Extending depth of field for ptychography using complex-valued wavelets

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corresponding focal planes. These sharp features can be extracted and merged to reconstruct an image with an extended apparent depth of field. Considering that the in-focus features contain sharp details and thus have more high frequency information, they can be distinguished through analyzing the frequency components using wavelet or windowed Fourier transforms \cite{1, 2}. The focus stacking method has been successfully implemented in optical \cite{3}, electron \cite{4}, and full field x-ray microscopy \cite{5, 6}.

The multi-slice method \cite{7, 8} provides an alternative way to extend the depth of field by decomposing a thick sample into thin slices and modeling the multiple scattering effect slice by slice. This method extracts depth information through numerical propagation, instead of the image stack. The integration of the multi-slice method with the ptychography technique was demonstrated as an effective approach to obtain diffraction-limited resolution from specimens thicker than the depth of field \cite{9}, and is able to provide 3D images without sample rotation \cite{10}. These benefits encourage emerging efforts on adopting the multi-slice ptychography method in the x-ray regime for improving both the lateral and depth resolutions \cite{11-16} and exploiting potential advantages as a novel approach for high-resolution 3D imaging with reduced number of projections beyond the Crowther criterion \cite{17-20}.

In this letter, we present a new approach to effectively extend the depth of field by numerically generating the focus stack from single-slice ptychography reconstructions with propagated illumination wavefronts and obtaining a single sharp image using an image fusion algorithm based on the complex-valued discrete wavelet transform. This approach does not require repeated measurements of translating the sample along the axial direction as in the conventional focus stacking method, and is computationally more efficient than the multi-slice ptychography method.

1. INTRODUCTION

The depth of field of an imaging system refers to the distance range in the vicinity of the focal plane where the image maintains an acceptable sharpness. The depth of field enforces a general constraint on the allowable sample thickness for obtaining the highest achievable spatial resolution. This limitation can severely deteriorate for high-resolution three-dimensional microscopy, because the typical depth of field can be substantially smaller than the lateral field of view. The focus stacking method tackles this problem by collecting a series of images at multiple object planes, where features at various depths sequentially appear in focus at their corresponding focal planes. These sharp features can be extracted and merged to reconstruct an image with an extended apparent depth of field. Considering that the in-focus features contain sharp details and thus have more high frequency information, they can be distinguished through analyzing the frequency components using wavelet or windowed Fourier transforms \cite{1, 2}. The focus stacking method has been successfully implemented in optical \cite{3}, electron \cite{4}, and full field x-ray microscopy \cite{5, 6}.

2. NUMERICAL SECTIONING IN PTYCHOGRAPHY

Ptychography is a scanning variation of the coherent diffractive imaging method for providing high-resolution quantitative images from specimens with extended dimensions. Its capability of achieving diffraction-limited spatial resolution can be compromised by the sample thickness, which is generally required to be thinner than the depth of field of the imaging system. In this study, we present a method to extend the depth of field for ptychography by numerically generating the focus stack from reconstructions with propagated illumination wavefronts and combining the in-focus features to a single sharp image using an algorithm based on the complex-valued discrete wavelet transform. This approach does not require repeated measurements by translating the sample along the optical axis as in the conventional focus stacking method, and offers a computation-efficient alternative to obtain high-resolution images with extended depth of field, complementary to the multi-slice ptychography. © 2018 Optical Society of America

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algorithm can not distinguish the initial exit wavefront from its propagated versions. This is known as the propagation ambiguity in the phase retrieval process. For the coherent diffractive imaging method, it has been pointed out that the real-space constraints used in the iterative reconstruction process eliminates the propagation non-uniqueness and effectively determines the plane where the wavefront is reconstructed [26, 27]. Similarly, the reconstruction plane in ptychography is determined by the illumination function used in the reconstruction [28]. The features on the reconstruction plane appear sharp as in focus, while the features away from the reconstruction plane that are more than the depth of field lose sharpness, becoming out of focus. In this manner, the optical sectioning can be numerically realized by propagating the incident illumination function to target image planes and reconstructing the focus stack plane-by-plane, using the same ptychographic dataset.

The sectioning capability, i.e. the depth resolution, is limited by the depth of field in the reconstructed image defined by the signal with the maximum scattering angle collected by the detector, which is typically narrower than the depth of field defined by the focusing optics. The right panel shows a representative far-field diffraction amplitude using an x-ray beam focused by MLLs. The green and red boxes illustrate the numerical apertures determined by detection and focusing optics, respectively.

3. IMAGE FUSION USING WAVELET TRANSFORM

For detecting the in-focus features, the wavelet transform works better than Fourier transform, since it employs locally oscillating wavelets instead of globally oscillating sinusoids in Fourier transform, allowing the capture of both location and frequency information [30, 31]. The complex-valued wavelet transform works better than the real-valued counterpart, because this redundant representation relaxes the inherent constraints in the real-valued case by using individual bases for the real and imaginary components [3, 32] and provides more information as the phase of the coefficient carries detailed frequency components while the magnitude part provides the corresponding weights [33].

We use the dual-tree complex discrete wavelet transform [34, 35] for the image fusion, which uses a set of orthonormal and smooth bases and is analytically invertible [31]. The maximum-absolute-value selection rule is used to pick up the most pronounced wavelet coefficients for generating the final sharp image. The image fusion algorithm is adopted and modified from [30] and consists of the following 4 steps:

1. Align 2D slices from single-slice ptychography reconstructions with propagated wavefronts with subpixel accuracy [36].

2. Apply the complex-valued discrete wavelet transform CWT [37] on each 2D slice in the focus stack FS:

\[
\{c_j(n, m; z)\} = \text{CWT}[FS(x, y, z)],
\]

where \(c_j\) is the wavelet coefficient for level \(j\) and \(z\) denotes the \(z\)th 2D slice in the focus stack.

3. Select the coefficients \(c_j^z\) with the maximum absolute value:

\[
c_j^z(n, m) = c_j(n, m; \arg \max_z |c_j(n, m; z)|).
\]

4. Apply the inverse complex-valued discrete wavelet transform to the selected coefficients and produce the fused image \(Im\):

\[
Im = \text{CWT}^{-1}[\{c_j^z(n, m)\}].
\]

For the ultimate image quality, a few consistency checks were suggested for the coefficient selection step [30]. For instance, if more than three coefficients out of six sub-bands of the doubletree complex discrete wavelet transform, or the majority of the coefficients in an adjacent 3 x 3 neighborhood, are selected from one slice, the coefficients from remaining sub-bands or rest pixels are enforced from the same slice too.
4. EXPERIMENTAL RESULTS

The proposed method is validated using an experimental dataset collected at the Hard X-ray Nanoprobe (HXN) beamline, National Synchrotron Light Source II (NSLS-II). The sample is a 10 µm thick silicon wafer, with gold and nickel oxide nanoparticles prepared on its front and rear surfaces, respectively. The wafer was scanned across a 12 keV nano-focused x-ray beam produced by MLLs. Details of the experimental setup can be found in [38, 39]. The front surface of the sample was placed 10 µm downstream from the focal plane to provide adequate overlapping condition with a diverged beam [40–42]. The scan trajectory followed a Fermat spiral pattern [43] covering a $1.2 \times 1.2 \mu m^2$ area with 15 nm radial step size. A Merlin pixel-array detector [44] was placed 0.5 m downstream and recorded 2035 data frames for the entire 2D ptychography scan. The dataset used in this work was taken with 1 second exposure time per scan point.

A typical diffraction amplitude is shown in the right panel of Figure 1. The cropped 188 × 188 data array gives 5 nm reconstruction pixel size and ~1 µm depth of field. The wavefront of the focused beam was determined from a ptychography reconstruction using a dataset collected with only the gold particles inside the field of view.

The dataset was firstly reconstructed using multi-slice ptychography with 1000 iterations of difference map algorithm [22] using the single-slice reconstruction results as the starting guess for the object functions. The obtained phase images on the front and rear surface of the sample are shown in Figure 2 (a) and (b), respectively. The nano-particles are sharply reconstructed on their corresponding layers, and they agree very well with the Au L and Ni K fluorescence images as shown in Figure 2 (c) and (d), which were measured by a mesh scan over the same area at the same axial position with 20 nm step size and 1 second dwell time. Multiplying these two reconstructed images (i.e. summing their phases) gives a single projection image with in-focus features over 10 µm range as shown in Figure 2 (e), which significantly exceeds the estimated 1 µm depth of field.

To generate the focus stack, the x-ray wavefront at the front sample surface was propagated from -2 µm to 12 µm in 1 µm steps to match the depth of field. The front and rear sample surfaces were at $z = 0$ µm and $z = 10$ µm, respectively. The single-slice ptychography reconstructions with 1000 difference map iterations were performed 15 times, each time using one fixed probe from 15 propagated x-ray wavefronts. Figure 3 (a)-(h) display 8 of the obtained phase images with 2 µm axial increments. At $z = 0$ µm and $z = 10$ µm planes, the particles on the front and rear surfaces are sharply reconstructed, each overlaid with a blurry image of the features on the other plane. At other $z$ planes, the image quality on both surfaces is compromised to a certain extend. Using this focus stack, the final image is obtained using the algorithm described in the previous section with 3-level wavelet transforms. Figure 3 (i) shows the merged image with features on both slices sharply presented. The obtained image is consistent with the result given by the multi-slice ptychography. Since the sample only consists of 2 planes and the thickness of each plane is thinner than the depth of field, 2 single-slice reconstructions at $z = 0$ µm and $z = 10$ µm planes are sufficient to give a merged image with a very similar quality as the one obtained from 15 reconstructions.

![Fig. 2. The reconstructed phase images from multi-slice ptychography. (a) The recovered image on the front surface. (b) The recovered image on the rear surface. (c) The Au L fluorescence map for the gold nanoparticles on the front surface. (d) The Ni K fluorescence map for the nickel oxide nanoparticles on the rear surface. (e) The projection image with extended depth of field obtained by multiplying two reconstructed slices.](image)

![Fig. 3. Image fusion using complex-valued discrete wavelet transform. (a)-(h) The single-slice reconstruction images with the illumination function propagated from -2 µm to +12 µm with 2 µm step size. (i) The merged image with extended depth of field using complex-valued discrete wavelet transform.](image)
We present a new method to extend the depth of field for
with the conventional focus stacking method, and it shows the
This method simplifies the data acquisition process compared
potential to significantly improve the computation efficiency
sharp image using complex-valued discrete wavelet transform.
propagations between the last slice and the detector plane,
In our case, the entire image fusion process only took less than 1
second. For this 2-layer sample, the proposed method increases
computational efficiency by 1/3 compared with the multi-slice ptychography approach. Considering the number of slices \(N_s\) can become remarkably large for a continuous sample with extended dimension and the multi-slice ptychography approach demands at least a factor of \(N_s\) more memory, numerically generating the
focus stack with single-slice ptychography reconstructions in the
proposed method is expected to bring a more significant improvement on the computational efficiency.

The numerical sectioning capability of this method relies on
an assumption that the probe profile is not altered through the
sample thickness. Otherwise, the multi-slice approach works
better than the focus stacking method [47]. Despite the
computational burden, the axially separated slices obtained from
multi-slice ptychography enable unique capabilities such as ef-
fectively reducing the projection numbers for tomography [19]
or 3D imaging without sample rotation [10].

5. CONCLUSION

We present a new method to extend the depth of field for
ptychography by numerically generating the focus stack from
single-slice ptychography reconstructions with propagated illu-
mination functions and merging the in-focus features to a final
sharp image using complex-valued discrete wavelet transform.
This method simplifies the data acquisition process compared
with the conventional focus stacking method, and it shows the
potential to significantly improve the computation efficiency
compared with the multi-slice ptychography method. It offers a
new opportunity to remove the limitation on sample thickness and obtain high resolution images from materials with extended dimensions.

6. FUNDING INFORMATION

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