Long-term variations in solar wind parameters, magnetopause location, and geomagnetic activity over the last five solar cycles

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Key Points:

• Average annual magnetopause standoff distance increased by nearly 2 $R_E$ from 1991 to 2009
• Solar wind dynamic pressure anticorrelates with sunspot number in cycles 20-21 and correlates in cycles 22-24
• The best correlation between annual solar wind dynamic pressure and sunspot number was found for 2-3 year delay

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Abstract

We use both solar wind observations and empirical magnetopause models to reconstruct time series of the magnetopause standoff distance for nearly five solar cycles. Since the average annual interplanetary magnetic field (IMF) $B_z$ is about zero, and the annual IMF cone angle varies between 54.0° and 61.2°, the magnetopause standoff distance on this time scale depends mostly on the solar wind dynamic pressure. The annual IMF magnitude well correlates with the sunspot number (SSN) with a zero time lag, while the annual solar wind dynamic pressure ($P_{dyn}$) correlates reasonably well with the SSN but with 3 years time lag. At the same time, we find an anticorrelation between $P_{dyn}$ and SSN in cycles 20–21 and a correlation in cycles 22–24 with 2 years time lag. Both the annual solar wind density and velocity well correlate with the dynamic pressure, but the correlation coefficient is higher for density than for velocity. The 11-year solar cycles in the dynamic pressure variations are superimposed by an increasing trend before 1991 and a decreasing trend between 1991 and 2009. The average annual solar wind dynamic pressure decreases by a factor of three from 1991 to 2009. Correspondingly, the predicted standoff distance in Lin et al.'s (2010) magnetopause model increases from 9.7 $R_E$ in 1991 to 11.6 $R_E$ in 2009. The annual SSN, IMF magnitude and magnetospheric geomagnetic activity indices display the same trends as the dynamic pressure. We calculate extreme solar wind parameters and magnetopause standoff distance in each year using daily values and find that both extremely small and large standoff distances during a solar cycle preferably occur at solar maximum rather than at solar minimum.

1 Introduction

Periodic variations of the coronal magnetic field (solar cycles) are synchronized with many processes in the geospace environment. Besides the well-known 11-year solar cycles, longer solar periodicities have also been revealed in the ground data. In particular, the studies of auroral records show variations with a mean period of about 80-90 years (Link, 1962; Gleissberg, 1965; Siscoe, 1980) often referred to as the Gleissberg cycle. The solar variations are transported to the Earth through the solar wind, solar energetic particles, and solar radiation. The 11-year periodicity has been observed in most solar wind parameters, such as the interplanetary magnetic field (IMF) magnitude (King, 1979), the IMF $|B_z|$ (Siscoe et al., 1978), and the helium content (Neugebauer, 1981; Aellig et al., 2001) almost from the start of the space era. A similar periodicity was found in the solar wind plasma parameters, e.g. density and velocity (Dmitriev et al., 2009).

However, the cycles of solar wind parameters and indices of geomagnetic activity might not have the same phase or shape as the sunspot cycle (Hirshberg, 1973; Feynman, 1982). In particular, Echer et al. (2004) reported about an average one-year time lag between the time series of the geomagnetic $aa$ index and sunspot numbers (SSN) using correlation analysis for the period of 1868-2000. At the same time, the authors noted that the time lag varied during the time interval. Gonzalez et al. (1990) observed a dual-peak solar cycle distribution of intense geomagnetic storms, with first peak occurring at the late ascending phase of the cycle or at solar maximum and second peak at the early descending phase of the cycle. The solar phenomena responsible for geomagnetic storms are Coronal Mass Ejections (CMEs) and Corotating Interaction Regions (CIRs). The occurrence rate of CMEs peaks during solar maximum, while the occurrence rate of CIRs peaks during the declining phase of the solar cycle (Borovsky & Denton, 2006, and references therein). Bothmer and the EU-INTAS-ESA Team (2004) noted that CIRs may play a role also during the rising phase. In general, however, the CME-driven storms mostly occur near solar maximum, and the CIR-driven storms mostly occur in the declining phase.

Several papers studied long-term variations in the solar wind velocity and the open solar magnetic flux by making reconstruction of the velocity from the geomagnetic indices (Lockwood et al., 2009; Rouillard et al., 2007). They mostly used the $aa$ index be-
cause the time series for \( \text{aa} \) is longer than for other geomagnetic indices. According to
Lockwood et al. (2009), the reconstructed annual solar wind velocity varied nearly from
300 to 550 km/s during the twentieth century. The averaged solar wind velocity and IMF
magnitude obtained from in-situ data between 1965 and 2010 were presented and dis-
cussed by Zerbo et al. (2013). This study also indicated significant variations in the so-
lar wind speed which generally match the variations in the \( \text{aa} \) index. Dmitriev et al. (2005,
2009) analyzed solar wind plasma and magnetic field properties during four solar cycles
from 20th to 23rd. In particular, Dmitriev et al. (2009) obtained the periodicity and dis-
tribution functions for several dimensional and dimensionless parameters. They showed
that the statistical distributions of both IMF magnitude and solar wind density are close
to a lognormal distribution function, while the velocity distribution is different from a
lognormal one. This reflects the observational fact that the relative dispersion of aver-
age solar wind velocity is smaller than the relative dispersion of IMF magnitude or so-
lar wind density.

The last (24th) solar cycle has the lowest sunspot activity since the Dalton min-
imum (early 1800s). Janardhan et al. (2015) reported that the solar photospheric fields
at high latitudes have been steadily declining since 1995. McComas et al. (2013) com-
pared average solar wind parameters observed from the mid-1970s through the mid-1990s
and from 2009 through the beginning of 2013. They showed a significant decrease in the
proton temperature, mass and momentum fluxes, and IMF magnitude in the last solar
cycle and noted that these results may have important implication for the solar wind in-
teraction with planetary magnetospheres. Similar results were obtained by Zerbo and
Richardson (2015) who noted that the solar wind magnetic field, speed, and density re-
mained anomalously low from the 23rd solar minimum to the 24th solar maximum. The
weak solar activity and small IMF result in decrease of the geomagnetic activity at the
same time. Kilpua et al. (2014) examined the geomagnetic activity using \( Dst \) and \( \text{AE} \)
indices, the solar wind conditions, and the occurrence rate of interplanetary coronal mass
ejections (ICME) during two periods, from 1995 to 1999 and from 2006 to 2012. They
concluded that the geomagnetic activity was considerably weaker during the second time
interval, in particular in terms of \( Dst \), and related this mainly to a weaker southward IMF
component.

The variations of solar wind parameters, such as the velocity and \( B_z \) magnitude,
modulate the solar wind energy input into the magnetosphere through the variations of
the reconnection rate at the dayside magnetopause. Besides, another consequence of vari-
ations in the solar wind parameters might be variable magnetospheric compression. Petrinec
et al. (1991) used 10 years ISEE data from 1977 to 1987 to study variations of the mag-
netopause size and shape with the solar wind data. Surprisingly, they found that the so-
lar wind dynamic pressure was the lowest values at solar maximum, in the 1979-1980 sea-
son, and the dynamic pressure had largest values, more than double the value in 1979-
1980, at the following solar minimum. According to most magnetopause models, the mag-
netopause standoff distance depends both on the solar wind dynamic pressure and IMF
\( B_z \). Since there are no continuous observations at the dayside magnetopause, the vari-
ations of magnetopause position during a solar cycle may be difficult to detect directly
using in situ observations. However, Petrinec et al. (1991) concluded that the average
size of the magnetosphere varies significantly throughout the course of the solar cycle
for both northward and southward IMF orientations. In agreement with the variations
of the dynamic pressure, the standoff magnetopause distance was largest near solar max-
imum. Richardson et al. (2000) studied the same solar maximum of cycle 21 using so-
lar wind data and geomagnetic \( \text{aa} \) index and showed both a temporal reduction in av-
verage solar wind speed and IMF magnitude and an associated depression in \( \text{aa} \) index in
1980. Dmitriev et al. (2005) also noted drops of the solar wind dynamic pressure and
flux density near solar maxima, especially in cycles 20 and 21.
To our knowledge, the long-term variations in the magnetopause size have not been studied so far, except for the above-mentioned work of Petrinec et al. (1991) in which only a relatively short time interval was investigated. At present, in situ solar wind data referred to the bow shock nose are available in the OMNIWeb database for almost five solar cycles. Besides, many empirical magnetopause models have been developed in order to predict the standoff distance as a function of the solar wind input parameters (Dmitriev et al., 2011; Kuznetsov & Suvorova, 1998; Lin et al., 2010; Petrinec & Russell, 1996; Pudovkin et al., 1998; Roelof & Sibeck, 1993; Shue et al., 1998). Despite some quantitative discrepancies in model predictions (Samsonov et al., 2016), they mostly use the same expressions connecting the solar wind dynamic pressure with the standoff distance. It is also known (and will be demonstrated again below) that the average IMF $B_z$ on the time scale of months or years is approaching zero (see, e.g., Dmitriev et al. (2009)), therefore we believe that the dynamic pressure is the main factor which determines the long-term variations in the magnetopause size.

Recent studies have pointed out that during intervals with a nearly radial IMF orientation, the dayside magnetopause expands (Dušík et al., 2010; Grygorov et al., 2017; Jelínek et al., 2010; Merka et al., 2003; Park et al., 2016) due to a significant decrease in the total pressure in the magnetosheath (Samsonov et al., 2012; Suvorova et al., 2010). In some exceptional cases, such time intervals may last several hours, and this may shift the magnetopause position about 1-2 $R_E$ outward (Samsonov et al., 2017). The magnetopause models have not taken into account this effect so far, nevertheless we discuss the influence of quasi-radial IMF intervals on our results below.

The main motivation of this work is to investigate how the average magnetopause size has varied in the space era using OMNI data and empirical magnetopause models. We do not limit our attention only to variations in the solar wind dynamic pressure, but also explore variations in the IMF $B_z$ and $|B|$, and in the geomagnetic indices searching for similar long-term trends. In addition to the study of average annual values, we consider variations in the extreme annual solar wind values and the extreme standoff distance. We highlight several events when our method predicts the extreme standoff distance and discuss them.

During very strong magnetospheric compressions, geosynchronous orbits may partly leave the magnetosphere and cross the magnetosheath or solar wind (such events are called geosynchronous magnetopause crossings, or GMCs). GMCs require sufficiently high dynamic pressures because the effects of negative IMF $B_z$ are saturated (Suvorova et al., 2005). GMCs may cause a significant damage to the geosynchronous spacecraft, therefore predictions of such events are an important space weather problem (Dmitriev et al., 2014; Dmitriev et al., 2016). In this work, we estimate the range of variations in the extreme annual magnetopause distance during the last five solar cycles using empirical magnetopause models.

The main reason of strong magnetospheric compression is a high solar wind dynamic pressure which is usually associated with a high solar wind speed. The intervals of high speed in the solar wind are associated both with CMEs and CIRs, however, an extremely high speed (e.g., $V_{SW} > 1000$ km/s) is usually related to CMEs (Gopalswamy, 2006, 2008; Yashiro et al., 2004). Consequently, extremely strong magnetic storms (in terms of the $Dst$ index) are mostly CME-driven (Gosling et al., 1990; Borovsky & Denton, 2006; Denton et al., 2006). Strong storms sometimes result from the interaction between two successive CMEs or a CME and a high speed stream (Liu et al., 2015; Lugaz et al., 2017). Oh et al. (2007) concluded that CMEs (or more precisely magnetic clouds) are also the most dominant and strong driver of interplanetary shocks. We suggest below that strong CMEs or sequences of CMEs result in events with extremely strong magnetospheric compression.
Besides the solar wind velocity, the dynamic pressure depends also on the solar wind density, and both CMEs and CIRs are usually accompanied by a density increase. We discuss below the correlations between the annual density, velocity and dynamic pressure.

The paper is organized as follows. In section 2, we show and discuss the average and extreme solar wind and magnetospheric parameters over the last five solar cycles. In section 3, we investigate events when the magnetosphere is extremely compressed. We close the paper with discussion and conclusions.

2 Solar wind and magnetospheric cycles and trends

We begin this study with the hourly average solar wind parameters from OMNI (omniweb.gsfc.nasa.gov) and find the daily average values. Later, we use these daily averages when finding maximal and minimal extreme values for each year (we call them extreme annual values below). On the next step, we calculate both the monthly and annual average values from the daily averages. The OMNI database contains solar wind parameters from 1964, but the data in 1964 and 1965 have many gaps, therefore we consider only the time interval from 1966 to 2018. However, the OMNI data still contain a lot of data gaps before 1995 (Lockwood et al., 2019). We exclude daily averages from the processing if they contain less than 8 hourly average solar wind values, either in magnetic field or in plasma data. Figure 1 shows the number of ”good” days, i.e. the days which can be used to find the averages for each year. We have tried different minimum threshold conditions demanding from 5 to 12 hours of good data for each day and found that the averages are slightly changed only before 1995, and that this does not change the conclusions of the paper. Thus, the considered time interval covers completely three solar cycles (21-23) and almost completely the 20th and 24th cycles, so nearly 5 cycles in total.

For a given solar wind dynamic pressure and IMF, we calculate the magnetopause standoff distance using Shue et al.’s (S98) and Lin et al.’s (L10) magnetopause models. We use the magnetospheric Dst and Kp indices for illustration of the magnetospheric response to solar wind variations. The Dst index reflects the variations in the ring current, magnetopause current, and partly in the tail current (Burton et al., 1975). We will use $-Dst$ throughout the paper because increase in the geomagnetic activity actually
means decrease in $D_{st}$. The $Kp$ index indicates the level of overall magnetospheric disturbance.

Figure 2 shows the annual sunspot numbers (SSN), average and extreme IMF magnitude and $B_z$ (we use GSM coordinates here and below), IMF cone angle (the angle between IMF vector and $x$ axis, i.e. $\cos(\angle B_z/|B|)$), solar wind dynamic pressure $P_{dyn}$ and velocity, magnetopause standoff distance, and $-D_{st}$ index. We discuss first the extreme annual solar wind values shown by red and blue lines in Figure 2. The maximum $|B|$, maximum and minimum $B_z$, maximum dynamic pressure, and finally maximum solar wind velocity in general display the 11-year cycle similar to the SSN, although with large fluctuations. The two exceptions are cycle 20 when both the maximum $|B|$ and maximum $D_{st}$ and the annual SSN is statistically significant with the coefficient of 0.364.

Since the extreme values in Figure 2 are obtained from daily averages (one extreme value for each year), we believe that they probably correspond to the strongest coronal mass ejections (CME) in each year reaching the Earth. Note that the date with extreme conditions for one parameter (e.g., for $|B|$) usually does not coincide with the date with extreme conditions for another parameter (e.g., $P_{dyn}$). However, the solar wind conditions for a whole day whether with a strong dynamic pressure, e.g. on average higher than 10 nPa, or with a high negative $B_z$, e.g. about -10 nT or lower, result in significant magnetospheric disturbances, possibly commencing magnetic storms.

Increase in the solar wind dynamic pressure results in decrease in the minimum magnetopause standoff distance as shown by blue lines on the 7th panel from the top of Figure 2. Both S98 and L10 models predict the smallest daily standoff distance in the middle of the 22nd cycle, in 1991, when the standoff distance decreased to 5.9 $R_E$ (see Table 3 below). Interestingly, the variations in the maximum standoff distance also roughly follow the solar cycles. The peaks in the maximum standoff distance which correspond to the deepest minima of the dynamic pressure are located mainly in the middle of solar cycles, although the correlation between maximum $R_{sub}$ and SSN is poor. In other words, the probability of getting an extremely small dynamic pressure seems to be higher near solar maximum than near solar minimum too. This is also the case for the extremely large dynamic pressure. The correlation between the maximum annual dynamic pressure and the annual SSN is statistically significant with the coefficient of 0.364.

Comparing the results of S98 (solid) and L10 (dashed) magnetopause models, we conclude that both models predict qualitatively very similar variations (since they are determined by dynamic pressure in both cases), but the L10 model usually predicts slightly larger maximum or smaller minimum standoff distance. The reason for this is that the L10 model implies a stronger dependence of the standoff distance on the dynamic pressure ($R_{S98} \sim P_{dyn}^{-0.15}$, while $R_{L10} \sim (P_{dyn} + Pm)^{-0.19}$, here $Pm$ is magnetic pressure). The maximum $D_{st}$ index also displays the 11-year cycle as expected.

After emphasizing the extreme solar wind parameters in Figure 2, we now consider the solar cycles and long-term trends in the average annual values. Figure 4 shows the annual SSN, IMF magnitude and average southward IMF, IMF cone angle, solar wind dynamic pressure, magnetopause standoff distance, $Kp$ and $-D_{st}$ indices. The average southward component $B_z$ has been obtained from hourly $B_z$ such that $B_z = 0$ for $B_z > 0$ and $B_z = -B_z$ for $B_z < 0$. Both the average $|B|$ and $B_z$ clearly vary with the 11-year periodicity, except may be during the 20th cycle. Note that the number of days with data gaps in the 20th cycle is larger than in the following cycles which might explain the different behavior of the average parameters in this cycle. At the same time, magneto-
Figure 2. The sunspot numbers (average daily number for each year), average and extreme IMF magnitude and $B_z$, IMF cone angle (the angle between IMF vector and x axis), solar wind dynamic pressure and velocity, magnetopause standoff distance (solid lines for Shue et al.’s model and dashed lines for Lin et al.’s model), and geomagnetic $-Dst$ index. Annual average values shown by black, daily maximal and minimal values for each year shown by red and blue. Vertical lines separate solar cycles as indicated by numbers at the top.
Table 1. Pearson correlation coefficients for annual sunspot numbers, solar wind parameters, magnetopause distance calculated by L10 model, and magnetospheric indices for a zero time lag between all parameters. Letter N instead of some correlation coefficients indicates that the correlation between these parameters is not statistically significant. The correlation between SSN and $P_{dyn}$ ($R_{sub}$) increases for a non-zero time lag (see explanation in text and Figure 4 below). All correlation coefficients for $Dst$ are negative because $Dst$ becomes stronger negative for more disturbed magnetospheric conditions.

|       | SSN  | $|B|$ | $B_s$ | $\theta$ | $N$ | $V$ | $P_{dyn}$ | $R_{sub}$ | $K_p$ | $Dst$ |
|-------|------|------|-------|---------|-----|-----|----------|----------|------|-------|
| SSN   | 1.000| 0.748| 0.784 | 0.301   | N   | N   | N        | N        | 0.435| -0.611|
| $|B|$  | 0.748| 1.000| 0.833 | N       | 0.339| 0.321| 0.665    | -0.588   | 0.836| -0.808|
| $B_s$ | 0.784| 0.833| 1.000 | N       | N   | N   | N        | -0.301   | 0.584| -0.714|
| $\theta$ | 0.301| N    | N     | 1.000   | -0.512| -0.608| -0.718   | 0.748    | -0.514| N     |
| $N$   | N    | 0.339| N     | -0.512  | 1.000| N   | 0.763    | -0.792   | 0.359| -0.371|
| $V$   | N    | 0.321| N     | -0.608  | N   | 1.000| 0.553    | -0.543   | 0.715| -0.346|
| $P_{dyn}$ | N    | 0.665| 0.340 | -0.718  | 0.763| 0.553| 1.000    | -0.976   | 0.828| -0.628|
| $R_{sub}$ | N    | -0.588| -0.301| 0.748   | -0.792| -0.543| -0.976   | 1.000    | -0.793| 0.582|
| $K_p$ | 0.435| 0.836| 0.584 | -0.514  | 0.359| 0.715| 0.828    | -0.793   | 1.000| -0.744|
| $Dst$ | -0.611| -0.808| -0.714| N       | -0.371| -0.346| -0.628   | 0.582    | -0.744| 1.000|

spheric indices in the 20th cycle also do not clearly match the solar cycle variations as they usually do, therefore the reason of unexpected variations in solar wind parameters in this cycle may be physical and is related to solar wind formation near the Sun.

According to Figure 4, the annual dynamic pressure exhibits slight correlation with the SSN (see discussion below), and even its annual plot displays several spikes in the whole 5-cycle interval. We suggest that the spikes of $P_{dyn}$ are related to strong CMEs or to pairs of CME-CME and CIR-CME (Lugaz et al., 2017), which usually concentrate near solar maximum and in the declining phase.

We quantify the correlations in Figure 4 by finding the Pearson correlation coefficients (Press et al., 1992) presented in Table 1. We show only the correlation coefficients for which p-values < 0.05, i.e. the correlation is statistically significant. The table demonstrates that the SSN well correlates with the IMF (the correlation coefficient $r$ is 0.75 for $|B|$ and 0.78 for $B_s$), but does not correlate with both the solar wind density and velocity (and correspondingly with the dynamic pressure). The IMF cone angle weakly correlates with the SSN ($r=0.30$), does not correlate with the IMF magnitude and $B_s$, but correlates reasonably well with the density ($r=-0.51$) and velocity ($r=-0.61$). The density and velocity do not correlate with each other, but both correlate with the dynamic pressure, and the correlation coefficient is higher for density ($r=0.76$) than for velocity ($r=0.55$). The magnetopause distance calculated by the L10 model anticorrelates extremely well with the dynamic pressure as expected. It is interesting to note that $K_p$ better correlates with $P_{dyn}$ and $V$, and $Dst$ better correlates with $B_s$, however both indices correlate well with $|B|$. As a result, the magnetopause distance is also better correlated with $K_p$ ($r=0.79$) than with $Dst$ ($r=0.58$). Finally, $Dst$ better correlates with SSN ($r=-0.61$) than $K_p$ ($r=0.43$).

Previous studies showed (Luhmann et al., 2009) that high speed solar wind streams mostly occur in the declining phases of solar cycles, therefore we have correlated the SSN and $P_{dyn}$ with variable time lag from 1 to 11 years. Indeed the correlation coefficient between the two parameters significantly increases: we obtain maximum correlation coefficient of 0.57 for the whole time series taking 3 years time lag, and 0.68 for only the
Figure 3. Expanded view of the annual average values from Fig. 2 (except for $B_s$ and $Kp$). From the top, the sunspot numbers, IMF magnitude and average southward component $B_s$, IMF cone angle, solar wind dynamic pressure, magnetopause standoff distance (solid lines for Shue et al.’s model and dashed lines for Lin et al.’s model), $Kp$ and $Dst$ indices. Vertical lines separate solar cycles as indicated by numbers at the top.
Figure 4. (a) The correlation coefficients between SSN and $B_s$ (black), $Dst$ (blue), and $Kp$ (red) as a function of time lag for five (plus signs) and three (stars) solar cycles. (b) The correlation coefficients between SSN and $P_{dyn}$ (black), $V$ (blue), and $N$ (red). Most correlations with coefficients below 0.3 are not statistically significant.

Since the correlations between the SSN and geomagnetic indices may also increase if taking into account a time lag (Echer et al., 2004), we calculate the correlations between the annual SSN and $B_s$, $Kp$, and $Dst$ for variable time lags from 0 to 4 years. As we note above, the correlation between SSN and $P_{dyn}$ is higher for three last solar cycles, than for the whole 53-year interval, therefore we provide the coefficients for both the last five and three cycles. Figure 4 shows the results of calculations. The left panel shows the correlation coefficients for $B_s$, $Dst$, and $Kp$, while the right panel shows the coefficients for $P_{dyn}$, $V$, and $N$.

The correlation coefficients between SSN and $B_s$, and SSN and $Dst$ are highest for a 0-year time lag. The correlation between SSN and $Kp$ is highest for 2-year time lag (for five cycles) and for 1-year time lag (for three cycles). As mentioned above, the correlation between SSN and $P_{dyn}$ is highest for 2–3 years time lag depending on the time interval. The correlation coefficient between SSN and $V$ peaks for 3-year time lag in both cases. The density correlation with the solar activity is significantly worse than with other solar wind parameters. In fact, the only statistically significant correlation (according to our criterion) has been obtained for 4-year time lag and 5 solar cycles interval. In this case, the correlation coefficient grows up to only 0.33.
Table 2. Comparison of average solar wind and magnetospheric parameters in cycles 22 and 24. The magnetopause standoff distance is calculated by the L10 model. \(< N_{22} >\) and \(< N_{24} >\) are the average values for corresponding cycles. \(N_{09}\) and \(N_{91}\) are the average annual values in 2009 (minimum between 23rd and 24th cycles) and 1991 (maximum of 24th cycle) respectively. The bottom two rows are dimensionless.

|                | SSN | \(|B|,\text{nT}\) | \(P_{\text{dyn}},\text{nPa}\) | \(R_{\text{sub}},R_E\) | \(K_p\) |
|----------------|-----|----------------|-----------------------------|---------------------|-------|
| \(< N_{22} >\) | 106.3 | 7.0 | 2.96 | 10.0 | 2.45 |
| \(< N_{24} >\) | 53.6 | 5.3 | 1.87 | 11.0 | 1.57 |
| \(< N_{24} > / < N_{22} >\) | 0.50 | 0.76 | 0.63 | 1.10 | 0.64 |
| \(N_{09}/N_{91}\) | 0.024 | 0.42 | 0.35 | 1.20 | 0.30 |

Considering the whole 53-year interval in Figure 4, we note that the dynamic pressure increases until 1991 (except for the local minima in 1980 and 1990) and then follows a decreasing trend between 1991 and 2009. It increases again in the present cycle until 2015. The average annual values vary significantly, from 3.80 nPa in 1991 to 1.33 nPa in 2009, i.e. by a factor of 3. Respectively, the average magnetopause standoff distance varies between 9.59 \(R_E\) for the S98 model (9.68 \(R_E\) for the L10 model) in 1991 and 11.04 \(R_E\) for the S98 model (11.62 \(R_E\) for the L10 model) in 2009. Thus the magnetopause models predict a 1.5–2 \(R_E\) variation in the standoff distance in the 17-years interval from the maximum of the 22nd to the minimum between the 23rd and 24th cycles.

In fact, the same decreasing trend after 1991 occurs for the other parameters in Figure 4, i.e. for the SSN, \(|B|\), and \(B_s\). At the same time the \(Dst\) index increases \((-Dst\) decreases) which may indicate both decrease in the average ring current and reduction in the magnetospheric compression (see discussion in Section 4). To emphasize this trend we draw the average solar wind and magnetospheric parameters for each solar cycle in Figure 5. In general, the trends for all of the parameters are very similar, taking into account that the variations of \(R_{\text{sub}}\) are reversed to \(P_{\text{dyn}}\). Both the average SSN and \(|B|\) have a maximum in the 21st cycle, while the solar wind dynamic pressure reaches its maximum in the 22nd cycle. However, the differences for all these parameters between the 21st and 22nd cycles are insignificant being smaller than the standard deviations. \(K_p\) has the maximum in the 21st cycle, and \(Dst\) in the 22nd cycle, but \(K_p\) in the 21st cycle is only 0.5% higher than in the 22nd cycle.

We quantify the differences between cycles 22 and 24 in Table 2. As follows from the table, the average \(P_{\text{dyn}}\) and \(K_p\) decrease by 37 % and 36 % respectively between cycles 22 and 24, and \(R_{\text{sub}}\) increases from 10.0 to 11.0 \(R_E\), i.e. by 10 %. If we compare the years 1991 and 2009, \(P_{\text{dyn}}\) and \(K_p\) decrease by 65 % and 70 % respectively, while \(R_{\text{sub}}\) increases by 20 %. In particular, the values of \(R_{\text{sub}}\) according to the L10 model in 1991 and 2009 are 9.68 and 11.62 \(R_E\) respectively. Note that the \(R_{\text{sub}}\) in the L10 model varies with \(P_{\text{dyn}}\) according to a power-law index of only -0.19, however the annual difference in the magnetopause position of about 2 \(R_E\) is significant and should be taken into account when preparing for the future space missions (as discussed in Section 4).

3 Extreme daily magnetopause distance

We further study the extreme solar wind conditions and identify the dates when the predicted magnetopause standoff distance is very small. We use the minimum daily average values shown by blue line in Figure 2. We take the L10 model which probably gives more realistic results for extreme solar wind and magnetospheric conditions (Dmitriev et al., 2016). Table 3 shows the dates and daily parameters for the events for which the
Figure 5. The sunspot numbers, IMF magnitude, solar wind dynamic pressure, magnetopause standoff distance in the L10 model, $K_p$ and $Dst$ indices averaged for each solar cycle. The error bars indicate standard deviations obtained from monthly values.
Table 3. The dates with daily minimal magnetopause distance according to the L10 model, the daily averages of $P_{dyn}$, $B_z$, and $R_{sub}$, average and minimal $Dst$, and average $Kp$.

<table>
<thead>
<tr>
<th>Date</th>
<th>$P_{dyn}$, nPa</th>
<th>$B_z$, nT</th>
<th>$R_{sub}$, $R_E$</th>
<th>$Dst$</th>
<th>$Dst_{min}$</th>
<th>$Kp$</th>
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<td>5 Jun 1991</td>
<td>20</td>
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<td>6.6</td>
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<td>-387</td>
<td>7.6</td>
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<tr>
<td>29 May 2003</td>
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<td>6.5</td>
<td>-46</td>
<td>-144</td>
<td>5.7</td>
</tr>
</tbody>
</table>

model predicts the daily magnetopause distance to be less than $6.62 \; R_E$, i.e. geosynchronous magnetopause crossings (GMCs). We can find only three such days probably because (1) the days with extreme solar wind conditions in the 20th and 21st cycles have large data gaps and (2) the condition for daily average $R_{sub} < 6.62 \; R_E$ is very restrictive. The average dynamic pressure is high, larger than 14 nPa, in all events, as expected. Moreover, the IMF $B_z$ is strongly negative, which is the second reason for the decreasing of the magnetopause standoff distance. The daily dynamic pressures and $B_z$ in these events match the necessary conditions for geosynchronous magnetopause crossings in Suvorova et al. (2005).

The last two events in Table 3 are classified as CME-related in the ACE Richardson and Cane catalogue (www.srl.caltech.edu/ACE/ASC/DATA/level3/icmetable2.htm) and, moreover, are associated with the subsequent CMEs, suggesting that possibly complex and interacting CMEs are causing the closest stand-off distance. The first event in 1991 seems to be also associated with a solar flare observed on 4 June and possibly CME-related (Rank et al., 2001). The major magnetic storm of 4-5 June 1991 was studied by Garner et al. (2004). All the events have minimum $Dst$ below -100 nT, therefore may be classified as magnetic storms, and $Kp$ is 5.7 or higher.

We used 1-min averaged magnetic field data obtained from geosynchronous spacecraft GOES 8-13, and 15 to identify the GMC events with negative $B_z$. Only intervals lasting more than five minutes have been selected and several events in one day have been classified as one event. Figure 6 reproduces the minimum annual magnetopause standoff distance for the L10 model shown in Figure 2 superimposed by the histogram with the number of days in each year when GOES observed negative $B_z$ on the dayside (0600-1800 MLT). The last two events in Table 3 are also included in this statistics.

The histogram covers the interval from 1996 to 2017, but the geosynchronous magnetopause crossings were observed only around the maximum of the 23rd cycle, from 1999 to 2006, and in 24th cycle from 2011 to 2014. Most of the crossings occur in 2000, 2001, and 2003, when the model predicts drops in the minimal standoff distance. In general, the anticorrelation between red and blue lines in Figure 6 seems to be good taking into account that the blue line reflects only minimum average magnetopause distance in one day, e.g. in one event, for each year. On the other hand, the red line may miss some GMC events if there were no GOES measurements at the particular time in the dayside region or GMCs were for positive $B_z$.

### 4 Discussion and Conclusions

This work investigates variations in the average magnetopause standoff distance from 1966 to 2018 using OMNI data and empirical magnetopause models. According to most empirical models, the standoff distance depends on the solar wind dynamic pressure and IMF $B_z$ (e.g., Shue et al. (1998)), but in addition to these two parameters it may also depend on the solar wind magnetic pressure (Lin et al., 2010). Other parameters, such as the solar wind velocity (in addition to the dynamic pressure) or ionospheric...
conductivity, may control the magnetospheric compression too (Němeček et al., 2016), but their influence is not yet firmly established. The ring current may also control the magnetopause standoff distance during geomagnetically disturbed conditions, especially in the main phase of magnetic storms (Dmitriev et al., 2016). Moreover, recent studies show that the magnetosphere may significantly expand during intervals with nearly radial IMF (Dušík et al., 2010; Grygorov et al., 2017; Park et al., 2016; Suvorova et al., 2010; Suvorova & Dmitriev, 2015), however this effect has not been incorporated in empirical models so far.

We use annual average and extreme solar wind and magnetospheric parameters in this work. On such a long timescale, the average IMF $B_z$ approaches zero. The annual IMF cone angle varies in a narrow interval between 54.0° and 61.2° with the average of 57.6°. Since a quasi-radial IMF orientation usually means small cone angles, e.g. less than or equal to 30° (Dušík et al., 2010), we think that quasi-radial intervals do not influence significantly our predictions of the magnetopause standoff distance on the annual timescale. As a result, the annual standoff distance depends mainly on the solar wind dynamic pressure. However, the power law indices of this dependence differ between the empirical models. For this reason, we have compared predictions of the two models, S98 and L10. The second model predicts stronger variations with $P_{dyn}$ and possibly better corresponds to observations even for disturbed magnetospheric conditions (Samsonov et al., 2016; Suvorova & Dmitriev, 2015).

We have calculated both the annual average standoff distance and extreme distances for each year. The extreme distances have been defined as minimum and maximum daily values. Both the minimum and maximum standoff distances vary with solar cycles in such a way that not only very compressed but also expanded subsolar magnetosphere can be observed near solar maximum, rather than just near solar minimum. The annual IMF magnitude ($IMF_{B_z}$) correlate with sunspot numbers with the correlation coefficients 0.75 (0.78) and a zero time lag. The annual average solar wind dynamic pressure correlates with the sunspot numbers with a coefficient of 0.57 if taking into account a time lag between $P_{dyn}$ and SSN. We obtain a time lag of three years for the whole 53-year time interval. Considering only the three last cycles increases the correlation coefficient to 0.68 and gives a time lag of two years. The solar wind density poorly correlates with the SSN, the only statistically significant correlation occurs for a 4-year time lag and the correlation coefficient grows up to only 0.33. The solar wind velocity correlates with the SSN better than the density, and the correlation coefficient is equal to

![Figure 6. The annual minimal (blue) magnetopause standoff distance in the L10 model (the same as in Figure 2), and the number of days with negative $B_z$ at geosynchronous orbit (red).](image-url)
do not correlate with the IMF $B_1$, for a zero time lag, very poorly correlate with the IMF $|B|$, but significantly better anticorrelate with the IMF cone angle. The correlation coefficient between the cone angle and velocity (density) is equal to -0.61 (-0.51). The correlation is even higher between the cone angle and dynamic pressure. The reason of this anticorrelation is possibly differences in solar wind on a large time scale, i.e. fast and slow solar wind may correspond to slightly different average cone angles. However, a detailed study of this problem is out of scope of the paper.

The correlations between SSN and magnetospheric indices ($K_p$ and $Dst$) are also higher for the last three cycles than for the whole time interval. Varying time lags, we obtain the highest correlation coefficients between SSN and $B_s$, and between SSN and $Dst$ for a zero year time lag. The correlation coefficient between SSN and $K_p$ peaks for 1–2 year time lag. In the whole interval, $K_p$ better correlates with $P_{dyn}$ and $R_{sub}$ (with coefficients of about 0.8), while $-Dst$ better correlates with $B_s$ (0.71) than with $P_{dyn}$ (0.63) or $R_{sub}$ (-0.58). At the same time, both $K_p$ and $-Dst$ nicely correlate with the IMF magnitude with correlation coefficients above 0.8. Note that we use annual average values for these correlations and the results may differ from the correlations on shorter timescales. The correlations between solar wind parameters and magnetospheric indices were previously calculated mostly using hourly values. For example, Newell et al. (2007) obtained the correlation coefficients between $K_p$ and $B_s$ equal to -0.57, between $K_p$ and $P_{dyn}$ equal to 0.51, between $Dst$ and $P_{dyn}$ equal to -0.55 (but in their study $Dst$ was corrected by adding an additional term proportional to $P_{dyn}^{1/2}$). Lockwood et al. (2019) noted that the correlation between solar wind parameters and magnetospheric indices is higher on a longer timescale. We think that the correlations between annual solar wind and magnetospheric parameters may reveal deeper relations between them than the correlations on shorter time scale, because we eliminate any uncertainty, e.g. in the time of magnetospheric response, and also remove the seasonal effects.

The $Dst$ index is calculated as the deviation of the H component at mid-latitude stations from their quiet day values and is supposed to depend on variations of the ring current, magnetopause current, and to a lesser extent tail current (Burton et al., 1975) (see also the description of $Dst$ at http://wdc.kugi.kyoto-u.ac.jp). An increase in the ring current decreases $Dst$, while an increase in the magnetopause current increases $Dst$. Solar wind dynamic pressure pulses may increase both the magnetopause and ring currents, however these increases occur on different time scales. The magnetopause current rapidly increases after the pressure pulse has reached the subsolar point. The ring current reacts on a much longer time scale. First, the solar wind energy flux into the magnetosphere increases due to the magnetopause reconnection, the energy is accumulated in the magnetotail and then released through energetic particles accelerated by magnetotail reconnection. Besides, the particles are also accelerated by the convective electric field which penetrates into the magnetosphere due to the magnetopause reconnection. Considering only the annual average parameters, we cannot detect a $Dst$ response to short time scale variations in the magnetopause current, and mostly observe a long time scale response to the ring current. The last explains the correlation between annual $P_{dyn}$ and $-Dst$.

The average solar wind dynamic pressure exhibits increasing trend before 1991 and decreasing trend between 1991 and 2009. It increases again in the 24th cycle until 2015. The same trends have been observed in the SSN and average IMF. Respectively, the magnetopause standoff distance increases from 9.7 to 11.6 $R_E$ (according to the L10 model) from 1991 to 2009. Later, it decreases to 10.4 $R_E$ in 2015 and slightly increases again. In 2017, the standoff distance is 10.6 $R_E$ (L10 model) and 10.2 (S98 model), and in 2018 the distance in the two models increases to 10.8 and 10.4 $R_E$, correspondingly. These standoff distances are close to the average values in the whole 53-years interval which equal 10.5 $R_E$ (L10 model) and 10.2 $R_E$ (S98 model). Meanwhile, the extreme daily stand-
off distances in 2018 (in the L10 model) equal 8.1 and 12.8 $R_E$ respectively. The annual solar wind dynamic pressure decreases from 2.23 nPa in 2017 to 1.99 nPa in 2018. Note that in the three last solar minima the minimum of the dynamic pressure whether coincided with the solar minimum (between 23rd and 24th cycles) or was 2-3 years delayed (between 21st and 22nd, and between 22nd and 23rd) as shown in Figure 4. Now the solar activity is nearly at minimum, and we may expect keeping about the same low average dynamic pressure for this year.

Lockwood et al. (2009) calculated solar wind parameters during the 20th century by reconstruction from geomagnetic activity data. They found that the solar wind velocity, IMF magnitude, and the open solar flux show a long-term increase during the first half of the 20th century followed by peaks around 1955 and 1986 and then a decrease. They predicted the end of the current grand solar maximum between 2013 and 2027 depending on the parameter considered. This generally agrees with the trends discussed in this paper. Our annual average results (Figure ) also agree with Petrinec et al. (1991) who noted that the solar wind dynamic pressure was lower in 1979-1980 than during the following solar minimum between 21st and 22nd cycles. This might be related to specific features of the 21st cycle in which a decrease of the open solar flux and solar wind speed appears right at SSN maximum in 1980 (Richardson et al., 2000). Furthermore, Dmitriev et al. (2009) concluded that the dynamic pressure anticorrelates with the SSN in the four solar cycles, from 20th to 23rd. Using the annual average values in our study, we confirm the anticorrelation between $P_{dyn}$ and SSN in cycles 20–21, but get the correlation with the 2 years time lag in cycles 22-24. We note that even the annual magnetospheric indices ($Kp$ and $Dst$) as well as the IMF magnitude display no correlation with the SSN in cycle 20. We just point out this phenomenon here, but do not suggest any explanation.

Using our dataset, we have found dates when the predicted subsolar magnetopause was very close to the Earth. Because of many datagaps before 1995, we find only three daily values of $R_{sub}$ smaller than the geostationary distance 6.62 (see Table 3). In all the events, the cause of the large magnetospheric compression seems to be related to CMEs, or, even, to CME series in at least two of the three events.

We suggest another way to check that the predictions of magnetopause distance with empirical models on a long timescale are reasonably good. We have compared the number of events with negative $B_z$ at geosynchronous orbit and annual minimum magnetopause distance between 1996 and 2018. We obtain that minima in the minimum $R_{sub}$ nearly coincide with maxima on the histogram of negative $B_z$ events although the two plots illustrate different processes. The minimum $R_{sub}$ corresponds to a minimum standoff distance in one event (possibly related to a strongest CME or a combination of CME-CME/CIR-CME in this year), while the number of negative $B_z$ events may be roughly proportional to the number of most geoeffective CMEs (CME-CME or CIR-CME) in the year.

We summarize the main results below.

1. The average annual magnetopause standoff distance significantly changes during the last five solar cycles. In particular, the empirical models predict increase of the standoff distance by nearly 2 $R_E$ from 1991 to 2009 which corresponds to a threefold decrease of the solar wind dynamic pressure. This reflects a long-term decrease of the solar activity manifested also in the annual SSN, IMF magnitude, and magnetospheric $Kp$ and $Dst$ indices.

2. The annual southward IMF $B_z$ correlates with SSN with a zero time lag, while the annual dynamic pressure correlates with SSN with 2–3 year time lag. The solar wind density poorly correlates with SSN, even taking into account the time lag, however the density and velocity are well anticorrelated with the IMF cone angle. The density bet-
ter correlates with the dynamic pressure than the velocity. The annual $Kp$ better correlates with $P_{dyn}$, while $Dst$ better correlates with $Bs$. Correspondingly, we obtain 1–2 years time lag for correlation between SSN and $Kp$, and a zero time lag between SSN and $Dst$. The time lags correspond to the maximum of the correlation coefficients.

3. We find an anticorrelation between the annual solar wind dynamic pressure and SSN in cycles 20–21 and a correlation in cycles 22–24.

4. The annual IMF cone angle weakly correlates with SSN and does not correlate with the IMF magnitude. The annual cone angle varies from $54.0^\circ$ to $61.2^\circ$ with average of $57.6^\circ$.

5. We find extreme (minimal and maximal) solar wind parameters and magnetospheric indices for each year, and their variations follow the solar cycles. We suggest that the extreme solar wind parameters often result from CMEs. We show that the three events with smallest daily magnetopause distance were related to CME impacts. At least in two of the three cases two successive CMEs were observed.

The knowledge of predicted magnetopause position for the next solar cycle is important for future space missions, especially for those which are intended to observe the dayside magnetopause whether in situ or remotely. One of the forthcoming missions which will study variations of the dayside magnetopause is the Solar Wind Magnetosphere Ionosphere Link Explorer (SMILE) (Raab et al., 2016).

Acknowledgments

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