Hybrid-DFT Modeling of Lattice and Surface Vacancies in MnO

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1. INTRODUCTION

Understanding the properties and stability of material defects is key in order to maximize the impact of materials engineering. Rock salt metal oxides are ideal test systems when studying how defects alter fundamental physico-chemical behavior, with their stability also making them particularly appealing for applications that do not involve ambient conditions, such as heterogeneous catalysis. In particular, rock salt oxides formed from early group 2 alkaline earth metals (Mg, Ca) have been extensively studied, both with respect to their defect structure and properties and with the focus on potential applications in the catalytic transformation of CO2. This is perhaps unsurprising given that MnO can be prepared by thermal decomposition of MnCO3, which is considered the initial step in the transformation of CO2 into hydrocarbons. CO2 adsorption was strongest over a neutral oxygen vacancy, where the associated trapped electrons of the defect alter strongly the overall nature of the defect relative to bulk.

In this highlighted work, MnO was identified as being reactive toward CO and CO2 in an anaerobic environment to prevent the formation of higher oxidation state compounds. Observations of chemical reactivity are not without precedent for MnO: concerted e- transfers to the adsorbate and thus activate it. However, we have shown with our embedded-cluster approach that the neutral oxygen vacancy is not necessarily the dominant species, which has implications when interpreting results for future catalytic applications.
have the stability of the host material while displaying novel catalytic chemistry. An example application of this nature is CO$_2$ adsorption over the (100) surface of Mn-doped MgO, with and without neighboring anion vacancies. The results showed that the multivalent Mn caused chemical bonding between the support and the adsorbate that was not present for undoped-MgO, which complements experimental observations for mixed Fe-MnO/MgO catalysts as being reactive for the formation of light olefins from syngas.

In this work, we have performed calculations to investigate the defect energetics in the bulk and at the (100) surface of MnO, and also investigated the surface reactivity. Defects, both intrinsic and extrinsic, are key for controlling the chemical properties of catalytic materials and optimizing surface reactivity. However, one of the complexities when investigating magnetic materials like MnO is the effect of temperature on the spin configuration. At room temperature, MnO is paramagnetic (PM) and adopts a cubic structure with lattice constant (a) of 4.445 Å, but MnO has a Néel temperature (T$_N$) of 118 K below which it adopts an antiferromagnetic spin-configuration (AFM) with the d$^5$ valence electrons alternating in their spin alignment between nearest neighbor Mn$^{2+}$ cations. In the case of MnO, the lowest energy AFM arrangement is with the spin aligned in a principal diagonal plane through the crystal [AFM(II)], rather than in the lowest-index (100), (010) or (001) plane [AFM(I)]. Calculations have confirmed this energetic ordering of spin configurations, with the ferromagnetic (FM) arrangement shown as higher in energy than either AFM option.

The AFM(II) spin-configuration is associated with a rhombohedral distortion to the unit cell: the experimental lattice constant, a, is 4.43015–4.4316 Å, and the unit cell angle, α, is 90.60–90.62°. The AFM(II) spin-configuration due to

$$E_{\text{MM}} = \frac{q_i q_j}{r_{ij}}$$

between two centers with indices i and j, separated by a distance $r_{ij}$. The FF parameters are the charge ($q$, in e), the spring constant ($k_s$, in eV Å$^{-2}$), and the Buckingham potential parameters $A$ (eV), $\rho$ (Å) and $C$ (Å$^6$ eV$^{-1}$), and $k_b$ is Coloumb’s constant. Our work builds on the FF parametrization of Lewis and Catlow (Table 1), which gives an MnO lattice parameter (a) of 4.44 Å that matches experiment (4.45 Å) for the room temperature, cubic, PM MnO. However, this FF does not reproduce the low-temperature AFM(II) rhombohedral unit cell, which is required to prevent unphysical strain occurring from a structural match between the QM and MM regions at the QM/MM interface. As a remedy, a Lennard-Jones potential ($E_{\text{MM}}^{\text{L-J}}$), taking the form of:

$$E_{\text{MM}}^{\text{L-J}} = \sum_{i<j} \frac{C}{r_{ij}^6}$$

was introduced between nearest neighbor Mn$^{2+}$ cations with opposing spin by using a short-range cutoff of 5 Å to include nearest and next-nearest neighbor Mn–Mn interactions. This implementation mimics the attractive exchange interactions between antiparallel spins, with the Buckingham potential continuing to provide short-range repulsion. The $C_6$ parameter,
which has units of Å\(^6\) eV, was fitted in order to reproduce the low-temperature structure of the AFM(II) MnO phase (\(a = 4.43\) Å, \(\alpha = 90.6^\circ\)).\(^{45-47}\)

For the QM calculations, hybrid density functional theory (hybrid-DFT) was used with the B3LYP\(^{65-67}\) and B97-3\(^{68}\) exchange-correlation (XC) functionals. Results obtained with B3LYP provide a direct comparison with previous work on MgO, while B97-3 is a more advanced XC functional that has been fitted to a more extensive thermochemical data set. A Def2 triple-ζ valence plus polarization (TZVP) basis set was used for oxygen and carbon,\(^{69}\) and a Stuttgart/Dresden relativistic small-core effective core potential (ECP), with modified basis sets, was used for Mn:\(^{50}\) the most diffuse functions were removed to prevent artificial spread of electron density outside the QM region (edited basis set provided in the Supporting Information).\(^{35,55}\)

At the boundary of the QM region, it is typical to have cation-centered large-core ECPs to contain the electron density; however, no such ECPs have been derived for Mn\(^{35}\). Given the similar ionic radii of Mg\(^{2+}\) and Mn\(^{2+}\), it was decided that large-core Mg\(^{2+}\) ECPs would be placed at the QM/MM boundary, with such an approach proving successful in a previous investigation of optical transitions for cubic-structured, FM- and AFM-ordered, MnO.\(^{35,55}\)

<table>
<thead>
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<th>(q_{\text{core}})</th>
<th>(q_{\text{shell}})</th>
<th>(k_2)</th>
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<tr>
<td>Mn</td>
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<td>(3.420)</td>
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<tr>
<td>O</td>
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<td>(\rho)</td>
<td>(C)</td>
<td>(r_e)</td>
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<td>LJ</td>
<td>(C_a)</td>
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<td>Mn(<em>{\text{core}}) (-) Mn(</em>{\text{core}})</td>
<td>(52.5)</td>
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\(^{4}\) Coul., Buck., and LJ are abbreviations/acronyms for Coulomb, Buckingham and Lennard-Jones, respectively.

### 3. BULK

#### 3.1. Pristine

A bulk model of MnO was cut from the FF-optimized AFM(II) crystal structure. The QM/MM cluster was centered on the atomic species of interest: the O-centered model contains 14 Mn and 19 O atoms (Figure 1), whereas the Mn-centered model contains 14 O and 19 Mn atoms. Previous work has shown a model of this size is optimal as it preserves the electronic structure was preserved in both models, with Mulliken analysis showing an average spin density of 4.8 e on each Mn\(^{2+}\) cation when using either XC functional, in agreement with experiments;\(^{\text{71}}\) however, the geometric structure is noted as being slightly distorted. For both the B3LYP and B97-3 O-centered models of pristine MnO, the mean bond distances in the QM region stay constant at 2.21 Å but in a range of 2.16–2.24 Å, with bond lengths longer in the center of the QM region. Mean bond distances across the QM/MM boundary contracted (expanded) slightly for O\(_{\text{QM}}\)–Mn\(_{\text{MM}}\) (Mn\(_{\text{QM}}\)–O\(_{\text{MM}}\)) interactions, with averages of 2.18 and 2.24 ± 0.01 Å, respectively. Central bond angles were unaltered (\(\alpha = 90.6^\circ\)). These results were compared with geometry optimization of a range of QM/MM models with 7, 19, 27, 33, 45, 57, 63, 75, and 81 atoms in the QM region. It is noted that average bond length within the QM region and across the QM/MM boundary remains relatively constant (±0.01 Å), with the exception of the Mn\(_{\text{QM}}\)–O\(_{\text{MM}}\) interaction for which 2.24 Å is large compared to the more common observation of 2.21–2.22 Å. Interestingly, the range of bond lengths for those intersecting the QM/MM boundary (and in the MM region) remains stable, whereas within the QM region the range increases up to 2.17–2.27 Å for the 81-atom QM region, which also results in significant distortion of the bond angles. For the Mn-centered clusters, the distances between central and nearest neighbor atoms also increased, up to 2.25 Å; however, bond lengths in the QM region toward the boundary contracted significantly (2.15 Å). This contraction...
led to inversion of the bond angle in some cases, with variation between 89.0 and 90.7°. While these observations are indicative of a slight force mismatch between the QM and MM regions, the structural changes do not adversely affect energetics, as discussed subsequently in our analysis.

The energetic position of the valence band maximum (VBM) can be calculated by simulating the ionization of an electron from the bulk environment in to vacuum, as

\[ \text{MnO}^0 \rightarrow \text{MnO}^+ + e^- \]  \hspace{1cm} (5)

The energy of an electron far removed from the bulk (i.e., at the vacuum level) is 0 eV, and so the vertical ionization energy \( I_v \) is

\[ I_v = E(\text{MnO}^+ ) - E(\text{MnO}^0) \]  \hspace{1cm} (6)

As well as \( I_v \), which represents the instantaneous process of removing an electron, one can subsequently calculate the stabilization of a hole state as the adiabatic ionization \( I_a \). For both \( I_v \) and \( I_a \), the starting structure is that of optimized MnO\(^0\), the nuclear coordinates are frozen for \( I_v \) allowing only the electronic configuration (and MM shells) to optimize, making this the appropriate method to place the VBM, whereas the nuclear centers are free to move for the \( I_a \) the energy of which could be compared to emission spectra. We note that for \( E(\text{MnO}^+ ) \), and any other charged QM/MM cluster, the \textit{a posteriori} long-range dielectric correction of Jost is included in the total energy to compensate for the finite size of the polarizable region in our QM/MM model.\(^{33,72,73} \)

For the O-centered clusters, which we will focus on throughout our work, \( I_v \) and \( I_a \) are 4.79 (5.14) eV and 3.46 (3.68) eV, respectively, when using the B3LYP (B97-3) XC functional; for the Mn-centered clusters, \( I_v \) is 4.76 (5.07) eV for the same XC functionals. The similarity in \( I_v \) between our two model configurations gives us significant confidence in the ability to compare the results of our calculations. To further clarify the error bar in our approach, we also calculated \( I_v \) for the O-centered cluster when varying the size of the QM region between 7, 19, 27, 33, 45, 57, and 63 atoms. The B3LYP calculated values, which were respectively 5.43, 4.63, 4.85, 4.79, 4.76, 4.75, and 4.77 eV, vary significantly at small sizes, due to quantum confinement effects, but converge to within 0.04 eV for sizes of 33 atoms and greater. This similarity is particularly noteworthy given the structural differences of the respective QM regions, as highlighted above, when changing the QM region size. Overall, we can combine the highlighted differences to present a conservative compound error bar of ±0.1 eV on our results. While previous calculations of \( I_v \) for bulk MnO are unavailable, calculated position of the VBM at surfaces were presented in the range of 4.5–5.5 eV (discussed further in section 4).\(^{12,13} \) However, we also note that the only available experimental data, taken from photo-electrochemical measurements of PM MnO, shows \( I_v \) to be considerably greater as 7.09 eV.\(^{74} \) This discrepancy between experiment and theory could be related to the differences in magnetic and structural configuration, though neither effect results typically in such significant deviations; therefore, the difference is perhaps more likely due to experimental error and/or DFT methodological choices. Tests show that the ionization potential of gas-phase Mn atoms match experiment (7.43 eV in experiment, 7.64 eV with B3LYP), but ligand-field interactions result in splitting of degenerate levels within the bulk materials; an underestimation of \( I_v \) with DFT XC functionals has been previously observed for bulk materials and should be remembered when considering the position of both conduction band (CB) and valence band (VB) edges.\(^{55} \)

Previous literature tells us the VBM is of mixed nature in AFM(II) MnO, with PBE0 giving a 25/75% split between O 2p- and Mn 3d-states, respectively\(^{41} \) in our calculations, Mulliken analysis on both the O-centered and Mn-centered models shows that the electron is removed from the Mn valence shells when forming MnO\(^+\), hence the good agreement between the two models, and the remaining hole localizes on an Mn atom during subsequent geometry relaxation.

The discrete nature of the QM region in the QM/MM cluster, and the resulting quantum confinement, results in a poor representation of the CB and an overestimation of the band gap, \( E_g \); therefore, bulk \( E_g \) has been taken from literature to position the conduction band minimum (CBM). Experimental reports of \( E_g \) are for the room temperature, PM ordering, and range between 3.6 and 4.9 eV;\(^{76–78} \) calculated band gaps of 2.9–4.02 eV and 3.5–4.2 eV have been presented for AFM(II) MnO from hybrid-DFT\(^{40–42} \) and GW\(^{12,79,80} \) calculations. In this work, we have taken the result of \( E_g \) for the B3LYP XC functional (3.92 eV) as this exactly matches one of our XC functionals;\(^{80} \) thus, we position the CBM of AFM(II) MnO using the \( I_v \) from our O-centered clusters, obtaining −0.87 (−1.22) eV relative to the vacuum level when using the B3LYP (B97-3) XC functionals.

3.2. Intrinsic Defects. In order to illustrate the capabilities of the embedded-cluster QM/MM approach, we have calculated the defect formation energy for neutral and charged vacancies in MnO, as well as the energy levels of trapped electrons/holes at the remaining vacancies. A Kröger–Vink defect notation is used. A neutral cation vacancy may be considered as forming thus

\[ \text{Mn}^x_{\text{Mn}} \rightarrow \text{V}^x_{\text{Mn}} + \text{Mn}^0_{\text{ref}} \]  \hspace{1cm} (7)

with a formation energy of

\[ \Delta H_f^x(V^x_{\text{Mn}}) = E(V^x_{\text{Mn}}) + E(Mn^0_{\text{ref}}) - E(Mn^x_{\text{Mn}}) \]  \hspace{1cm} (8)

The energy of the reference states, \( E(Mn^0_{\text{ref}}) \), is defined as \( E(Mn_{\text{gas}}) + \mu(Mn) \), where \( E(Mn_{\text{gas}}) \) is the calculated energy of the gas-phase atom and \( \mu(Mn) \) is the chemical potential of Mn. Here, \( E(Mn_{\text{gas}}) \) was calculated as \( E(Mn_{\text{gas}}) \) minus the first and second experimental ionization energies, as successfully applied previously for embedded-cluster calculations with modified basis sets.\(^{3,5,81} \) Ideally, \( \mu(Mn) \) would also be calculated at the same level of theory as our QM/MM calculations of MnO, which in turn requires calculating \( \Delta H_f(Mn) \), i.e., the energy of bulk Mn; however, due to the weakness in hybrid-DFTs at representing delocalized states in metallic systems, we found \( \Delta H_f(Mn) \) to be underestimated by >1 eV when using hybrid-DFT (see the Supporting Information). This inability to accurately model transition metals is not isolated to our particular choices of hybrid DFT exchange-correlation functionals, but a more general problem for the field as highlighted by Janthon et al.\(^{82} \) Thus, in order to minimize the impact of these inaccurate hybrid-DFT models for bulk Mn, the experimental \( \Delta H_f \) was used for the reference states of Mn and MnO, and only \( \Delta H_f(O_2) \) was calculated to acquire \( \mu(Mn) \); from this, the respective products in high- and low partial pressures of \( O_2 \), \( p(O_2) \), are MnO\(^0\) \( \Delta H_f(MnO) \) and

\[ \Delta H_f(O_2) = \Delta H_f(MnO) - \Delta H_f(Mn) \]

For the equivalent calculation of \( O_2 \) vacancies in high- and low-\( p(O_2) \), the reference states are \( O_2 \).


\[ \Delta H_f (O_2) = -258.90 \text{ kJ mol}^{-1} \text{ using B3LYP and} -261.67 \text{ kJ mol}^{-1} \text{ using B97-3} \] and MnO (s) \[ \Delta H_f (\text{MnO}) - \Delta H_f (\text{Mn}) = -105.62 \text{ kJ mol}^{-1} \text{, respectively.} \]

If a given vacancy forms in a charged state, the energy associated with adding/removing an electron must be included. The Fermi Level (\( \epsilon_f \)) is a common source of electrons and holes in traditional semiconductors, depending on its positioning, and its inclusion in our calculations makes \( \Delta H_f \):

\[ \Delta H_f(V_{\text{Mn}}^n) = E(V_{\text{Mn}}^n) + E(\text{Mn}^{n+}) - E(\text{Mn}^{n+}) - q\epsilon_f \]

Both positive and negative values of the charge, \( q \), are feasible: in the case of \( q < 0 \), electrons are taken from the Fermi Level and thus \(-q\epsilon_f\) is positive to reflect the energy required for this abstraction; in the case of \( q > 0 \), electrons are transferred to the Fermi level; thus, there is an energy gain. For an oxygen vacancy, the enthalpy of formation is similarly:

\[ \Delta H_f = E(V_{\text{Mn}}^n) + E(\text{O}^{n+}) - E(\text{O}^{n+}) - q\epsilon_f \]

An alternative charge compensation is the formation of Schottky defect pairs, which are prevalent in wide band gap materials,\(^{\text{24}}\) whereby the charge on a cation vacancy is compensated by an opposing charge on an anion vacancy. For a pair of double-charged vacancies, this is

\[ \text{Mn}_2^+ + \text{O}_2^+ \rightarrow V_{\text{Mn}} + V_{\text{Mn}}^{**} + \text{O}_2^+ \]

with the recombination of the charged ions in eq 11 leading to the reformation of MnO(s) in eq 12. In this case, \( \Delta H_f \) for the Schottky defect is

\[ \Delta H_f(V_{\text{Mn}}^n + V_{\text{Mn}}^{**}) = \Delta H_f(V_{\text{Mn}}^n) + \Delta H_f(V_{\text{Mn}}^{**}) + \Delta H_f(\text{MnO}(s)) \]

where we calculate \( \Delta H_f(\text{MnO}(s)) \) as

\[ \Delta H_f(\text{MnO}(s)) = E(\text{MnO}(s)) + \Delta H_f(\text{Mn}) + \Delta H_f(\text{Mn}^{+}) + \Delta H_f(\text{Mn}^{+}) + \frac{1}{2} \Delta H_f(\text{Mn}^{+}) + \frac{1}{2} \Delta H_f(\text{Mn}^{+}) \]

B3LYP-calculated defect formation energies are presented in Figure 2 for the atomic vacancies. For O vacancies, calculated with the O-centered model, \( V_{\text{O}}^{**} \) is the most stable at low \( \epsilon_f \) with the neutral \( V_{\text{O}}^0 \) defect preferred as \( \epsilon_f \) tends toward \( \epsilon_f^{\text{CBM}} \). However, the \( V_{\text{O}} \) defects are only more favorable than \( \text{Mn}_2^+ \) under high-\( p(O_2) \) when \( \epsilon_f \) is in the lower half of the band gap. The neutral and negatively charged \( V_{\text{O}} \) defects show little disruption of the perfect bulk structure, with minimal atomic displacements. Mulliken analysis shows the two electrons (\( e^- \)) freed when forming the \( V_{\text{O}} \) defect would be trapped in the vacancy, forming an F-center, with an F'-center also stable when one of the defect electrons has been removed i.e. a \( V_{\text{O}}^{**} \) defect. Unsurprisingly, negatively charged \( V_{\text{O}} \) defects are unstable at all values of \( \epsilon_f \).

For Mn vacancies, calculated with the Mn-centered model, \( \Delta H_f \) decreases with \( q \) when \( \epsilon_f = \epsilon_f^{\text{CBM}} \) and increases with \( q \) when \( \epsilon_f = \epsilon_f^{\text{VBM}} \): this shows that the defects would donate electrons when \( \epsilon_f \) is low (large energy gain) and accept electrons when \( \epsilon_f \) is high (small energy cost). For the B3LYP XC functional, we calculate that \( \Delta H_f \) (\( \text{Mn}_2^+ \)) is exothermic when \( \epsilon_f \) is \( \epsilon_f^{\text{CBM}} \) at both low- and high-\( p(O_2) \); we note that n-type conditions of \( \epsilon_f \) would require an excess of electrons generated from e.g. oxygen vacancies. In previous literature, n-type conditions have more commonly been considered: Aschauer et al. presented results from periodic PBEsol+U calculations with \( \epsilon_f \) positioned 2.8 eV above the VBM, i.e. toward the CBM, and found that \( \Delta H_f(\text{V}_{\text{Mn}}^{**}) \) was 1.5 eV lower than \( \Delta H_f(\text{V}_{\text{Mn}}^0) \), which in turn was 1.7 eV more preferable than \( \Delta H_f(\text{V}_{\text{Mn}}^{**}) \); they also reported \( \Delta H_f(\text{V}_{\text{Mn}}^{**}) \) as 4.5 eV higher in energy than \( \Delta H_f(\text{V}_{\text{Mn}}^{**}) \). These observations are in agreement with our results, with the same \( \epsilon_f \) positioning giving respective differences between \( \Delta H_f(\text{V}_{\text{Mn}}^{**}) \), \( \Delta H_f(\text{V}_{\text{Mn}}^0) \), and \( \Delta H_f(\text{V}_{\text{Mn}}^{**}) \) of 1.27 and 1.13 eV (Figure S1, Supporting Information), and between \( \Delta H_f(\text{V}_{\text{Mn}}^0) \) and \( \Delta H_f(\text{V}_{\text{Mn}}^{**}) \) of 4.26 (7.45) eV for high (low)-\( p(O_2) \). Previous experimental work focuses on the dominant Mn vacancy at varying high temperatures (> 1000 K), the modeling of which is beyond the scope of this work, but generally notes the prevalence of \( \text{V}_{\text{Mn}}^{**} \).

As the VBM is lower at \(-5.14 \text{ eV for B97-3, we observe that both} \Delta H_f(\text{V}_{\text{Mn}}^{**}) \) and \( \Delta H_f(\text{V}_{\text{Mn}}^{**}) \) are exothermic for \( \epsilon_f = \epsilon_f^{\text{CBM}} \) and \( \epsilon_f^{\text{VBM}} \), respectively, under low-\( p(O_2) \) conditions. At both high and low values of \( \epsilon_f \), the transition from endothermic to exothermic for \( \Delta H_f \) indicates the limit for \( \epsilon_f \) in this material as,
in the exothermic regime, the material properties would change due to the propensity for defect formation. Thermodynamic stability regimes for the singly charged VMn and V\textsuperscript{\textast}}\textsubscript{Mn} defects are not observed for either B3LYP or B97-3.

Structurally, VMn\textsuperscript{\textast}} formation results in expansion around the vacant site, with contraction of Mn−O bonds between neighboring atoms to compensate for the lost coordination. For the B3LYP optimized model, Mn−O bonds around the VMn defect are 2.12−2.14 Å, in agreement with Aschauer et al., who report bond lengths of 2.11 Å\textsuperscript{42}\textsuperscript{45}\textsuperscript{47} while we observe shorter bonds of ∼2.01 Å for bonds between O atoms neighboring the defect and Mn atoms at the edge of the QM region. As the charge of QM region is reduced (i.e., electrons are removed), much shorter Mn−O bonds are observed: for VMn\textsuperscript{\textast}, there is a shorter bond of 1.98 Å; for VMn\textsuperscript{\textast\ast}, two bonds of 1.81 and 1.88 Å are observed; for VMn\textsuperscript{\textast\ast\ast}, there is an additional bond of 1.98 Å; and for VMn\textsuperscript{\textast\ast\ast\ast}, four bonds of between 1.81 and 1.88 Å are calculated. These shorter bonds are all indicative of Mn−O bond lengths after the oxidation of Mn\textsuperscript{\textast}\textsuperscript{2} to Mn\textsuperscript{\textast\ast}\textsuperscript{3}\textsuperscript{42}\textsuperscript{45}\textsuperscript{47} with Aschauer et al. reporting distances of 1.92 Å for the PBESol+U approach. For B97-3, similar structural observations are made, except that for VMn and VMn\textsuperscript{\textast}} the short bonds are all below 1.86 Å; however, this geometric difference does not appear to influence the defect energetics as neither of the singly charged defects are stable with either XC functional. Mulliken spin analysis shows that the holes (h\textsuperscript{\textast}) created by removing a lattice Mn cation localize on nearest neighbor Mn sites, forming Mn\textsuperscript{\textast\ast\ast}\textsuperscript{3} cations (Mn\textsuperscript{\textast\ast\ast\ast}Mn\textsuperscript{\textast\ast\ast\ast}), which is consistent for VMn through to VMn\textsuperscript{\textast\ast\ast\ast}Mn\textsuperscript{\textast\ast\ast\ast}. Additionally, via a comparison of states of different multiplicity and Mulliken spin analysis, we observe that the singly charged defects of VMn\textsuperscript{\textast} and VMn\textsuperscript{\textast\ast} are >1.5 eV more stable when the defect electron aligns with the d\textsuperscript{3} valence electrons of the removed Mn atom, i.e. in agreement with the AFM(II) configuration.

In general, MnO is characterized by experiment as a p-type material (i.e., rich in h\textsuperscript{\textast} charge carriers) due to Mn vacancies caused by an excess of oxygen, with investigations having been performed exclusively at room temperature or higher; thus considering cubic, paramagnetic MnO\textsuperscript{35}\textsuperscript{38}\textsuperscript{39}. O’Keeffe et al. stated that the majority defects in their samples were VMn\textsuperscript{\textast\ast\ast}, with charge compensation via two Mn\textsuperscript{\textast\ast\ast\ast} centers and 1/2O\textsubscript{2}(g)\textsuperscript{35} in our calculations, Mulliken analysis shows that multiple Mn\textsuperscript{\textast\ast\ast\ast}Mn\textsuperscript{\textast\ast\ast\ast} defects are the preferred stabilizer for all VMn defects, but the formation enthalpies imply that VMn\textsuperscript{\textast\ast\ast\ast}Mn\textsuperscript{\textast\ast\ast\ast} would only form with ε\textsubscript{f} positioned midgap or higher (Figure 2). Our results for low-p(O\textsubscript{2}) agree with expectation of VMn\textsuperscript{\textast\ast\ast\ast} being most stable; for high-p(O\textsubscript{2}), our calculations show competition between the VMn\textsuperscript{\textast\ast\ast\ast} and VMn\textsuperscript{\textast\ast\ast\ast\ast} defects at low ε\textsubscript{f}, which would be shifted to further favor VMn\textsuperscript{\textast\ast\ast\ast} if we were to consider an MnO\textsubscript{2} (s) reference state, which is most likely at high-p(O\textsubscript{2}): µ(Mn) = −2.2 kJ mol\textsuperscript{−1} i.e. the ΔH\textsubscript{f} (VMn\textsuperscript{\textast\ast\ast\ast}) line would be shifted further upward\textsuperscript{37}\textsuperscript{38}. A possible source of this difference is the temperature and phase of the MnO in our work, although we also suggest that a lack of long-distance exchange coupling may have affected the VMn\textsuperscript{\textast\ast\ast\ast} calculations, which could possibly be rectified by consideration of a larger QM region. Overall, the presence of a stability window for ε\textsubscript{f} charge carries is in agreement with (high temperature) Hall measurements that show the existence of ε\textsubscript{f} charge carriers with higher mobility than h\textsuperscript{\textast} at low-p(O\textsubscript{2})\textsuperscript{38}\textsuperscript{90}\textsuperscript{92}.

We present ΔH\textsubscript{f} for vacancy defects in Table 2, compared with ε\textsubscript{f}-compensated defects in their most favored conditions, i.e. elemental products, when ε\textsubscript{f} is equal to the midgap branch point. As shown in eq 13, Schottky defects are mutually cooperative as holes and electrons recombine. Our results show that a Schottky defect with Mn\textsuperscript{2+}/O\textsuperscript{2−} pairings are energetically most favorable. By summing ΔH\textsubscript{f} for the charge-carrier-compensated vacancies and comparing to the formation energy of Schottky defects, we also see that, when ε\textsubscript{f} is positioned midgap or higher (i.e., n-type), this Schottky defect is more favorable than all possible combinations of charge-carrier-compensated defects; however, in general the individual ε\textsubscript{f}-compensated defects remain energetically more preferable. Experimentally, Schottky defects were considered previously by Crevecoeur and de Wit in order to explain conductivity measurements\textsuperscript{11} however, further work by Pai and Honig concluded that a two-carrier model in MnO is very unlikely.\textsuperscript{92} As an additional note, we see in Table 2 that the most stable VMn\textsuperscript{\textast\ast\ast\ast} defects differ between the B3LYP and B97-3 XC functionals at the midgap point. This difference occurs because of the larger I\textsubscript{c} when using B97-3 (5.14 eV) compared to B3LYP (4.79 eV), which in turn lowers the energy of the midgap point and favors the loss of ε\textsubscript{f} charge carriers more when using B97-3 than with B3LYP.

The energy levels of electrons trapped at defect sites are presented in Figure 3. Here, the ΔSCF method (analogous to

<table>
<thead>
<tr>
<th>defect reactions</th>
<th>ΔH\textsubscript{f} (eV)</th>
</tr>
</thead>
<tbody>
<tr>
<td>oxygen vacancy, low-p(O\textsubscript{2})</td>
<td>12.84 (13.63)</td>
</tr>
<tr>
<td>oxygen vacancy, high-p(O\textsubscript{2})</td>
<td>11.25 (12.04)</td>
</tr>
<tr>
<td>manganese vacancy, low-p(O\textsubscript{2})</td>
<td>3.81 (3.31)</td>
</tr>
<tr>
<td>manganese vacancy, high-p(O\textsubscript{2})</td>
<td>3.54 (4.35)</td>
</tr>
</tbody>
</table>

From Table 2, it is clear that oxygen vacancies are the most stable defects, followed by manganese vacancies. The energy levels of electrons trapped at defect sites are shown in Figure 3. The ΔSCF method (analogous to...
with values of \(I_v\) and PBE+U give outward O displacement by 1.3\% while PBE was prepared at the MM level, using the AFM(II).

The equivalent charged systems in Figure 2; defect levels marked with blue and red arrows, respectively, with the color scheme matched to the Vacancies, the sites with two and one associated electrons (VMn)

supporting information, in agreement with our observations similar results are observed for the B97-3, as shown in the consolidation our observation that these defects are unstable; such results are not observed for VO, where VO

are higher than defects with an extra electron, further from Table 2. Such results are not observed for VO, where VO

experiment: MEIS and LEED indicate that the distance between surface and subsurface layers increases, by 0.1–1.1\%, whereas DFT gives interlayer contraction by 0.3–1.6\%. Our calculated displacements match previous computations well, and we note that the error bars on experiment are large compared to the values being considered.

AQM/MM model was constructed from our MM surface, centered on a surface oxygen atom; structural optimization resulted in atom displacements of only 0.01 Å (0.5\%) compared to the MM model. The surface ionization potential was then calculated using eq 6, with both high- and low-spin configurations considered for the MnO\(^{+}\) surface: a high-spin configuration corresponds to ionization from the O 2p-orbitals, whereas the low-spin configuration corresponds to removing an electron from the Mn 3d-orbitals. Our calculations show that the highest occupied states (VBM) belong to the Mn 3d-orbitals, for which \(I_v\) is 4.77 (5.09) eV and \(I_a\) is 3.32 (3.52) eV when using the B3LYP (B97-3) XC functional, whereas the O 2p-states are marginally lower in energy with \(I_v\) = 4.95 (5.29) eV, for the same XC functionals. We note that our results for \(I_v\) and \(I_a\) are similar to bulk: for the favorable low spin ionization of the surface, \(I_v\) differs by <0.1 eV and \(I_a\) by <0.2 eV. Mulliken analysis shows that this similarity is because surface ionization removes an electron from a subsurface, rather than surface, Mn cation. Further calculations using constrained DFT, whereby the ionized electron is removed specifically from a surface atom, result in \(I_v\) = 5.06 and 5.43 eV for B3LYP and B97-3 XC functionals, respectively, which indicates the surface valence-band bending downward.

Motivated by these results, we also calculated second and third ionization energies for the MnO surface. It was noted that the lowest energy configurations for the vertical ionization of a second electron is with two Mn\(^{3+}\) cations positioned subsurface, forming a [Mn\(^{3+}\)]\(_2\) complex, which is more stable than a Mn\(^{4+}\) positioned subsurface or on the surface; the respective energetic ordering is 5.65 (5.97) < 6.27 (6.72) < 6.45 (6.91) eV when using the B3LYP (B97-3) XC functional. The [Mn\(^{3+}\)]\(_2\) configuration was also more favorable for \(I_a\). Analogous to eq 9, we then looked at formation energies of the ionized surface defects, finding that Mn\(^{3+}\) through to Mn\(^{4+}\), and combinations therein, would be exothermic as \(\epsilon_f\) approaches the VBM; isolated occurrences of Mn\(^{3+}\) are most favorable when considered per hole created: \(-1.46 (-1.57), -1.20 (-1.32)\) and \(-0.97 (-1.22)\) eV for single, double and triple Mn\(^{3+}\) defect coupling, when using the B3LYP (B97-3) XC functional. Again, we note that negative \(\Delta H\) values indicate a physically unstable \(\epsilon_p\) as the material would spontaneously lose electrons; however, we emphasize the trend in stability of different defects. Compensating Mn vacancies were also considered, but found to be higher in energy than compensation via \(\epsilon_p\).

Our positioning of the VBM at the (100) surface is in good agreement with previous computations by Toroker et al. using hybrid-DFT methods, where a periodic slab model was used with a vacuum region and the electrostatic potential in the vacuum gap taken as the reference vacuum level. With this model, they obtained \(\epsilon_{\text{VBM}}\) of \(-4.48, -4.96, -5.28\), and \(-5.57\) eV for the PBE+U, HSE, PBE0, and G0W0 (DFT+U) methods. Stevanovic et al. used a similar technique to obtain \(I_v\) = 5.08 eV. However, neither our nor other authors’ results match with the experimental estimates of \(-7.5 \pm 0.8\) eV, taken from photoelectron spectroscopy (PES) measurements by Fujimori et al., though these relate to the room temperature.
PM phase. A position of the VB can also be implied from the 

\[ \Delta H_f (V_{0\text{ff}}^\text{ff}) = 2.81 \pm 0.2 \text{ eV} \]

for the B3LYP (B97-3) XC functional, differing by 

only 0.02 eV. This difference relative to bulk increases \(-0.2 \text{ eV} \)

for \( V_{0\text{ff}}^\text{ff} \) with \( \Delta H_f (V_{0\text{ff}}^\text{ff}) = 2.81 (2.37) \text{ eV} \) at the surface when considering \( \epsilon_f = \epsilon_{\text{VRBM}} \) for \( V_{0\text{ff}}^\text{ff} \), \( \Delta H_f (V_{0\text{ff}}^\text{ff}) \) is then almost identical for the surface and bulk, at 0.63 \((-0.04) \text{ eV} \) for the B3LYP (B97-3) XC functional. Analysis of the defect levels shows that, like the bulk, the favored spin configuration when ionizing to the \( V_{0\text{ff}}^\text{ff} \) states is low-spin (LS): \( I_f^\text{LS} (V_{0\text{ff}}^\text{ff}) = 2.84 \text{ eV} \) compared to \( I_f^\text{HS} (V_{0\text{ff}}^\text{ff}) = 3.13 \text{ eV} \) for high-spin (HS) configurations, using the B3LYP XC functional. Also similar to the bulk, the structural integrity of the void is preserved, with neighboring bond distances remaining close to the bulk values. However, removing a second electron from the oxygen vacancy is more difficult: \( I_f (V_{0\text{ff}}^\text{ff}) \) and \( I_f (V_{0\text{ff}}^\text{ff}) \) are 4.06 (4.22) and 2.60 (2.73) eV, respectively, with the B3LYP (B97-3) XC functional, which is \(-0.6 \text{ eV} \) larger than for the bulk. The structure of the defect remains relatively unchanged.

4.2. Intrinsic Defects. The formation energies of neutral and positively charged oxygen surface vacancies are presented in Figure 4. \( \Delta H_f (V_{0\text{ff}}^\text{ff}) \) is almost identical to the bulk at 5.88 eV compared to 6.06 eV for the B3LYP (B97-3) XC functional, differing by only 0.02 eV. This difference relative to bulk increases \(-0.2 \text{ eV} \)

for \( V_{0\text{ff}}^\text{ff} \) with \( \Delta H_f (V_{0\text{ff}}^\text{ff}) = 2.81 (2.37) \text{ eV} \) at the surface when considering \( \epsilon_f = \epsilon_{\text{VRBM}} \) for \( V_{0\text{ff}}^\text{ff} \), \( \Delta H_f (V_{0\text{ff}}^\text{ff}) \) is then almost identical for the surface and bulk, at 0.63 \((-0.04) \text{ eV} \) for the B3LYP (B97-3) XC functional. Analysis of the defect levels shows that, like the bulk, the favored spin configuration when ionizing to the \( V_{0\text{ff}}^\text{ff} \) states is low-spin (LS): \( I_f^\text{LS} (V_{0\text{ff}}^\text{ff}) = 2.84 \text{ eV} \) compared to \( I_f^\text{HS} (V_{0\text{ff}}^\text{ff}) = 3.13 \text{ eV} \) for high-spin (HS) configurations, using the B3LYP XC functional. Also similar to the bulk, the structural integrity of the void is preserved, with neighboring bond distances remaining close to the bulk values. However, removing a second electron from the oxygen vacancy is more difficult: \( I_f (V_{0\text{ff}}^\text{ff}) \) and \( I_f (V_{0\text{ff}}^\text{ff}) \) are 4.06 (4.22) and 2.60 (2.73) eV, respectively, with the B3LYP (B97-3) XC functional, which is \(-0.6 \text{ eV} \) larger than for the bulk. The structure of the defect remains relatively unchanged.

4.3. \( \text{CO}_2 \) Adsorption. Rock salt oxides have recently been proposed as candidate materials for the catalytic transformation of \( \text{CO}_2 \), and here we investigate the initial step of that reaction: \( \text{CO}_2 \) surface adsorption. Previously, it has been shown that surface defects on MgO, specifically oxygen vacancies, can affect \( \text{CO}_2 \) adsorbate binding,\(^6\) both structurally and energetically, which is further amplified by the presence of extrinsic cation dopants like \( \text{Mn}_{\text{Mg}} \).\(^8\) A favorable initial step involves charge transfer from the support to the \( \text{CO}_2 \), which results in bending of the linear \( \text{CO}_2 \), and this can be aided by high-energy defect levels associated with oxygen vacancies.

There are two possible orientations for a \( \text{CO}_2 \) molecule on the (100) surface: parallel or perpendicular to the surface xy-plane.\(^5\) Downing et al. showed that, for pure MgO, parallel adsorption is stronger over the pristine surface, whereas perpendicular orientation is more favorable in the presence of \( V_{0\text{ff}} \). In the case of MnO, parallel adsorption is again stronger over the pristine surface than perpendicular, with the C atom interacting with a surface oxygen (Figure 5) with an adsorption energy of \(-0.64 \text{ eV} \) (Table 3). This result is very similar to previous work on MgO \((-0.68 \text{ eV} \)\) and Mn-doped MgO \((-0.66 \text{ to } -0.79 \text{ eV} \)\).\(^3,5\) For \( V_{0\text{ff}} \), the energetics of \( \text{CO}_2 \) adsorption in parallel or perpendicular configurations are similar (2.60 eV), with structural analysis showing that, in both cases, the \( \text{CO}_2 \) adopts a bent structure coordinated with both the defect and the surface atoms (Figure 5). In particular, one oxygen from the \( \text{CO}_2 \) fills the void while the second oxygen coordinates with a surface Mn, resulting in \( z(\text{OOC}) \) of 115.5°. This angular distortion prevents the adsorption energy from being as strong as for \( \text{CO}_2 \) \( z \)-aligned over MgO.\(^5\)

As we remove an electron from \( V_{0\text{ff}} \) to form \( V_{0\text{ff}}^\text{ff} \), the interaction between \( \text{CO}_2 \) and MnO weakens yet the adsorbate is still strongly coordinated with the surface, and the internal angle of \( z(\text{OOC}) \) is 119.7°. The maintenance of an adsorbed structure, yet weakening of the adsorption energy, shows how
important it is for electron transfer to occur from the support to the adsorbate. This factor is further exemplified for \( \text{V}_{\text{O}} \) defects, where the CO\(_2\) only interacts weakly with the support, at a separation distance of 3.5 Å. Thus, we can conclude that defect electrons positioned high in the band gap, as made available through the existence of oxygen vacancies, are important for catalytic CO\(_2\) activation, in contrast with, e.g., MgO.\(^{55}\) Furthermore, one can consider these observations are also indicative of preferential conditions for the reverse reaction of CO oxidation over MnO, where weaker CO\(_2\) binding is preferential for the product to leave the support surface;\(^{108}\) in this case, formation of \( \text{V}_{\text{O}}^{**} \) would be most beneficial.

### 5. SUMMARY AND CONCLUSIONS

We have used embedded cluster QM/MM calculations to investigate the electronic and energetic stability of MnO in pristine and defective bulk and in similar arrangements for (100) surfaces. We have modeled the system using low-energy principal diagonal antiferromagnetic ordering and the appropriate rhombohedrally distorted unit cell throughout.

For the bulk system, our calculations have shown that the valence band maximum and conduction band minimum are positioned at \(-4.79\) eV and \(-0.87\) eV relative to the vacuum level, with the valence band maximum formed of Mn 3d-states. We then use our model to calculate the preferential defect formation to be ionized vacancies, with a 2\(^+\) charge, when atomic defects are introduced with electron removal to the Fermi Level, \(\epsilon_{\rho}\) at the valence band maximum; at the conduction band minimum, double-charged Mn vacancies are far more stable than other defects, being exothermic to form in most cases. Schottky defects, whereby charged defects compensate each other to maintain charge neutrality at the macroscopic level, are most preferable for a combination of \( \text{V}_{\text{O}}^{**} \) and \( \text{V}_{\text{Mn}}^- \) defects: the formation energy is \(2.40\) eV when using the B3LYP XC functional. The defect levels for charged vacancies were also investigated, with the \( \text{V}_{\text{O}}^- \) and \( \text{V}_{\text{O}}^{**} \) defects positioned mid band gap, similar to MgO; the \( \text{V}_{\text{Mn}}^- \) and \( \text{V}_{\text{Mn}}^{**} \) defects are marginally lower in energy.

For the (100) surface, the structure proves similar to previous calculations, with interlayer contraction and slight oxygen protrusion from the surface. Again, we pursued calculations for the formation of oxygen vacancies, with results almost identical to the bulk, which highlights the relative stability of the surface; most defect levels were also similar to those in the bulk, with a notable exception being the \( \text{V}_{\text{O}} \) state, which was \(\sim0.6\) eV lower for the surface. Finally, we presented testing of the chemical properties of the pristine and defective (100) surface for applications in CO\(_2\) transformation. We show that the presence of defect-levels at surface vacancies on an MnO catalyst are crucial for activating the CO\(_2\), with charge transfer resulting in strong adsorption and structural distortion. We are currently expanding this investigation to include MnO\(_x\) materials, where the higher oxidation state of the cation may influence the electronic and energetic properties.

### ASSOCIATED CONTENT

#### Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.jpcc.8b07846.

Edited basis set for an Mn atom, as used in our calculations, documentation of periodic calculations for the formation enthalpies of MnO, figures illustrating defect formation enthalpies, and a pictorial representation of the defect levels for neutral and charged defects in MnO when using the B97-3 exchange-correlation functional (PDF)

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**Notes**

The authors declare no competing financial interest.

The raw data from which all energetic results were derived is available to access at DOI: 10.17035/d.2018.0052063074.

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