably a consequence of the fact that when both linear and branched surfactants are present on the nanotube (1) the surfactant molecules wrap more tightly around the (6,6) SWNT than pure linear isomers do, and (2) linear molecules within the equimolar mixtures accommodate the presence of the branched counterparts. On (20,20) SWNT, at low and high surface coverage (Fig. 8), the results show no significant difference in orientation probability distributions for either surfactant tails or benzene-sulfonate groups among those obtained for equimolar SDBS mixtures, pure linear and branched surfactants. The surfactant
tails tend to form any angle with respect to the nanotube axis (Fig. 8a and c), while the benzene-sulfonate segments mainly orient perpendicular to it, as indicated by the broad peak at $90^\circ$.

Fig. 7 Probability distribution of the surfactant tail [(a) and (c)] and the benzene-sulfonate segment [(b) and (d)] orientation angle with respect to the (6,6) SWNT axis. In the left and right panels, the results are obtained at low and high surface coverages, respectively. The black-solid, blue-dashed, and red-dotted lines represent the results obtained on mixed linear and branched, pure linear, and pure branched molecules, respectively. The results of pure linear and branched SDBS are reproduced from our prior work.$^{33}$
Finally, we compare the radial density profiles obtained from equimolar mixtures of linear and branched SDBS surfactants to those obtained for pure linear and branched ones. The results are shown in Fig. 9 and 10, obtained on (6,6) and (20,20) SWNTs, respectively. On the (6,6) SWNT at low surface coverage the peak positions of each surfactant segment (i.e., tail groups, benzene rings, head groups, and Na$^+$ ions) in the density profiles for equimolar SDBS mixtures are found near the correspondent peaks obtained for pure linear and branched surfactants. This can, for instance, be seen clearly in the benzene ring and sulfonate group density profiles, in which some benzene rings and head groups for equimolar SDBS mixtures remain in contact to the nanotube surface (which is consistent with results obtained for pure linear surfactants), while some other benzene rings are further from substrate (consistent with results obtained for pure branched molecules). When the surface coverage increases, the adsorbed aggregates formed by equimolar SDBS mixtures are very similar to those obtained for the pure branched surfactants (Fig. 9e-h). In particular, our results show that most head groups from the equimolar mixture of linear and branched SDBS surfactants are exposed to water, as was the case for pure branched surfactant. The Na$^+$ ions accumulate near
their head groups. On the (20,20) SWNT the radial density profiles obtained for the equimolar mixtures of linear and branched SDBS surfactants show that the results obtained for the surfactants near the tube surface are similar to those obtained for the pure linear surfactants, while those obtained for the surfactants whose heads are protruded into water are similar to those obtained for pure branched SDBS surfactants. This is observed both at low (Fig. 10a-d) and high (Fig. 10e-h) surface coverage.
Fig. 9 Radial atomic density profiles of (a, e) surfactant tails, (b, f) benzene rings, (c, g) sulfonate heads, and (d, h) Na\(^+\) ions belonging to mixed linear and branched systems (black-solid line), pure linear (blue-dashed line), and pure branched (red-dotted line) surfactants adsorbed on the (6,6) SWNT. In the left panels we report the results obtained at low surface coverage; in the right panels, we report those obtained at high surface coverage. The results of pure linear and branched SDBS are reproduced from our prior work.\(^{33}\)
CONCLUSIONS

We employed all-atom molecular dynamics simulations to investigate the morphology of equimolar mixtures of linear and branched SDBS surfactants on (6,6) and (20,20) SWNTs in water. Equimolar...
SDBS mixtures were found to yield disordered aggregates on both SWNTs, although the aggregates structure depends on surface coverage. At both surface coverages considered, the surfactant tails pack on the SWNT surfaces, while the head groups tend to extend more towards water as the surfactant coverage increases. We did not observe significant changes in the structure of the adsorbed aggregates as a function of the SWNT diameter. Comparing the self-assembled aggregates formed by equimolar SDBS mixtures against prior simulation results obtained for isomerically pure linear and branched SDBS surfactants at comparable surface densities, we found that, in general, mixtures of SDBS surfactants yield features (e.g., probability orientation distribution and radial density profiles for each surfactant portion) that are consistent with those obtained for either pure linear or pure branched SDBS surfactants. These simulation results suggest that experimentally SDBS does not show the ability of stabilizing SWNTs of selective diameters because experimental samples contain isomeric mixtures of the surfactants. While experimental validation is required to assess the reliability of our predictions, our simulations suggest that using mixtures of different surfactants could help manipulate the stability of aqueous dispersions of carbon nanotubes, which is consistent with recent advances reported in the literature (ACS Nano, 2015, 9, 5377).

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NOTES AND REFERENCES