

Putative magnetic quantum criticality in  $(\text{Sr}_{1-x}\text{La}_x)_3\text{Ir}_2\text{O}_7$ J. G. Vale<sup>1,\*</sup> and E. C. Hunter<sup>2,3</sup><sup>1</sup>*London Centre for Nanotechnology and Department of Physics and Astronomy, University College London, Gower Street, London WC1E 6BT, United Kingdom*<sup>2</sup>*School of Physics and Astronomy, The University of Edinburgh, James Clerk Maxwell Building, Mayfield Road, Edinburgh EH9 2TT, United Kingdom*<sup>3</sup>*Inorganic Chemistry Laboratory, South Parks Road, Oxford OX1 3QR, United Kingdom*

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$(\text{Sr}_{1-x}\text{La}_x)_3\text{Ir}_2\text{O}_7$  undergoes a bulk insulator-to-metal transition at  $x \approx 0.04$ . Through careful analysis of previously published data ( $x = 0.053, 0.061, 0.076$ ), we find an extended region below the Debye temperature in which the resistivity appears to scale linearly with temperature. Meanwhile, resonant (in)elastic x-ray scattering data ( $x = 0.065$ ) suggest a possible crossover from quantum paramagnetic to quantum critical phenomenology between 100 and 200 K. We put this into context with other results, and propose a possible phase diagram as a function of doping.

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The properties of a system proximate to a quantum critical point (QCP) at  $g = g_c$  generally fit the following scenario. At low temperatures, and for  $g < g_c$ , the ground state may exhibit some form of long-range order (LRO) above its lower critical dimension. In antiferromagnets, for instance, this corresponds to Néel order. This order is destroyed by classical thermal fluctuations, which dictate the scaling of thermodynamic properties in the vicinity of some critical temperature  $T_c$ . Above the transition, quasiparticles may still be well defined on intermediate length scales, even though LRO has disappeared. This corresponds to a so-called thermal disordered regime. At sufficiently high temperatures ( $T \sim |g - g_c|^{\nu z}$ ), these quasiparticles are replaced by a critical continuum of excitations. This continuum is thermally excited, which leads to a characteristic  $\omega/T$  scaling of the spin fluctuations in the vicinity of the critical wave vector, and unconventional power-law temperature dependences of physical observables. If instead  $g > g_c$ , then the ground state is disordered and characterized by well-defined quasiparticle excitations. The properties of the system are dictated primarily by the magnitude of a singlet-triplet gap  $\Delta \sim (g - g_c)^{\nu z}$ , which exists at all wave vectors. We refer to this as a quantum paramagnetic state, although it is also known as quantum disordered behavior in the literature. A crossover to quantum critical behavior typically occurs around  $T \sim \Delta$  [Fig. 2(d)]. Detailed reviews of quantum phase transitions (QPTs) are given in Refs. [1,2], among others.

A number of the cuprates have been proposed—albeit with some controversy—to undergo QPTs as a function of doping. These include the (hole-doped) high-temperature superconductor  $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$  (LSCO), in which a magnetic QCP may lie underneath the superconducting dome [3–5]. Some similarities can be drawn between LSCO and the electron-doped perovskite iridate  $(\text{Sr}_{1-x}\text{La}_x)_2\text{IrO}_4$ . This material, as

LSCO, is an insulator and easy-plane antiferromagnet below the Néel temperature at low carrier doping. It undergoes an insulator-to-metal transition (IMT) at  $x \approx 0.04$  [6,7], with evidence of a pseudogap and holelike Fermi surface in the metallic phase  $x \geq 0.05$  [8,9], along with possible spin density wave (SDW) order [10]. In contrast with LSCO, however, nanoscale electronic phase separation can be observed well into the metallic regime [7]. Moreover, experimental evidence of a QPT in this system is still outstanding.

Meanwhile, the bilayer compound  $(\text{Sr}_{1-x}\text{La}_x)_3\text{Ir}_2\text{O}_7$  has no direct analogs with any of the cuprates. Resistivity measurements have shown that  $(\text{Sr}_{1-x}\text{La}_x)_3\text{Ir}_2\text{O}_7$  undergoes an IMT at  $x = 0.04$  [11–13], similar to the single-layer material. Neutron scattering and second harmonic generation (SHG) measurements determined that the IMT is first order, with a structural phase transition occurring in the metallic phase at  $T_s \approx 200$  K [12,14]. Yet, no pseudogap could be observed by angle-resolved photoelectron spectroscopy (ARPES), with small electronlike Fermi pockets present in the metallic phase [15–17]. Furthermore, electronic phase separation does occur in the vicinity of the IMT, but disappears for  $x > 0.04$  [12]. Magnetization and neutron scattering measurements show that Néel LRO disappears above the IMT [12]. Resonant elastic x-ray scattering (REXS) data demonstrate, however, that short-ranged in-plane magnetic order persists up to 300 K [18], at least for  $x = 0.065$  [19]. The lack of dependence upon  $L$  implies the loss of interlayer correlations deep in the metallic phase. Resonant inelastic x-ray scattering (RIXS) measurements on the undoped compound reveal strongly gapped spin wave excitations, with an additional longitudinal mode interpreted as evidence of a possible quantum dimer character and a proximate QPT [20,21]. Upon electron doping, the spin excitations become progressively more damped [18,22]. While there are discrepancies between the two studies [23], Lu *et al.* find that the spin gap collapses dramatically for  $x = 0.065$ , proposing that the two-dimensional (2D) behavior also extends to the dynamics.

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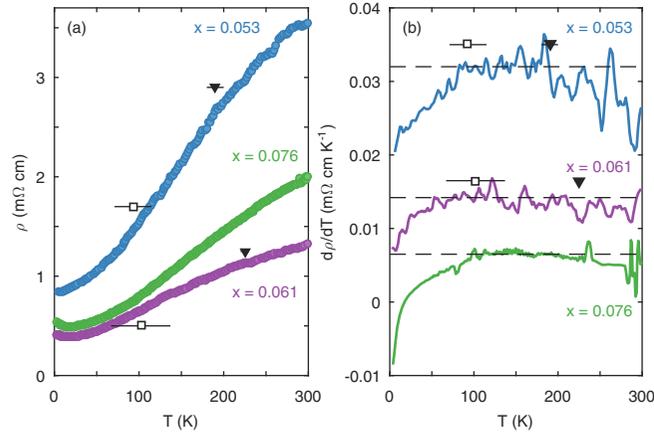


FIG. 1. (a) Summary of resistivity data from Refs. [12] ( $x = 0.053, 0.061$ ) and [13] ( $x = 0.076$ ). Solid triangles indicate the structural phase transition at  $T_s$  [14]. Open squares: Quasiparticle spectral weight at  $T_{\text{coh}}$  determined from ARPES [17]. (b) Derivative  $d\rho/dT$  of the same data; smoothed with an unweighted five-point moving average and offset by a constant scale factor for clarity. Dotted line: Guide to the eye highlighting the region where  $d\rho/dT$  is approximately constant. All other annotations are the same as displayed in (a).

We examine some of the previously published experimental data for  $(\text{Sr}_{1-x}\text{La}_x)_3\text{Ir}_2\text{O}_7$  in more detail. What we find are three distinct electronic regimes for  $x > 0.05$ , which can be discriminated through clear gradient changes in the resistivity as a function of temperature. These correlate well with phase boundaries determined by other techniques. Meanwhile, REXS data suggest a possible crossover between quantum paramagnetic and quantum critical behavior between 100 and 200 K. This is corroborated by apparent  $\omega/T^\alpha$  scaling observed in RIXS data. Each of these shall be discussed in turn, starting with the temperature dependence of the resistivity.

In Fig. 1(a), the resistivity of three different samples with  $x = 0.053(10)$ ,  $0.061(10)$ , and  $0.076(11)$ , has been plotted as a function of temperature. There are three immediately apparent observations from the data. The first is that all three samples are clearly metallic up to 300 K. The low-temperature upturn present for the  $x = 0.061$  and  $x = 0.076$  samples can be attributed to Anderson localization, likely due to sample inhomogeneity. Moreover, the  $x = 0.061$  sample has a consistently lower resistivity than the other two samples. It has been noted, however, that a sample-to-sample variation within a batch can lead to differences in the absolute magnitude of the resistivity by a factor of 2 [13]. The corresponding residual resistivity ratio (RRR) is about 4 for all three samples, which is a direct consequence of the flux growth method used to generate single crystals of this material. In this sense,  $(\text{Sr}_{1-x}\text{La}_x)_3\text{Ir}_2\text{O}_7$  is a somewhat dirty system.

A less obvious observation is that a kink is evident at ca. 200 K, which we note is a similar temperature to the structural phase transition observed via neutron scattering in Ref. [12]. This is more clearly displayed in Fig. 1(b), in which we plot the temperature derivative of the resistivity  $d\rho/dT$ . A further change in slope occurs around 100 K, which coincides remarkably well with the loss of coherent quasiparticle

spectral weight at  $T_{\text{coh}}$  observed via ARPES [17]. Between these two temperatures,  $d\rho/dT$  is approximately constant, implying  $\rho \propto T$ . Such behavior is expected for good metals well above the Debye temperature  $\Theta_D$  due to electron-phonon scattering. Yet, specific heat measurements reveal that the Debye temperature  $\Theta_D \approx 380$  K, and is essentially independent of doping. We also note that the absolute value of the resistivity at 200 K is comparable to the Mott-Ioffe-Regel (MIR) limit, within which the mean free path  $l$  is on the order of the lattice constant  $a$  [16,24]. This implies that the system is close to the so-called bad metal regime. Hence we can rule out phonons as the leading cause for  $T$ -linear resistivity in  $(\text{Sr}_{1-x}\text{La}_x)_3\text{Ir}_2\text{O}_7$  and our observations are likely indicative of alternative phenomenology. One possibility is that the linear scaling of the resistivity above  $T_{\text{coh}}$  may be representative of underlying quantum critical behavior. In the cuprates, for instance, the  $\rho \propto T$  scaling present in the “strange metal” phase has been suggested to manifest due to scattering from some fluctuating order parameter.

If  $(\text{Sr}_{1-x}\text{La}_x)_3\text{Ir}_2\text{O}_7$  does indeed undergo a QPT, then signatures of this should also be seen in the magnetic behavior. As mentioned previously, REXS measurements by Lu *et al.* [18] reveal short-ranged magnetic order which persists above the IMT for  $x > 0.04$ . The magnetic  $(0.5, 0.5, 2\pi)$  Bragg peak appears to weaken and broaden with increasing temperature, however, significant in-plane correlations are still observable at 300 K. Hogan *et al.* also found with RIXS that the magnon peak was invariant with  $L$  for their  $x = 0.07$  sample (within experimental uncertainty) [22]. Noting that two-dimensional layered materials frequently exhibit such behavior, we proceeded to examine the data in more detail [Fig. 2(a)].

We fitted the data at each temperature to a Voigt function, with the Gaussian component fixed to the width of a typical structural Bragg reflection, in order to approximate the instrumental resolution function. Varying this width within sensible bounds does not change our results significantly. Additionally, the background was fixed at all temperatures to that obtained from fitting at 20 K. What can be seen is that the correlation length  $\xi$  and equal-time structure factor  $S_0$  are approximately constant up to 100 K [Figs. 2(b) and 2(c)], with these parameters decreasing at higher temperatures. There thus appear to be two distinct temperature regimes within the data.

Our findings shall initially be discussed in terms of the  $O(N)$  quantum nonlinear sigma model (QNL $\sigma$ M), probably the simplest model to undergo a continuous quantum phase transition (QPT) in  $2 + 1$  dimensions. Specifically, we use key results given within Ref. [25], which have been obtained through exact solution in the  $N = \infty$  limit. Corrections to order  $1/N$  are nontrivial to calculate for  $g > g_c$ , which is why they have been neglected in this initial study. We note at this point that further-neighbor interactions (and anisotropies) are important for  $(\text{Sr}_{1-x}\text{La}_x)_3\text{Ir}_2\text{O}_7$ , which clearly manifest in the observed spin wave dispersion [18,20–22]. Therefore, unless otherwise stated, the following discussion applies to an effective exchange interaction  $\tilde{J}$  which includes the effects of the other terms in the Hamiltonian.

The QNL $\sigma$ M exhibits LRO at  $T = 0$ , provided that the coupling  $g = \hbar c \sqrt{2\pi} / (k_B \rho_s a) < g_c$ , where  $c = 2\sqrt{2} Z_c S \tilde{J} a$  is the spin wave velocity,  $a$  is the lattice constant,  $\rho_s$  is the spin

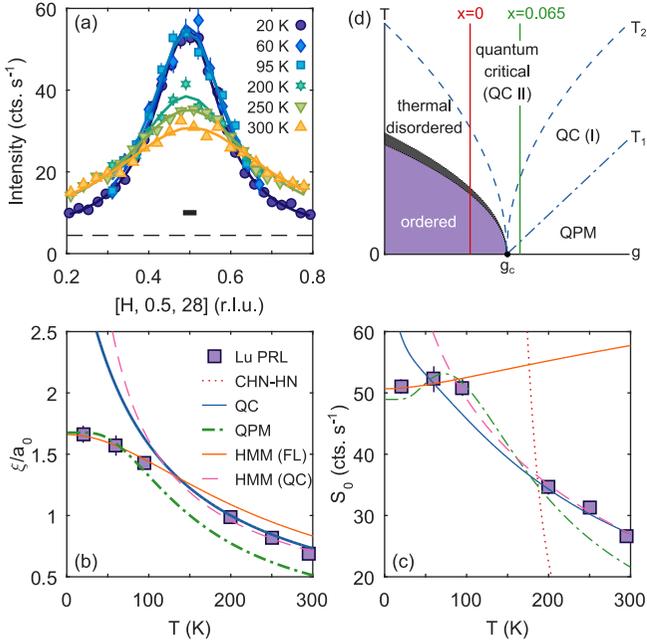


FIG. 2. Analysis of resonant x-ray magnetic scattering (REXS) data collected by Lu *et al.* for  $x = 0.065$  [18]. (a) Intensity of (0.5, 0.5, 28) magnetic Bragg peak as a function of temperature. The solid line is the best fit to the data, and the dashed line indicates linear background. The solid bar is the full width at half maximum (FWHM) of the nearby structural Bragg peak. (b) Comparison of in-plane correlation length  $\xi$  divided by Ir-Ir nearest-neighbor distance  $a_0 = 3.9 \text{ \AA}$  with various theoretical models. (c) Peak amplitude  $S_0$ . (d) Possible magnetic phase diagram for  $(\text{Sr}_{1-x}\text{La}_x)_3\text{Ir}_2\text{O}_7$  as a function of doping and temperature. CHN-HN: Renormalized classical model [26]. QC: Quantum critical [25]. QPM: Quantum paramagnet (quantum disordered) [25]. Orange solid (pink dashed): Hertz-Millis-Moriya model in the Fermi liquid (quantum critical) regime [2]. The CHN-HN, QC, and QPM models plotted in (b) and (c) use  $\tilde{J} = 62 \text{ meV}$ , with  $\Delta = 14 \text{ meV}$  also used for the QC and QPM models.

stiffness, and  $Z_c = 1 + \eta$  is a renormalization factor which describes the effect of quantum fluctuations. From now on we take  $Z_c = 1$ , in order to better compare with the experimental results. Real materials typically order at nonzero temperatures as a consequence of weak anisotropies or further-neighbor interactions. Given the intrinsically broad magnetic Bragg peak at 30 K, and that bulk susceptibility data show paramagnetic behavior at all temperatures, then this implies that the material lies on the  $g > g_c$  side of the putative QPT for  $x = 0.065$ .

In this regime, both  $\xi$  and  $S_0$  are expected to scale with  $x_2 = k_B T / \Delta$ , where  $\Delta$  is the singlet-triplet gap,

$$\xi^{-1} = \frac{k_B T}{\hbar c} X_2(x_2),$$

$$S(k \rightarrow 0) \propto \frac{(\hbar c)^2 x_2 \coth(X_2/2)}{k_B T 2X_2(x_2)}. \quad (1)$$

The parameter  $X_2$  in the preceding expressions is a scaling function, which has the following asymptotic limits in the quantum paramagnetic ( $x_2 \ll 1$ ) and quantum critical

( $x_2 \gg 1$ ) regions,

$$X_2(x_2) = x_2^{-1} + 2e^{-1/x_2}, \quad x_2 \ll 1,$$

$$= 2 \ln \left( \frac{\sqrt{5} + 1}{2} \right) + \frac{1}{\sqrt{5}x_2}, \quad x_2 \gg 1. \quad (2)$$

Hence this implies a correlation length which is on the order of  $\Delta^{-1}$  (for  $x_2 \ll 1$ ) or  $T^{-1}$  (for  $x_2 \gg 1$ ).

This theoretical model is compared with the experimental data in Figs. 2(b) and 2(c). We find that the quantum paramagnetic model describes the experimental data below 100 K quite well. At higher temperatures, however, it appears to underestimate the correlation length and structure factor. Meanwhile, the quantum critical model agrees with the data above 200 K, but diverges at lower temperatures. This suggests that there may be a crossover between the two regimes in the temperature range 100–200 K. Unfortunately, there are currently no experimental data available which correspond to this region.

The agreement between the experimental data and theory is also quantitative. Note that the value of  $\Delta$  we obtain ( $\Delta = 14 \text{ meV}$ ) is comparable with the magnon gap observed in RIXS for  $x = 0.065$  [18]. Furthermore,  $\tilde{J} = 62 \text{ meV}$  is in excellent agreement with the effective nearest-neighbor coupling derived from the RIXS data,  $\tilde{J} = \sum_i J_i z_i = 64 \text{ meV}$ , where  $J_i$  are the individual coupling parameters (including anisotropies), and  $z_i$  the number of neighbors. While there are some question marks regarding the quantitative mapping of the QNL $\sigma$ M to  $S = 1/2$  Heisenberg spin systems (for example, see the discussion in Ref. [27]), the correlation is, nevertheless, remarkable.

We also plot the expected temperature dependence of the correlation length and structure factor within the Hertz-Millis-Moriya model (HMM) for three-dimensional (3D) nearly antiferromagnetic metals ( $d = 3, z = 2$ ). In the HMM picture, spin fluctuations become soft at the QCP, and are damped by a background of itinerant electrons. This is somewhat related to the paramagnon (SCR) theory by Moriya [28]. At low temperature ( $T < T^*$ ), the inverse correlation length  $\xi^{-1}$  exhibits the  $T^2$  dependence characteristic of a Fermi liquid. Above  $T^*$ , the system exhibits quantum criticality. It has been determined that  $\xi^{-2} = |g - g_c| + AT^{2/3}$ , with the first term dominating in region I, and the second in region II [Fig. 2(d)]. Meanwhile, the equal-time structure factor  $S_0$  is given by

$$S_0(k \rightarrow 0) = \frac{1}{\pi} \int_{-\infty}^{\infty} [n(\omega) + 1] \text{Im} \left[ \frac{A\xi^2}{1 - i\omega/\omega_{\text{SF}}} \right] \hbar\omega, \quad (3)$$

where  $n(\omega) = (e^{\hbar\omega/k_B T} - 1)^{-1}$ , and  $\omega_{\text{SF}}$  is the characteristic energy for spin fluctuations. We assume that  $\omega_{\text{SF}} = 20 \text{ meV}$ , which corresponds to the experimental spin wave energy at 30 K, and is fixed as a function of temperature. Again, we observe that the data below 100 K are well described by the low-temperature predictions of the HMM model, with the higher-temperature data more representative of quantum critical phenomenology (mostly region II).

There is further evidence that the magnetic fluctuations at high temperature may be indicative of quantum critical behavior. In the vicinity of a QCP, spin fluctuations at the antiferromagnetic (AFM) wave vector  $\mathbf{Q}_{\text{AF}}$  are expected to

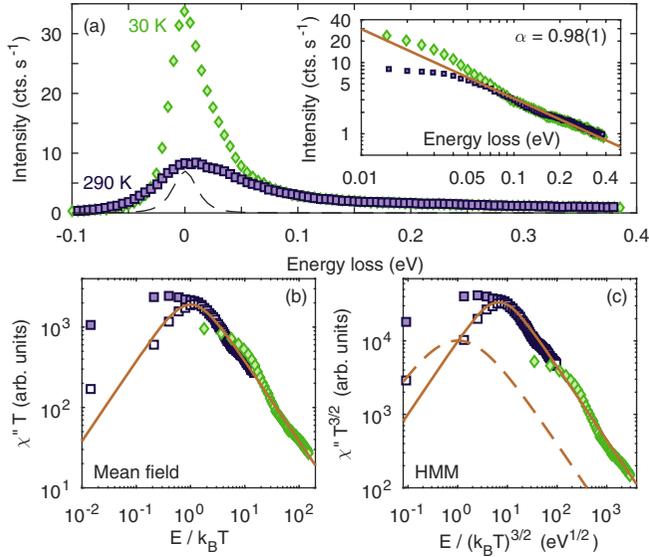


FIG. 3. Temperature dependence of RIXS spectra at (0.5, 0.5, 26.5) for  $x = 0.065$ . (a) Comparison of data at 30 K (green diamonds) and 290 K (purple squares). Dashed line: Elastic line at 290 K. Reproduced from Fig. S3(a) of Ref. [18]. The inset shows the same data plotted on double logarithmic axes, along with the best fit to the power law with exponent  $\alpha = 0.98(1)$ . (b), (c) Scaling plots of the imaginary part of the dynamic susceptibility  $\chi''(E, T)$ , plotted as  $\chi'' T^\alpha = f(E/T^\beta)$ , with (b)  $\alpha = \beta = 1$  or (c)  $\alpha = \beta = 3/2$ . Note  $\chi''$  has been obtained from the data presented in (a) using the relation  $\chi''(E, T) = I[1 - \exp(-E/k_B T)]$ . The scaling functions  $f(E/T^\beta)$  are defined in the main text. Open symbols reflect 290 K data with the elastic line subtracted off. Solid lines are fits to the data. The dashed line in (c) uses  $b = 1$ .

exhibit  $\omega/T^\alpha$  scaling, where  $\alpha$  is an independent scaling exponent. Different models for the criticality predict different results. For instance, in the HMM model, spin fluctuations are dominated by the AFM order parameter. Consequently, for a 3D nearly AFM metal, it predicts  $E/T^{3/2}$  scaling of the dynamic spin susceptibility,  $\chi^{-1}(\mathbf{Q}_{\text{AF}}, E, T) = a^{-1}(T^{3/2} - ibE)$ . The parameter  $b$  is related to the characteristic energy of spin fluctuations  $\omega_{\text{SF}}$  defined earlier. Meanwhile, anomalous exponents have been observed in some heavy fermion systems, which are believed to correspond to “local criticality.” Schröder [29] and Poudel [30] have proposed a modified Curie-Weiss law to describe the inverse dynamic susceptibility in such systems,  $\chi^{-1}(\mathbf{q}, E, T) = c^{-1}[\theta^\alpha + (T - iE)^\alpha]$ , where  $\theta(\mathbf{Q} - \mathbf{Q}_{\text{AF}})$  captures the wave-vector dependence of the magnetic fluctuations similar to the Curie-Weiss temperature. Note that in the latter picture, the fluctuations become critical in the time domain everywhere in  $\mathbf{q}$ , rather than just at  $\mathbf{Q}_{\text{AF}}$ .

In Fig. 3(a), we plot resonant inelastic x-ray scattering (RIXS) data at  $(\pi, \pi)$  for  $x = 0.065$ , which were previously published in Ref. [18]. The spin excitations appear highly damped, and extend to a 0.4 eV energy loss at both 30 and 295 K. Moreover, when we plot the data on double logarithmic axes [inset of Fig. 3(a)], they appear to scale approximately linearly for  $E > 0.05$  eV. This implies that the dynamic critical exponent  $z = 2/\alpha \sim 2$ . Such a value is expected both

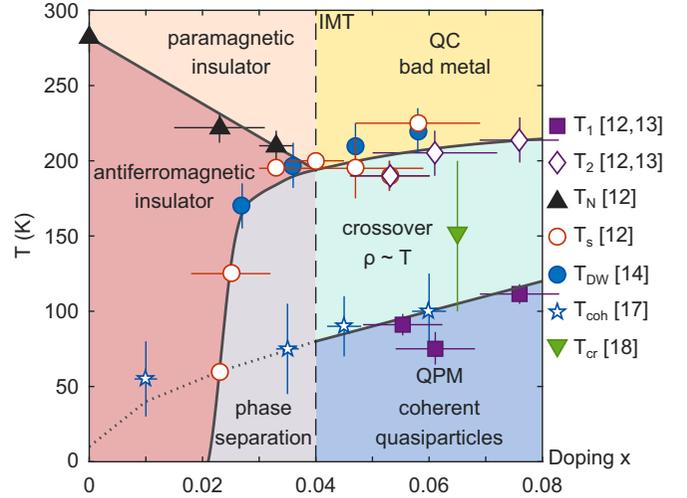


FIG. 4. Possible unified phase diagram for  $(\text{Sr}_{1-x}\text{La}_x)_3\text{Ir}_2\text{O}_7$  summarizing transition temperatures observed with various techniques. Black triangles (red open circles): Néel temperature  $T_N$  (structural transition temperature  $T_s$ ) from neutron powder diffraction [12]. Blue solid circles: Onset of putative CDW  $T_{\text{DW}}$  from pump-probe optical reflectivity [14]. Green solid triangles: Crossover temperature from REXS [18]. Blue stars: Loss of coherent spectral weight in ARPES [17]. Solid squares (open diamonds): Onset (end) of constant  $d\rho/dT$  at  $T_1$  ( $T_2$ ) [12,13].

for three-dimensional nearly AFM metals [2], and quantum dimer models on a square lattice [31]. One complication is that the ideal QNL $\sigma$ M assumes Lorentz invariance, and hence  $z = 1$ . However, the presence of disorder (caused by doping) can break this invariance and give rise to  $z \neq 1$  [25].

Scaling plots in Figs. 3(b) and 3(c) compare the experimental data to the theoretical predictions for the mean-field ( $\alpha = 1$ ) and HMM ( $\alpha = 3/2$ ) models, respectively. Broadly speaking, both models provide an adequate description of the data. Some discrepancies at low  $E/T$  can be overcome by subtracting off the resolution-limited elastic line and low-energy phonon contributions, the latter being observed in the undoped compound at 25 meV (compare the solid and open symbols). We find that the best fit for the HMM model is obtained with  $b = 0.14$ , significantly smaller from the expected value of unity. Note that the simple model given here is defined precisely at the QCP and AFM wave vector, and assumes zero anisotropy. Yet, the REXS data presented earlier suggest that the putative magnetic QCP lies at  $x < 0.065$ . Furthermore, the finite momentum resolution of the RIXS spectrometer means that we sample a number of momentum transfers close to  $(\pi, \pi)$ . Finally, the 20-meV spin gap present at 30 K may persist to some degree at high temperatures. Such a deviation, is therefore, not entirely unexpected.

We conclude by putting the analysis presented here in context with other experimental results. Specifically, we extend the temperature-doping phase diagram to include recent ARPES data, and our resistivity and REXS results (Fig. 4). A striking correlation is apparent between the onset of constant  $d\rho/dT$  at  $T_1$ , and the loss of coherent spectral weight at  $T_{\text{coh}}$  observed in ARPES [17]. A further change in slope of the resistivity at  $T_2$  also appears to coincide with the structural

phase transition observed by neutron scattering [12], and the loss of putative charge density wave (CDW) ordering from pump-probe optical reflectivity data [14]. Whether the  $\rho \propto T$  behavior persists above  $T_c$  is still uncertain within the limits of the data presented here. We note the apparent similarity in the transport behavior as observed for overdoped cuprates [32]. In the cuprates, however, the quasiparticle peak (from ARPES) persists into the  $\rho \propto T$  regime.

The REXS results also show a possible crossover between quantum paramagnetic and quantum critical phenomenology somewhere between 100 and 200 K. This is consistent with our value of  $T^*$ , which implies that the Hertz-Millis-Moriya picture [Fig. 2(d)] may be relevant for  $(\text{Sr}_{1-x}\text{La}_x)_3\text{Ir}_2\text{O}_7$ . Yet, the (limited) RIXS data is less clear cut. There appears to be  $E/T^\alpha$  scaling of the dynamic spin susceptibility, as would be expected in the vicinity of a QCP. At present, it is not possible to conclusively distinguish between the HMM or simple mean-field pictures. Even so, it demonstrates that quantum criticality seems to extend to the spin dynamics.

Clearly, there is a significant difference in the electronic and magnetic behavior of  $(\text{Sr}_{1-x}\text{La}_x)_3\text{Ir}_2\text{O}_7$  compared to its single-layer counterpart  $(\text{Sr}_{1-x}\text{La}_x)_2\text{IrO}_4$ . What the data presented here show is that structural, electronic, and magnetic degrees of freedom are directly coupled in  $(\text{Sr}_{1-x}\text{La}_x)_3\text{Ir}_2\text{O}_7$ , giving rise to a rich phase diagram, and potentially containing a hidden magnetic QCP.

A number of outstanding questions remain. The first is the nature of the apparent crossover between the quantum paramagnetic and quantum critical regimes. This can only be definitively answered through collection of more data—both in the elastic and inelastic channels—between 100 and 200 K at various doping levels. This in turn leads to whether the  $E/T^\alpha$  scaling is universal as a function of temperature and wave vector. If so, then this would imply a departure from the HMM picture, which is only expected to be relevant in the vicinity of  $Q_{\text{AF}}$ . At present it remains unclear whether there is a single zero temperature QCP, or a line of first-order IMTs which end at a finite-temperature critical end point [33,34]. Magnetic susceptibility measurements as a function of pressure may help to discriminate between these two scenarios. It is also curious that the nominally three-dimensional  $(\text{Sr}_{1-x}\text{La}_x)_3\text{Ir}_2\text{O}_7$  appears to map onto the 2+1-dimensional QNL $\sigma$ M, yet the single-layer  $(\text{Sr}_{1-x}\text{La}_x)_2\text{IrO}_4$  does not (for low doping at any rate). This may be related to the electronic phase separation prevalent in the single-layer compound above the IMT. Nevertheless, it may be worth revisiting  $(\text{Sr}_{1-x}\text{La}_x)_2\text{IrO}_4$  to look for evidence of quantum criticality in the metallic phase.

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