Rates, Polarizations, and Asymmetries in Charmless Vector-Vector $B$ Meson Decays


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Charmless $B$ meson decays provide an opportunity to measure the weak-interaction phases arising from the elements of the Cabibbo-Kobayashi-Maskawa quark-mixing matrix [1] and to search for phenomena outside the standard model, including charged Higgs bosons and supersymmetric particles [2].

The decays to two vector particles are of special interest because their angular distributions reflect both
strong- and weak-interaction dynamics [3]. The asymmetries constructed from the number of $B$ decays with each flavor and with each sign of a triple product are sensitive to $CP$ violation or to final-state interactions (FSI) [4]. The triple product is defined as $(q_1 - q_2) \cdot p_1 \times p_2$, where $q_1$ and $q_2$ are the momenta of the two vector particles in the $B$ frame and $p_1$ and $p_2$ represent their polarization vectors.

The first evidence for the decays of $B$ mesons to pairs of charmless vector mesons was provided by the CLEO [5] and BABAR [6] experiments with the observation of $B \rightarrow \phi K^*$ decays. The CLEO experiment also set upper limits on the $B$ decay rates for several other vector-vector final states [7]. The BELLE experiment recently announced observation of $B^+ \rightarrow \rho^0 \rho^+$ [8].

In this analysis, we use the data collected with the BABAR detector [9] at the PEP-II asymmetric-energy $e^+ e^-$ collider [10]. These data represent an integrated luminosity of 81.9 fb$^{-1}$, corresponding to $88.9 \times 10^6$ $BB$ pairs, at the $\Upsilon(4S)$ resonance (on resonance) and 9.6 fb$^{-1}$ approximately 40 MeV below this energy (off resonance). The $\Upsilon(4S)$ resonance occurs at the $e^+ e^-$ center-of-mass (c.m.) energy, $\sqrt{s}$, of 10.58 GeV.

Charged-particle momenta are measured in a tracking system that is a combination of a silicon vertex tracker (SVT) consisting of five double-sided detectors and a 40-layer central drift chamber (DCH), both operating in a 1.5 T solenoidal magnetic field. Charged-particle identification is provided by the energy loss ($dE/dx$) in the tracking devices (SVT and DCH) and by an internally reflecting ring-imaging Cherenkov detector covering the central region. Photons are detected by a CsI(Tl) electromagnetic calorimeter.

We search for charmless vector-vector $B$ meson decays involving $\phi$, $\rho$, and $K^*(892)$ resonances. The event selection and analysis technique have been discussed earlier [6]. We fully reconstruct the charged and neutral decay products including the intermediate states $\phi \rightarrow K^+ K^-$, $K^{*0} \rightarrow K^+ \pi^-$ and $K^0 \pi^0$, $K^{*+} \rightarrow K^+ \pi^0$ and $K^0 \pi^+$, $\rho^0 \rightarrow \pi^+ \pi^-$, $\rho^+ \rightarrow \pi^+ \pi^0$, with $\pi^0 \rightarrow \gamma \gamma$ and $K^0 \rightarrow K^+ \pi^- \pi^0$, where inclusion of the charge conjugate states is implied. Candidate charged tracks are required to originate from the interaction point. Looser criteria are applied to tracks forming $K^0_S$ candidates, which are required to satisfy $|m_{\pi^+ \pi^-} - m_{K^0}| < 12$ MeV with the cosine of the angle between their reconstructed flight and momentum directions greater than 0.995, and the measured proper decay time greater than 5 times its uncertainty. Charged-particle identification provides separation of kaon tracks from pion tracks.

We reconstruct $\pi^0$ mesons from pairs of photons, each with a minimum energy of 30 MeV. The invariant mass of the $\pi^0$ candidates is required to be within 15 MeV of the nominal mass. The helicity angle of a $\phi$, $K^*$, or $\rho$ is defined as the angle between the momentum ($p_1$ or $p_2$) of one of its two daughters ($K^+$, $K$, or $\pi^+$, respectively) in the resonance rest frame and the momentum ($q_1$ or $q_2$) of the resonance in the $B$ frame. To suppress combinatorial background with low-energy $\pi^0$ candidates we restrict the $K^\ast \rightarrow K \pi^0$ and $\rho^+ \rightarrow \pi^+ \pi^0$ helicity-angle $\theta$ range to $\cos \theta < +0.5$.

We identify $B$ meson candidates kinematically using two nearly independent variables [9]: the beam-energy-substituted mass $m_{ES} = [(s/2 - \mathbf{p}_1 \cdot \mathbf{p}_B)/E^2 - \mathbf{p}_B^2]^{1/2}$ and the energy difference $\Delta E = (E_i E_b - \mathbf{p}_i \cdot \mathbf{p}_B - s)/\sqrt{s}$, where $(E_i, \mathbf{p}_i)$ is the initial state four-momentum obtained from the beam momenta, and $(E_b, \mathbf{p}_B)$ is the four-momentum of the reconstructed $B$ candidate. Our initial selection requires $m_{ES} > 5.2$ GeV and $|\Delta E| < 0.2$ GeV.

To reject the dominant quark-antiquark continuum background, we require $|\cos \theta_T| < 0.8$, where $\theta_T$ is the angle between the $B$-candidate thrust axis and that of the rest of the tracks and neutral clusters in the event, calculated in the c.m. frame. We also construct a Fisher discriminant that combines II event-shape variables defined in the c.m. frame [6,11].

Monte Carlo (MC) simulation [12] demonstrates that contamination from other $B$ decays is negligible for the modes with a narrow $\phi$ resonance and is relatively small for other charmless $B$ decay modes. We achieve further suppression of $B$-decay background by removing signal candidates that have decay products consistent with $D \rightarrow K \pi \pi$ decays. The remaining small background coming from $B$ decays (about 6% of the total background) is taken into account in the fit described below. In this analysis we do not explicitly provide a fit component for other partial waves with the same final-state particles selected within vector resonance mass windows.

We use an unbinned, extended maximum-likelihood (ML) fit [6] to extract signal yields, asymmetries, and angular polarizations simultaneously. We define the likelihood $L_i$ for each event candidate $i$ as the sum of $n_{ijk} P_i (x_i; \tilde{a})$ over three event categories $j$, where $P_i (x_i; \tilde{a})$ are the probability density functions (PDF’s) for measured variables $x_i$, $n_{ijk}$ are the yields to be extracted from the fit, and $k$ is the measured tag (1 or 2, as defined for asymmetry measurements later). There are three categories: signal ($j = 1$), continuum $q\bar{q}$ ($j = 2$), and $BB$ combinatorial background ($j = 3$). The fixed numbers $\tilde{a}$ parametrize the expected distributions of measured variables in each category. They are extracted from MC simulation, on-resonance $\Delta E$m$_{ES}$ sidebands, and off-resonance data.

The fit input variables $x_i$ are $\Delta E$, $m_{ES}$, Fisher discriminant, invariant masses of the candidate $K^*$ and $\phi$ (or $\rho$) resonances, and the $K^*$ and $\phi$ (or $\rho$) helicity angles $\theta_1$ and $\theta_2$. The correlations among the fit input variables in the data and signal MC are found to be small (typically less than 5%), except for angular correlations in the signal as discussed below. The PDF $P_i (x_i; \tilde{a})$ for a given candidate $i$ is the product of the PDF’s for each of the variables and a
TABLE I. Summary of results for the measured $B$-decay modes; $\varepsilon$ denotes the reconstruction efficiency, and $\varepsilon_{\text{tot}}$ is the total efficiency including daughter branching fractions, $n_{\text{sig}}$ is the fitted number of signal events, $B$ is the branching fraction, $f_L$ is the longitudinal polarization, and $A_{CP}$ is the signal charge asymmetry. The decay channels of $K^*$ are shown when more than one final state is measured for the same $B$ decay mode. All results include systematic errors, which are quoted following the statistical errors. The errors are combined for the reconstruction efficiency. The upper limit on the $B^0 \rightarrow \rho^0 \rho^0$ branching fraction is given at 90% confidence level including systematic uncertainties and conservatively assuming the efficiency for $f_L = 1$.

<table>
<thead>
<tr>
<th>Mode</th>
<th>$\varepsilon$ (%)</th>
<th>$\varepsilon_{\text{tot}}$ (%)</th>
<th>$n_{\text{sig}}$</th>
<th>$B \times 10^{-6}$</th>
<th>$f_L$</th>
<th>$A_{CP}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\phi K^{*+}$</td>
<td>5.0</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\rightarrow K^0 \pi^+$</td>
<td>23.9 ± 2.1</td>
<td>2.7</td>
<td>33.3$^{+7.2}_{-6.4} \times 1.2$</td>
<td>$12.7^{+2.2}_{-2.0} \times 1.1$</td>
<td>0.46 ± 0.12 ± 0.03</td>
<td>+0.16 ± 0.17 ± 0.03</td>
</tr>
<tr>
<td>$\rightarrow K^+ \pi^0$</td>
<td>14.3 ± 1.4</td>
<td>2.3</td>
<td>22.3$^{+7.5}_{-6.5} \times 3.2$</td>
<td>$10.7^{+3.6}_{-3.1} \times 1.8$</td>
<td>0.40$^{+0.20}_{-0.19} \times 0.06$</td>
<td>+0.63$^{+0.25}_{-0.31} \times 0.05$</td>
</tr>
<tr>
<td>$\phi K^{0*}$</td>
<td>10.3</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\rightarrow K^+ \pi^-$</td>
<td>29.7 ± 2.6</td>
<td>9.7</td>
<td>101$^{+11}_{-11} \times 3$</td>
<td>$11.7^{+1.4}_{-1.4} \times 0.8$</td>
<td>0.64 ± 0.07 ± 0.02</td>
<td>+0.04 ± 0.12 ± 0.02</td>
</tr>
<tr>
<td>$\rightarrow K^0 \pi^0$</td>
<td>10.5 ± 1.0</td>
<td>0.6</td>
<td>2.0$^{+3.3}_{-1.4} \times 0.6$</td>
<td>$3.8^{+6.6}_{-2.5} \times 1.1$</td>
<td>1.00$^{+0.00}_{-0.00} \times 0.25$</td>
<td></td>
</tr>
<tr>
<td>$\rho^0 K^{*+}$</td>
<td>4.8</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\rightarrow K^0 \pi^+$</td>
<td>12.3 ± 2.0</td>
<td>2.8</td>
<td>35.7$^{+11.8}_{-11.0} \times 3.6$</td>
<td>$14.3^{+4.7}_{-4.4} \times 2.9$</td>
<td>0.90$^{+0.10}_{-0.16} \times 0.04$</td>
<td>+0.17$^{+0.31}_{-0.34} \times 0.04$</td>
</tr>
<tr>
<td>$\rightarrow K^+ \pi^0$</td>
<td>6.0 ± 1.4</td>
<td>2.0</td>
<td>8.5$^{+8.2}_{-6.0} \times 5.2$</td>
<td>$4.82^{+4.6} \times 3.2$</td>
<td>1.00$^{+0.00}_{-0.00} \times 0.03$</td>
<td>+0.28$^{+0.72}_{-0.82} \times 0.19$</td>
</tr>
<tr>
<td>$\rho^0 \rho^+$</td>
<td>4.7 ± 0.9</td>
<td>4.6</td>
<td>93$^{+22}_{-23} \times 10$</td>
<td>$22.5^{+5.7}_{-5.4} \times 5.8$</td>
<td>0.97$^{+0.03}_{-0.07} \times 0.04$</td>
<td>-0.19 ± 0.23 ± 0.03</td>
</tr>
<tr>
<td>$\rho^0 \rho^0$</td>
<td>17.6 ± 1.5</td>
<td>17.6</td>
<td>9.7$^{+11.9}_{-9.4} \times 2.0$</td>
<td>&lt;2.1</td>
<td></td>
<td></td>
</tr>
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</table>

We rewrite the event yields $n_{jk}$ ($k = 1, 2$) in each category $j$ in terms of the asymmetry $A_j$ and the total event yield $n_j$: $n_{j1} = n_j \times (1 + A_j)/2$ and $n_{j2} = n_j \times (1 - A_j)/2$. We define three signal asymmetries using the tags $k$: $A_{CP} (k = 1$ for $Q_{ch} > 0$, $k = 2$ for $Q_{ch} < 0$), $A_{ip} (k = 1$ for $Q_{ch} \times Q_{ip} > 0$, $k = 2$ for $Q_{ch} \times Q_{ip} < 0$), and $A_{sp} (k = 1$ for $Q_{ip} > 0$, $k = 2$ for $Q_{ip} < 0$). A nonzero value for $A_{CP}$ would provide evidence for direct-CP violation, nonzero $A_{ip}$ indicates CP violation even in the absence of FSI, and $A_{sp}$ is sensitive to strong-interaction phases [4].

To describe the signal distributions, we use Gaussian functions for the parametrization of the PDF’s for $\Delta E$ and $m_{ES}$, and a relativistic $P$-wave Breit-Wigner distribution, convoluted with a Gaussian resolution function, for the resonance masses. For the background, we use low-degree polynomials or, in the case of $m_{ES}$, an empirical phase-space function [13]. The background parametrizations for resonance masses also include a resonant component to account for resonance production in the continuum. The background helicity-angle distribution is again separated into contributions from combinatorial background and from real vector mesons, both described by polynomials. The PDF for the Fisher discriminant is represented by a Gaussian distribution with different widths above and below the mean.

We denote $Q_{ip}$ as the sign of the triple product and $Q_{ch}$ as the $B$-flavor sign ($Q_{ch} = +1$ for $B$ and $Q_{ch} = -1$ for $\bar{B}$). The charged $B$ is intrinsically flavor tagged. The flavor of a neutral $B$ is determined from the charge of the kaon in the final states with the $K^{*0} \rightarrow K^+ \pi^-$ but is undetermined for the decay mode $K^{*0} \rightarrow K^0 \pi^0$ and for the decay $B^0 \rightarrow \rho^0 \rho^0$.

![FIG. 1. Projections of the multidimensional fit onto the variable $m_{ES}$ for (a) $B^+ \rightarrow \phi K^{*+}$, (b) $B^0 \rightarrow \phi K^{0*}$, (c) $B^+ \rightarrow \rho^0 K^{*+}$, and (d) $B^+ \rightarrow \rho^0 \rho^+$ candidates after a requirement on the signal-to-background probability ratio $P_{sig}/P_{bg}$ with the PDF for $m_{ES}$ excluded. The points with error bars show the data; the solid (dashed) line shows the signal-plus-background (background only) PDF projection.](https://example.com/figure1.png)
FIG. 2. Invariant mass projections (a) $\phi$, (b) $K^*$ for $B \to \phi K^*$; (c) $\rho^0$, (d) $K^{*+}$ for $B^+ \to \rho^0 K^{*+}$; (e) $\rho^0$, (f) $\rho^+$ for $B^+ \to \rho^0 \rho^+$ candidates after a requirement on the signal-to-background probability ratio $P_{\text{sig}}/P_{\text{bkg}}$ with the PDF for mass excluded. For point and line definitions, see Fig. 1.

The event yields $n_j$, asymmetries $\mathcal{A}_j$, and polarization $f_L$ are obtained by minimizing the quantity $\chi^2 \equiv -2 \ln L$. The dependence of $\chi^2$ on a fit parameter $n_j$, $\mathcal{A}_j$, or $f_L$ is obtained with the other fit parameters floating, their values are constrained to the physical range $0 \leq f_L \leq 1$ and $0 \leq n_j$. We quote statistical errors corresponding to unit change in $\chi^2$. When more than one $K^*$ decay channel is measured for the same $B$ decay, the channels are combined by adding their $\chi^2$ distributions for $n_j$, $\mathcal{A}_j$, or $f_L$. The statistical significance of a signal is defined as the square root of the change in $\chi^2$ when constraining the number of signal events to zero in the likelihood fit. If no significant event yield is observed, we quote an upper limit for the branching fraction obtained by integrating the normalized likelihood distribution. Performance of the ML fit is tested with generated MC and control samples.

The results of our maximum-likelihood fits are summarized in Table I. For the branching fractions, we assume equal production rates of $B^0 \overline{B}^0$ and $B^+ B^-$. We find significant signals in $\rho^0 K^{*+}$ (4.8$\sigma$), $\rho^0 \rho^+$ (6.1$\sigma$), and in both $\phi K^*$ (above 10$\sigma$ each) decay modes. We measure the charge asymmetries and longitudinal polarizations in the above modes. The projections of the fit results are shown in Figs. 1 and 2. The asymmetries involving triple products are obtained from separate fits. The results are shown in Table II.

Systematic uncertainties in the ML fit originate from assumptions about the PDF’s. We vary the PDF parameters within their respective uncertainties, and derive the associated systematic errors. The signals remain statistically significant under these variations. Additional systematic errors in the number of signal events originate from uncertainty in the background component for $\rho K^*$ that peaks in $m_{KS}$, where we take the uncertainties to be the estimated values.

The systematic errors in the efficiencies are for track finding (0.8% per track), particle identification (2% per track), and $K_S$ and $\phi^0$ reconstruction (5% each). Other minor systematic effects are from event-selection criteria, daughter branching fractions [14], MC statistics, and number of $B$ mesons. We account for the fake combinations in signal events passing the selection criteria with a systematic uncertainty of 3%–12%, depending on the mode. The reconstruction efficiency depends on the decay polarization. We calculate the efficiencies using the polarization measured in each decay mode [15] (combined for the two $\phi K^*$ modes) and assign a systematic error corresponding to the total polarization measurement error. The $B^0 \to \rho^0 \rho^0$ branching fraction limit incorporates uncertainties in the PDF’s and in the reconstruction efficiency, while we conservatively assume $f_L = 1$ for the efficiency (which is 29% for $f_L = 0$ and 18% for $f_L = 1$).

In the polarization and asymmetry measurements, we again include systematic errors from PDF variations that account for uncertainties in the detector acceptance and background parametrizations. The biases from the finite resolution in helicity-angle measurement and dilution due to the presence of the fake combinations are studied with MC simulation and are accounted for with a systematic error of 0.02 for polarization. We find the uncertainty on the charge asymmetry due to the track reconstruction efficiency to be less than 0.02 [6]. The asymmetry measurements are corrected by the small dilution factors.

In summary, we have observed the decays $B^+ \to \phi K^{*+}$, $B^0 \to \phi K^{*0}$, $B^+ \to \rho^0 K^{*+}$, and $B^+ \to \rho^0 \rho^+$, measured their branching fractions and longitudinal polarizations, and looked for asymmetries sensitive to $CP$ violation and FSI. These results supersede the earlier BABAR measurements of the $B \to \phi K^*$ [6]. Our asymmetry results rule out a significant part of the physical region, providing constraints on models with hypothetical particles, but are not yet sufficiently precise to allow detailed comparison with standard model predictions. Our measurement of longitudinal polarization is of interest for the study of decay dynamics.
We are grateful for the excellent luminosity and machine conditions provided by our PEP-II colleagues, and for the substantial dedicated effort from the computing organizations that support BABAR. The collaborating institutions wish to thank SLAC for its support and kind hospitality. This work is supported by DOE and NSF (USA), NSERC (Canada), IHEP (China), CEA and CNRS-IN2P3 (France), BMBF and DFG (Germany), INFN (Italy), FOM (The Netherlands), NFR (Norway), MIST (Russia), and PPARC (United Kingdom). Individuals have received support from the A.P. Sloan Foundation, Research Corporation, and Alexander von Humboldt Foundation.

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§Deceased.

[15] Preliminary BABAR results prior to polarization measurements assumed $f_L = 0.5$, leading to a smaller branching fraction. The systematic error on the branching ratio due to the unknown polarization was underestimated in the preliminary result.