Star–galaxy classification in the Dark Energy Survey Y1 data set


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ABSTRACT

We perform a comparison of different approaches to star–galaxy classification using the broad-band photometric data from Year 1 of the Dark Energy Survey. This is done by performing a wide range of tests with and without external ‘truth’ information, which can be ported to other similar data sets. We make a broad evaluation of the performance of the classifiers in two science cases with DES data that are most affected by this systematic effect: large-scale structure and Milky Way studies. In general, even though the default morphological classifiers used for DES Y1 cosmology studies are sufficient to maintain a low level of systematic contamination from stellar misclassification, contamination can be reduced to the O(1 per cent) level by using multi-epoch and infrared information from external data sets. For Milky Way studies, the stellar sample can be augmented by ∼20 per cent for a given flux limit. Reference catalogues used in this work are available at http://des.ncsa.illinois.edu/releases/y1a1.

Key words: Methods: data analysis – Methods: statistical – Techniques: photometric.

1 INTRODUCTION

Accurate classification of astrophysical sources is essential for interpreting photometric surveys. Specifically, separating foreground stars from background galaxies is important for many astronomical research topics, from Galactic science to cosmology. Conventional morphological classification techniques separate point sources (mostly stars) from resolved sources (galaxies) using selections in magnitude–radius space or similar variables (MacGillivray et al. 1976; Kron 1980; Heydon-Dumbleton, Collins & MacGillivray 1989; Yee 1991). For bright sources, morphology has proven to be a sufficient metric for classification. In this regime, for weak-lensing applications, a very pure, but also abundant, star sample...
is vital for deriving the correct point spread function (PSF) in the images, which is used to later infer cosmic shear (Soumagnac et al. 2015; Jarvis et al. 2016; Zuntz et al. 2017). At fainter magnitudes, unresolved galaxies will begin to contaminate catalogues of point-like sources and noisy measurements of stars will contaminate the galaxy sample. Blended sources become an issue as well because distant and/or faint sources start to merge into single detected objects with spurious shapes. Misclassification of stars and galaxies at faint magnitudes can introduce spurious features in galaxy survey (Crocce et al. 2011) and will hamper the study of galaxy distributions (Drlica-Wagner et al. 2015).

The advent of CCD detectors provided larger, more reliable data sets that became an obvious target for machine learning (ML) classification algorithms (e.g. Odewahn et al. 1992; Bertin & Arnouts 1996; Sevilla-Noarbe & Elayo-Sotos 2015; Machado et al. 2016; Kim & Brunner 2017). In addition, many large, multiband imaging surveys use morphology, such as for Sloan Digital Sky Survey (SDSS; Stoughton et al. 2002) and/or have incorporated colour information into their classifiers (see Ball et al. 2006 for SDSS as well, Hildebrand et al. 2012 for CFHTLS or Saglia et al. 2012 for Pan-STARRS). Adopting a Bayesian approach to incorporate fits to stellar and galaxy templates has been shown to be a promising avenue (Fadely, Hogg & Willman 2012) as well as the use of infrared data to complement the optical band observations (Malek et al. 2013; Banerji et al. 2015; Kovács & Szapudi 2015).

In this paper, we test different strategies for classifying objects as point-like or extended sources in the Dark Energy Survey (DES) Year 1 data (Y1). We subsequently analyse the impact in two broad science cases and possible developments to improve object classification in future analyses of these data. Throughout this paper, ‘extended’ will be used as a synonym for ‘galaxy’, whereas ‘point-like’ includes both stars and quasi-stellar objects (QSOs) on first approximation, and we will collectively call them ‘stars’ in this work. For the case studies considered here and the general catalogue, the contamination of QSOs in the large-scale stellar and galactic catalogue is not deemed important. However, a good star–QSO separation is needed for quasar science, as studied in detail in Tie et al. (2017) for DES data.

After a description of the data set in Section 2 and the classifiers we are considering here in Section 3, we compare the classifiers in calibration fields (Section 4) and then analyse the response in the complete Y1 data set for a few selected ones (Section 5). Then, we study the impact on large-scale structure (LSS) and Milky Way studies (Section 6). Finally, Section 7 presents the conclusions and discusses possible additional developments.

2 DARK ENERGY SURVEY DATA SETS

The DES consists of a 5000 deg$^2$ ‘wide’ survey using the grizY photometric bands to AB 10′′ magnitude limits of (24.6, 24.4, 23.7, 22.7, 21.5), respectively, for 2 arcsec apertures, together with a ~27 deg$^2$ supernovae (SNe) survey observed in the griz bands with an approximately weekly cadence. In 2018 February, the project completed the original five planned observing seasons (Years 1 through 5, Y1−Y5). Additional science-quality data were collected during an earlier Science Verification (SV) season. The core goal of DES is a multiprobe study of dark energy at different cosmological epochs using the same DECam instrument (Flaugher et al. 2015) and DES Data Management (DESDM) pipeline (Morganson et al. 2018), as showcased with its first results in DES Collaboration (2017). However, the richness of this data set allows astronomers and cosmologists to go beyond this initial objective (DES Collaboration 2016).

For this study, we use the subset of highest quality data from DES SV$^1$ and Y1$^1$ (Drlica-Wagner et al. 2018) comprising the ‘Gold’ catalogue. We note the following features that are relevant for this study:

(i) The object catalogues are obtained applying SExtractor (Bertin & Arnouts 1996) to coadded images with typically two to four overlapping exposures in each band in the case of Y1 or ~10 for SV data, with object detection performed on a combined riz image.

(ii) SExtractor magnitudes have been calibrated through a global calibration module (Tucker et al. 2007) and subsequently adjusted through a fit to the stellar locus (High et al. 2009) anchored to the i band.$^3$ This procedure also corrects for Galactic extinction. In general, $\text{MAG\_AUTO}$ is used for photometry (for binning purposes and as inputs for the template-based method described next), as it behaves more robustly for these coadded catalogues. $\text{MAG\_MODEL}$, $\text{MAG\_DETMODEL}$ and $\text{MAG\_PSF}$ are used as inputs for the ML methods as well. Shape measurements in this code include $\text{FLUX\_RADIUS}$, $\text{CLASS\_STAR}$ and $\text{SPREAD\_MODEL}$, some of which will be specifically studied here.

(iii) In addition, a multi-object, multi-epoch fitting pipeline (MOF) has been run on the single-epoch image counterparts for each coadd catalogue detection to obtain more precise photometric measurements for the objects. It simultaneously fits a Gaussian mixture model to the individual images, also modelling light from nearby neighbours for each object (more details in Drlica-Wagner et al. 2018). The main flux measurements used for the methods described here are the fluxes using this composite Gaussian mixture model ($\text{CM\_MAG}$) and the PSF magnitudes derived from the same MOF pipeline ($\text{PSF\_MAG}$). $\text{CM\_T}$ is a size estimator from the code before PSF convolution, which will be studied here in detail.

(iv) All objects are required to be in areas for which there is at least one exposure in each of the griz bands.

We define two distinct regions in which we will perform our tests:

(i) A calibration field: defined by those areas that overlap external data sets that we can use to train, validate, and test our methods. These are the SN fields from the DES SN survey, which overlap specific spectroscopic surveys and miscellaneous Hubble Space Telescope (HST) data sets; and the area of the survey overlapping the SDSS (York et al. 2000) Stripe 82 region (Frieman et al. 2008). In addition, the COSMOS field$^4$ has been imaged with DECam, providing a very useful data set given the richness of multiband imaging and spectroscopy available. Table 1 summarizes the numbers of objects matched to various external data sets (details in Section 4.3). Some of these fields have a large number of DES exposures, due to their application for SN searches, so special coadds were made from ~4 exposures in each band in order to resemble the Y1 depth. The selection of these exposures was made so that their coaddition would provide similar characteristics in terms of

1https://des.ncsa.illinois.edu/releases/sva1
2https://des.ncsa.illinois.edu/releases/y1a1
3This calibration approach was eventually superseded in Y3 data products with the Forward Global Photometric Calibration approach described in Burke et al. (2018).
4In this case, the exponential model used in SExtractor is fitted on the detection image and scaled in the measurement images of each band.

http://cosmos.astro.caltech.edu/
sky brightness and seeing as the wide survey coadds (Neilsen et al. 2016; Drlica-Wagner et al. 2018). This procedure is not needed in forthcoming releases as the wide survey extends to cover the SN regions.

(ii) An application field: the remaining area of the DES footprint for which suitable external data sets for training are not presently available. This includes the so-called ‘SPT’ region due to the overlap with the South Pole Telescope6 (Ruhl et al. 2004) observations, in which we can make some quality assessment as well, though limited by the lack of external references.

3 DESCRIPTION OF THE OBJECT CLASSIFIERS

Table 2 summarizes the methods explored in this paper to perform object classification. These include a variety of algorithms using ML methods (training on morphological and/or colour information), pixel-level flux measurements, and template fitting. For the sake of clarity and conciseness, not all algorithms are subjected to every test in this paper, but usually a selection is made in each case. Additional details and references are given next.

3.1 CLASS_STAR

This is the standard SEXTRACTOR star–galaxy classifier, providing a neural network real number output (a ‘stellarity’ index from 0 to 1) based on the training on a large simulation of galaxy and star images on CCDs.

Input data: For every object, eight isophotal areas above the background are measured, plus the value of the intensity at the peak pixel in the object, and the value of the full width at half-maximum (FWHM) for the image.

Method: It uses a back-propagation model (Werbos 1982) for learning, based on simulations that include a wide range of PSF profiles and sizes, though they are optimized to work best on intermediate magnitude ranges (in the DES magnitude scale) of V ∼ 8 – 22 due to the types of galaxies simulated and relative star–galaxy mixture.

3.2 SPREAD_MODEL

This quantity is a linear discriminant-based algorithm available with the Sextractor package. The SPREAD_MODEL estimator was originally developed as a star–galaxy classifier for the DESDM pipeline and has also been used in other surveys (e.g. Desai et al. 2012; Bouy et al. 2013).

$SPREAD_{\text{MODEL}} = \frac{G^T V p}{\phi^T W p} - \frac{G^T W \phi}{\phi^T W \phi}$. (1)

where $p$ is the image vector centred on the source. $W$ is a weight matrix constant along the diagonal except for bad pixels where the weight is 0. By construction, $SPREAD_{\text{MODEL}}$ is close to zero for point sources, positive for extended sources (galaxies), and negative for detections smaller than the PSF, such as cosmic ray hits. The RMS error on $SPREAD_{\text{MODEL}}$ is estimated by propagating the uncertainties on individual pixel values:

$SPREADERR_{\text{MODEL}} = \frac{1}{\phi^T W p} \left( G^T V G (\phi^T W p)^2 + \phi^T V \phi (G^T W p)^2 - 2G^T V \phi (G^T W p \phi^T W p) \right)^{1/2}$. (2)

where $V$ is the noise covariance matrix, which is assumed to be diagonal.

An example of a classifier derived from $SPREAD_{\text{MODEL}}$ is the default classification scheme (MODEST_CLASS) used in the Y1 Gold catalogue, which includes the following criteria:

$galaxies \iff SPREAD_{\text{MODEL,I+}}$

$(5/3) \times SPREADERR_{\text{MODEL,I}} > 0.005$

AND

$\left| WAVG_{\text{SPREAD_{\text{MODEL,I}}} \right| < 0.002$

AND

$MAG_{\text{AUTO,I}} < 21.5$. (3)

6https://pole.uchicago.edu/
Table 2. Summary of classification methods. Type of data denotes whether measurements or direct pixel data are used, and in the first case if it is based on morphological and/or flux measurements. The specific algorithmical approach is named on the third column.

<table>
<thead>
<tr>
<th>Name</th>
<th>Type of data used</th>
<th>Algorithm</th>
</tr>
</thead>
<tbody>
<tr>
<td>CLASS_STAR</td>
<td>Isophotal level measurements, morphological</td>
<td>Neural network</td>
</tr>
<tr>
<td>SPREAD_MODEL</td>
<td>Measurements on fitted shape, morphological</td>
<td>Second moments of Gaussian mixture fit (object)</td>
</tr>
<tr>
<td>CM_T</td>
<td>Measurements on fitted shape, morphological</td>
<td>Second moments of Gaussian mixture fit (noisified object and PSF)</td>
</tr>
<tr>
<td>MCAL_RATIO</td>
<td>From a combination of simple functions used over all catalogue columns.</td>
<td>Boosted decision trees</td>
</tr>
<tr>
<td>ADA_PROB</td>
<td>Most discriminating features</td>
<td>Random forests</td>
</tr>
<tr>
<td>GALSIFT_PROB</td>
<td>All catalogue columns (PCA)</td>
<td>Support vector machine</td>
</tr>
<tr>
<td>SVM</td>
<td>MAG_AUTO, FLUX_RADIUS, SPREAD_MODEL, flux and morphology</td>
<td></td>
</tr>
<tr>
<td>CONCENTRATION</td>
<td>Catalogue information, morphological</td>
<td>Direct subtraction of magnitudes measured with model and PSF</td>
</tr>
<tr>
<td>WI-J, J-K</td>
<td>Catalogue information, fluxes</td>
<td>Colour cut</td>
</tr>
<tr>
<td>HB_PROB</td>
<td>Catalogue information, fluxes</td>
<td>Template fitting of spectral energy distributions</td>
</tr>
</tbody>
</table>

\[
\begin{align*}
\text{stars} & \iff \\
& |\text{SPREAD\_MODEL}\_\text{II} + (5/3) \times \text{SPREADERR\_MODEL}\_\text{I}| < 0.002
\end{align*}
\]

(4)

where WAVG\_SPREAD\_MODEL has been computed from a weighted average of the SPREAD\_MODEL values of single-epoch shapes corresponding to that coadd object. These provide a better separation (DES Collaboration 2018) with respect to the standard SPREAD\_MODEL on coadd images, albeit with a limited depth reach, as not all coadd objects have single-epoch detections from which a weighted average can be computed (a faint object could be detected only in the coadded image and not in the individual epochs contributing to the image). The weights come from the weight map of the data management processing outputs and the band chosen is the \(i\) band, where the images have a higher signal to noise and have also demonstrated best performance in detailed simulations. Objects that do not fall into the categories expressed by equations (3) and (4) are grouped into either a ‘fringe’ category or both. Typical values are in the range \(-0.5\) and 0.5.

3.4 \text{MCAL\_RATIO}

This measurement is derived from the size estimates obtained by the metacalibration technique, developed for shear measurement in weak-lensing studies (Sheldon & Huff 2017), in which the single epoch objects are artificially sheared to quantify the response of such an effect in the image.

\text{Input data:} The object size and PSF model size obtained using this technique.

\text{Method:} This approach uses the same \textsc{ngmix} code as MOF above. However, this measurement is much noisier as the metacalibration technique (Huff & Mandelbaum 2017) adds extra noise as part of the correlated noise correction. This is part of the procedure to correct for selection effects in shear inference, as detailed in Sheldon & Huff (2017). The discriminating quantity used is

\[\text{MCAL\_RATIO} = \frac{T_{\text{mcal}}}{T_{\text{PSF}}},\]  \hspace{1cm} (6)

where \(T_{\text{mcal}}\) and \(T_{\text{PSF}}\) are sizes of the object or PSF, respectively, as defined in equation (5). In this case, the size is obtained from a single Gaussian fit, so the suffix \(\text{CM}\) (composite model) is not used. Values are not constrained, but typical ranges explored for star–galaxy separation are between 0 and 1.

3.5 \text{ADA\_PROB}

This is the name given to a ML framework using the \textsc{scikit-learn} package (Pedregosa et al. 2011).

where \(x\) and \(y\) denote the distance from the object’s centre determined by the model fit. The value \((x^2) + (y^2)\) can be obtained analytically from the individual component Gaussians. The PSF is convolved with the fitted model to obtain these pre-PSF values. An associated uncertainty is computed as well, and our best-performing classifier, as tested\(^{10}\) in the COSMOS field, is based on the quantity \(CM\_T + 2 \times CM\_T\_\text{ERR}\). Typical values are in the range between \(-0.5\) and 0.5.

\(^{10}\)Technically, a different, validation set would be required to tune this classifier in terms of the quantity multiplying \(CM\_T\_\text{ERR}\), to avoid a bias towards a specific value, though in practice the differences are small between different choices.
Input data: This method uses feature generation (using various simple mathematical functions of various catalogue variables) and feature pre-selection (selecting the most informative variables).

Method: The selected quantities are fed into several ML algorithms (including AdaBoost) that are drawn from scikit-learn with an additional probability recalibration step. The details of the framework are described in detail in Appendix A. Two variants have been used of this approach, using either SExtractor quantities ADA_PROB or MOF quantities ADA_PROB_MOF.

3.6 GALSIFT_PROB

A probabilistic estimate based on ML approach over principal components, as used in the 'Multi_class' algorithm in Soumagnac et al. (2015).

Input data: A principal component analysis (PCA) over the catalogue quantities is performed to outline the correlations between the object parameters and extract the most relevant information. We perform a calculation of the Fisher discriminant (Fisher 1936) for each of the new parameters to quantify their aptitude to separate between the classes:

\[ F_i = \frac{(X_{G,i} - X_{S,i})^2}{\sigma_{G,i} + \sigma_{S,i}}, \]

where G and S corresponding to the galaxy and star classes, respectively.

Method: We select the parameters with the highest Fisher discriminant (hence the highest 'separation power' of the classes) and use them as input to a ML classification algorithm. Although in Soumagnac et al. (2015) the authors used ANNz (Collister & Lahav 2004), in this application we have replaced it by a random forest classification algorithm implemented as part of the scikit-learn package for PYTHON (Pedregosa et al. 2011). The output is a probability of the object being a star or a galaxy. In this case, we have used a classifier based only on MOF quantities, GALSIFT_PROB_MOF.

3.7 SVM

Following Wei et al. (in preparation), the support vector machine (SVM) is a single-band, purely morphological, and magnitude-based classifier.

Input data: The input features used by the SVM are MAG_AUTO_I, FLUX_RADIUS_I and SPREAD_MODEL_I.

Method: SVM is a supervised ML algorithm that constructs a separating hyperplane in any arbitrary n-dimensional space that maximizes the margins of objects to the hyperplane. To make the SVM robust across various data sets with intrinsic variations in observation conditions, the algorithm performs linear transformations on the three input features to remove the means and make the standard deviations across all objects to be one. This pre-processing procedure also allows all three features to have equal levels of feature importance. This prevents any features with particularly large numerical values from dominating the SVM classification decision. The SVM uses a Gaussian radial basis function kernel, where the hyperparameters, \( \gamma = 0.01 \) and \( C = 46.4 \), are selected while training the SVM through an exhaustive cross-validated grid search. The SVM outputs distances of objects to the hyperplane, where a high positive (negative) value corresponds to a high confidence star (galaxy) classification.

3.8 CONCENTRATION

A parameter similar to what was used as a star–galaxy classifier for SDSS (Abazajian et al. 2004).

Input data: The PSF and model magnitudes for each object.

Method: In the case of DES, this translates to the use of the difference between the MOF PSF magnitude and a bulge + disc, or composite, model magnitude computed by the MOF pipeline:

\[ \text{CONCENTRATION} = \text{PSF}_\text{MAG}_I - CM \text{MAG}_I. \] (8)

3.9 W1–J, J–K infrared bands

In the Stripe 82 region, we will compare with the information provided by the Vista Hemisphere Survey DR3 (McMahon et al. 2013) as proposed in Banerji et al. (2015) up to the available depth. We will also estimate the classification power of a cut in the infrared bands from WISE (Wright et al. 2010), 2MASS (Skrutskie et al. 2006), as described in Kovács & Szapudi (2015).

Input data: Magnitudes WI (WISE), J (2MASS, VHS), and K (VHS).


3.10 HB_PROB

Additionally, we implemented a hierarchical Bayesian method (HB_PROB) developed and explored by Fadely et al. (2012) and Kim et al. (2015) with CFHTLS data. The lack of u-band in our case severely impacted the performance of this method, so it was not pursued further in our analysis.

Table 3 shows the specific selection methods used with respect to a varying threshold \( t \) for each of the algorithms used in this work.

4 PERFORMANCE ON CALIBRATION FIELDS

In this section, we will look first at the metrics used to compare classifiers using the calibration fields, describe the data sets (including training and validation), and finally analyse the results.

4.1 Receiver operating characteristic curves

We compare the performance of the different classification techniques using the calibration fields by calculating Receiver operating characteristic (ROC; Bradley 1997; Fawcett 2006) curves that compare the true positive rate (TPR) of galaxy or star detection, given a specific threshold for the classifier, versus the false positive rate (FPR), as defined by

\[ TPR = \frac{TP}{TP + FN}, \] (9)

\[ FPR = \frac{FP}{FP + TN}, \] (10)

where TP are correctly identified galaxies, given a cut for a specific classifier; FN are incorrectly classified galaxies as stars; FP are incorrectly classified stars as galaxies and TN correctly identified stars (in the assumption of using 'truth' for galaxy type). See Table 4 for a reference on these concepts. Therefore, the ROC curve is confined by construction to an area spanning from 0 to 1 in FPR and TPR. As we vary the threshold \( t \) for classification for a given classifier (Table 3), a curve will be drawn across the area from (0,0) to (1,1). A completely random ‘classifier’ would show as a diagonal line.
Definitions of different figures of merit for classifiers, according to the outcome of the classification using a ‘truth’ reference (also termed ‘confusion matrix’). The term ‘positive’ can refer to ‘galaxy’ or ‘star’ classes depending on the use case. The metrics examined in this work are emphasised in bold. ‘Purity’ can be used as a synonym for the positive predictive value (PPV), whereas ‘completeness’ can be interchanged with the TPR.

<table>
<thead>
<tr>
<th>Prediction</th>
<th>Positive</th>
<th>Negative</th>
</tr>
</thead>
<tbody>
<tr>
<td>Truth</td>
<td>True positive (TP)</td>
<td>False negative (FN)</td>
</tr>
<tr>
<td></td>
<td>False positive (FP)</td>
<td>True negative (TN)</td>
</tr>
</tbody>
</table>

**Positive predictive value**

\[ PPV = \frac{TP}{TP + FP} \]

**False discovery rate**

\[ FDR = \frac{FP}{TN + FP} \]

**False omission rate**

\[ FOR = \frac{FN}{TN + FN} \]

**Negative predictive value**

\[ NPV = \frac{TN}{TN + FN} \]

In particular, the area under the ROC curve (AUC) has been classically used as a threshold-independent metric to compare the performance of classifiers as well as being relatively insensitive to the specific positive to negative composition (as long as sufficient statistics are available). The closer the AUC gets to unity, the better the discriminating power of the classifier associated with that particular curve. Again, a random classifier would show an AUC value of 0.5. There are, however, some caveats to be aware of, namely the possibility of misleading results when ROC curves cross each other (Hand 2009) and that misclassification costs can be different according to the scientific case, and this is not reflected in ROC curves. We address this by extending the range of metrics used for different classifiers, in order to have a broader view of the performance for our particular needs.

4.2 Purity and completeness

In astronomy, we are interested in evaluating the performance of classifiers in terms of their impact on measurable parameters of interest. It is common to find the requirements for a survey defined in terms of purity and completeness. In Soumagnac et al. (2015), for example, the authors formulate the scientific requirements for weak-lensing and LSS studies in terms of these two observables.

‘Purity’ is a measurement of the contamination of a sample by misclassified objects, which can also be called precision or PPV:

\[ PPV = \frac{TP}{TP + FP} \]

‘Completeness’ (also known as, recall) is another name for the TPR defined in equation (9). A good approach to easily compare the performances of several classifiers is to use the Precision-Recall (PR) curve, where both quantities can be visualized simultaneously.

4.3 Training and testing fields

The data set on which we train the ML codes is the weak-lensing catalogue from HST-ACS in the COSMOS field (Leauthaud et al. 2007), as this provides a largely unbiased measurement of all extended and point-like sources from DES (albeit the star–galaxy mixture is affected by the specific position in the sky with respect to the Galactic plane). In particular, the $M_{\text{CLASS}}$ parameter is used for this reference, defined in the peak surface brightness – $M_{\text{AUTO}}$ space, which in space-based imaging shows very distinct loci with respect to the same objects viewed through the atmosphere. This has been used previously in star–galaxy separation assessments in, e.g. Crocce et al. (2016) and Aihara et al. (2018).

This training set, after a larcmin positional match with DES sources, contains $\sim 114 \, k$ extended and $\sim 12 \, k$ point-like sources. The COSMOS data set will also be used for some tests only with the non-ML codes in order to avoid biased conclusions based on their training in that same area.

Even in the case in which we use unbiased, imaging data, the particular position on the sky of the field will condition the relative mixture of stars and galaxies in a prominent way. Therefore, we add some extra imaging data extracted from the Hubble Source Catalog11 (Hubble-SC; Whitmore et al. 2016) where it overlaps the DES survey. Most of it is either too inhomogeneous or targets specific objects (nearby, large galaxies or globular clusters), but a

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11 https://archive.stsci.edu/hst/hsc/
few deep fields can be matched with some of the SN fields from DES. In this case, we use the Hubble-SC catalogues’ concentration index with a cut of 1.2 that seems optimal in the concentration–magnitude plane.

Spectroscopy is also a valuable resource to provide a one-to-one truth table for our classifications. However, the spectroscopic targeting and measurement efficiency is not complete in a statistical sense relative to the DES catalogue, as certain types of sources were given higher priority and some types are more difficult to classify spectroscopically therefore the testing of purity/completeness can be strongly biased. The photometric properties of the stars and galaxies selected can also be highly skewed to particular types that introduce additional biases. This limits the usefulness of any purity metric we try to derive from these fields. For this reason, the spectroscopic data sets have been limited to those that provide a relatively unbiased sample by construction, which includes the VVDS-DEEP and VVDS-CDFS (Le Fèvre et al. 2013) data releases. The SDSS DR13 (Albareti et al. 2017) updated spectro-photometric sample over Stripe 82 is also used due to the relative variety of spectra available, and the possibility to test our classification methods against ‘true’ spectroscopic typing. We use redshifts (a cut in \( z < 0.001 \)) as the method to identify stars. However, we also consider a selection based on SDSS spectroscopic \textit{CLASS} obtaining similar conclusions. For the VVDS data, we require the redshifts to be ‘reliable’ according to the classification in Le Fèvre et al. (2013), that is, values of 2, 3, 4, or 9 in their redshift quality estimate.

Both the COSMOS catalogues and the ones recovered from the Hubble-SC have been cross-tested against spectroscopic catalogues VIMOS-Ultra Deep Survey DR1 (Tasca et al. 2017), \( z \text{COSMOS DR3} \) (Lilly et al. 2009), and VVDS-CDFS (Le Fèvre et al. 2013) to check the robustness of their morphological classifications against a ‘true’ type based on their spectra. In both cases, around 5 per cent of spectroscopically classified stars are misclassified as galaxies when using these space-imaging based measurements, whereas around 2 per cent of spectroscopically classified galaxies are misclassified as stars. This misclassification happens at faint magnitudes (\( F814W > 24 \)) from ACS-HST, \( F814W > 23 \) for the other Hubble fields used), denoting possible compact galaxies that are unresolvable by HST, errors in the spectroscopic measurement, or matching. These corrections are not considered for the purity estimates derived here as they belong to fainter fluxes than the truth tables used in our tests.

See Table 1 and Appendix B for details on the reference data in different fields including the data base queries used to create these data sets.

### 4.4 Results

#### 4.4.1 Using HST imaging

We compare here the results for the classifiers used on the COSMOS field (excluding the ML codes that were trained on this field) and the SN fields for which we have found publicly available deep HST data from the Hubble-SC.

(i) The results for the ROC comparison are shown in Fig. 1 for the COSMOS field and Fig. 2 for the SN fields with Hubble-SC data. The AUC of the respective curves are tabulated in Table 5.

From these plots, it can be readily seen that among the morphological classifiers, the algorithms based on a linear discriminant over coadded images, SPREAD\_MODEL\_I, and intrinsic size on MOF estimates, CM\_T, are the best-performing ones. It is also seen that the ML classifiers (in Figs 2 and 3) do perform better, even considering a different field with respect to training as in the case of the Hubble-SC test. It is noteworthy to point out that most of the differences showcased in Figs 1 and 2 become more evident when we restrict ourselves to faint objects \((i > 22)\). The SPREAD\_MODEL-based cut does a good job at avoiding stellar contamination but suffers from decreased galaxy completeness. This is a result of the galaxy locus merging with the stellar locus in the magnitude-SPREAD\_MODEL space where noisier measurements will increase the effect even further. CM\_T fares better in this respect, but a conservative cut will provide a more pure galaxy sample using SPREAD\_MODEL. On the other hand, the metacalibration size ratio does not perform as well as the other morphological classifiers, though this measurement is noisier than the direct assessment of sizes and shapes from the MOF pipeline.
Table 5 Area under the ROC curves for different classifiers. Dashes indicate tests that have not been run for that specific code and dataset combination.

<table>
<thead>
<tr>
<th>Name</th>
<th>COSMOS, imaging</th>
<th>SN fields, imaging</th>
<th>SN fields, spectroscopy</th>
<th>Stripe 82, spectroscopy</th>
</tr>
</thead>
<tbody>
<tr>
<td>CLASS_STAR</td>
<td>0.898</td>
<td>0.885</td>
<td>0.950</td>
<td>0.976</td>
</tr>
<tr>
<td>SPREAD_MODEL</td>
<td>0.954</td>
<td>0.956</td>
<td>0.975</td>
<td>0.962</td>
</tr>
<tr>
<td>CM_T (MOF)</td>
<td>0.957</td>
<td>0.959</td>
<td>0.971</td>
<td>0.972</td>
</tr>
<tr>
<td>CONCENTRATION (MOF)</td>
<td>0.938</td>
<td>0.953</td>
<td>0.950</td>
<td>0.967</td>
</tr>
<tr>
<td>MCAL_RATIO</td>
<td>0.910</td>
<td>0.924</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>VHS J-K vs G-I</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>ADA_PROB</td>
<td>–</td>
<td>0.978</td>
<td>0.983</td>
<td>0.967</td>
</tr>
<tr>
<td>ADA_PROB (MOF)</td>
<td>–</td>
<td>0.967</td>
<td>0.980</td>
<td>0.967</td>
</tr>
<tr>
<td>GALSIFT_PROB (MOF)</td>
<td>–</td>
<td>0.969</td>
<td>0.981</td>
<td>0.962</td>
</tr>
<tr>
<td>SVM</td>
<td>–</td>
<td>0.962</td>
<td>–</td>
<td>–</td>
</tr>
</tbody>
</table>

Figure 3. Precision-Recall (or completeness-purity) plot for classifiers tested on the SN fields over the Hubble-SC catalogue, using galaxies as truth. Magnitude range is given by $M_{AUTO,I} = (17, 24)$. The SPREAD_MODEL-based cut is similar to the MODEST_CLASS used in DES Y1 analyses.

(ii) Fig. 2 shows that ML classifiers are able to take advantage of ancillary information for very faint objects, where shape measurements are uncertain. Results with SVM in the SN fields show that an ML approach based exclusively on morphological and magnitude information can provide some advantage over simple cuts on morphological variables. SVM is shown to be robust outside its training field, however, other ML algorithms provide an extra edge in performance as shown by the higher AUC values. This is due to forgoing the additional information encoded in the rest of the variables available in the catalogue. However, this approach could provide a middle-ground solution to the issues one might encounter when incorporating colour-based information, which can incorporate interesting physics we would not like to be entangled with our star–galaxy sample selection (see Section 6). Further developments of this approach are explored in Wei et al. (in preparation).

The comparison between the COSMOS and Hubble-SC fields reveals that the CM_T classification is more robust as we switch between fields. SPREAD_MODEL and CLASS_STAR, which are derived from coadded PSFs, are more vulnerable to the contribution of bad exposures and PSF inhomogeneities in the coadded image. It is worthwhile noting here that preliminary tests on Y3 data (DES Collaboration 2018) using Hyper Suprime Camera deep data (Aihara et al. 2018) reinforce this idea, which will be explored further in a future publication therefore favouring in general the use of a multi-epoch classifier (such as CM_T based on the MOF pipeline). Both the COSMOS field data set and SN field coadds have a much smaller dithering than the wide-field exposures. This might artificially bias classifications based on the coadded PSF to somewhat better performances than actually present in the wide-field data.

(iii) Figs 3 and 4 show the PR metric, for galaxies and stars, respectively (COSMOS plots not shown for conciseness but provide similar conclusions). These plots provide a similar conclusion as the ROC curves, though in terms of more useful quantities with respect to scientific requirements such as the recall (i.e. completeness) and precision (i.e. purity). Again, the CM_T morphological classifier and the ML codes provide the best results, and this manifests even more strongly for selecting a star sample (these results motivate the choice for stellar classification based on multi-epoch pipelines in Shipp et al. 2018). It is noteworthy to add that the ML classifiers using MOF quantities do not add much more than a straight cut in CM_T itself due to the large information content included in this classifier regarding star–galaxy classification. On the other hand, the ML classifiers based on SExtractor quantities are able to extract more value from the different outputs of this code, with respect to a simple SPREAD_MODEL cut.

(iv) In Figs 5 and 6, we can appreciate the dependence of the completeness with the magnitude as we go to the fainter end in the sample, in the galactic and stellar case, respectively. Unlike in the previous plots, in this case a choice of threshold has to be made. We have decided to pick cuts in the variables in question in order to have a similar galaxy purity (99 per cent) in each magnitude
bin, so we can compare completeness appropriately, and similarly for stars (80 per cent). We chose the COSMOS field that has good statistics to faint magnitudes, though this disallows using the ML codes in the comparison. This example shows a case where classifiers such as the concentration estimation from the MOF pipeline, not necessarily favoured at first sight from the integral under the ROC curve, works better in this regime due to its good selection of very pure samples. The ROC curve only informs about overall classifier performance (i.e. considering all possible thresholds), and different classifiers have to be tested for the specific science case at hand.

For stars, a similar behaviour is seen for CM\textsubscript{T}, CONCENTRATION and SPREAD\textsubscript{MODEL}. CLASS\textsubscript{STAR} for instance suffer from a poor completeness near the faint end, as a high thresholding cut in this case removes most of the objects, which in the neural network tend to cluster towards intermediate values when the object classification is uncertain. MCAL\textsubscript{RATIO} incorporates noisier measurements and additional cuts to the sample that make it less complete when providing a classified sample.

(v) In addition, in Fig. 7 a similar comparison is shown as a function of a realization of the photometric redshift from the probability distribution function obtained from the Bayesian Photometric Redshift algorithm (BPZ, Benítez 2000), this time also adding the}

\begin{figure}[h]
\centering
\includegraphics[width=0.5\textwidth]{figure5.png}
\caption{Completeness of a galaxy sample as a function of magnitude for classifiers tested on the COSMOS field, for a fixed galaxy purity of 99 per cent.}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=0.5\textwidth]{figure6.png}
\caption{Completeness of stellar sample as a function of magnitude for classifiers tested on the COSMOS field, for a fixed 80 per cent purity.}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=0.5\textwidth]{figure7.png}
\caption{Purity of the galaxy sample as a function of photometric redshift for classifiers tested on Hubble-SC matches over the SN fields field, for a fixed 90 per cent completeness.}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=0.5\textwidth]{figure8.png}
\caption{ROC plot for classifiers tested on the SN fields over the VVDS catalogues. Magnitude range is given by $M_{\text{AUTO}I} = (17,24)$. The ROC curve is obtained by varying the threshold at which the classification divides the galaxy and star sample.}
\end{figure}

ML classifiers (again over the SN fields with Hubble-SC). A similar conclusion is drawn from these plots; MOF fitting methods and ML classifiers perform best, as indicated by the ROC curves. Note the stability of the purity of the galaxy sample with respect to photo-$z$, suggesting that a photo-$z$ selected sample would not be biased by the star–galaxy separation classifiers analysed here (however, see Section 6.1 for an important caveat to this conclusion).

4.4.2 Using ground-based spectroscopy

Turning now to tests on the overlapping spectroscopic data, we show ROC plots to demonstrate the consistency with the results from the previous section and add a comparison with external infrared information.

Fig. 8 shows the ROC for the VVDS test, and Fig. 9 shows the ROC for the Stripe 82 test. The former does not add much to the conclusions mentioned above but provides an assurance that conclusions are consistent with a different class of 'truth' typing. We also add here a test on the SN fields computing the ROC curves.
and their areas, versus the signal to noise of the detected objects, to demonstrate it behaves as expected as well, including the ML codes (see Fig. 10).

The Stripe 82 data set is shallower and therefore does not allow for a clear distinction between the performance of most of the algorithms described here. The comparison with the combination with external infrared colour cuts on the other hand, shows an important increase in performance, specifically when attempting to select a very pure stellar sample, as already advanced in Baldry et al. (2010) and Banerji et al. (2015). It is important to note here again that the nature of the test is different with respect to the ones based on space imaging. In this case, we are using spectroscopic redshifts to determine the nature of the object (galactic or extra-galactic) and not its extendedness. What we see here is that infrared information will select out the stars from the galaxy and QSO (which are point-like generally) population. We have also attempted to add W1-J version from 2MASS and WISE (as suggested in Kovács & Szapudi 2015), but the matches proved too shallow to be of any interest for these samples.

Unfortunately, the current VHS data do not cover the full breadth and depth of the survey and a careful combined catalogue with adequate matching is needed (overcoming the less-precise infrared astrometry) beyond what was done here for comparison purposes. Cross-matching with bright sources will be explored in more detail with DES Y3 data with the goals of enhancing star selection for creating PSF models and reference catalogues for LSS. A combination of classifiers, as done for instance in Kim et al. (2015) or Molino et al. (2014), seems to be an appropriate option in this case and even more so if matched-aperture photometry of VHS data can be performed survey wide for DES (Banerji et al. 2015). This would also have important applications for photometric redshift determination (Banerji et al. 2008).

5 PERFORMANCE ON APPLICATION FIELD

It has been shown by Fadely et al. (2012) that ML techniques in star–galaxy classification will perform better if a representative training data set is found. We have studied the impact of this effect by testing ML algorithms over different fields other than the training set in Section 4. However, all these additional areas are quite constrained either in depth or area, when compared to the complete DES volume.

In this section, we extend the scope of the performance tests in classification to have a broader picture by making the following checks on the application field (see Section 2):

(i) General distribution of the classifier-flux space to qualitatively analyse the algorithms’ outputs.

(ii) Number count distributions of stars against a well-tested simulation, both as a function of magnitude and as function of galactic latitude.

(iii) Galaxy versus star density profiles in search of correlations, using different proxies for the true stellar distribution.

(iv) Density of classified galaxies as a function of proximity to the Large Magellanic Cloud (LMC).

(v) Consistency of classified stars with the expected stellar locus (Covey et al. 2007).

Except where noted, the sample sizes for each of these cases are approximately 1 million objects, limited by the size of tested region, magnitude range, or photo-$z$ binning.

5.1 Classifier outputs

A first step towards understanding the quality of classification for different algorithms in the application field of DES is to study the outputs as a function of magnitude and the number counts of classified objects.

In Fig. 11, several density plots showcase how objects distribute in the classifier-magnitude space. These distributions are based on a 1 per cent sample of the Y1 Gold catalogue. Direct morphological outputs from the DESDM pipeline (CLASS_STAR, SPREAD_MODEL and CM_T) show two loci that merge in the faint end. CLASS_STAR outputs merge into a region of 50 per cent probability by construction of its base neural network. This uncertainty region appears at shallower magnitudes than other classifiers as shown previously, due to the characteristics of the simulations used for its training. However, a classifier using a feature importance selection manifests a more ‘clear-cut’ classification of objects, with a large predominance of galaxies at the faint end, as expected. This can be attributed to the fact that there is a large predominance

A pre-selection of the input variables that provide the most predictive power for the task at hand, e.g. star–galaxy separation.
Star–galaxy classification in DESY1 data

5.2 Number counts of classified stars

On the other hand, if we limit our study to the point in which Y1 data are fairly complete over a large area \( r \sim 22.5 \), we can assess for instance the similarity of the stellar distribution in magnitude versus a detailed simulation such as Galaxia (Sharma et al. 2011), which has been tested against Gaia DR1 data (Gaia Collaboration 2016; Koposov, private communication). This is shown in Fig. 12 for a few selected classifiers, spanning a varied range of those mentioned in Section 3, in the DES \( r \) band. Thresholds were used to provide a similar number of stars as MODEST_CLASS, the default DES Y1 Gold star–galaxy classifier based on SPREAD_MODEL. Up to \( r \sim 21 \), the behaviour for most of them with respect to the simulation is similar. Two ML classifiers based on MOF quantities show a significant lack of bright objects \( r < 19 \) due to failures from the Y1 version of the MOF pipeline in fitting stars in this regime.\(^\text{13}\) This has been identified as failures of the galaxy fits for which MOF was designed when applied to moderately bright stars. A consistent overestimation of stars by Galaxia with respect to DES stars is apparent for all classifiers, as was seen in Li et al. (2016). On the other hand, other simulations such as the ones described in Robin et al. (2003) and Girardi et al. (2005) show discrepancies of this size as well at this latitude and longitude. This disappears at the faint end, as compact galaxies start to leak into the stellar sample. After that, a completeness drop kicks in as we enter the survey’s magnitude limit. At the faint end, CLASS_STAR shows a drop in completeness sooner than the other classifiers. The nature of this classifier, which provides an intermediate value of probability for ‘uncertain’ sources, is such that a fixed threshold cut tends to ‘lose’ stars at the faint end, if we adjust all classifiers to the same number of stars.

5.3 Stellar density as a function of Galactic latitude

As a complementary measure of goodness of stellar identification, we compare the number of stars as a function of Galactic latitude (Fig. 13). We limit the comparison to the range in which any possible issues deriving from the current MOF processing are avoided (see Section 5.2). A slight deficit is seen none the less as was verified before, but the comparison of all these different approaches is qualitatively in the same range, without any preferred or outstanding behaviour from any of the classifiers tested here.

\(^{13}\)Y3 Gold MOF photometry has solved this issue.
5.4 Galaxy versus stellar density

As mentioned in Section 4.2, we do not have a large-scale ‘truth’ table available that we could use as reference to check the precision of our classification on an object-by-object basis. However, several studies of LSS (e.g. Ross et al. 2011) have devised an estimate of the purity of the galaxy sample, for a given classification scheme, by measuring correlations of classified galaxy density versus some reliable measurement of the relative stellar distribution (using a very pure cut for stars, a model, or an external catalogue). This is done via the pixelization of the field using the HEALPix software (Górski et al. 2005) and fitting a linear relation between the galaxy overdensity as a function of stellar density in said pixels. For this study, we used a pixelization parameter NSIDE = 512, which corresponds to a pixel size of approximately 0.01 deg².

In Fig. 14, we show a comparison of the galaxy density as a function of stellar density for several classifiers, tested on the application field for the galaxy sample with the magnitude cuts shown in Table 6. Errors for each point are computed using the jackknife method (Efron & Stein 1981), whereas the ones in the table correspond to the estimated error from the fit.

The galaxy density over samples of increasing stellar density would theoretically increase with a linear relationship, if stellar contamination was the only effect that a dense star field would introduce. However, as seen already in Ross et al. (2011; in their fig. 3), moderately bright stars can also induce an ‘occultation’ effect that makes detection around them more difficult. This effect is more predominant for fainter sources. This will create an inverse, possibly non-linear, relationship between galaxy density and stellar density. The overall effect is to create a proportionality relationship at low to moderate stellar densities, which may or may not change in slope and even decrease, depending on the separation power of the classifier, as galaxies get removed from the catalogue due to the presence of foreground bright stars. For our purposes here, i.e. to understand the star–galaxy separation power for different classifiers, we use the intercept value of the linear fit to the first part of the plot, in order to estimate the purity of the galaxy sample. We adjusted the cuts for the classifiers to provide a similar number of detected ‘galaxies’ (i.e. a similar completeness) as MODEST_CLASS, in order to get a better handle on how purity compares on the same grounds, similar to what we did on Section 4.4.1.

We note that using the application sample in bulk shows no strong contamination component for the SPREAD_MODEL- or MOF-based quantities or for the ML approaches using magnitude and colour information. Slightly better performance is found using MOF quantities and the ADABoost code, especially for fainter objects. This is explained by the more accurate shape measurement of the MOF code and by how additional information is captured by ADA_PROB_MOF.

One of the components of these calculations is the choice of a star map to establish the density relationships. We have derived a ∼1 per cent systematic uncertainty in the estimation of the impurity derived from comparing brighter and fainter stellar samples (Fig. 15). The 2MASS and Tycho-2 (Skrutskie et al. 2006; Hög et al. 2000) stellar maps are included for completeness, but their magnitude range does not track accurately the range of brightness we need to account for Milky Way distribution in DES. Gaia’s DR2 corresponds to the data described in Gaia Collaboration (2018).

5.5 Galaxy ratio near the Large Magellanic Cloud

Using the same pixelization as above, we also approach the comparison of different classifiers using a figure of merit based on the identified galaxy density in each of these pixels, as compared to the one found at a certain distance to the centre of the LMC, set at (α, δ) = (5°23′34″.5, −69°45′11″). This value is normalized to one at 30 deg from the centre of the LMC (Fig. 16). Here, we use a flux-limited sample with i < 23. In this case, we can see a clear advantage in using a classifier with multiple input attributes (including colour), possibly helped by the fact that in a crowded field such as the peripheries of the LMC, morphology starts to have a smaller discriminating power. On the other hand, the LMC has a bluer population, but this doesn’t seem to offset the ML classification significantly, though this aspect is worth studying further in a future work.

Figure 13. Counts for stars as classified by different algorithms compared to a Galaxia simulation (Sharma et al. 2011) for the application field (SPT region of the DES-Y1 footprint) for the magnitude range r = (19, 21.5).

Figure 14. Galaxy versus star density plot for several classifiers, for i < 22 (top) and i < 23 (bottom). Star density is traced by an external map of ‘secure’ moderately bright stars.
Table 6. Contamination for different classification methods for the galaxy versus stellar density tests. Threshold cuts were selected to adjust to the same number of detected galaxies as provided by MODEST_CLASS.

<table>
<thead>
<tr>
<th>Sample</th>
<th>MODEST_CLASS</th>
<th>CLASS_STAR</th>
<th>ADA_PROB</th>
<th>ADA_PROB_MOF</th>
<th>GALSHIFT_PROB_MOF</th>
<th>CM_T</th>
</tr>
</thead>
<tbody>
<tr>
<td>$i &lt; 22$</td>
<td>2.7 ± 0.4 per cent</td>
<td>2.1 ± 0.5 per cent</td>
<td>2.2 ± 0.4 per cent</td>
<td>2.2 ± 0.4 per cent</td>
<td>2.3 ± 0.4 per cent</td>
<td>2.3 ± 0.4 per cent</td>
</tr>
<tr>
<td>$i &lt; 23$</td>
<td>3.2 ± 0.4 per cent</td>
<td>4.6 ± 0.2 per cent</td>
<td>2.4 ± 0.4 per cent</td>
<td>2.1 ± 0.4 per cent</td>
<td>2.8 ± 0.3 per cent</td>
<td>2.4 ± 0.4 per cent</td>
</tr>
</tbody>
</table>

Figure 15. Star contamination levels for different stellar maps. A ~1 per cent systematic uncertainty, derived by comparing the MODEST_CLASS moderate to bright stars, is estimated from this plot. Tycho and 2MASS stars are added for comparison, but their magnitude ranges (much brighter than the stellar sample considered as contaminants) do not make them good candidates for deriving this uncertainty.

Figure 16. Galaxy ratio (with respect to galaxy density at 30 deg from LMC) for as a function of angular distance from the LMC centre.

Using a metric such as this at a given fixed distance of the LMC could be useful as a figure of merit. In this case, 10 deg seems convenient, but we must remark that this could be due to the odd geometry available around the LMC, so other photometric surveys might find other ranges for comparison more valuable.

5.6 Stellar locus of classified stars

Finally, we tested the consistency of the stellar locus derived in $r - i$ versus $g - r$ colour space to a similar fit to stars in the COSMOS field. The stellar locus was fit by a fifth-order polynomial, as shown in Fig. 17, similar to what is realized in Covey et al. (2007). The same fit curve from Fig. 17 is shown again versus several classifiers in Fig. 18. In general, a good agreement is seen except for the faintest end, where classified stars seem to deviate from the expected stellar locus for CLASS_STAR.

Figure 17. Fit to stellar locus using a fifth-order polynomial.

Figure 18. Stellar locus for star samples from various classifiers, for a bright sample ($i < 21$, top) and a fainter one ($i < 24$, bottom).

6 DISCUSSION: IMPLICATIONS FOR LARGE-SCALE STRUCTURE AND MILKY WAY STUDIES

In the previous section, we explored a variety of tests both with and without truth information assessing the relative performance of a
wide range of star–galaxy classifiers in DES Y1 data. We now turn to the impact of making different selections on scientific analyses of interest to astronomers and cosmologists. Though it is beyond the scope of this work to define specific choices for any arbitrary study, in this section we sketch out the general implications of the results shown here for two broad ranging topics of interest, namely the LSS of galaxies and Milky Way analyses within DES. Regarding weak-lensing shear catalogues, Zuntz et al. (2017) have shown that star–galaxy contamination is at most a second-order contaminant when either MODEST_CLASS or MCAL_RATIO are used for the DES Y1 cosmology analyses. For a thorough discussion on LSS and weak-lensing requirements for star–galaxy separation, Soumagnac et al. (2015) provides an in-depth review.

6.1 Large-Scale Structure

The impact of stellar contamination on studies of clustering amplitude has been well studied for several years now (e.g. Ross et al. 2011; Crocce et al. 2016) with an impact of the order of \((1 - \theta)^2\) in the angular correlation function \(\omega(\theta)\) if we assume an unclustered component that contaminates the galaxy population with impurity fraction \(I\). A large contamination can severely dilute the signal (reducing the significance of the BAO peak as shown by Carnero et al. 2012), or even create a large-scale component if unaccounted for, thus mimicking an effect such as primordial non-Gaussianities (Giannantonio & Percival 2014). However, in the range \(I \sim 0\) (2 per cent), the accuracy by which we determine \(I\) becomes much more relevant, as this is the systematic that will dominate in the determination of the uncertainty in galaxy bias measurements and multiple probe analyses.

Fig. 14 implies that the choice of classifier does not matter too much for cosmology analyses in the broadest sense. However, going into a more realistic sample for LSS studies, using a selection for red galaxies that have better estimated photo-\(z\) and galaxy bias (Crocce et al. 2017) for BAO analysis for example, some evident differences appear for the highest redshifts (where due to their colours, many faint stars are misclassified into those bins of photo-\(z\)). This is the main photo-\(z\) region of interest for BAO for DES. Also between the classifiers, which become more evident, when the flux cut is driven to fainter magnitudes as shown before. See Fig. 19.

These results show that a realistic LSS sample, is more severely affected by stellar contamination, driving the impurity levels up to 5–6 per cent in some redshift bins. This is seen more clearly in Fig. 20 where photo-\(z\)-stars are shown for the true stars in the fields overlapping the COSMOS region for a general selection and an LSS-like, red galaxy selection. One way to drive down this impurity therefore is either apply more stringent constraints to the star–galaxy thresholds, sacrificing a per centage of true galaxies along the way. For the case of MODEST_CLASS and ADA_PROB_MOF, we can push down to 2 per cent by removing \(\sim 9\) per cent and \(\sim 4\) per cent galaxies, respectively. Though an ML approach seems more convenient in this case, the use of colour and magnitude information may lead to potential correlations between object classification and photo-\(z\) determination that must be investigated in more detail. As for the uncertainty of determining \(I\) using the density plots, Fig. 15 shows that using fainter stellar maps to derive the impurity via this method generates a different contamination rate. This can be due to tracing of different components of the Galaxy, but for maps built upon possibly contaminated data it could well be that the star maps themselves are not ideal (e.g. the bright MODEST_CLASS stars could have a small component from misclassified compact galaxies). An improvement in understanding the underlying Galac-

![Figure 19](https://example.com/figure19)

**Figure 19.** Stellar contamination level as a function of redshift for a bright sample (top, \(i < 22\)) and a faint sample (bottom, \(i < 23\)), derived with the method described in Section 5.4 for different samples classified by photometric redshift.

![Figure 20](https://example.com/figure20)

**Figure 20.** Normalized distribution of BPZ redshifts for a typical red galaxy sample that would be used for LSS studies, over a region with known identification of stars and galaxies through *Hubble Space Telescope* imaging.
magnitudes, we have to be very careful with introducing biases or for Milky Way neighbours with a particular range of colours and want to study the distribution of specific types of stars, or search (e.g. Willman 2010; Bechtol et al. 2015; Drlica-Wagner et al. 2015; Pieres et al. 2017). This problem is evidenced returning to the COSMOS ACS catalogue used in Section 4, which can be used to understand the ratio of stars to galaxies up to a very faint limit (shown in Fig. 21).

In this sense, the results in Pieres et al. (2017) or Shipp et al. (2018), for example, show that the very good results can be obtained based on a multi-epoch based classifier such as the weighted averaged SPREAD\_MODEL quantity or the MOF pipeline. The use of ML codes in this case is limited by the fact that if we want to study the distribution of specific types of stars, or search for Milky Way neighbours with a particular range of colours and magnitudes, we have to be very careful with introducing biases or complex selection functions in our application sample, much like what happens with photometric redshifts for the LSS case.

What the results of this study show (e.g. Fig. 4) is that the MOF technique has the potential of being the best candidate for selecting stellar candidates from its very tight morphological stellar locus and its capacity of reaching deeper into the separation of extended and point-like sources, increasing by \( \sim \) 20 per cent the amount of stars in the sample for a given purity and magnitude cut versus a ‘classical’ SPREAD\_MODEL cut (in this plot, at 0.8 purity we go from 0.70 to 0.84 completeness). However, additional fine tuning of the algorithm is needed to reach a good completeness in the bright end, where the model fit is not especially attuned to fits of stellar shapes. This is an open line of development in the algorithm in DES.

7 CONCLUSIONS

In this paper, we have compiled a wide variety of tests over a diverse array of star–galaxy classifiers for the DES Y1 data set. These tests can be ported or used as examples for any other photometric data set. The classifiers range from well-tested algorithms in the literature, to new developments using morphological information and/or flux information, using priors for stars/galaxies or training sets for ML codes based on space imaging information from the Hubble Space Telescope. We have studied their relative performance both using accurate truth information from spectroscopic and space imaging external data sets, and devised tests over the broad DES Y1 footprint that do not require this information. In the light of these results, we have analysed the impact of using these algorithms on two broad science cases of interest to users of the DES data, namely, LSS analyses and Milky Way studies. Star–galaxy classification remains as a non-dominant but important systematic source of error for cosmology, and very critical for Milky Way structure measurements and discoveries. These are the specific items that were highlighted in this work:

(i) ML methods perform very well on calibration fields tests (Figs 2–4 and Table 5). In the application field the results are slightly better than for non-ML classification, especially in the faint end (Fig. 19). Optical colour-based classifiers, however, could potentially introduce biases in sample selection.

(ii) Although CLASS\_STAR has been used in the past to good effect, its lack of performance in the faint end (see e.g. Figs 1 and 12) leads us to recommend alternative classification methods such as SExtractor\_SPREAD\_MODEL or a multi-epoch fit to the shape. In this sense, using multi-epoch, multi-object fitting instead of directly using coadded information is the preferred option for object classification in optical wavelengths (as shown in Section 4).

(iii) As has been demonstrated in the past, the addition of infrared data is very valuable, albeit limited currently by the depth and extension of such surveys (Section 4.4.2).

(iv) Photometric redshift binning will affect stellar contamination of specific galaxy samples (Fig. 20).

7.1 Expected improvements for Y3 and beyond

Considering these results, we have identified very clear future directions to expand and improve star–galaxy classification in forthcoming DES science analyses (Y3 and beyond):

(i) Improvement of the MOF quantities to better fit stellar shapes and prevention of fitting failures.

(ii) Understanding the impact of using colour information on specific science cases (photo-z, stellar type selections) to ascertain whether or not the usage of this information in ML codes hampers their utility for star–galaxy separation in extragalactic and Milky Way studies, respectively, in exchange of an additional 2–5 per cent in purity depending on the case.

(iii) The combination of information as done in Kim et al. (2015) from different approaches, especially adding external infrared colours, could greatly benefit the performance of some classifiers. Once an adequate template set is studied for the DES data, trying to overcome the impact of the lack of u-band information, template-based codes could be considered as well to complement this impact study. In addition, this would provide a truly probabilistic output that could be employed in statistical studies of LSS, removing the need of having to eliminate a subsample of galaxies according to an arbitrary threshold.

(iv) Besides VHS data, the addition of Gaia’s DR2 information (Gaia Collaboration 2018) will provide a robust and broad complement to these tests at magnitudes \( r < 21 \).

7.2 Ideas for further study

Finally, we call attention to other approaches and tests that we have not specifically investigated here that could be relevant for future studies:

Figure 21. Star–galaxy ratio in differential MAG\_AUTO bins, taken from the COSMOS ACS catalogue. Point sources are overwhelmed by extended sources in the faint end.
(i) Adding available $\lambda$ band and specially infrared band information using matched-aperture photometry as part of the algorithms used here.

(ii) With respect to a template-fitting approach, the characteristics of this data set (lack of $\lambda$ band or infrared information), severely limit its usability. But expanding the data set, jointly with an accurate understanding of the template range to be used can be considered as a promising approach, if these requirements are met, to be used in a joint probabilistic method.

(iii) Including very detailed image-based simulations for training, such as Balrog (Suchyta et al. 2016) or UFIG (Chang et al. 2015), to understand the failure modes of different classifiers.

(iv) Adding seeing as part of the features of the ML classifiers as well as for characterization of the performance of the different approaches.

(v) Usage of the object position in the sky can also provide an additional lever for a probabilistic approach, as a prior to be added to the overall posterior estimation. This should be approached with care for certain analysis (e.g. Milky Way structure).

(vi) PSF homogenization will improve the SExtractor estimates as shown in Desai et al. (2012). However, using MOF-based photometry is a more promising alternative that avoids some of the problems associated with homogenization.

(vii) Convolutional neural networks (e.g. Kim & Brunner 2017) can be applied directly to the images to provide a new and complementary approach to ML applied at catalogue-level. Image-level analyses may benefit using information from multiple (>10) bands (e.g. Cabayol et al. 2018).

The data used in this paper are provided at http://des.ncsa.illinois.edu/releases/y1a1.

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APPENDIX A: ADA_PROB TECHNICAL DETAILS

This appendix describes the details of one of the ML frameworks called ADA_PROB.

The framework first selects an exhaustive list of photometric properties, or features, and generates linear combinations of these features to produced new features. This may include unphysical combinations, such as magnitudes and radii being combined. We also generate features ‘intelligently’, by using the current state of the art. For the problem of star–galaxy separation for DES, this means including both a binary MODEST_CLASS class value, and a continuous MODEST_CLASS variable for both stars and galaxies.

Next, the enormous feature list is sorted by rank, using the value of the mutual information,\(^ {14}\) which is a non-linear correlation coefficient, between the selected feature and the target class. Finally the top 150 features are selected to form the inputs to the ML algorithms.

The framework then explores many ML algorithms, each of which are trained with random variations of each of their own hyper-parameters. The framework explores a plethora of algorithms, drawn from the sci-kit-learn (Pedregosa et al. 2011) package. These include AdaBoost, which often performs well, and also Random Forests, Extra Randomised Trees, Quadratic Discriminant Analysis and the K-Nearest Neighbours Classifier.

The performance of each selected algorithm and set of hyper-parameters is quantified by measuring the average \(F_1\) score on 30 held out samples during 30 fold cross validation. The \(F_1\) score is the geometric mean between the precision and the recall, and 30 fold cross validation is akin to making 30 jackknife samples of the data, training on all but the held out sample, and then making predictions on that held out sample, and then repeating. The held out jackknife results, or ‘class weights’, for each training object are retained for future classification calibration.

The winning algorithm and hyper-parameter set is then retrained on the full training sample. The training procedure is deemed to have been completed once at least 50 systems have been explored and when the \(F_1\) score has not been improved upon after 20 iterations. In our empirical experience, we find this to be a generally stable point at which one can stop the exploration of the different algorithms, hyper-parameters, and move on to the final stage of the framework.

This final stage then uses isotonic regression to calibrate the held out class weights of the training data. This enforces the statistical properties of the class weights to more closely resemble a probability. This rescaling is performed by comparing the total number of those objects within a class weight bin, with the fraction of objects to have the true class value. This comparison leads to a rescaling of class weights to class probabilities which we note are conditional on the training data.

The winning ML algorithm, which happened to be AdaBoost in this case, is then used to make class weight predictions on both the test sample and the science samples, and their output class weights are scaled using the previously learned rescaling, to make them more closely resemble probabilities.

We can also perform a feature importance analysis (see, e.g. Hoyle et al. 2015) which suggests that the features with the most predictive power are indeed those derived from MODEST, with other ranking features being WAVG_SPREAD_MODEL_R and MAGERR_MODEL_I.

APPENDIX B: EXTERNAL DATA SETS

B1 Access to external catalogues used in this work

The catalogue used in Section 4 and listed on Table 1 can be obtained from the following website: http://des.ncsa.illinois.edu/releases/y1a1.

B2 Queries used to extract the data sets

Query to the SDSS CASJOBS interface (used as imaging truth table for some tests) to obtain 2MASS, WISE matches with SDSS data, to match with DES data on same area.

\[
\begin{align*}
\text{SELECT} & \quad \text{s.ra, s.dec, s.dered_r,} \\
& \quad \text{w.wlmpro as w1, w.jm_2mass as j, s.z,} \\
& \quad \text{s.class} \\
\text{INTO} & \quad \text{mydb.stripe82.wise_2mass_z_match} \\
& \quad \text{wise_xmatch as xm} \\
& \quad \text{JOIN specPhoto as s on xm.sdss_objid = s.objid} \\
& \quad \text{JOIN wise_allsky as w on xm.wise_cntr = w.cntr} \\
\text{WHERE} & \quad ((\text{s.dered_g} < 23.0) \text{ or } (\text{s.dered_r} < 23.0) \text{ or } (\text{s.dered_i} < 23.0)) \text{ and } \\
& \quad ((\text{s.ra} > 0 \text{ and } \text{s.ra} < 5 \text{ and } \text{s.dec} > -2.5 \text{ and } \text{s.dec} < 3.5) \text{ or } (\text{s.ra} > 315 \text{ and } \text{s.dec} > -3 \text{ and } \text{s.dec} < 3)) \text{ and } \text{s.zWarning} = 0 \text{ and } \\
& \quad \text{s.zErr < 0.001}
\end{align*}
\]

Query to the SDSS CASJOBS interface (used as imaging truth table for some tests) to match with DES and VHS data on same area.

\[
\begin{align*}
\text{SELECT} & \quad \text{s.ra, s.dec, s.dered_r, s.z, s.class} \\
\text{INTO} & \quad \text{mydb.stripe82.z_dr13} \\
\text{FROM} & \quad \text{specPhoto as s} \\
\text{WHERE} & \quad ((\text{s.ra} > 0 \text{ and } \text{s.ra} < 5 \text{ and } \text{s.dec} > -2.5 \text{ and } \text{s.dec} < 3.5) \text{ or } \\
& \quad (\text{s.ra} > 315 \text{ and } \text{s.dec} > -3 \text{ and } \text{s.dec} < 3)) \text{ and } \text{s.zWarning} = 0
\end{align*}
\]

\(^{14}\)https://en.wikipedia.org/wiki/Mutual_information
and s.zErr < 0.001

Query to the Hubble-SC CASJOBS interface (used as imaging truth table for some tests):

```sql
INTO hsc_source_catalogue
FROM SumPropMagAutoCat p
JOIN SumMagAutoCat m ON p.MatchID = m.MatchID
WHERE m.A.F814W > 0 and m.A.F814W_Sigma is not null and p.numimages > 2
```

Query to the VISTA Science Archive, using the VHSDR3 database:

```sql
SELECT ra, dec, jpetromag, jpetromagerr, jmksext, jmksexterr
FROM vhsSource
WHERE jerrbits = 0 and kserrbits = 0 and (priOrSec=0 OR priOrSec=frameSetID) and dec between -2 and 2 and (ra > 315 or ra < 5)
```

Query to Gaia’s DR2, using the CosmoHub (Carretero et al. 2017) interface.

```sql
FROM gaia_dr2
WHERE ((‘ra’ > 305) or (‘ra’ < 90)) and (‘dec’ > -61) and (‘dec’ < -35) and phot_g_mean_mag > 18.5
```

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